

# $(g-2)_\mu$ , B-anomalies and DM: A loop model tale

M. Fedele

based on [arXiv:1904.05890](#), [2103.09835](#), [2104.03228](#) in collaboration with:  
G. Arcadi, P. Arnan, L. Calibbi, A. Crivellin & F. Mescia

# Summary

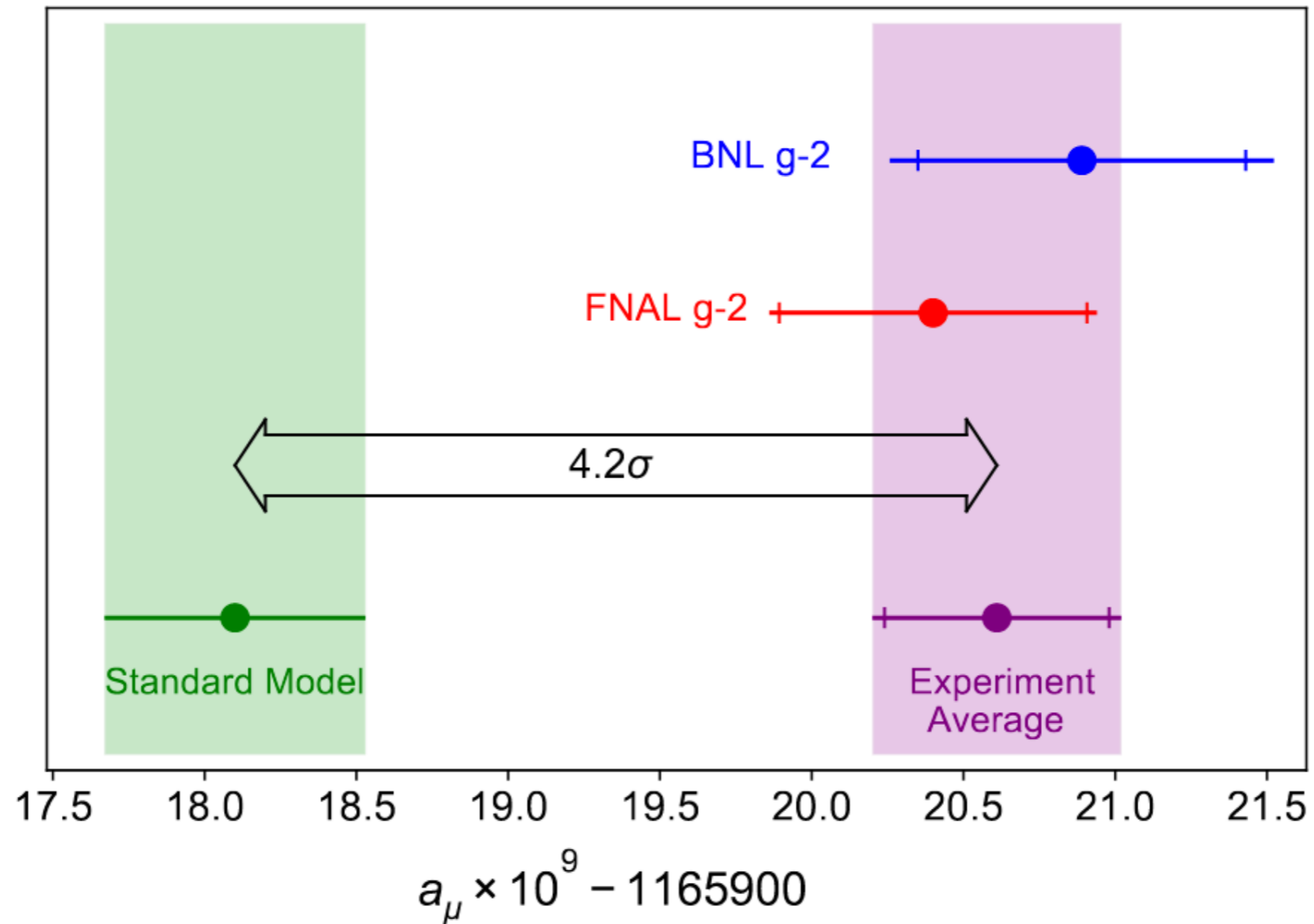
- *Introduction*
- *$g-2$  and  $B$ -anomalies*
- *$B$ -anomalies and DM*
- *All together now!*

# Summary

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# The anomalous muon (g-2)

Striking discrepancy among Theory recommended value and exp. measurements



Potentially the single most striking cry for NP observed so far!

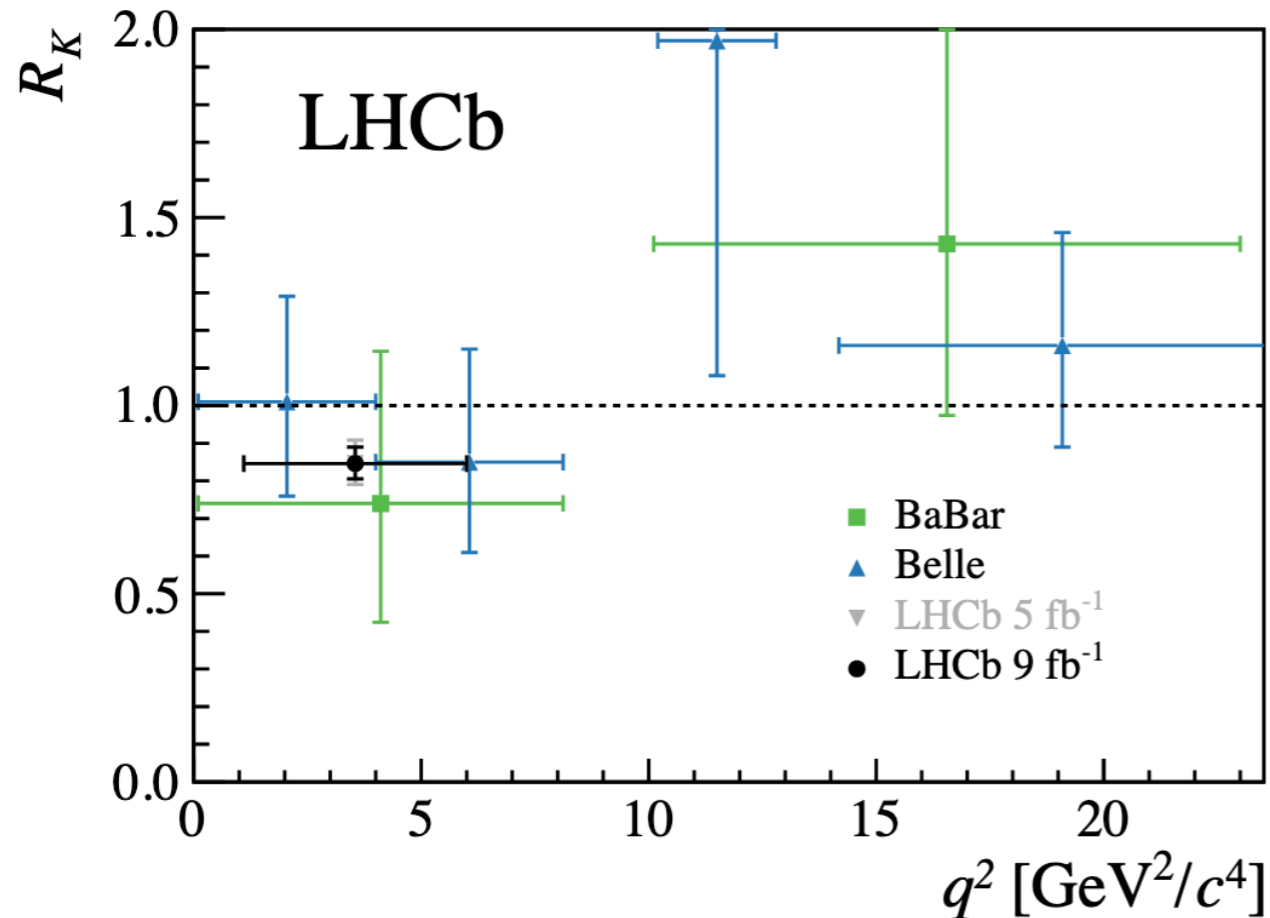


# Opportunities with Semi-Leptonic B Decays

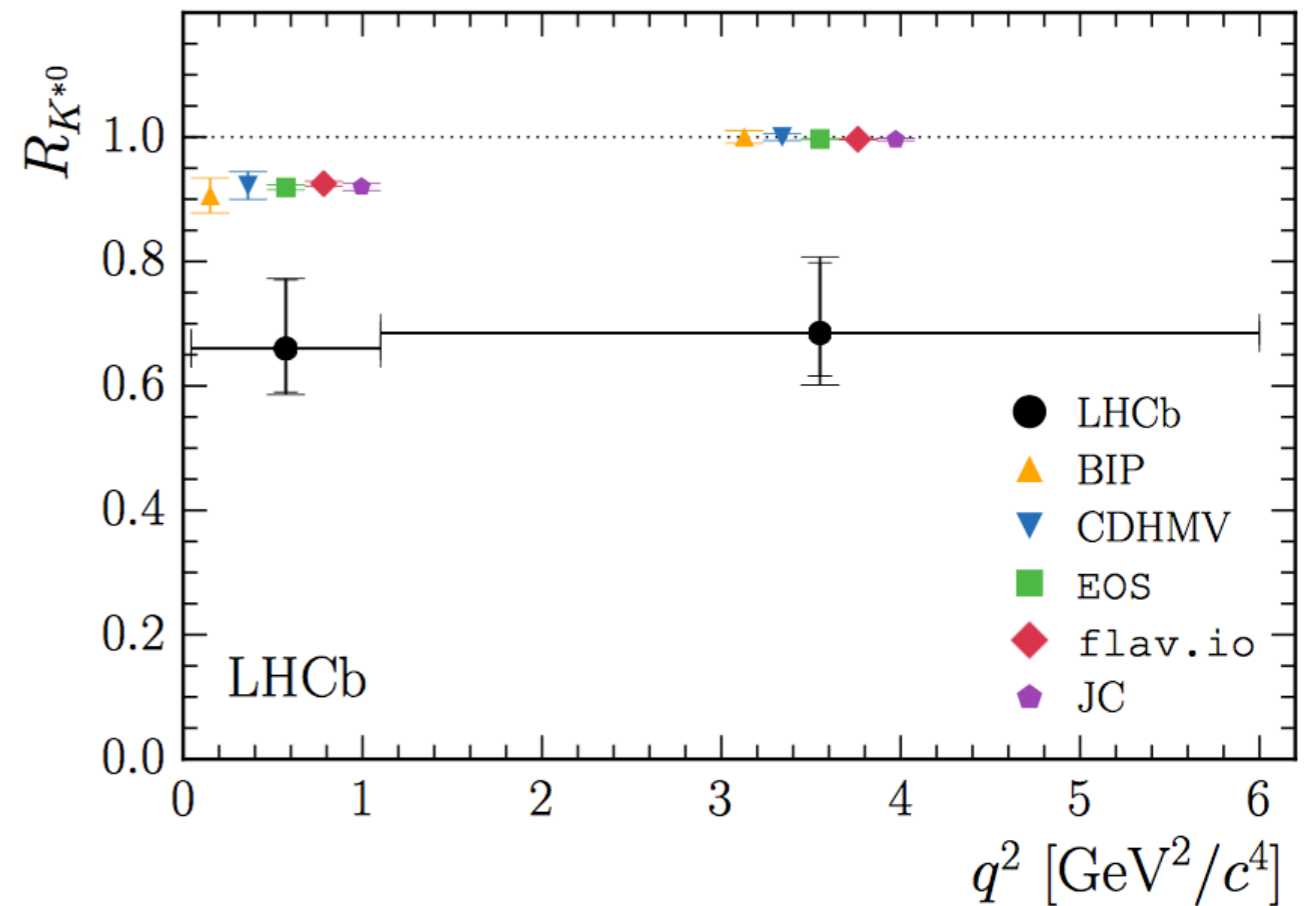
No tree-level flavour changing neutral currents (FCNC) in the SM

&

Intriguing set of “Anomalies” in data of exclusive B rare Decays



$\sim 3.1 \sigma$



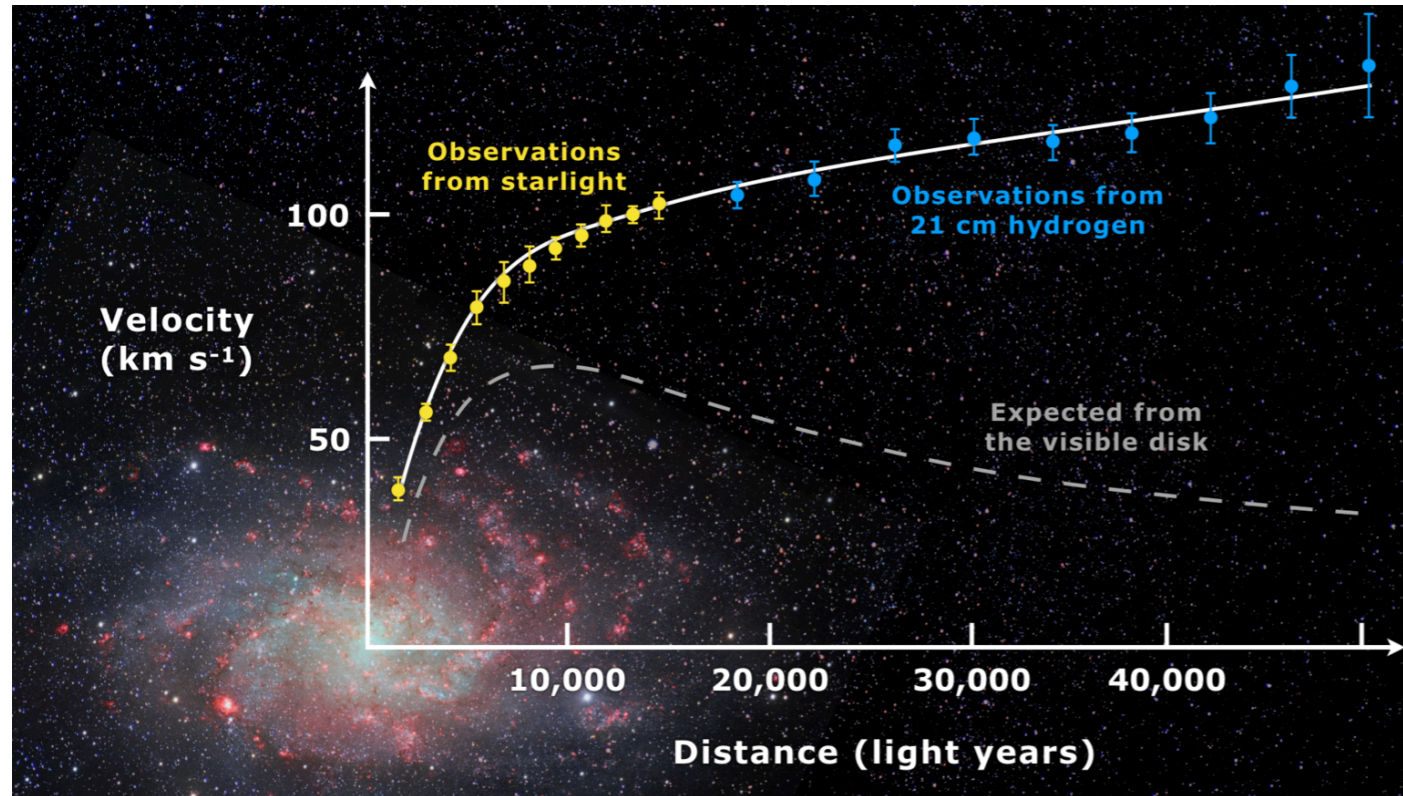
$\sim 2.5 \sigma$

$$R_{K^{(*)}} = Br(B \rightarrow K^{(*)} \mu \mu) / Br(B \rightarrow K^{(*)} ee)$$

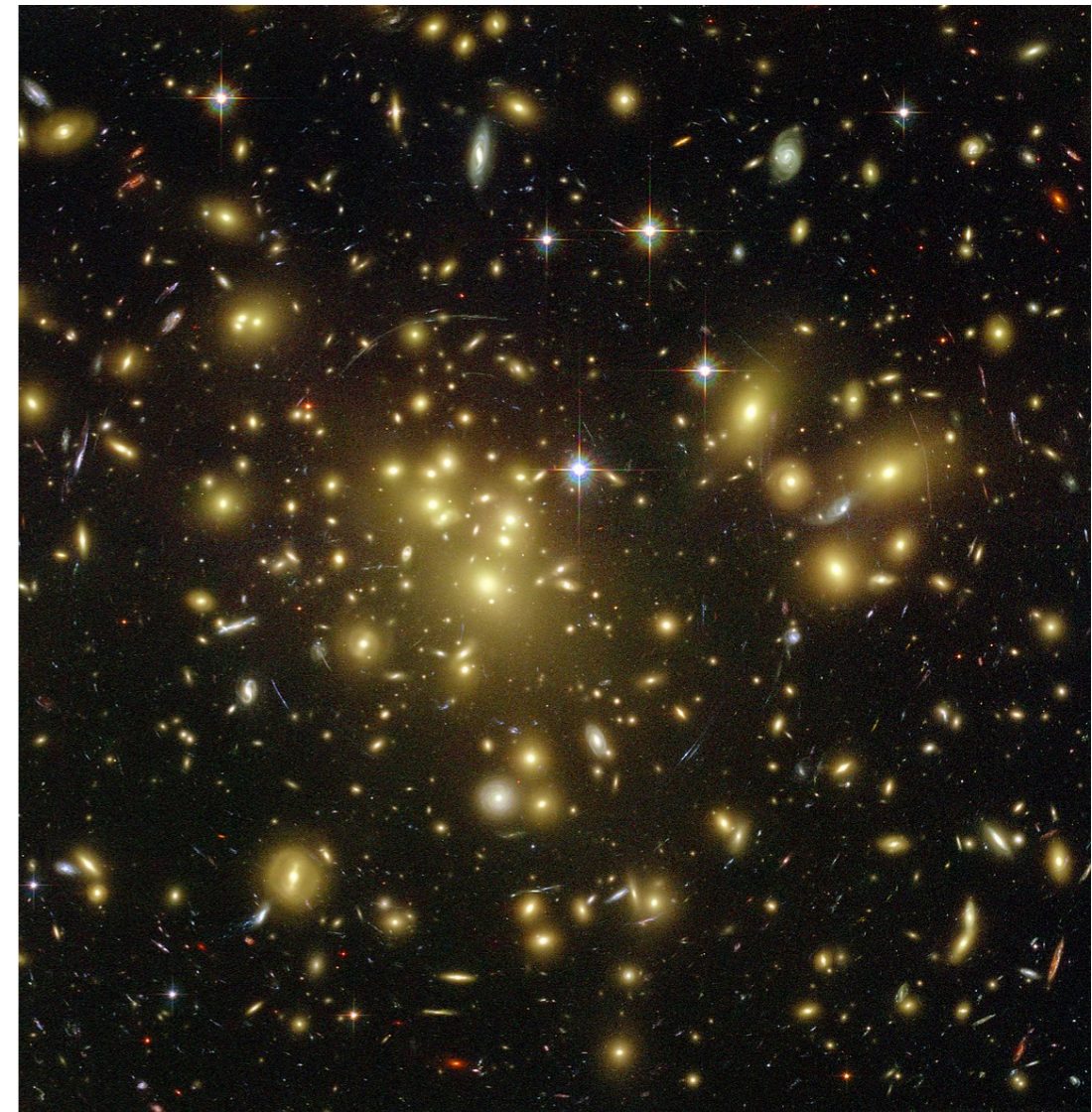
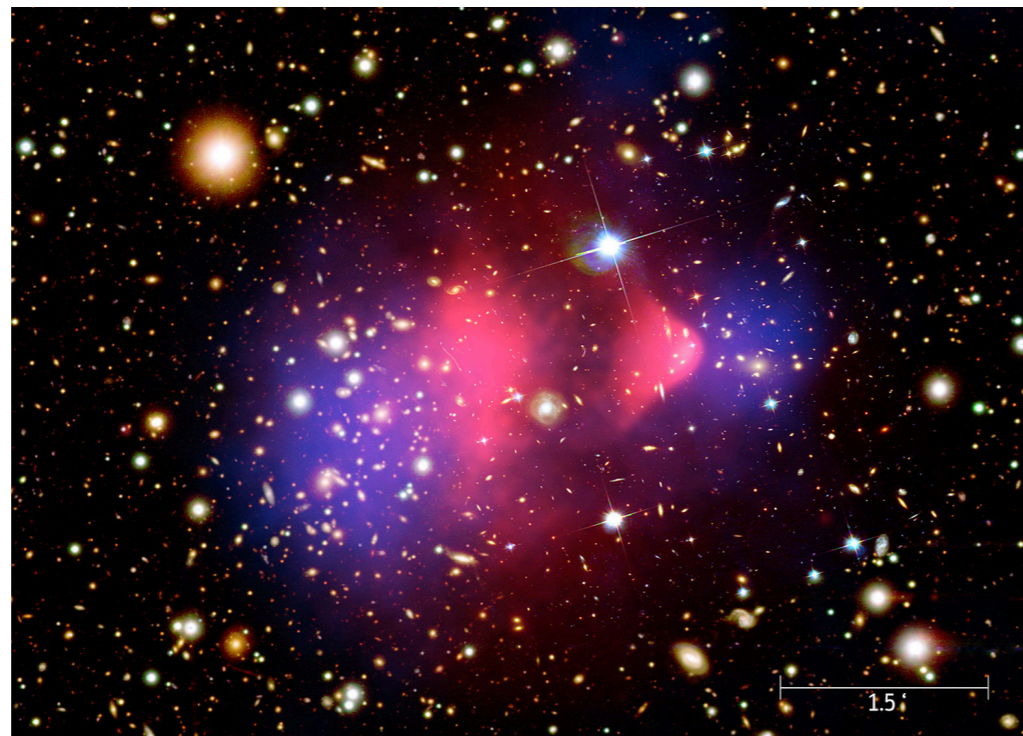


# Evidence of DM in the Universe

Multiple evidences of presence of DM from Astrophysical observations



Galaxy rotation curves



Gravitational lensing

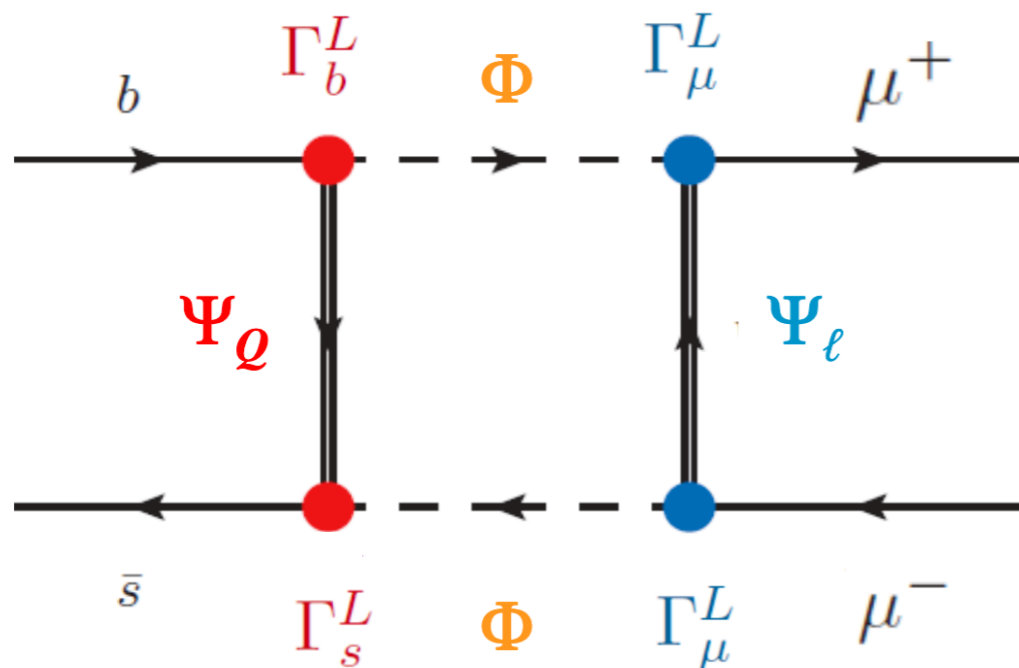
Bullet Cluster



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# Loop Models

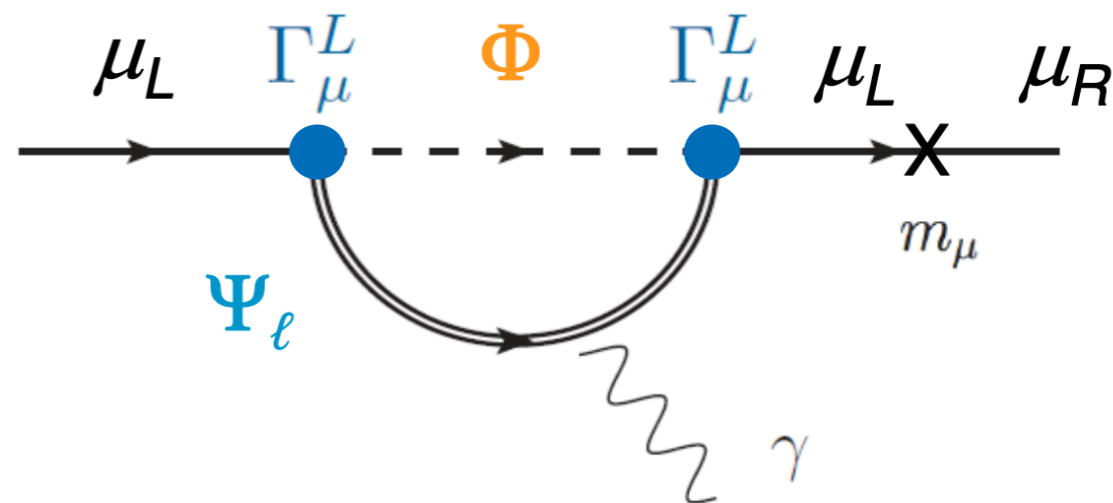
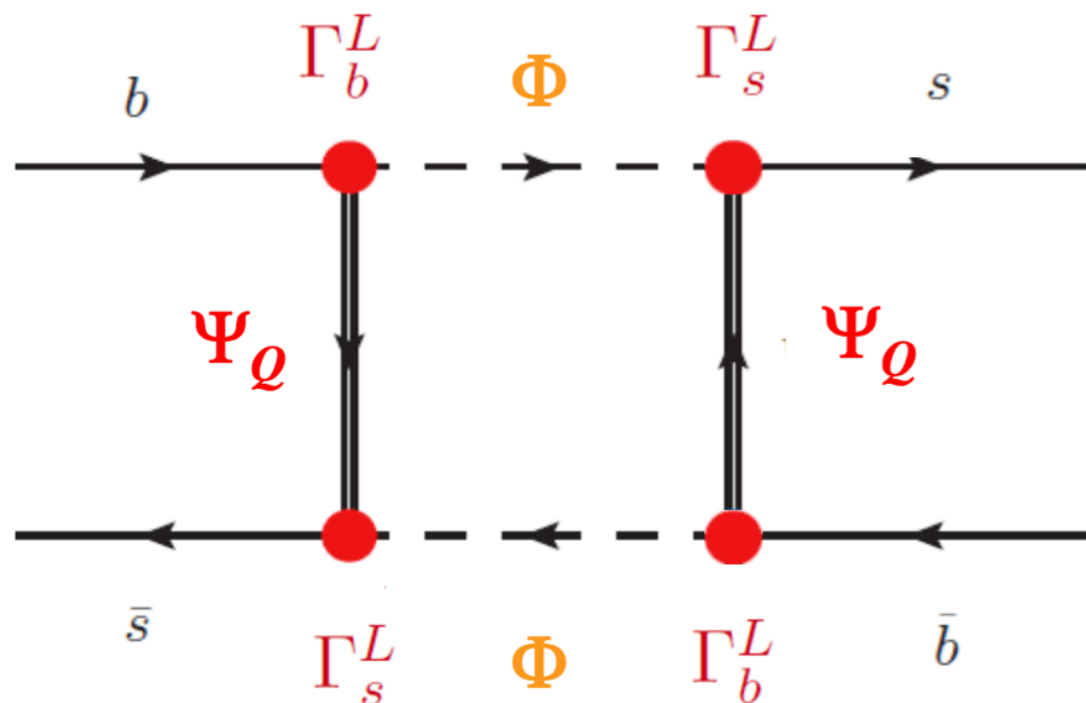


One scalar and 2 vector-like fermions (or vice versa)

$$\Rightarrow \boxed{C9 = -C10}$$

Gripaios, Nardecchia, Renner '15  
 Arnan, Crivellin, Hofer, Mescia '16

Induces contributions to  $\Delta M_s$  and muon  $g-2$



It is not possible to address everything with  $O(1)$  couplings and viable masses

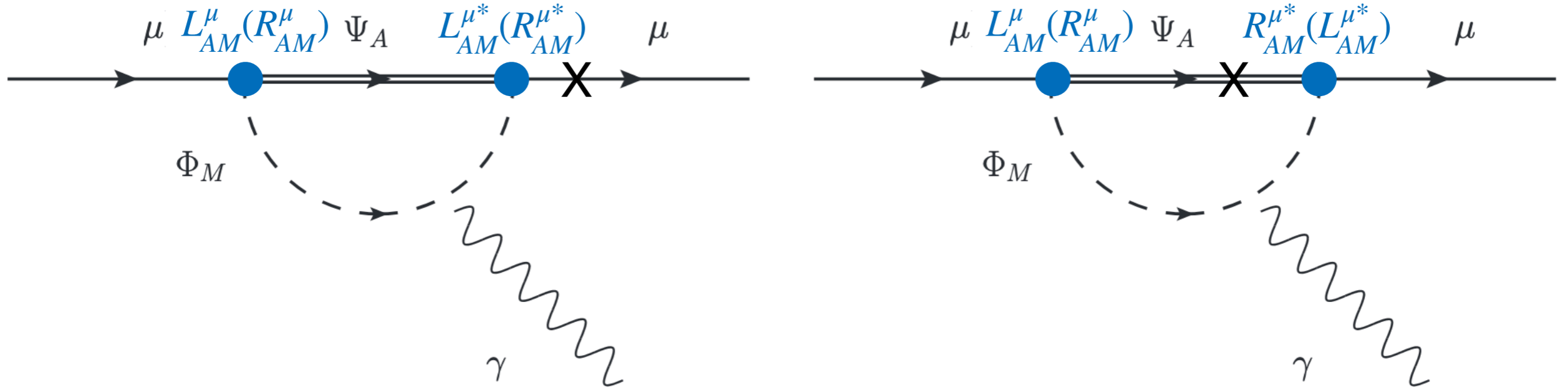
# A Generic Loop Model including RH couplings

$$\mathcal{L}_{\text{int}} = \left[ \bar{\Psi}_A \left( L_{AM}^b P_L b + L_{AM}^s P_L s + L_{AM}^\mu P_L \mu \right) \Phi_M + \bar{\Psi}_A \left( R_{AM}^b P_R b + R_{AM}^s P_R s + R_{AM}^\mu P_R \mu \right) \Phi_M \right] + \text{h.c.}$$

$\Psi_A, \Phi_M$  : Generic lists containing an arbitrary number of fields

$L_{AM}^{b,s,\mu}, R_{AM}^{b,s,\mu}$  : Generic matrices in (A-M) space

- A and M also include implicitly SU(3) indices
- Non-vanishing entries of the coupling matrices ensure the preservation of colour and electric charge



$$\Delta a_\mu = \frac{\chi a_\mu m_\mu^2}{8\pi^2 m_{\Phi_M}^2} \left[ (L_{AM}^{\mu*} L_{AM}^\mu + R_{AM}^{\mu*} R_{AM}^\mu) (Q_{\Phi_M} \tilde{F}_7(x_{AM}) - Q_{\Psi_A} F_7(x_{AM})) \right. \\ \left. + (L_{AM}^{\mu*} R_{AM}^\mu + R_{AM}^{\mu*} L_{AM}^\mu) \frac{2m_{\Psi_A}}{m_\mu} (Q_{\Phi_M} \tilde{G}_7(x_{AM}) - Q_{\Psi_A} G_7(x_{AM})) \right]$$

Additional term induced by SU(2) breaking, and chirally enhanced

# 4th Generation Model

$$\begin{aligned}
L^{4\text{th}} = & \sum_i \left( \Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \Gamma_{u_i}^R \bar{\Psi}_u P_R u_i + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i \right) \Phi + \text{h.c.} \\
& + \sum_{C=L,R} \left( \lambda_C^U \bar{\Psi}_q P_C \tilde{h} \Psi_u + \lambda_C^D \bar{\Psi}_q P_C h \Psi_d + \lambda_C^E \bar{\Psi}_\ell P_C h \Psi_e \right) + \text{h.c.} \\
& + \sum_{F=q,\ell,u,d,e} M_F \bar{\Psi}_F \Psi_F + \kappa h^\dagger h \Phi^\dagger \Phi + m_\Phi^2 \Phi^\dagger \Phi
\end{aligned}$$

We start writing down the most general Lagrangian before EWSB including a 4th vector-like generation and a neutral scalar

	$SU(3)$	$SU(2)$	$U(1)$	$U'(1)$
$\Psi_q$	3	2	1/6	$Z$
$\Psi_u$	3	1	2/3	$Z$
$\Psi_d$	3	1	-1/3	$Z$
$\Psi_\ell$	1	2	-1/2	$Z$
$\Psi_e$	1	1	-1	$Z$
$\Phi$	1	1	0	$-Z$

NB. We work in the basis with diagonal down-type quarks

# 4th Generation Model

$$\begin{aligned}
 L^{4\text{th}} = & \sum_i \left( \Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \cancel{\Gamma_{u_i}^R \bar{\Psi}_u P_R u_i} + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i \right) \Phi + \text{h.c.} \\
 & + \sum_{C=L,R} \left( \cancel{\lambda_C^U \bar{\Psi}_q P_C \tilde{h} \Psi_u} + \cancel{\lambda_C^D \bar{\Psi}_q P_C h \Psi_d} + \lambda_C^E \bar{\Psi}_\ell P_C h \Psi_e \right) + \text{h.c.} \\
 & + \sum_{F=q,\ell,u,d,e} M_F \bar{\Psi}_F \Psi_F + \kappa h^\dagger h \Phi^\dagger \Phi + m_\Phi^2 \Phi^\dagger \Phi
 \end{aligned}$$

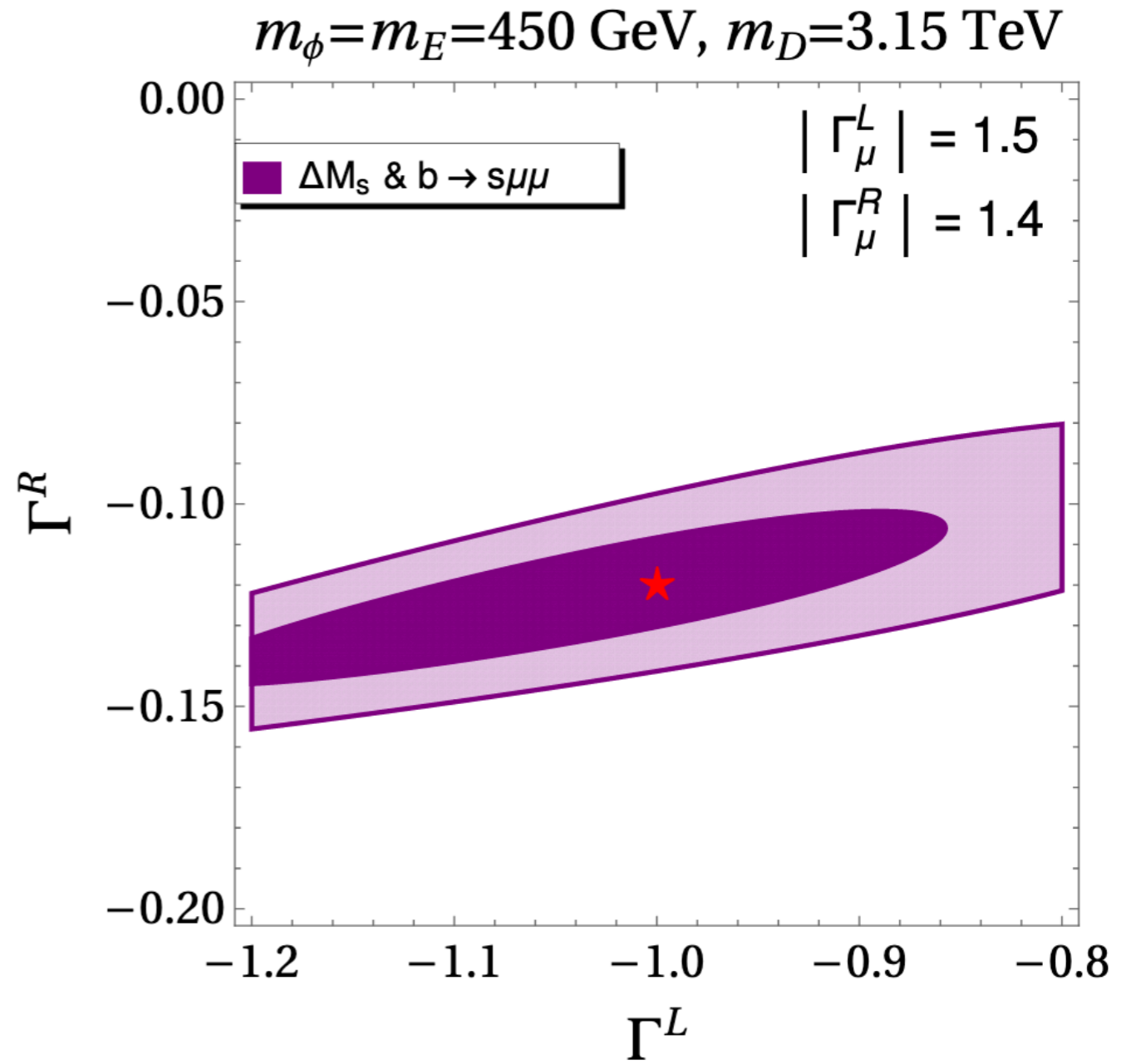
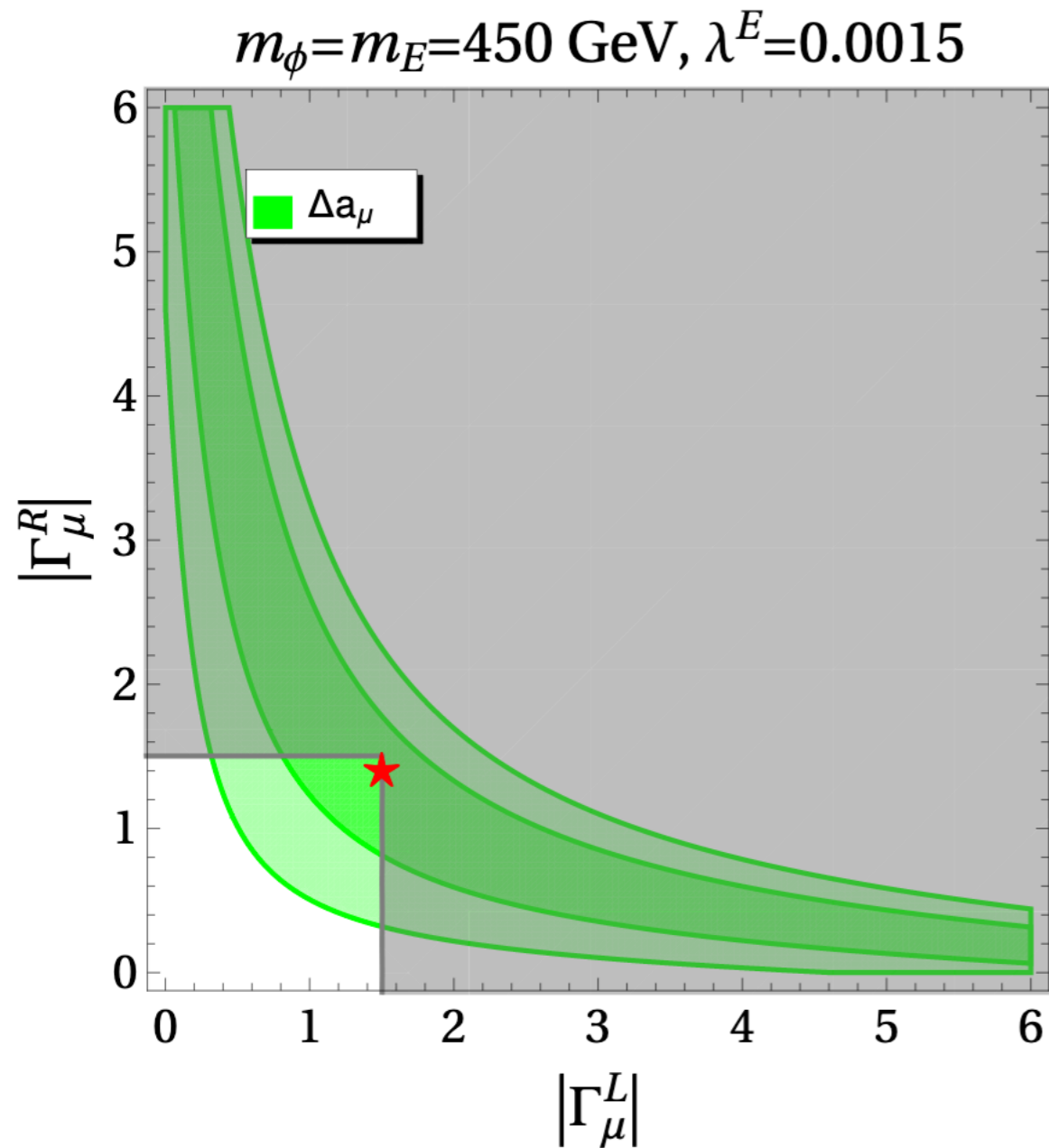
We're interested only in couplings to bottom, strange, muon

We neglect SU(2) breaking for down-type quarks  
(responsible for phenomenological un-relevant scalar/tensor operators)

We need to diagonalize the lepton sector!



# Fit to the Observables



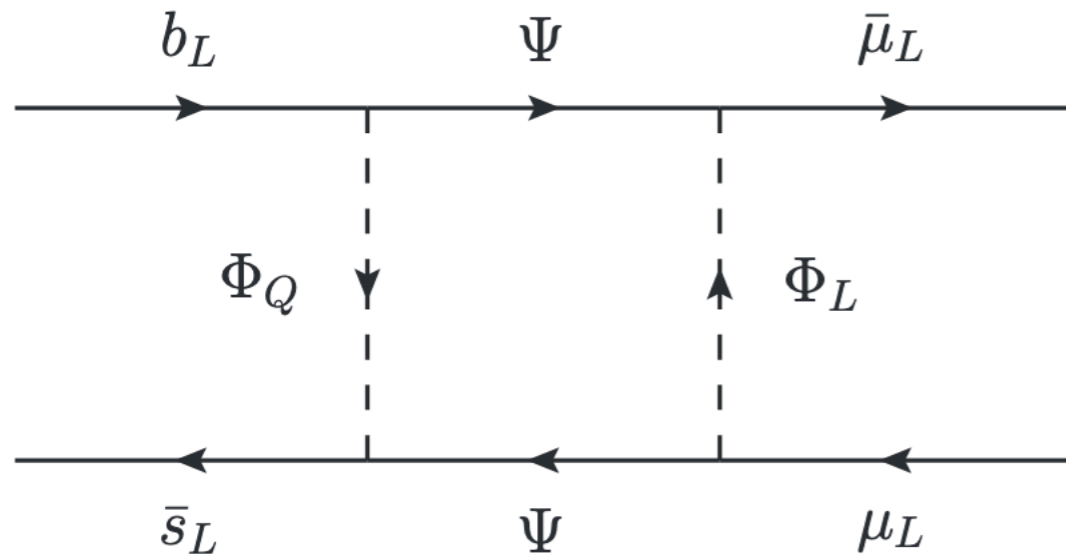
Right-handed coupling (in both sectors) and SU(2) breaking  
(in the muon sector) both fundamental!

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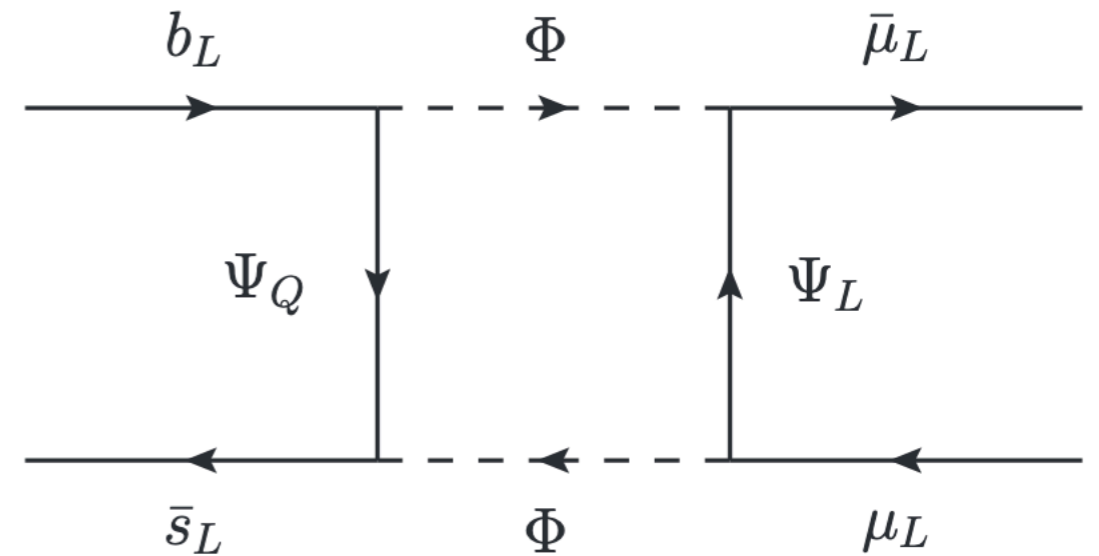
# Systematic Studies of All Possible Loop Models

We're not addressing the muon (g-2), so we focus here on LH couplings (only 3 fields)



*Class F* – Fermion mediator

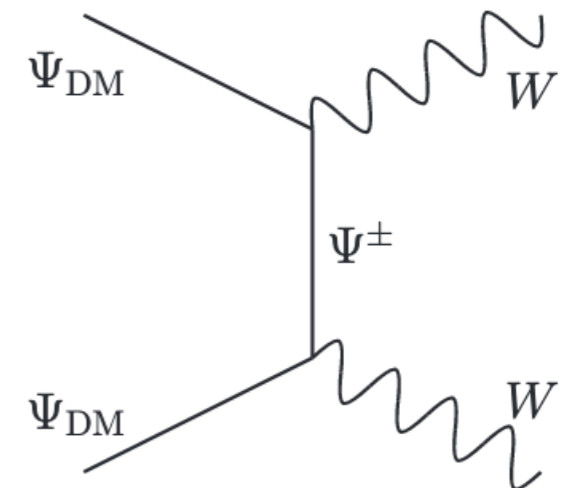
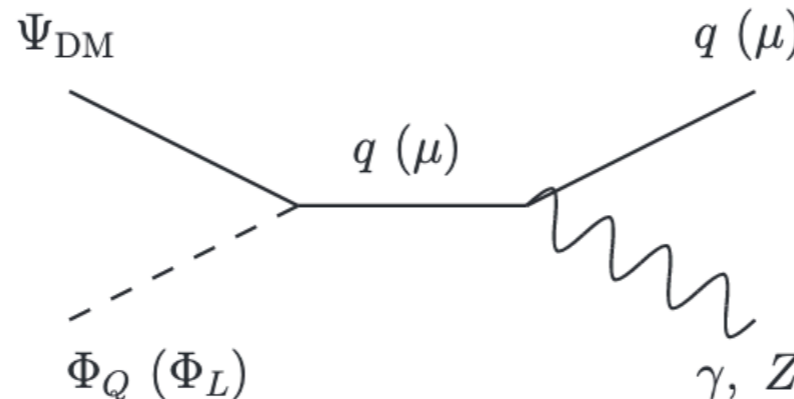
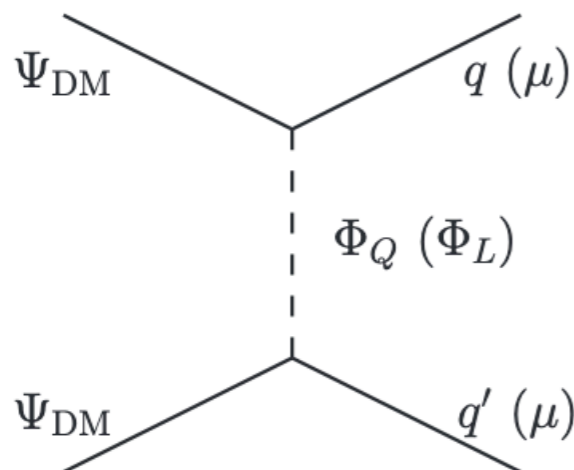
$$\mathcal{L}_F \supset \Gamma_i^Q \bar{Q}_i P_R \Psi \Phi_Q + \Gamma_i^L \bar{L}_i P_R \Psi \Phi_L + \text{h.c.}$$



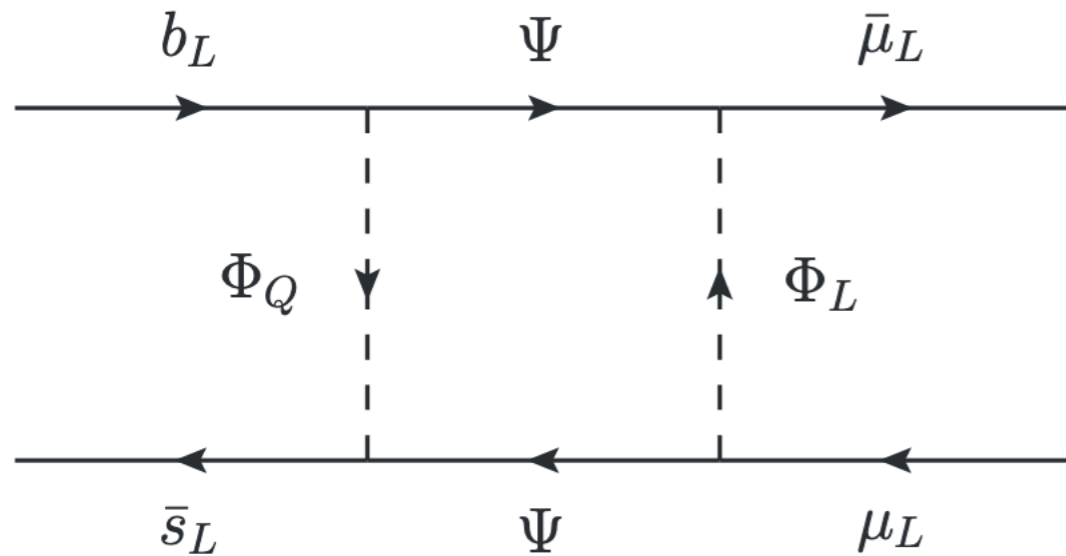
*Class S* – Scalar mediator

$$\mathcal{L}_S \supset \Gamma_i^Q \bar{Q}_i P_R \Psi_Q \Phi + \Gamma_i^L \bar{L}_i P_R \Psi_L \Phi + \text{h.c.}$$

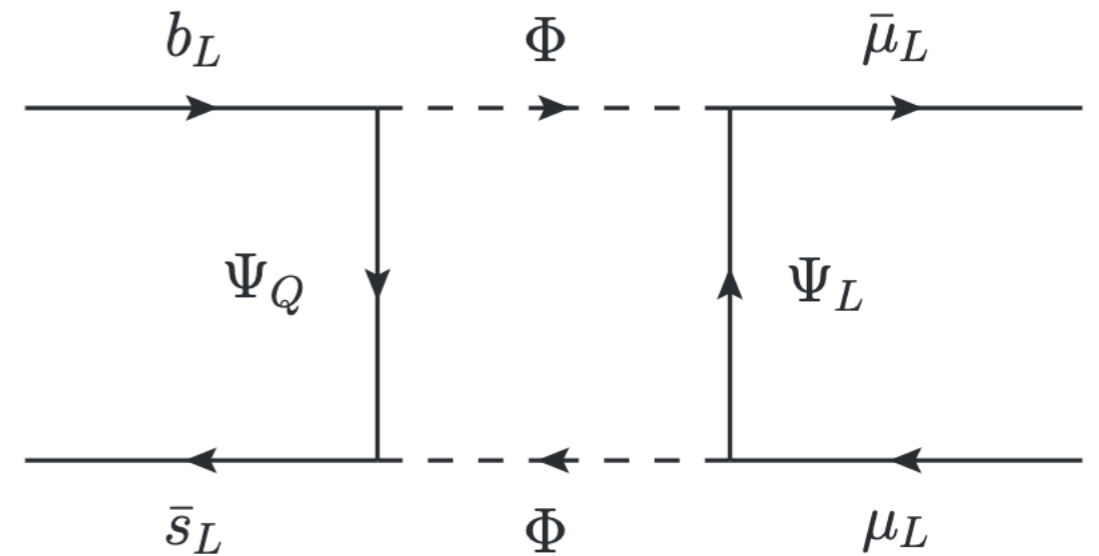
However we're looking for a DM candidate now, which has to be stable and must not be over abundant (ideally reproducing the relic density)



# Allowed representations



*Class F* – Fermion mediator



*Class S* – Scalar mediator

$SU(3)_c$	$\Phi_Q, \Psi_Q$	$\Phi_L, \Psi_L$	$\Psi, \Phi$
A	<b>3</b>	<b>1</b>	<b>1</b>
B	<b>1</b>	<b><math>\bar{3}</math></b>	<b>3</b>
$SU(2)_L$	$\Phi_Q, \Psi_Q$	$\Phi_L, \Psi_L$	$\Psi, \Phi$
I	<b>2</b>	<b>2</b>	<b>1</b>
II	<b>1</b>	<b>1</b>	<b>2</b>
III	<b>3</b>	<b>3</b>	<b>2</b>
IV	<b>2</b>	<b>2</b>	<b>3</b>
V	<b>3</b>	<b>1</b>	<b>2</b>
VI	<b>1</b>	<b>3</b>	<b>2</b>
$U(1)_Y$	$\Phi_Q, \Psi_Q$	$\Phi_L, \Psi_L$	$\Psi, \Phi$
	$1/6 - X$	$-1/2 - X$	$X$

- $X$  chosen so that there is a neutral state (DM candidate)
- Fermionic DM only allowed for  $SU(2)$  singlet or triplet (doublet would require the presence of a additional Majorana fermions)
- Scalar DM allowed for any  $SU(2)$  rep. (doublet allowed by suitable mass splitting between CP-even and CP-odd, i.e. Inert Doublet)

# Allowed representations

Label	$\Phi_Q$	$\Phi_L$	$\Psi$
$\mathcal{F}_{IA;-1}$	$(\mathbf{3}, \mathbf{2}, 7/6)$	$(\mathbf{1}, \mathbf{2}, 1/2)^*$	$(\mathbf{1}, \mathbf{1}, -1)$
$\mathcal{F}_{IA;0}$	$(\mathbf{3}, \mathbf{2}, 1/6)$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$	$(\mathbf{1}, \mathbf{1}, 0)^*$
$\mathcal{F}_{IB;-1/3}$	$(\mathbf{1}, \mathbf{2}, 1/2)^*$	$(\bar{\mathbf{3}}, \mathbf{2}, -1/6)$	$(\mathbf{3}, \mathbf{1}, -1/3)$
$\mathcal{F}_{IB;2/3}$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$	$(\bar{\mathbf{3}}, \mathbf{2}, -7/6)$	$(\mathbf{3}, \mathbf{1}, 2/3)$
$\mathcal{F}_{IIA}$	$(\mathbf{3}, \mathbf{1}, 2/3)$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)$
$\mathcal{F}_{IIB}$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\bar{\mathbf{3}}, \mathbf{1}, -2/3)$	$(\mathbf{3}, \mathbf{2}, 1/6)$
$\mathcal{F}_{IIIA;-3/2}$	$(\mathbf{3}, \mathbf{3}, 5/3)$	$(\mathbf{1}, \mathbf{3}, 1)^*$	$(\mathbf{1}, \mathbf{2}, -3/2)$
$\mathcal{F}_{IIIA;-1/2}$	$(\mathbf{3}, \mathbf{3}, 2/3)$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)$
$\mathcal{F}_{IIIA;1/2}$	$(\mathbf{3}, \mathbf{3}, -1/3)$	$(\mathbf{1}, \mathbf{3}, -1)^*$	$(\mathbf{1}, \mathbf{2}, 1/2)$
$\mathcal{F}_{IIIB;-5/6}$	$(\mathbf{1}, \mathbf{3}, 1)^*$	$(\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	$(\mathbf{3}, \mathbf{2}, -5/6)$
$\mathcal{F}_{IIIB;1/6}$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\bar{\mathbf{3}}, \mathbf{3}, -2/3)$	$(\mathbf{3}, \mathbf{2}, 1/6)$
$\mathcal{F}_{IIIB;7/6}$	$(\mathbf{1}, \mathbf{3}, -1)^*$	$(\bar{\mathbf{3}}, \mathbf{3}, -5/3)$	$(\mathbf{3}, \mathbf{2}, 7/6)$
$\mathcal{F}_{IVA;-1}$	$(\mathbf{3}, \mathbf{2}, 7/6)$	$(\mathbf{1}, \mathbf{2}, 1/2)^*$	$(\mathbf{1}, \mathbf{3}, -1)$
$\mathcal{F}_{IVA;0}$	$(\mathbf{3}, \mathbf{2}, 1/6)$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$	$(\mathbf{1}, \mathbf{3}, 0)^*$
$\mathcal{F}_{IVB;-1/3}$	$(\mathbf{1}, \mathbf{2}, 1/2)^*$	$(\bar{\mathbf{3}}, \mathbf{2}, -1/6)$	$(\mathbf{3}, \mathbf{3}, -1/3)$
$\mathcal{F}_{IVB;2/3}$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$	$(\bar{\mathbf{3}}, \mathbf{2}, -7/6)$	$(\mathbf{3}, \mathbf{3}, 2/3)$
$\mathcal{F}_{VA}$	$(\mathbf{3}, \mathbf{3}, 2/3)$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)$
$\mathcal{F}_{VB;-5/6}$	$(\mathbf{1}, \mathbf{3}, 1)^*$	$(\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	$(\mathbf{3}, \mathbf{2}, -5/6)$
$\mathcal{F}_{VB;1/6}$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\bar{\mathbf{3}}, \mathbf{1}, -2/3)$	$(\mathbf{3}, \mathbf{2}, 1/6)$
$\mathcal{F}_{VB;7/6}$	$(\mathbf{1}, \mathbf{3}, -1)^*$	$(\bar{\mathbf{3}}, \mathbf{1}, -5/3)$	$(\mathbf{3}, \mathbf{2}, 7/6)$
$\mathcal{F}_{VIA;-3/2}$	$(\mathbf{3}, \mathbf{1}, 5/3)$	$(\mathbf{1}, \mathbf{3}, 1)^*$	$(\mathbf{1}, \mathbf{2}, -3/2)$
$\mathcal{F}_{VIA;-1/2}$	$(\mathbf{3}, \mathbf{1}, 2/3)$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)$
$\mathcal{F}_{VIA;1/2}$	$(\mathbf{3}, \mathbf{1}, -1/3)$	$(\mathbf{1}, \mathbf{3}, -1)^*$	$(\mathbf{1}, \mathbf{2}, 1/2)$
$\mathcal{F}_{VIB}$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\bar{\mathbf{3}}, \mathbf{3}, -2/3)$	$(\mathbf{3}, \mathbf{2}, 1/6)$

Label	$\Psi_Q$	$\Psi_L$	$\Phi$
$\mathcal{S}_{IA}$	$(\mathbf{3}, \mathbf{2}, 1/6)$	$(\mathbf{1}, \mathbf{2}, -1/2)$	$(\mathbf{1}, \mathbf{1}, 0)^*$
$\mathcal{S}_{IIA;-1/2}$	$(\mathbf{3}, \mathbf{1}, 2/3)$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$
$\mathcal{S}_{IIA;1/2}$	$(\mathbf{3}, \mathbf{1}, -1/3)$	$(\mathbf{1}, \mathbf{1}, -1)$	$(\mathbf{1}, \mathbf{2}, 1/2)^*$
$\mathcal{S}_{IIB}$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\bar{\mathbf{3}}, \mathbf{1}, -2/3)$	$(\mathbf{3}, \mathbf{2}, 1/6)$
$\mathcal{S}_{IIIA;-1/2}$	$(\mathbf{3}, \mathbf{3}, 2/3)$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$
$\mathcal{S}_{IIIA;1/2}$	$(\mathbf{3}, \mathbf{3}, -1/3)$	$(\mathbf{1}, \mathbf{3}, -1)$	$(\mathbf{1}, \mathbf{2}, 1/2)^*$
$\mathcal{S}_{IIIB}$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\bar{\mathbf{3}}, \mathbf{3}, -2/3)$	$(\mathbf{3}, \mathbf{2}, 1/6)$
$\mathcal{S}_{IVA;-1}$	$(\mathbf{3}, \mathbf{2}, 7/6)$	$(\mathbf{1}, \mathbf{2}, 1/2)$	$(\mathbf{1}, \mathbf{3}, -1)^*$
$\mathcal{S}_{IVA;0}$	$(\mathbf{3}, \mathbf{2}, 1/6)$	$(\mathbf{1}, \mathbf{2}, -1/2)$	$(\mathbf{1}, \mathbf{3}, 0)^*$
$\mathcal{S}_{IVA;1}$	$(\mathbf{3}, \mathbf{2}, -5/6)$	$(\mathbf{1}, \mathbf{2}, -3/2)$	$(\mathbf{1}, \mathbf{3}, 1)^*$
$\mathcal{S}_{VA;-1/2}$	$(\mathbf{3}, \mathbf{3}, 2/3)$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$
$\mathcal{S}_{VA;1/2}$	$(\mathbf{3}, \mathbf{3}, -1/3)$	$(\mathbf{1}, \mathbf{1}, -1)$	$(\mathbf{1}, \mathbf{2}, 1/2)^*$
$\mathcal{S}_{VB}$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\bar{\mathbf{3}}, \mathbf{1}, -2/3)$	$(\mathbf{3}, \mathbf{2}, 1/6)$
$\mathcal{S}_{VIA;-1/2}$	$(\mathbf{3}, \mathbf{1}, 2/3)$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$
$\mathcal{S}_{VIA;1/2}$	$(\mathbf{3}, \mathbf{1}, -1/3)$	$(\mathbf{1}, \mathbf{3}, -1)$	$(\mathbf{1}, \mathbf{2}, 1/2)^*$
$\mathcal{S}_{VIB}$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\bar{\mathbf{3}}, \mathbf{3}, -2/3)$	$(\mathbf{3}, \mathbf{2}, 1/6)$

DM multiplets marked by \*,  
highlighted models studied in  
detail in the paper

# Flavour bounds

Again not only B-anomalies, but also  $B_s$ - $B_s$ bar mixing!

$$(\delta C_\mu^9)_F = -(\delta C_\mu^{10})_F = \frac{\sqrt{2}}{4G_F V_{tb} V_{ts}^*} \frac{\Gamma_Q |\Gamma_\mu^L|^2}{32\pi\alpha_{EM} M_\Psi^2} (\eta F(x_Q, x_L) + 2\chi^M \eta^M G(x_Q, x_L)) ,$$

$$(\delta C^{B\bar{B}})_F = \frac{\Gamma_Q^2}{128\pi^2 M_\Psi^2} (\eta_{BB} F(x_Q, x_L) + 2\chi^M \eta^M G(x_Q, x_L)) ,$$

$$(\delta C_\mu^9)_S = -(\delta C_\mu^{10})_S = -\frac{\sqrt{2}}{4G_F V_{tb} V_{ts}^*} \frac{\Gamma_Q |\Gamma_\mu^L|^2}{32\pi\alpha_{EM} M_\Phi^2} (\eta - \chi^M \eta^M) F(y_Q, y_L) ,$$

$$(\delta C^{B\bar{B}})_S = \frac{\Gamma_Q^2}{128\pi^2 M_\Phi^2} (\eta_{BB} - \chi^M \eta^M) F(y_Q, y_L) ,$$

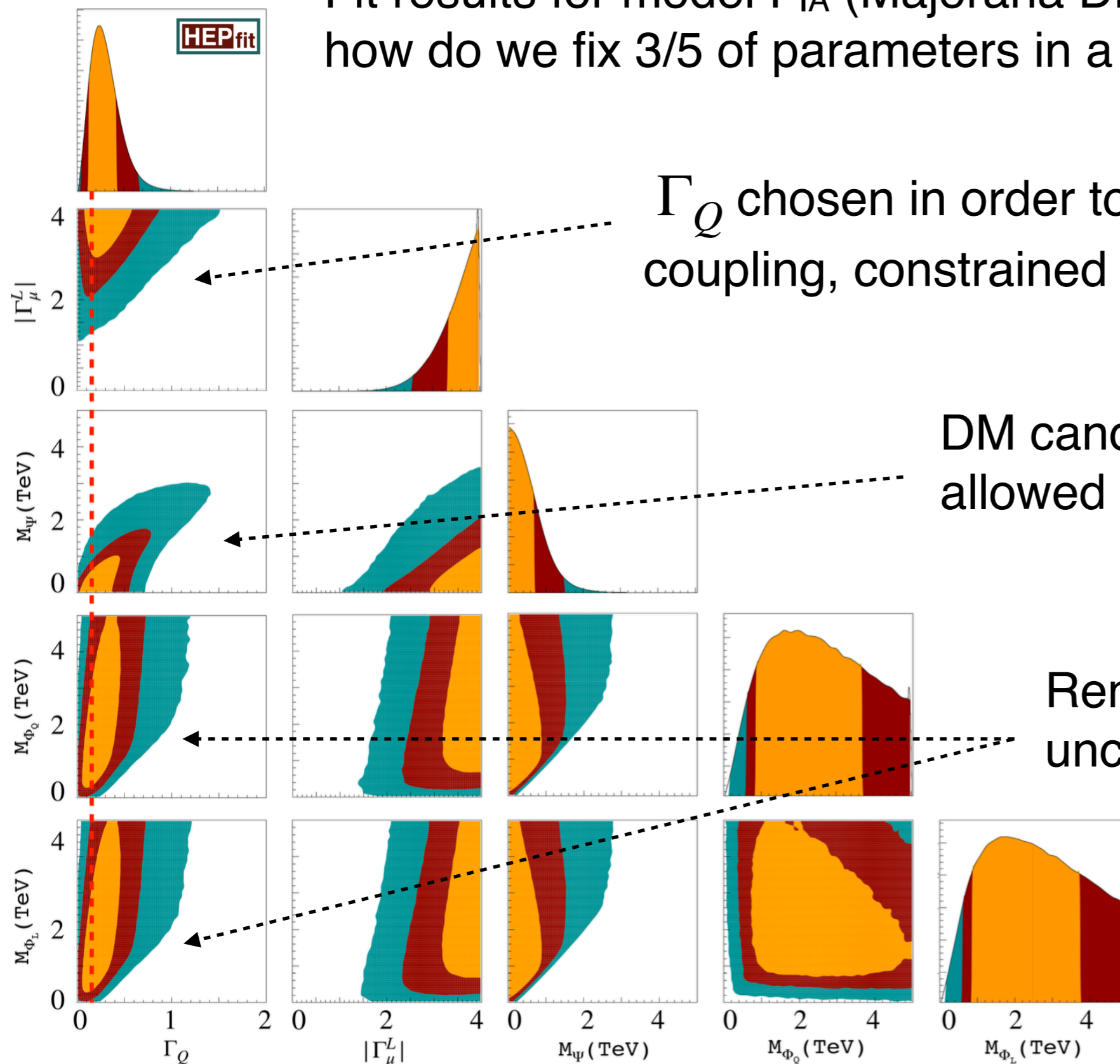
We start by making a combined fit to Flavour anomalies and  $B_s$ - $B_s$ bar mixing, in order to extract allowed ranges for 3 masses and 2 couplings

- We require that the DM candidate has to be the lightest NP state
- We allow the remaining masses to be as heavy as 5 TeV
- We allow the lepton coupling in the range  $[0, 4]$ , while for the quark coupling  $[0, 2]$  in models of class F and  $[-2, 0]$  in models of class S, in order to reproduce the desired sign in C9 (no effect on  $B_s$ - $B_s$ bar mixing)



# Flavour bounds

Fit results for model  $F_{IA}$  (Majorana DM) to extract benchmarks:  
 how do we fix 3/5 of parameters in a 2D plot?



$\Gamma_Q$  chosen in order to minimise the lepton coupling, constrained by  $B_s$ - $B_s$ bar mixing

DM candidate mass allowed only up to  $\sim 1$  TeV

Remaining masses largely unconstrained at the  $2\sigma$  level

# Main LHC constraints

A pair of heavy NP candidates can be produced at LHC by QCD / EW Drell-Yann mediated processes, subsequently decaying in jets/leptons + DM

- DM coupling to both heavy states (e.g. scalar DM in class S)

$$pp \rightarrow \Psi_Q \Psi_Q \rightarrow qq' + \cancel{E}_T$$

$$pp \rightarrow \Psi_L \Psi_L \rightarrow \mu^+ \mu^- + \cancel{E}_T$$

- DM coupling to only 1 heavy state (e.g. fermion DM in class S)

$$pp \rightarrow \Phi\Phi \rightarrow qq' + \cancel{E}_T$$

$$pp \rightarrow \Psi_L \Psi_L \rightarrow \mu^+ \mu^- + \Phi\Phi \rightarrow \mu^+ \mu^- + qq' + \cancel{E}_T$$

or

$$pp \rightarrow \Phi\Phi \rightarrow \mu^+ \mu^- + \cancel{E}_T$$

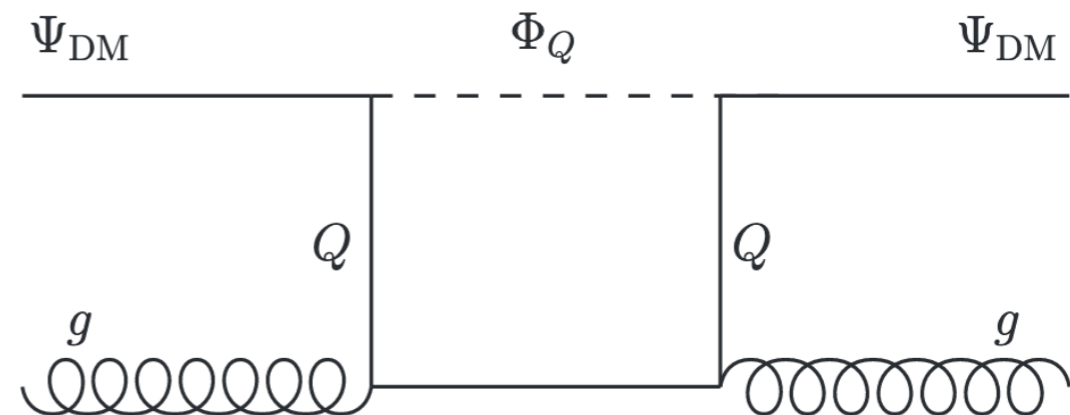
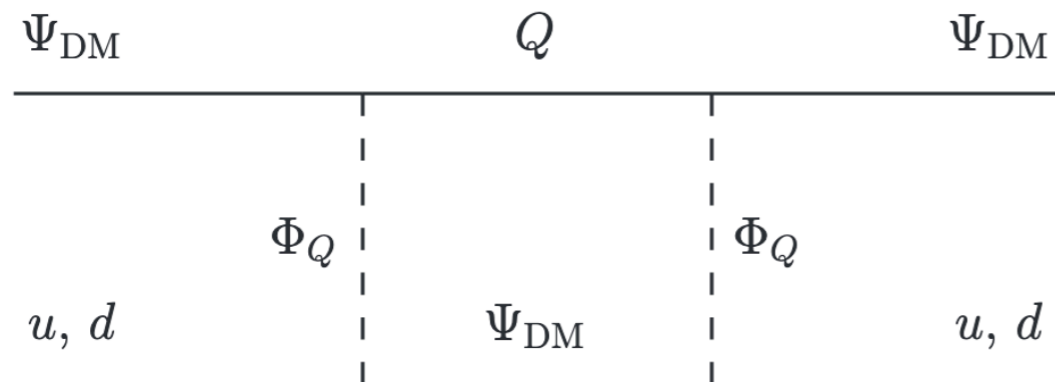
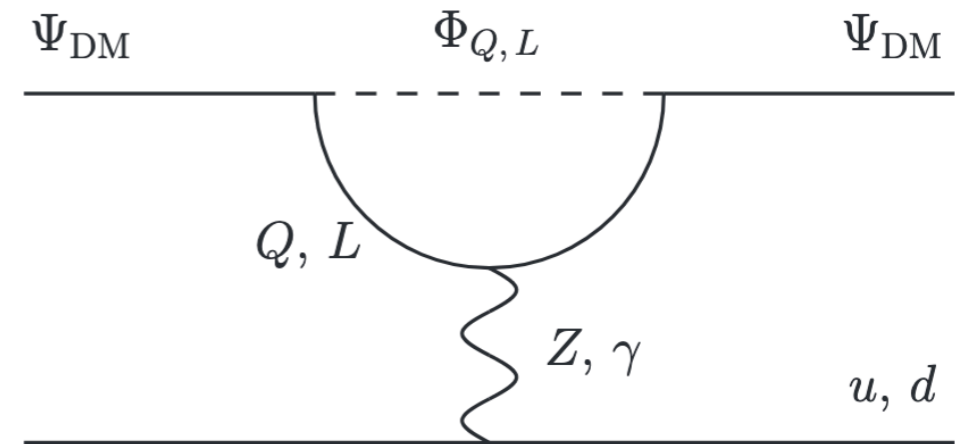
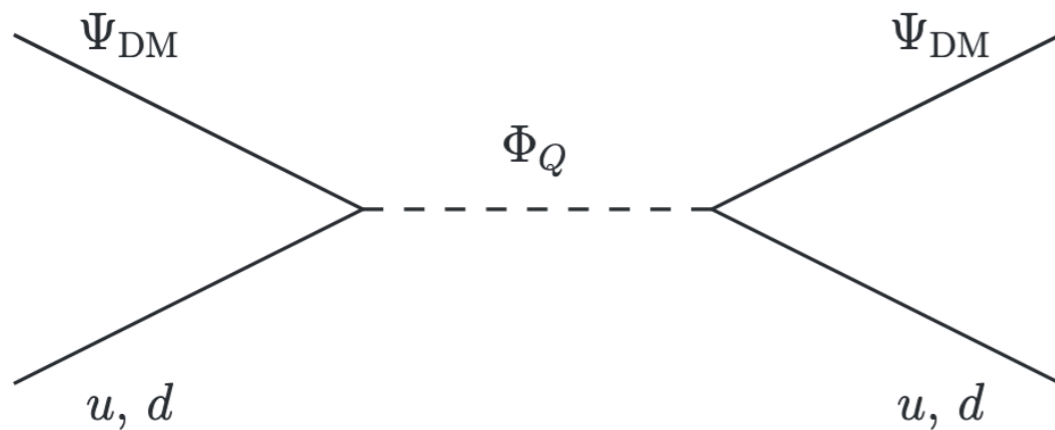
$$pp \rightarrow \Psi_Q \Psi_Q \rightarrow qq' + \Phi\Phi \rightarrow qq' + \mu^+ \mu^- + \cancel{E}_T$$

We will recast LHC SUSY searches of jets and/or leptons + ME



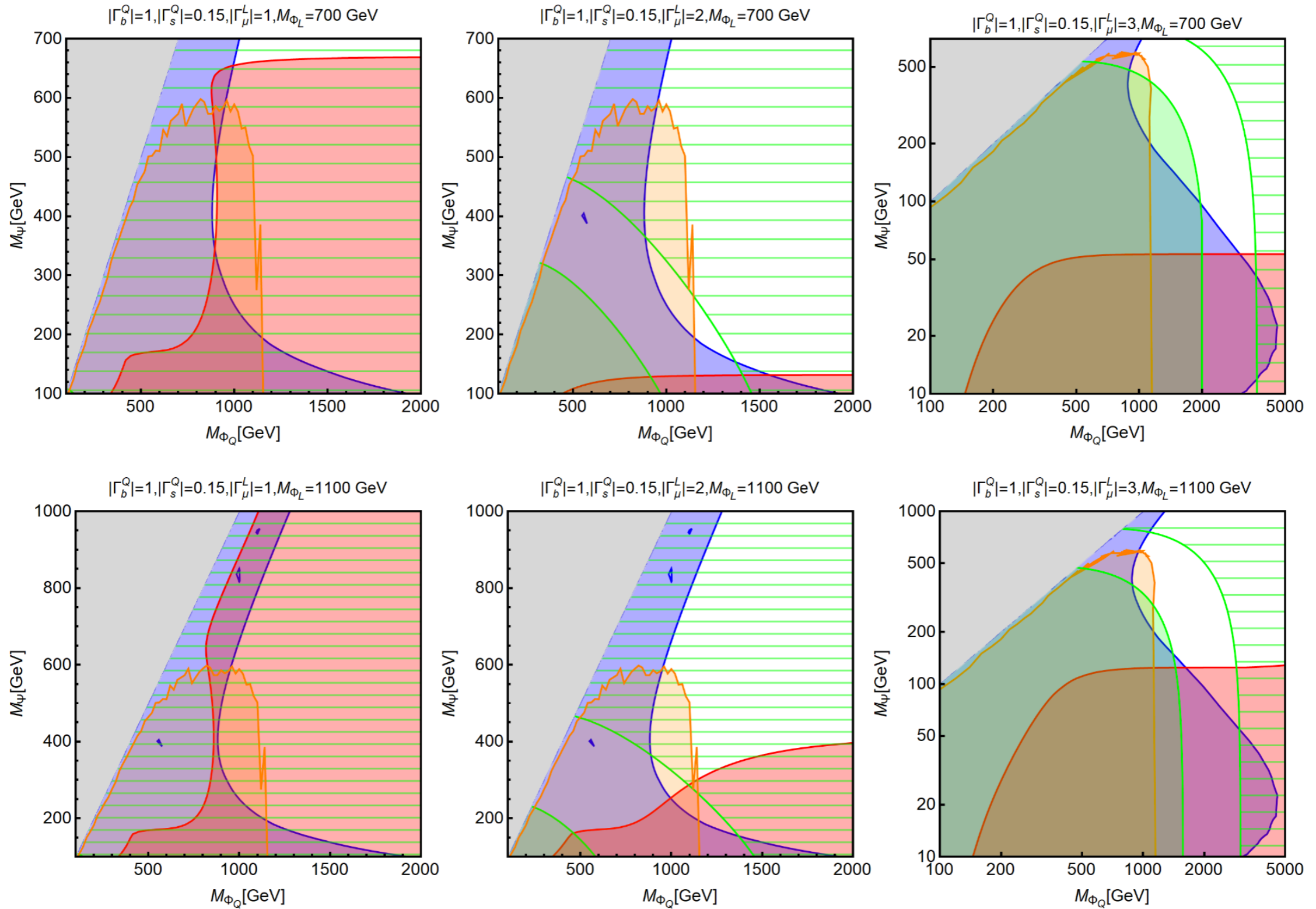
# Main DM constraints

- DM should reproduce the measured relic density  $\Omega_{\text{DM}} h^2 = 0.1199 \pm 0.0022$  (or at most be under-abundant)
- DM should evade DD constraints, where non-relativistic DM scatters with nucleons in an atom. Principal constraints come from Xenon1T experiment



# F<sub>IA</sub> with Majorana DM

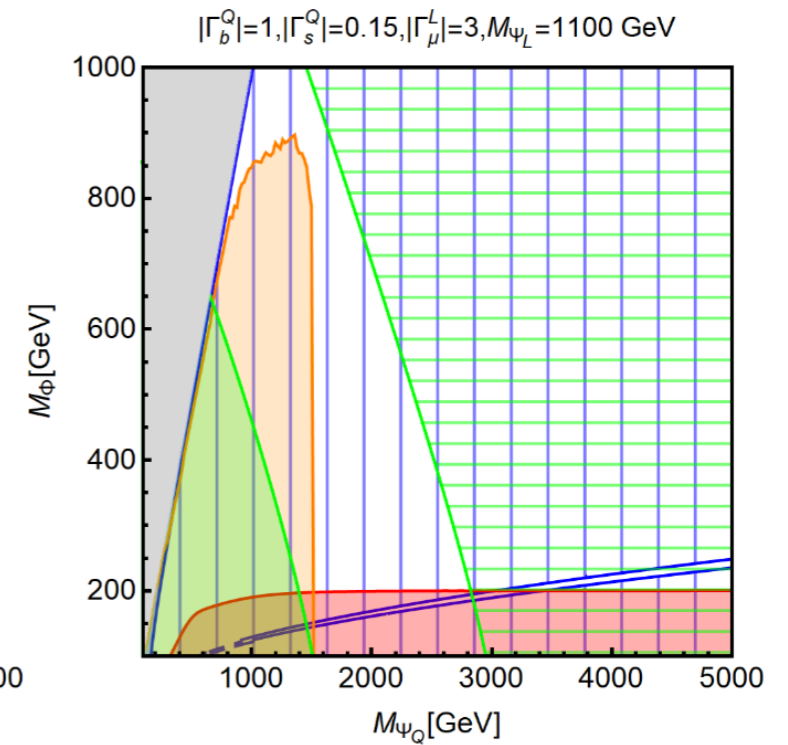
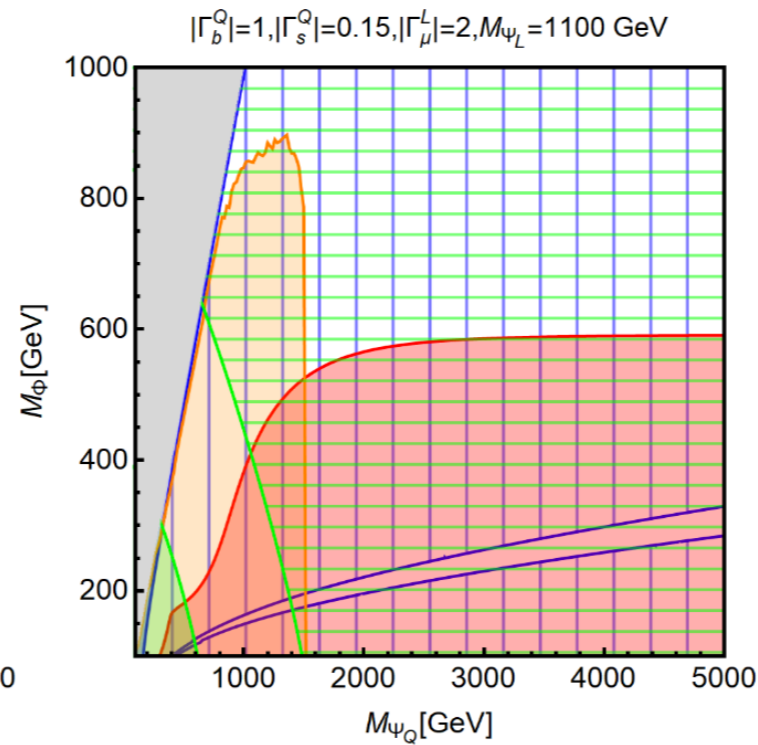
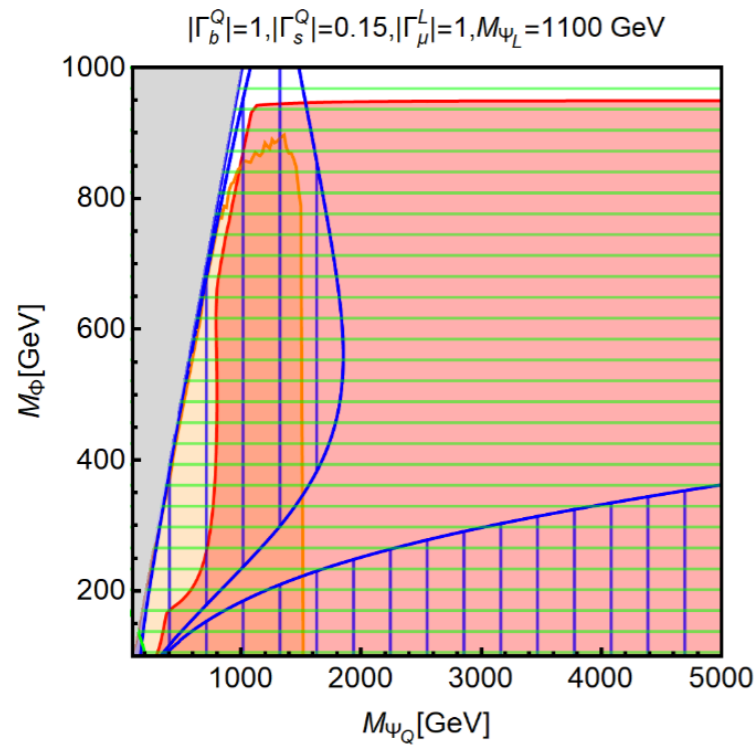
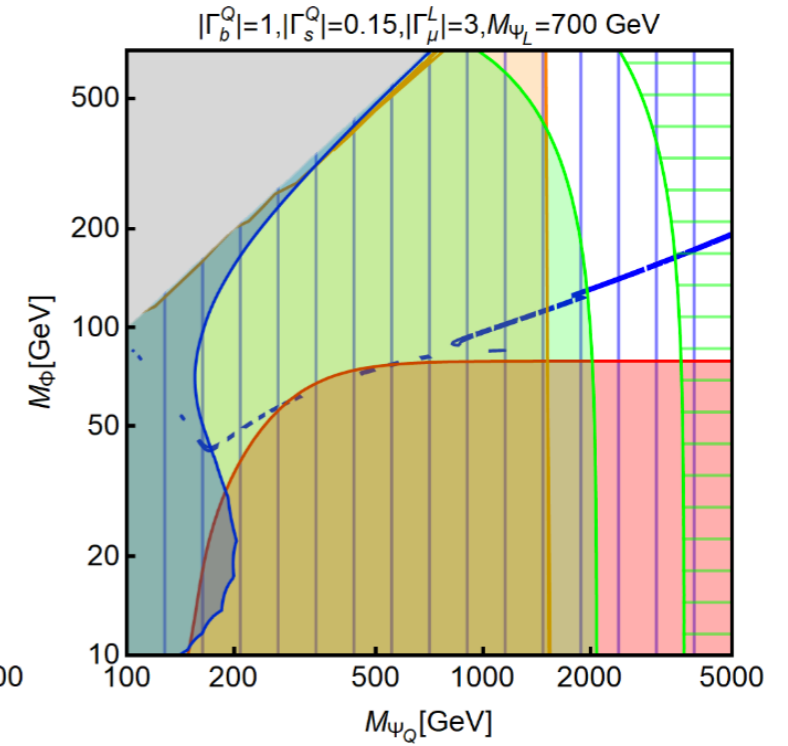
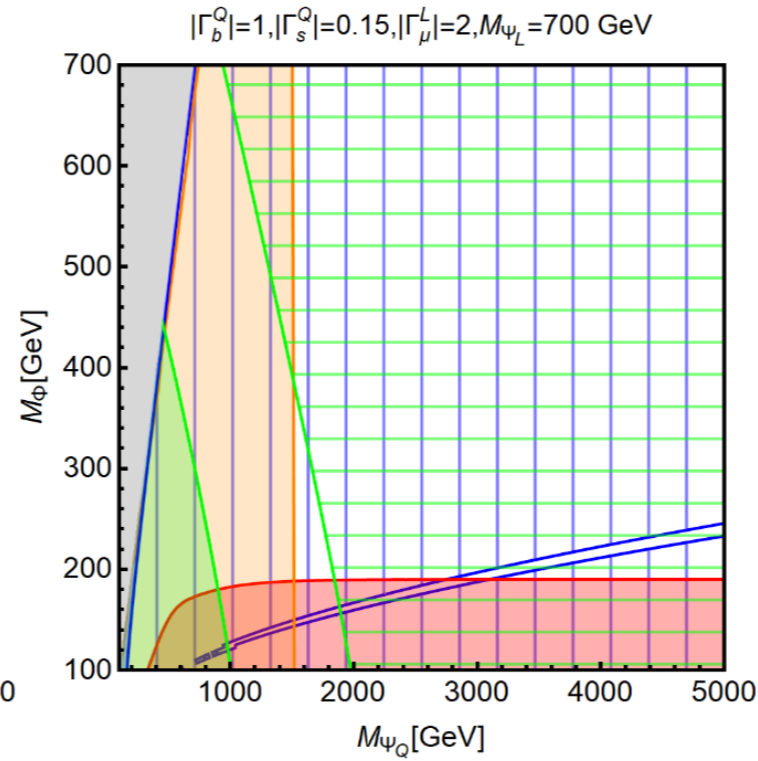
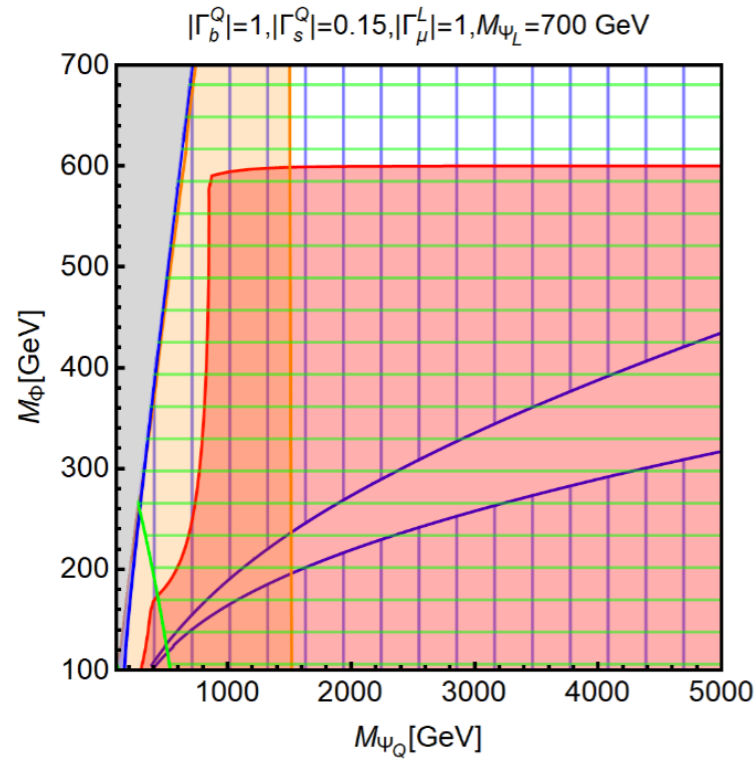
$\Phi_Q$	$\Phi_L$	$\Psi$
$(\mathbf{3}, \mathbf{2}, 1/6)$	$(\mathbf{1}, \mathbf{2}, -1/2)$	$(\mathbf{1}, \mathbf{1}, 0)^*$



Viable model to address everything simultaneously! Allowed only with Majorana, since Dirac interactions with Z/ $\gamma$  induces strong constraints from DD

# S<sub>IA</sub> with complex DM

$\Psi_Q$	$\Psi_L$	$\Phi$
$(3, 2, 1/6)$	$(1, 2, -1/2)$	$(1, 1, 0)^*$



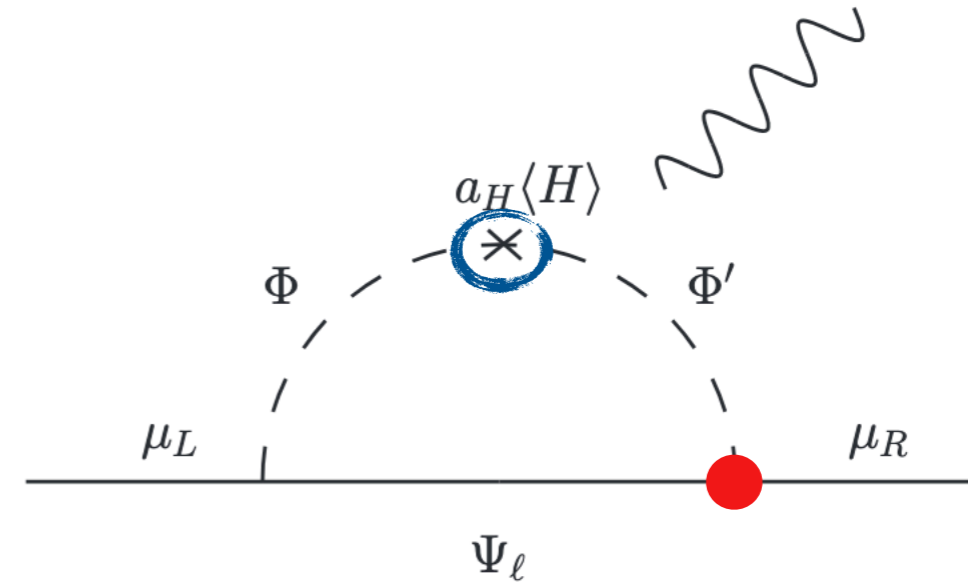
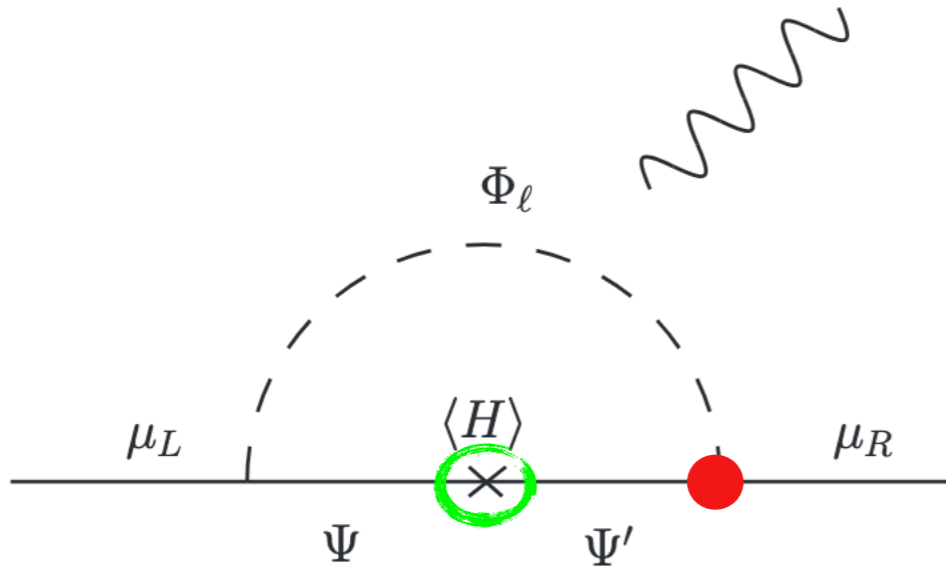
Viable model only if  $O(100\text{KeV})$  mass splitting is assumed between CP-even and CP-odd DM comp. (avoiding DD constr. due to non-relativistic scattering)

# Summary

- *Introduction*
- *$g-2$  and  $B$ -anomalies*
- *$B$ -anomalies and DM*
- *All together now! (2104.03228)*

# Systematic Studies of All Possible Loop Models

We're adding back the muon (g-2), so we allow also muon RH couplings (only 4 fields)



## ● Fermion flavour mediator

$$\mathcal{L}_{\mathcal{F}}^{\Phi_\ell \Phi'_\ell} \supset \Gamma_i^Q \bar{Q}_i P_R \Psi \Phi_q + \Gamma_i^L \bar{L}_i P_R \Psi \Phi_\ell + \Gamma_i^E \bar{E}_i P_L \Psi \Phi'_\ell + a_H \Phi_\ell^\dagger \Phi'_\ell H + \text{h.c.}$$

$$\mathcal{L}_{\mathcal{F}}^{\Psi \Psi'} \supset \Gamma_i^Q \bar{Q}_i P_R \Psi \Phi_q + \Gamma_i^L \bar{L}_i P_R \Psi \Phi_\ell + \Gamma_i^E \bar{E}_i P_L \Psi' \Phi_\ell + \lambda_{HL} \bar{\Psi} P_L \Psi' H + \lambda_{HR} \bar{\Psi} P_R \Psi' H + \text{h.c.}$$

## ● Scalar flavour mediator

$$\mathcal{L}_{\mathcal{S}}^{\Phi \Phi'} \supset \Gamma_i^Q \bar{Q}_i P_R \Psi_q \Phi + \Gamma_i^L \bar{L}_i P_R \Psi_\ell \Phi + \Gamma_i^E \bar{E}_i P_L \Psi_\ell \Phi' + a_H \Phi^\dagger \Phi' H + \text{h.c.}$$

$$\mathcal{L}_{\mathcal{S}}^{\Psi_\ell \Psi'_\ell} \supset \Gamma_i^Q \bar{Q}_i P_R \Psi_q \Phi + \Gamma_i^L \bar{L}_i P_R \Psi_\ell \Phi + \Gamma_i^E \bar{E}_i P_L \Psi'_\ell \Phi + \lambda_{H1} \bar{\Psi}_\ell P_R \Psi'_\ell H + \lambda_{H2} \bar{\Psi}_\ell P_L \Psi'_\ell H + \text{h.c.}$$

# Allowed representations

We start from the models that we know fit B-anomalies and DM, and add a fourth field inducing RH muon couplings

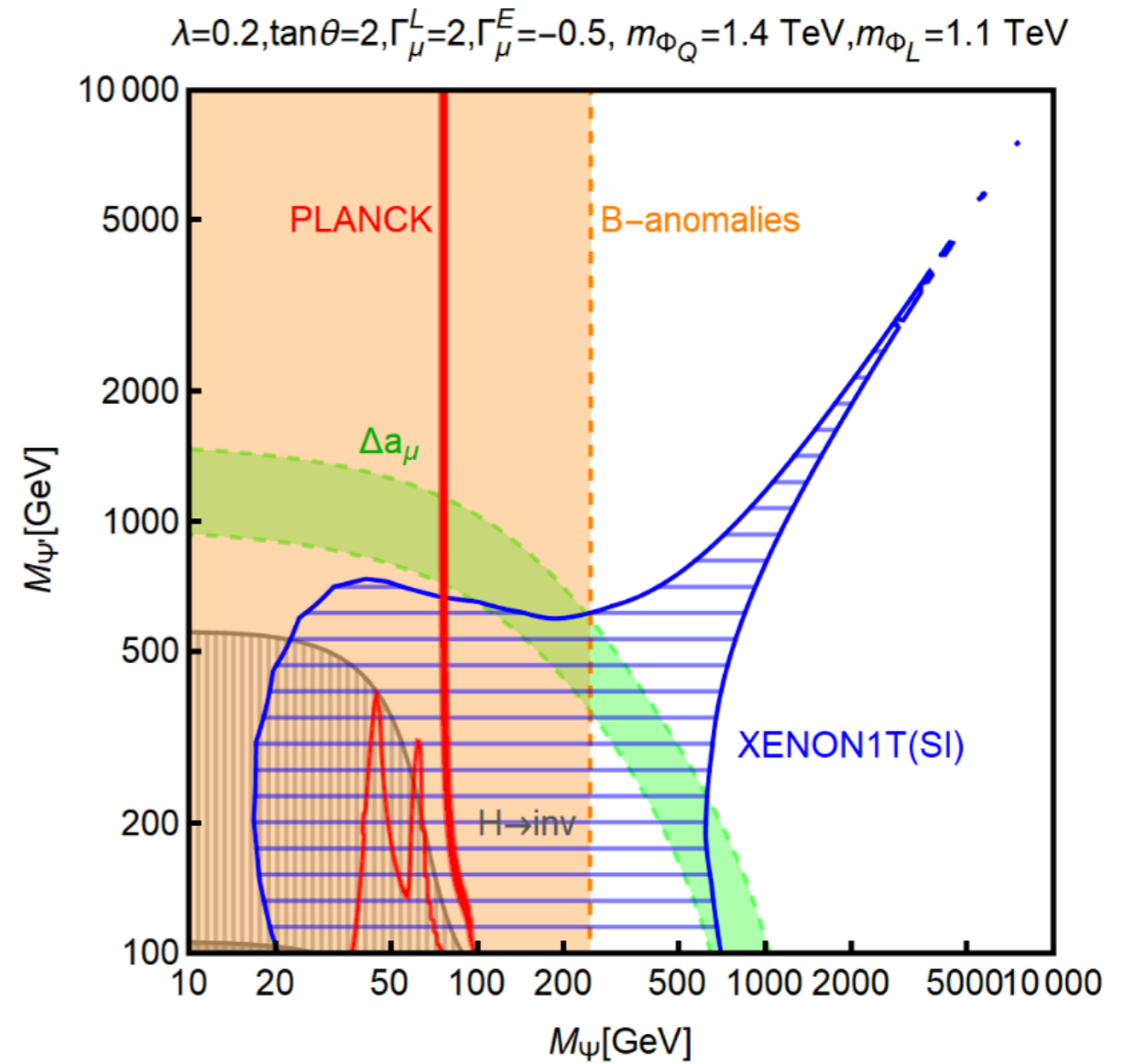
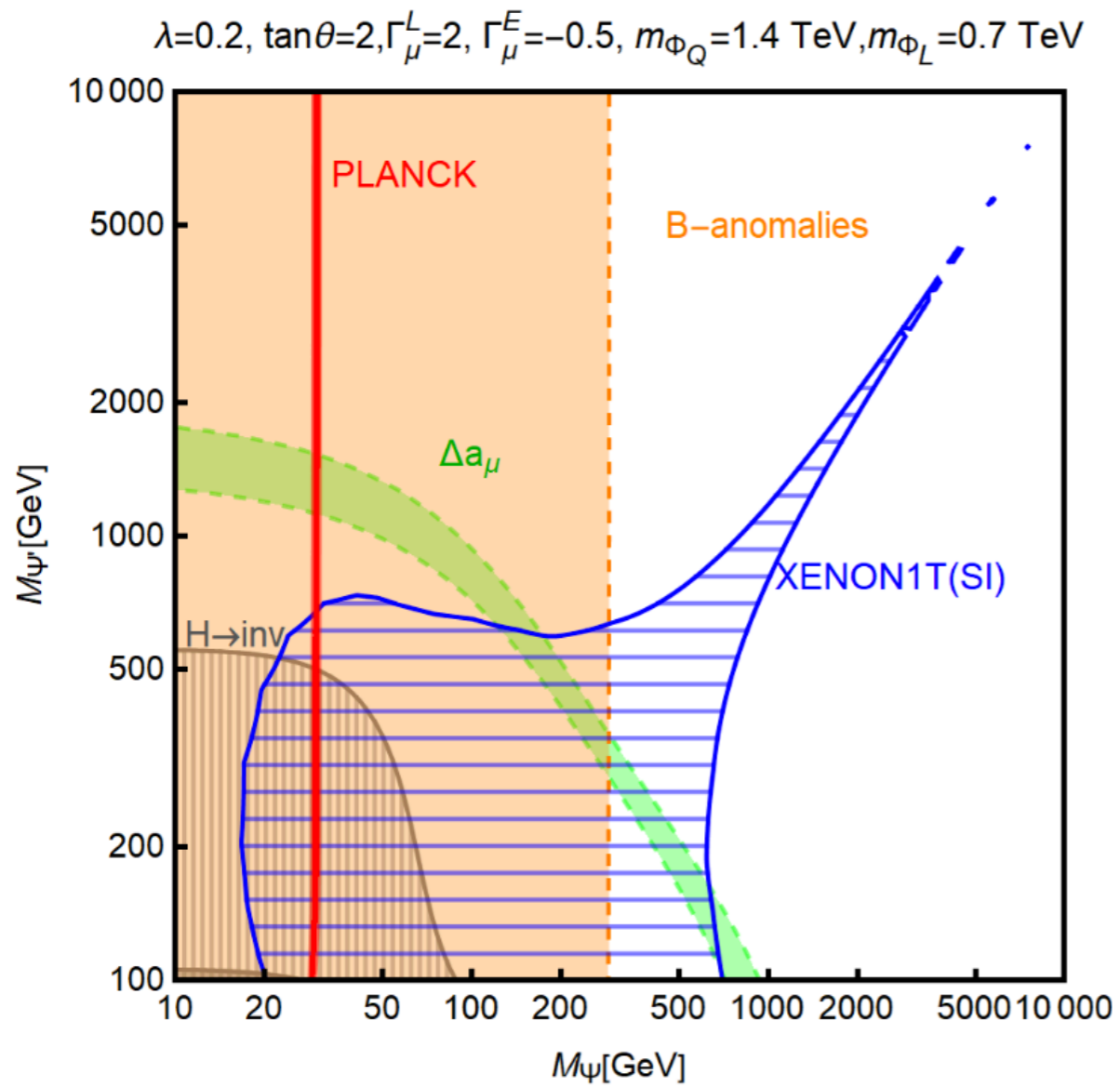
Label	$\Phi_q/\Psi_q$	$\Phi_\ell/\Psi_\ell$	$\Psi/\Phi$	$\Phi'_\ell/\Psi'_\ell$	$\Psi'/\Phi'$
$\mathcal{F}_{Ia}/\mathcal{S}_{Ia}$	( <b>3</b> , <b>2</b> , 1/6)	( <b>1</b> , <b>2</b> , -1/2)	( <b>1</b> , <b>1</b> , 0)	( <b>1</b> , <b>1</b> , -1)	–
$\mathcal{F}_{Ib}/\mathcal{S}_{Ib}$	( <b>3</b> , <b>2</b> , 1/6)	( <b>1</b> , <b>2</b> , -1/2)	( <b>1</b> , <b>1</b> , 0)	–	( <b>1</b> , <b>2</b> , -1/2)
$\mathcal{F}_{Ic}/\mathcal{S}_{Ic}$	( <b>3</b> , <b>2</b> , 7/6)	( <b>1</b> , <b>2</b> , 1/2)	( <b>1</b> , <b>1</b> , -1)	( <b>1</b> , <b>1</b> , 0)	–
$\mathcal{F}_{IIa}/\mathcal{S}_{IIa}$	( <b>3</b> , <b>1</b> , 2/3)	( <b>1</b> , <b>1</b> , 0)	( <b>1</b> , <b>2</b> , -1/2)	( <b>1</b> , <b>2</b> , -1/2)	–
$\mathcal{F}_{IIb}/\mathcal{S}_{IIb}$	( <b>3</b> , <b>1</b> , 2/3)	( <b>1</b> , <b>1</b> , 0)	( <b>1</b> , <b>2</b> , -1/2)	–	( <b>1</b> , <b>1</b> , -1)
$\mathcal{F}_{IIc}/\mathcal{S}_{IIc}$	( <b>3</b> , <b>1</b> , -1/3)	( <b>1</b> , <b>1</b> , -1)	( <b>1</b> , <b>2</b> , 1/2)	–	( <b>1</b> , <b>1</b> , 0)
$\mathcal{F}_{Va}/\mathcal{S}_{Va}$	( <b>3</b> , <b>3</b> , 2/3)	( <b>1</b> , <b>1</b> , 0)	( <b>1</b> , <b>2</b> , -1/2)	( <b>1</b> , <b>2</b> , -1/2)	–
$\mathcal{F}_{Vb}/\mathcal{S}_{Vb}$	( <b>3</b> , <b>3</b> , 2/3)	( <b>1</b> , <b>1</b> , 0)	( <b>1</b> , <b>2</b> , -1/2)	–	( <b>1</b> , <b>1</b> , -1)
$\mathcal{F}_{Vc}/\mathcal{S}_{Vc}$	( <b>3</b> , <b>3</b> , -1/3)	( <b>1</b> , <b>1</b> , -1)	( <b>1</b> , <b>2</b> , 1/2)	–	( <b>1</b> , <b>1</b> , 0)

Singlet DM

Singlet-Doublet mixed DM

# F<sub>IB</sub> with singlet-doublet DM

$\Phi_Q$	$\Phi_L$	$\Psi$	$\Psi'$
$(\mathbf{3}, \mathbf{2}, 1/6)$	$(\mathbf{1}, \mathbf{2}, -1/2)$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$



Viable model to address everything simultaneously!



# Conclusions

- To address  $g-2$  and B-anomalies via loop models, we need at least 4 fields, with 2 of them coupling to RH muons
- To address B-anomalies and DM via loop models, we need at least 3 fields, with the DM either being a  $SU(2)$  singlet or doublet
- Combining the above, to address everything together via loop models, we need at least 4 fields, with 2 of them coupling to RH muons and the DM either being a  $SU(2)$  singlet or doublet
- This is actually doable! Constraints from LHC and DM searches are complementary, and allowed models can be further test with the advent of new data in both fields!



# Back-up Slides

# What kind of NP could be cut for the job?

- $g-2$

NP coupling to Muons; couplings with both Muon chirality is preferred, inducing also coupling to the SM Higgs to exploit chiral enhancement

$\Rightarrow$  Leptoquark, or fermion(s) and scalar(s) (allowing for chirality flip)

- $b \rightarrow s \mu \mu$

NP coupling to Muons;

$\Rightarrow$  Leptoquark and/or Zprime, or 2 fermions (1 fermion) and 1 scalar (2 scalars) with the single particle acting as mediator between the sectors

- DM

Stable candidate, neutral and colour singlet; possibly connected to the SM by means of a Dark Sector

$\Rightarrow$  Axions, ALPs, fermions, scalars...

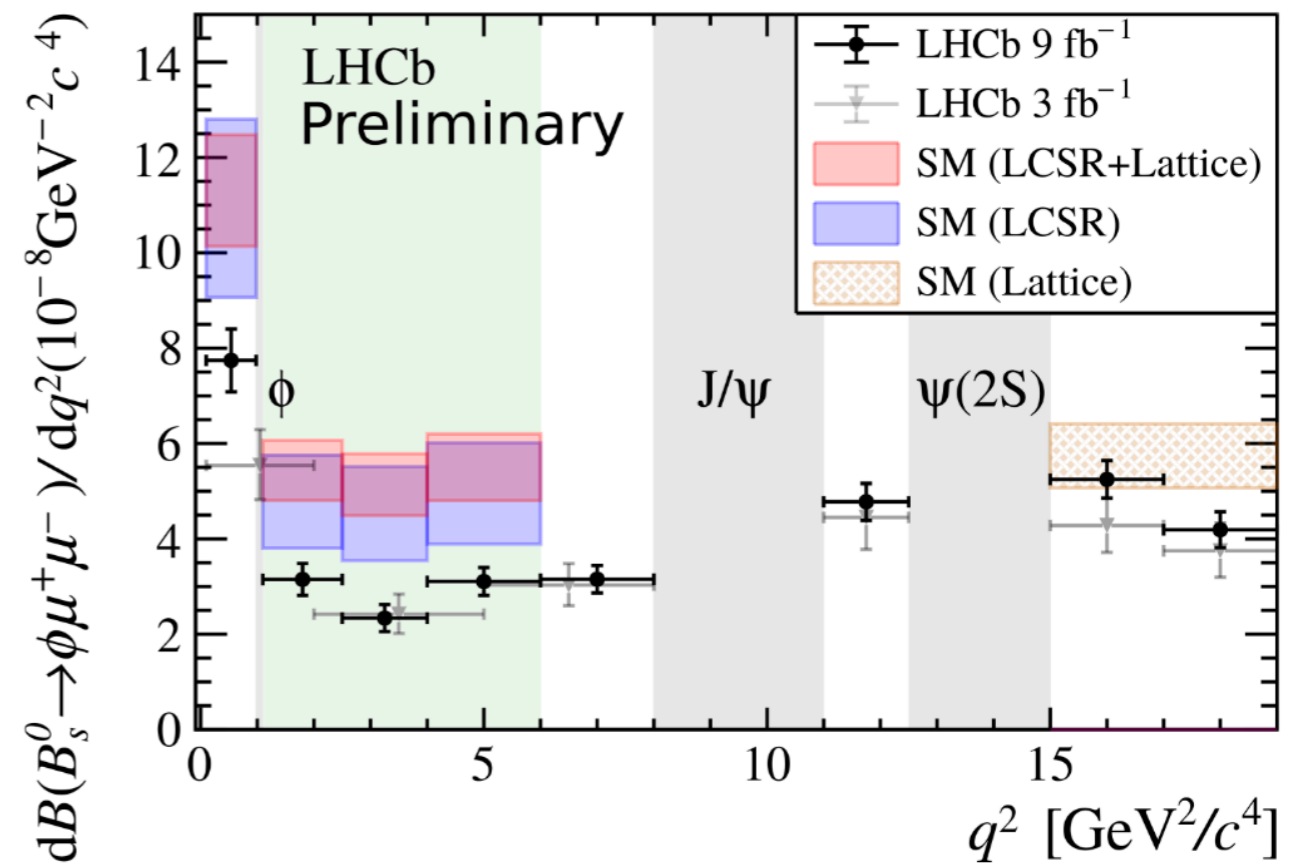
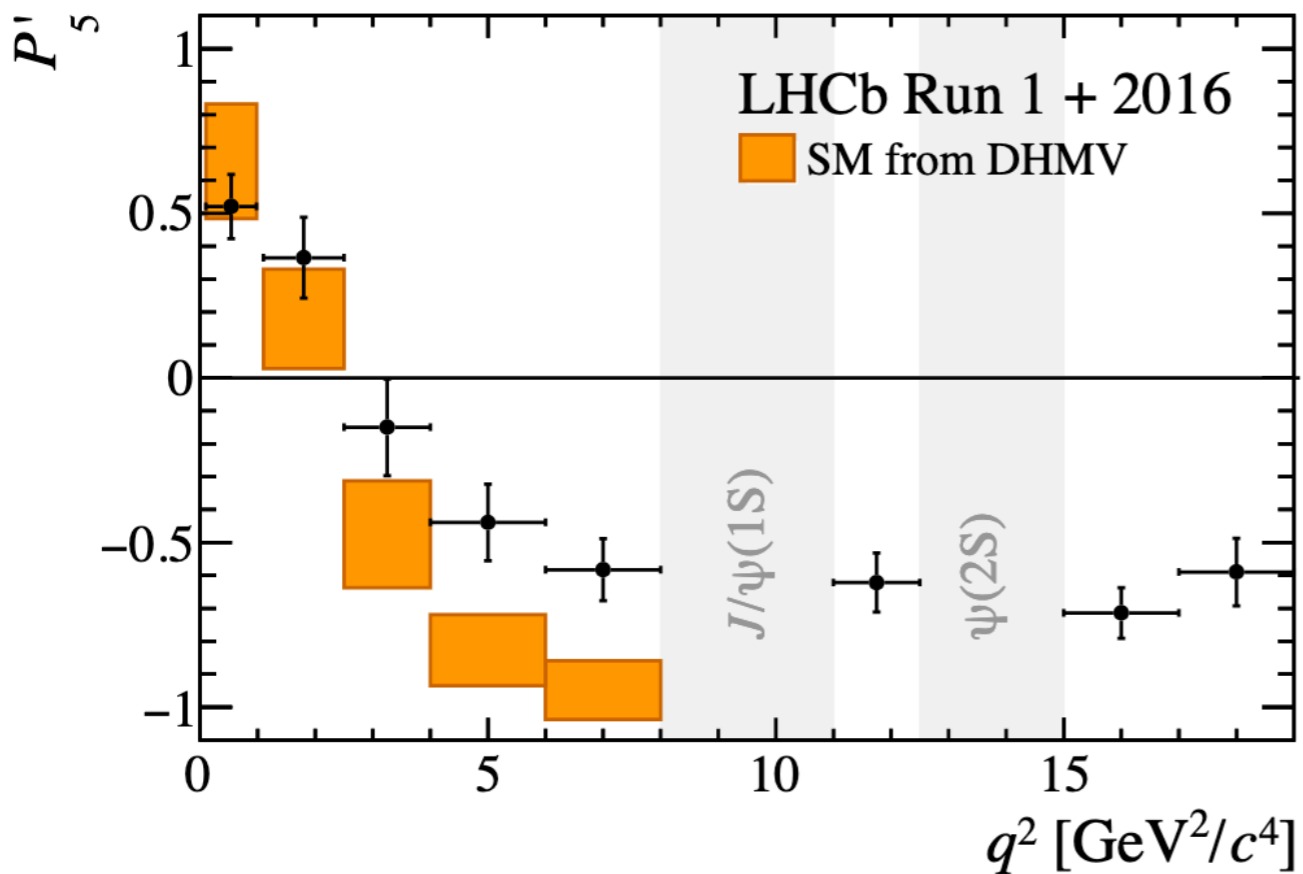
# Opportunities with Semi-Leptonic B Decays

No tree-level flavour changing neutral currents (FCNC) in the SM

&

Intriguing set of “Anomalies” in data of exclusive B rare Decays

[LHCb-PAPER-2021-014, in preparation]



$\sim 3 \sigma$

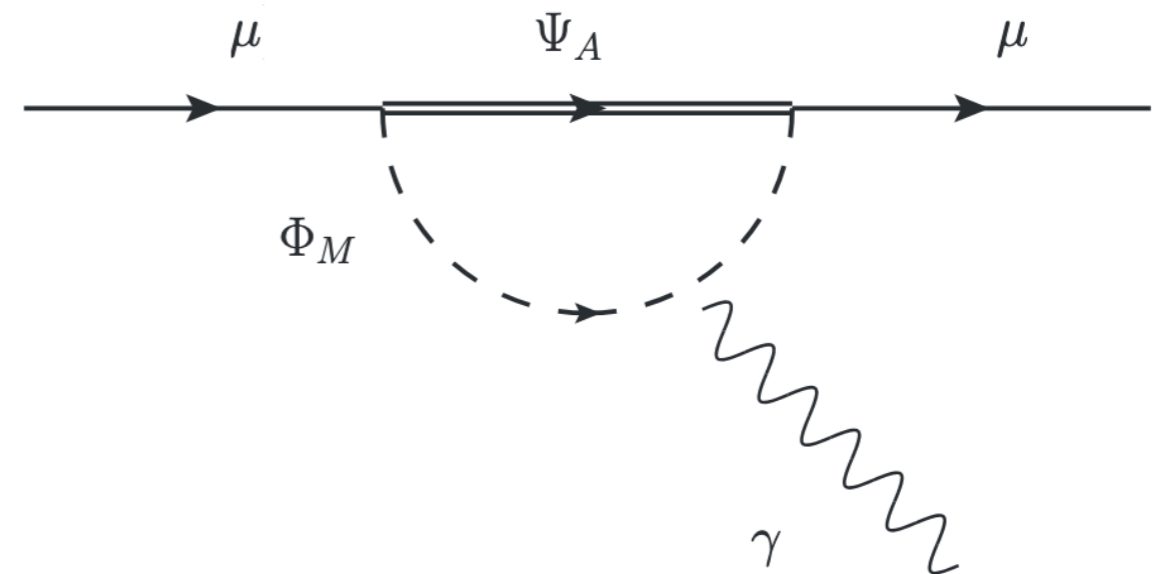
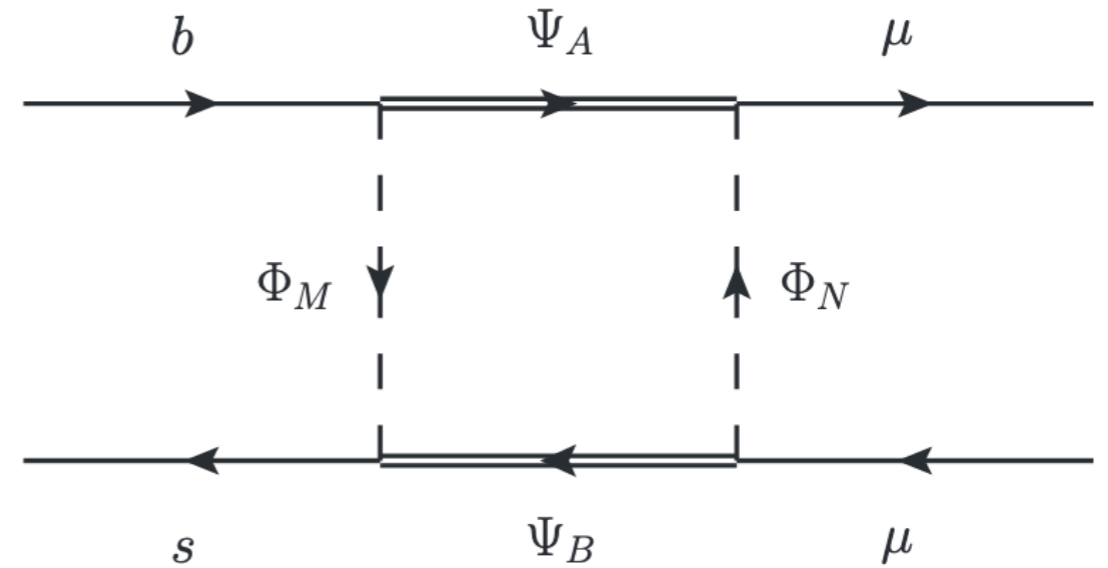
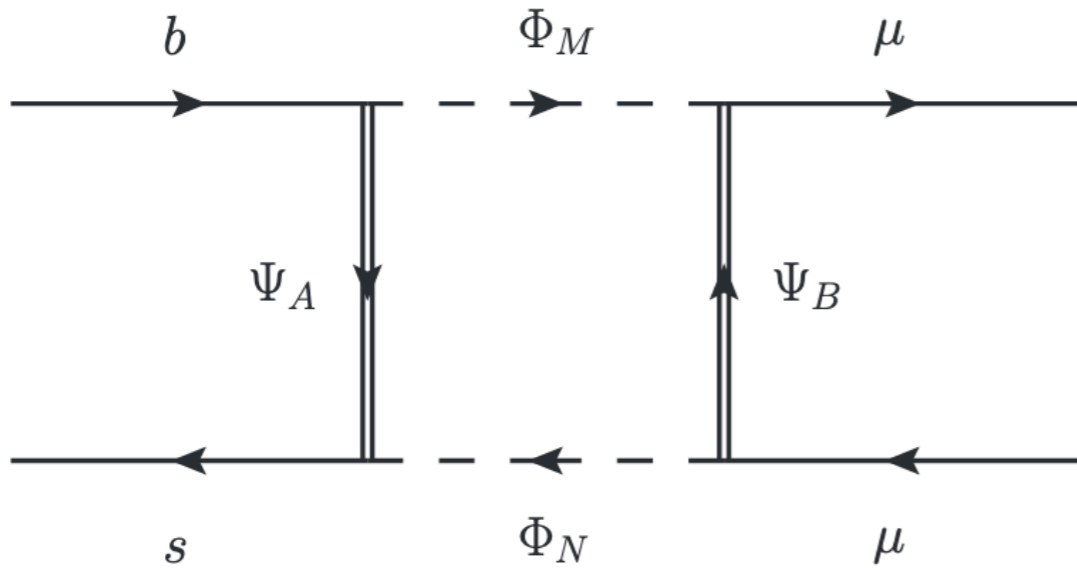
Angular analysis of  $B \rightarrow K^* \mu \mu$  for small dilepton mass,  $4 < q^2 / \text{GeV}^2 <_{31} 8$ .

$\sim 1.8/3.6 \sigma$

$Br$  of  $B_s \rightarrow \phi \mu \mu$

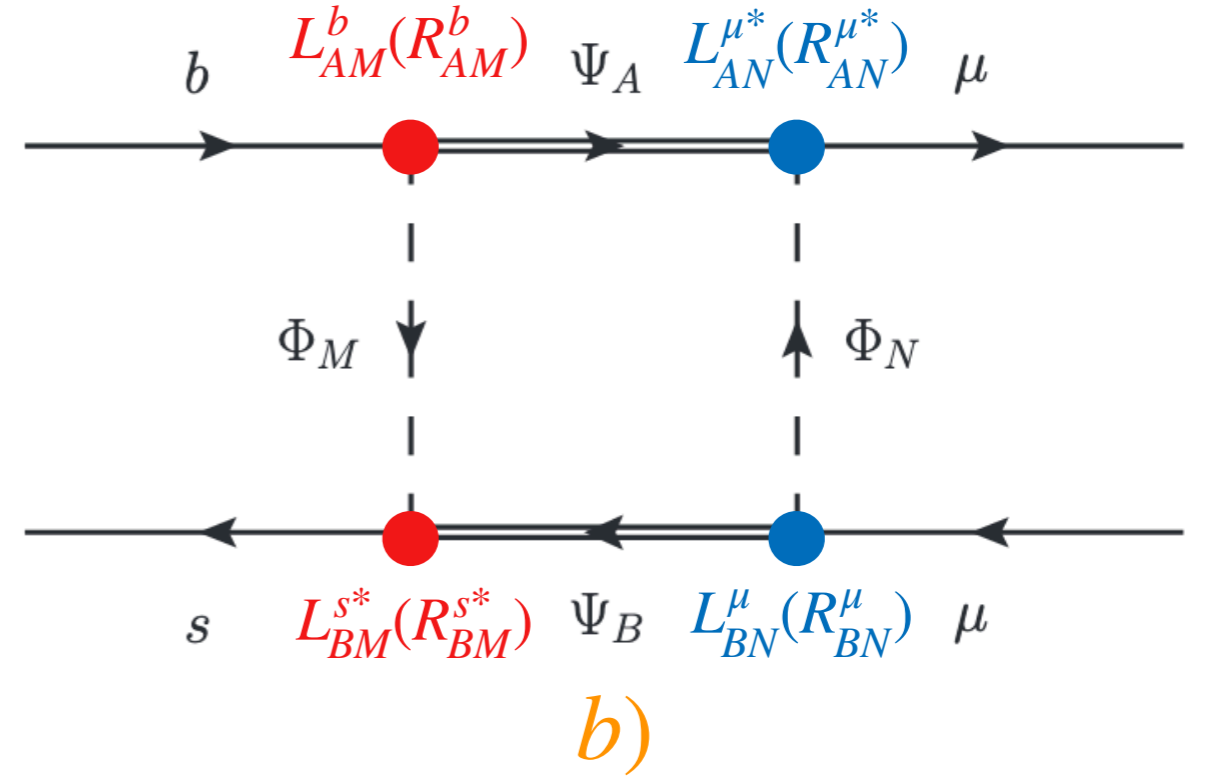
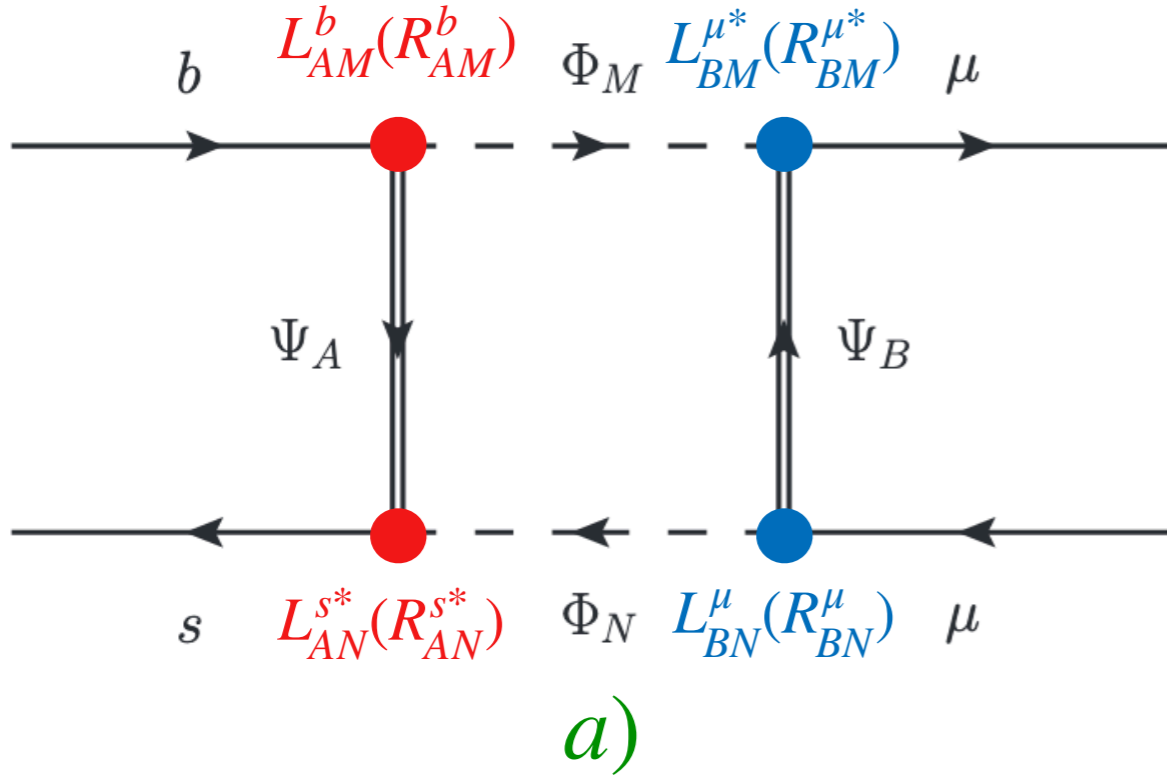
# A Generic Loop Model including RH couplings

$$\mathcal{L}_{\text{int}} = \left[ \bar{\Psi}_A \left( L_{AM}^b P_L b + L_{AM}^s P_L s + L_{AM}^\mu P_L \mu \right) \Phi_M + \bar{\Psi}_A \left( R_{AM}^b P_R b + R_{AM}^s P_R s + R_{AM}^\mu P_R \mu \right) \Phi_M \right] + \text{h.c.}$$



$SU(3)$	$b \rightarrow s\ell\bar{\ell}$ type a)				$b \rightarrow s\ell\bar{\ell}$ type b)			
	$\Psi_A$	$\Psi_B$	$\Phi_M$	$\Phi_N$	$\Psi_A$	$\Psi_B$	$\Phi_M$	$\Phi_N$
I	3	1	1	1	1	1	$\bar{3}$	1
II	1	$\bar{3}$	$\bar{3}$	$\bar{3}$	3	3	1	3
III	3	8	8	8	8	8	$\bar{3}$	8
IV	8	$\bar{3}$	$\bar{3}$	$\bar{3}$	3	3	8	3
V	$\bar{3}$	3	3	3	$\bar{3}$	$\bar{3}$	3	$\bar{3}$

# $b \rightarrow s \mu \mu$



Two distinct solutions, whether the fermion or the scalar is the NP field that couples to both quarks and leptons

$$C_9^{\text{box}, a) = -\mathcal{N} \frac{\chi L_{AN}^{s*} L_{AM}^b}{32\pi\alpha_{\text{EM}} m_{\Phi_M}^2} [L_{BM}^{\mu*} L_{BN}^{\mu} + R_{BM}^{\mu*} R_{BN}^{\mu}] F(x_{AM}, x_{BM}, x_{NM})$$

$$C_{10}^{\text{box}, a) = \mathcal{N} \frac{\chi L_{AN}^{s*} L_{AM}^b}{32\pi\alpha_{\text{EM}} m_{\Phi_M}^2} [L_{BM}^{\mu*} L_{BN}^{\mu} - R_{BM}^{\mu*} R_{BN}^{\mu}] F(x_{AM}, x_{BM}, x_{NM})$$

$$x_{AM} \equiv (m_{\Psi_A}/m_{\Phi_M})^2$$

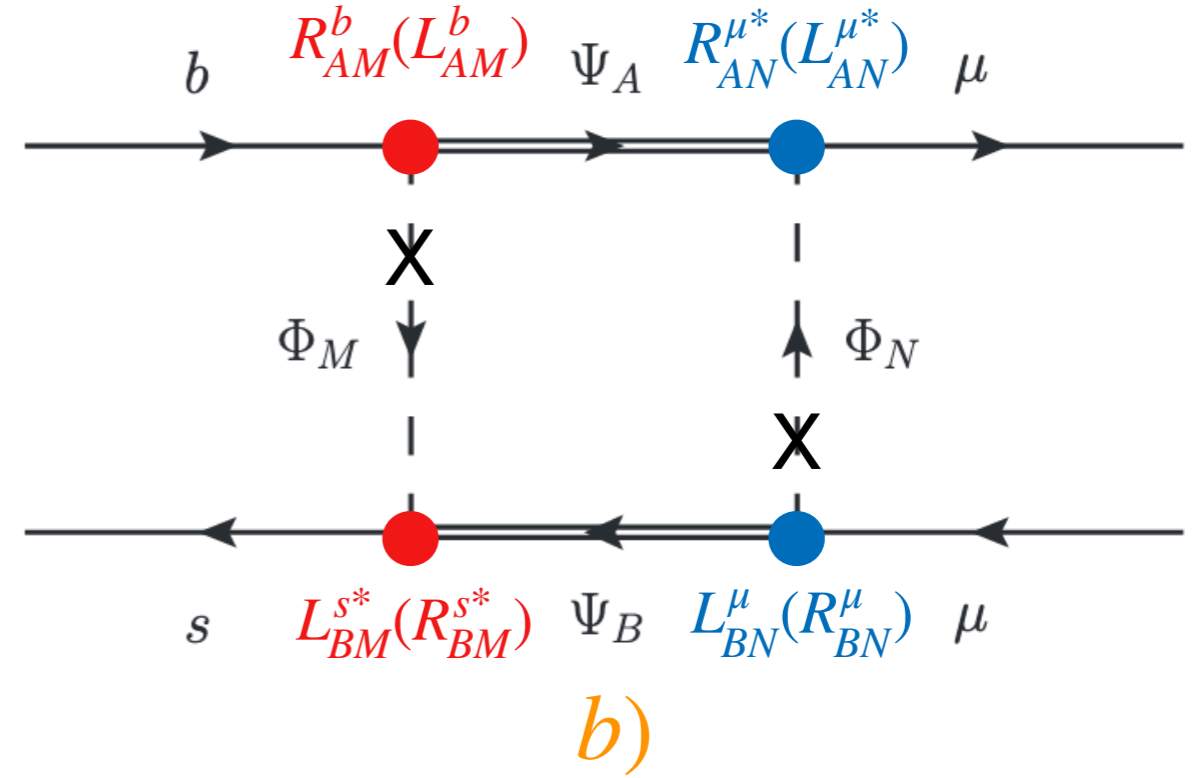
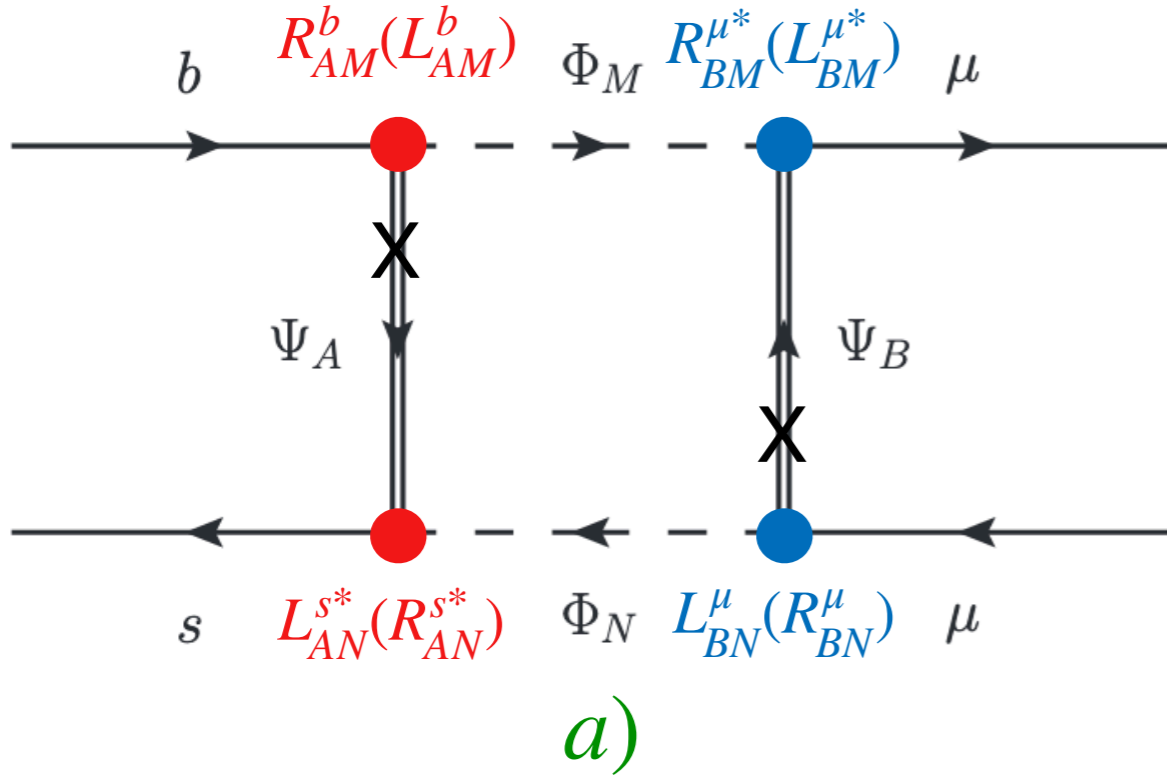
$$C_{9(10)}^{\text{box}} = \pm C_{9(10)}^{\text{box}} (L \leftrightarrow R)$$

$$x_{NM} \equiv (m_{\Phi_N}/m_{\Phi_M})^2$$

$$C_9^{\text{box}, b) = -\mathcal{N} \frac{\chi L_{BM}^{s*} L_{AM}^b}{32\pi\alpha_{\text{EM}} m_{\Phi_M}^2} \left[ L_{AN}^{\mu*} L_{BN}^{\mu} F(x_{AM}, x_{BM}, x_{NM}) - R_{AN}^{\mu*} R_{BN}^{\mu} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \right]$$

$$C_{10}^{\text{box}, b) = \mathcal{N} \frac{\chi L_{BM}^{s*} L_{AM}^b}{32\pi\alpha_{\text{EM}} m_{\Phi_M}^2} \left[ L_{AN}^{\mu*} L_{BN}^{\mu} F(x_{AM}, x_{BM}, x_{NM}) + R_{AN}^{\mu*} R_{BN}^{\mu} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \right]$$

# $b \rightarrow s\mu\mu$



$$C_S^{\text{box}, a) = -\mathcal{N} \frac{\chi L_{AN}^{s*} R_{AM}^b}{16\pi\alpha_{EM} m_{\Phi_M}^2} [R_{BM}^{\mu*} L_{BN}^\mu + L_{BM}^{\mu*} R_{BN}^\mu] \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM})$$

$$C_P^{\text{box}, a) = \mathcal{N} \frac{\chi L_{AN}^{s*} R_{AM}^b}{16\pi\alpha_{EM} m_{\Phi_M}^2} [R_{BM}^{\mu*} L_{BN}^\mu - L_{BM}^{\mu*} R_{BN}^\mu] \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM})$$

$$C_{S,T(P)}^{\text{box}} = \pm C_{S,T(P)}^{\text{box}} (L \leftrightarrow R)$$

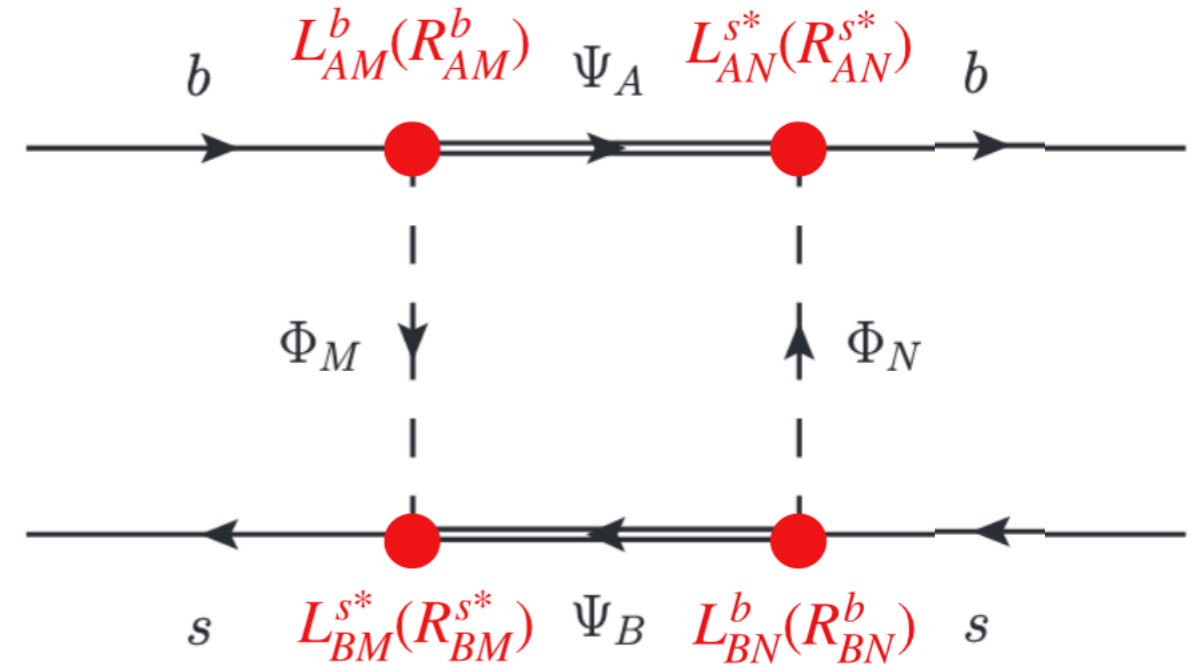
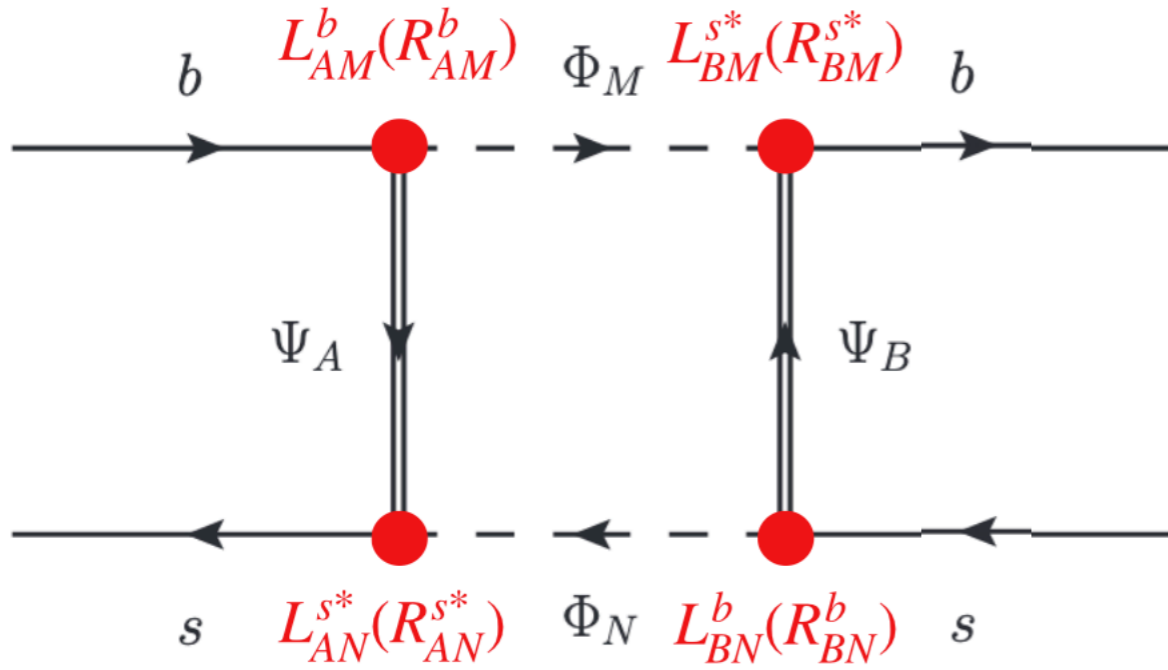
$$C_S^{\text{box}, b) = \mathcal{N} \frac{\chi L_{BM}^{s*} R_{AM}^b}{16\pi\alpha_{EM} m_{\Phi_M}^2} \left[ R_{AN}^{\mu*} L_{BN}^\mu F(x_{AM}, x_{BM}, x_{NM}) + L_{AN}^{\mu*} R_{BN}^\mu \frac{m_{\Psi_A} m_{\Psi_B}}{2m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \right]$$

$$C_P^{\text{box}, b) = -\mathcal{N} \frac{\chi L_{BM}^{s*} R_{AM}^b}{16\pi\alpha_{EM} m_{\Phi_M}^2} \left[ R_{AN}^{\mu*} L_{BN}^\mu F(x_{AM}, x_{BM}, x_{NM}) - L_{AN}^{\mu*} R_{BN}^\mu \frac{m_{\Psi_A} m_{\Psi_B}}{2m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \right]$$

$$C_T^{\text{box}, b) = -\mathcal{N} \frac{\chi L_{BM}^{s*} R_{AM}^b L_{AN}^{\mu*} R_{BN}^\mu}{16\pi\alpha_{EM} m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM})$$

Additional WC present only in the presence of additional SU(2) breaking effects

# $\Delta Ms$

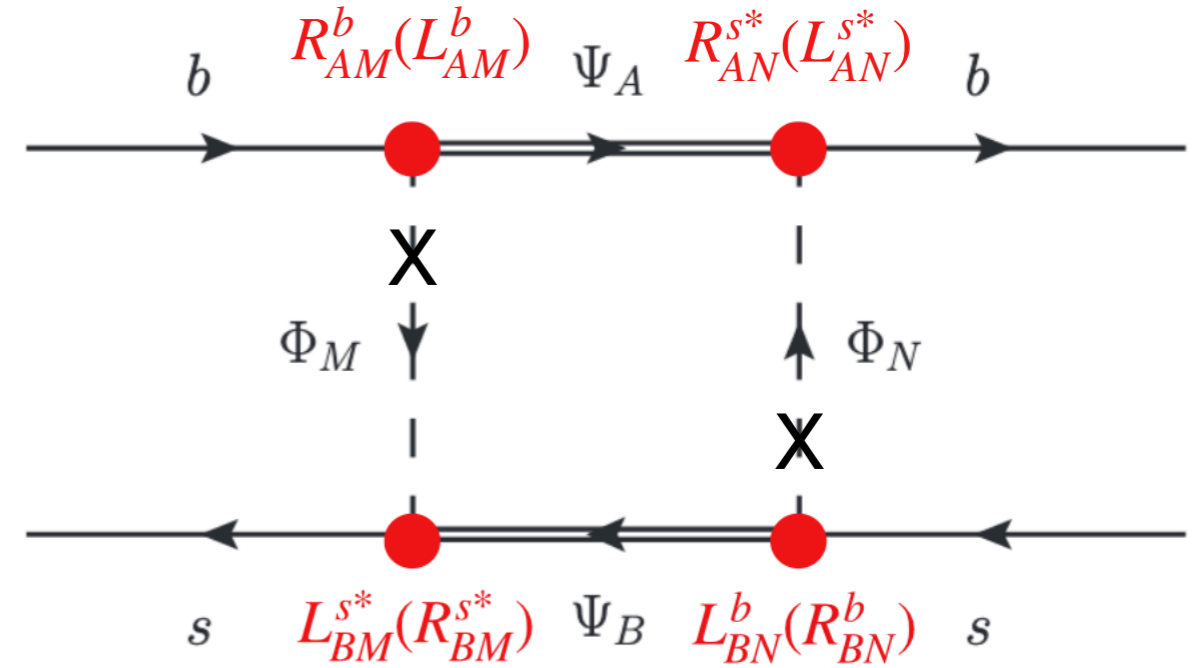
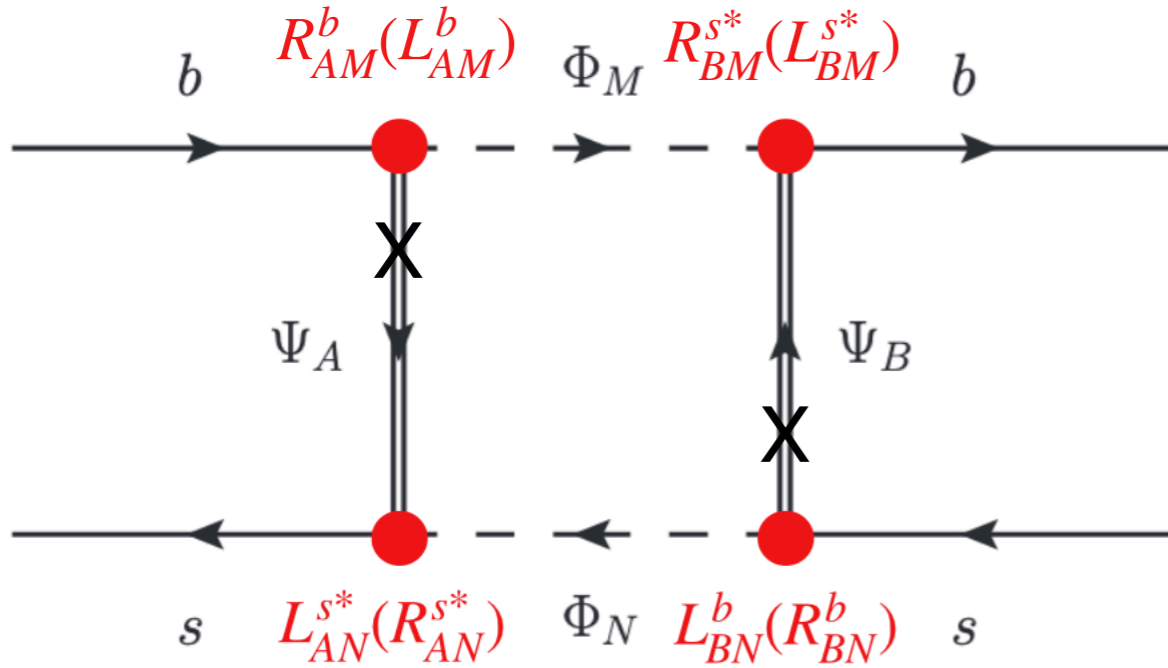


Both diagrams appear, independently on  $b \rightarrow s \mu \mu$ , since no leptons are involved in this channel

$$\begin{aligned}
 C_1 &= (\chi_{BB} + \tilde{\chi}_{BB}) \frac{L_{AN}^{s*} L_{AM}^b L_{BM}^{s*} L_{BN}^b}{128\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), & C_4 &= \chi_{BB} \frac{R_{AN}^{s*} L_{AM}^b L_{BM}^{s*} R_{BN}^b}{32\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \\
 C_2 &= \chi_{BB} \frac{R_{AN}^{s*} L_{AM}^b R_{BM}^{s*} L_{BN}^b}{64\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}), & & \ominus \tilde{\chi}_{BB} \frac{R_{AN}^{s*} R_{AM}^b L_{BM}^{s*} L_{BN}^b}{32\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), \\
 C_3 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b R_{BM}^{s*} L_{BN}^b}{64\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}), & C_5 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b L_{BM}^{s*} R_{BN}^b}{32\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \\
 & & & \ominus \chi_{BB} \frac{R_{AN}^{s*} R_{AM}^b L_{BM}^{s*} L_{BN}^b}{32\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), \\
 \tilde{C}_{1,2,3} &= C_{1,2,3} (L \leftrightarrow R)
 \end{aligned}$$



# $\Delta Ms$



Both diagrams appear, independently on  $b \rightarrow s \mu \mu$ , since no leptons are involved in this channel

$$\begin{aligned}
 C_1 &= (\chi_{BB} + \tilde{\chi}_{BB}) \frac{L_{AN}^{s*} L_{AM}^b L_{BM}^{s*} L_{BN}^b}{128\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), & C_4 &= \chi_{BB} \frac{R_{AN}^{s*} L_{AM}^b L_{BM}^{s*} R_{BN}^b}{32\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \\
 C_2 &= \chi_{BB} \frac{R_{AN}^{s*} L_{AM}^b R_{BM}^{s*} L_{BN}^b}{64\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}), & & \ominus \tilde{\chi}_{BB} \frac{R_{AN}^{s*} R_{AM}^b L_{BM}^{s*} L_{BN}^b}{32\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), \\
 C_3 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b R_{BM}^{s*} L_{BN}^b}{64\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}), & C_5 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b L_{BM}^{s*} R_{BN}^b}{32\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \\
 & & & \ominus \chi_{BB} \frac{R_{AN}^{s*} R_{AM}^b L_{BM}^{s*} L_{BN}^b}{32\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), \\
 \tilde{C}_{1,2,3} &= C_{1,2,3} (L \leftrightarrow R)
 \end{aligned}$$

Additional contributions to WC present in the presence of additional SU(2) breaking effects



# $\Delta M_s$

Additional contributions to WC present in the presence of additional SU(2) breaking effects

$$\begin{aligned}
 C_1 &= (\chi_{BB} + \tilde{\chi}_{BB}) \frac{L_{AN}^{s*} L_{AM}^b L_{BM}^{s*} L_{BN}^b}{128\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}) , \\
 C_2 &= \chi_{BB} \frac{R_{AN}^{s*} L_{AM}^b R_{BM}^{s*} L_{BN}^b}{64\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) , \\
 C_3 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b R_{BM}^{s*} L_{BN}^b}{64\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) , \\
 \tilde{C}_{1,2,3} &= C_{1,2,3} (L \leftrightarrow R) \\
 C_4 &= \chi_{BB} \frac{R_{AN}^{s*} L_{AM}^b L_{BM}^{s*} R_{BN}^b}{32\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) , \\
 &\ominus \tilde{\chi}_{BB} \frac{R_{AN}^{s*} R_{AM}^b L_{BM}^{s*} L_{BN}^b}{32\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}) , \\
 C_5 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b L_{BM}^{s*} R_{BN}^b}{32\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) , \\
 &\ominus \chi_{BB} \frac{R_{AN}^{s*} R_{AM}^b L_{BM}^{s*} L_{BN}^b}{32\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}) ,
 \end{aligned}$$

$$\begin{aligned}
 \frac{\Delta M_s^{\text{exp}}}{\Delta M_s^{\text{SM}}} &= \left| 1 + \sum_{i,j=1}^3 R_i(\mu_b) \frac{\eta_{ij}(\mu_b, \mu_H)}{C_1^{\text{SM}}(\mu_b)} (C_j + \tilde{C}_j) + \sum_{i,j=4}^5 R_i(\mu_b) \frac{\eta_{ij}(\mu_b, \mu_H)}{C_1^{\text{SM}}(\mu_b)} C_j \right| \\
 &= \left| 1 + \frac{0.8 (C_1 + \tilde{C}_1) - 1.9 (C_2 + \tilde{C}_2) + 0.5 (C_3 + \tilde{C}_3) + 5.2 C_4 + 1.9 C_5}{C_1^{\text{SM}}(\mu_b)} \right|
 \end{aligned}$$

$R_i(\mu_b)$ : ratios of matrix elements

$\mu_H$ : heavy scale, set at 1 TeV

# 4th Generation Model

$$\begin{aligned}
 L^{4\text{th}} = & \sum_i \left( \Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \cancel{\Gamma_{u_i}^R \bar{\Psi}_u P_R u_i} + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i \right) \Phi + \text{h.c.} \\
 & + \sum_{C=L,R} \left( \cancel{\lambda_C^U \bar{\Psi}_q P_C \tilde{h} \Psi_u} + \lambda_C^D \bar{\Psi}_q P_C h \Psi_d + \lambda_C^E \bar{\Psi}_\ell P_C h \Psi_e \right) + \text{h.c.} \\
 & + \sum_{F=q,\ell,u,d,e} M_F \bar{\Psi}_F \Psi_F + \kappa h^\dagger h \Phi^\dagger \Phi + m_\Phi^2 \Phi^\dagger \Phi
 \end{aligned}$$

We're interested only in couplings to bottom, strange, muon

# 4th Generation Model

$$\begin{aligned}
 L^{4\text{th}} = & \sum_i \left( \Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \cancel{\Gamma_{u_i}^R \bar{\Psi}_u P_R u_i} + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i \right) \Phi + \text{h.c.} \\
 & + \sum_{C=L,R} \left( \cancel{\lambda_C^U \bar{\Psi}_q P_C \tilde{h} \Psi_u} + \cancel{\lambda_C^D \bar{\Psi}_q P_C h \Psi_d} + \lambda_C^E \bar{\Psi}_\ell P_C h \Psi_e \right) + \text{h.c.} \\
 & + \sum_{F=q,\ell,u,d,e} M_F \bar{\Psi}_F \Psi_F + \kappa h^\dagger h \Phi^\dagger \Phi + m_\Phi^2 \Phi^\dagger \Phi
 \end{aligned}$$

We're interested only in couplings to bottom, strange, muon

We neglect SU(2) breaking for down-type quarks  
(responsible for phenomenological un-relevant scalar/tensor operators)

# 4th Generation Model

$$\begin{aligned}
 L^{4\text{th}} = & \sum_i \left( \Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \cancel{\Gamma_{u_i}^R \bar{\Psi}_u P_R u_i} + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i \right) \Phi + \text{h.c.} \\
 & + \sum_{C=L,R} \left( \cancel{\lambda_C^U \bar{\Psi}_q P_C \tilde{h} \Psi_u} + \cancel{\lambda_C^D \bar{\Psi}_q P_C h \Psi_d} + \lambda_C^E \bar{\Psi}_\ell P_C h \Psi_e \right) + \text{h.c.} \\
 & + \sum_{F=q,\ell,u,d,e} M_F \bar{\Psi}_F \Psi_F + \kappa h^\dagger h \Phi^\dagger \Phi + m_\Phi^2 \Phi^\dagger \Phi
 \end{aligned}$$

Below EWSB:

$$L_{\text{mass}}^{4\text{th}} = \begin{pmatrix} \bar{\Psi}_{\ell,2} \\ \bar{\Psi}_e \end{pmatrix}^T \begin{pmatrix} M_\ell & \sqrt{2}v\lambda_R^E \\ \sqrt{2}v\lambda_L^{E*} & M_e \end{pmatrix} P_L \begin{pmatrix} \Psi_{\ell,2} \\ \Psi_e \end{pmatrix} \Rightarrow \boxed{
 \begin{aligned}
 P_L \begin{pmatrix} \Psi_{\ell,2} \\ \Psi_e \end{pmatrix}_I & \rightarrow W_{IJ}^{E_L} \Psi_J^{E_L} \\
 \begin{pmatrix} \bar{\Psi}_{\ell,2} \\ \bar{\Psi}_e \end{pmatrix}_I^T P_L & \rightarrow \bar{\Psi}_J^{E_R} W_{IJ}^{E_R}
 \end{aligned}
 }$$

# 4th Generation Model

$$L^{4\text{th}} = \sum (\Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \cancel{\Gamma_{u_i}^R \bar{\Psi}_u P_R u_i} + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i) \Phi + \text{h.c.}$$

$$P_L \begin{pmatrix} \Psi_{\ell,2} \\ \Psi_e \end{pmatrix}_I \rightarrow W_{IJ}^{E_L} \Psi_J^{E_L}$$

$$\begin{pmatrix} \bar{\Psi}_{\ell,2} \\ \bar{\Psi}_e \end{pmatrix}_I^T P_L \rightarrow \bar{\Psi}_J^{E_R} W_{IJ}^{E_R}$$

$$P_L \begin{pmatrix} \Psi_{q,2} \\ \Psi_d \end{pmatrix}_I \rightarrow \delta_{IJ} \Psi_J^{D_L}$$

$$\begin{pmatrix} \bar{\Psi}_{q,2} \\ \bar{\Psi}_d \end{pmatrix}_I^T P_L \rightarrow \bar{\Psi}_J^{D_R} \delta_{IJ}$$

$$L_{\text{int}}^{4\text{th}} = (L_1^b \bar{\Psi}_1^D P_L b + L_1^s \bar{\Psi}_1^D P_L s + L_I^\mu \bar{\Psi}_I^E P_L \mu) \Phi$$

$$+ (R_2^b \bar{\Psi}_1^D P_R b + R_2^s \bar{\Psi}_1^D P_R s + R_I^\mu \bar{\Psi}_I^E P_R \mu) \Phi$$

$$L_1^s = \Gamma_s^L, \quad L_1^b = \Gamma_b^L, \quad R_2^s = \Gamma_s^R, \quad R_2^b = \Gamma_b^R,$$

$$L_1^\mu = \Gamma_\mu^L \cos \theta_L, \quad L_2^\mu = -\Gamma_\mu^L \sin \theta_L, \quad R_1^\mu = \Gamma_\mu^R \sin \theta_R, \quad R_2^\mu = \Gamma_\mu^R \cos \theta_R$$

# 4th Generation Model - WC

$$\Gamma^L \equiv L_1^b L_1^{s*}, \quad \Gamma^R \equiv R_2^b R_2^{s*}$$

## ● $b \rightarrow s \mu \mu$

$$C_9^{\text{box}} = -\mathcal{N} \frac{\Gamma^L}{32\pi\alpha_{\text{EM}}m_\Phi^2} (|\Gamma_\mu^L|^2 + |\Gamma_\mu^R|^2) F(x_D, x_E)$$

$$C_{10}^{\text{box}} = \mathcal{N} \frac{\Gamma^L}{32\pi\alpha_{\text{EM}}m_\Phi^2} (|\Gamma_\mu^L|^2 - |\Gamma_\mu^R|^2) F(x_D, x_E)$$

$$C_{9(10)}^{\text{box}} = \pm C_{9(10)}^{\text{box}} (L \leftrightarrow R)$$

## ● $\Delta M_S$

$$C_1 = \frac{|\Gamma^L|^2}{128\pi^2 m_\Phi^2} F(x_D), \quad C_5 = -\frac{\Gamma^L \Gamma^R}{32\pi^2 m_\Phi^2} F(x_D), \quad \tilde{C}_1 = \frac{|\Gamma^R|^2}{128\pi^2 m_\Phi^2} F(x_D)$$

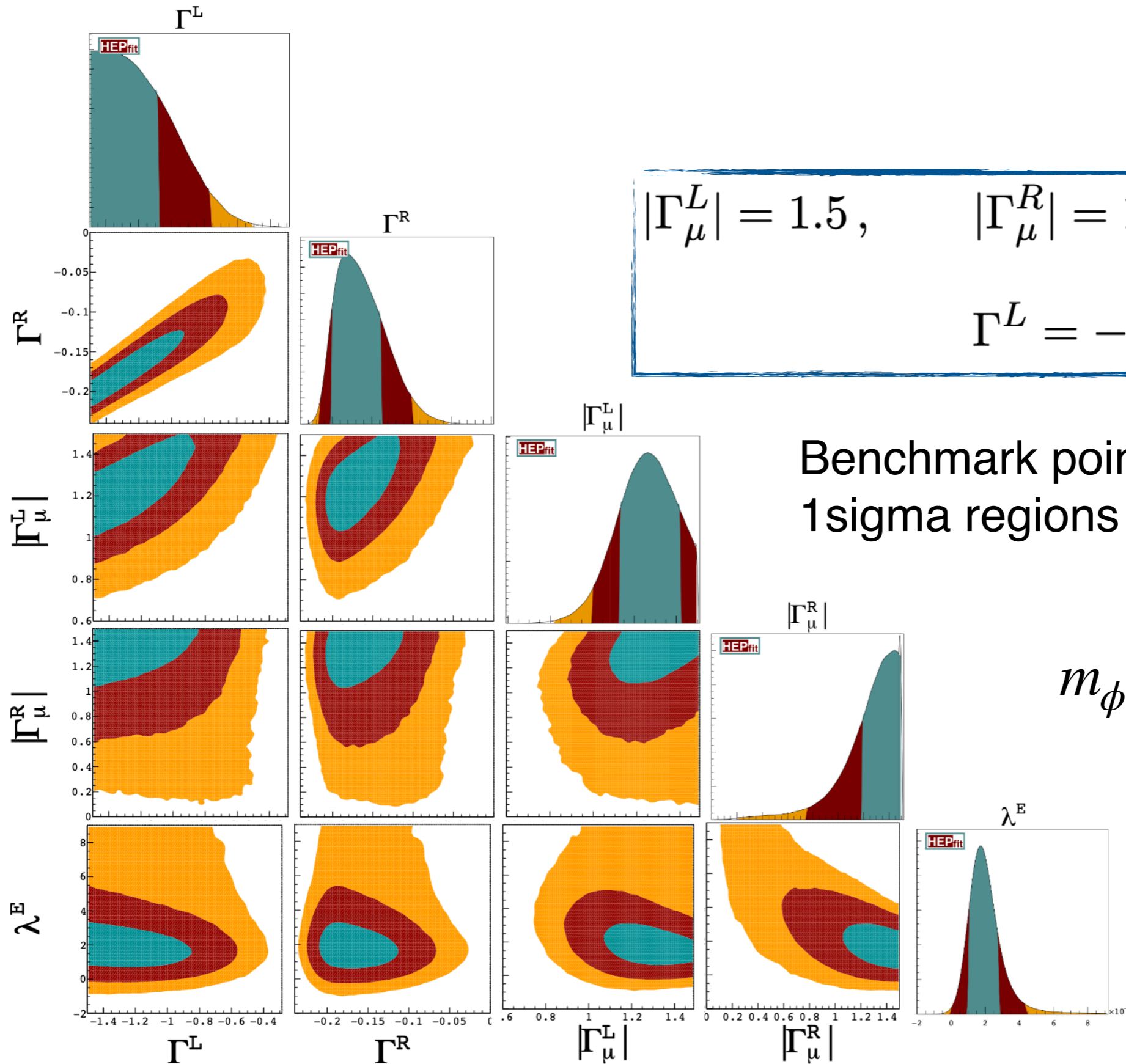
## ● g-2

$$\lambda_R^E = -\lambda_L^E \equiv \lambda^E$$

$$\Delta a_\mu = \frac{m_\mu^2}{8\pi^2 m_\Phi^2} \left[ (|\Gamma_\mu^L|^2 + |\Gamma_\mu^R|^2) F_7(x_E) + \frac{8}{\sqrt{2}} \frac{v \lambda^E}{m_\mu} \Gamma_\mu^L \Gamma_\mu^R G_7(x_E) \right]$$



# Global Fit



$$|\Gamma_\mu^L| = 1.5, \quad |\Gamma_\mu^R| = 1.4, \quad \lambda^E = 0.0015$$

$$\Gamma^L = -1.0, \quad \Gamma^R = -0.12$$

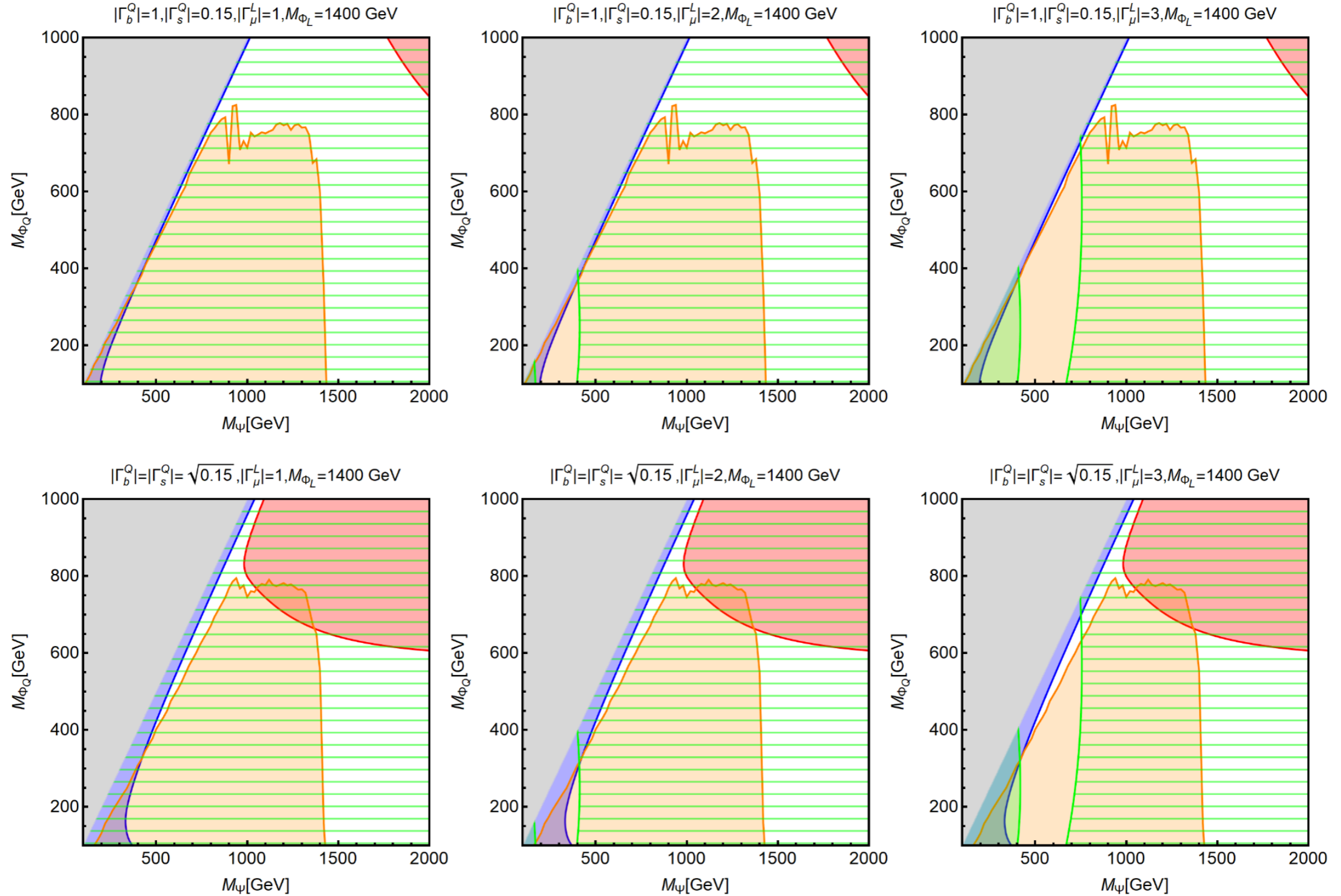
Benchmark point, compatible with all 1 sigma regions of combined pdf

$$m_\phi = m_E = 450 \text{ GeV}$$

$$m_D = 3150 \text{ GeV}$$

# $F_{IB}$ with real DM

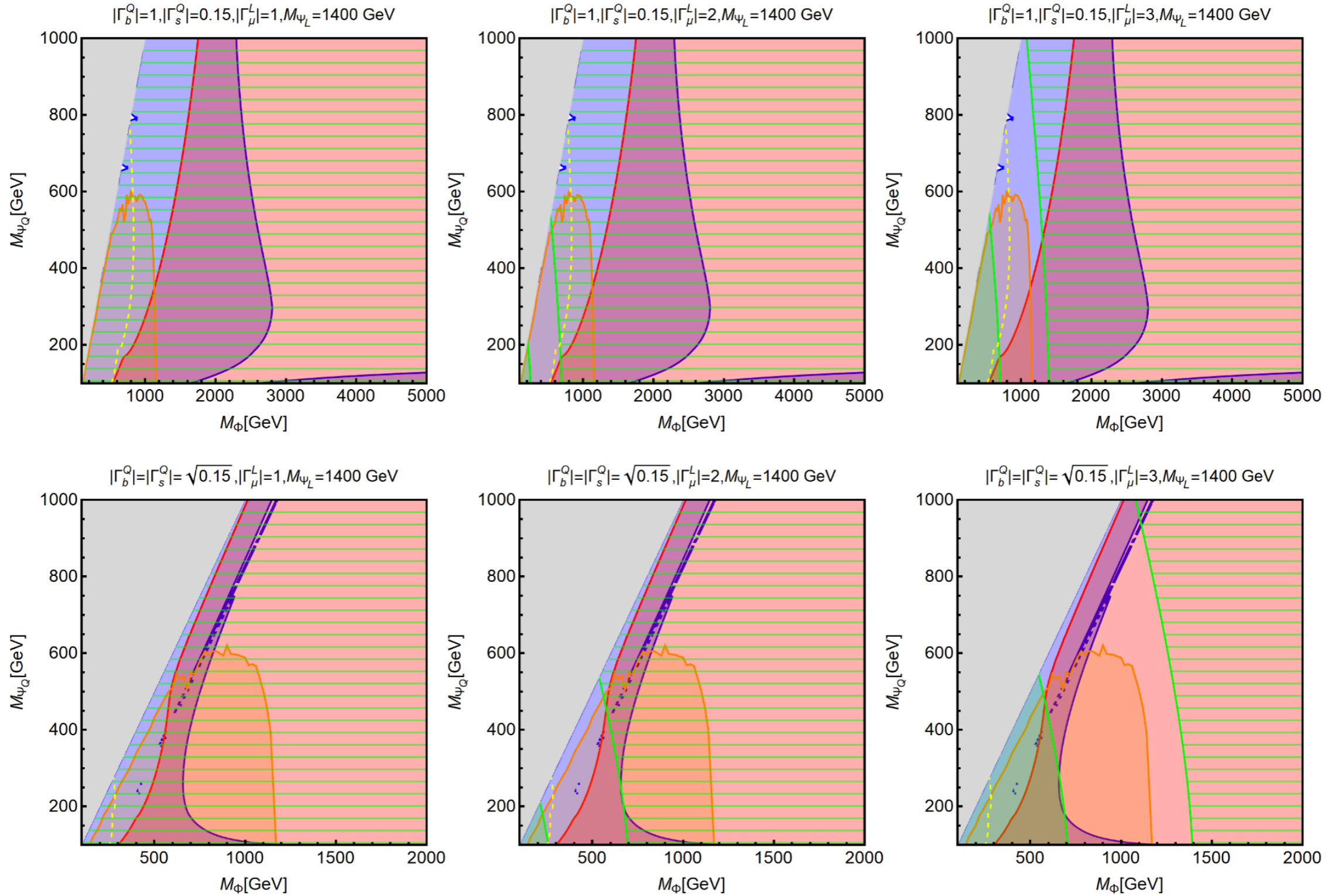
$\Phi_Q$	$\Phi_L$	$\Psi$
$(\mathbf{1}, \mathbf{2}, 1/2)^*$	$(\mathbf{\bar{3}}, \mathbf{2}, -1/6)$	$(\mathbf{3}, \mathbf{1}, -1/3)$



Requires mass splitting between CP-even and CP-odd DM comp. Either an under-abundant DM is produced, or a not-good-enough contribution to B-anomalies

# S<sub>II</sub>B with Dirac DM

$\Psi_Q$	$\Psi_L$	$\Phi$
$(1, 1, 0)^*$	$(\bar{3}, 1, -2/3)$	$(3, 2, 1/6)$

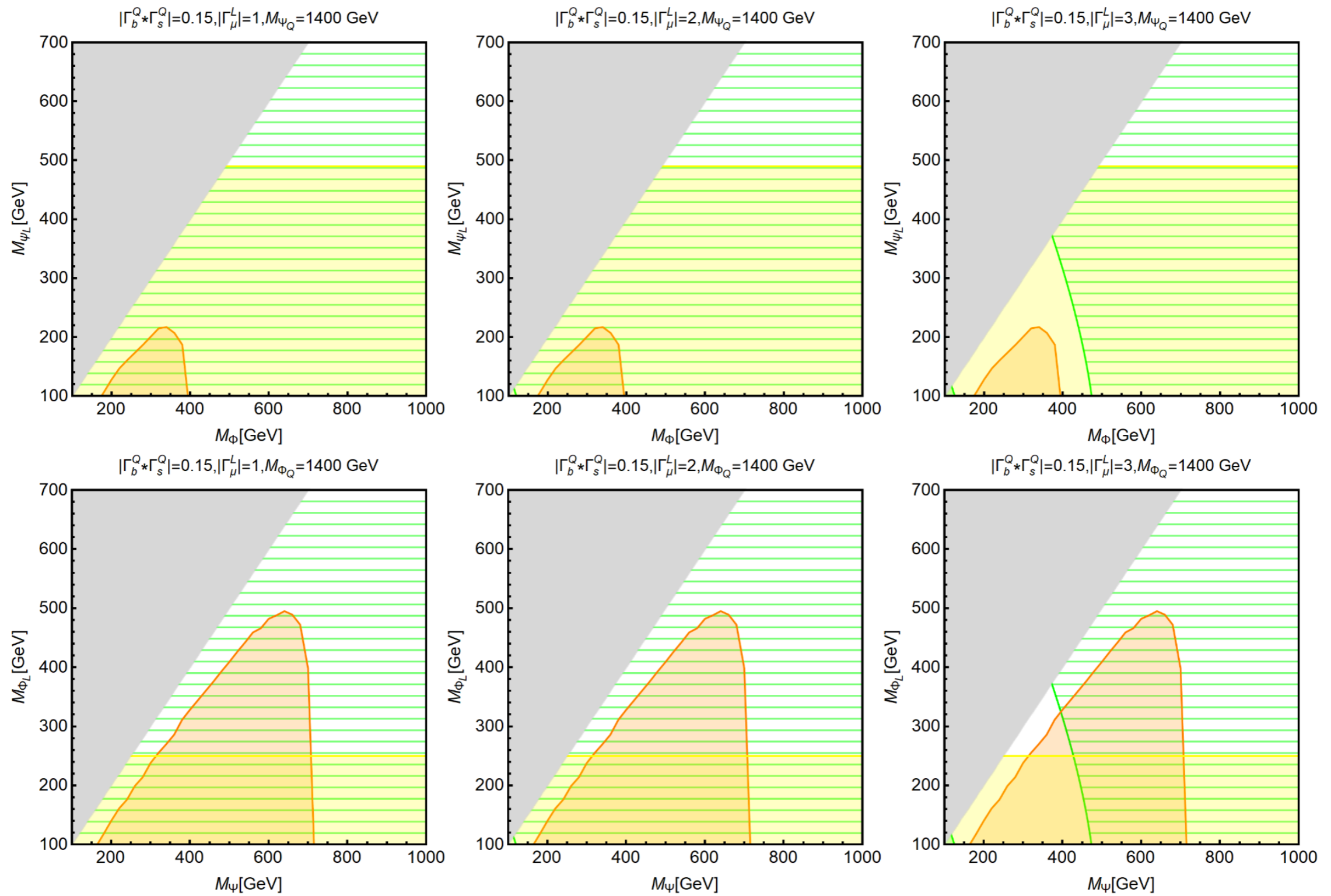


Model excluded by DM bounds!

$\Psi_Q$	$\Psi_L$	$\Phi$
$(\mathbf{3}, \mathbf{3}, 2/3)$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)^*$

# S<sub>IIIA</sub> and F<sub>IIIA</sub>: triplet DM

$\Phi_Q$	$\Phi_L$	$\Psi$
$(\mathbf{3}, \mathbf{3}, 2/3)$	$(\mathbf{1}, \mathbf{3}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)$

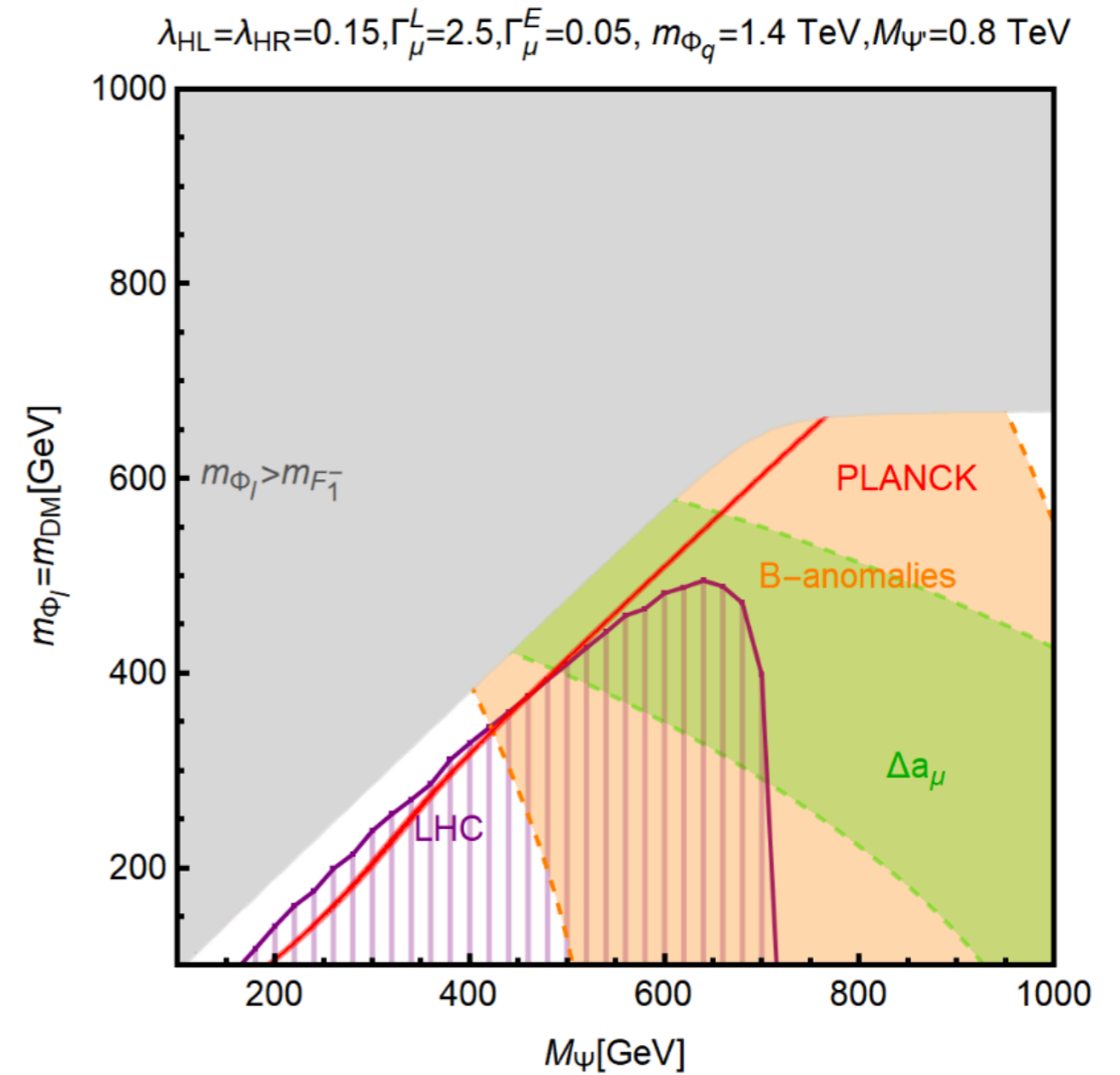
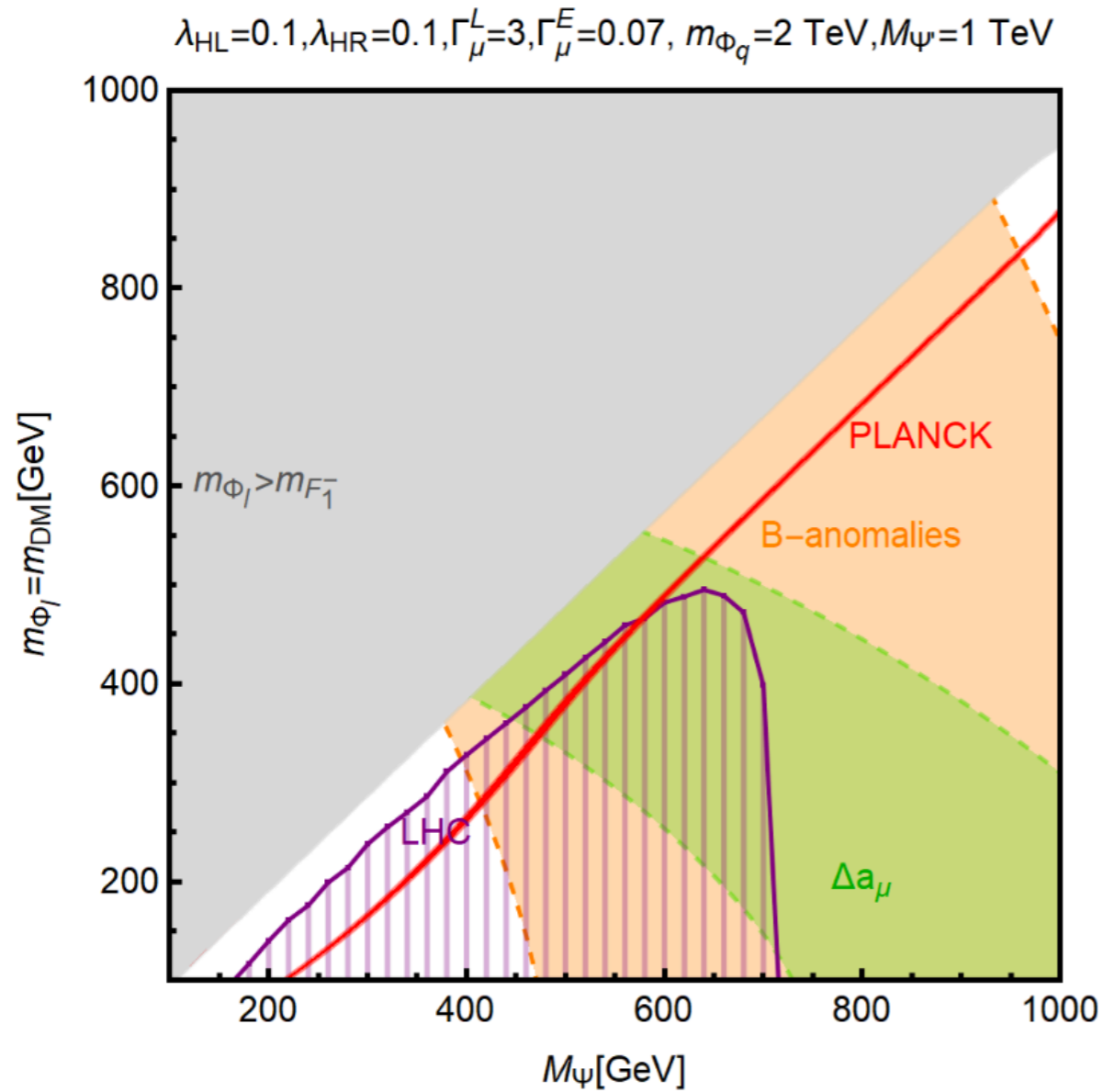


**Models strongly constraint by LHC disappearing tracks,  
DM strongly under-abundant!**



# F<sub>IIB</sub> with singlet DM

$\Phi_Q$	$\Phi_L$	$\Psi$	$\Psi'$
$(\mathbf{3}, \mathbf{1}, 2/3)$	$(\mathbf{1}, \mathbf{1}, 0)^*$	$(\mathbf{1}, \mathbf{2}, -1/2)$	$(\mathbf{1}, \mathbf{1}, -1)$



Viable model to address everything simultaneously!