

Precision Higgs Physics

CRC Annual Meeting 2021

Robert Harlander, 28 May 2021

A MODEL OF LEPTONS*

Steven Weinberg†

Laboratory for Nuclear Science and Physics Department,
Massachusetts Institute of Technology, Cambridge, Massachusetts

(Received 17 October 1967)

Nobel 1979

Therefore, we shall construct our Lagrangian out of L and R , plus gauge fields $\vec{A}_\mu$ and B_μ coupled to $\vec{T}$ and Y , plus a spin-zero doublet

$$\varphi = \begin{pmatrix} \varphi^0 \\ \varphi^- \end{pmatrix} \quad (3)$$

whose vacuum expectation value will break $\vec{T}$ and Y and give the electron its mass. The on-

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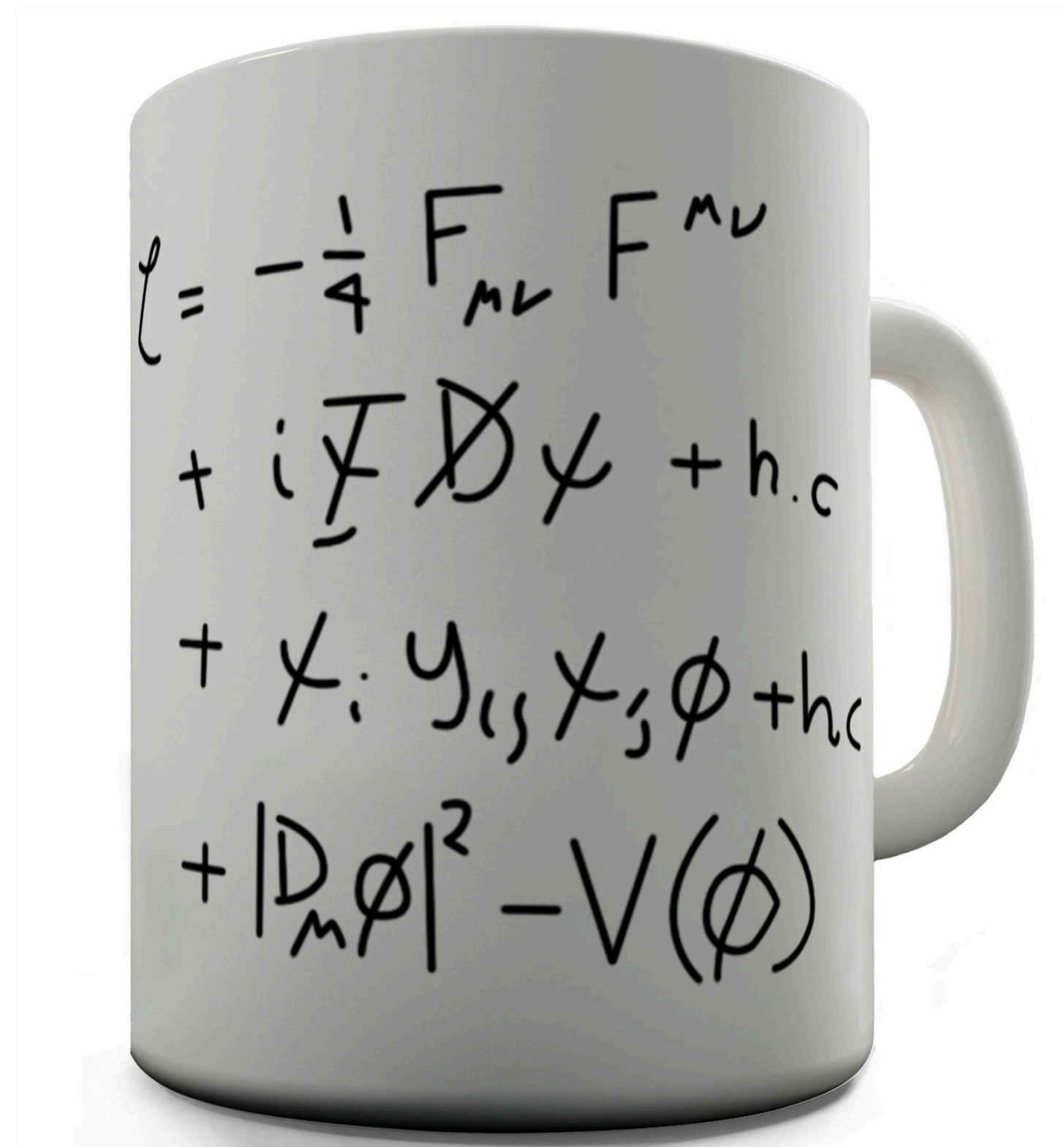
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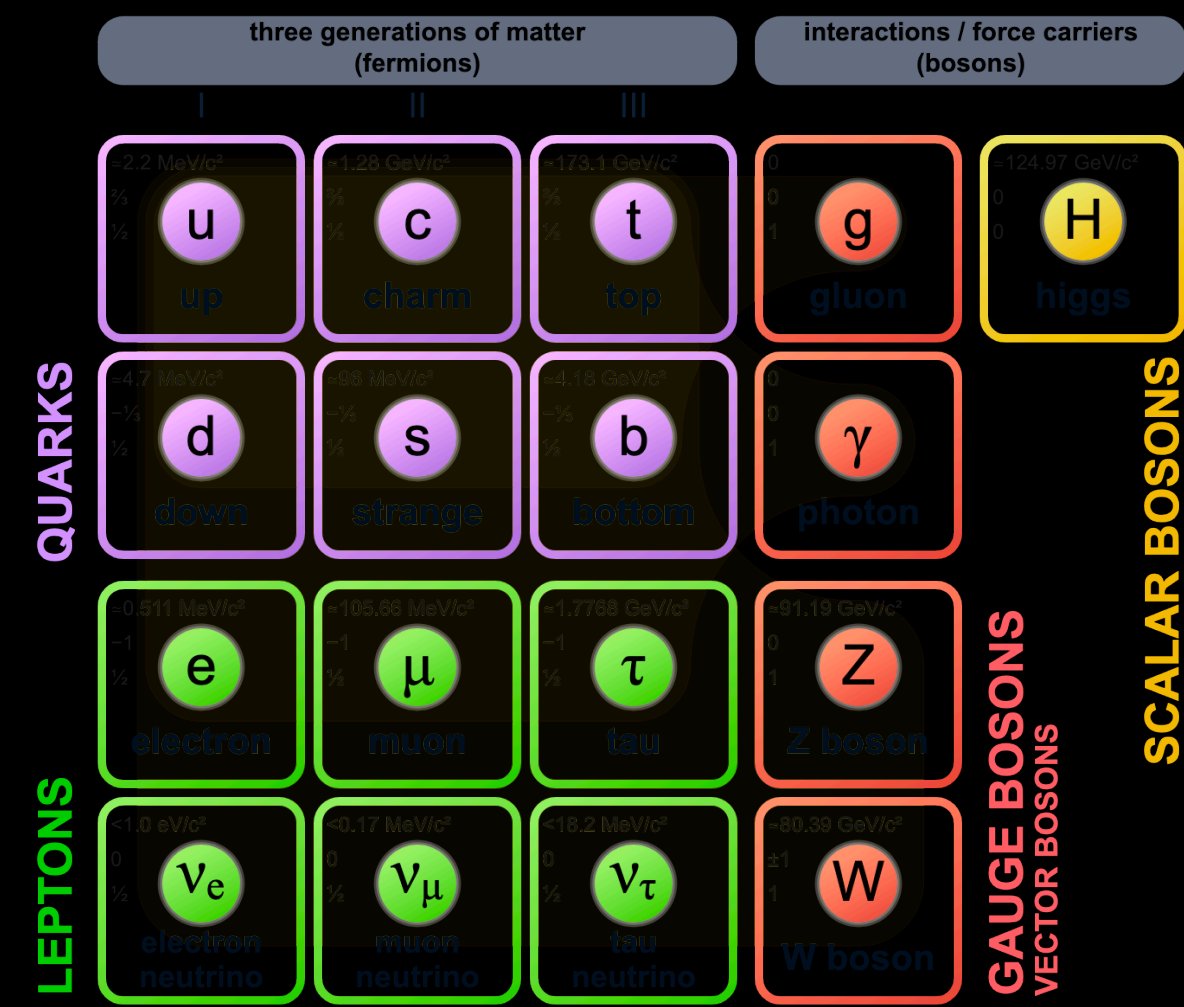
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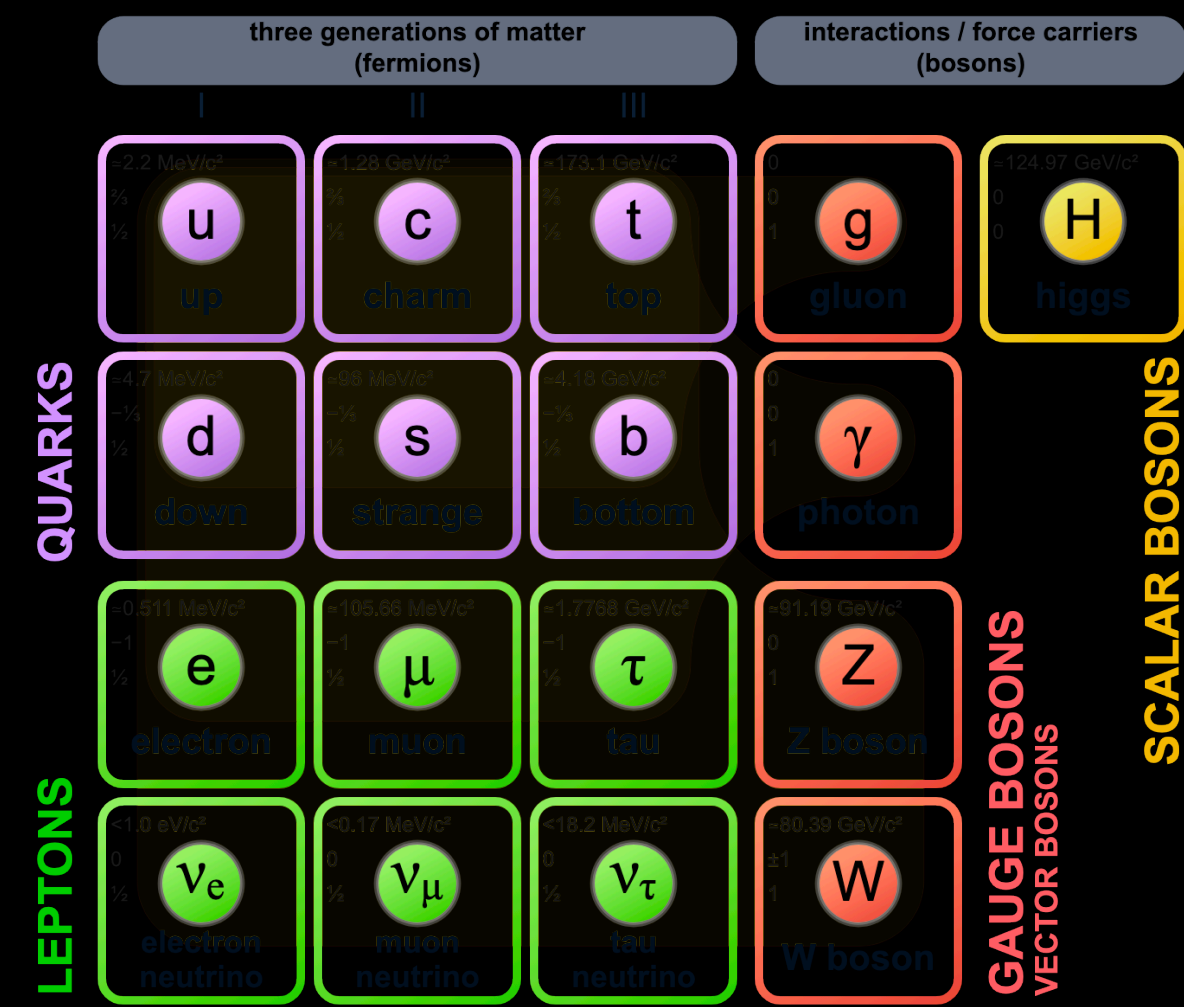
whose vacuum expectation value will break $\vec{T}$ and Y and give the electron its mass. The on-

interaction is multiplied by a factor $-\frac{1}{2}$ rather than $\frac{3}{2}$. Of course our model has too many arbitrary features for these predictions to be taken very seriously, but it is worth keeping in mind that the standard calculation⁸ of the

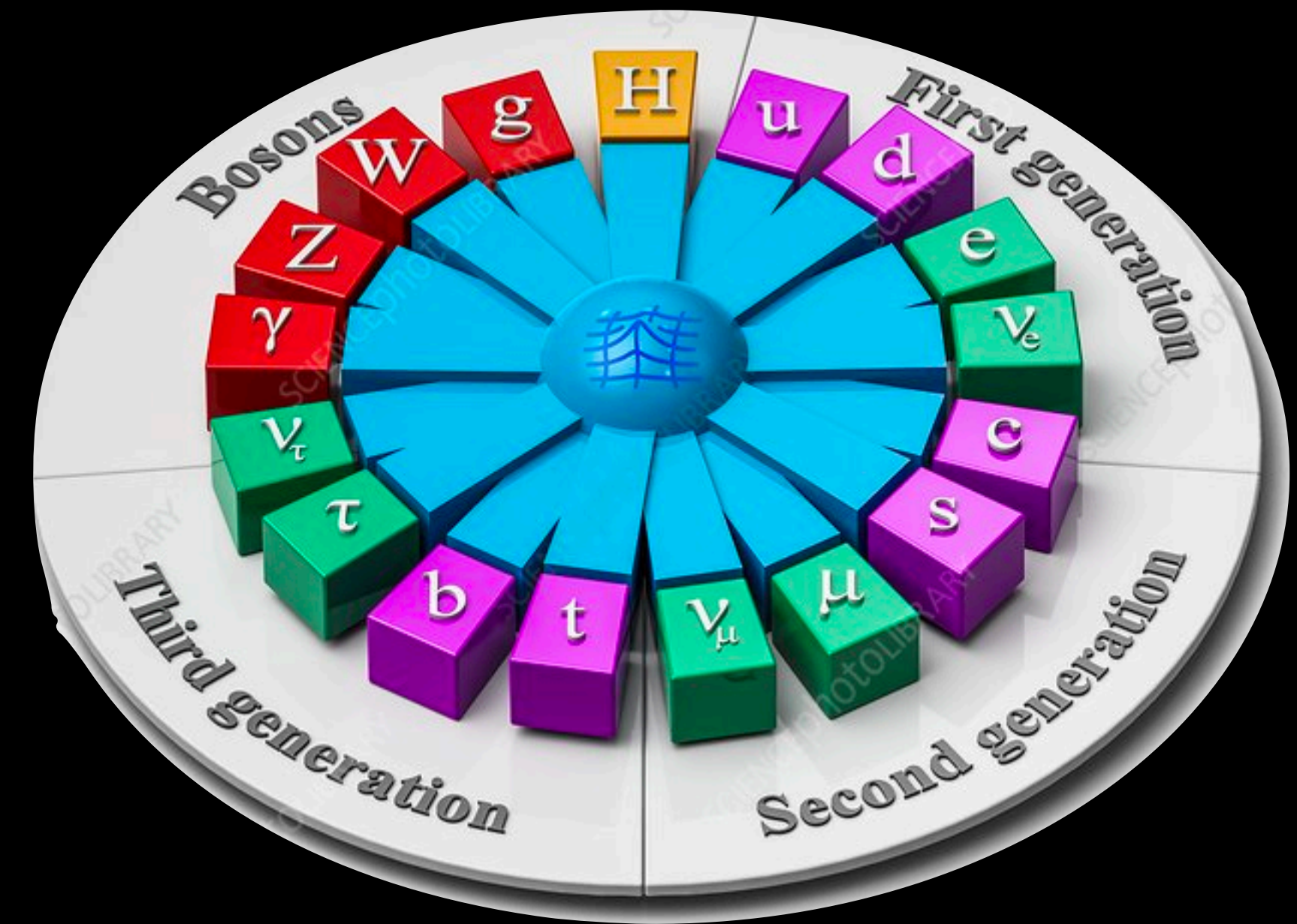




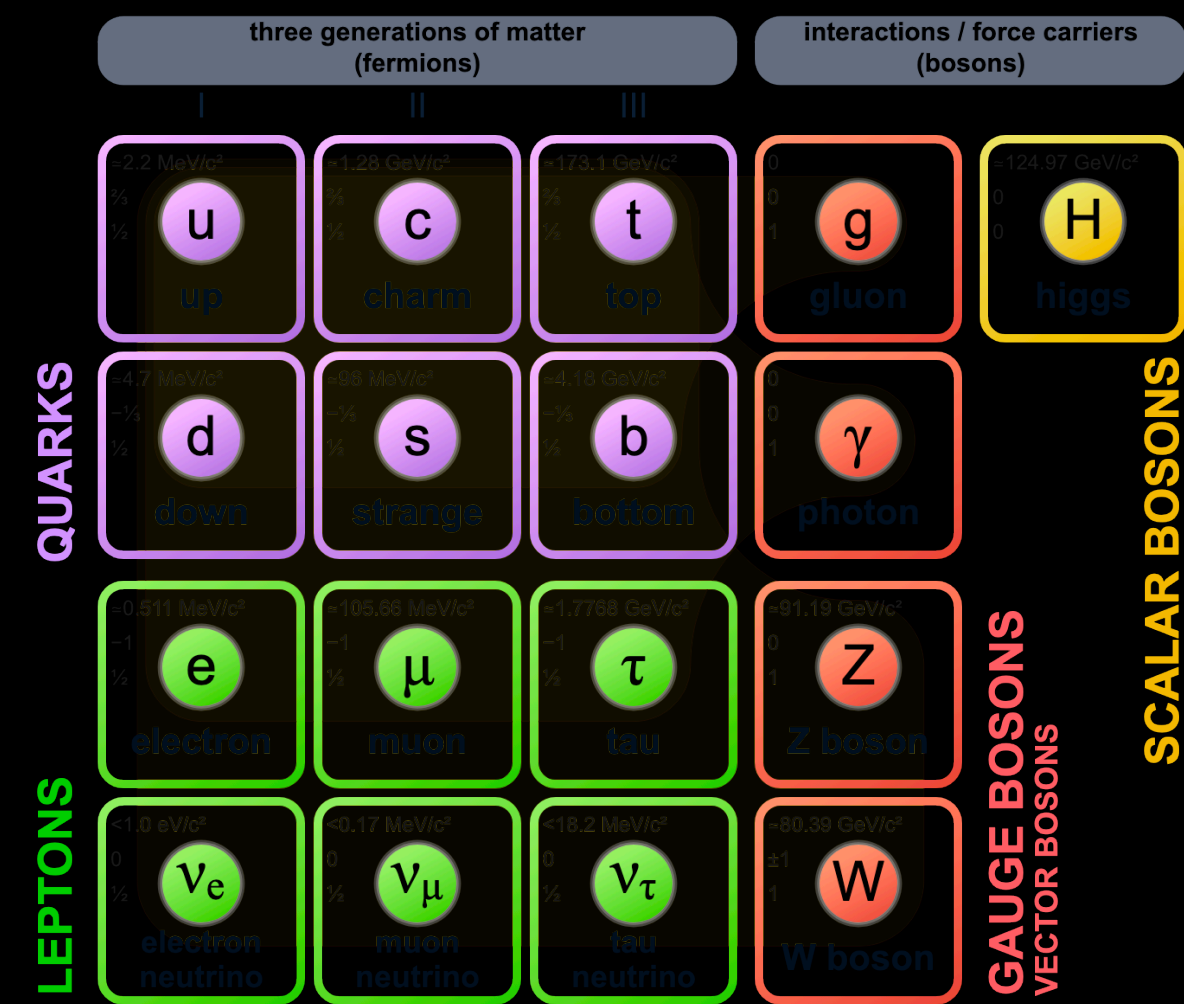
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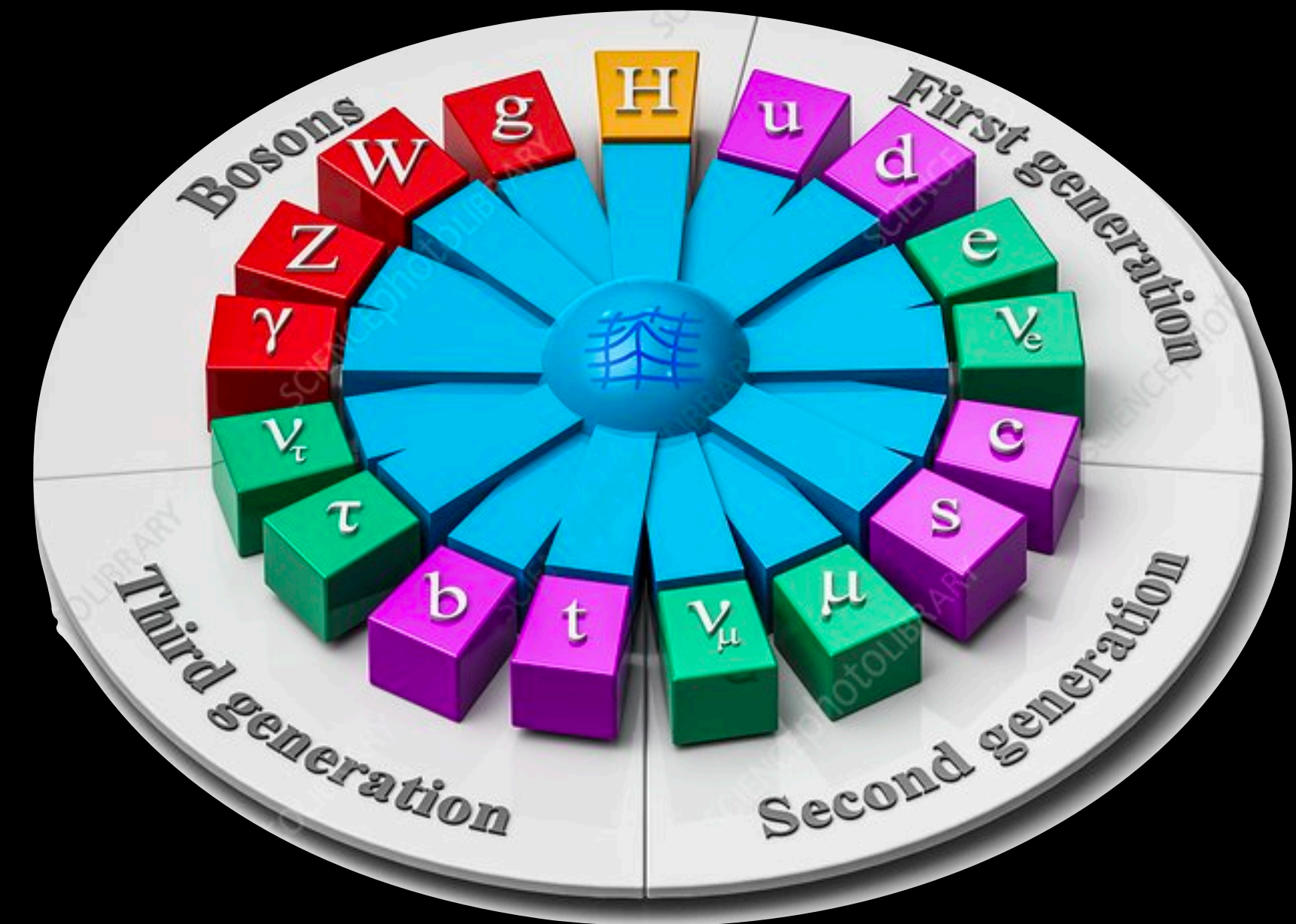
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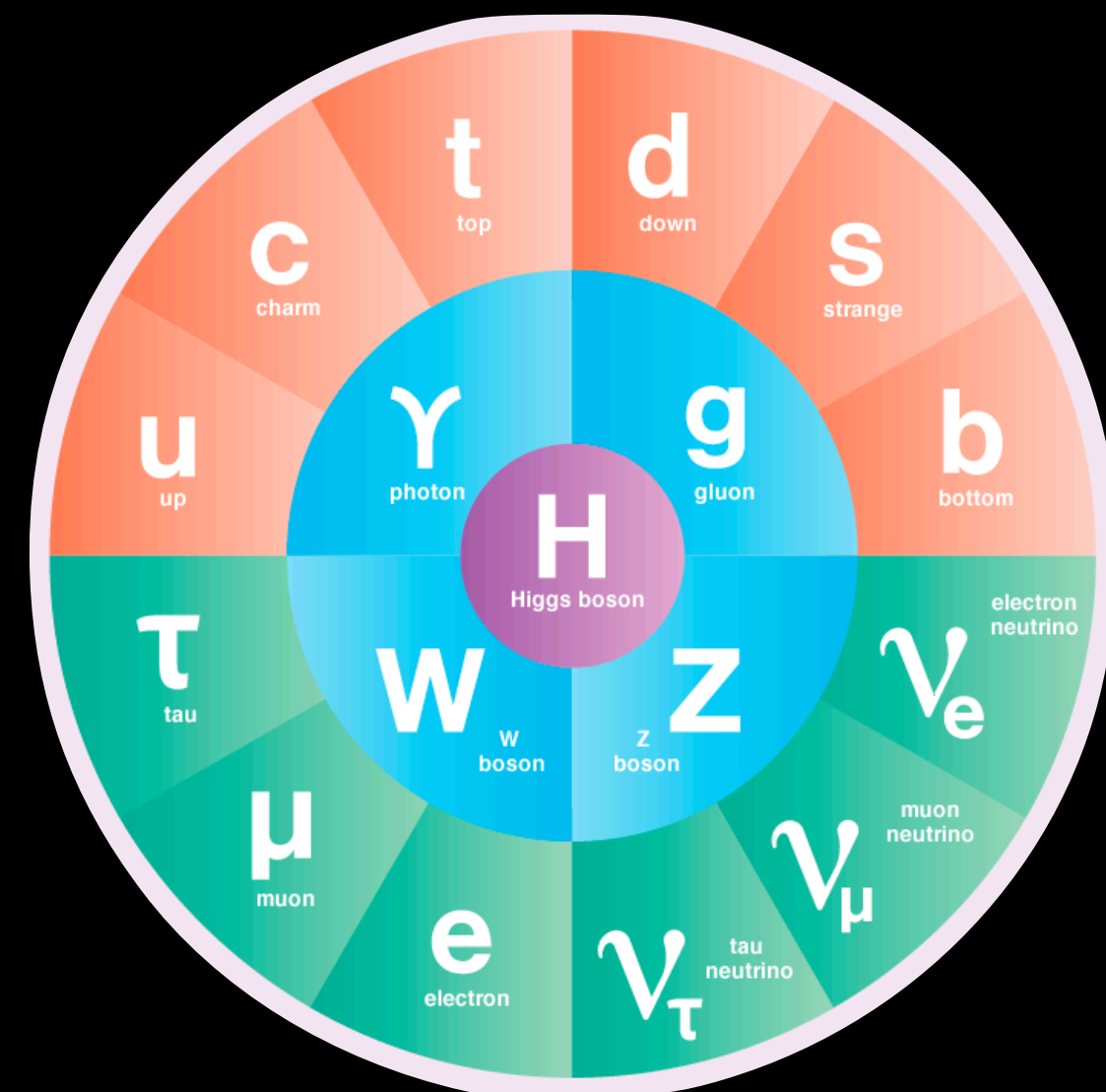
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The

PARTICLE

ZOO

Subatomic Particle Plush Toys

FROM THE STANDARD MODEL OF PHYSICS & beyond!

QUARKS



UP QUARK
A teeny little point inside the proton and neutron, it is friends forever with the down quark.



DOWN QUARK
A tiny little point inside the proton and neutron, it is friends forever with the up quark.



CHARM QUARK
A second generation quark, he is charmed, indeed.



STRANGE QUARK
What's so strange about this second generation quark?



TOP QUARK
This heavyweight champion doesn't live long enough to make friends with anyone.



BOTTOM QUARK
This third generation quark is puttin' on the pounds.

FORCE CARRIERS



PHOTON
The massless wavicle we know and love.



GLUON
The "glue" of the strong nuclear force.



W BOSON



Z BOSON
As the carrier particles of the weak nuclear force, they're downright obese.

LEPTONS



ELECTRON-NEUTRINO
This minuscule bandit is so light, he is practically massless.



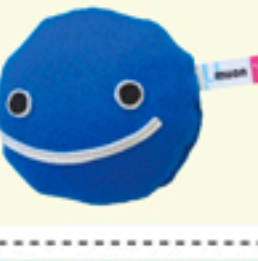
MUON-NEUTRINO
Like the other 2 neutrinos, he's got an identity crisis from oscillation.



TAU-NEUTRINO
He's a tau now, but what type of neutrino will he be next?



ELECTRON
A familiar friend, this negatively charged, busy li'l guy likes to bond.



MUON
A "heavy electron" who lives fast and dies young.



TAU
A "heavy muon" who could stand to lose a little weight.

THEORETICALS



HIGGS BOSON
He's the one everyone wants to meet, but for now he's playing hard to get. You'd be smiling too if everyone was looking to interview *you*.



TACHYON
Can this devious and clever particle really travel faster than light?



GRAVITON
Still unobserved, yet theoretically *everywhere*, he's got big legs for jumping branes.

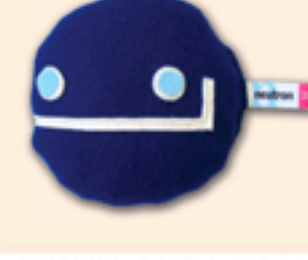


DARK MATTER
The mysterious missing mass. Difficult to see because he's *so dark*.

NUCLEONS



PROTON
We would not be here without her positivity.



NEUTRON
He insists on remaining neutral.

Visit the ANTIPARTICLE ANNEX

You can now buy antimatter on the web!



NEW! GIFT CARDS



STAMPSHEET

Twenty-three particles on one 8.5x11" sheet of perforated "stamps"



© Universe Today

10^{-35}m

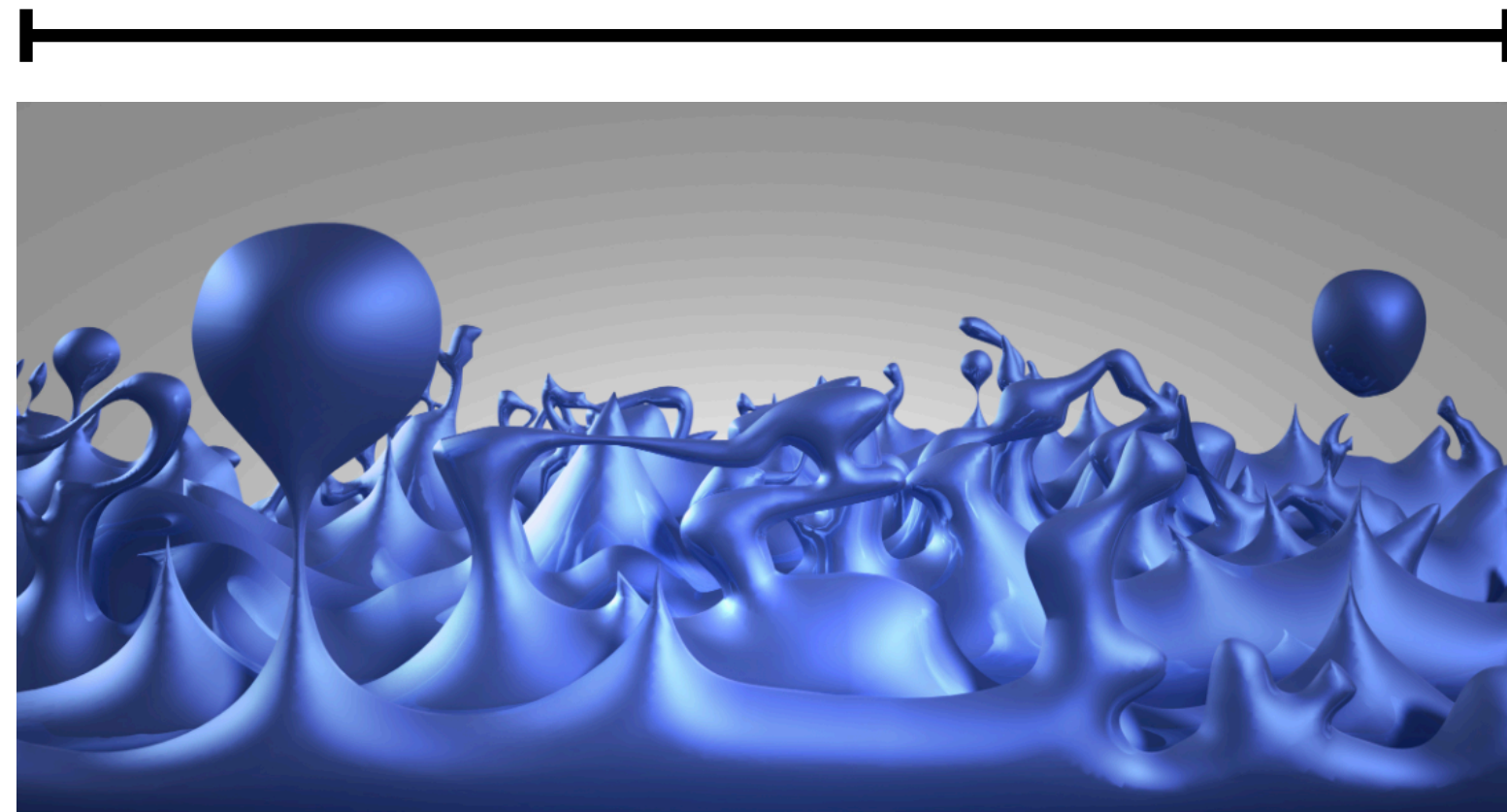
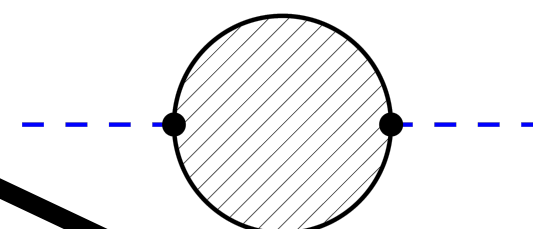


Image Credit: NASA/CXC/
M. Weiss

RGE



10^{-18}m

Standard Model of Elementary Particles

	three generations of matter (fermions)			interactions / force carriers (bosons)	
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
QUARKS	u up	c charm	t top	g gluon	H higgs
	$\approx 4.7 \text{ MeV}/c^2$	$\approx 96 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	d down	s strange	b bottom	γ photon	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
LEPTONS	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.66 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$	$\approx 91.19 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	e electron	μ muon	τ tau	Z Z boson	
	$< 1.0 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 18.2 \text{ MeV}/c^2$	$\approx 80.39 \text{ GeV}/c^2$	
	0	0	0	± 1	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	

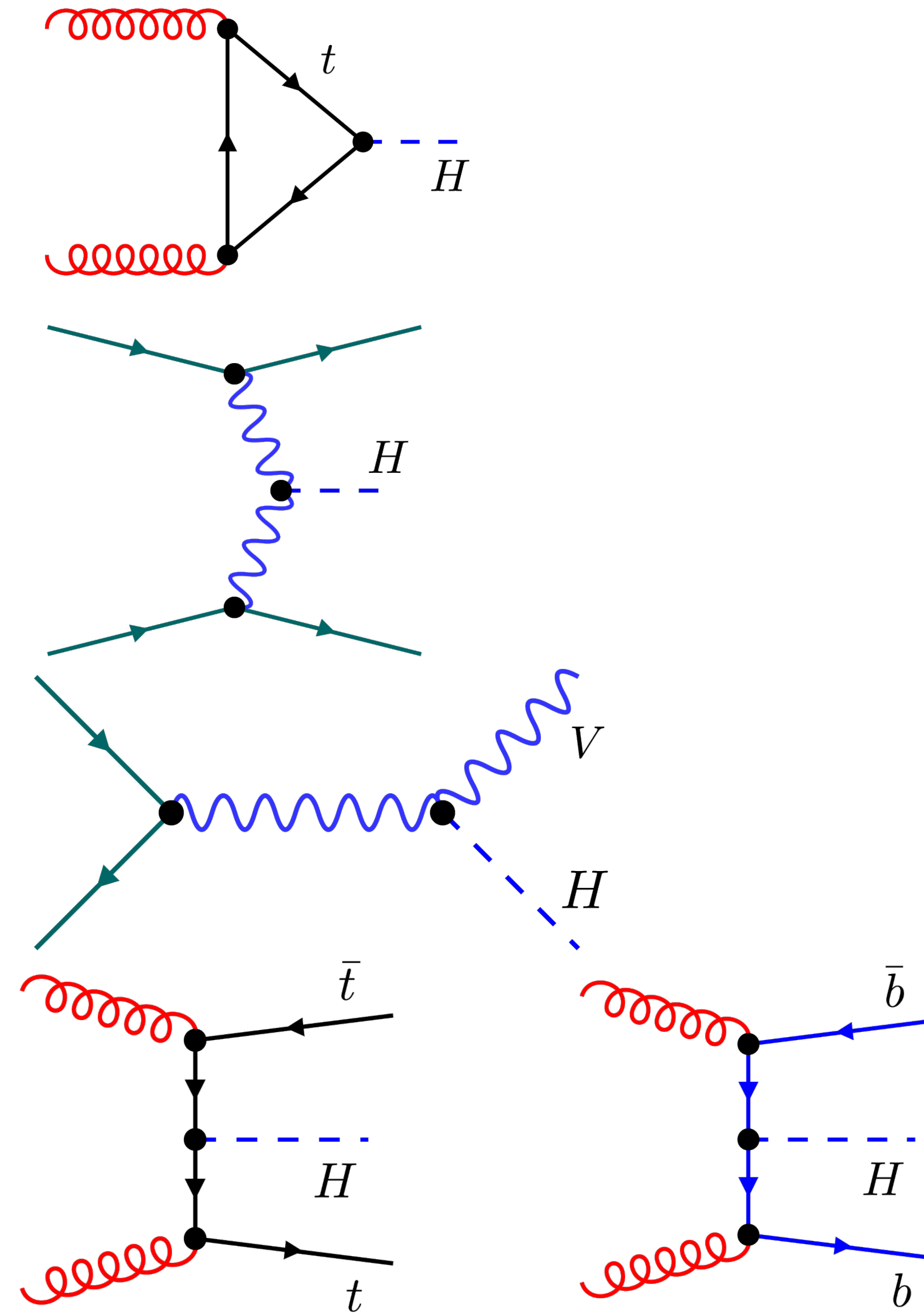
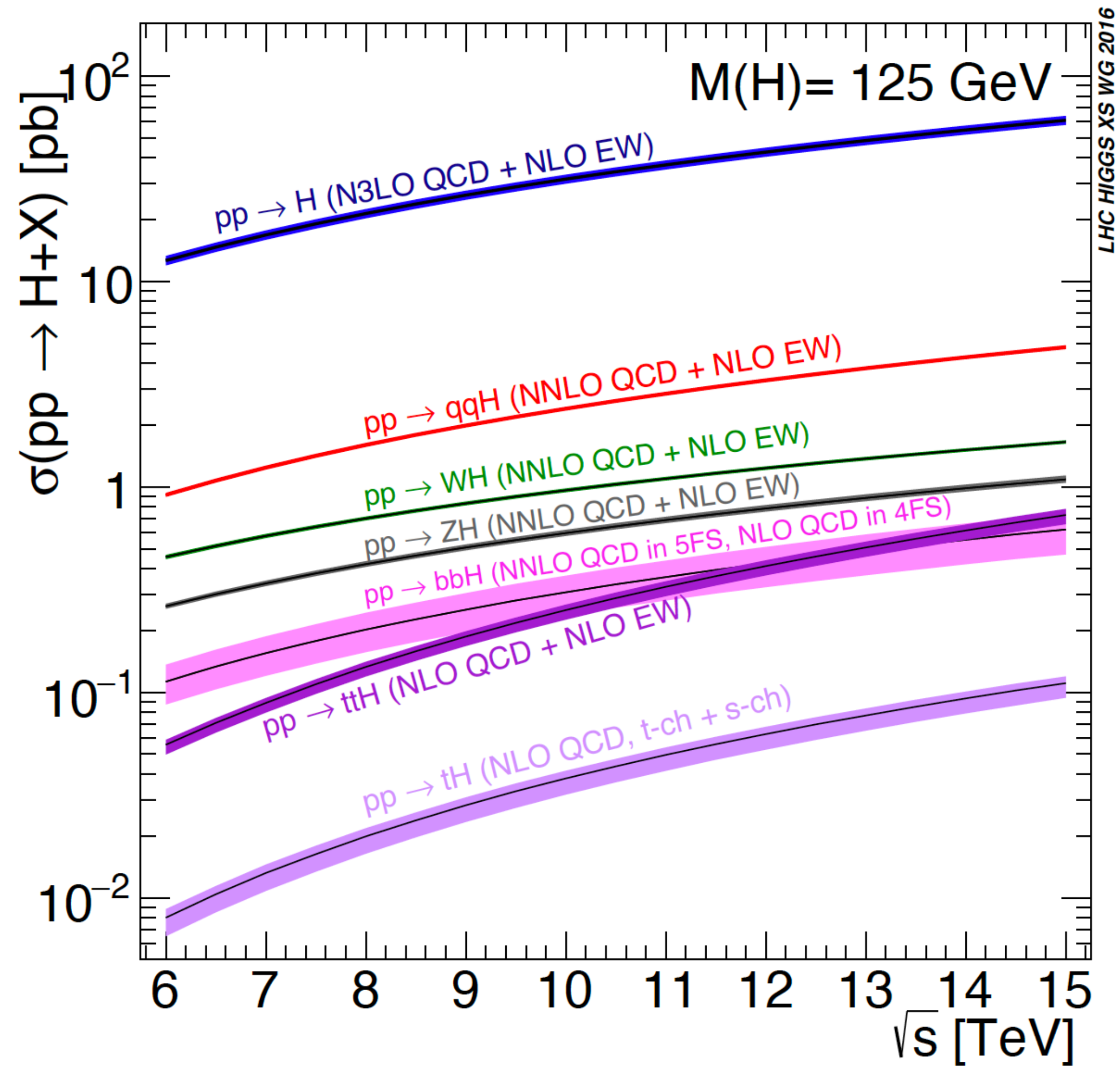
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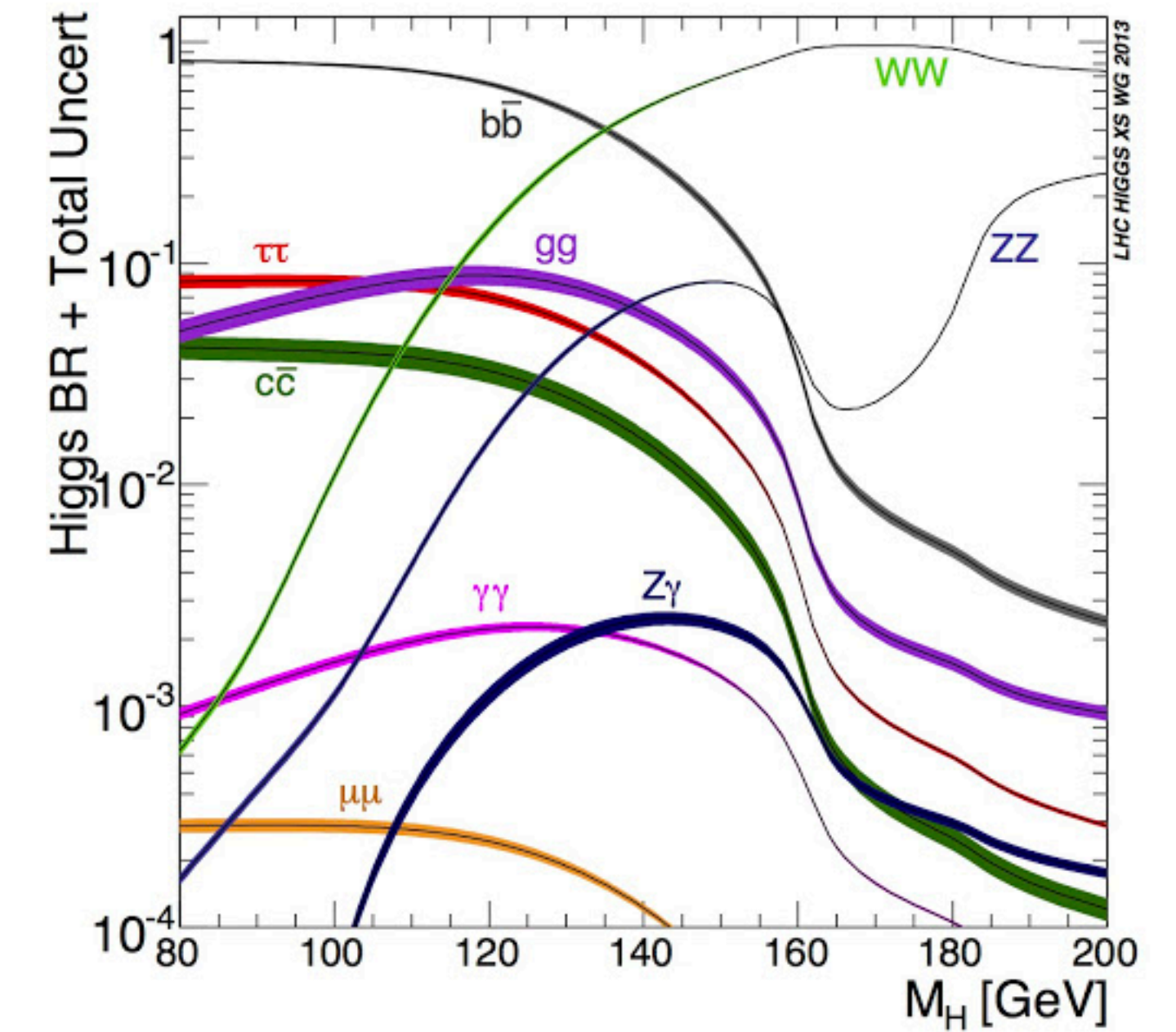
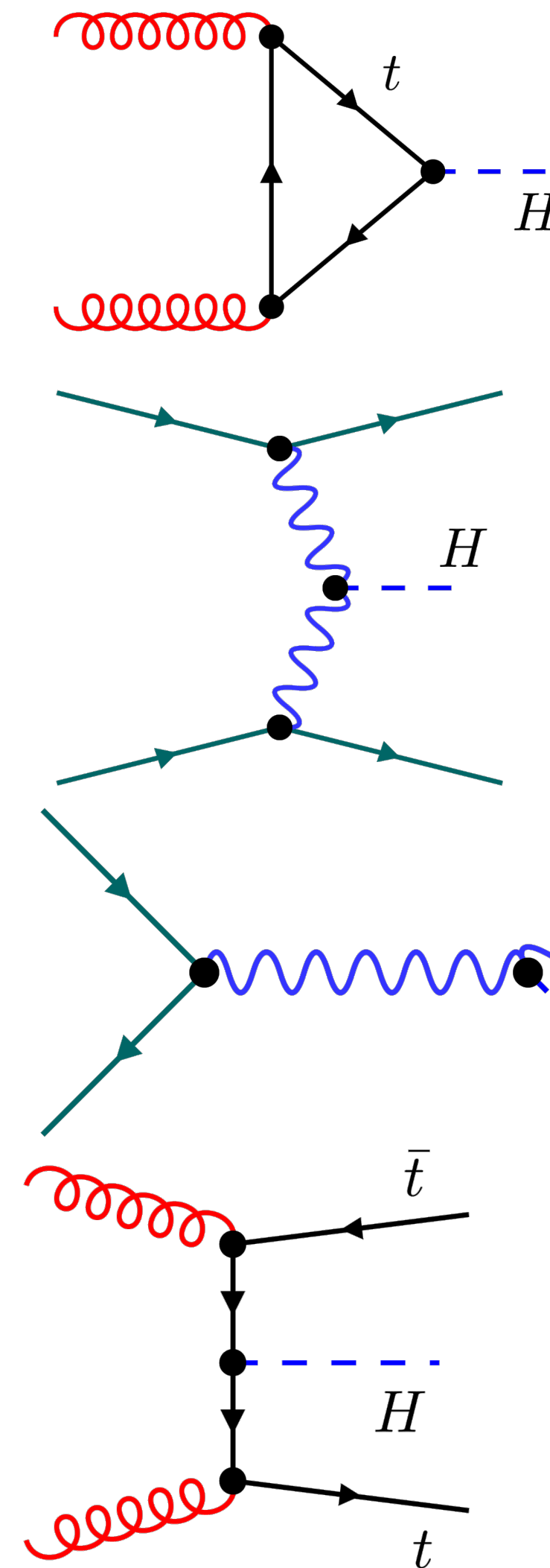
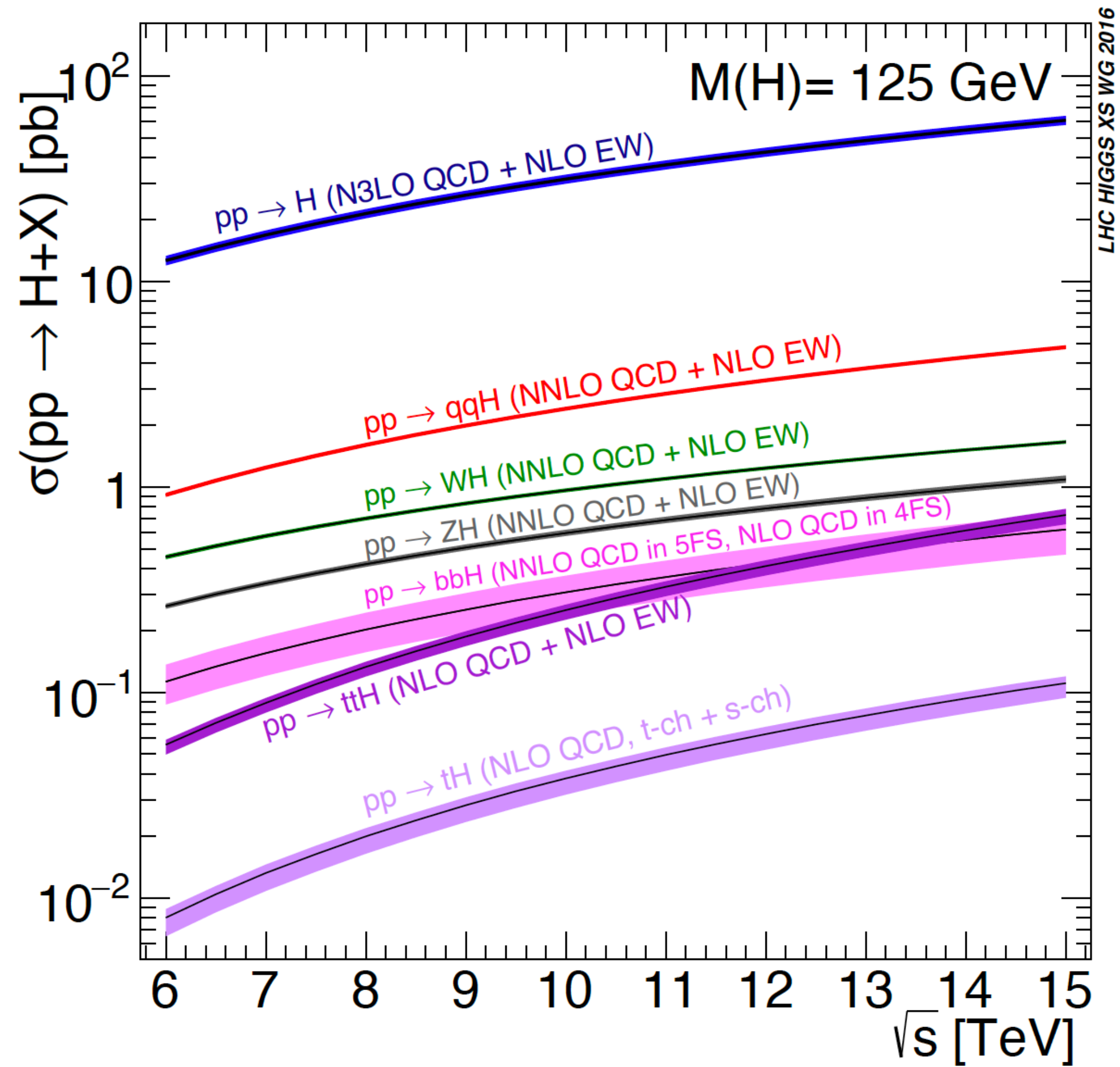
NATURALNESS, CHIRAL SYMMETRY, AND SPONTANEOUS
CHIRAL SYMMETRY BREAKING

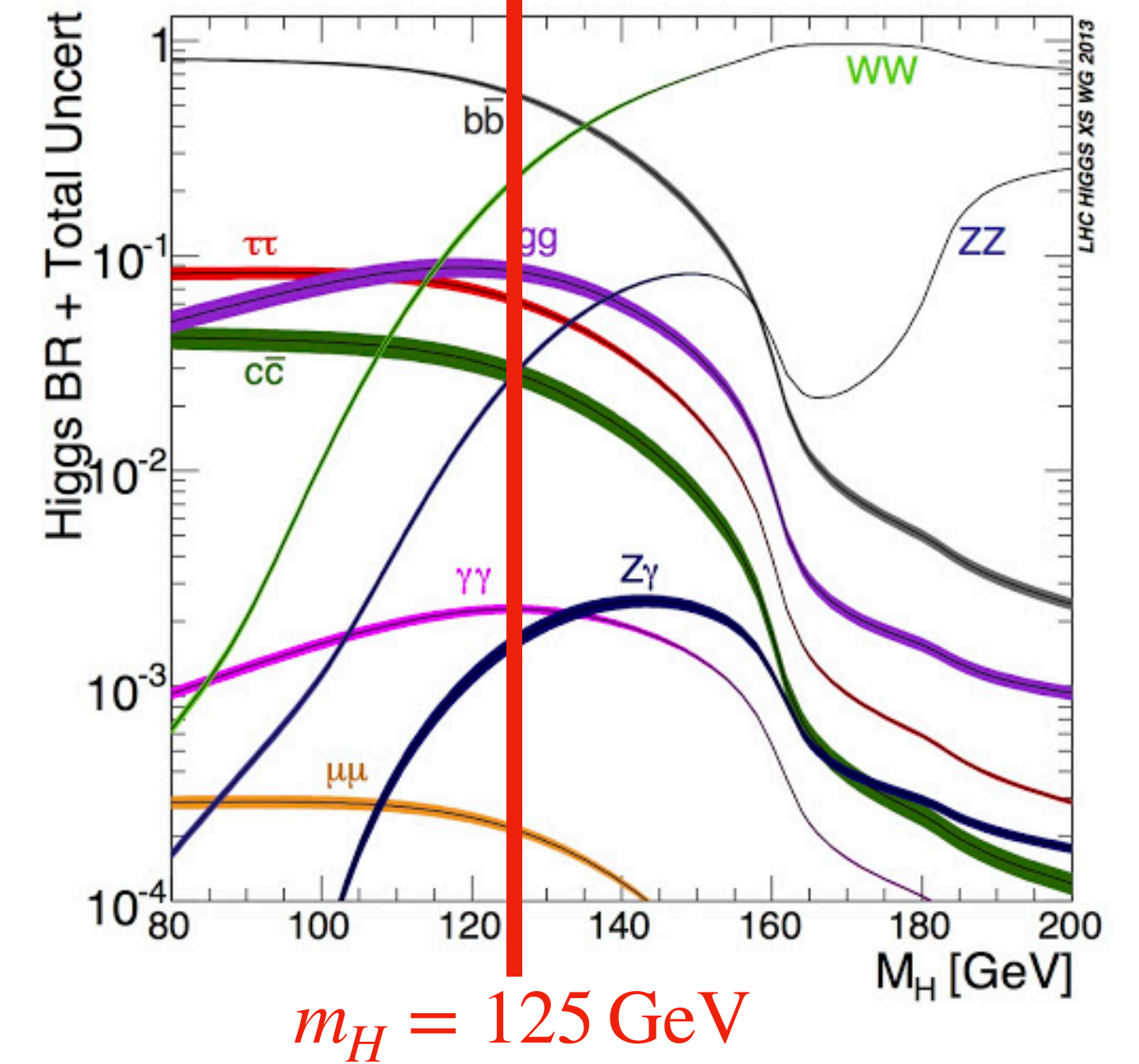
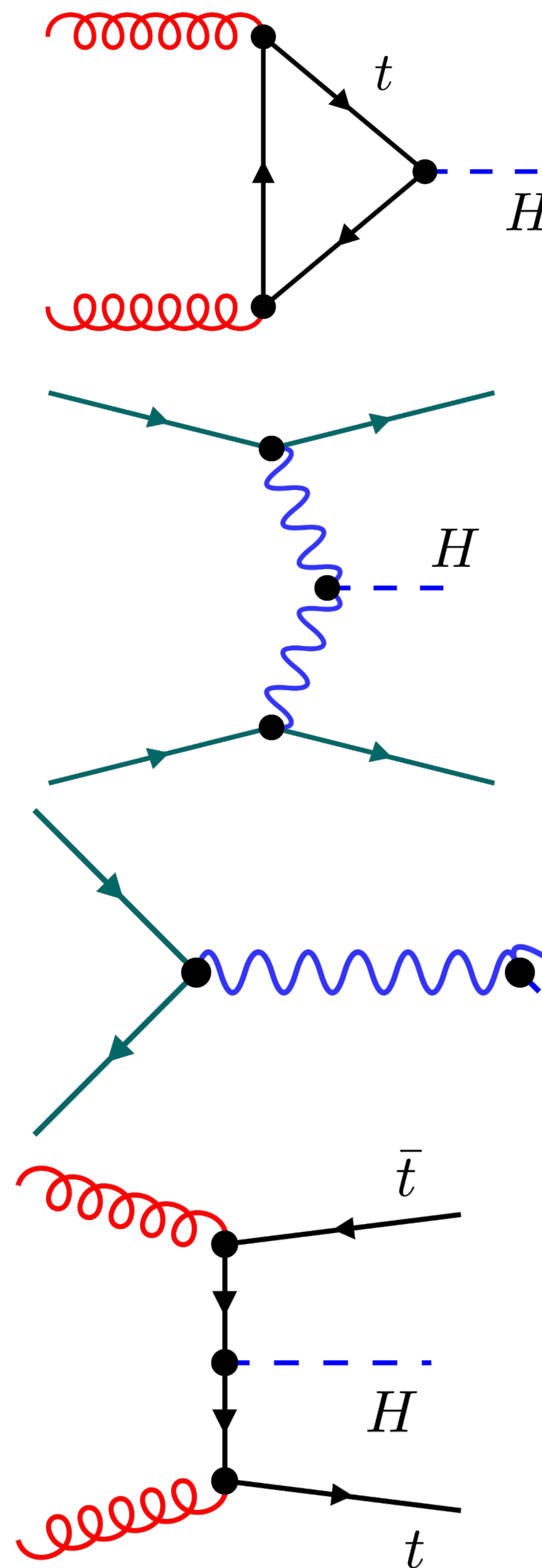
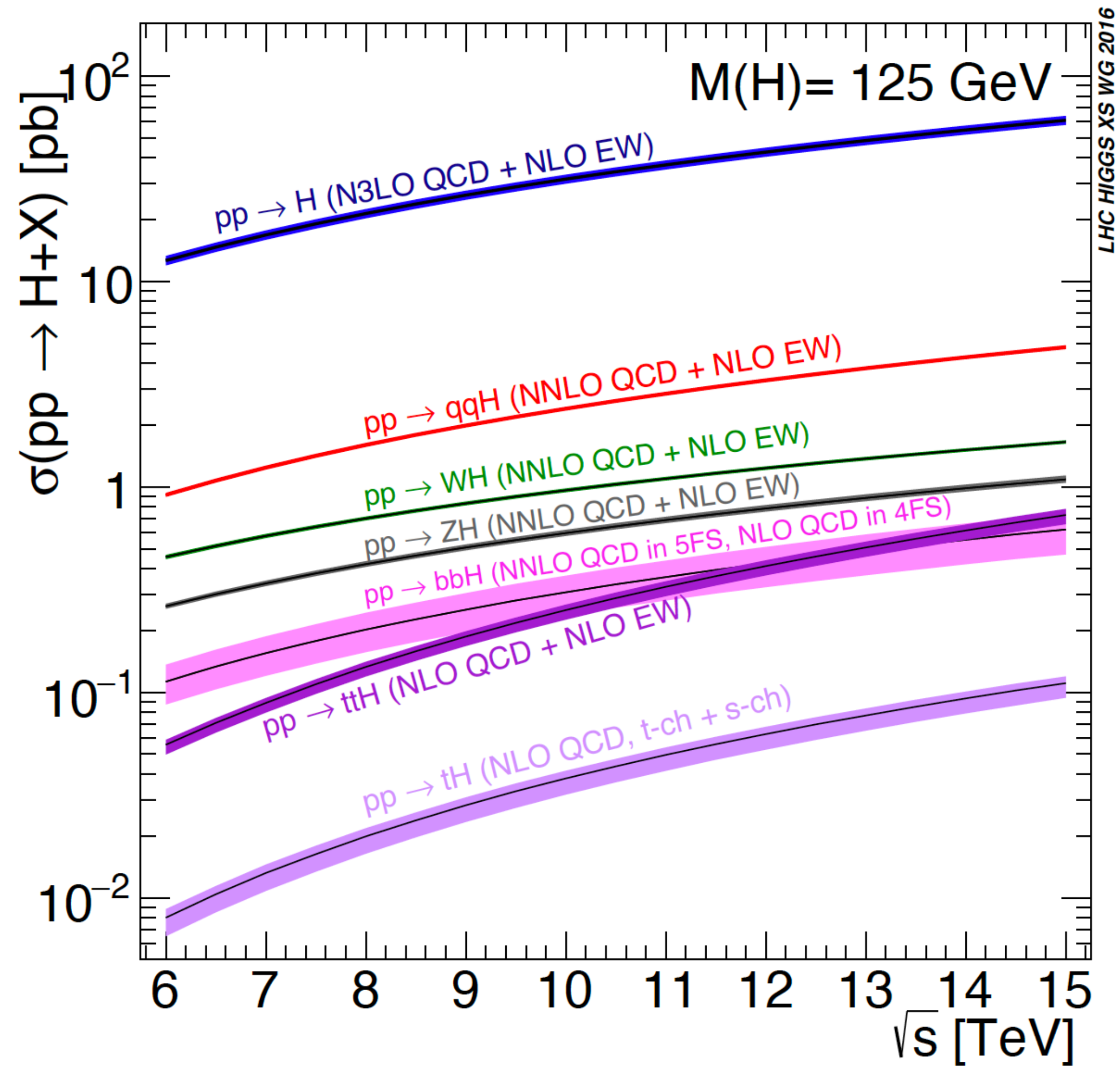
G. 't Hooft

1980

magnitude smaller than another then the smallest must satisfy our "dogma" separately. As we will see, naturalness will put the severest restriction on the occurrence of scalar particles in renormalizable theories. In fact we conjecture that this is the reason why light, weakly interacting scalar particles are not seen.







Collider Physics at the Precision Frontier

Gudrun Heinrich

P3H-20-044

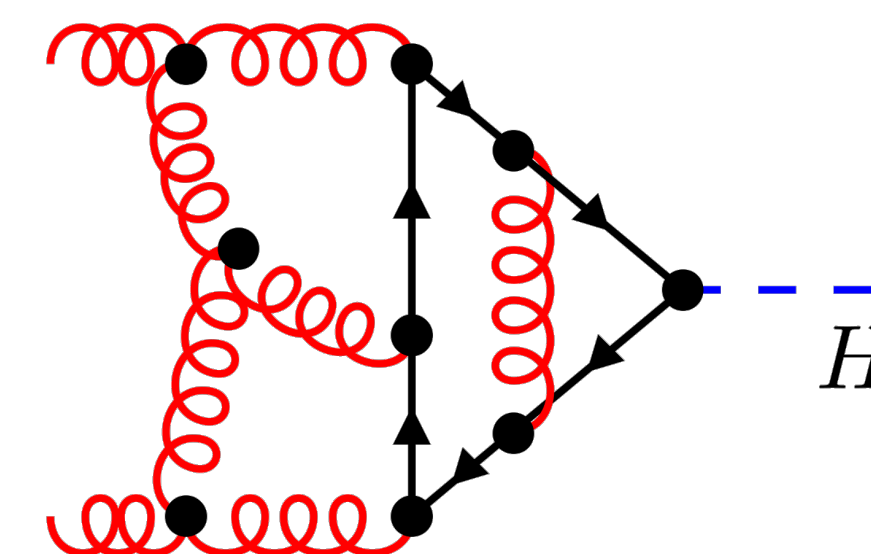
*Karlsruhe Institute of Technology, Institute for Theoretical Physics, Wolfgang-Gaede-Str. 1,
76131 Karlsruhe, Germany*

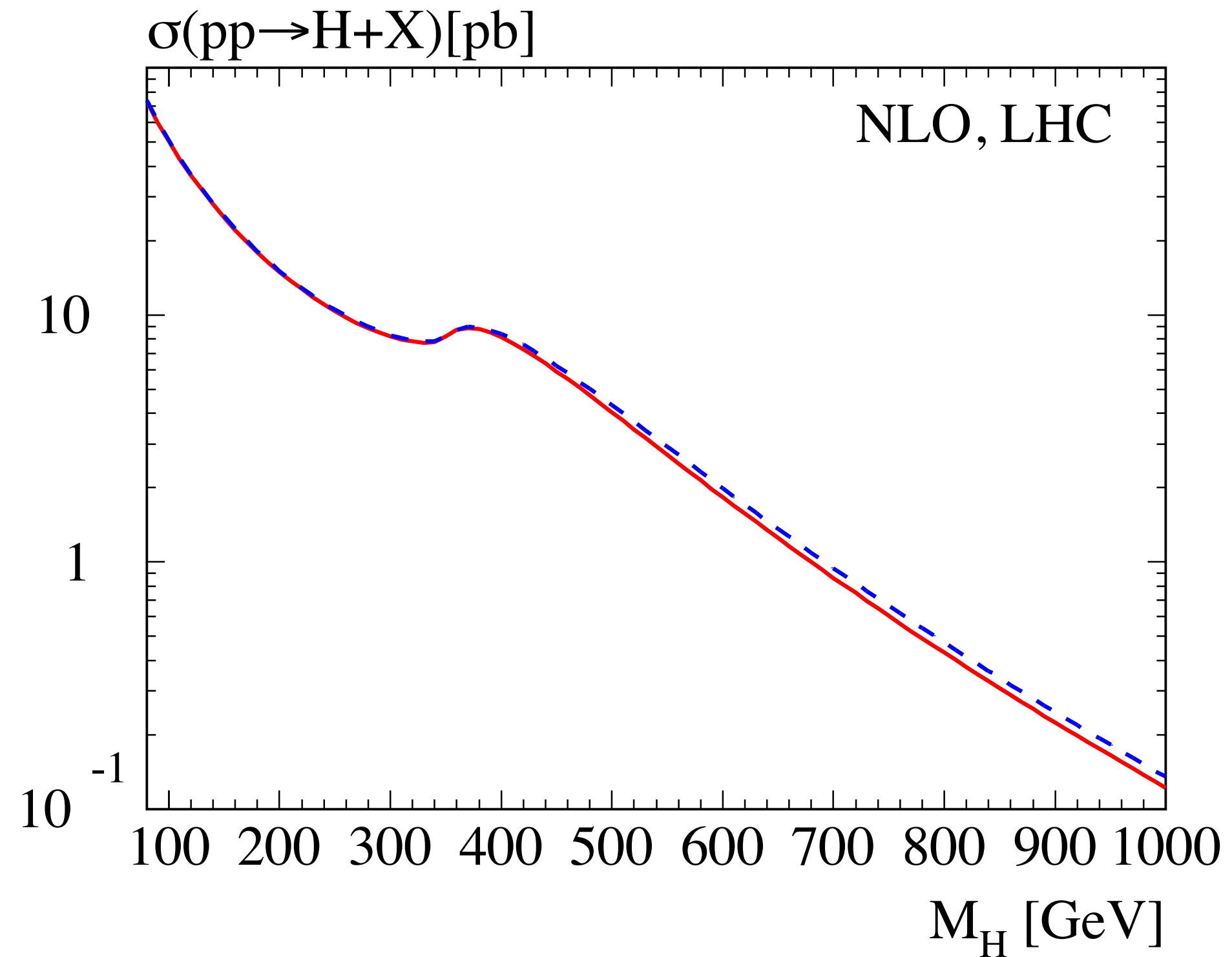
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LHCH(XS)WG YR4 '16

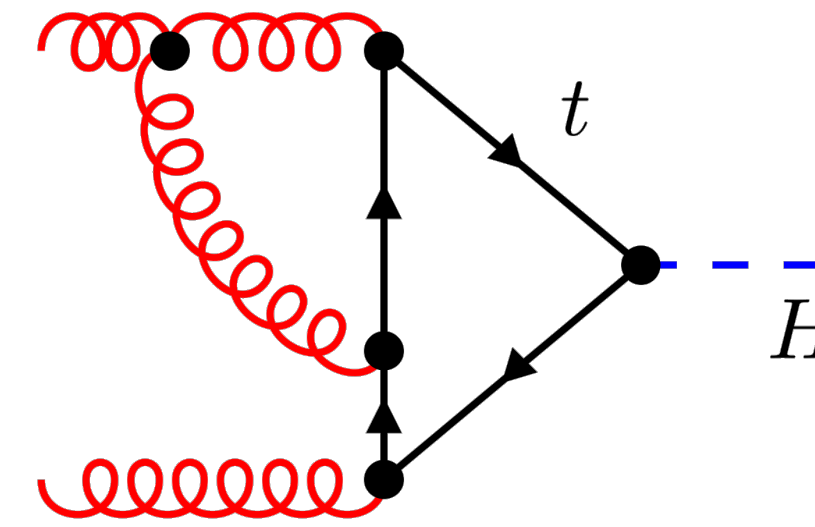
Inclusive gluon fusion cross section:

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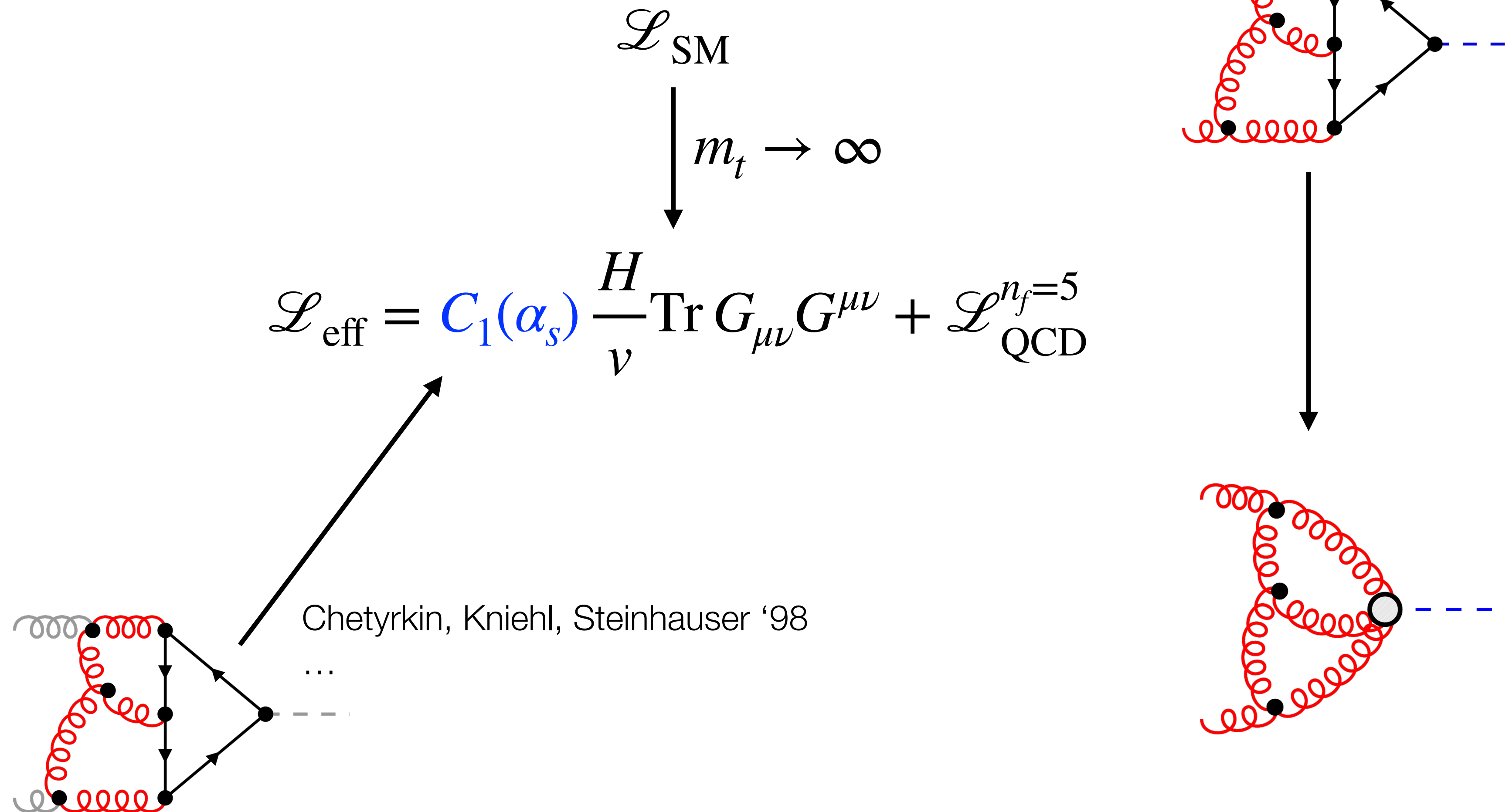
Graudenz, Djouadi, Spira, Zerwas '93

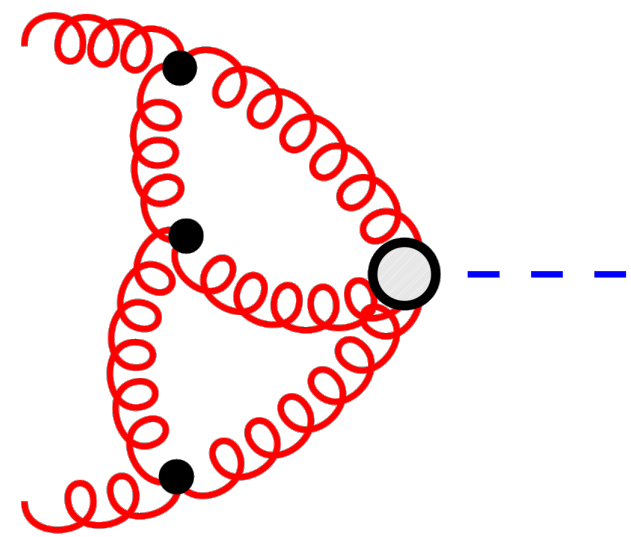


$$\sigma_{\text{HEFT}}^{\text{HO}} = \sigma^{\text{LO}} \left(\frac{\sigma^{\text{HO}}}{\sigma^{\text{LO}}} \right)_{m_t \rightarrow \infty}$$

$$\sigma_{\text{exact}}^{\text{NLO}} = (1 - 0.008) \cdot \sigma_{\text{HEFT}}^{\text{NLO}}$$

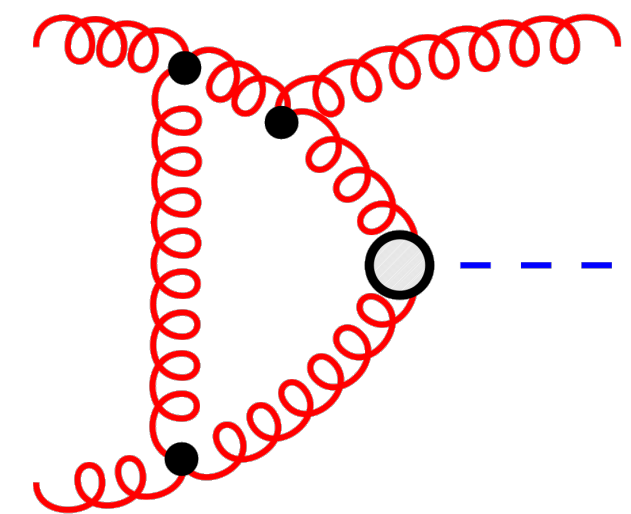
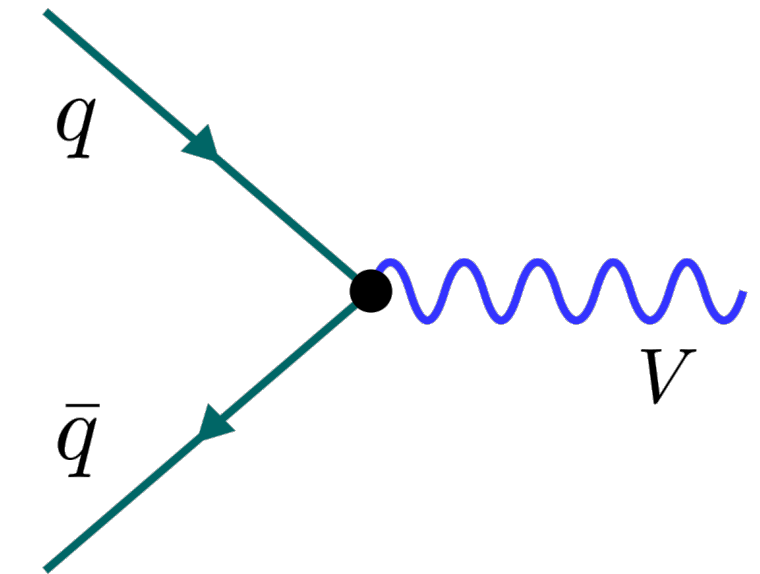
for $m_H = 125 \text{ GeV}$



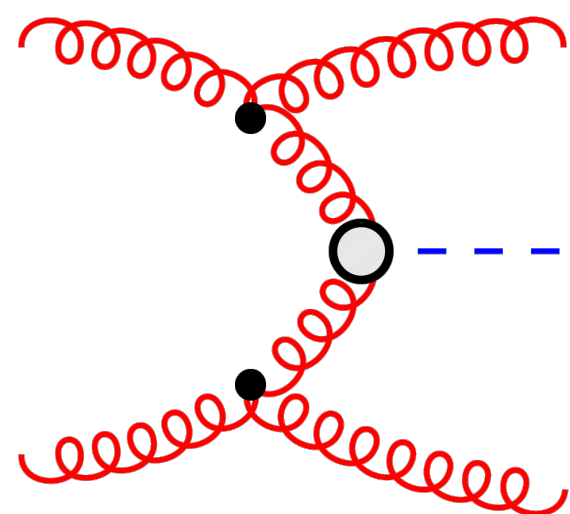


- need to cancel IR divergences
- around '01: only NLO methods
- but: NNLO Drell-Yan 1990

v. Neerven et al.



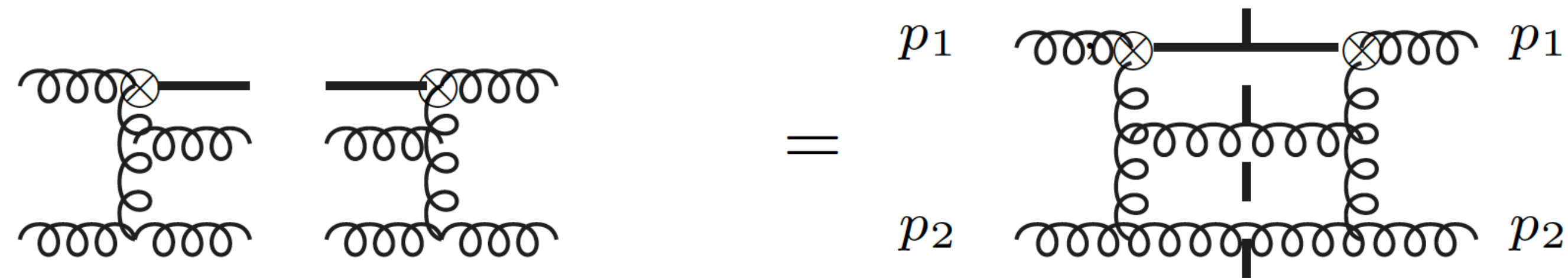
perform phase space integrals analytically
in D dimensions



IR poles cancel analytically (no “subtraction scheme”)

still: phase space integration complicated (back then...)

Reverse unitarity:



$$2i\pi\delta(p^2 - m^2) \rightarrow \frac{1}{p^2 - m^2 + i0} - \frac{1}{p^2 - m^2 - i0}$$

Anastasiou, Melnikov '02

Anastasiou, Dixon, Melnikov '03

Treat phase space integrals like loop integrals:

integration-by-parts $\rightarrow$ master integrals $\rightarrow$ differential equations

soft expansion:

$$z = \hat{s}/M_H^2 \rightarrow 1$$

$$\hat{\sigma}_{ij} = \sum_{n \geq 0} \left(\frac{\alpha_s}{\pi} \right)^n \hat{\sigma}_{ij}^{(n)},$$

$$\begin{aligned} \hat{\sigma}_{ij}^{(n)} = & a^{(n)} \delta(1-x) + \sum_{k=0}^{2n-1} b_k^{(n)} \left[\frac{\ln^k(1-x)}{1-x} \right]_+ \\ & + \sum_{l=0}^{\infty} \sum_{k=0}^{2n-1} c_{lk}^{(n)} (1-x)^l \ln^k(1-x), \end{aligned}$$

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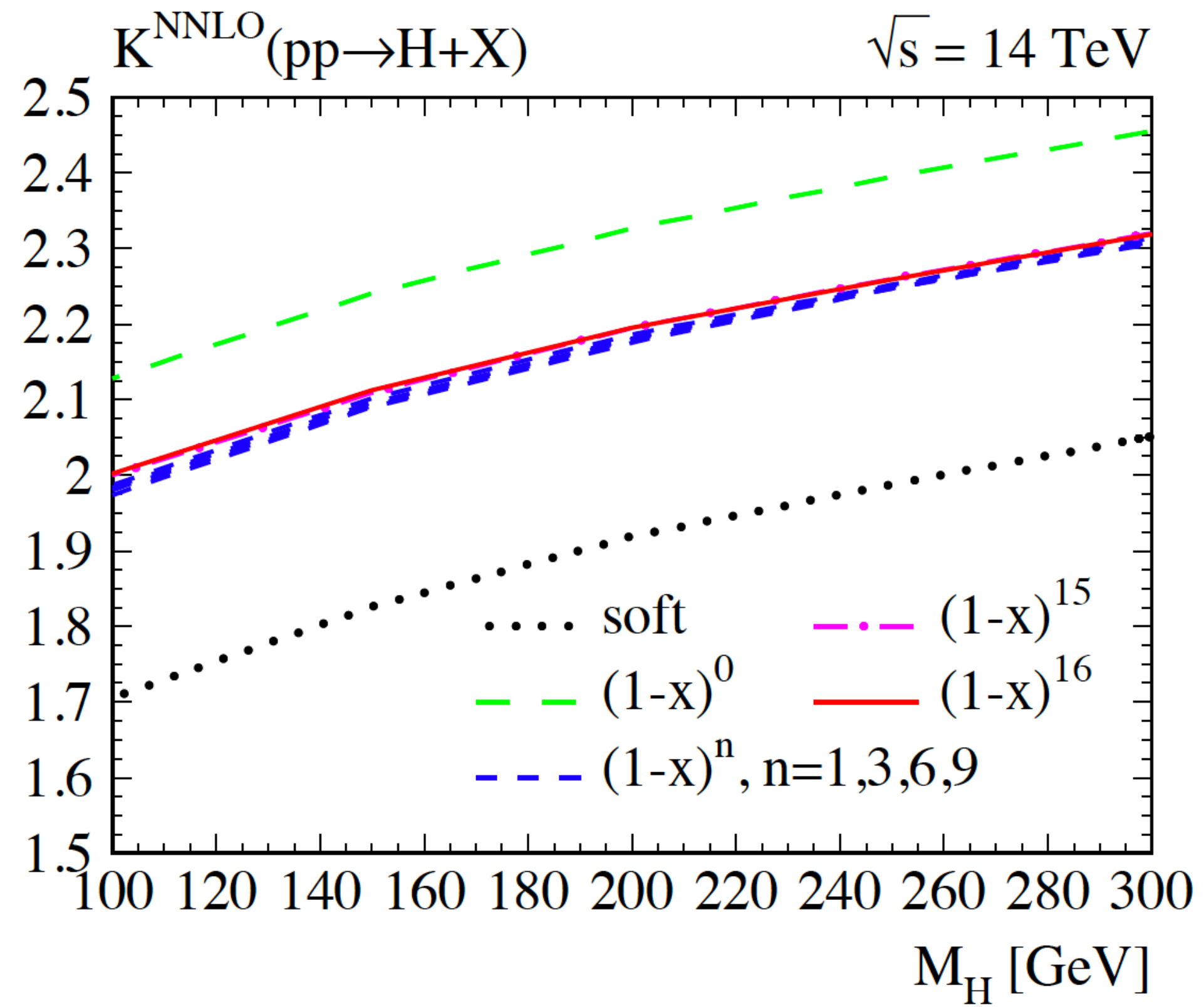
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$l = 0, k > 0$: next-to-soft approximation

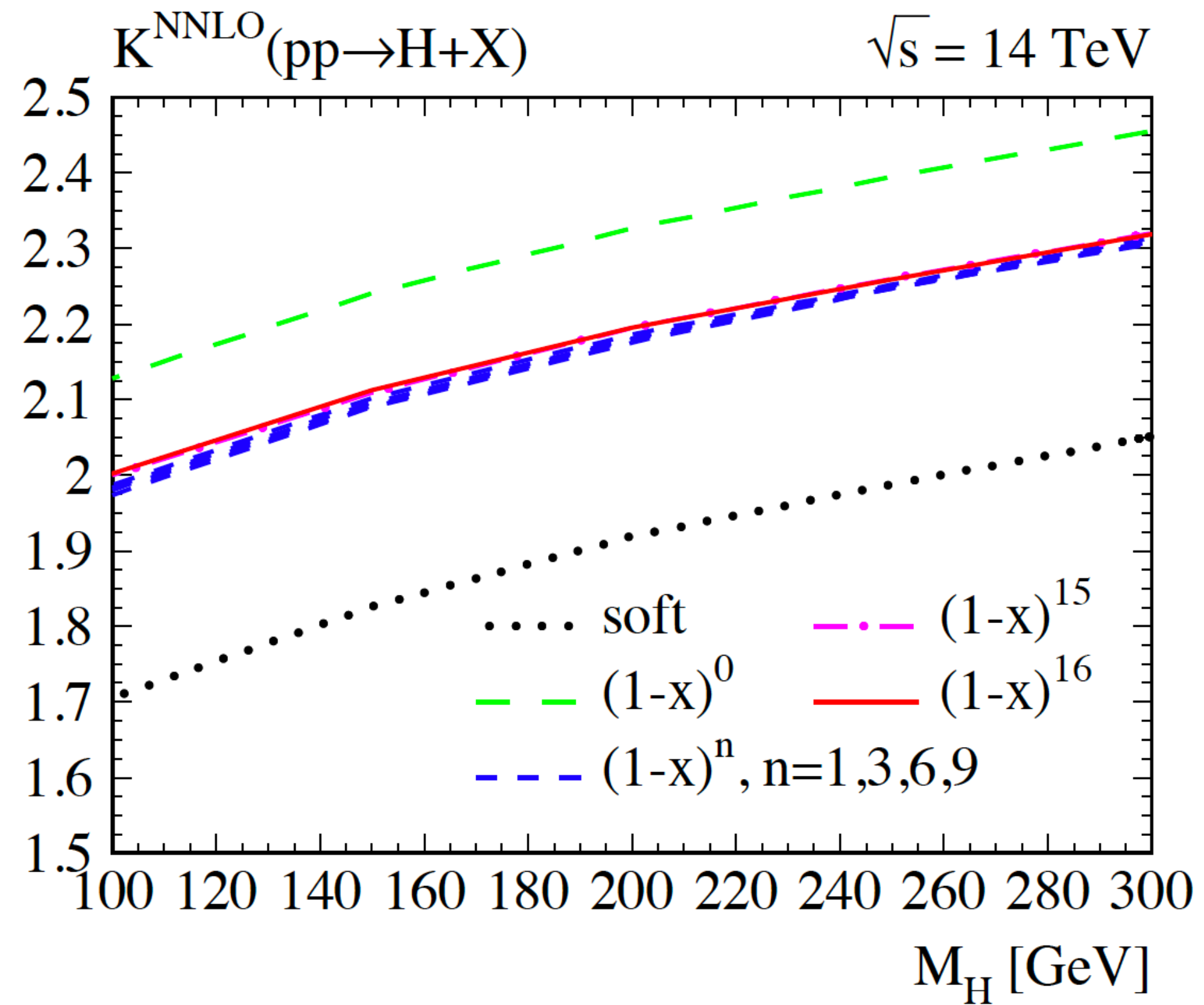
Krämer, Laenen, Spira '96

NNLO



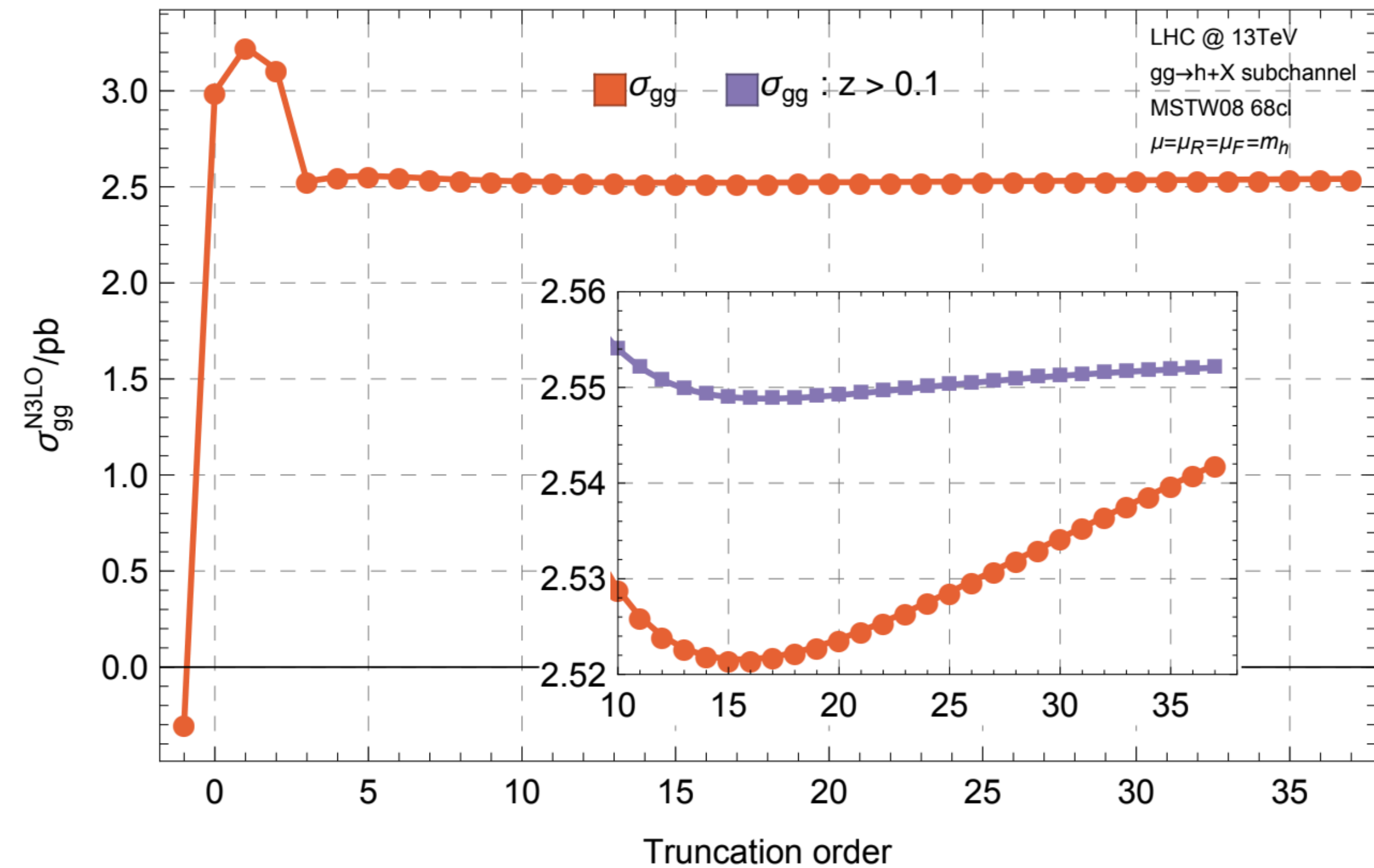
RH, Kilgore '02

NNLO



RH, Kilgore '02

N³LO



Anastasiou, Duhr, Dulat, Herzog, Mistlberger '15

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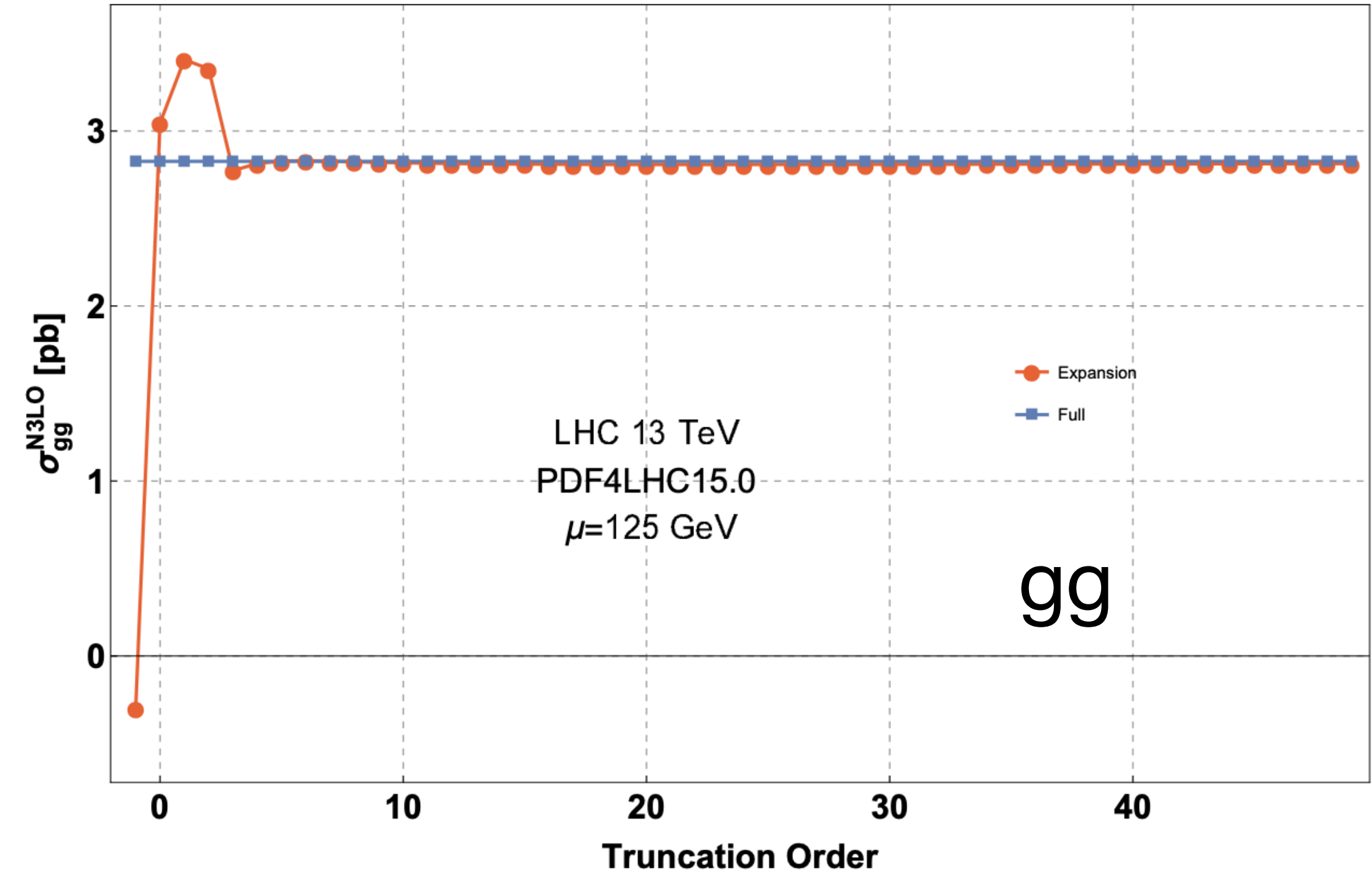
LHCHWG YR4 '16

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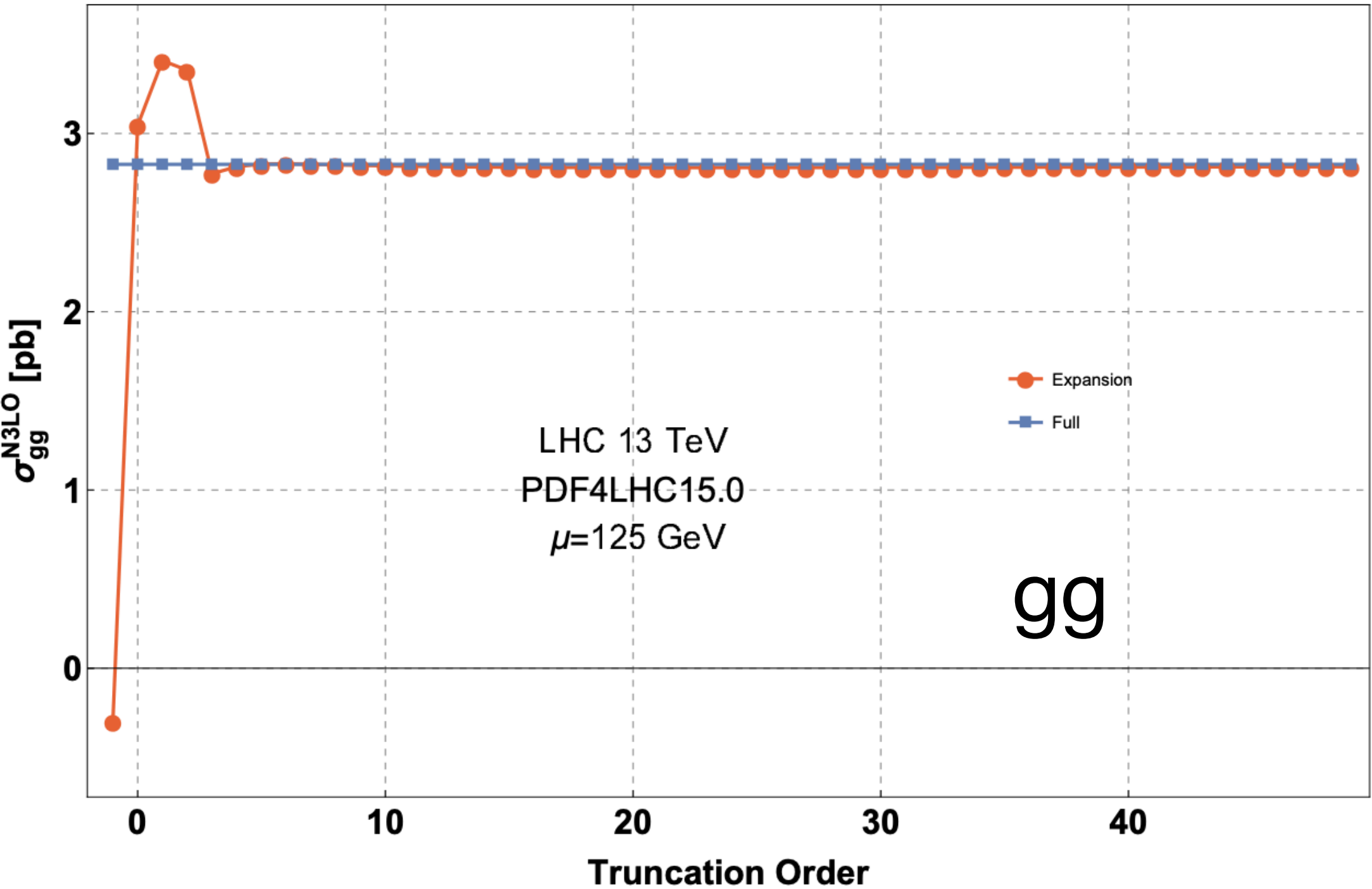
LHCHWG YR4 '16



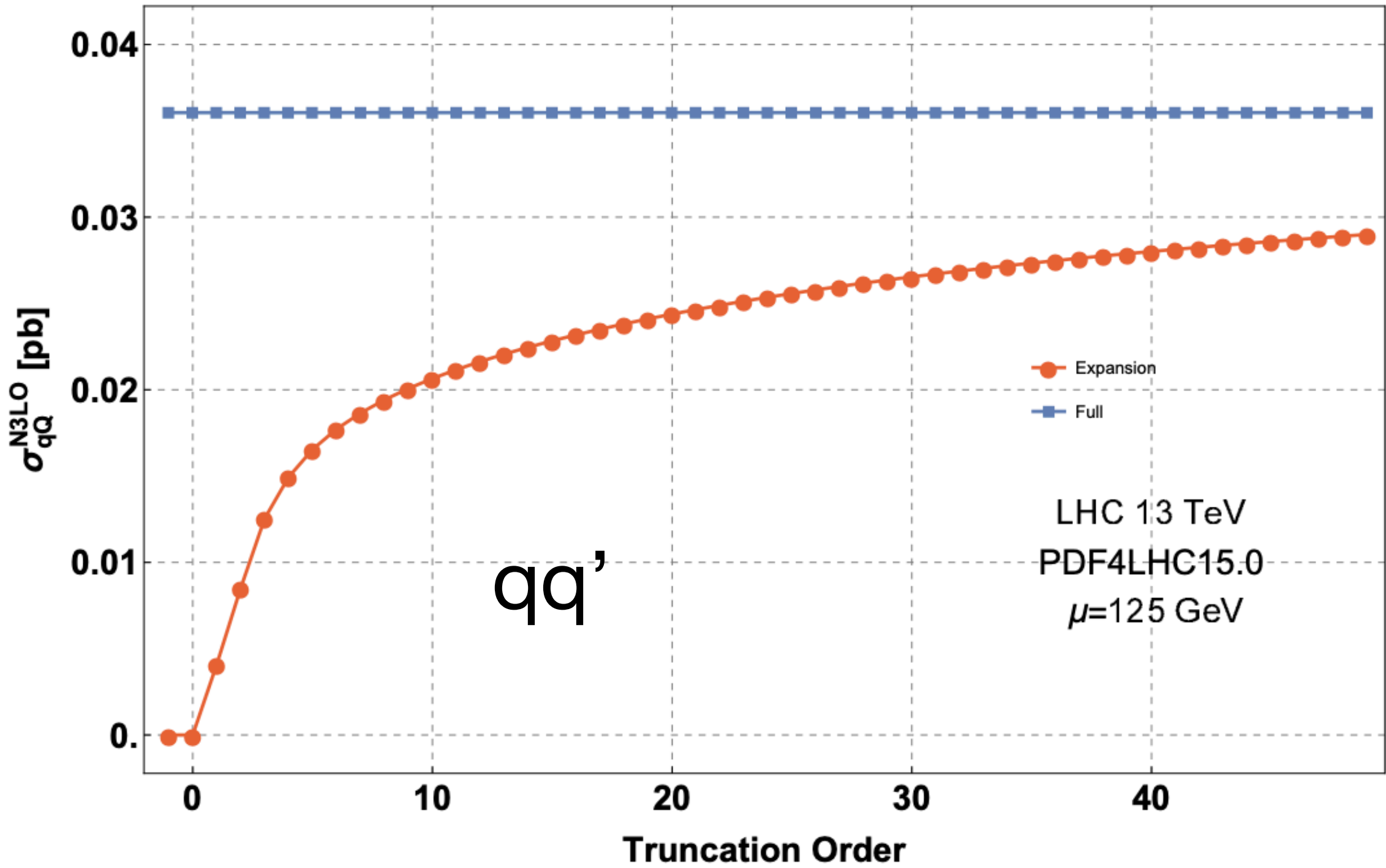
Mistlberger '18

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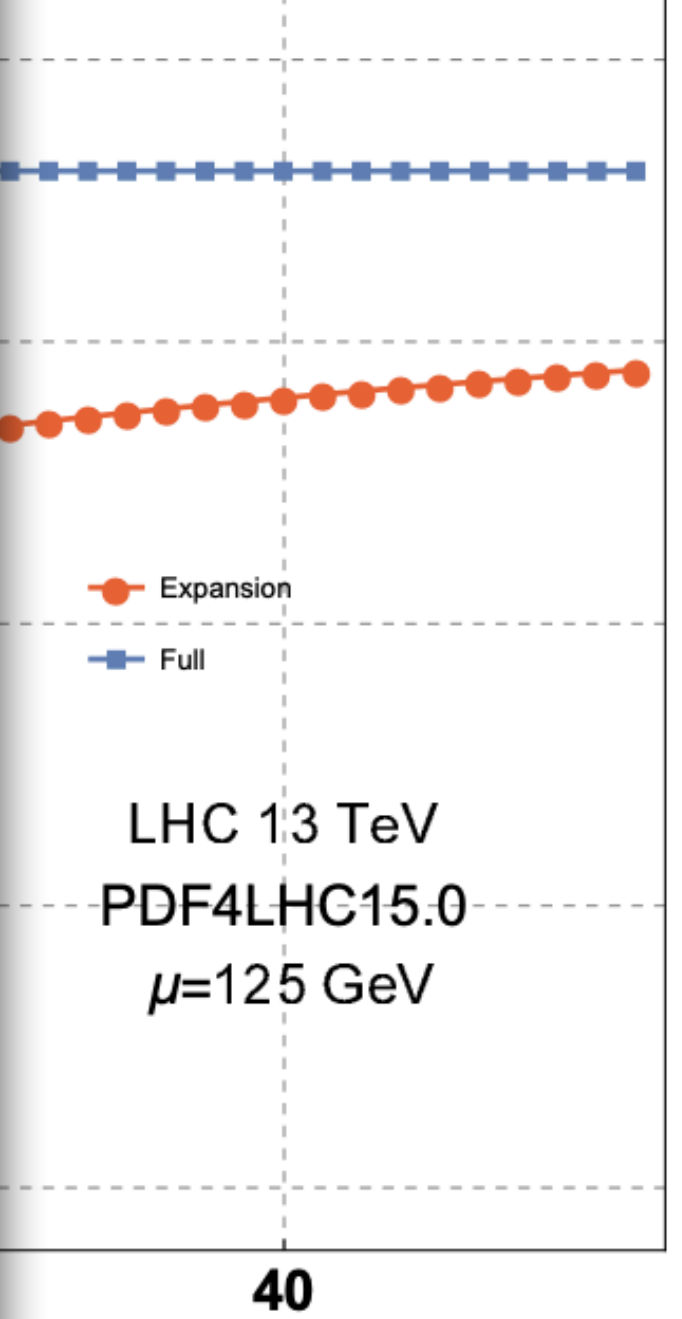
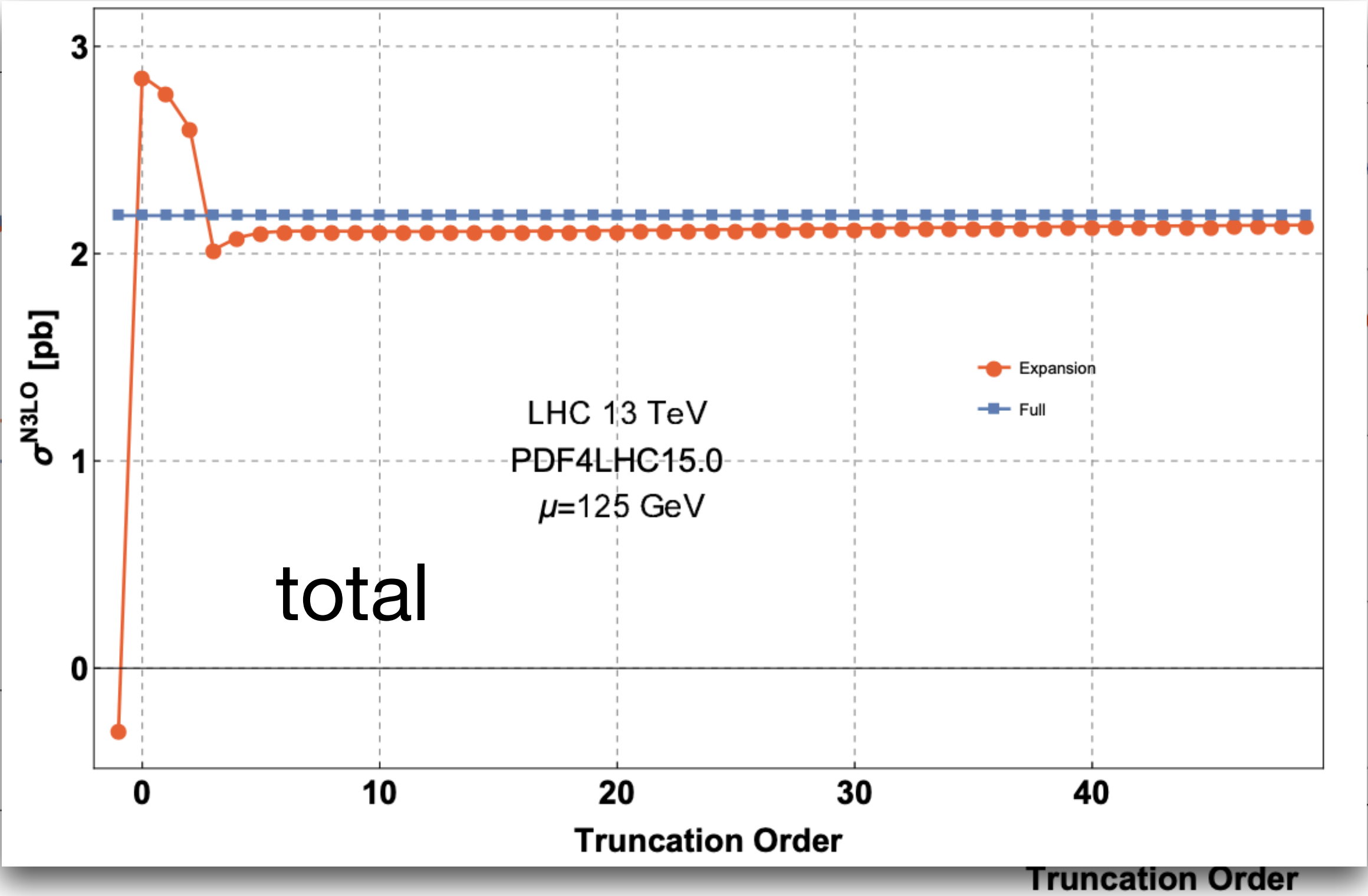
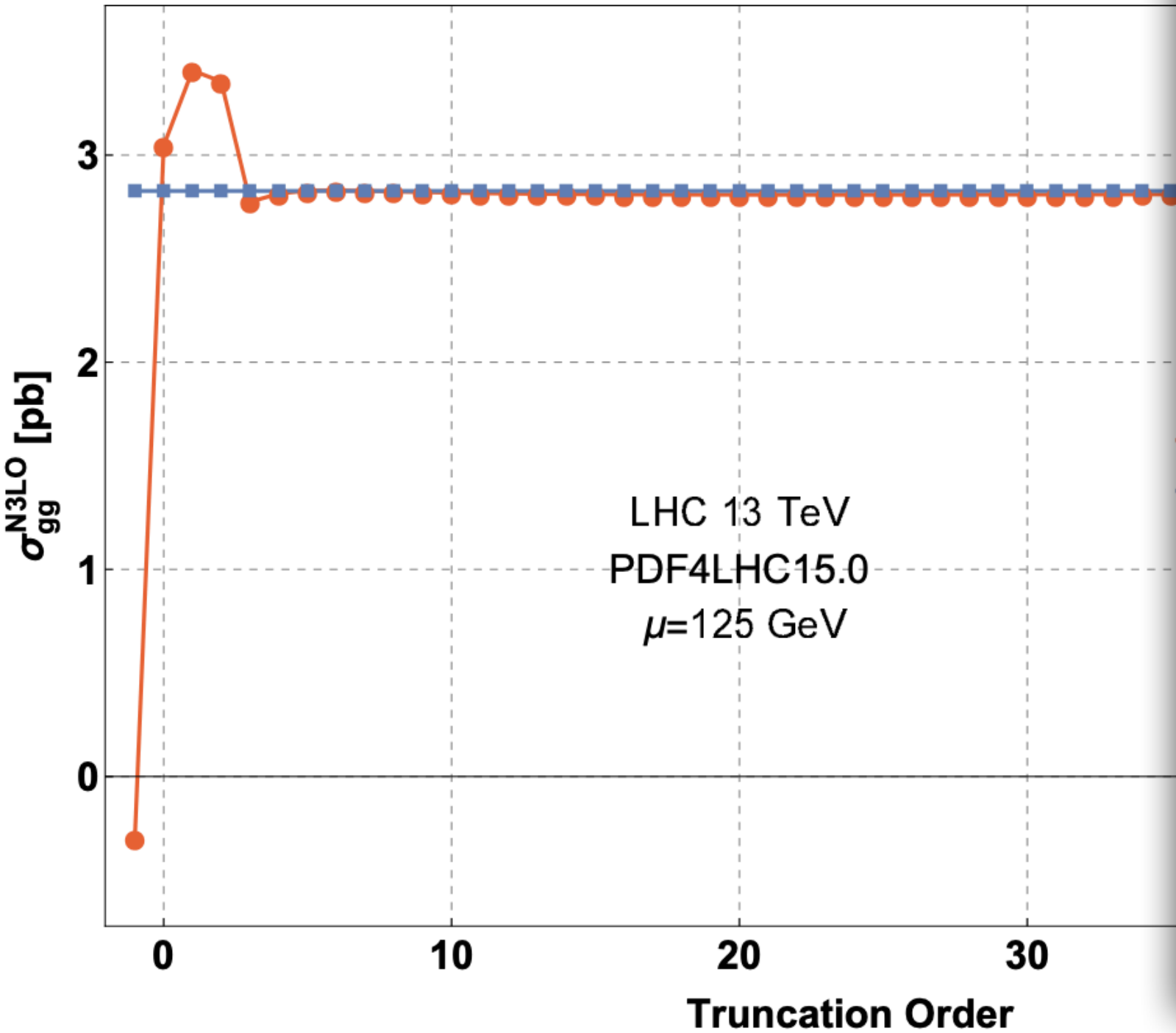


Mistlberger '18



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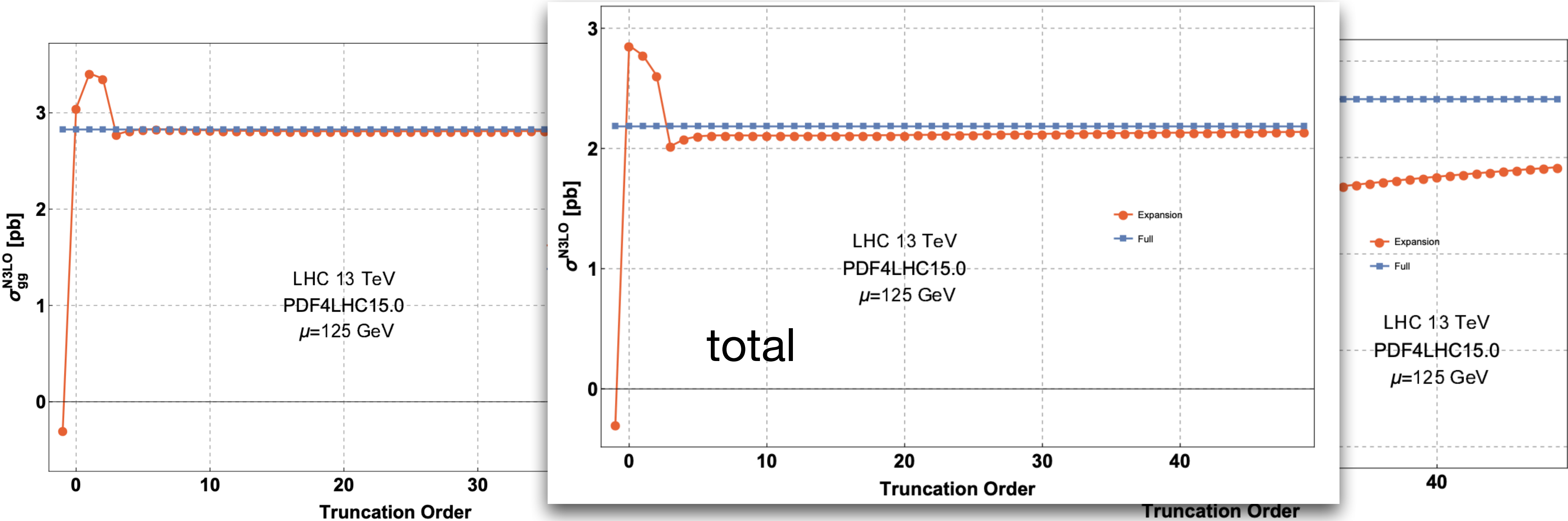
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LHCHWG YR4 '16



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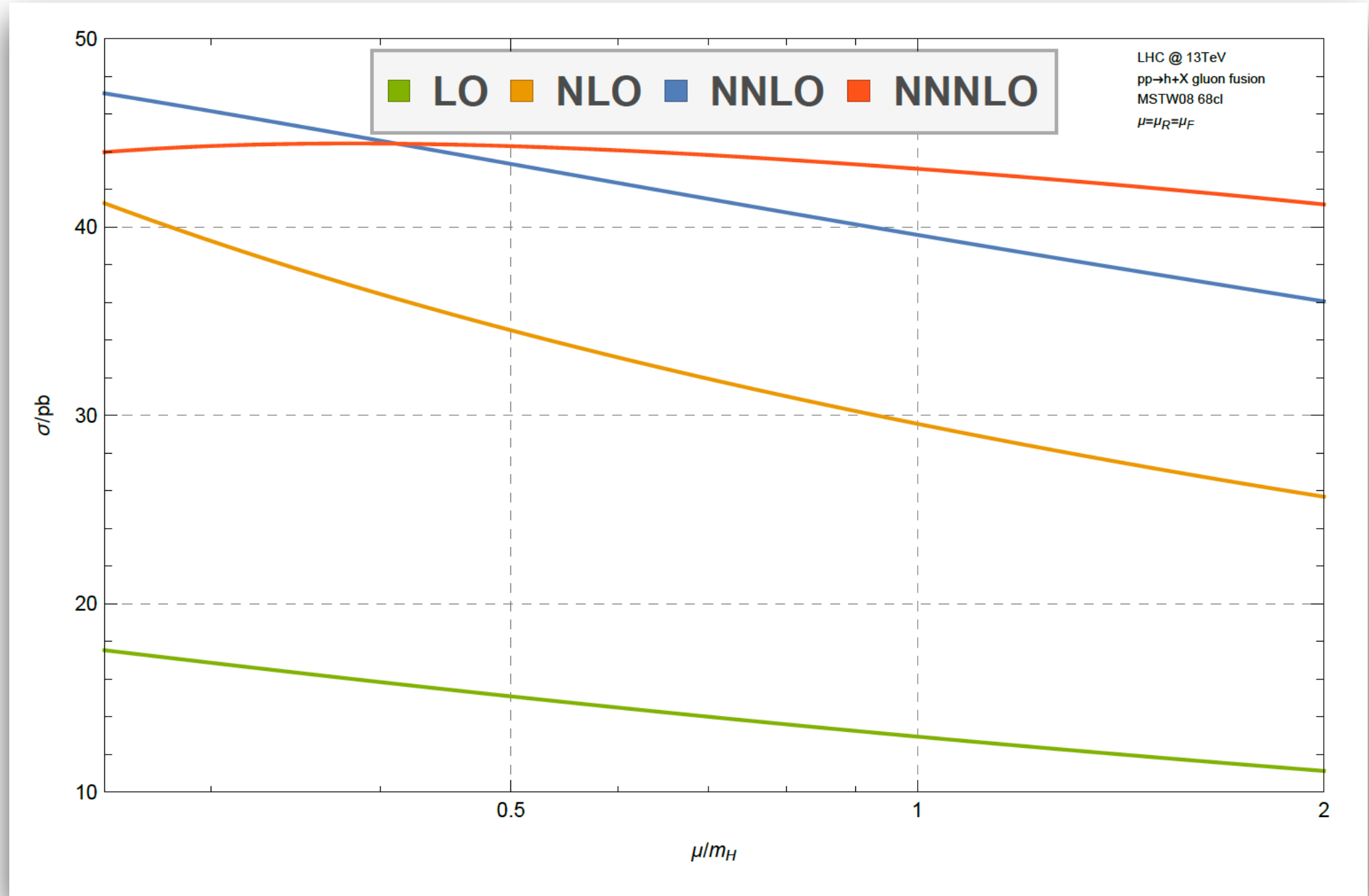
$$K \approx 3$$

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 &+ 20.84 \text{ pb} \\
 &- 2.05 \text{ pb} \\
 &+ 9.56 \text{ pb} \\
 &+ 0.34 \text{ pb} \\
 &+ 2.40 \text{ pb} \\
 &+ 1.49 \text{ pb}
 \end{aligned}$$



$$K \approx 3$$

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
+0.10 pb -1.15 pb	± 0.18 pb	± 0.56 pb	± 0.49 pb	± 0.40 pb	± 0.49 pb
+0.21% -2.37%	$\pm 0.37\%$	$\pm 1.16\%$			

Approximate four-loop QCD corrections to the Higgs-boson production cross section

P3H-20-054

G. Das^{*a}, S. Moch^{†b} and A. Vogt^{‡c}

soft-virtual approximation

$$\hat{\sigma}_{ij} = \sum_{n \geq 0} \left(\frac{\alpha_s}{\pi} \right)^n \hat{\sigma}_{ij}^{(n)},$$

$$\hat{\sigma}_{ij}^{(n)} = a^{(n)} \delta(1-x) + \sum_{k=0}^{2n-1} b_k^{(n)} \left[\frac{\ln^k(1-x)}{1-x} \right]_+ + \sum_{l=0}^{\infty} \sum_{k=0}^{2n-1} c_{lk}^{(n)} (1-x)^l \ln^k(1-x),$$

$\delta(\text{scale}) = \mu_R = m_H/2$

$\delta(\text{PDF-TH})$

$\delta(\text{EW})$

$\delta(t, b, c)$

$\delta(1/m_t)$

$\pm 0.56 \text{ pb}$

$\pm 0.49 \text{ pb}$

$\pm 0.40 \text{ pb}$

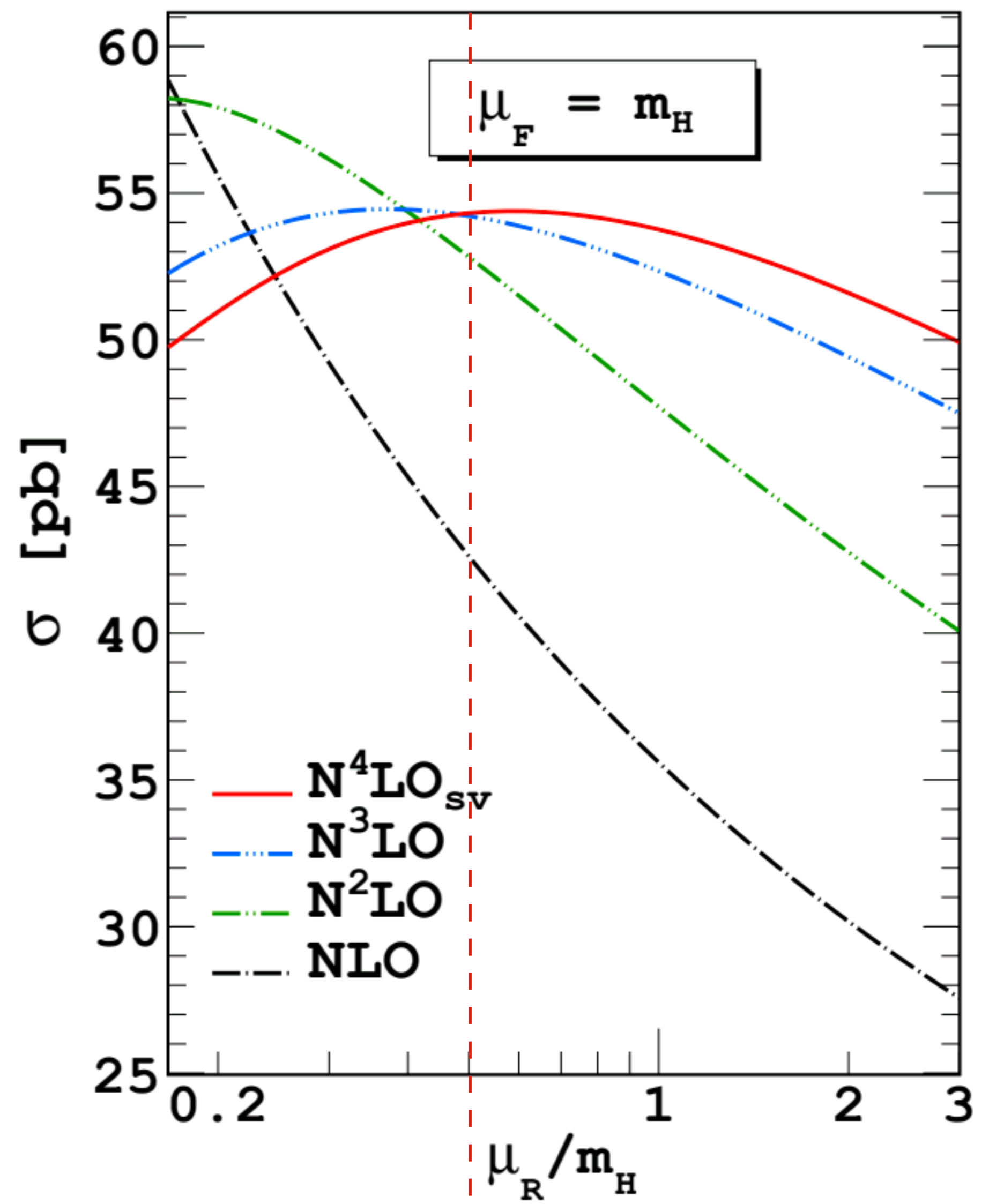
$\pm 0.49 \text{ pb}$

Approximate four-loop QCD corrections to the Higgs-boson production cross section

P3H-20-054

G. Das^{*a}, S. Moch^{†b} and A. Vogt^{‡c}

soft-virtual approximation



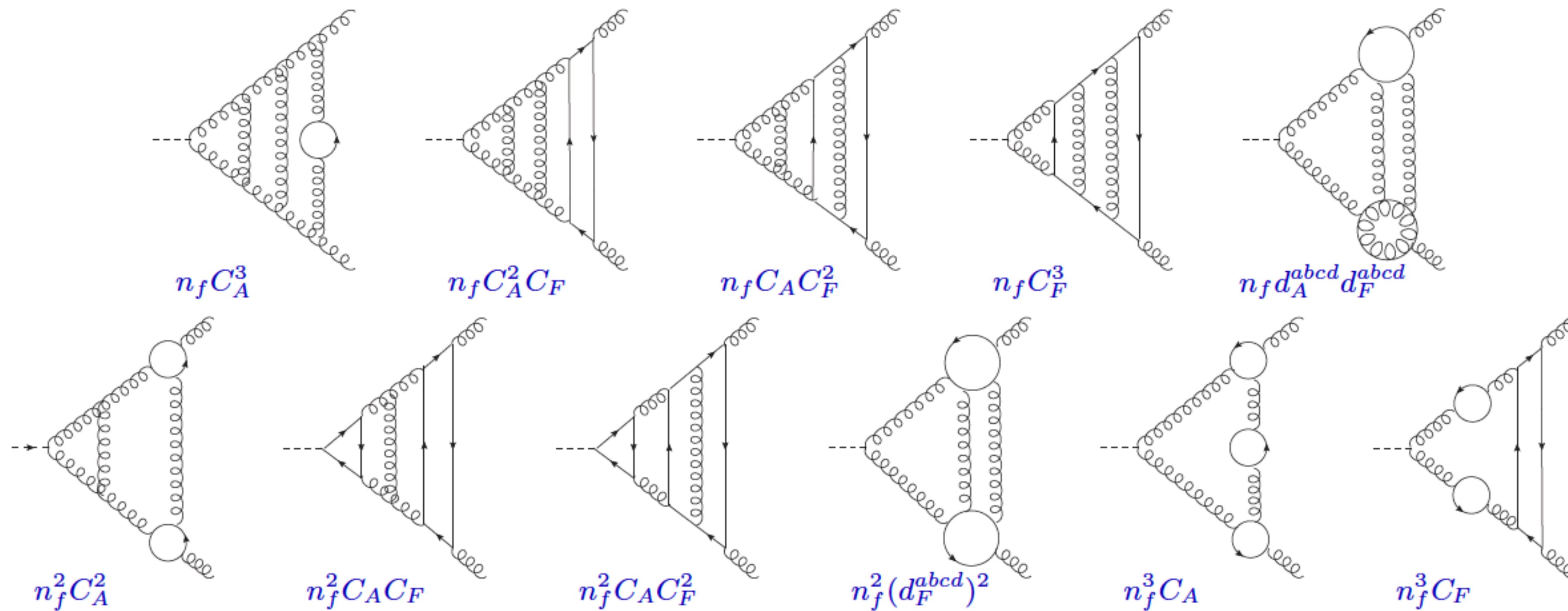
$$\left[\frac{\ln^k(1-x)}{1-x} \right]_+$$

$$k(1-x),$$

Fermionic corrections to quark and gluon form factors in four-loop QCD

Roman N. Lee,¹ Andreas von Manteuffel,² Robert M. Schabinger,²
Alexander V. Smirnov,³ Vladimir A. Smirnov,⁴ and Matthias Steinhauser⁵

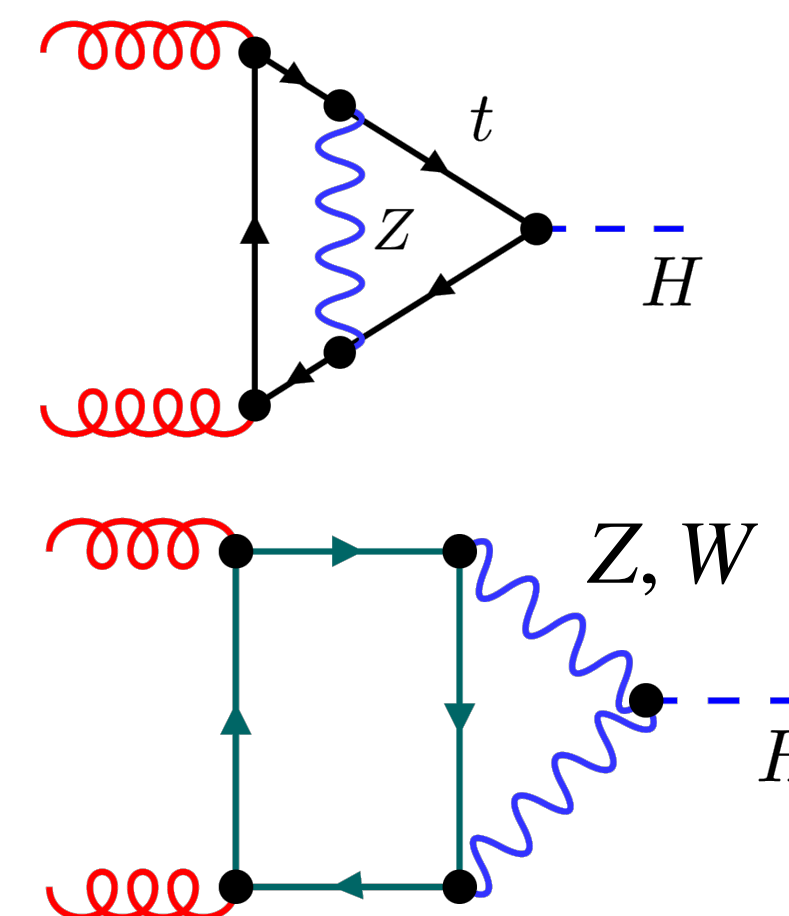
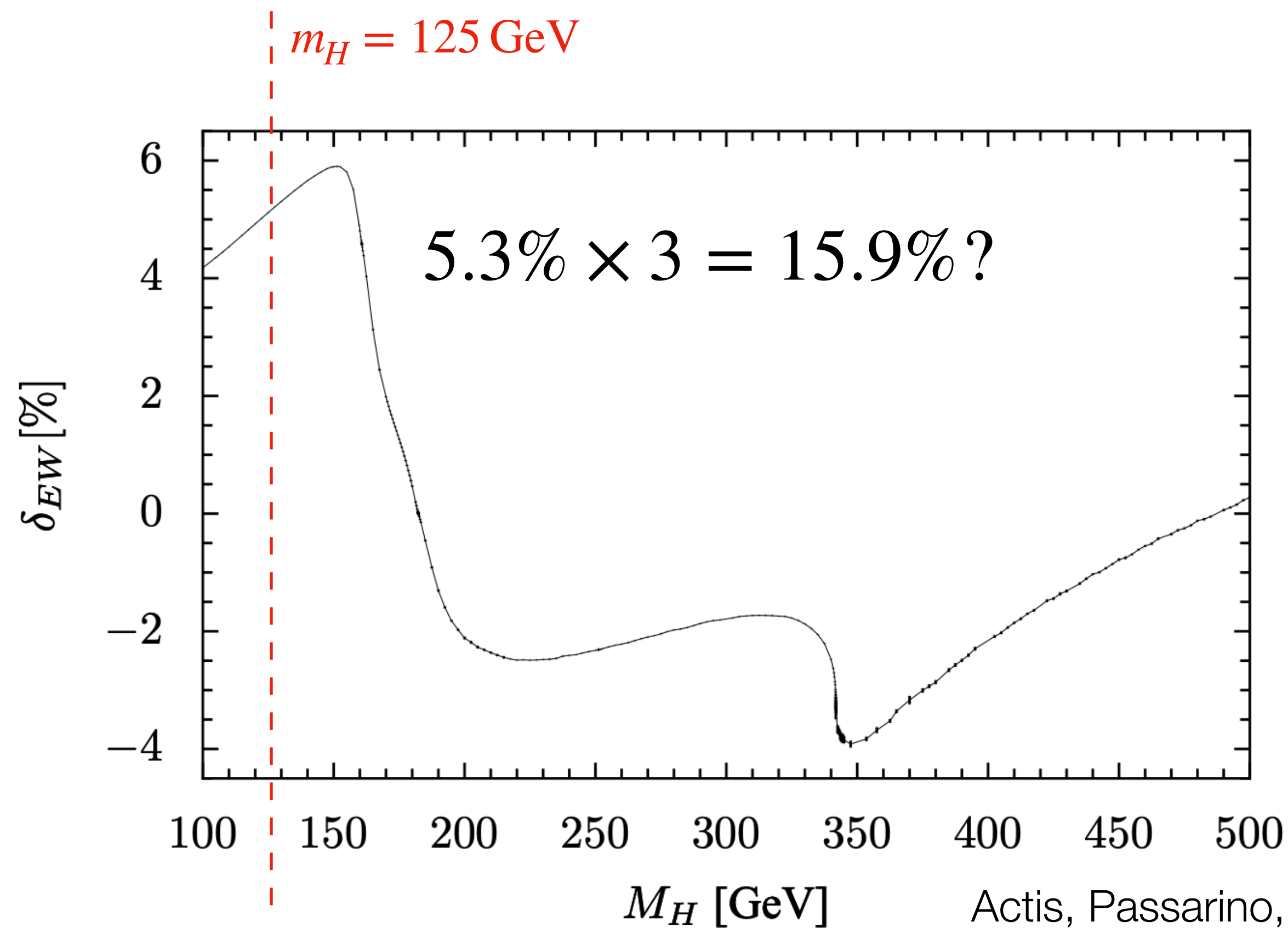
P3H-21-013



$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
$+0.10 \text{ pb}$ -1.15 pb	$\pm 0.18 \text{ pb}$	$\pm 0.56 \text{ pb}$	$\pm 0.49 \text{ pb}$	$\pm 0.40 \text{ pb}$	$\pm 0.49 \text{ pb}$
$+0.21\%$ -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$

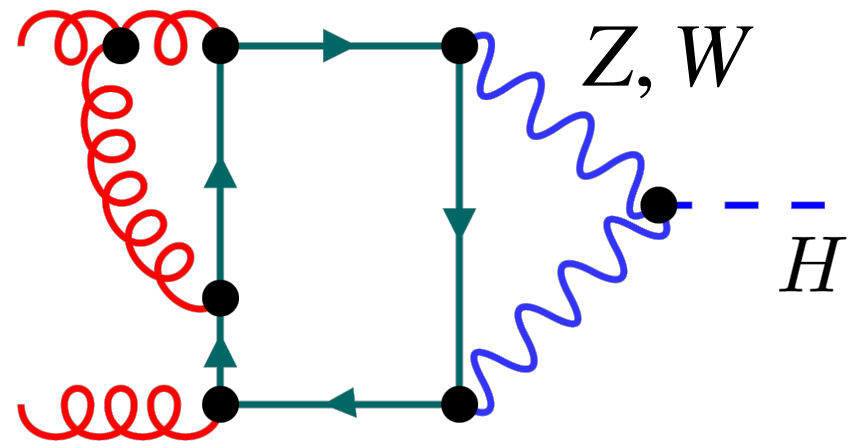
LHCHWG YR4 '16

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
+0.10 pb -1.15 pb	± 0.18 pb	± 0.56 pb	± 0.49 pb	± 0.40 pb	± 0.49 pb
+0.21% -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$



Actis, Passarino, Sturm, Uccirati '08

Mixed QCD/EW effects



Factorization hypothesis:

$$\sigma \sim C^2 \cdot \left| \begin{array}{c} \text{red curly line} \\ \text{blue dashed line} \end{array} + \dots \right|^2$$

$$C \sim (1 + \lambda_{\text{EW}}) \left(1 + a_s C_{\text{QCD}}^{(1)} + \dots \right) = 1 + \lambda_{\text{EW}} + a_s C_{\text{QCD}}^{(1)} + \lambda_{\text{EW}} a_s C_{\text{QCD}}^{(1)} + \dots$$

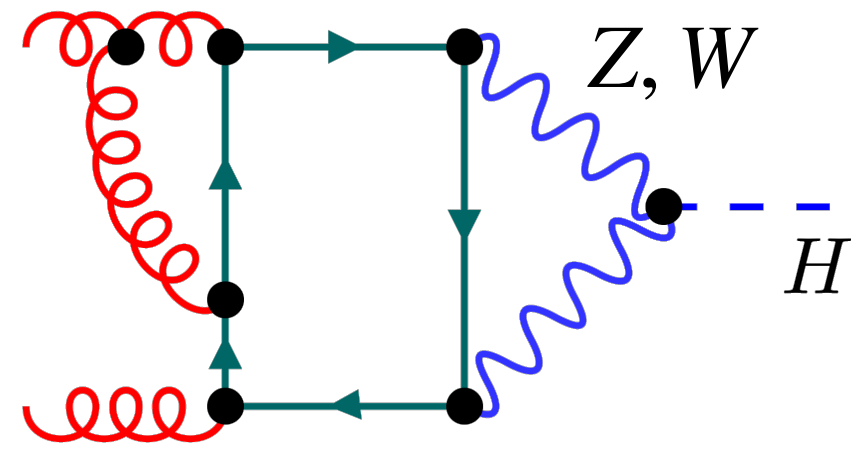
$\uparrow$ 0.026 $\uparrow$ $\frac{11}{4} = 2.75$

$$= 1 + \lambda_{\text{EW}} + a_s C_{\text{QCD}}^{(1)} + \lambda_{\text{EW}} a_s C_w^{(1)} + \dots$$

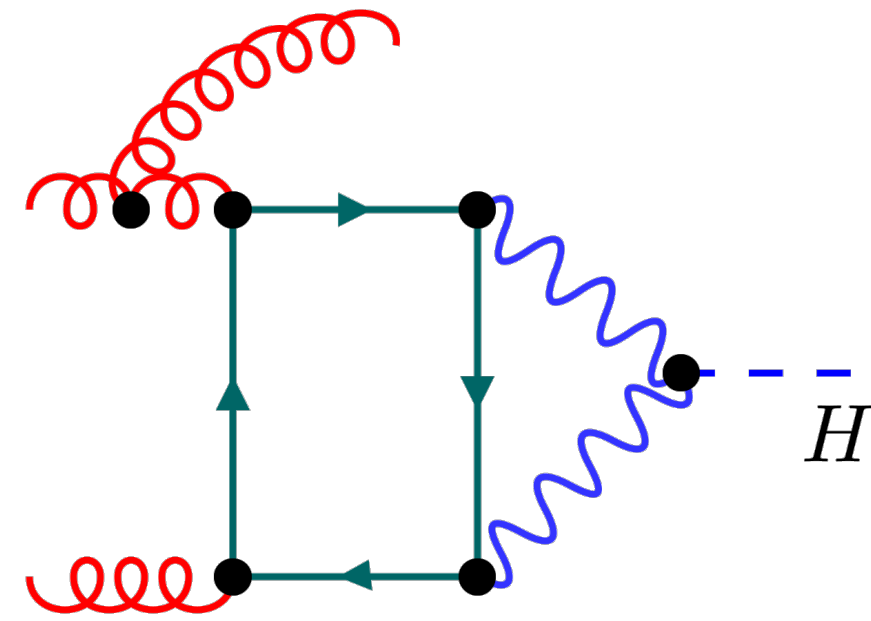
$$M_W, M_Z \gg M_H : \quad C_w^{(1)} = \frac{7}{6} \approx 1.17 \quad [\text{Anastasiou, Boughezal, Petriello '09}]$$

varying $C_w^{(1)}$: 1% uncertainty estimate

Mixed QCD/EW effects



complete



soft gluon

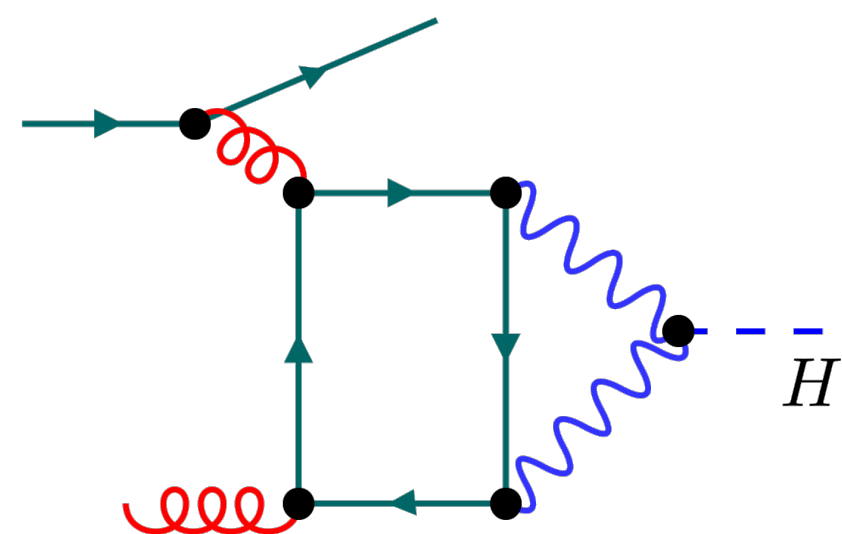
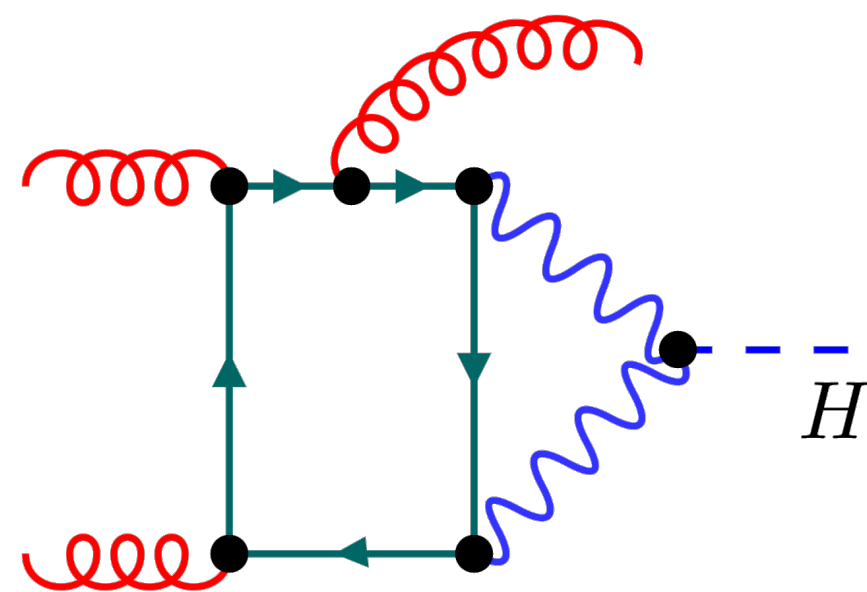
Bonetti, Melnikov, Tancredi '17

$$\lim_{E_4 \rightarrow 0} |A_{\text{NLO}}^{\text{real}}|^2 = \frac{\alpha_s}{4\pi} N_C \frac{2p_1 \cdot p_2}{p_1 \cdot p_4 p_2 \cdot p_4} |A_{\text{LO}}|^2 + \mathcal{O}(p_4^{-1}),$$

$\sigma_{\text{LO}}^{\text{QCD}} = 20.6 \text{ pb},$	$\sigma_{\text{LO}}^{\text{QCD-EW}} = 21.7 \text{ pb}$	$\Rightarrow$	$+5.3\%$	at LO
$\sigma_{\text{NLO}}^{\text{QCD}} = 32.7 \text{ pb},$	$\sigma_{\text{NLO}}^{\text{QCD-EW}} = 34.4 \text{ pb}$	$\Rightarrow$	$+5.2\%$	at NLO

Anastasiou, Del Duca, Furlan, Mistlberger, Moriello, Schweitzer, Specchia '18 $m_W, m_Z \rightarrow 0$

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
+0.10 pb -1.15 pb	± 0.18 pb	± 0.56 pb	± 0.49 pb	± 0.40 pb	± 0.49 pb
+0.21% -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$



missing

Two-loop mixed QCD-EW corrections to $gg \rightarrow Hg$

P3H-20-036

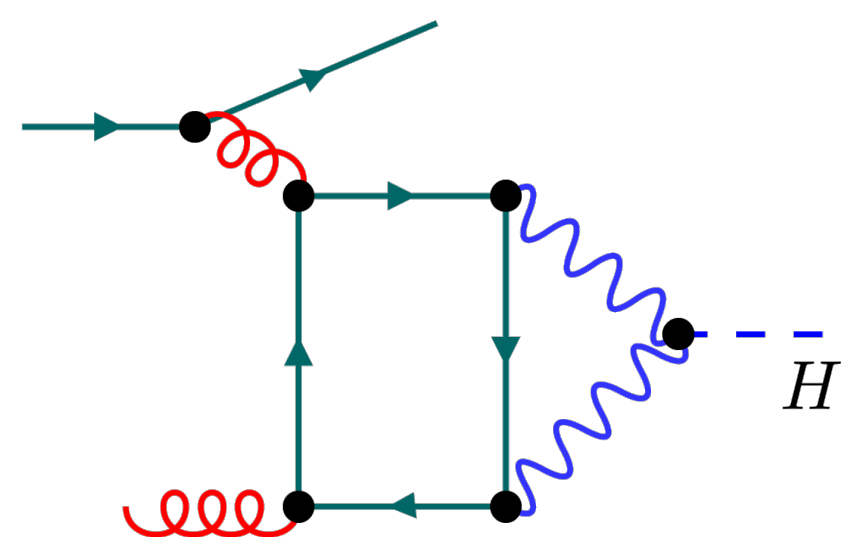
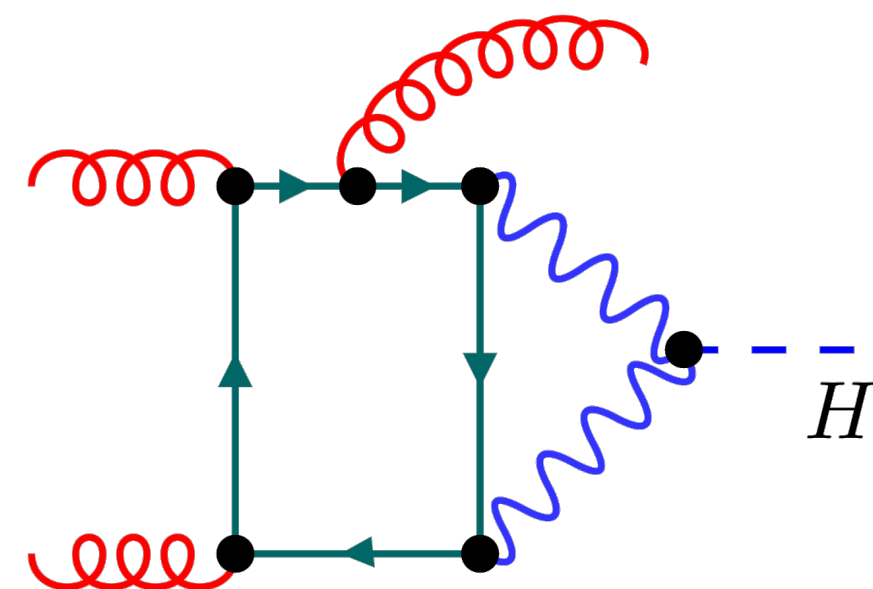
Marco Bonetti^{a,b} Erik Panzer^c Vladimir A. Smirnov^{d,e} Lorenzo Tancredi^f

^a*Institute for Theoretical Particle Physics, KIT,
Wolfgang-Gaede-Strasse 1, D-76128 Karlsruhe, Germany*

^b*Institute for Theoretical Particle Physics and Cosmology, RWTH Aachen University,
Sommerfeldstrasse 16, D-52056 Aachen, Germany*

also: Becchetti, Bonciani, Del Duca, Hirschi, Moriello '21
Hirschi, Lionetti, Schweitzer '19

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
+0.10 pb -1.15 pb	± 0.18 pb	± 0.56 pb	± 0.49 pb	± 0.40 pb	± 0.49 pb
+0.21% -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$



missing

Two-loop mixed QCD-EW corrections to $gg \rightarrow Hg$

P3H-20-036

Marco Bonetti^{a,b} Erik Panzer^c Vladimir A. Smirnov^{d,e} Lorenzo Tancredi^f

^a*Institute for Theoretical Particle Physics, KIT,
Wolfgang-Gaede-Strasse 1, D-76128 Karlsruhe, Germany*

^b*Institute for Theoretical Particle Physics and Cosmology, RWTH Aachen University,
Sommerfeldstrasse 16, D-52056 Aachen, Germany*

also: Becchetti, Bonciani, Del Duca, Hirschi, Moriello '21

Hirschi, Lionetti, Schweitzer '19

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
+0.10 pb -1.15 pb	± 0.18 pb	± 0.56 pb	± 0.49 pb	± 0.40 pb	± 0.49 pb
+0.21% -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$

LHCHWG YR4 '16

NNLO cross section with

NNLO PDFs

NLO PDFs

$$\frac{1}{2} \left| \frac{\sigma_{EFT}^{(2),NNLO} - \sigma_{EFT}^{(2),NLO}}{\sigma_{EFT}^{(2),NNLO}} \right| = \frac{1}{2} 2.31\% = 1.16\%$$

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
$+0.10 \text{ pb}$ -1.15 pb	$\pm 0.18 \text{ pb}$	$\pm 0.56 \text{ pb}$	$\pm 0.49 \text{ pb}$	$\pm 0.40 \text{ pb}$	$\pm 0.49 \text{ pb}$
$+0.21\%$ -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$

LHCHWG YR4 '16

$$\sigma_{\text{HEFT}}^{\text{HO}} = \sigma^{\text{LO}} \left(\frac{\sigma^{\text{HO}}}{\sigma^{\text{LO}}} \right)_{m_t \rightarrow \infty}$$

$$48.58 \text{ pb} =$$

16.00 pb	$(+32.9\%)$	(LO, rEFT)
$+ 20.84 \text{ pb}$	$(+42.9\%)$	(NLO, rEFT)
$- 2.05 \text{ pb}$	(-4.2%)	((t, b, c), exact NLO)
$+ 9.56 \text{ pb}$	$(+19.7\%)$	(NNLO, rEFT)
$+ 0.34 \text{ pb}$	$(+0.7\%)$	(NNLO, $1/m_t$)
$+ 2.40 \text{ pb}$	$(+4.9\%)$	(EW, QCD-EW)
$+ 1.49 \text{ pb}$	$(+3.1\%)$	(N ³ LO, rEFT)

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
$+0.10 \text{ pb}$ -1.15 pb	$\pm 0.18 \text{ pb}$	$\pm 0.56 \text{ pb}$	$\pm 0.49 \text{ pb}$	$\pm 0.40 \text{ pb}$	$\pm 0.49 \text{ pb}$
$+0.21\%$ -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$

NLO:

	α_s^2	α_s^3	Δm_t	
gg	$16.30 + 19.64$	$+0.0345$	$+0.2 \%$	$\rightarrow +0.1 \%$
qg		1.49	-0.3696	-24.8% $\rightarrow -1.0 \%$
qq		0.02	$+0.0322$	$+161 \%$ $\rightarrow +0.1 \%$
total	$16.30 + 21.15$	-0.3029	$+1.4 \%$	$\rightarrow -0.8 \%$

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
$+0.10 \text{ pb}$ -1.15 pb	$\pm 0.18 \text{ pb}$	$\pm 0.56 \text{ pb}$	$\pm 0.49 \text{ pb}$	$\pm 0.40 \text{ pb}$	$\pm 0.49 \text{ pb}$
$+0.21\%$ -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$

NNLO:

	α_s^2	α_s^3	α_s^4	
gg	$16.30 + 19.64 + 8.76$			$0.2\% \rightarrow 0.04\%$
qg	$1.49 + 0.84$			$24.8\% \rightarrow 0.4\%$
qq	$0.02 + 0.10$			$161\% \rightarrow 0.3\%$
total	$16.30 + 21.15 + 9.79$			$3.5\% \rightarrow 0.74\%$

$$\begin{array}{c}
 \mathcal{L}_{\text{SM}} \\
 \downarrow m_t \rightarrow \infty \\
 \mathcal{L}_{\text{eff}} = C_1(\alpha_s) \frac{H}{v} \text{Tr } G_{\mu\nu} G^{\mu\nu} + \mathcal{L}_{\text{QCD}}^{n_f=5}
 \end{array}$$

$$\begin{array}{c}
 \mathcal{L}_{\text{SM}} \\
 \downarrow m_t \rightarrow \infty \\
 \mathcal{L}_{\text{eff}} = C_1(\alpha_s) \frac{H}{v} \text{Tr } G_{\mu\nu} G^{\mu\nu} + \mathcal{L}_{\text{QCD}}^{n_f=5}
 \end{array}$$

higher orders in $1/m_t$:
need higher dimensional operators

$$\begin{array}{c}
 \mathcal{L}_{\text{SM}} \\
 \downarrow m_t \rightarrow \infty \\
 \mathcal{L}_{\text{eff}} = C_1(\alpha_s) \frac{H}{v} \text{Tr} G_{\mu\nu} G^{\mu\nu} + \mathcal{L}_{\text{QCD}}^{n_f=5}
 \end{array}$$

higher orders in $1/m_t$:
 need higher dimensional operators

$$C_2(\alpha_s) \left\langle \frac{H}{v} \text{Tr} G_{\mu\nu} G^{\mu\rho} G_{\rho}^{\nu} \right\rangle$$

$$\underline{\text{dim } 6 \text{ (0 + 1)}}$$

$$\mathcal{O}''_{6;1} = \frac{1}{3} \text{Tr}(F_{12} F_{13} F_{23}) . \quad (\text{B.1})$$

$$\underline{\text{dim } 8 \text{ (1 + 1)}}$$

$$\mathcal{O}''_{8;1} = \text{Tr}(D_1 F_{23} D_4 F_{23} F_{14}); \quad \mathcal{O}''_{8;2} = \text{Tr}(D_1 F_{23} D_1 F_{24} F_{34}) . \quad (\text{B.2})$$

$$\underline{\text{dim } 10 \text{ (3 + 2)}}$$

$$\mathcal{O}''_{10;1} = \text{Tr}(D_{12} F_{34} D_{15} F_{34} F_{25}), \quad \mathcal{O}''_{10;2} = \text{Tr}(D_{12} F_{34} D_5 F_{34} D_1 F_{25}), \quad \mathcal{O}''_{10;3} = \text{Tr}(D_2 F_{34} D_{15} F_{34} D_1 F_{25});$$

$$\mathcal{O}''_{10;4} = \text{Tr}(D_{12} F_{34} D_1 F_{35} D_2 F_{45}), \quad \mathcal{O}''_{10;5} = \text{Tr}(D_{12} F_{34} D_{12} F_{35} F_{45}) . \quad (\text{B.3})$$

$$\underline{\text{dim } 12 \text{ (6 + 4)}}$$

$$\mathcal{O}''_{12;1} = \text{Tr}(D_{123} F_{45} D_{126} F_{45} F_{36}), \quad \mathcal{O}''_{12;2} = \text{Tr}(D_{123} F_{45} D_{16} F_{45} D_2 F_{36}), \quad \mathcal{O}''_{12;3} = \text{Tr}(D_{13} F_{45} D_{126} F_{45} D_2 F_{36}),$$

$$\mathcal{O}''_{12;4} = \text{Tr}(D_{123} F_{45} D_6 F_{45} D_{12} F_{36}), \quad \mathcal{O}''_{12;5} = \text{Tr}(D_{13} F_{45} D_{26} F_{45} D_{12} F_{36}), \quad \mathcal{O}''_{12;6} = \text{Tr}(D_3 F_{45} D_{126} F_{45} D_{12} F_{36});$$

$$\mathcal{O}''_{12;7} = \text{Tr}(D_{12} F_{45} D_{13} F_{46} D_{23} F_{56}), \quad \mathcal{O}''_{12;8} = \text{Tr}(D_{12} F_{45} D_{123} F_{46} D_3 F_{56}), \quad \mathcal{O}''_{12;9} = \text{Tr}(D_{123} F_{45} D_{12} F_{46} D_3 F_{56}),$$

$$\mathcal{O}''_{12;10} = \text{Tr}(D_{123} F_{45} D_{123} F_{46} F_{56}) . \quad (\text{B.4})$$

$$\underline{\text{dim } 14 \text{ (10 + 5)}}$$

$$\mathcal{O}''_{14;1} = \text{Tr}(D_{1234} F_{56} D_{1237} F_{56} F_{47}), \quad \mathcal{O}''_{14;2} = \text{Tr}(D_{1234} F_{56} D_{127} F_{56} D_3 F_{47}), \quad \mathcal{O}''_{14;3} = \text{Tr}(D_{124} F_{56} D_{1237} F_{56} D_3 F_{47}),$$

$$\mathcal{O}''_{14;4} = \text{Tr}(D_{1234} F_{56} D_{17} F_{56} D_{23} F_{47}), \quad \mathcal{O}''_{14;5} = \text{Tr}(D_{124} F_{56} D_{137} F_{56} D_{23} F_{47}), \quad \mathcal{O}''_{14;6} = \text{Tr}(D_{14} F_{56} D_{1237} F_{56} D_{23} F_{47})$$

$$\mathcal{O}''_{14;7} = \text{Tr}(D_{1234} F_{56} D_7 F_{56} D_{123} F_{47}), \quad \mathcal{O}''_{14;8} = \text{Tr}(D_{124} F_{56} D_{37} F_{56} D_{123} F_{47}), \quad \mathcal{O}''_{14;9} = \text{Tr}(D_{14} F_{56} D_{237} F_{56} D_{123} F_{47}),$$

$$\mathcal{O}''_{14;10} = \text{Tr}(D_4 F_{56} D_{1237} F_{56} D_{123} F_{47});$$

$$\mathcal{O}''_{14;11} = \text{Tr}(D_{123} F_{56} D_{124} F_{57} D_{34} F_{67}), \quad \mathcal{O}''_{14;12} = \text{Tr}(D_{1234} F_{56} D_{12} F_{57} D_{34} F_{67}), \quad \mathcal{O}''_{14;13} = \text{Tr}(D_{123} F_{56} D_{1234} F_{57} D_4 F_{67}),$$

$$\mathcal{O}''_{14;14} = \text{Tr}(D_{1234} F_{56} D_{123} F_{57} D_4 F_{67}), \quad \mathcal{O}''_{14;15} = \text{Tr}(D_{1234} F_{56} D_{1234} F_{57} F_{67}) . \quad (\text{B.5})$$

$$\underline{\text{dim } 16 \text{ (15 + 7)}}$$

$$\mathcal{O}''_{16;1} = \text{Tr}(D_{12345} F_{67} D_{12348} F_{67} F_{58}), \quad \mathcal{O}''_{16;2} = \text{Tr}(D_{12345} F_{67} D_{1238} F_{67} D_4 F_{58}), \quad \mathcal{O}''_{16;3} = \text{Tr}(D_{1235} F_{67} D_{12348} F_{67} D_4 F_{58}),$$

$$\mathcal{O}''_{16;4} = \text{Tr}(D_{12345} F_{67} D_{128} F_{67} D_{34} F_{58}), \quad \mathcal{O}''_{16;5} = \text{Tr}(D_{1235} F_{67} D_{1248} F_{67} D_{34} F_{58}), \quad \mathcal{O}''_{16;6} = \text{Tr}(D_{125} F_{67} D_{12348} F_{67} D_{34} F_{58})$$

$$\mathcal{O}''_{16;7} = \text{Tr}(D_{12345} F_{67} D_{18} F_{67} D_{234} F_{58}), \quad \mathcal{O}''_{16;8} = \text{Tr}(D_{1235} F_{67} D_{148} F_{67} D_{234} F_{58}), \quad \mathcal{O}''_{16;9} = \text{Tr}(D_{125} F_{67} D_{1348} F_{67} D_{234} F_{58}),$$

$$\mathcal{O}''_{16;10} = \text{Tr}(D_{15} F_{67} D_{12348} F_{67} D_{234} F_{58}), \quad \mathcal{O}''_{16;11} = \text{Tr}(D_{12345} F_{67} D_8 F_{67} D_{1234} F_{58}), \quad \mathcal{O}''_{16;12} = \text{Tr}(D_{1235} F_{67} D_{48} F_{67} D_{1234} F_{58}),$$

$$\mathcal{O}''_{16;13} = \text{Tr}(D_{125} F_{67} D_{348} F_{67} D_{1234} F_{58}), \quad \mathcal{O}''_{16;14} = \text{Tr}(D_{15} F_{67} D_{2348} F_{67} D_{1234} F_{58}), \quad \mathcal{O}''_{16;15} = \text{Tr}(D_5 F_{67} D_{12348} F_{67} D_{1234} F_{58});$$

$$\mathcal{O}''_{16;16} = \text{Tr}(D_{1234} F_{67} D_{125} F_{68} D_{345} F_{78}), \quad \mathcal{O}''_{16;17} = \text{Tr}(D_{123} F_{67} D_{12345} F_{68} D_{45} F_{78}), \quad \mathcal{O}''_{16;18} = \text{Tr}(D_{1234} F_{67} D_{1235} F_{68} D_{45} F_{78}),$$

$$\mathcal{O}''_{16;19} = \text{Tr}(D_{12345} F_{67} D_{123} F_{68} D_{45} F_{78}), \quad \mathcal{O}''_{16;20} = \text{Tr}(D_{1234} F_{67} D_{12345} F_{68} D_5 F_{78}), \quad \mathcal{O}''_{16;21} = \text{Tr}(D_{12345} F_{67} D_{1234} F_{68} D_5 F_{78}),$$

$$\mathcal{O}''_{16;22} = \text{Tr}(D_{12345} F_{67} D_{12345} F_{68} F_{78}) . \quad (\text{B.6})$$

Jin, Ren, Yang '21

$$\begin{aligned} &\underline{\text{dim } 6 \text{ (0 + 1)}} \\ \mathcal{O}''_{6;1} &= \frac{1}{3} \text{Tr}(F_{12} F_{13} F_{23}) . \end{aligned} \tag{B.1}$$

$$\begin{aligned} &\underline{\text{dim } 8 \text{ (1 + 1)}} \\ \mathcal{O}''_{8;1} &= \text{Tr}(D_1 F_{23} D_4 F_{23} F_{14}); \quad \mathcal{O}''_{8;2} = \text{Tr}(D_1 F_{23} D_1 F_{24} F_{34}) . \end{aligned} \tag{B.2}$$

$$\begin{aligned} &\underline{\text{dim } 10 \text{ (3 + 2)}} \\ \mathcal{O}''_{10;1} &= \text{Tr}(D_{12} F_{34} D_{15} F_{34} F_{25}), \quad \mathcal{O}''_{10;2} = \text{Tr}(D_{12} F_{34} D_5 F_{34} D_1 F_{25}), \quad \mathcal{O}''_{10;3} = \text{Tr}(D_2 F_{34} D_{15} F_{34} D_1 F_{25}); \\ \mathcal{O}''_{10;4} &= \text{Tr}(D_{12} F_{34} D_1 F_{35} D_2 F_{45}), \quad \mathcal{O}''_{10;5} = \text{Tr}(D_{12} F_{34} D_{12} F_{35} F_{45}) . \end{aligned} \tag{B.3}$$

$$\begin{aligned} &\underline{\text{dim } 12 \text{ (6 + 4)}} \\ \mathcal{O}''_{12;1} &= \text{Tr}(D_{123} F_{45} D_{126} F_{45} F_{36}), \quad \mathcal{O}''_{12;2} = \text{Tr}(D_{123} F_{45} D_{16} F_{45} D_2 F_{36}), \quad \mathcal{O}''_{12;3} = \text{Tr}(D_{13} F_{45} D_{126} F_{45} D_2 F_{36}), \\ \mathcal{O}''_{12;4} &= \text{Tr}(D_{123} F_{45} D_6 F_{45} D_{12} F_{36}), \quad \mathcal{O}''_{12;5} = \text{Tr}(D_{13} F_{45} D_{26} F_{45} D_{12} F_{36}), \quad \mathcal{O}''_{12;6} = \text{Tr}(D_3 F_{45} D_{126} F_{45} D_{12} F_{36}); \\ \mathcal{O}''_{12;7} &= \text{Tr}(D_{12} F_{45} D_{13} F_{46} D_{23} F_{56}), \quad \mathcal{O}''_{12;8} = \text{Tr}(D_{12} F_{45} D_{123} F_{46} D_3 F_{56}), \quad \mathcal{O}''_{12;9} = \text{Tr}(D_{123} F_{45} D_{12} F_{46} D_3 F_{56}), \\ \mathcal{O}''_{12;10} &= \text{Tr}(D_{123} F_{45} D_{123} F_{46} F_{56}) . \end{aligned} \tag{B.4}$$

$$\begin{aligned} &\underline{\text{dim } 14 \text{ (10 + 5)}} \\ \mathcal{O}''_{14;1} &= \text{Tr}(D_{1234} F_{56} D_{1237} F_{56} F_{47}), \quad \mathcal{O}''_{14;2} = \text{Tr}(D_{1234} F_{56} D_{127} F_{56} D_3 F_{47}), \quad \mathcal{O}''_{14;3} = \text{Tr}(D_{124} F_{56} D_{1237} F_{56} D_3 F_{47}), \\ \mathcal{O}''_{14;4} &= \text{Tr}(D_{1234} F_{56} D_{17} F_{56} D_{23} F_{47}), \quad \mathcal{O}''_{14;5} = \text{Tr}(D_{124} F_{56} D_{137} F_{56} D_{23} F_{47}), \quad \mathcal{O}''_{14;6} = \text{Tr}(D_{14} F_{56} D_{1237} F_{56} D_{23} F_{47}) \\ \mathcal{O}''_{14;7} &= \text{Tr}(D_{1234} F_{56} D_7 F_{56} D_{123} F_{47}), \quad \mathcal{O}''_{14;8} = \text{Tr}(D_{124} F_{56} D_{37} F_{56} D_{123} F_{47}), \quad \mathcal{O}''_{14;9} = \text{Tr}(D_{14} F_{56} D_{237} F_{56} D_{123} F_{47}), \\ \mathcal{O}''_{14;10} &= \text{Tr}(D_4 F_{56} D_{1237} F_{56} D_{123} F_{47}); \\ \mathcal{O}''_{14;11} &= \text{Tr}(D_{123} F_{56} D_{124} F_{57} D_{34} F_{67}), \quad \mathcal{O}''_{14;12} = \text{Tr}(D_{1234} F_{56} D_{12} F_{57} D_{34} F_{67}), \quad \mathcal{O}''_{14;13} = \text{Tr}(D_{123} F_{56} D_{1234} F_{57} D_4 F_{67}), \\ \mathcal{O}''_{14;14} &= \text{Tr}(D_{1234} F_{56} D_{123} F_{57} D_4 F_{67}), \quad \mathcal{O}''_{14;15} = \text{Tr}(D_{1234} F_{56} D_{1234} F_{57} F_{67}) . \end{aligned} \tag{B.5}$$

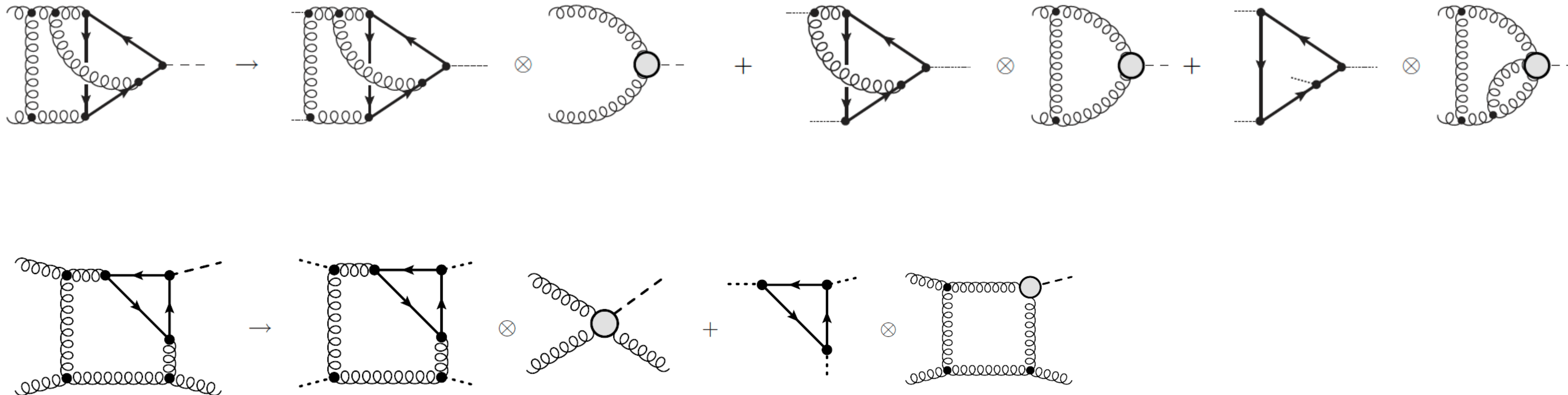
$$\begin{aligned} &\underline{\text{dim } 16 \text{ (15 + 7)}} \\ \mathcal{O}''_{16;1} &= \text{Tr}(D_{12345} F_{67} D_{12348} F_{67} F_{58}), \quad \mathcal{O}''_{16;2} = \text{Tr}(D_{12345} F_{67} D_{1238} F_{67} D_4 F_{58}), \quad \mathcal{O}''_{16;3} = \text{Tr}(D_{1235} F_{67} D_{12348} F_{67} D_4 F_{58}), \\ \mathcal{O}''_{16;4} &= \text{Tr}(D_{12345} F_{67} D_{128} F_{67} D_{34} F_{58}), \quad \mathcal{O}''_{16;5} = \text{Tr}(D_{1235} F_{67} D_{1248} F_{67} D_{34} F_{58}), \quad \mathcal{O}''_{16;6} = \text{Tr}(D_{125} F_{67} D_{12348} F_{67} D_{34} F_{58}) \\ \mathcal{O}''_{16;7} &= \text{Tr}(D_{12345} F_{67} D_{18} F_{67} D_{234} F_{58}), \quad \mathcal{O}''_{16;8} = \text{Tr}(D_{1235} F_{67} D_{148} F_{67} D_{234} F_{58}), \quad \mathcal{O}''_{16;9} = \text{Tr}(D_{125} F_{67} D_{1348} F_{67} D_{234} F_{58}), \\ \mathcal{O}''_{16;10} &= \text{Tr}(D_{15} F_{67} D_{12348} F_{67} D_{234} F_{58}), \quad \mathcal{O}''_{16;11} = \text{Tr}(D_{12345} F_{67} D_8 F_{67} D_{1234} F_{58}), \quad \mathcal{O}''_{16;12} = \text{Tr}(D_{1235} F_{67} D_{48} F_{67} D_{1234} F_{58}), \\ \mathcal{O}''_{16;13} &= \text{Tr}(D_{125} F_{67} D_{348} F_{67} D_{1234} F_{58}), \quad \mathcal{O}''_{16;14} = \text{Tr}(D_{15} F_{67} D_{2348} F_{67} D_{1234} F_{58}), \quad \mathcal{O}''_{16;15} = \text{Tr}(D_5 F_{67} D_{12348} F_{67} D_{1234} F_{58}); \\ \mathcal{O}''_{16;16} &= \text{Tr}(D_{1234} F_{67} D_{125} F_{68} D_{345} F_{78}), \quad \mathcal{O}''_{16;17} = \text{Tr}(D_{123} F_{67} D_{12345} F_{68} D_{45} F_{78}), \quad \mathcal{O}''_{16;18} = \text{Tr}(D_{1234} F_{67} D_{1235} F_{68} D_{45} F_{78}), \\ \mathcal{O}''_{16;19} &= \text{Tr}(D_{12345} F_{67} D_{123} F_{68} D_{45} F_{78}), \quad \mathcal{O}''_{16;20} = \text{Tr}(D_{1234} F_{67} D_{12345} F_{68} D_5 F_{78}), \quad \mathcal{O}''_{16;21} = \text{Tr}(D_{12345} F_{67} D_{1234} F_{68} D_5 F_{78}), \\ \mathcal{O}''_{16;22} &= \text{Tr}(D_{12345} F_{67} D_{12345} F_{68} F_{78}) . \end{aligned} \tag{B.6}$$

Instead: asymptotic expansions

Jin, Ren, Yang ‘21

Asymptotic expansions

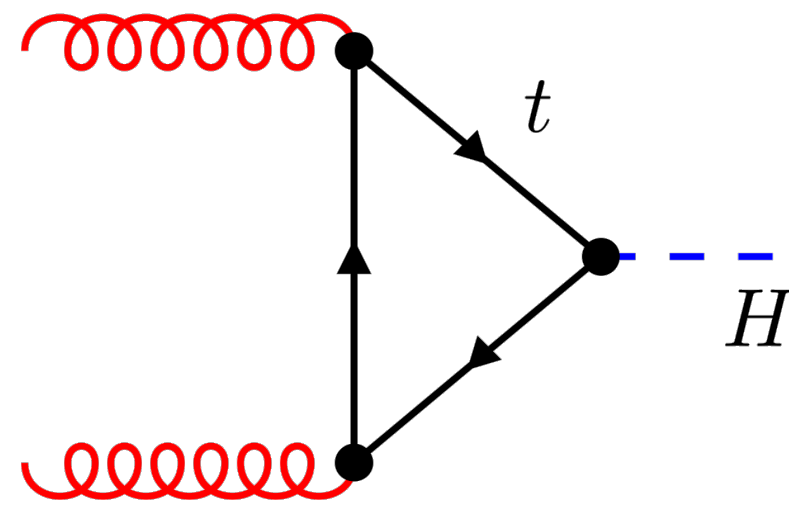
Calculating Wilson coefficient and matrix element “at once”:



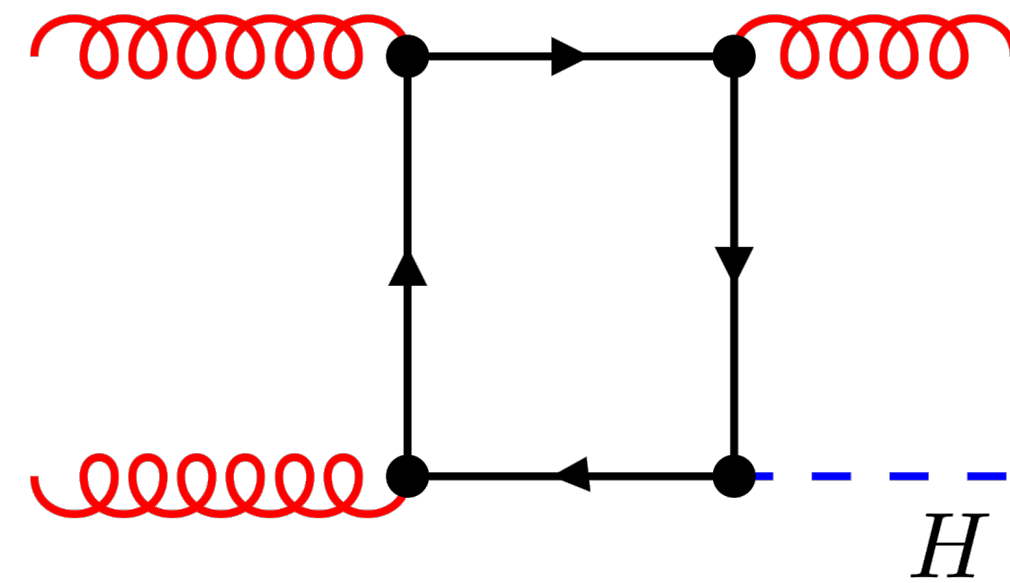
RH, Ozeren '09

Pak, Regal, Steinhauser '09

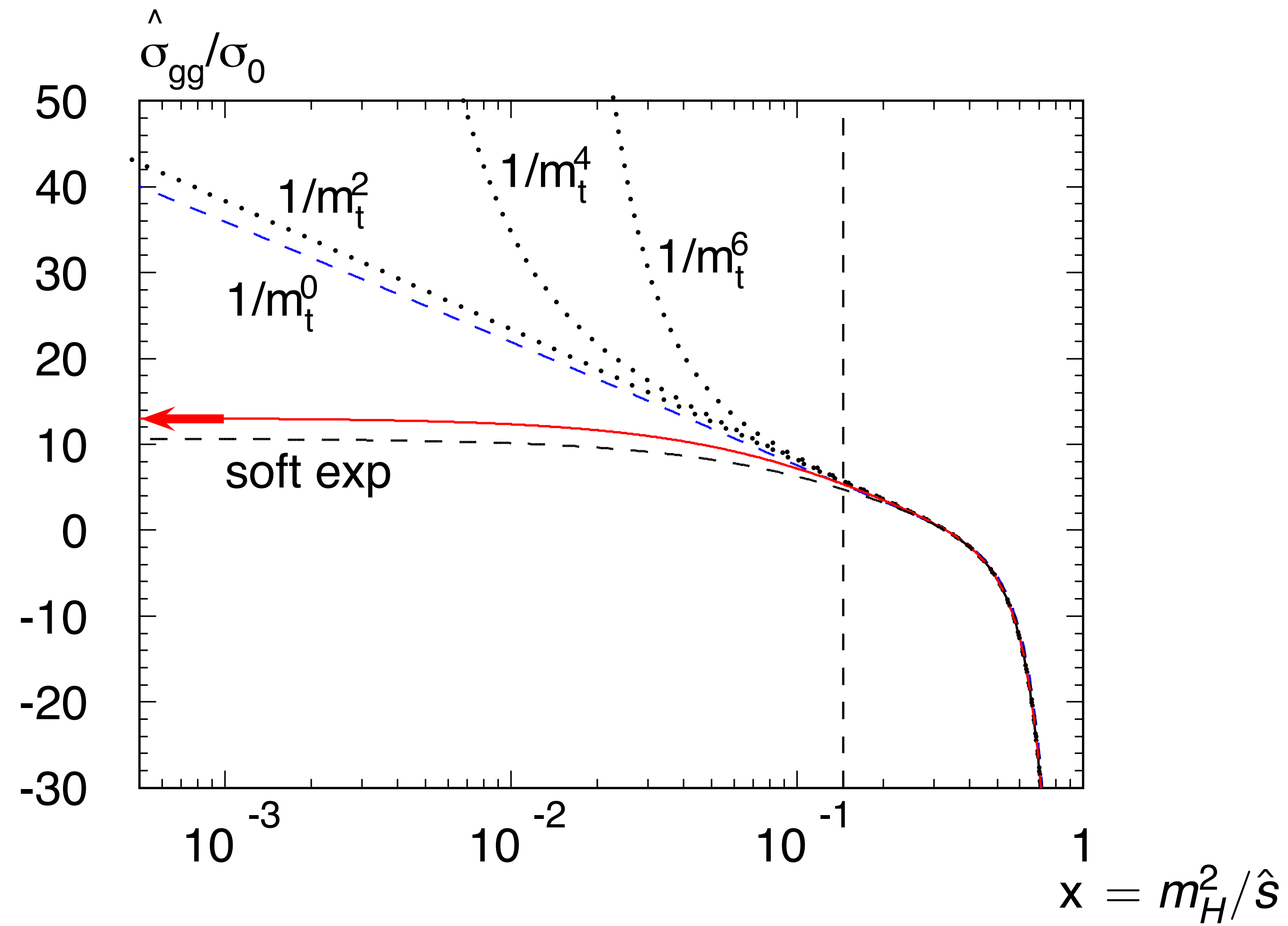
problem:



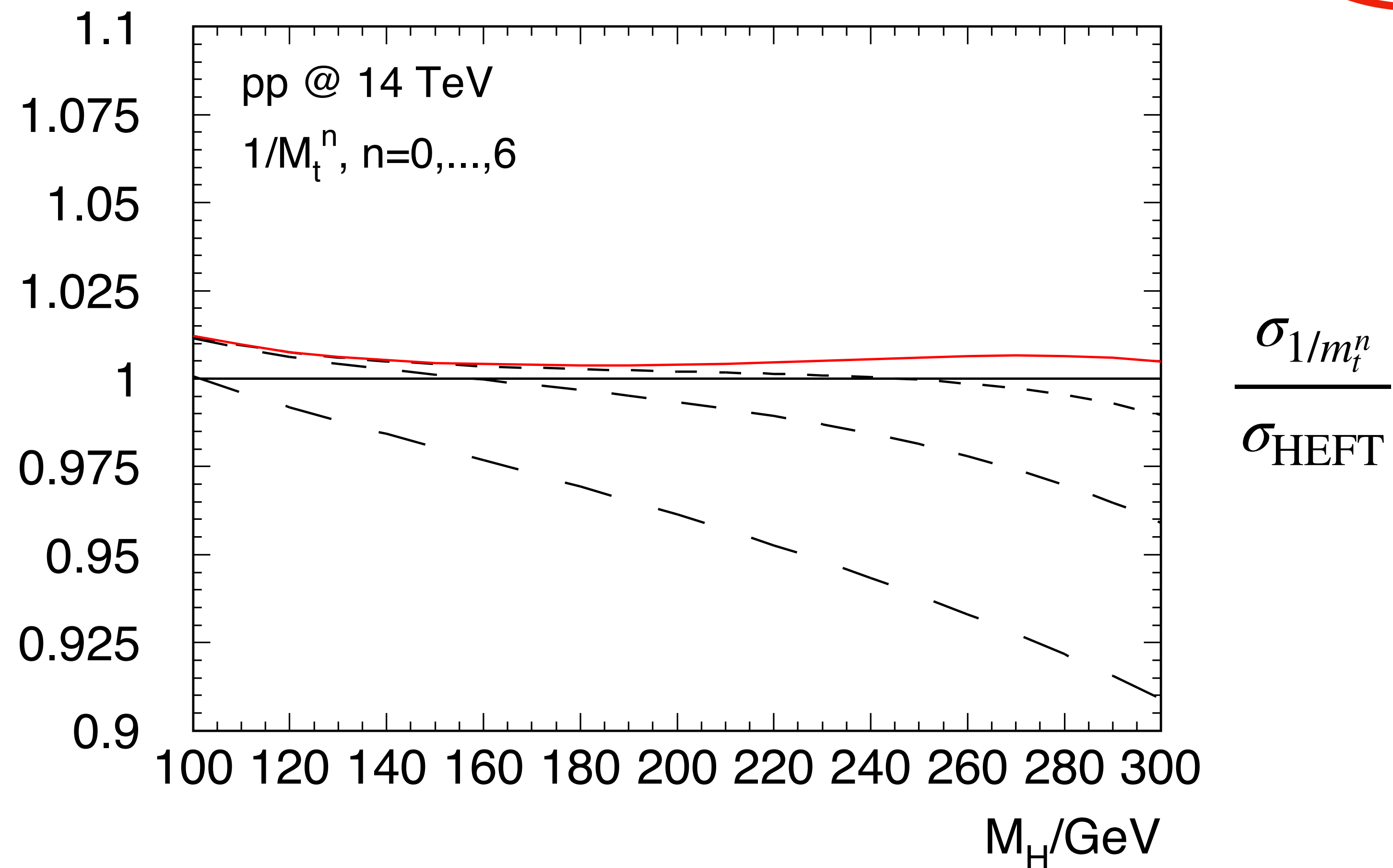
$$\hat{s} = m_H^2 < 4m_t^2$$



$$m_H^2 < \hat{s} < s < 13 \text{ TeV}$$



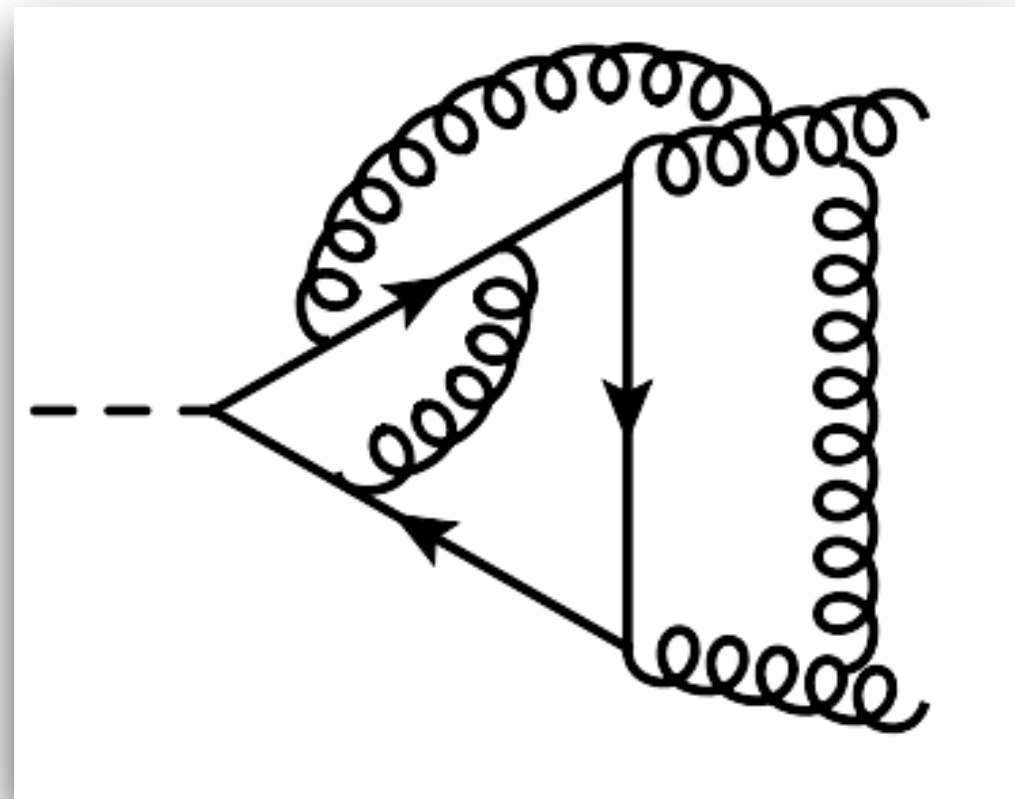
$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
$+0.10 \text{ pb}$ -1.15 pb	$\pm 0.18 \text{ pb}$	$\pm 0.56 \text{ pb}$	$\pm 0.49 \text{ pb}$	$\pm 0.40 \text{ pb}$	$\pm 0.49 \text{ pb}$
$+0.21\%$ -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$



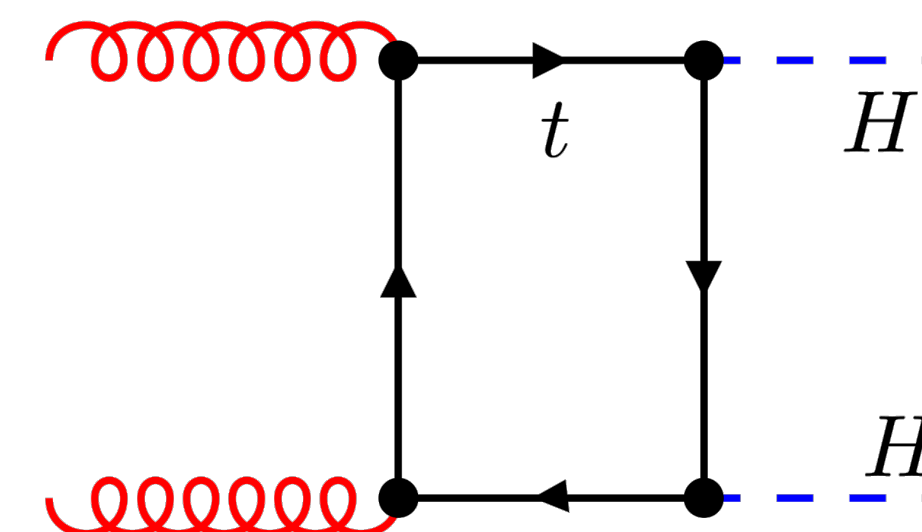
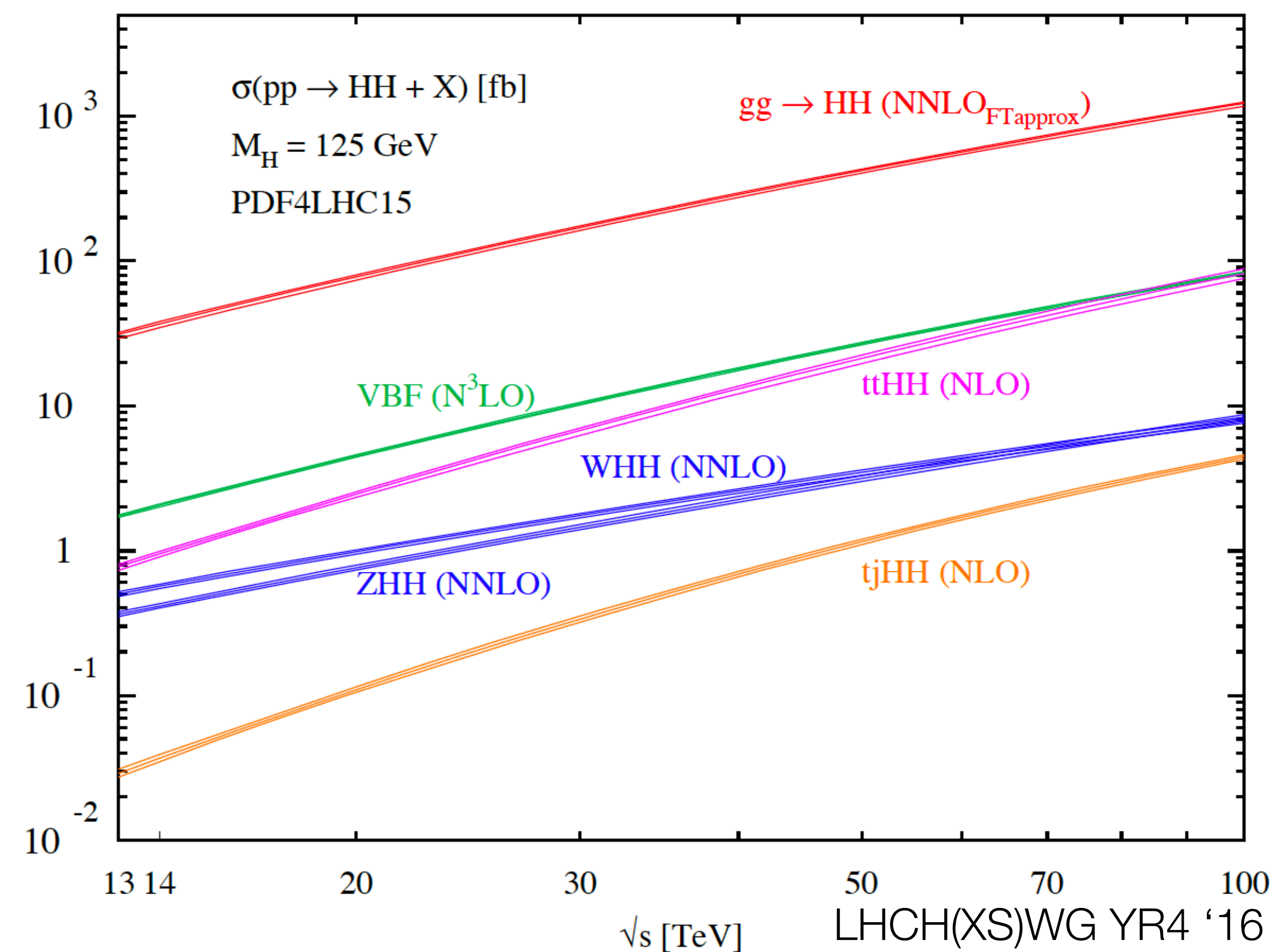
Top Quark Mass Effects in Next-To-Next-To-Next-To-Leading Order Higgs Boson Production: Virtual Corrections

P3H-19-045

Joshua Davies,^{1,*} Florian Herren,^{1,†} and Matthias Steinhauser^{1,‡}

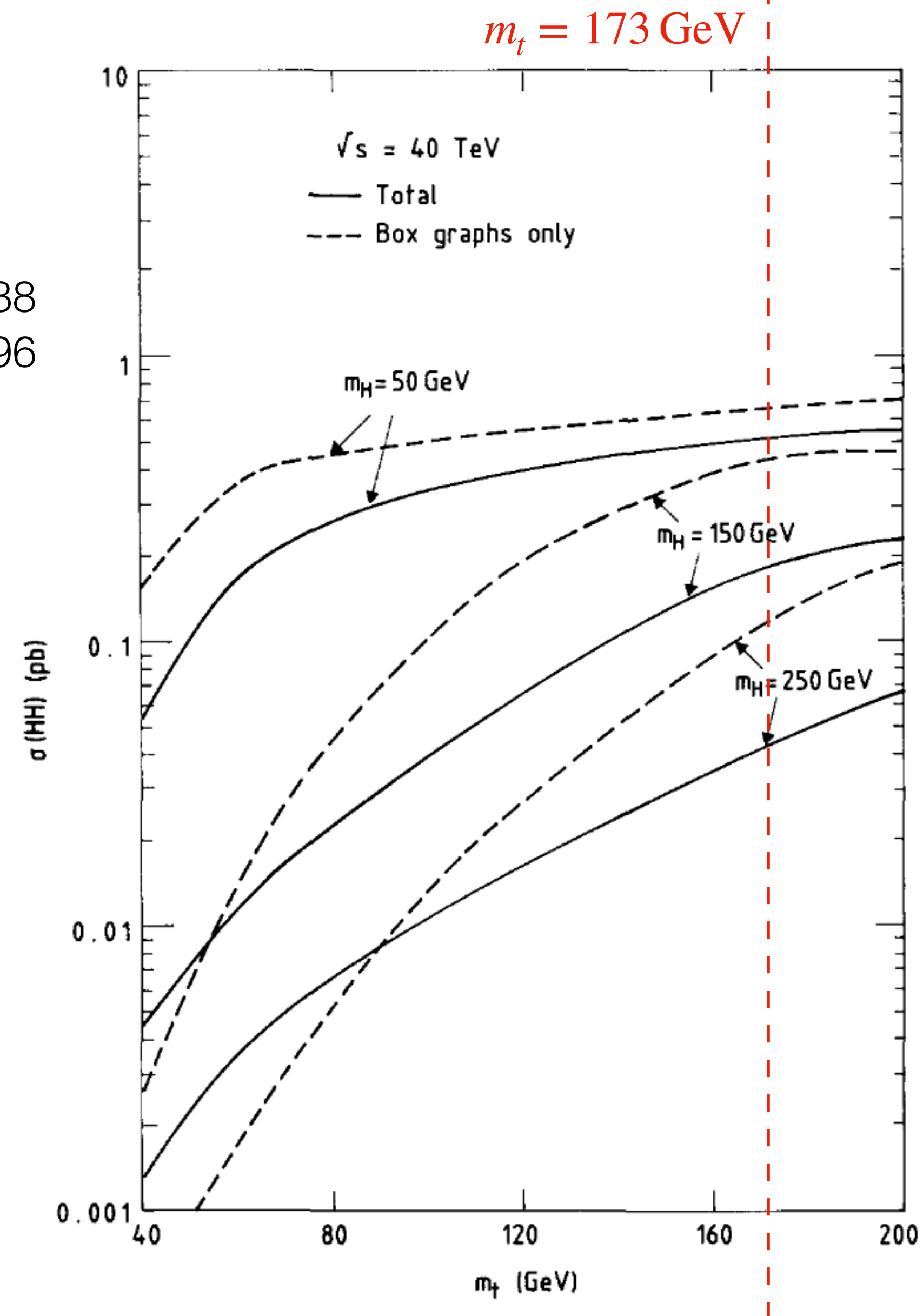
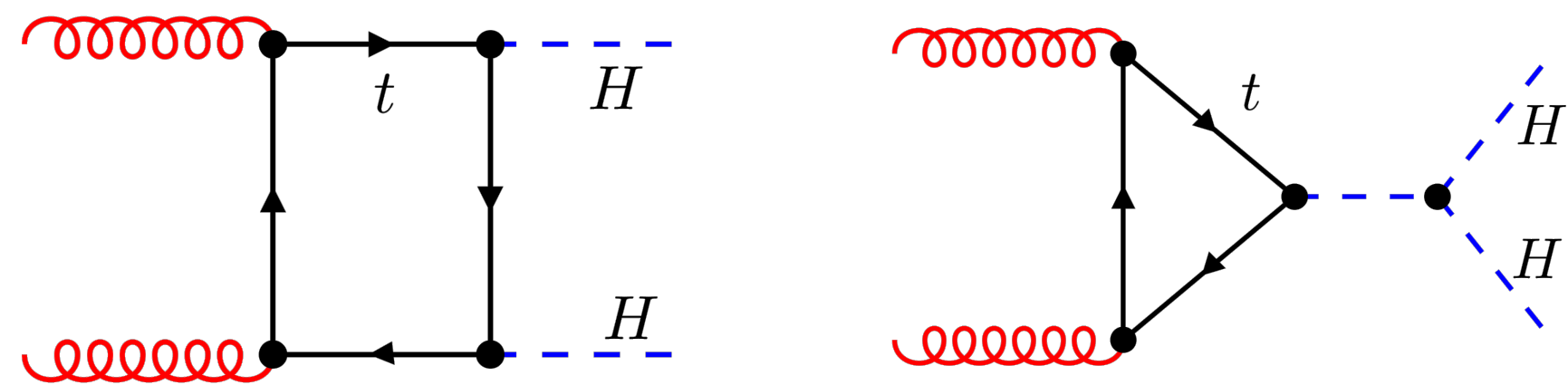


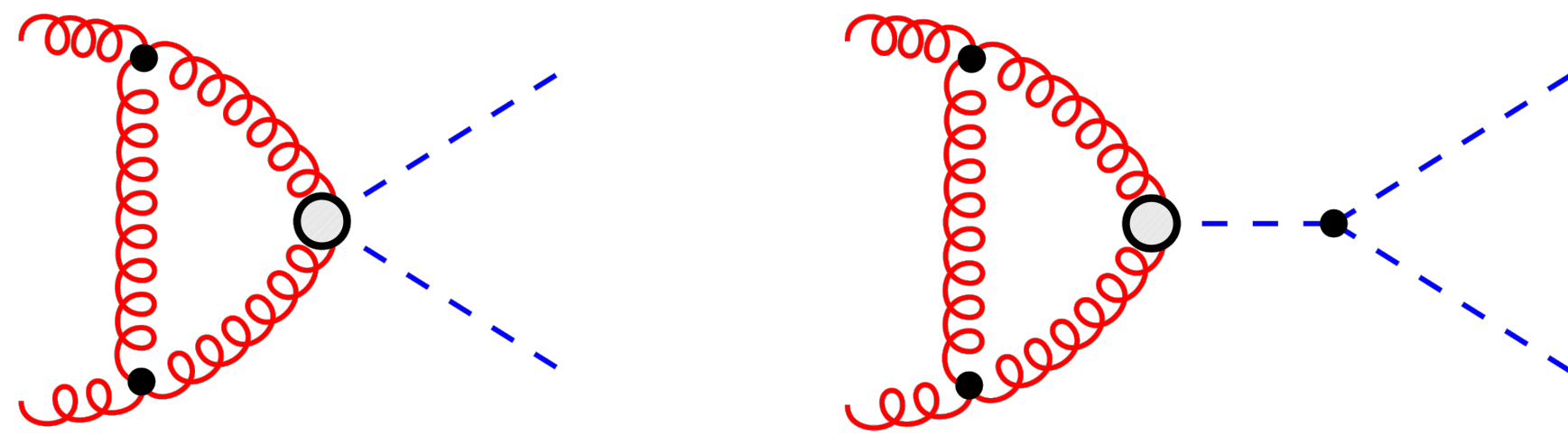
Double-Higgs production



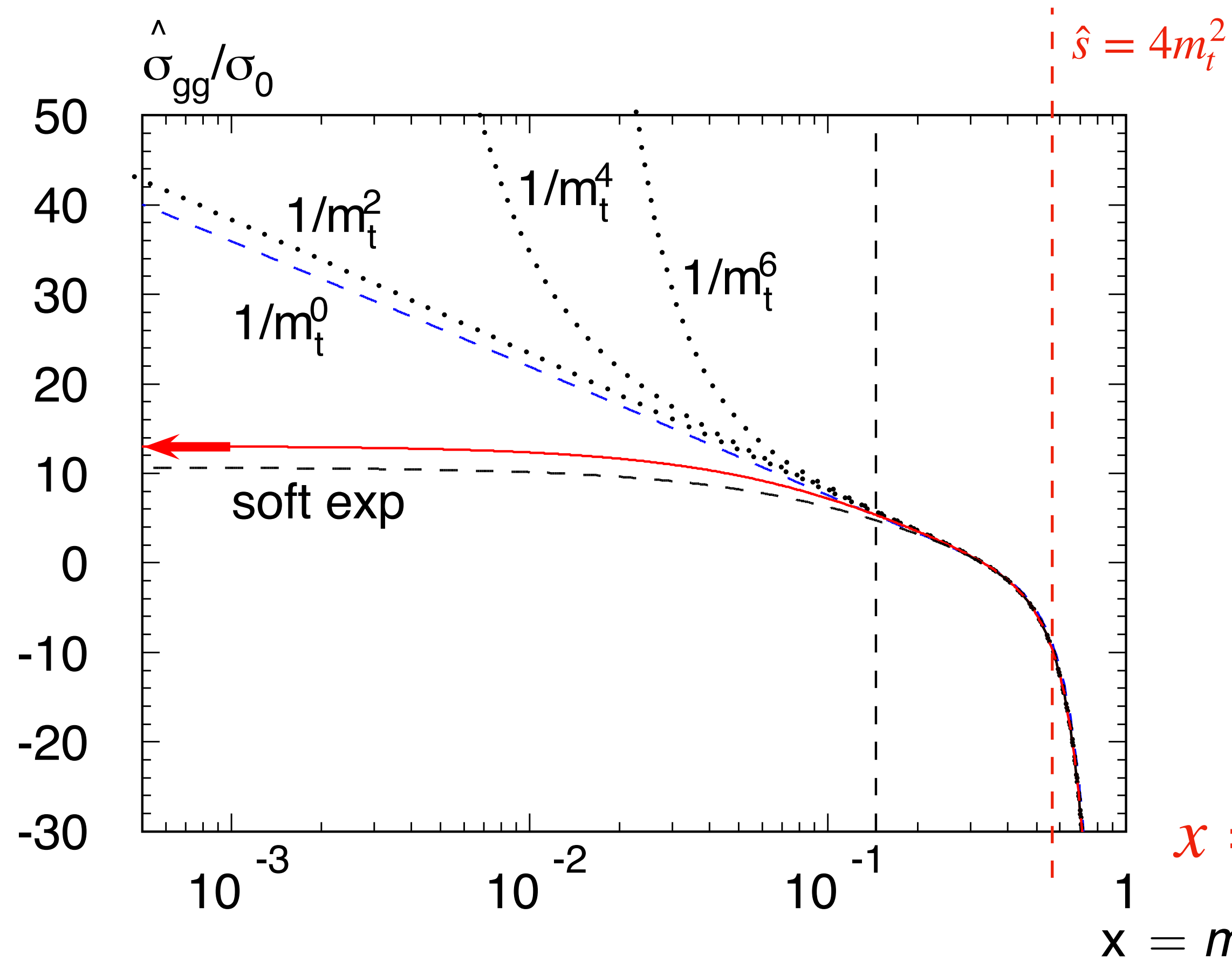
Double-Higgs production

v.d.Bij, Glover '88
Plehn, Spira, Zerwas '96



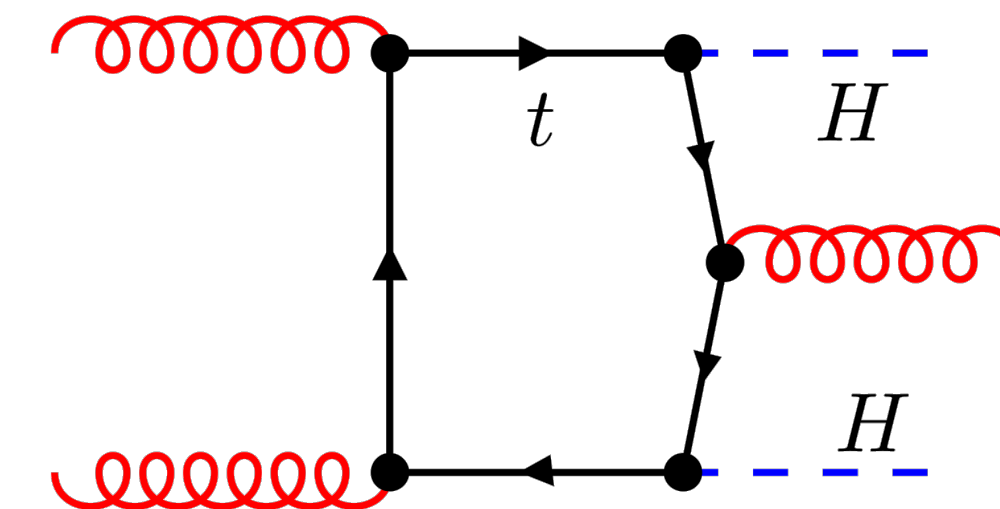


Dawson, Dittmaier, Spira '98



FT_{approx} real radiation exact

Maltoni, Vryonidou, Zaro '14



J. Grigo, J. Hoff, K. Melnikov, and M. Steinhauser, *On the Higgs boson pair production at the LHC*, *Nucl. Phys.* **B875** (2013) 1–17, [[arXiv:1305.7340](#)].

J. Grigo, K. Melnikov, and M. Steinhauser, *Virtual corrections to Higgs boson pair production in the large top quark mass limit*, *Nucl. Phys.* **B888** (2014) 17–29, [[arXiv:1408.2422](#)].

J. Grigo, J. Hoff, and M. Steinhauser, *Higgs boson pair production: top quark mass effects at NLO and NNLO*, *Nucl. Phys.* **B900** (2015) 412, [[arXiv:1508.00909](#)].

G. Degrandi, P. P. Giardino, and R. Gruber, *On the two-loop virtual QCD corrections to Higgs boson pair production in the Standard Model*, *Eur. Phys. J.* **C76** (2016), no. 7 411, [[arXiv:1603.00385](#)].

D. de Florian and J. Mazzitelli, *Two-loop virtual corrections to Higgs pair production*, *Phys. Lett.* **B724** (2013) 306–309, [[arXiv:1305.5206](#)].

D. de Florian and J. Mazzitelli, *Higgs Boson Pair Production at Next-to-Next-to-Leading Order in QCD*, *Phys. Rev. Lett.* **111** (2013) 201801, [[arXiv:1309.6594](#)].

D. Y. Shao, C. S. Li, H. T. Li, and J. Wang, *Threshold resummation effects in Higgs boson pair production at the LHC*, *JHEP* **07** (2013) 169, [[arXiv:1301.1245](#)].

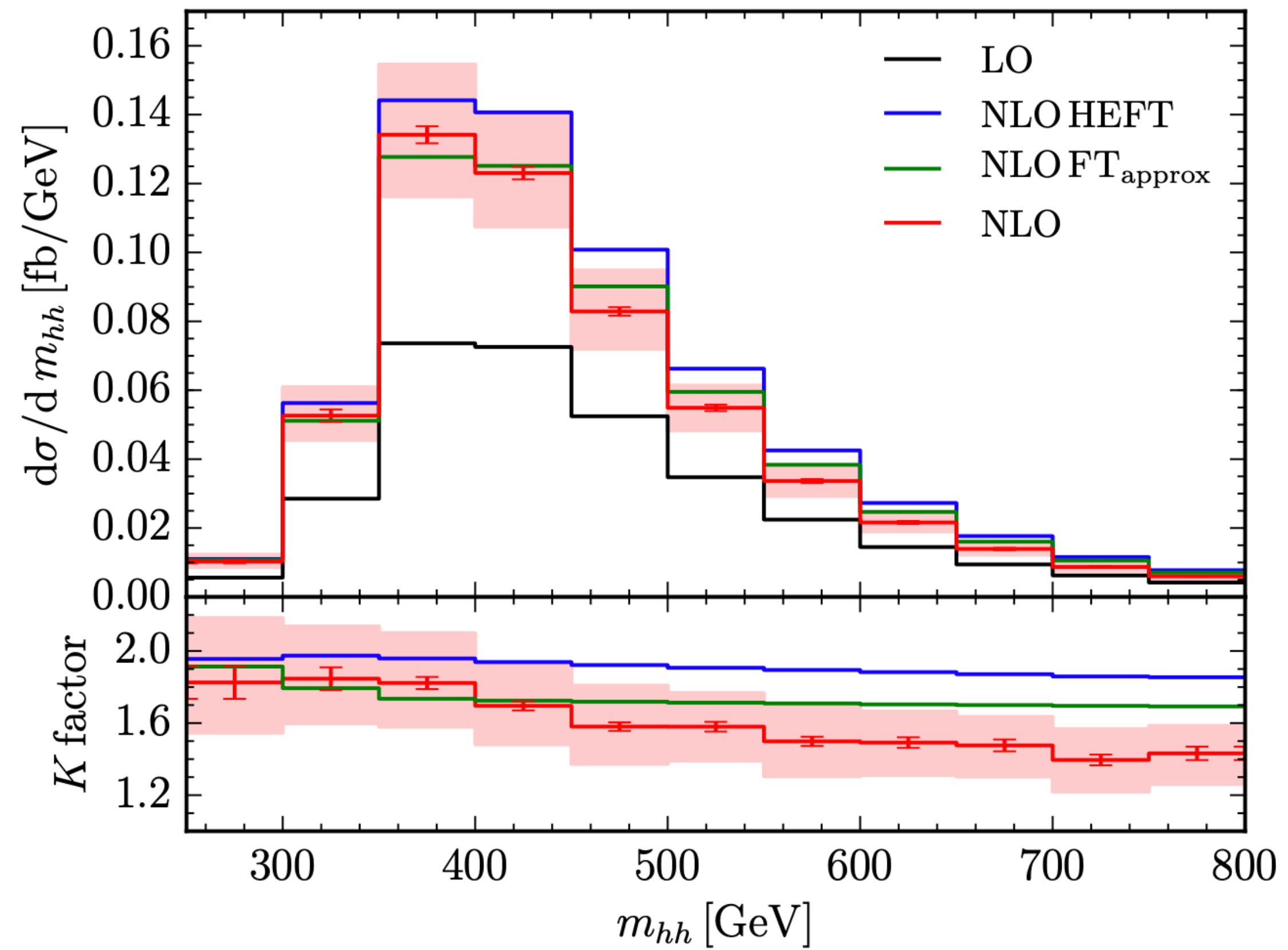
D. de Florian and J. Mazzitelli, *Higgs pair production at next-to-next-to-leading logarithmic accuracy at the LHC*, *JHEP* **09** (2015) 053, [[arXiv:1505.07122](#)].

D. de Florian, M. Grazzini, C. Hanga, S. Kallweit, J. M. Lindert, P. Maierhofer, J. Mazzitelli, and D. Rathlev, *Differential Higgs Boson Pair Production at Next-to-Next-to-Leading Order in QCD*, [arXiv:1606.09519](#).

L.-B. Chen, H. T. Li, H.-S. Shao and J. Wang, *Higgs boson pair production via gluon fusion at N^3LO in QCD*, *Phys. Lett.* **B803** (2020) 135292 [[1909.06808](#)].

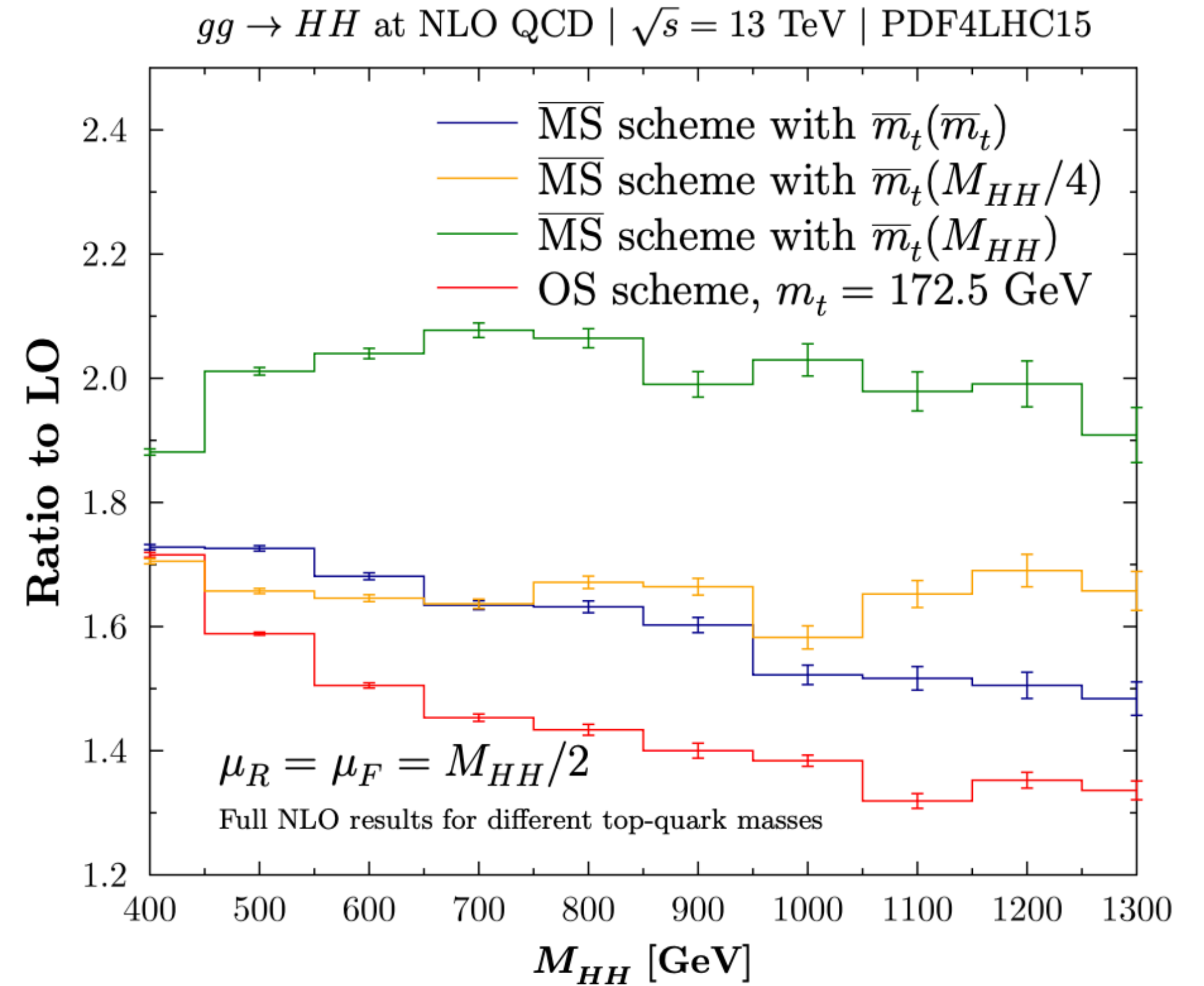
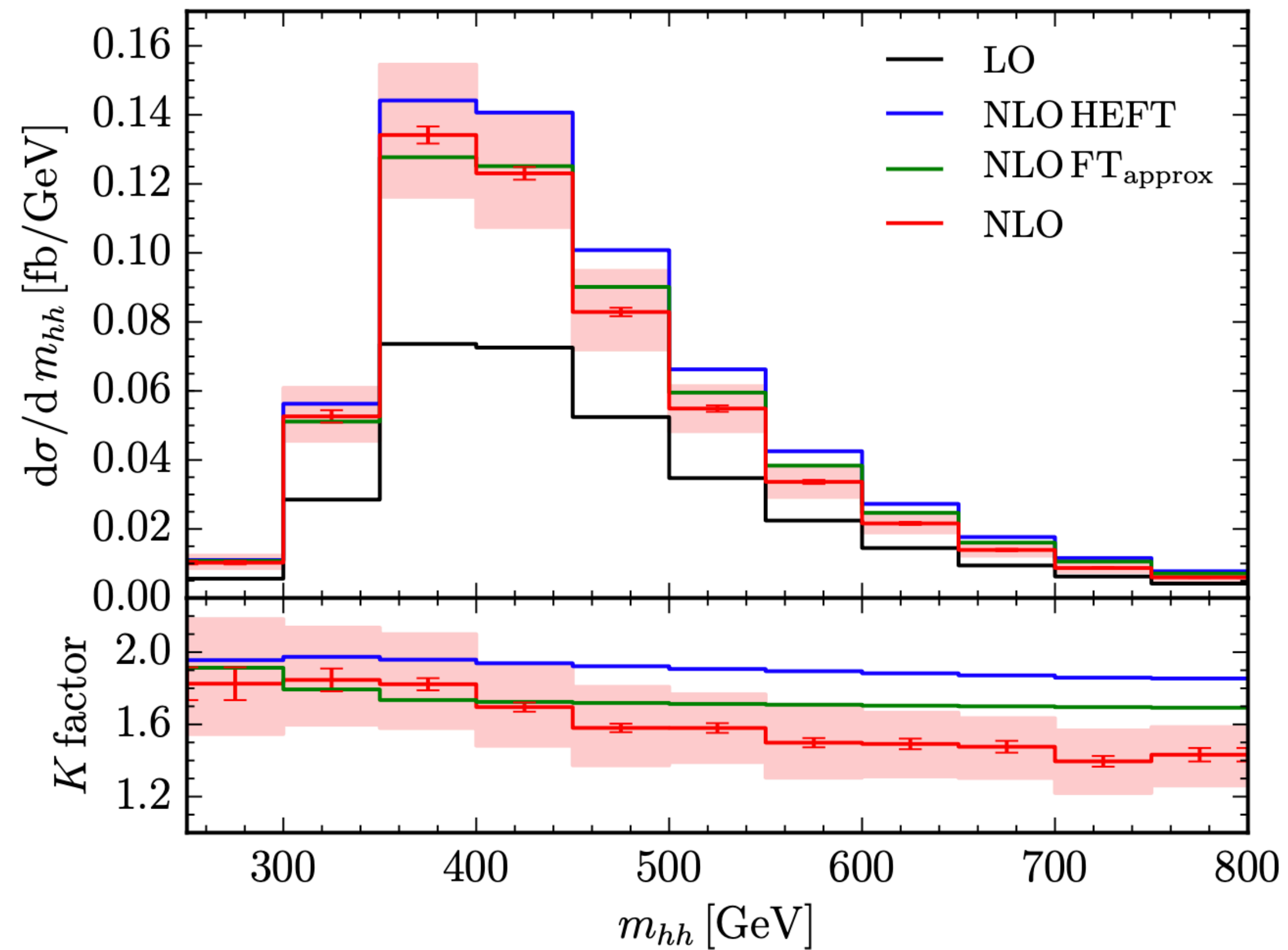
HEFT and
sub-leading terms
in $1/m_t$
through NLO

HEFT through N^3LO



Borowka, Greiner, Heinrich, Jones, Kerner, Schlenk, Schubert, Zirke ‘16

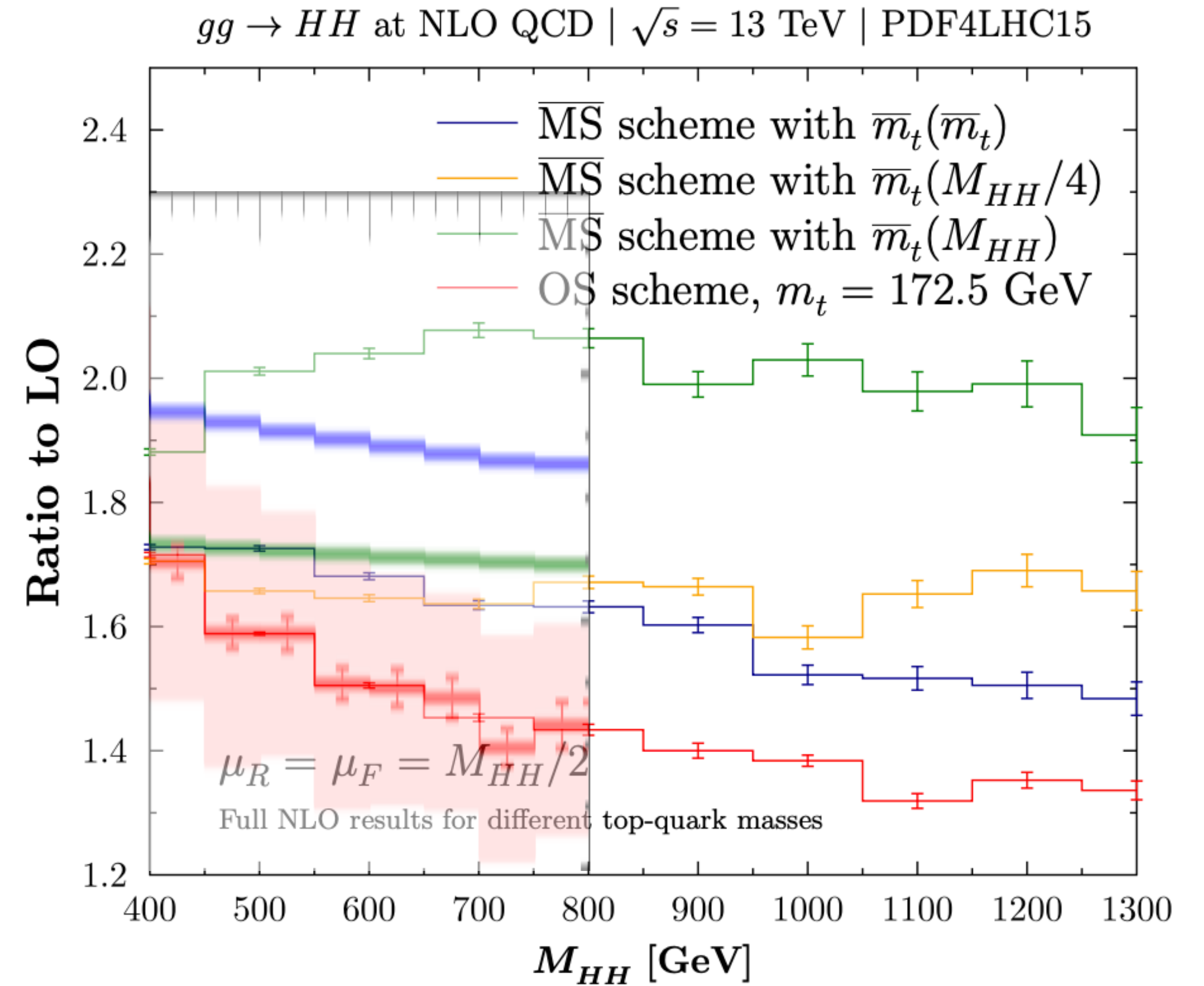
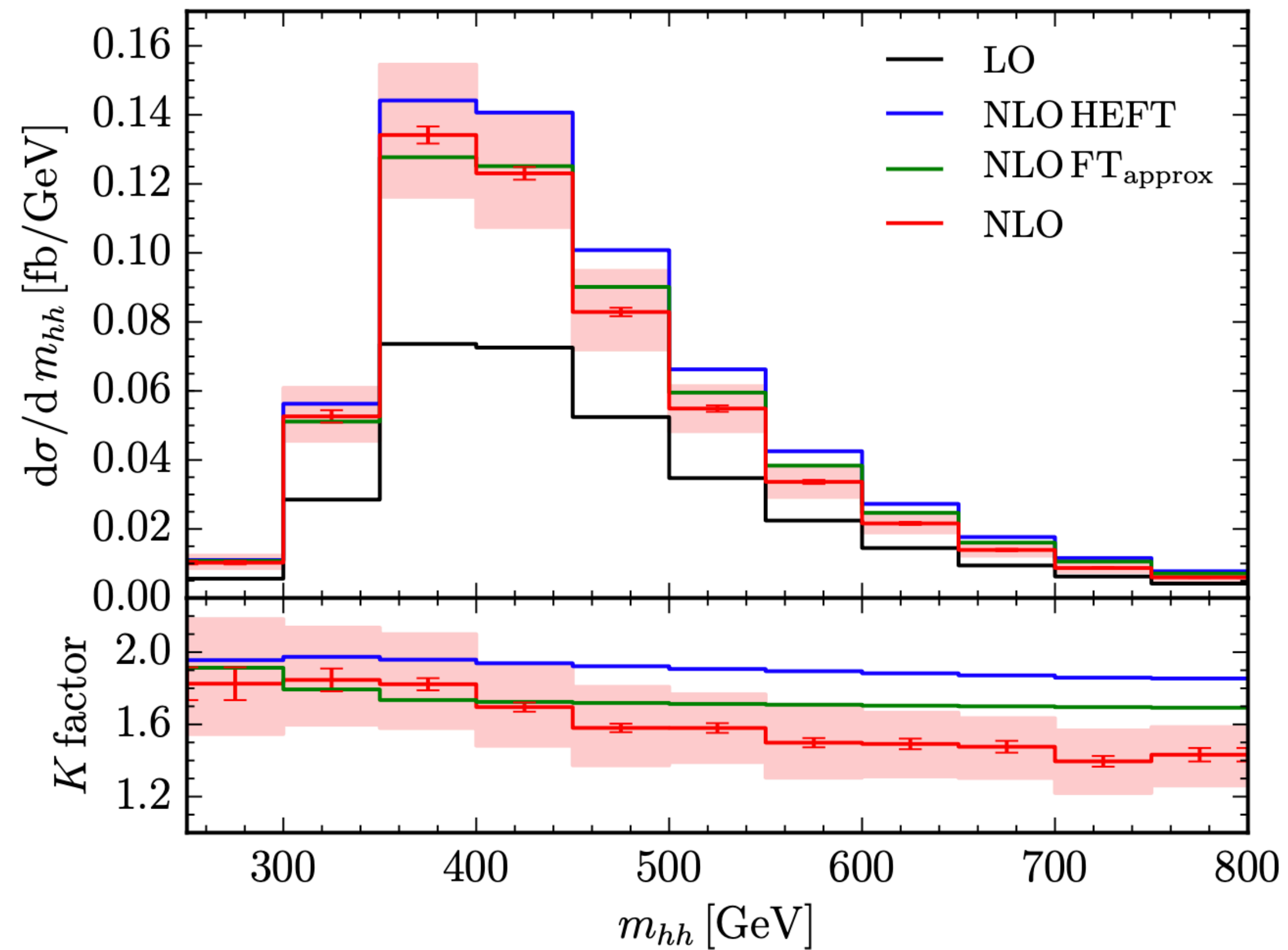
Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher ‘19



Borowka, Greiner, Heinrich, Jones, Kerner, Schlenk, Schubert, Zirke '16

Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher '19

Baglio, Campanario, Glaus, Mühlleitner, Ronca, Spira '20

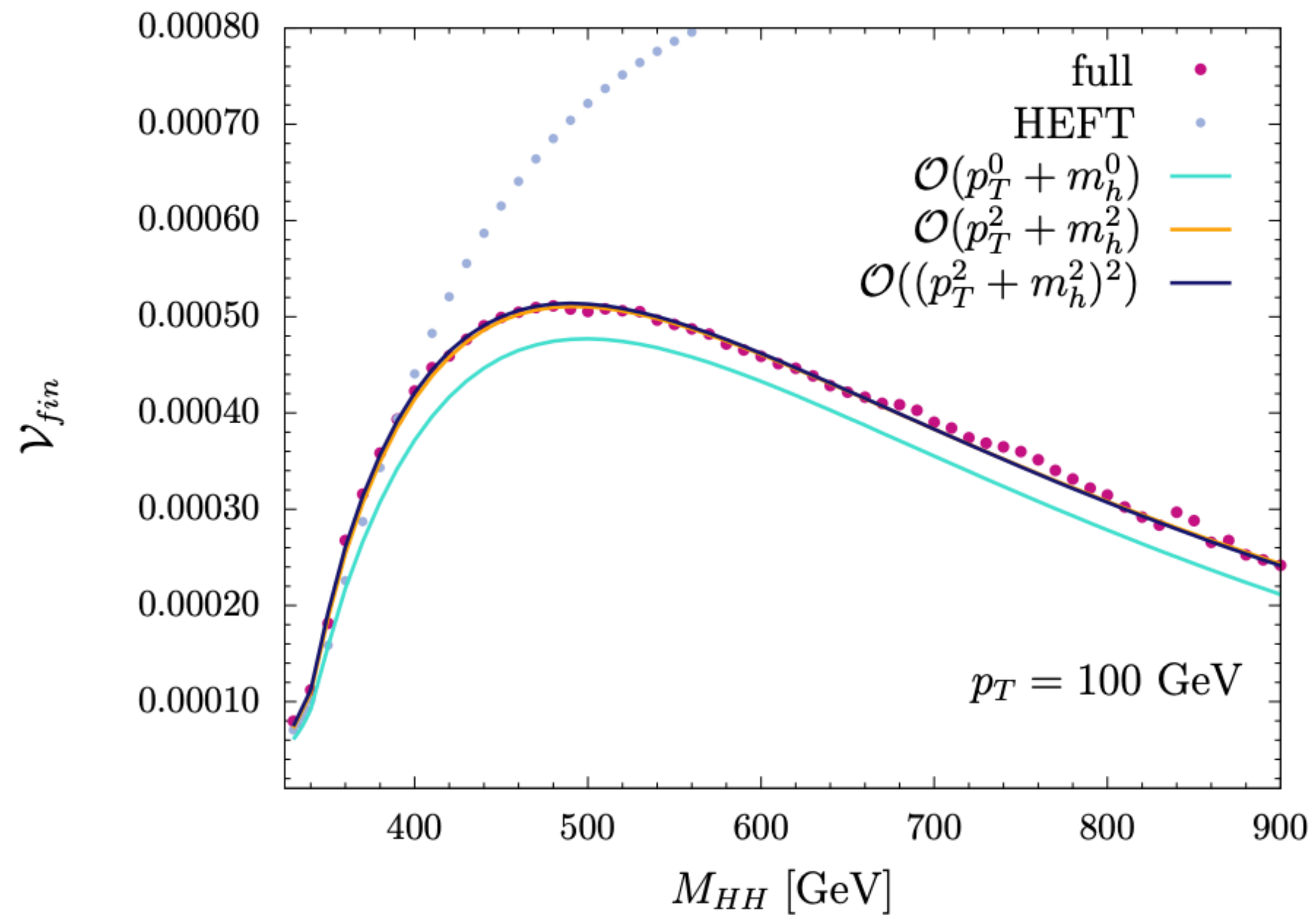


Baglio, Campanario, Glaus, Mühlleitner, Ronca, Spira '20

Borowka, Greiner, Heinrich, Jones, Kerner, Schlenk, Schubert, Zirke '16

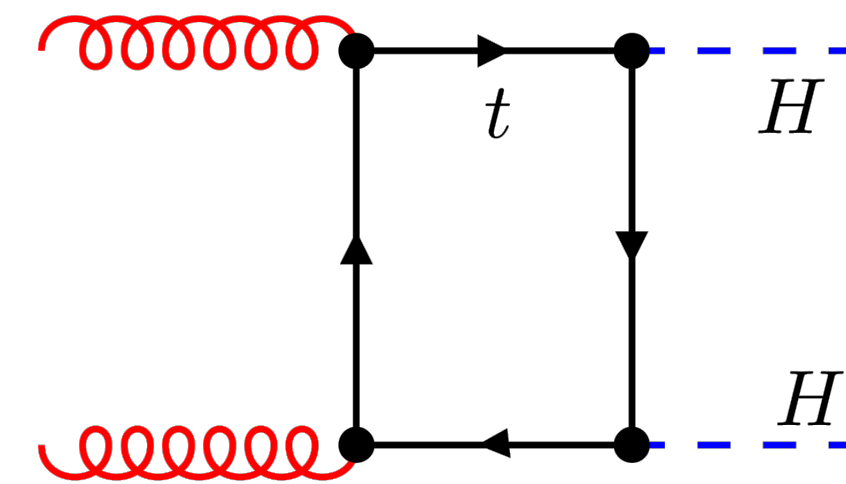
Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher '19

Improved/alternative approximations:

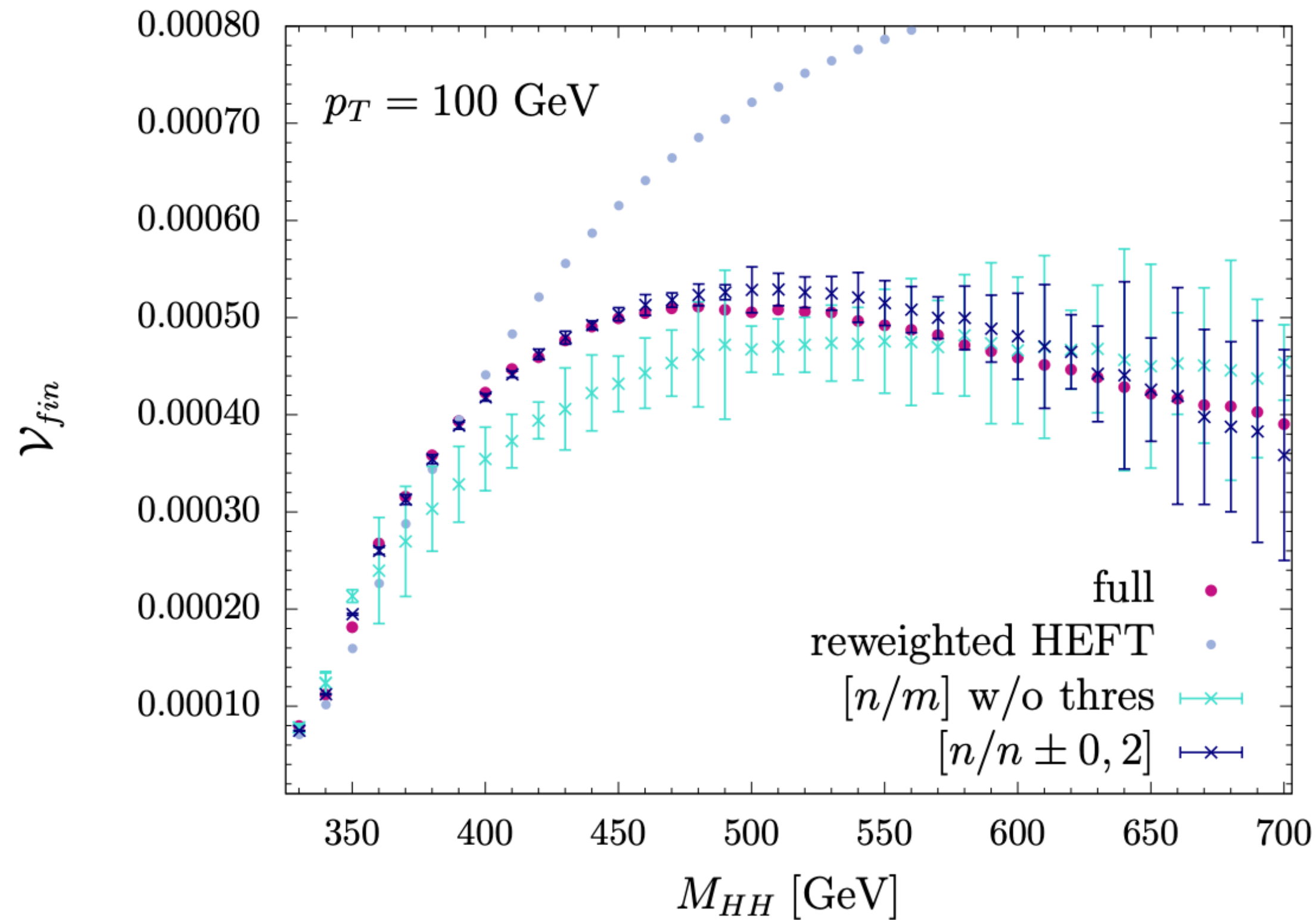


small p_T expansion

Bonciani, Degrandi, Giardino, Gröber '18



Improved/alternative approximations:



Padé approximation

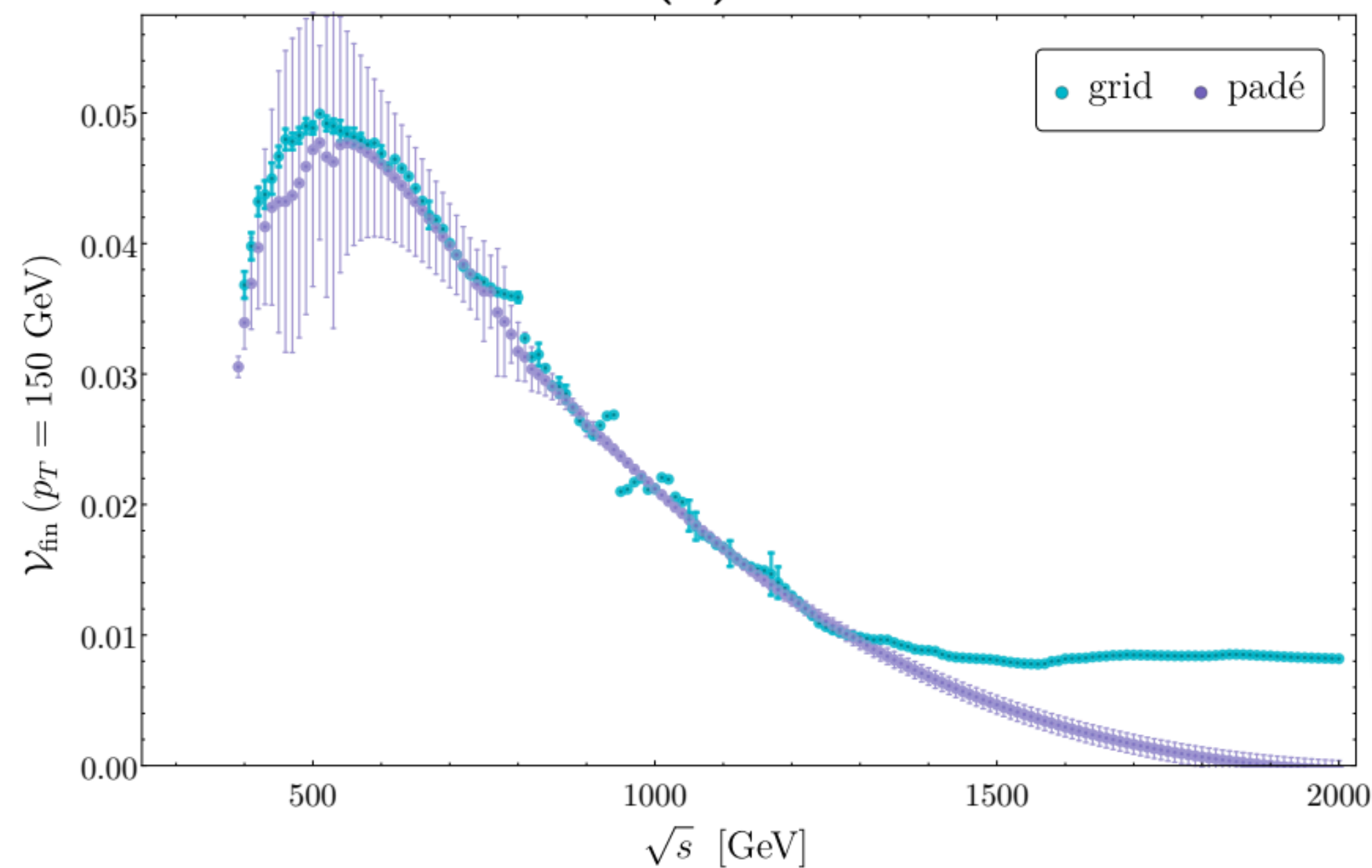
Gröber, Maier, Rauh '18

1/mt with threshold expansion:

$$F_{\Delta, C_F}^{2l} \stackrel{z \rightarrow 1}{\sim} \pi^2(1-z) \ln(1-z) - \frac{\pi(40-3\pi^2)}{12}(1-z)^{3/2} + \frac{2\pi^2}{3}(1-z)^2 \ln(1-z) + \mathcal{O}((1-z)^{5/2}), \quad (10)$$

Combination with high-energy form factors ($\sqrt{\hat{s}} \gg m_t > m_H, m_W$):

Davies, Mishima, Steinhauser, Wellmann '18



Double Higgs boson production at NLO: combining the exact numerical result and high-energy expansion

P3H-19-015

Joshua Davies^a, Gudrun Heinrich^b, Stephen P. Jones^c, Matthias Kerner^d,
Go Mishima^{a,e}, Matthias Steinhauser^a, David Wellmann^a

Combination with NNLO

Grazzini, Heinrich, Jones, Kallweit, Kerner, Lindert, Mazzitelli '18

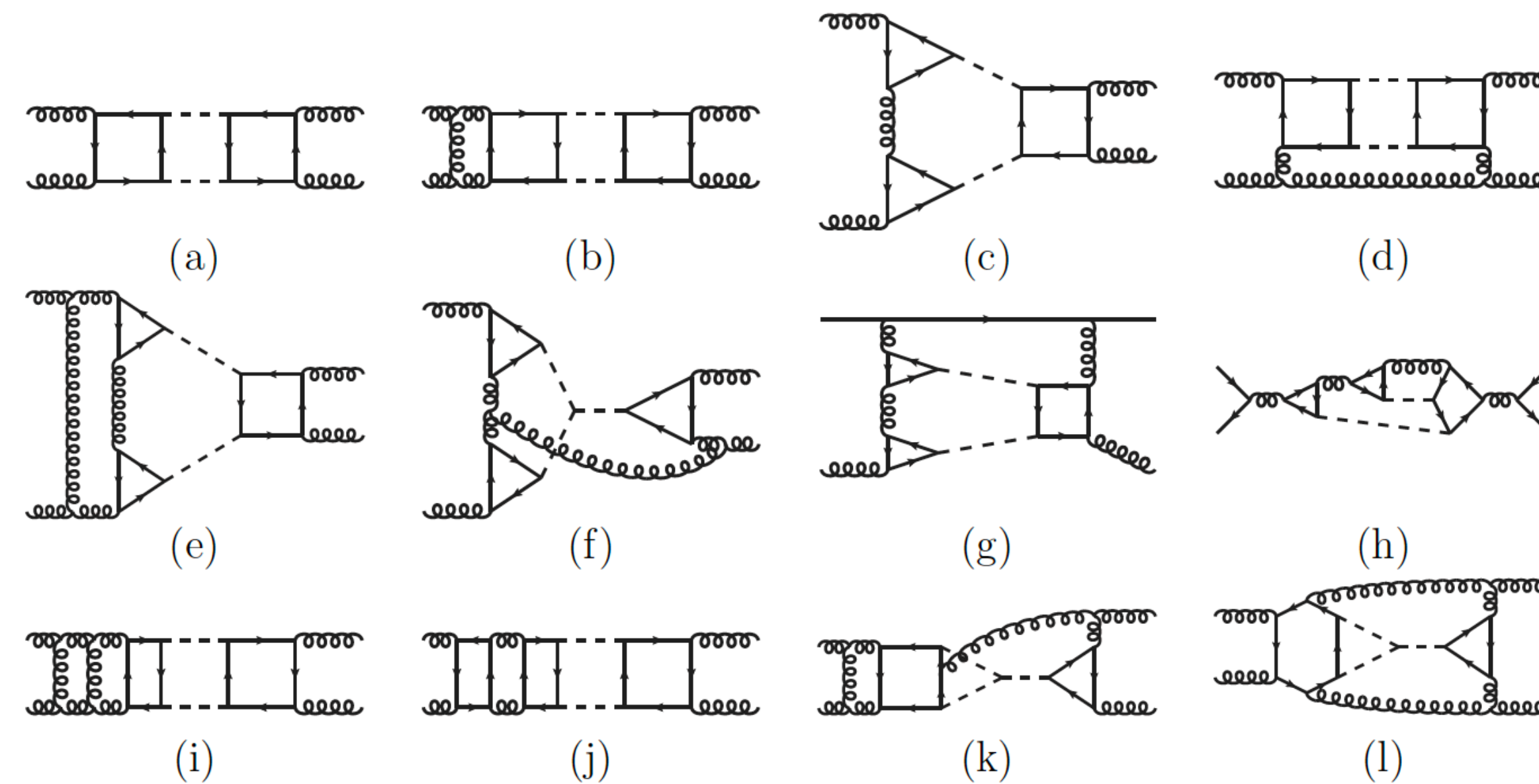
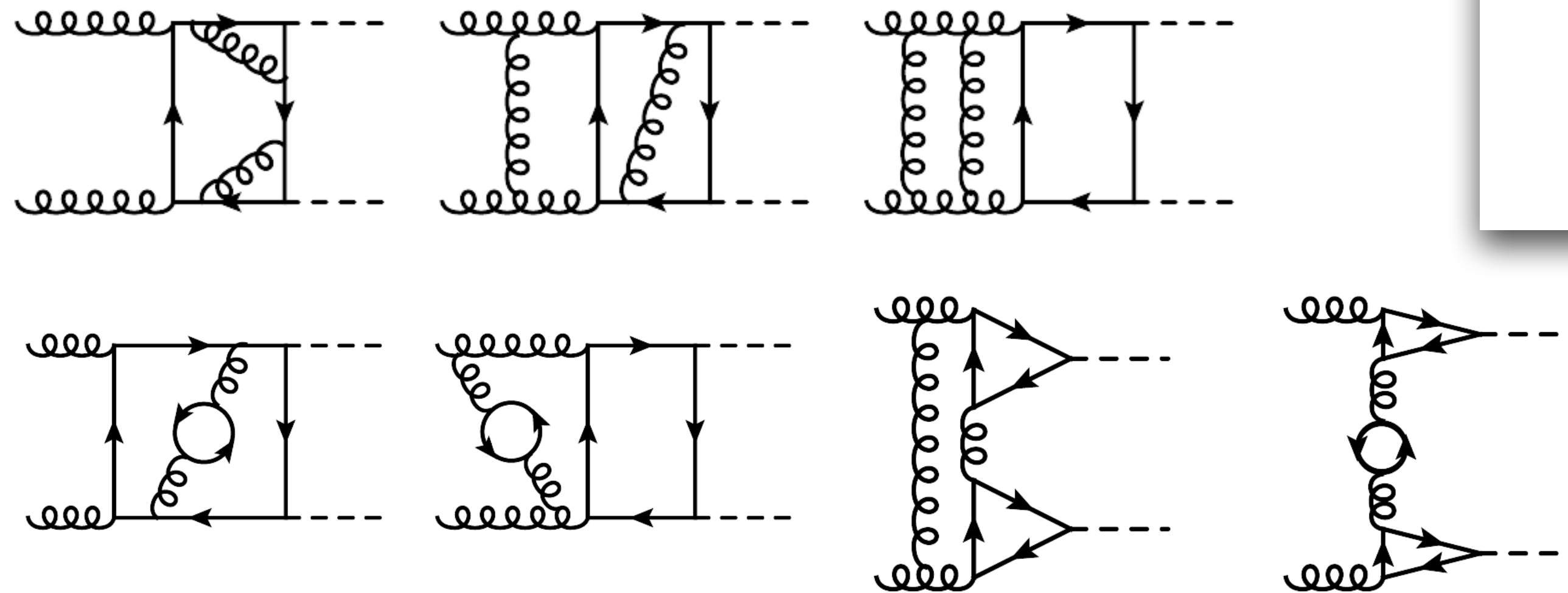
N³LO in heavy-top limit

Chen, Li, Shao, Wang '20

Three-loop form factors for Higgs boson pair
production in the large top mass limit

P3H-19-030

Joshua Davies and Matthias Steinhauser,



Real-virtual corrections to Higgs boson pair
production at NNLO: three closed top quark loops

P3H-19-009

Joshua Davies^a, Florian Herren^a, Go Mishima^{a,b}, Matthias Steinhauser^a

Application to BSM

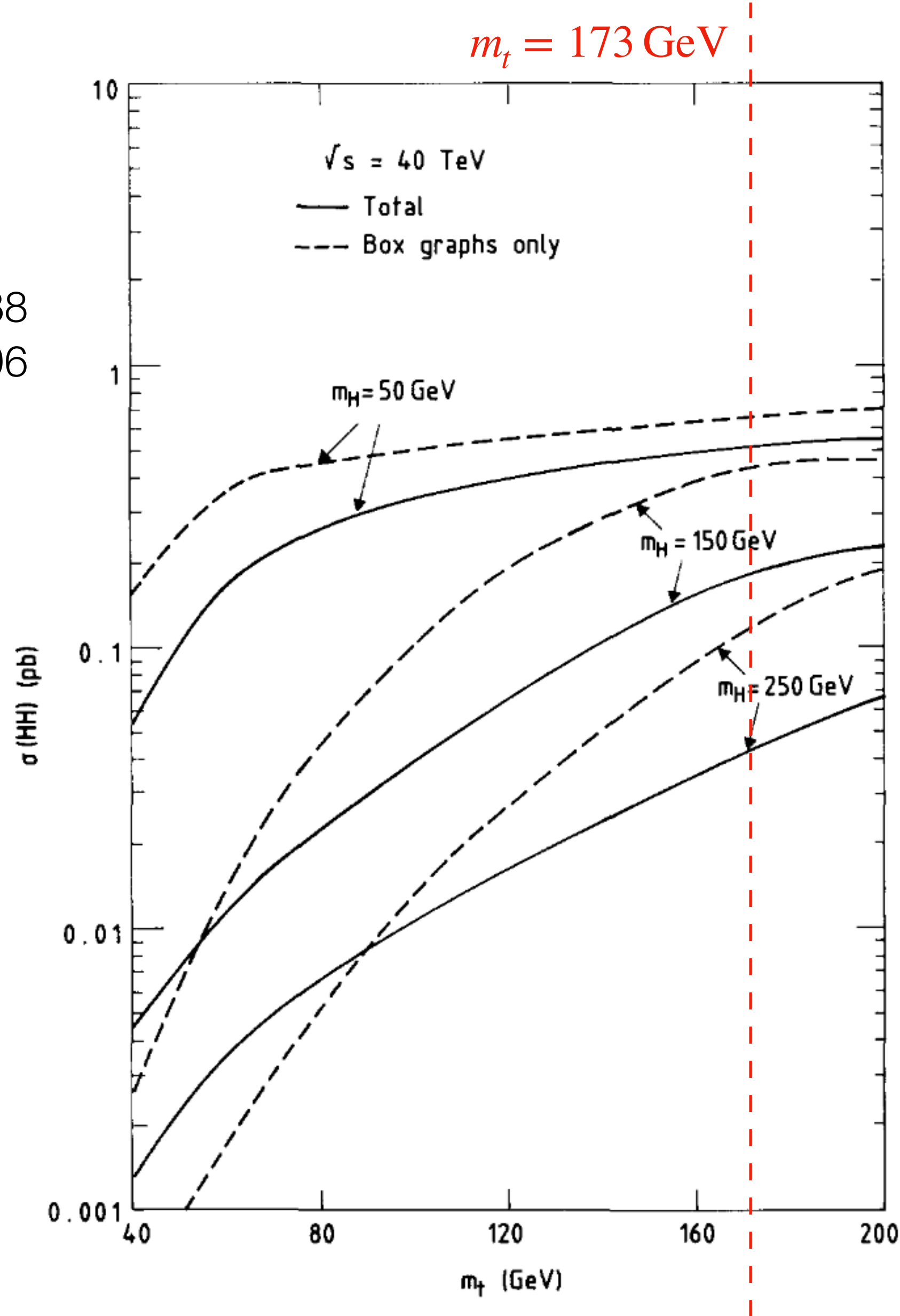
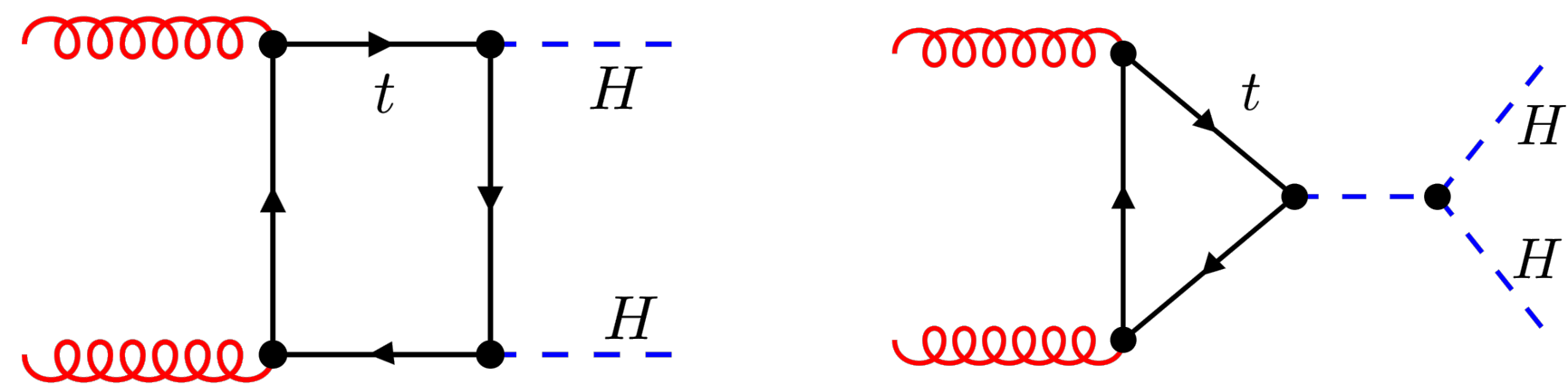
$$\mathcal{L} \supset -m_t \left(c_t \frac{h}{v} + c_{tt} \frac{h^2}{v^2} \right) \bar{t} t - c_{hhh} \frac{m_h^2}{2v} h^3 + \frac{\alpha_s}{8\pi} \left(c_{ggh} \frac{h}{v} + c_{gghh} \frac{h^2}{v^2} \right) G_{\mu\nu}^a G^{a,\mu\nu}$$

A non-linear EFT description of $gg \rightarrow HH$ at NLO interfaced to POWHEG P3H-20-026

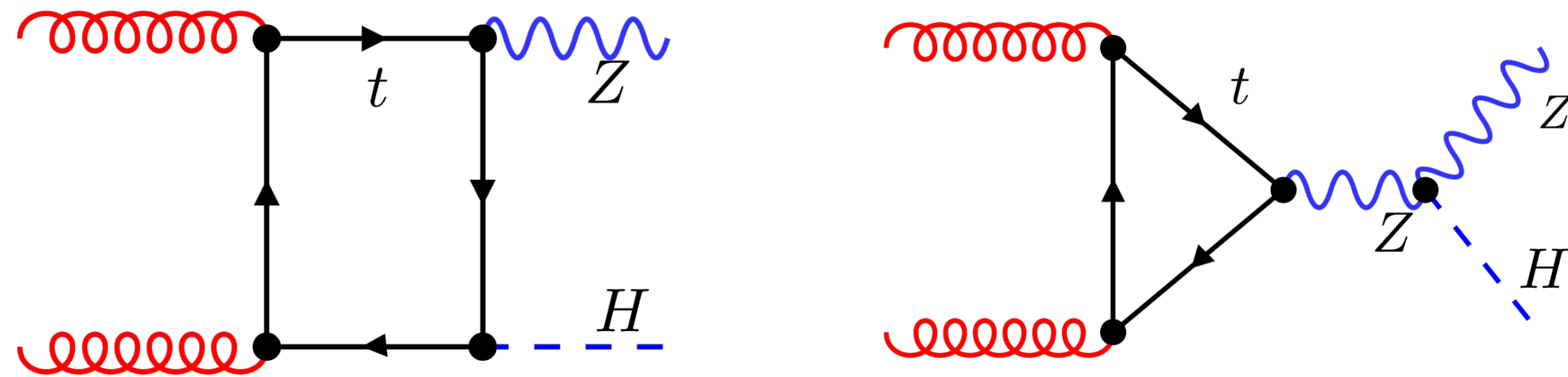
Gudrun Heinrich,^a Stephen P. Jones,^b Matthias Kerner,^c Ludovic Scyboz^d

HH production

v.d.Bij, Glover '88
Plehn, Spira, Zerwas '96



ZH production



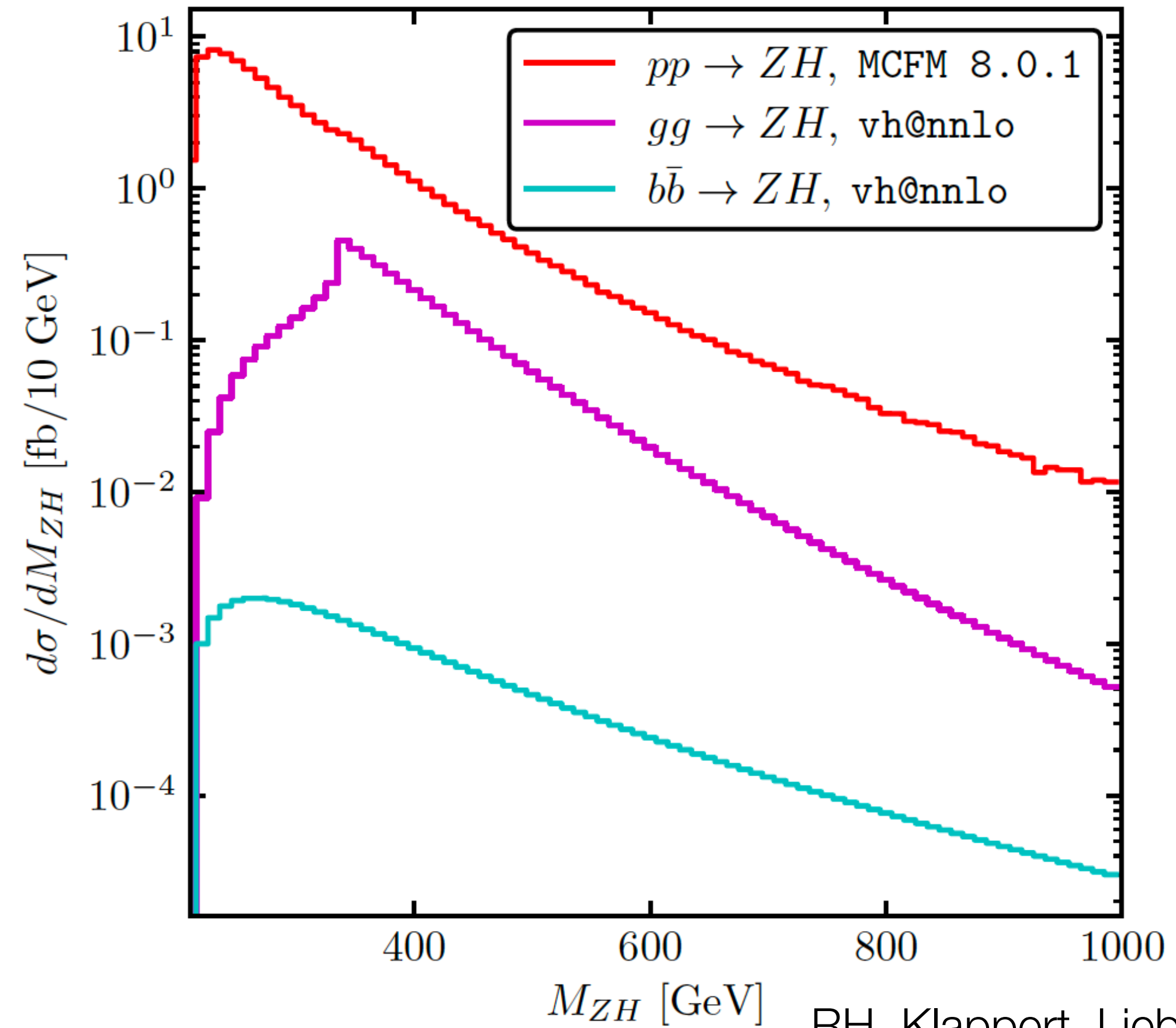
LO

Kniehl '90

NLO $1/m_t$

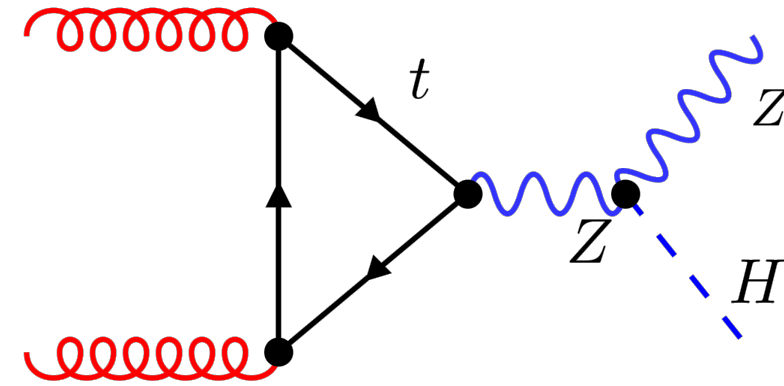
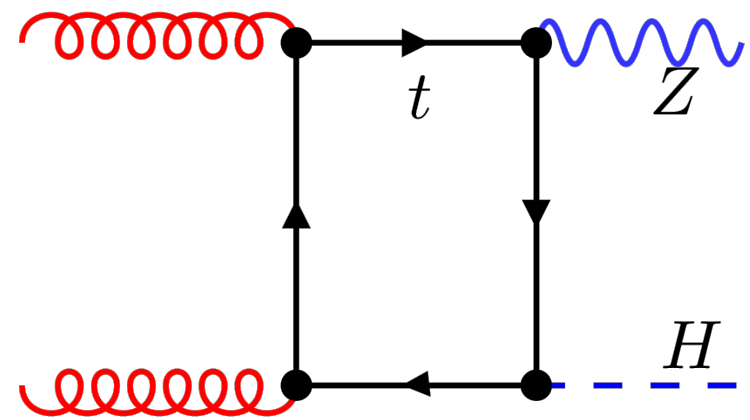
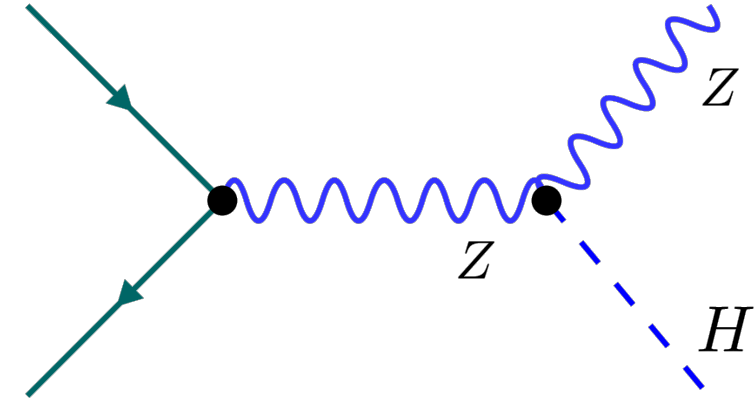
Altenkamp, Dittmaier, RH, Rzehak, Zirke '13

Hasselhuhn, Luthe, Steinhauser '17



RH, Klappert, Liebler, Simon '18
RH, Klappert, Pandini, Papaefstathiou, '18

ZH production



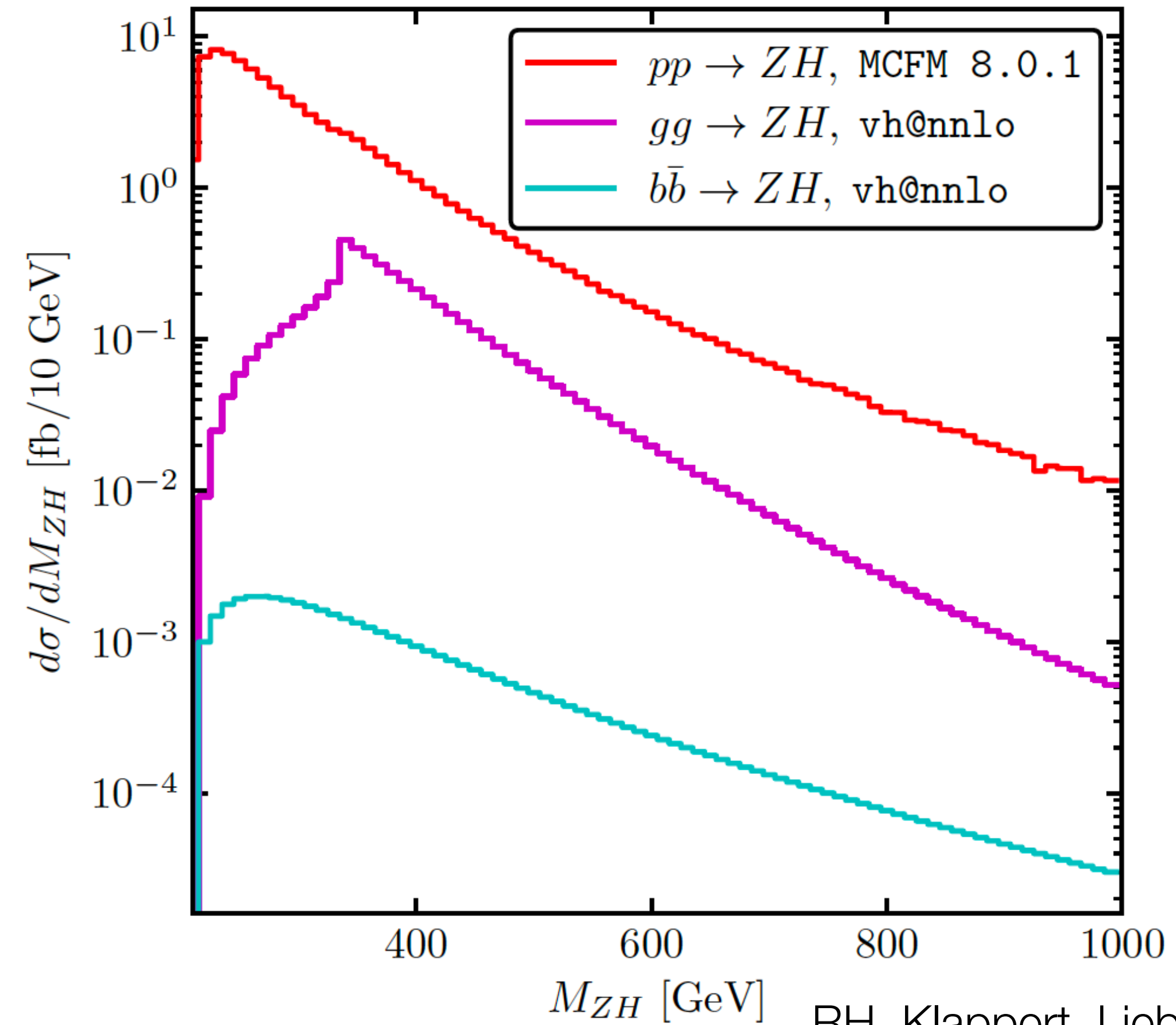
LO

Kniehl '90

NLO $1/m_t$

Altenkamp, Dittmaier, RH, Rzehak, Zirke '13

Hasselhuhn, Luthe, Steinhauser '17

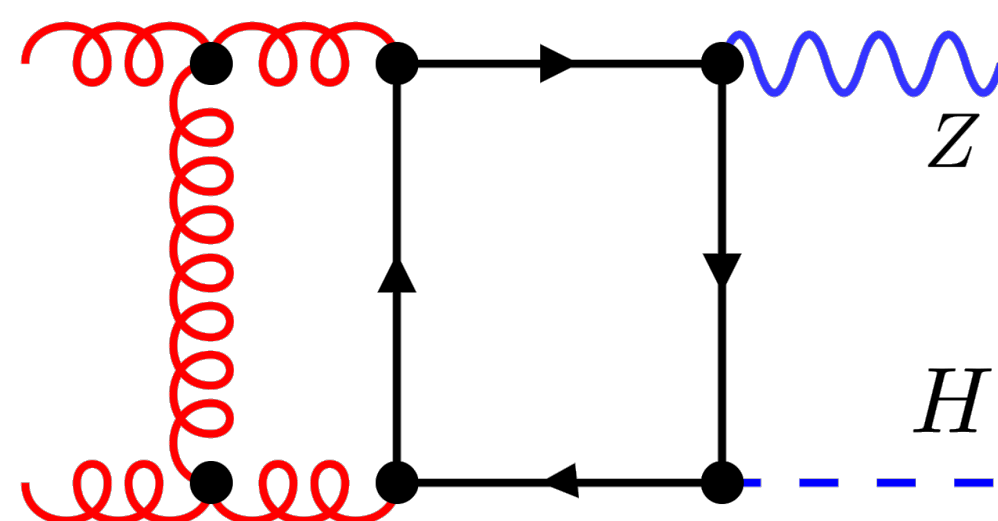


RH, Klappert, Liebler, Simon '18
RH, Klappert, Pandini, Papaefstathiou, '18

exact virtual:

**ZH production in gluon fusion: two-loop
amplitudes with full top quark mass
dependence** P3H-20-076

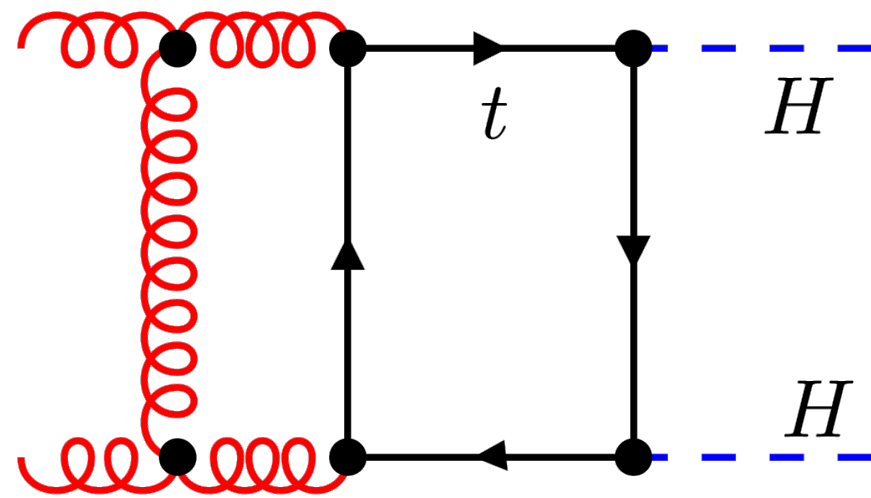
Long Chen,^{a,f} Gudrun Heinrich,^b Stephen P. Jones,^{c,d} Matthias Kerner,^e Jonas Klappert,^f Johannes Schlenk^g



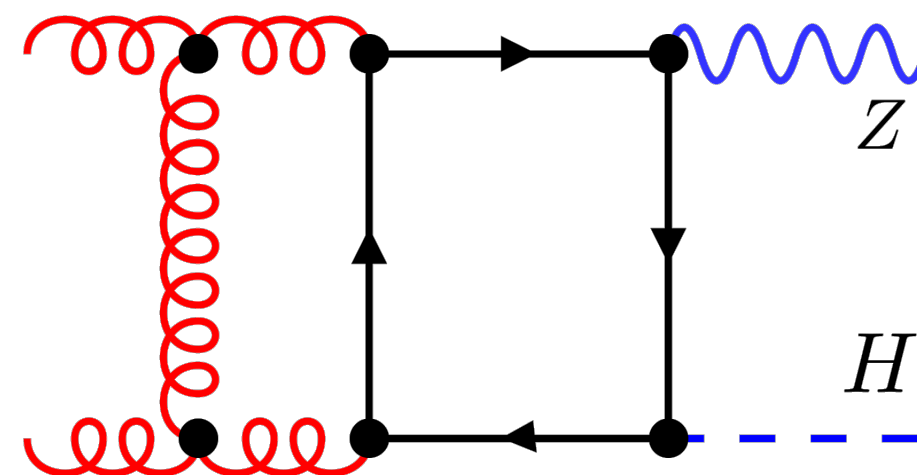
using Kira+FireFly:

**Integral Reduction with Kira 2.0 and
Finite Field Methods** P3H-20-041

Jonas Klappert^{*,a}, Fabian Lange^{†,a}, Philipp Maierhöfer^{‡,b}, and Johann Usovitsch^{§,c}

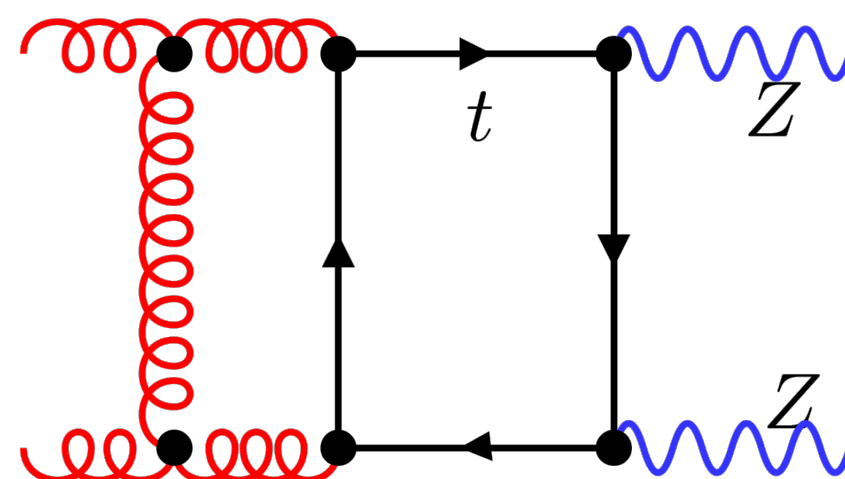


Borowka, Greiner, Heinrich, Jones, Kerner, Schlenk, Schubert, Zirke '16
 Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher '19



**ZH production in gluon fusion: two-loop
 amplitudes with full top quark mass
 dependence** P3H-20-076

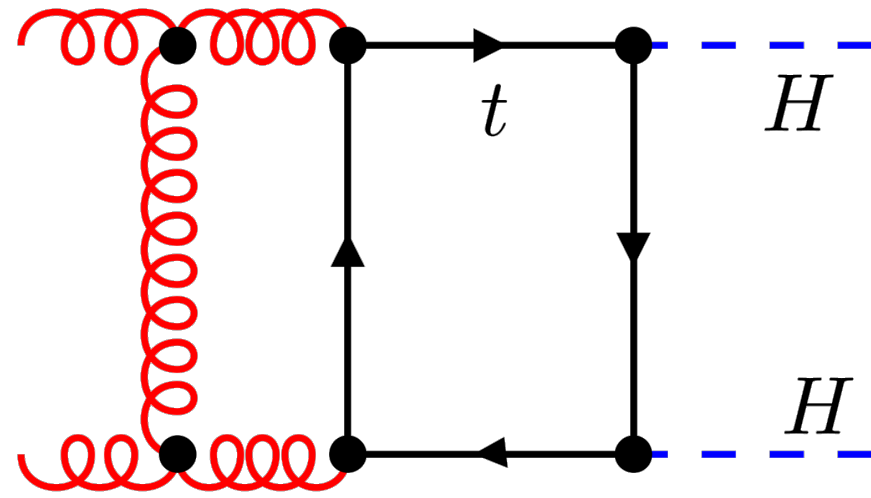
Long Chen,^{a,f} Gudrun Heinrich,^b Stephen P. Jones,^{c,d} Matthias Kerner,^e Jonas Klappert,^f Johannes Schlenk^g



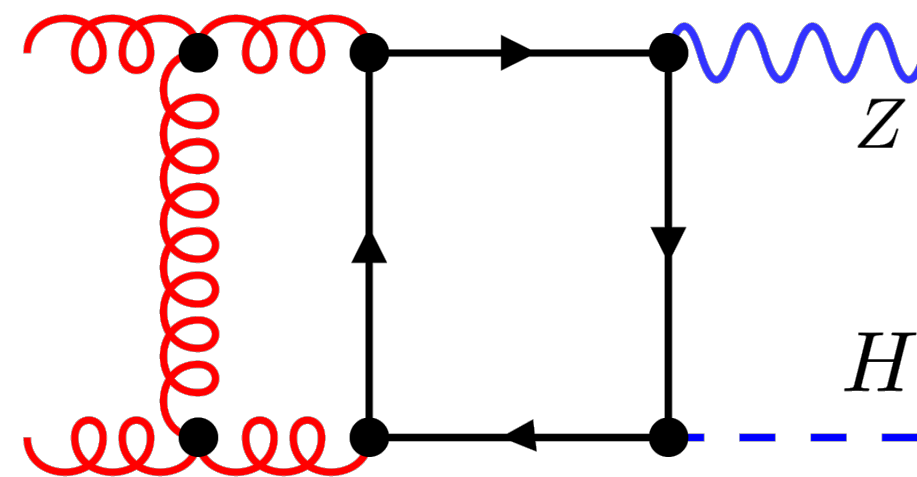
**Top quark contribution to two-loop helicity
 amplitudes for Z boson pair production in gluon
 fusion**

P3H-21-008

Christian Brønnum-Hansen and Chen-Yu Wang



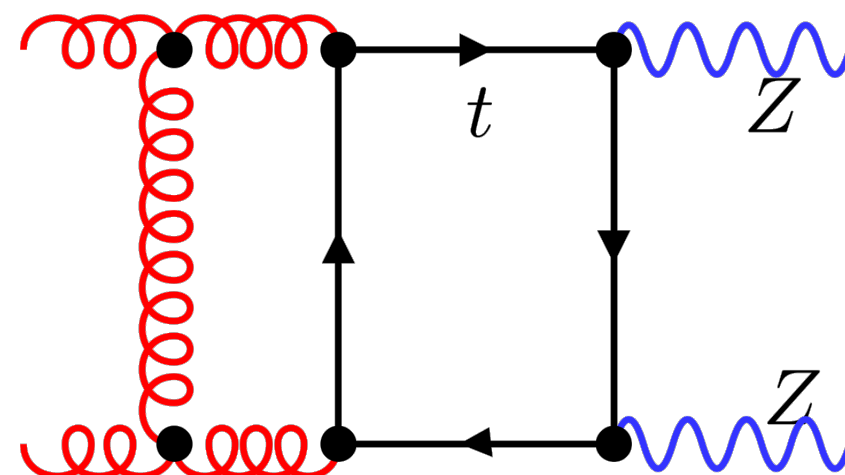
Borowka, Greiner, Heinrich, Jones, Kerner, Schlenk, Schubert, Zirke '16
 Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher '19



ZH production in gluon fusion: two-loop amplitudes with full top quark mass dependence

P3H-20-076

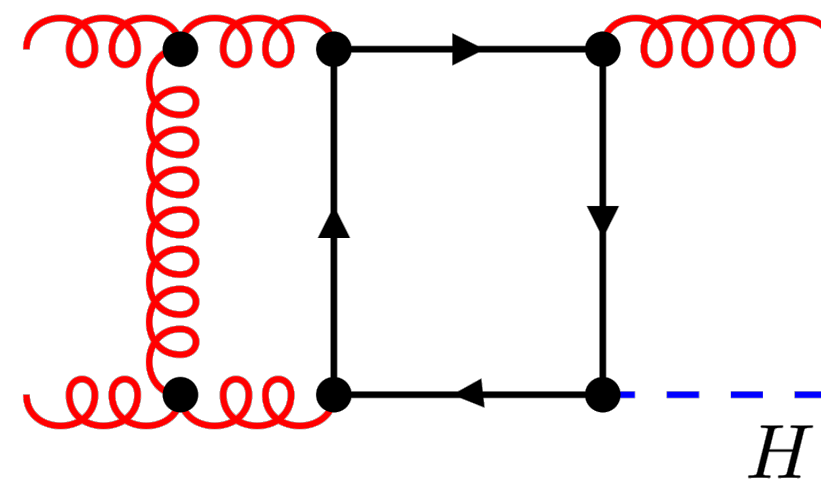
Long Chen,^{a,f} Gudrun Heinrich,^b Stephen P. Jones,^{c,d} Matthias Kerner,^e Jonas Klappert,^f Johannes Schlenk^g

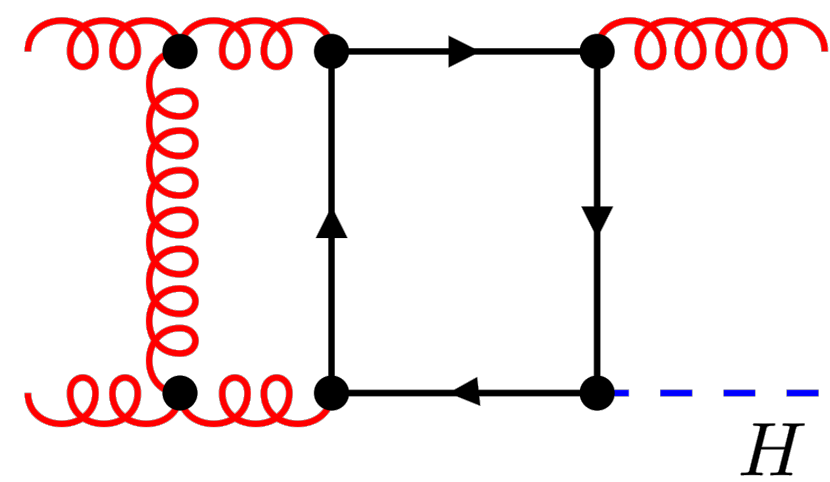


Top quark contribution to two-loop helicity amplitudes for Z boson pair production in gluon fusion

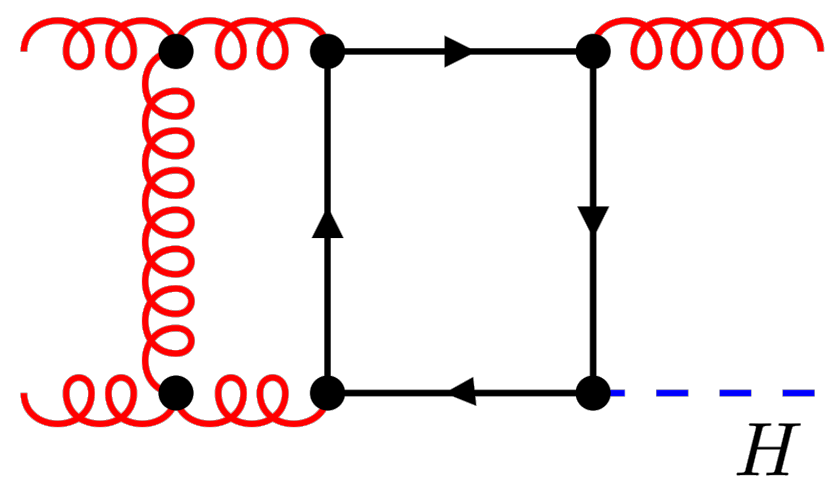
P3H-21-008

Christian Brønnum-Hansen and Chen-Yu Wang

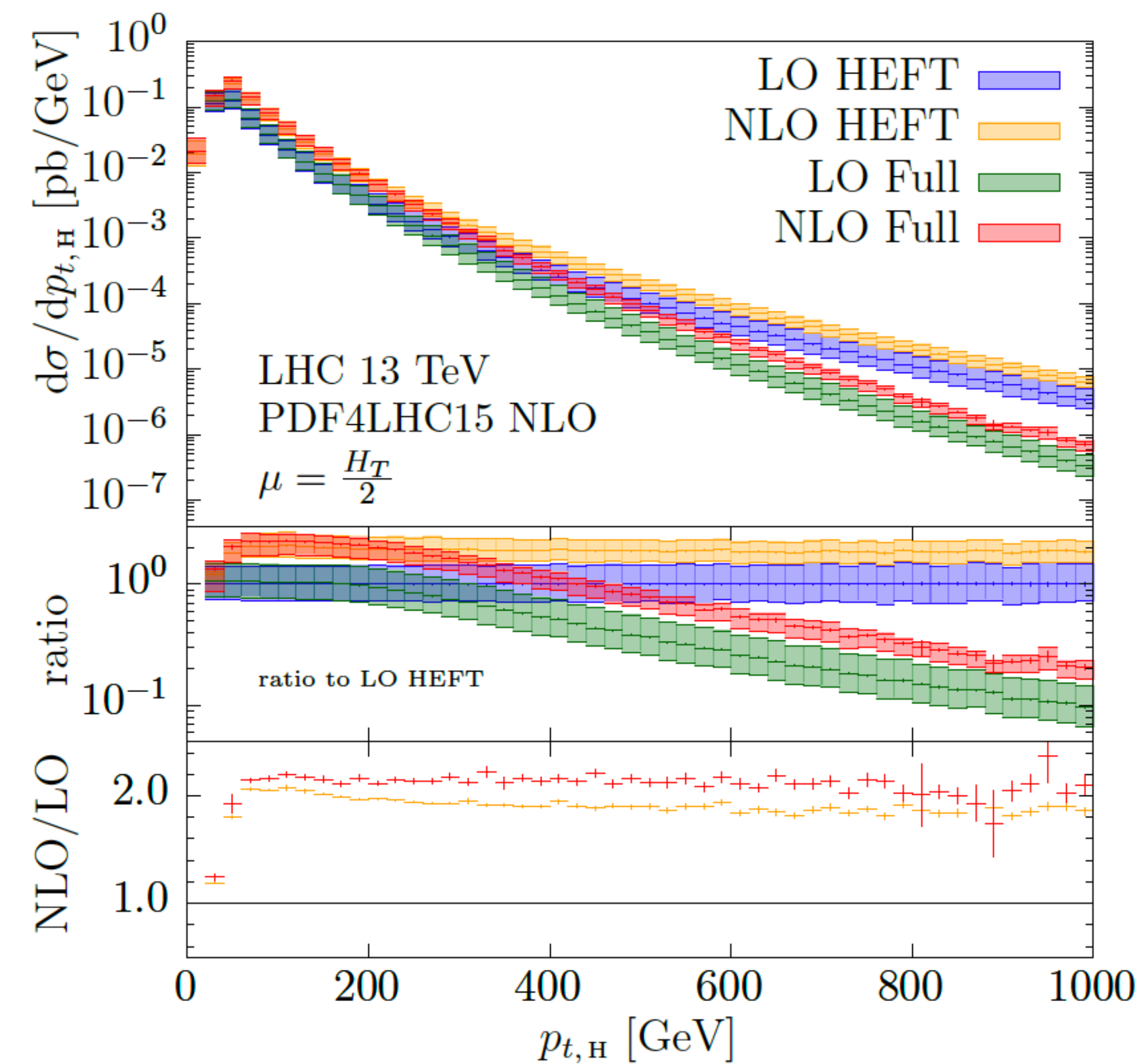


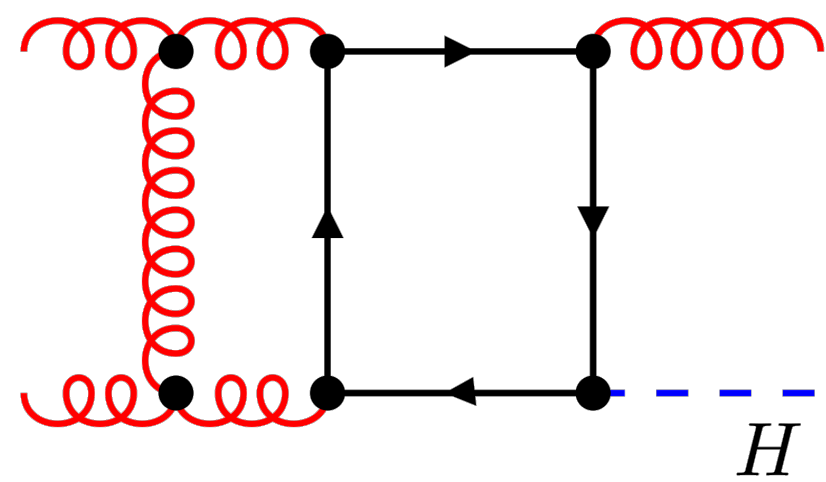


Lindert, Kudashkin, Melnikov, Wever '18 (large p_T)
 Jones, Kerner, Luisoni '18

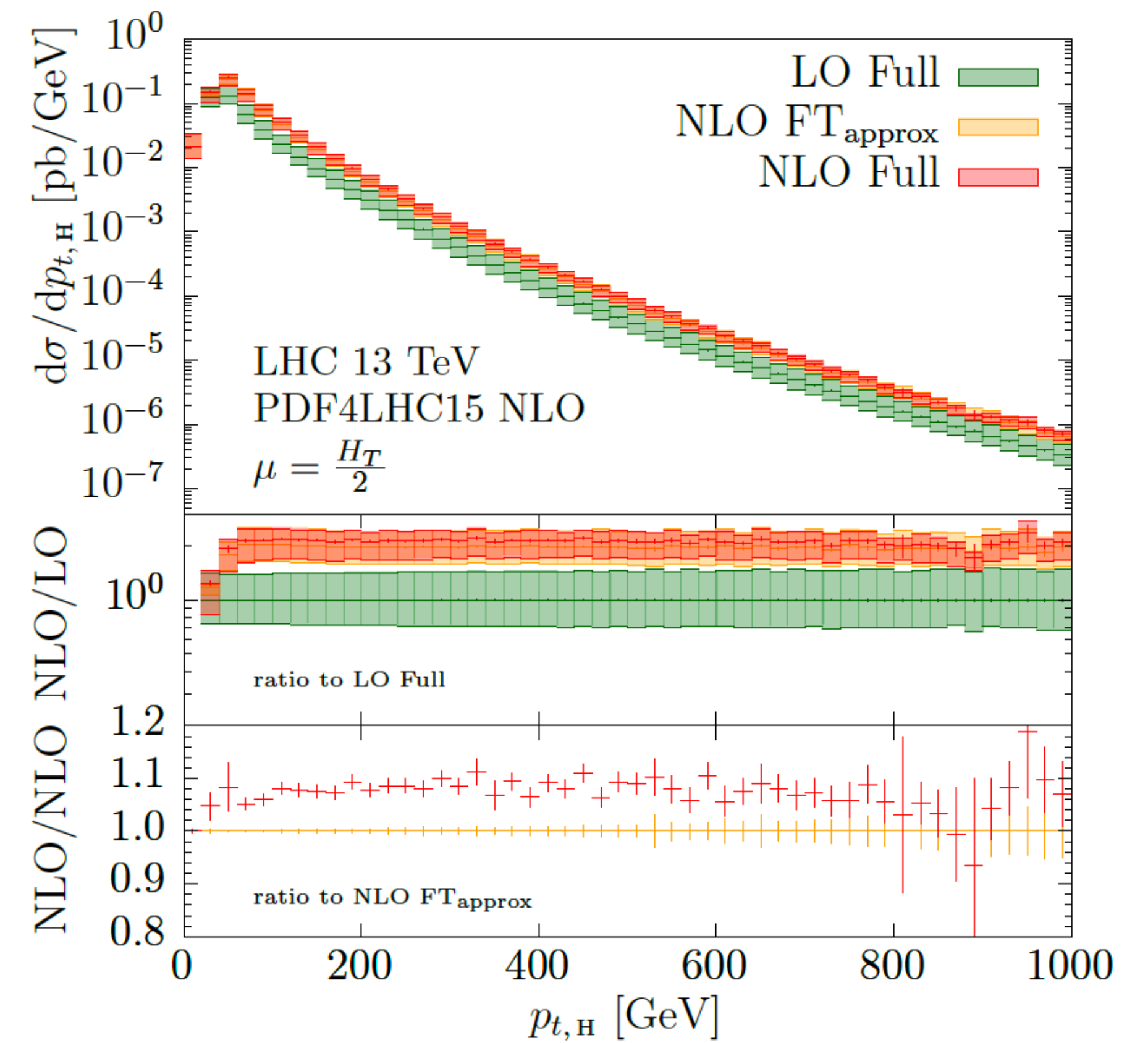


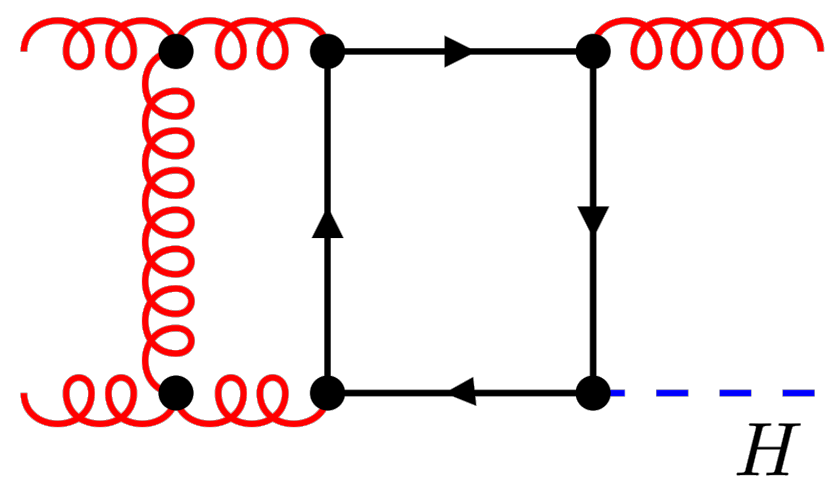
Lindert, Kudashkin, Melnikov, Wever '18 (large p_T)
 Jones, Kerner, Luisoni '18



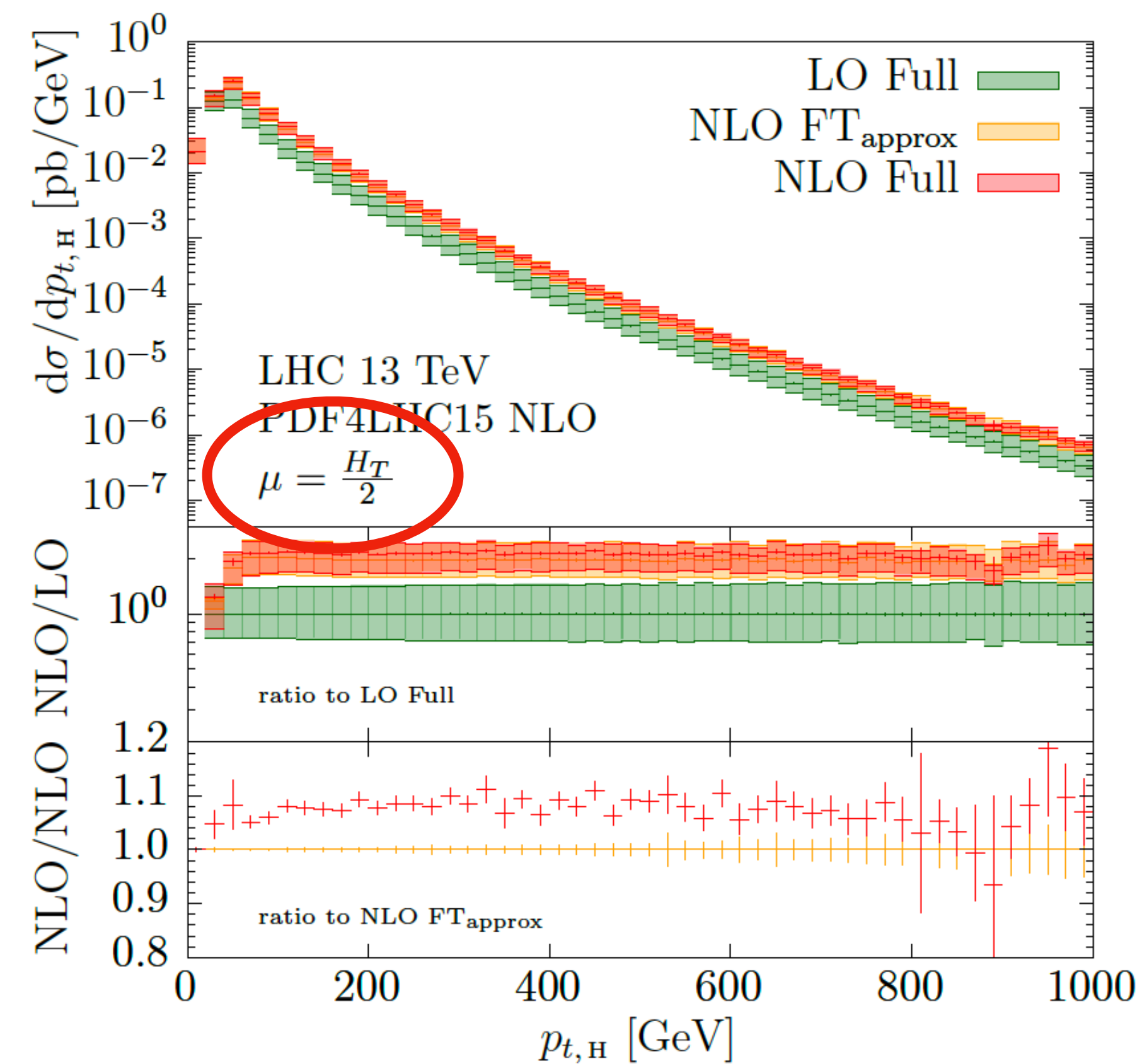


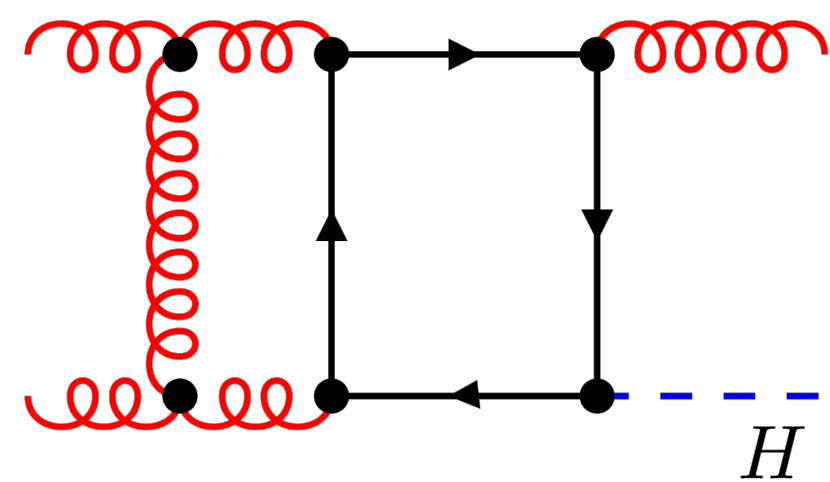
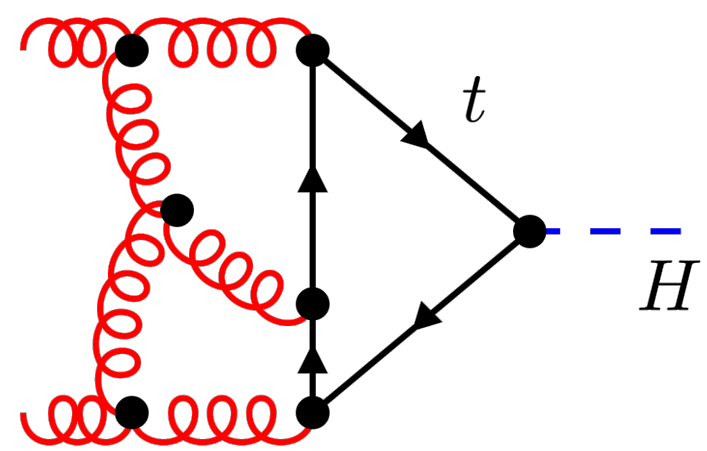
Lindert, Kudashkin, Melnikov, Wever '18 (large p_T)
 Jones, Kerner, Luisoni '18



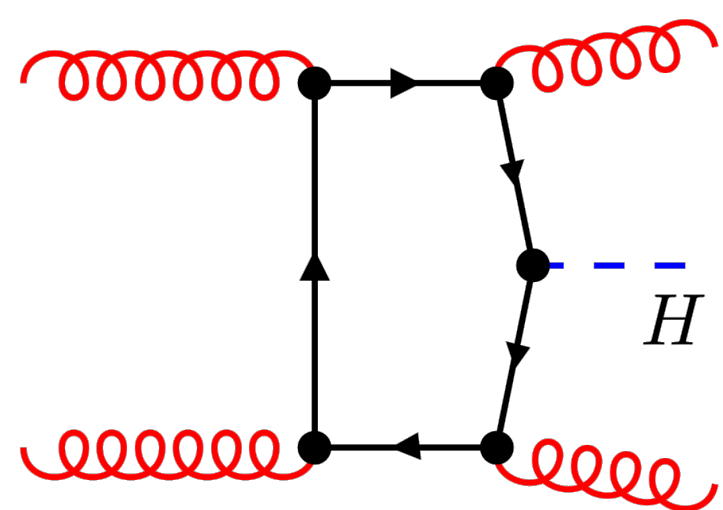


Lindert, Kudashkin, Melnikov, Wever '18 (large p_T)
 Jones, Kerner, Luisoni '18

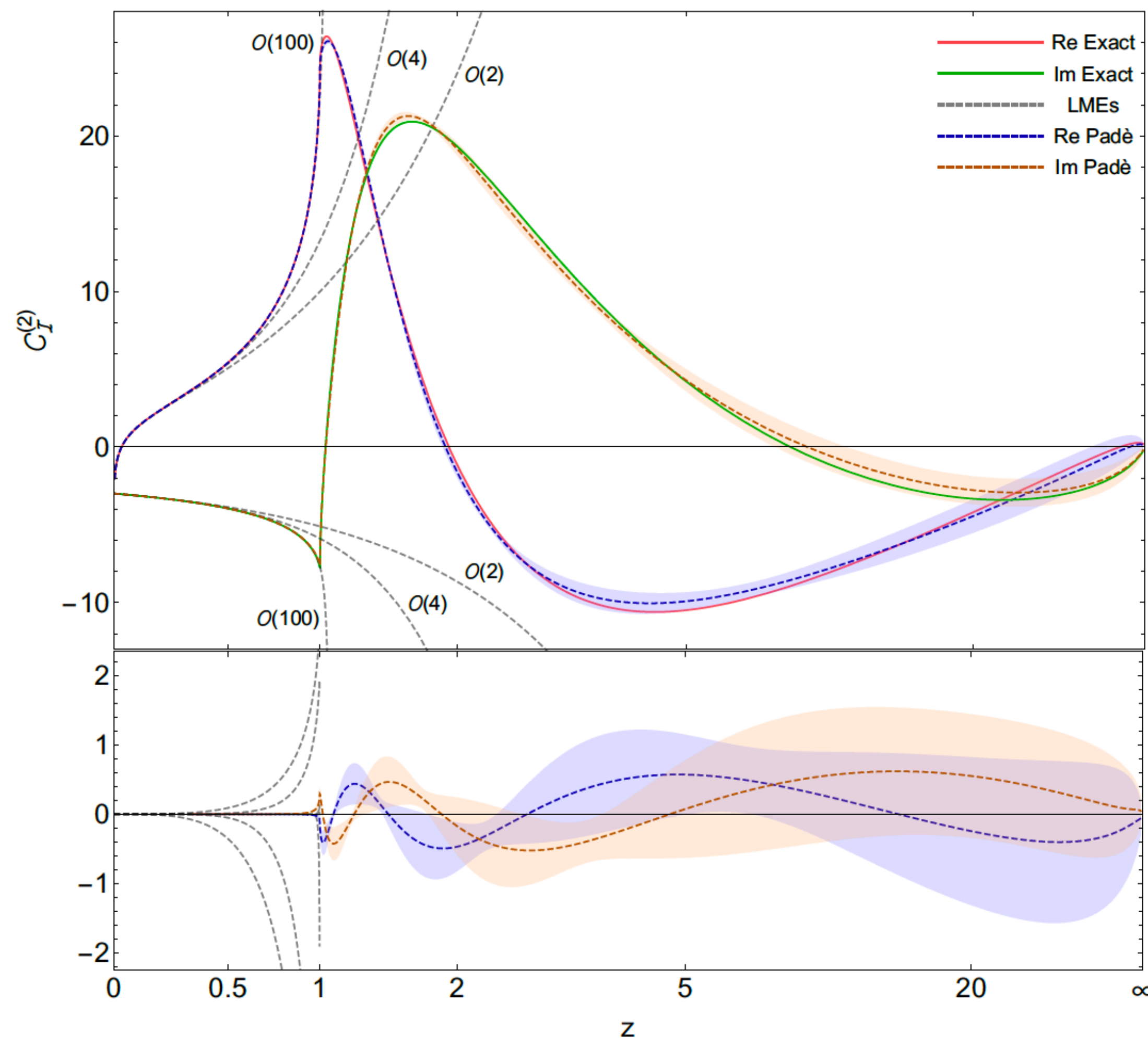
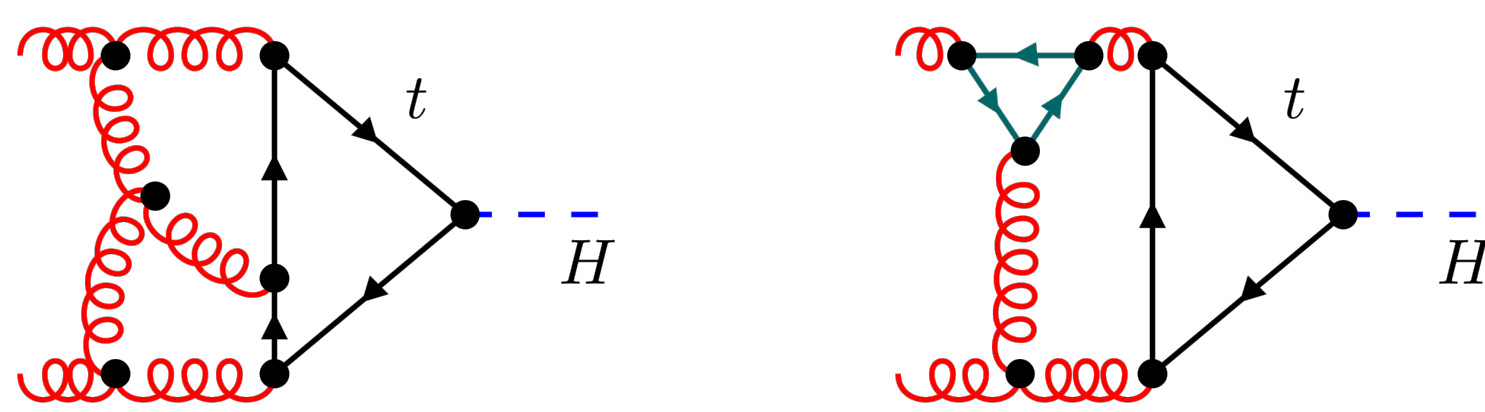




Lindert, Kudashkin, Melnikov, Wever '18 (large p_T)
 Jones, Kerner, Luisoni '18



Del Duca, Kilgore, Schmidt, Oleari, Zeppenfeld '01
 meanwhile: OpenLoops, MCFM, ...



Top quark mass dependence of the Higgs-gluon form factor at three loops

P3H-19-012

Joshua Davies^(a), Ramona Gröber^(b), Andreas Maier^(c),
Thomas Rauh^(d), Matthias Steinhauser^(a),

The light-fermion contribution to the exact Higgs-gluon form factor in QCD

P3H-19-021

Robert V. Harlander¹, Mario Prausa², and Johann Usovitsch³

Exact quark-mass dependence of the Higgs-gluon form factor at three loops in QCD

P3H-20-001

Michał Czakon and Marco Niggetiedt

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
+0.10 pb −1.15 pb	± 0.18 pb	± 0.56 pb	± 0.49 pb	± 0.40 pb	± 0.49 pb
+0.21% −2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$

	α_s^2	α_s^3	α_s^4			
gg	16.30	+ 19.64	+ 8.76	0.2 %	2.8 %	$\rightarrow + 0.5 \%$
qg		1.49	+ 0.84	24.8 %	−1.4 %	$\rightarrow - 0.02 \%$
qq		0.02	+ 0.10	161 %	−50 %	$\rightarrow - 0.1 \%$
total	16.30	+ 21.15	+ 9.79	3.5 %	+1.9 %	$\rightarrow + 0.38 \%$

Exact top-quark mass dependence in hadronic Higgs production

M. Czakon, R.V. Harlander, J. Klappert, M. Niggetiedt
*Institute for Theoretical Particle Physics and Cosmology,
 RWTH Aachen University, 52056 Aachen, Germany*
 (Dated: May 11, 2021)

P3H-21-031

NLO+NNLO: -0.26%

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
$+0.10 \text{ pb}$ -1.15 pb	$\pm 0.18 \text{ pb}$	$\pm 0.56 \text{ pb}$	$\pm 0.49 \text{ pb}$	$\pm 0.40 \text{ pb}$	$\pm 0.49 \text{ pb}$
$+0.21\%$ -2.37%	$\pm 0.27\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$

	α_s^2	α_s^3	α_s^4	
gg	$16.30 + 19.64 + 8.76$			$0.2\% \quad 2.8\% \rightarrow +0.5\%$
qg	$1.49 + 0.84$			$24.8\% \quad -1.4\% \rightarrow -0.02\%$
qq	$0.02 + 0.10$			$161\% \quad -50\% \rightarrow -0.1\%$
total	$16.30 + 21.15 + 9.79$			$3.5\% \quad +1.9\% \rightarrow +0.38\%$

Exact top-quark mass dependence in hadronic Higgs production

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P3H-21-031

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	α_s^2	α_s^3	α_s^4		
gg	16.30	+ 19.64	+ 8.76	0.2 %	2.8 %
qg		1.49	+ 0.84	24.8 %	−1.4 %
qq		0.02	+ 0.10	161 %	−50 %
total	16.30	+ 21.15	+ 9.79	3.5 %	+1.9 %

Exact top-quark mass dependence in hadronic Higgs production

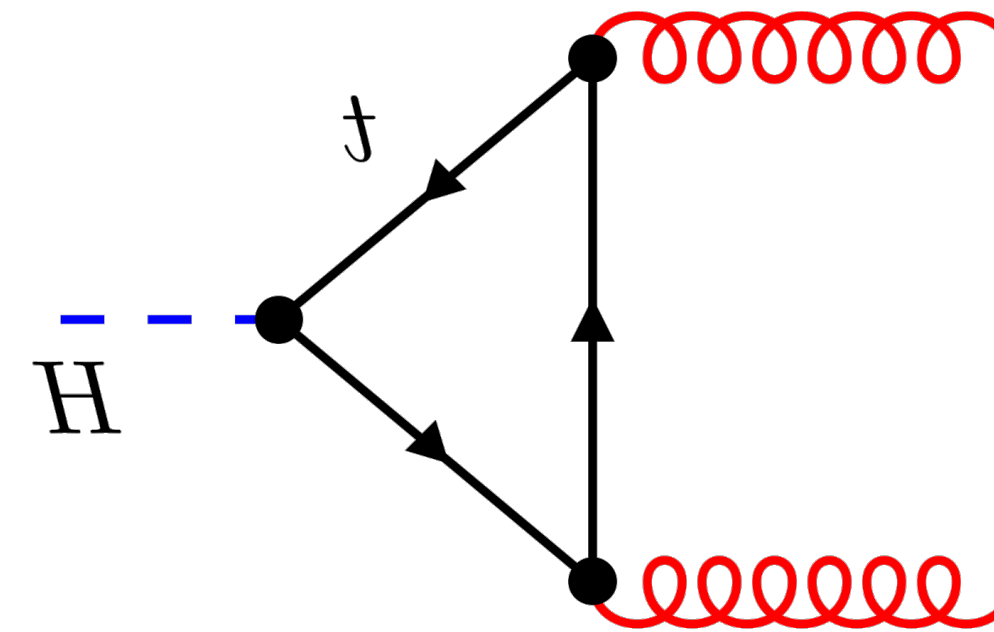
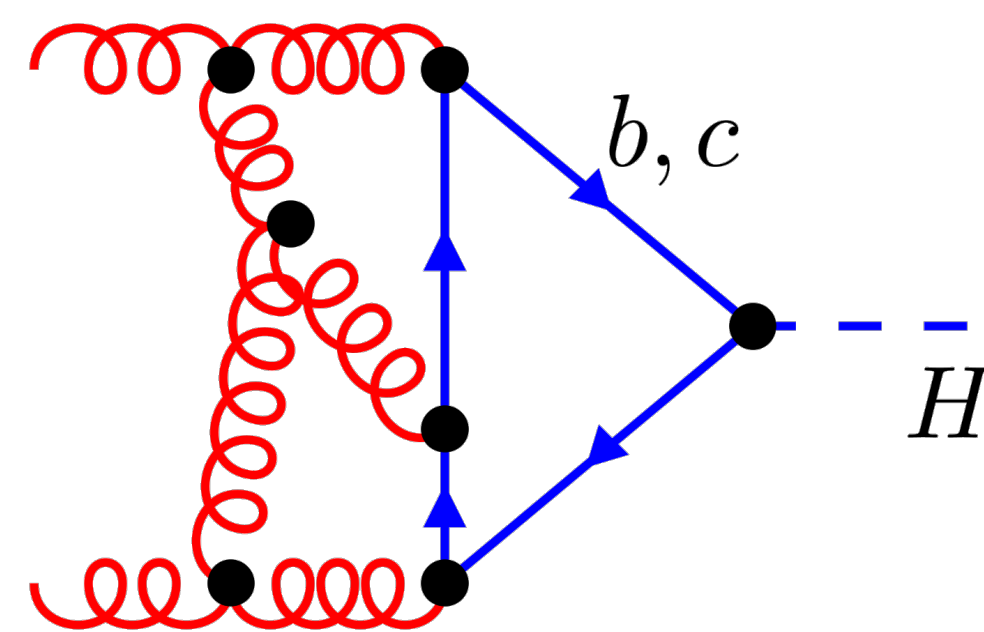
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*Institute for Theoretical Particle Physics and Cosmology,
 RWTH Aachen University, 52056 Aachen, Germany*
 (Dated: May 11, 2021)

YSF

P3H-21-031

NLO+NNLO: −0.26 %

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
+0.10 pb -1.15 pb	± 0.18 pb	± 0.56 pb	± 0.49 pb	± 0.40 pb	± 0.49 pb
+0.21% -2.37%	$\pm 0.27\%$ ✓	$\pm 1.16\%$	$\pm 1\%$ ✓	$\pm 0.83\%$	$\pm 1\%$ ✓



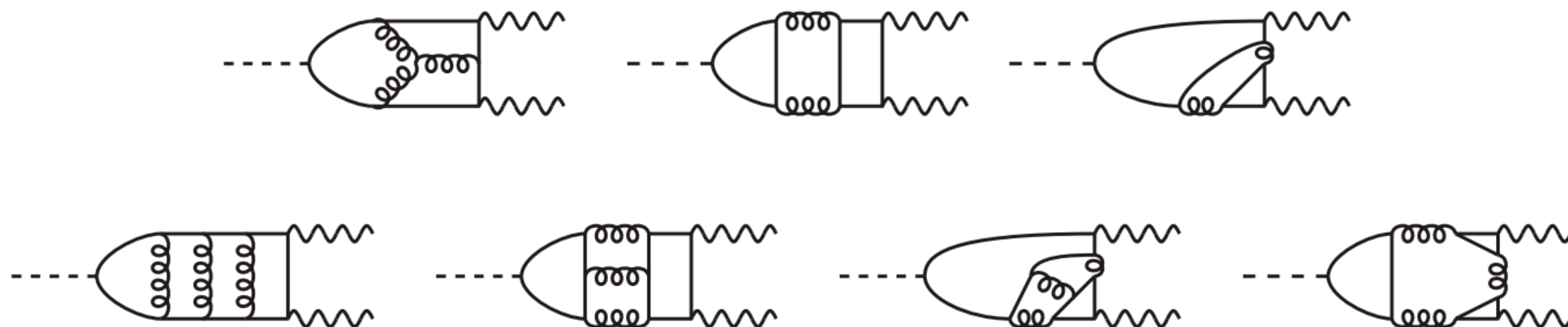
intricate structure of $\ln \frac{m_b}{m_H}$

Melnikov, Penin '16

Anastasiou, Penin '20

Liu, Mecaj, Neubert, Wang '20

What I could not talk about...



Exact quark-mass dependence of the Higgs-photon form factor at three loops in QCD

P3H-20-050

Marco Niggetiedt

3-loop exact

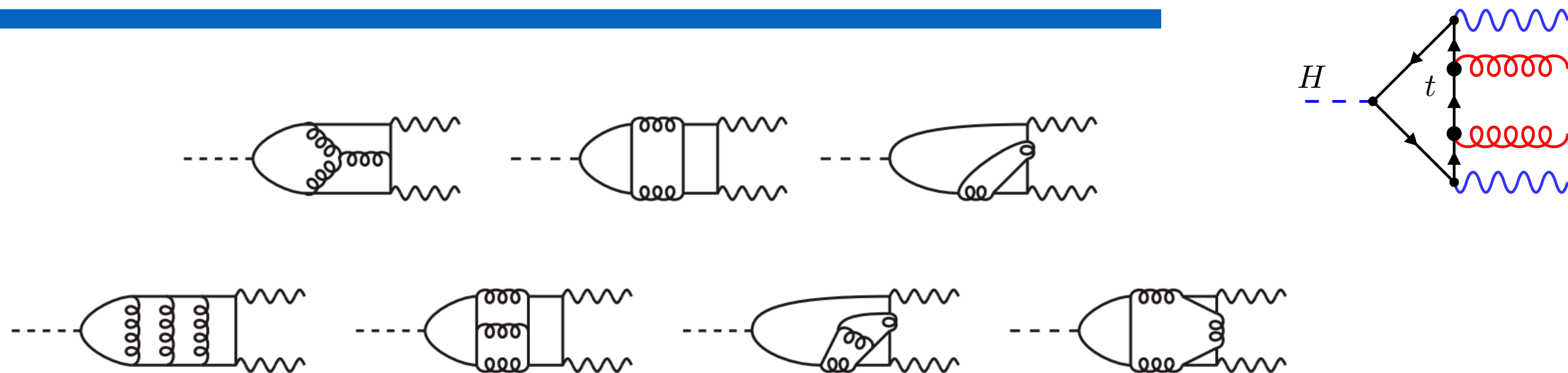
Higgs boson decay into photons at four loops

P3H-21-028

Joshua Davies¹ and Florian Herren^{2*}

4-loop, expansion in $1/m_t$

What I could not talk about...



Exact quark-mass dependence of the Higgs-photon form factor at three loops in QCD

P3H-20-050

Marco Niggetiedt

3-loop exact

Higgs boson decay into photons at four loops

P3H-21-028

Joshua Davies¹ and Florian Herren^{2*}

4-loop, expansion in $1/mt$

NNLO QCD corrections to three-photon production at the LHC

P3H-19-041

Herschel A. Chawdhry,^a Michał Czakon,^b Alexander Mitov,^a Rene Poncelet^a

Two-loop leading-colour QCD helicity amplitudes for two-photon plus jet production at the LHC

P3H-21-014

Herschel A. Chawdhry,^a Michał Czakon,^b Alexander Mitov,^c Rene Poncelet^c

NNLO QCD corrections to diphoton production with an additional jet at the LHC

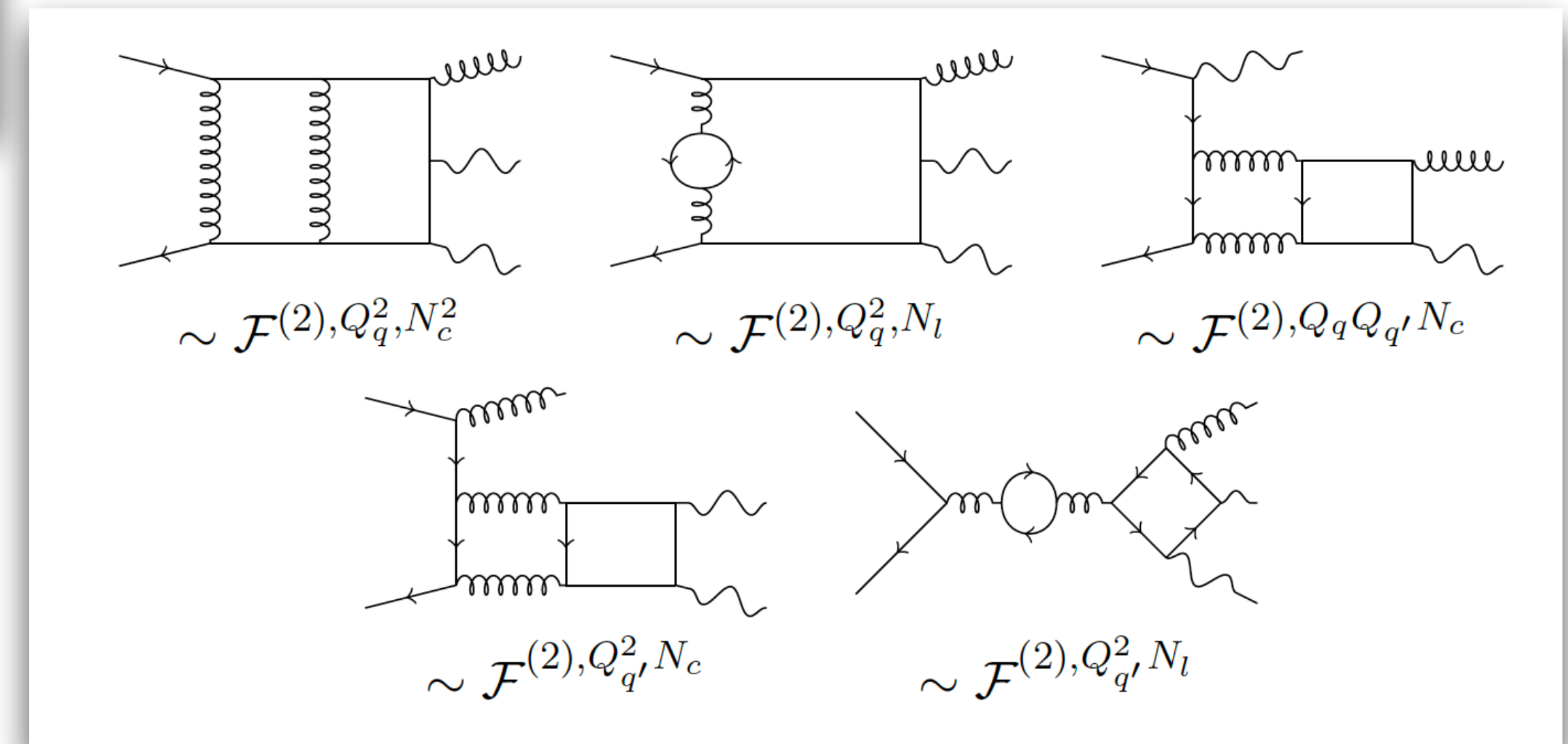
P3H-21-032

Herschel A. Chawdhry,^a Michał Czakon,^b Alexander Mitov,^c Rene Poncelet^c

Two-loop leading-color helicity amplitudes for three-photon production at the LHC

P3H-21-084

Herschel A. Chawdhry,^a Michał Czakon,^b Alexander Mitov,^c Rene Poncelet^c



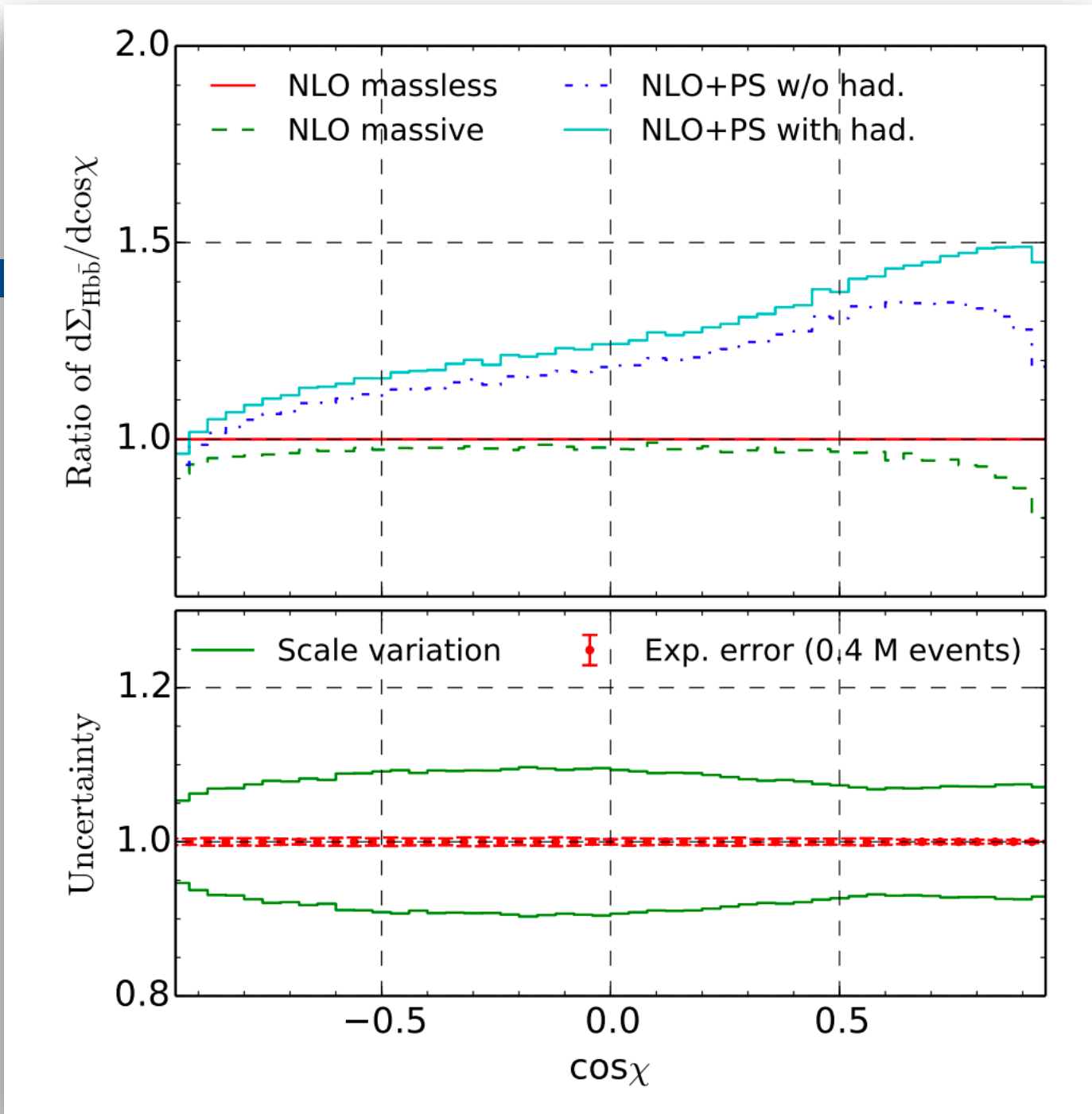
also: Agarwal, Buccioni, von Manteuffel, Tancredi '21

What I could not talk about...

Energy-energy correlation in hadronic Higgs decays: analytic results and phenomenology at NLO

P3H-20-060

Jun Gao,^{a,b} Vladyslav Shtabovenko,^{c,e} Tong-Zhi Yang,^{d,e}



Bottom quark mass effects in associated WH production

with $H \rightarrow b\bar{b}$ decay through NNLO QCD
P3H-20-009

Arnd Behring,^{1,*} Wojciech Bizoń,^{1,2,†} Fabrizio Caola,^{3,‡}

Kirill Melnikov,^{1,§} and Raoul Röntschi,^{4,¶}

Higgs decay into massive b -quarks at NNLO QCD in the nested soft-collinear subtraction scheme

P3H-19-047

Arnd Behring^a, Wojciech Bizoń^{a,b}.

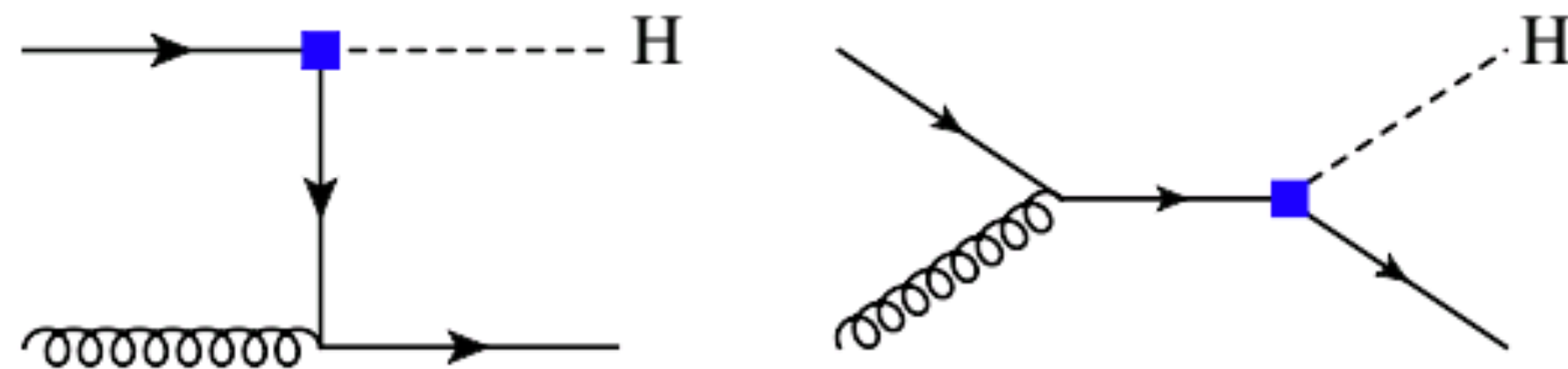
Order	b quarks	σ_{fid} [fb]	$\sigma_{\text{fid}}(\text{boosted})$ [fb]
LO	massive	$22.623^{+0.845}_{-1.047}$	$3.735^{+0.000}_{-0.016}$
	massless	$22.501^{+0.796}_{-1.007}$	$3.638^{+0.000}_{-0.009}$
NLO	massive	$25.364(1)^{+0.778}_{-0.756}$	$4.586(1)^{+0.158}_{-0.141}$
	massless	$24.421(1)^{+0.852}_{-0.879}$	$4.333(1)^{+0.165}_{-0.154}$
NNLO	massive	$24.225(4)^{+0.642}_{-0.742}$	$4.530(2)^{+0.071}_{-0.096}$
	massless	$22.781(3)^{+0.791}_{-0.898}$	$4.207(1)^{+0.097}_{-0.116}$

What I could not talk about...

On the interference of ggH and $c\bar{c}H$ Higgs production mechanisms and the determination of charm Yukawa coupling at the LHC

P3H-21-010

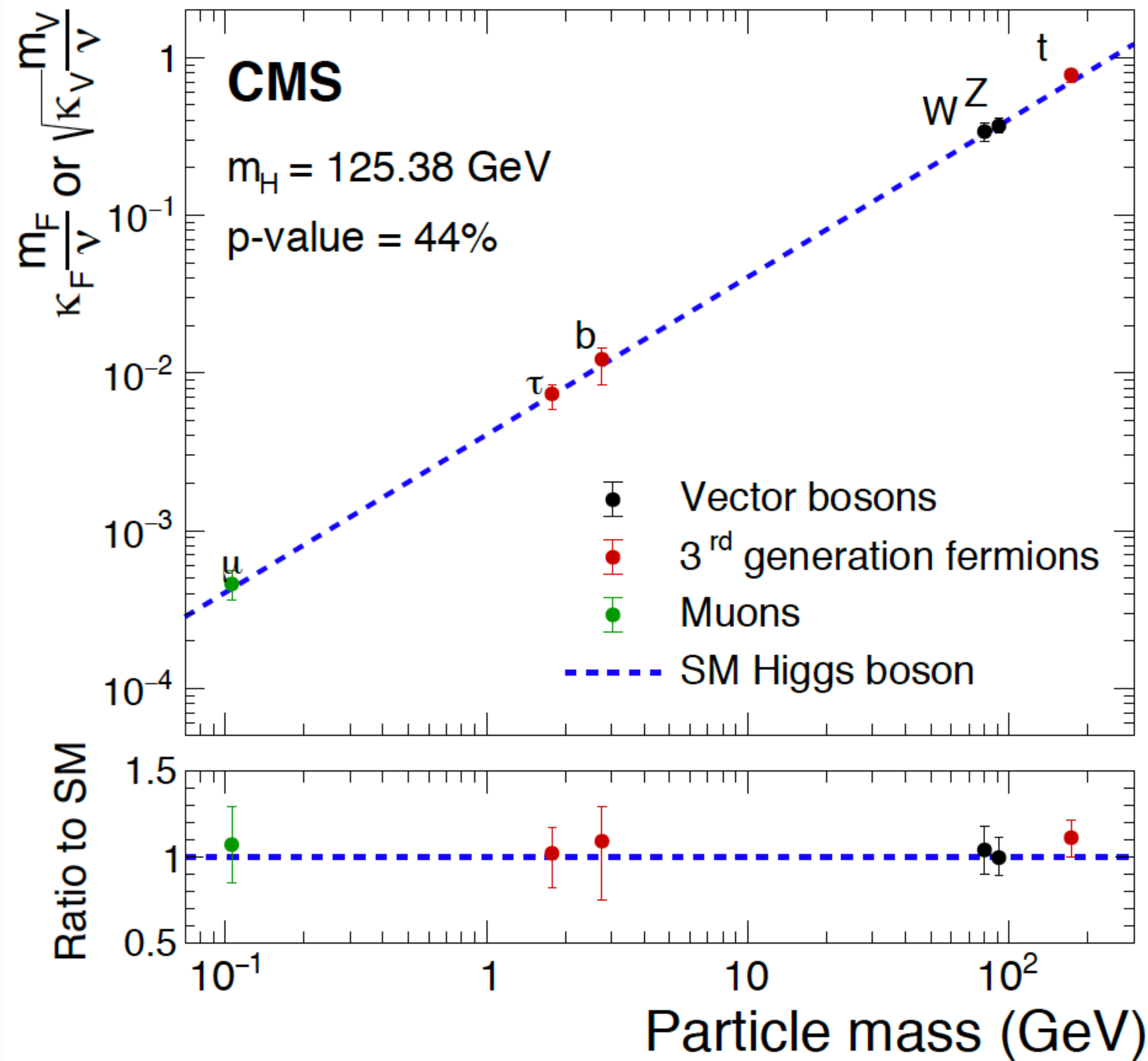
Wojciech Bizoń,^{a,b} Kirill Melnikov,^a Jérémie Quarroz^a



(a) Yukawa coupling

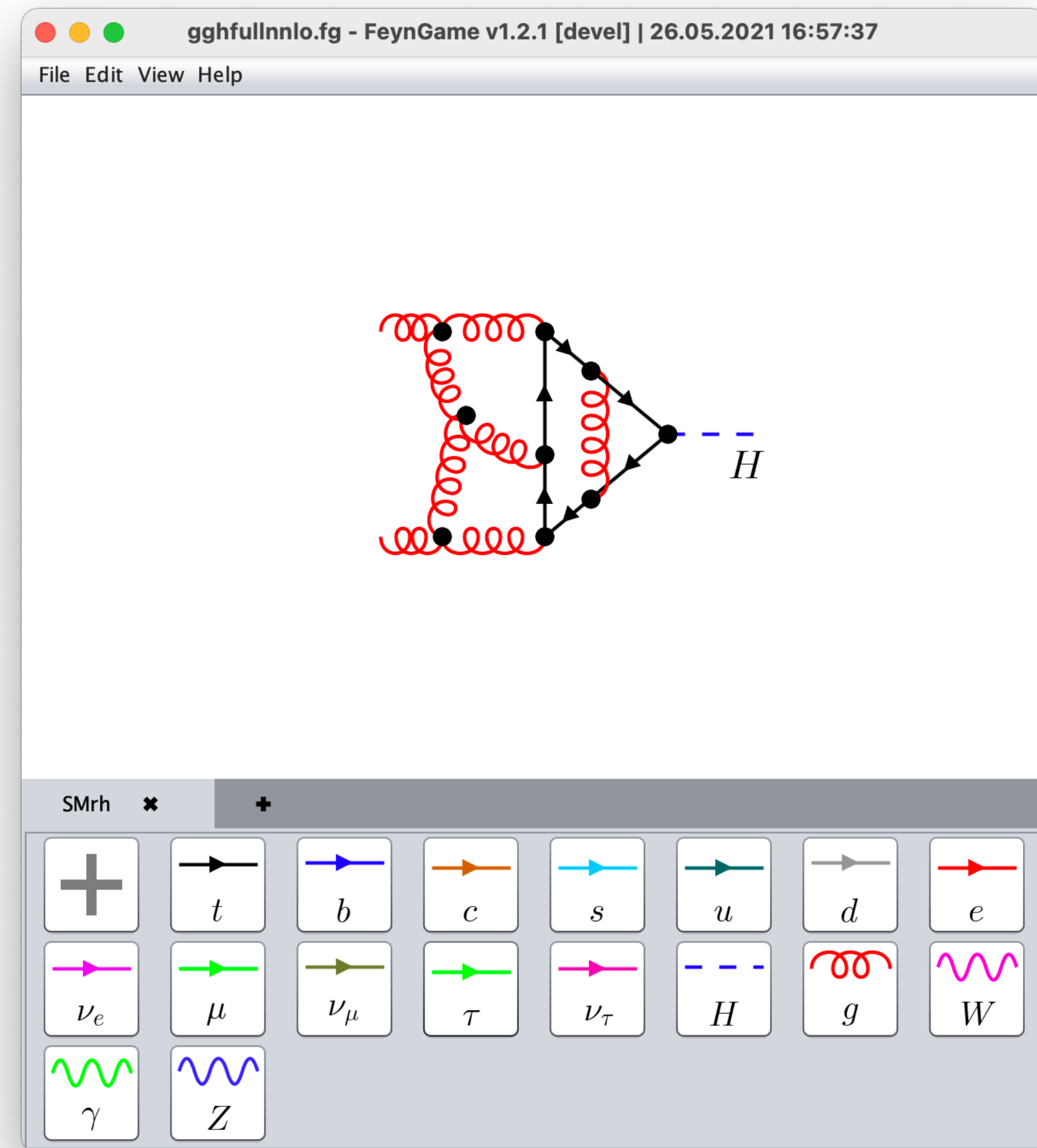
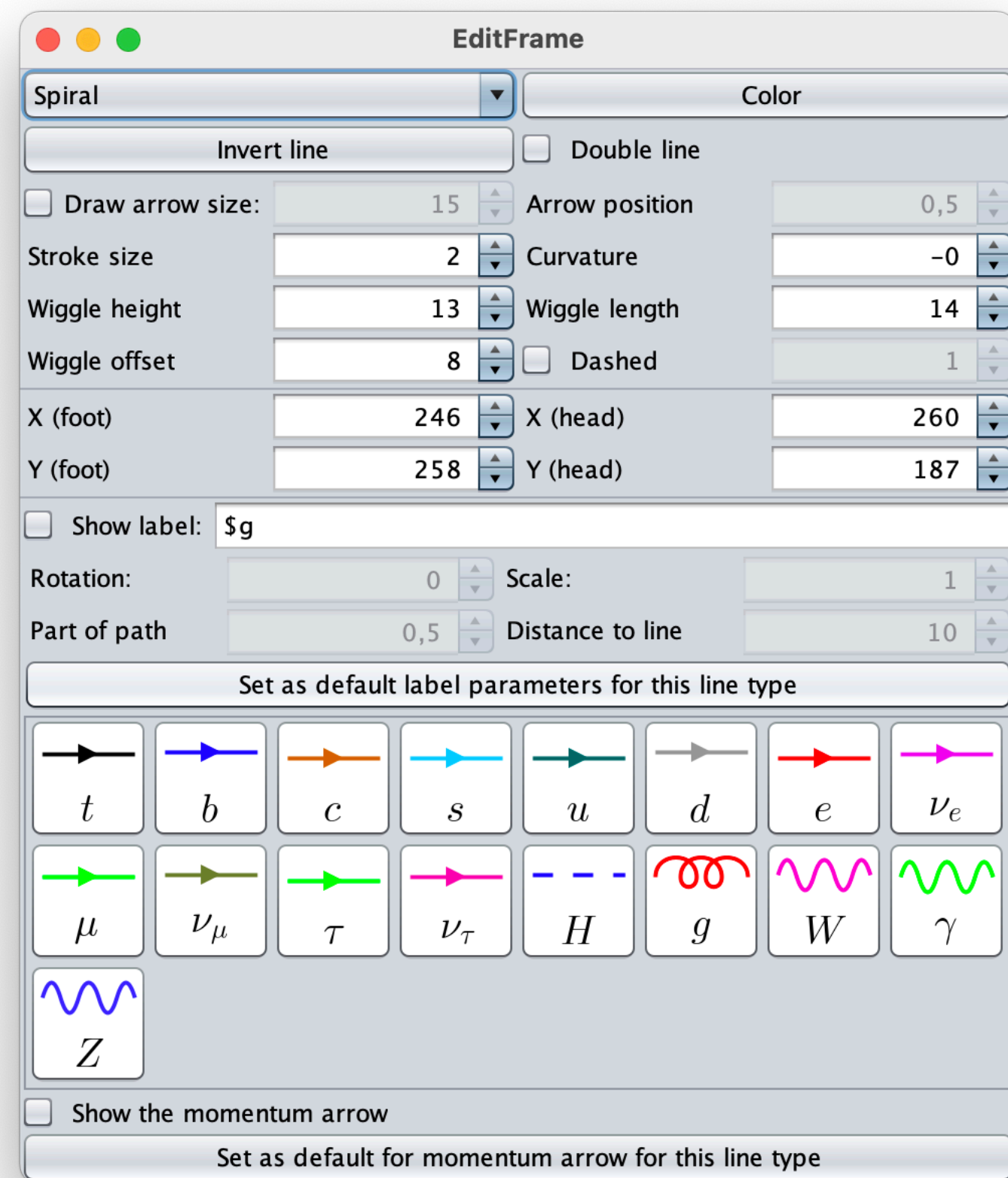
(b) Effective ggH vertex

JHEP 2101 (2021) 148 35.9-137 fb⁻¹ (13 TeV)



interaction is multiplied by a factor $-\frac{3}{2}$ rather than $\frac{3}{2}$. Of course our model has too many arbitrary features for these predictions to be taken very seriously, but it is worth keeping in mind that the standard calculation⁸ of the

Weinberg '67



FeynGame

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Thank you!