

# Collider Physics at the Precision Frontier

**Gudrun Heinrich** *Institute for Theoretical Physics*

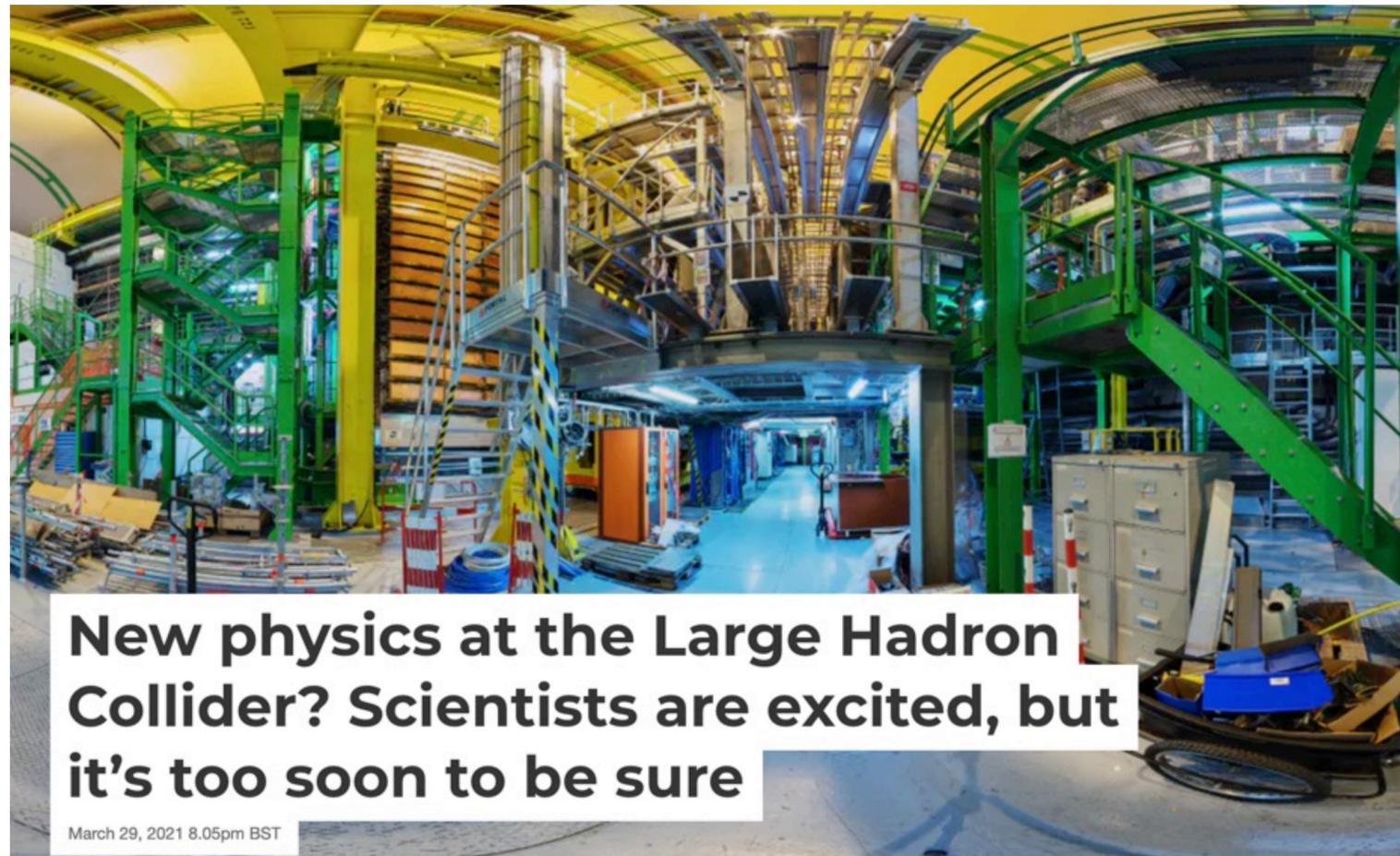


**KSETA plenary workshop**

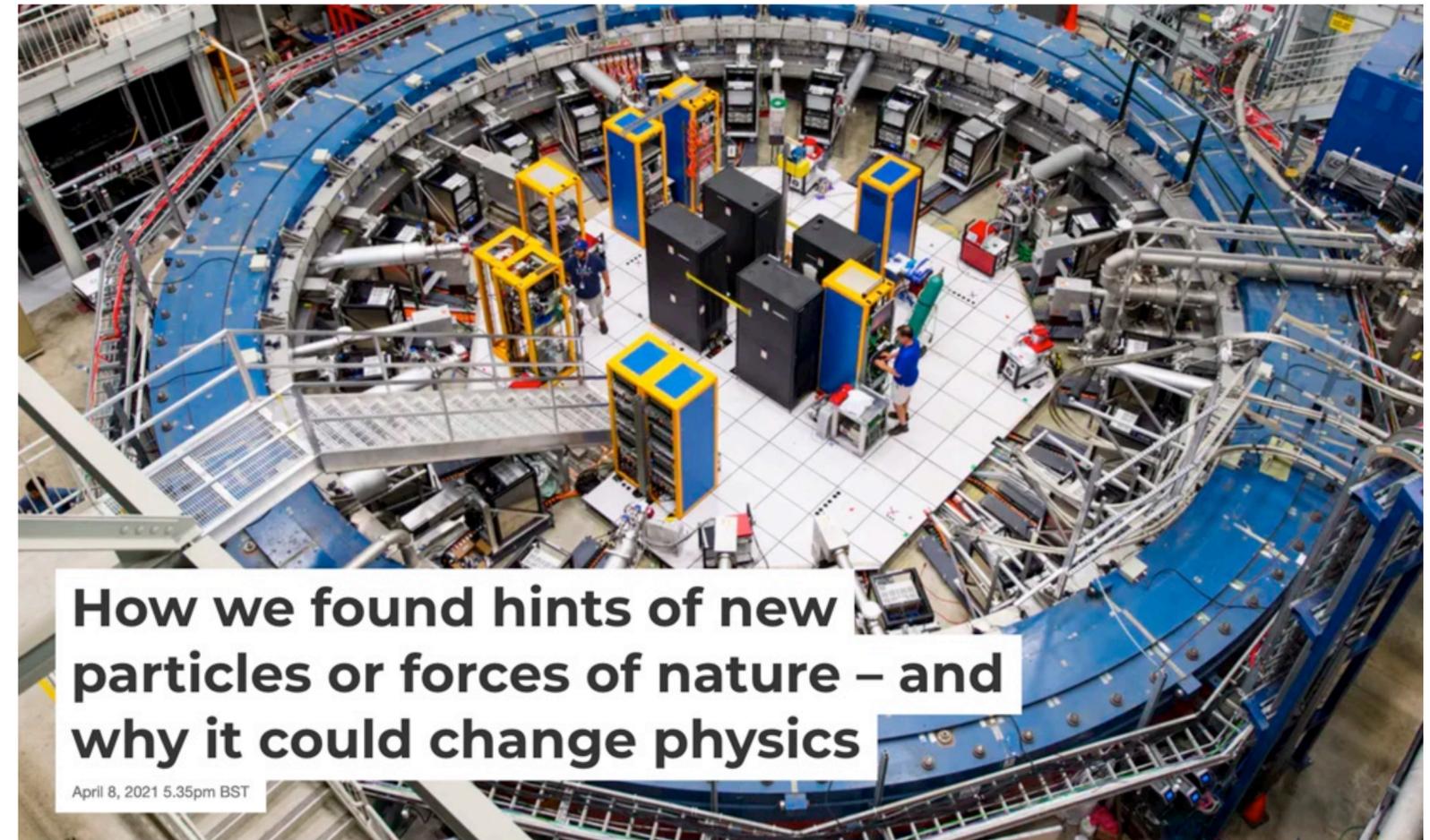
*Durbach, September 27, 2021*

# Motivation

The Standard Model of Particle Physics is unlikely to be the end of the story



LHCb (CERN)



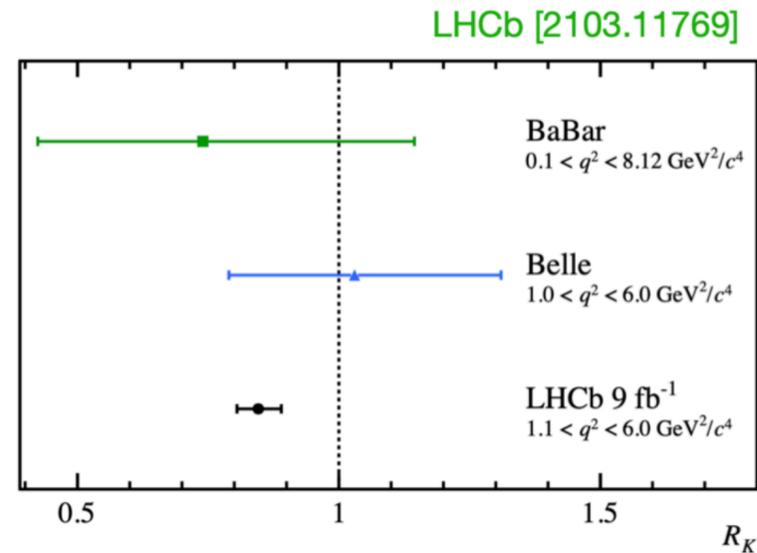
The muon experiment. Reidar Hahn/Fermilab

muon anomalous magnetic moment measurement (Fermilab)

# Motivation

Exciting new experimental value of  $R_K$

$$R_H \equiv \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(B \rightarrow H\mu^+\mu^-)}{dq^2} dq^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(B \rightarrow He^+e^-)}{dq^2} dq^2}$$

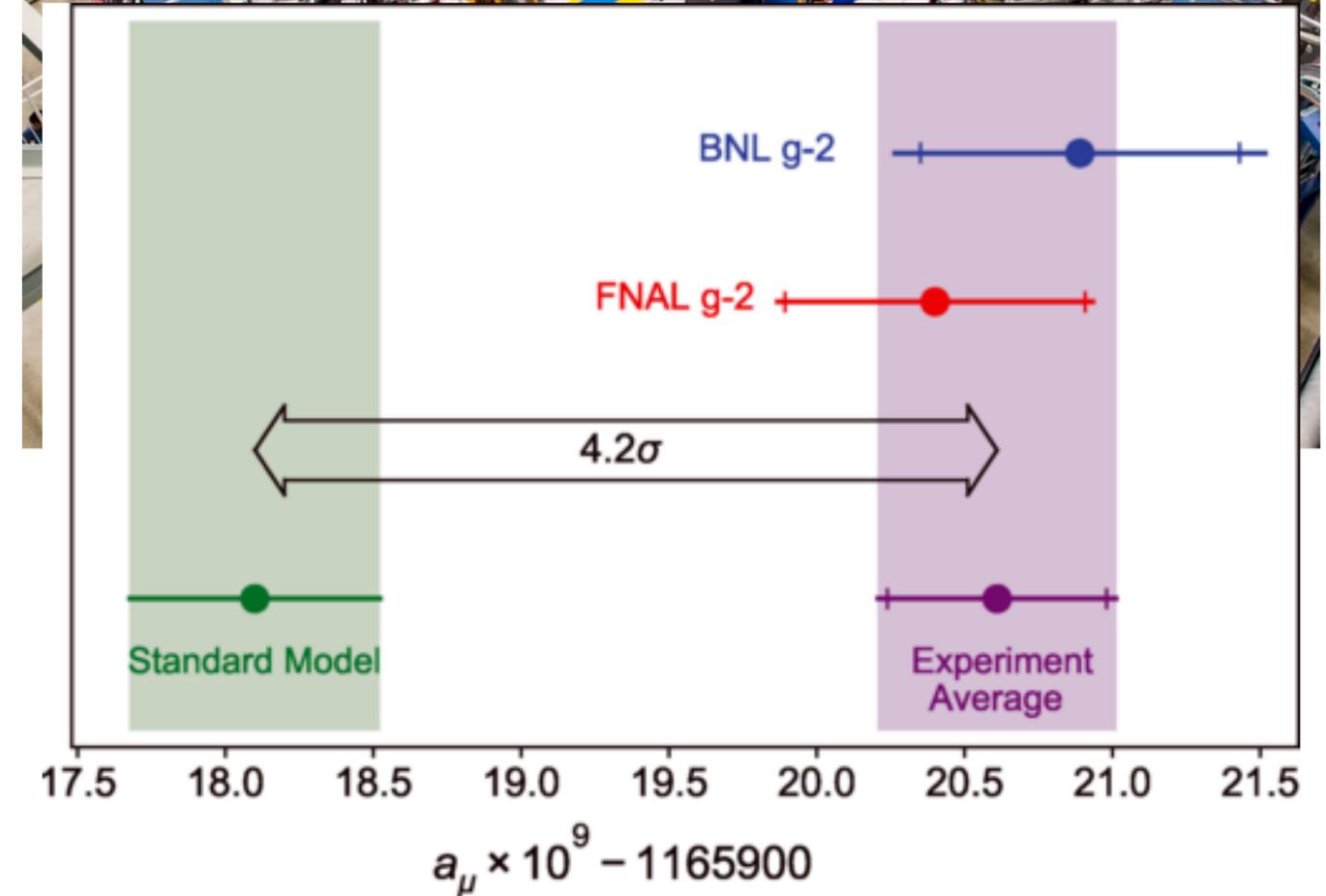


$$R_K^{\text{LHCb}} = 0.846^{+0.042+0.013}_{-0.039-0.012}$$

+ Likelihood

⇒ 3.1σ !!

M. Alguero, Moriond 2021



New physics at the Large Hadron Collider? Scientists are excited, but it's too soon to be sure

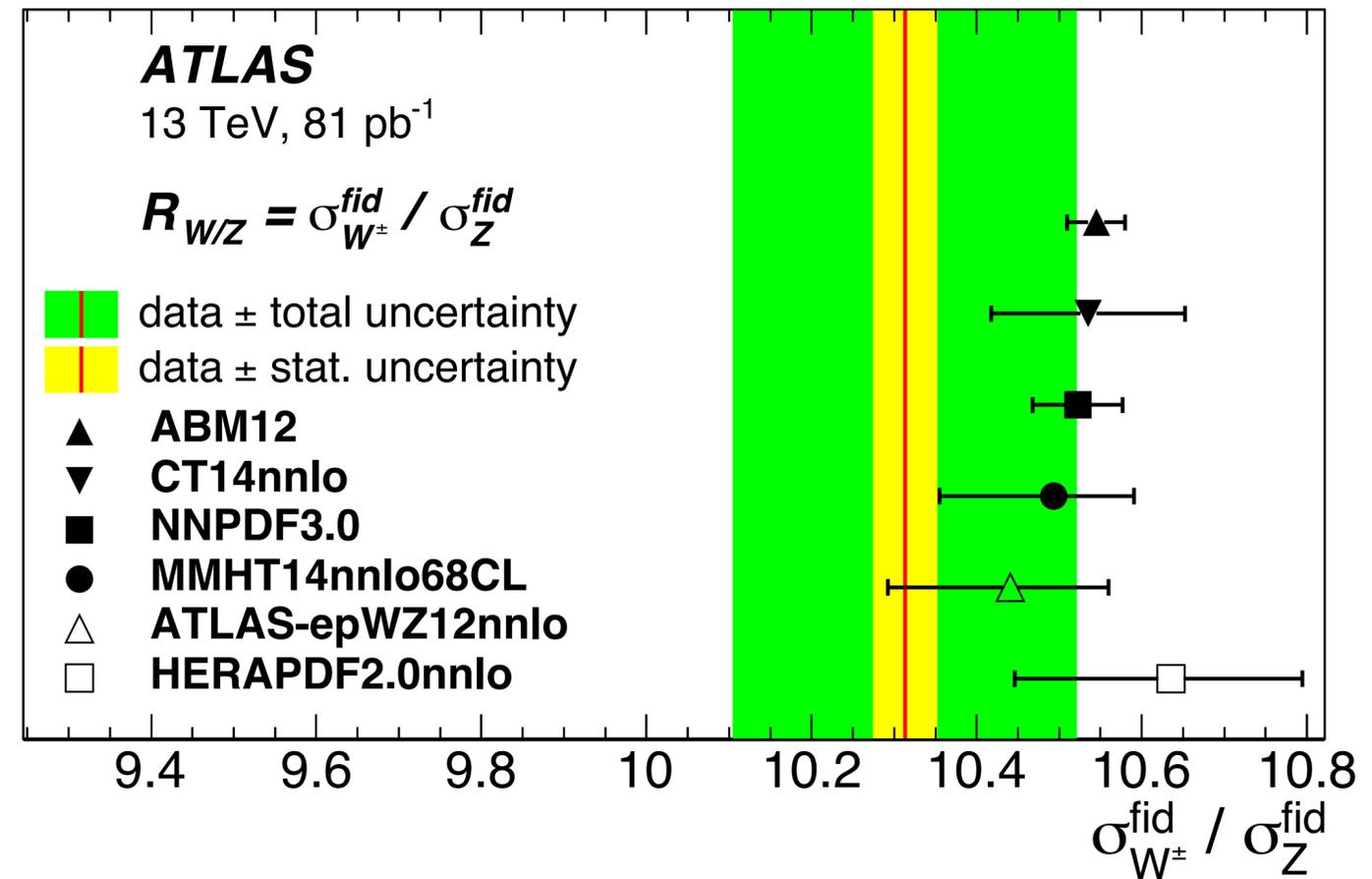
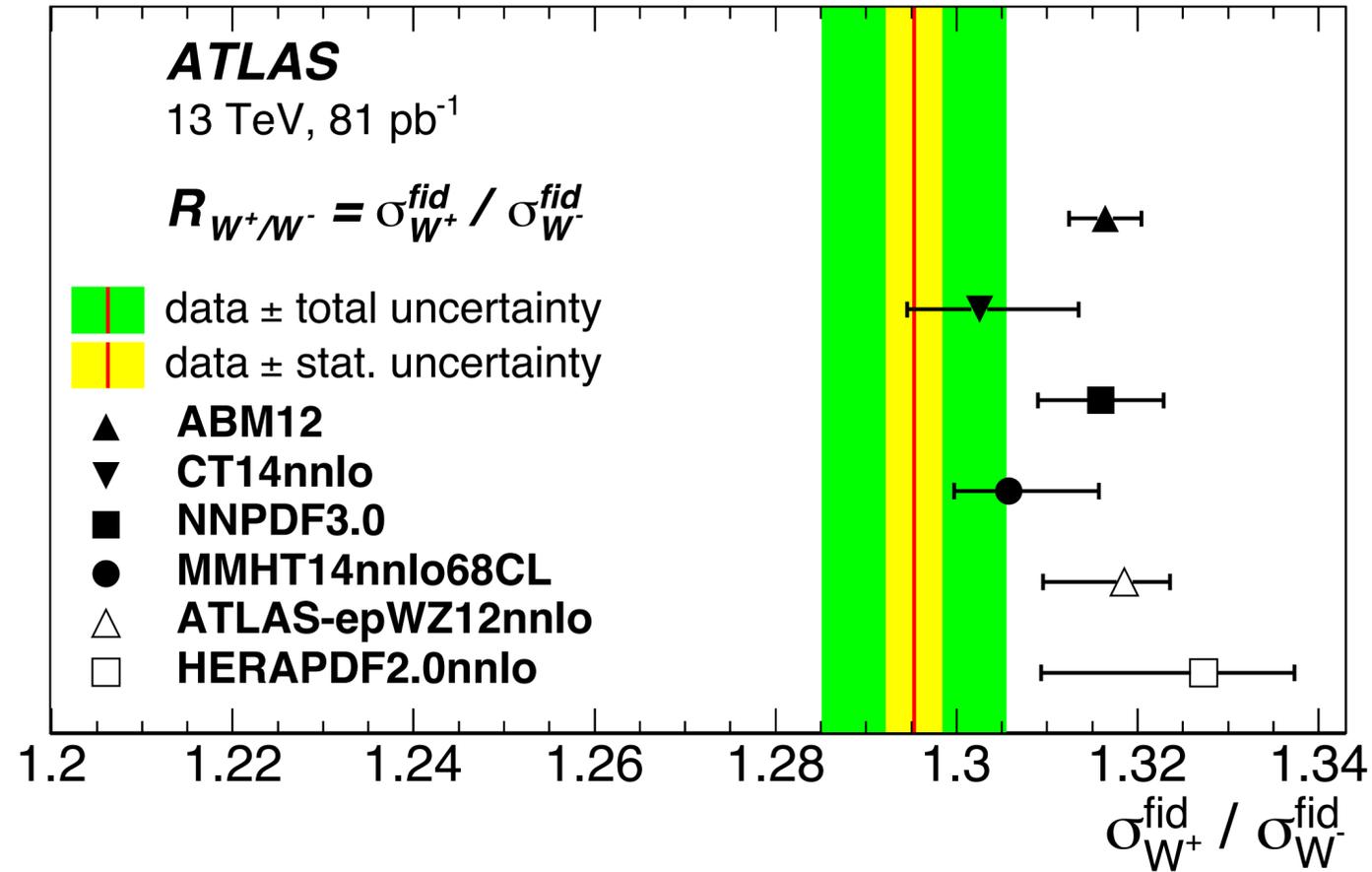
March 29, 2021 8.05pm BST

# Current high energy frontier





# The need for precise predictions

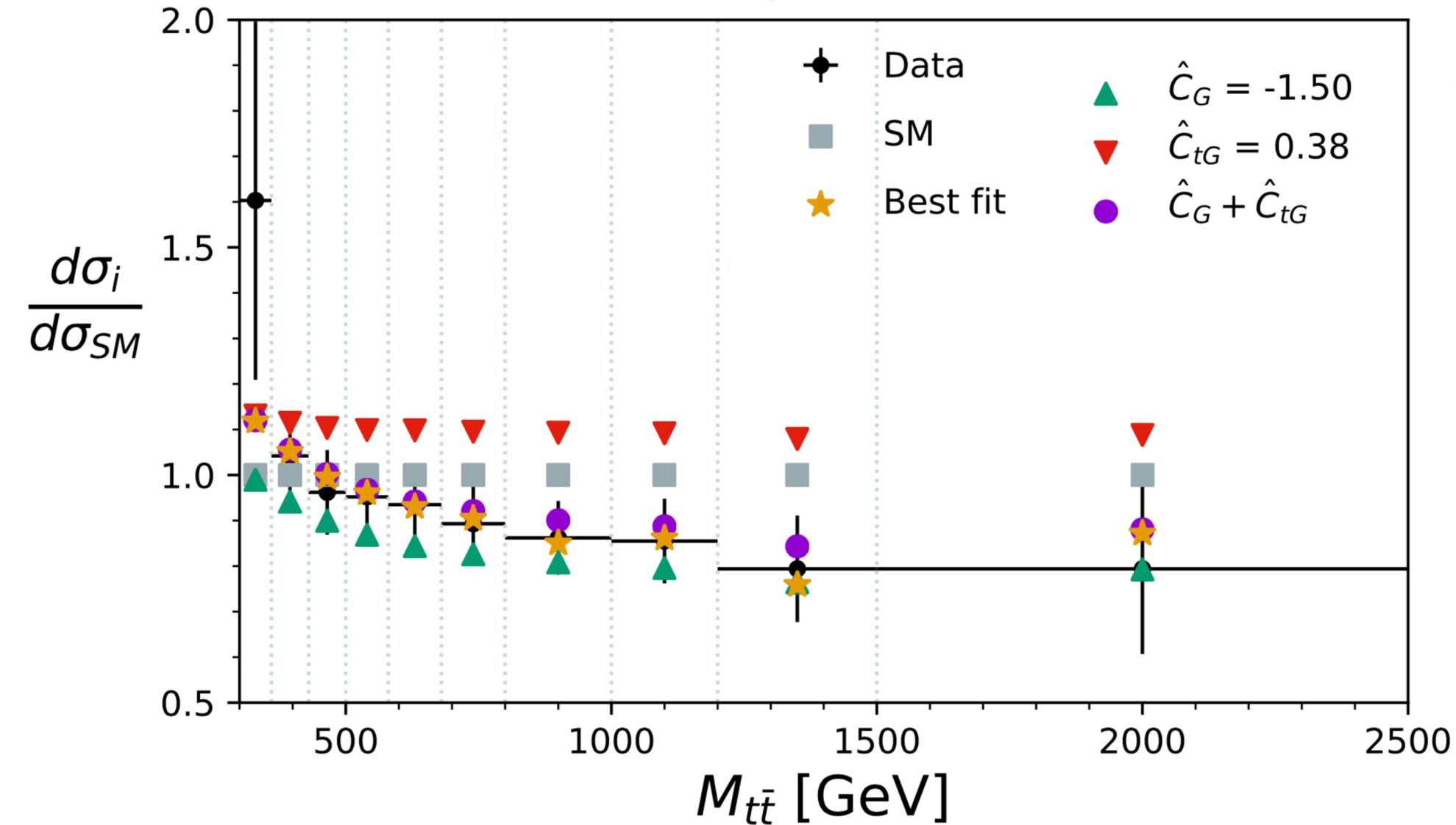


1603.09222

large spread in theory predictions based on different parton distribution functions

# EFT parametrisation of new physics effects

## CMS $t\bar{t}(l+jets)$ , 13 TeV



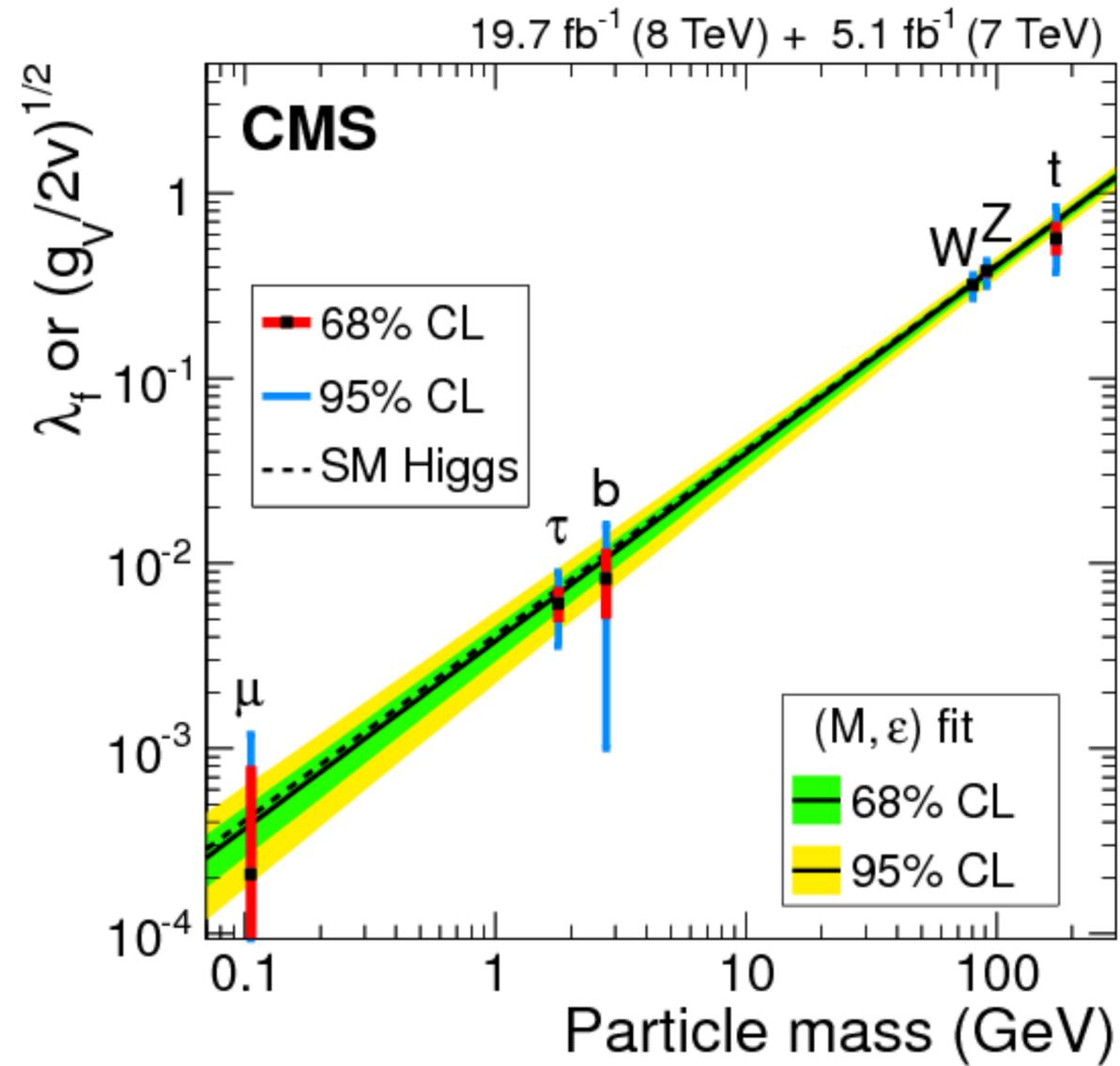
top quark pairs at large invariant mass

best fit includes anomalous couplings

J. Ellis, Madigan, Mimasu, Sanz, You  
2012.02779

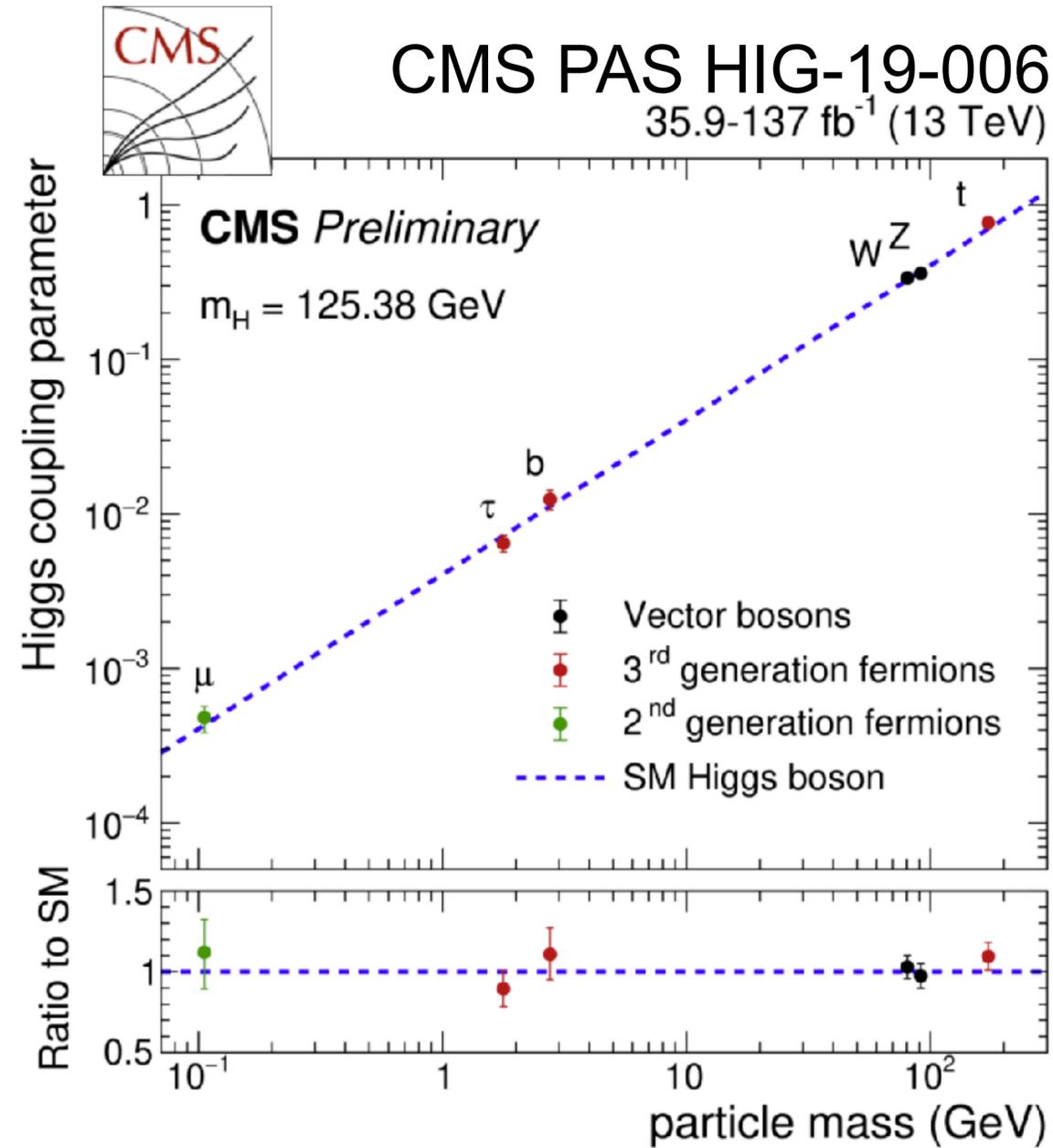
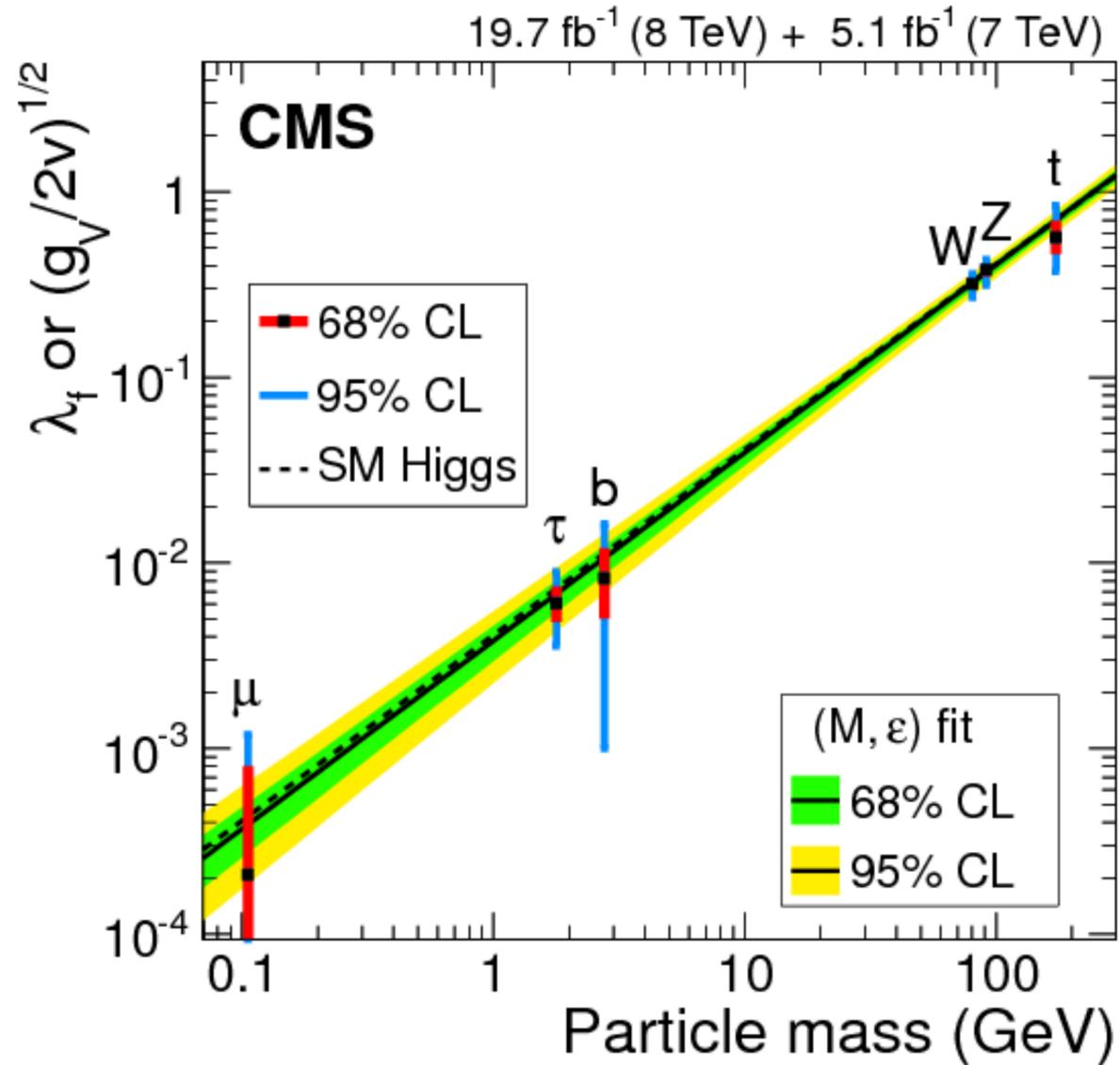
# Higgs couplings

Run I



# Higgs couplings

Run I



H?

**enormous experimental progress**

# High-Luminosity LHC

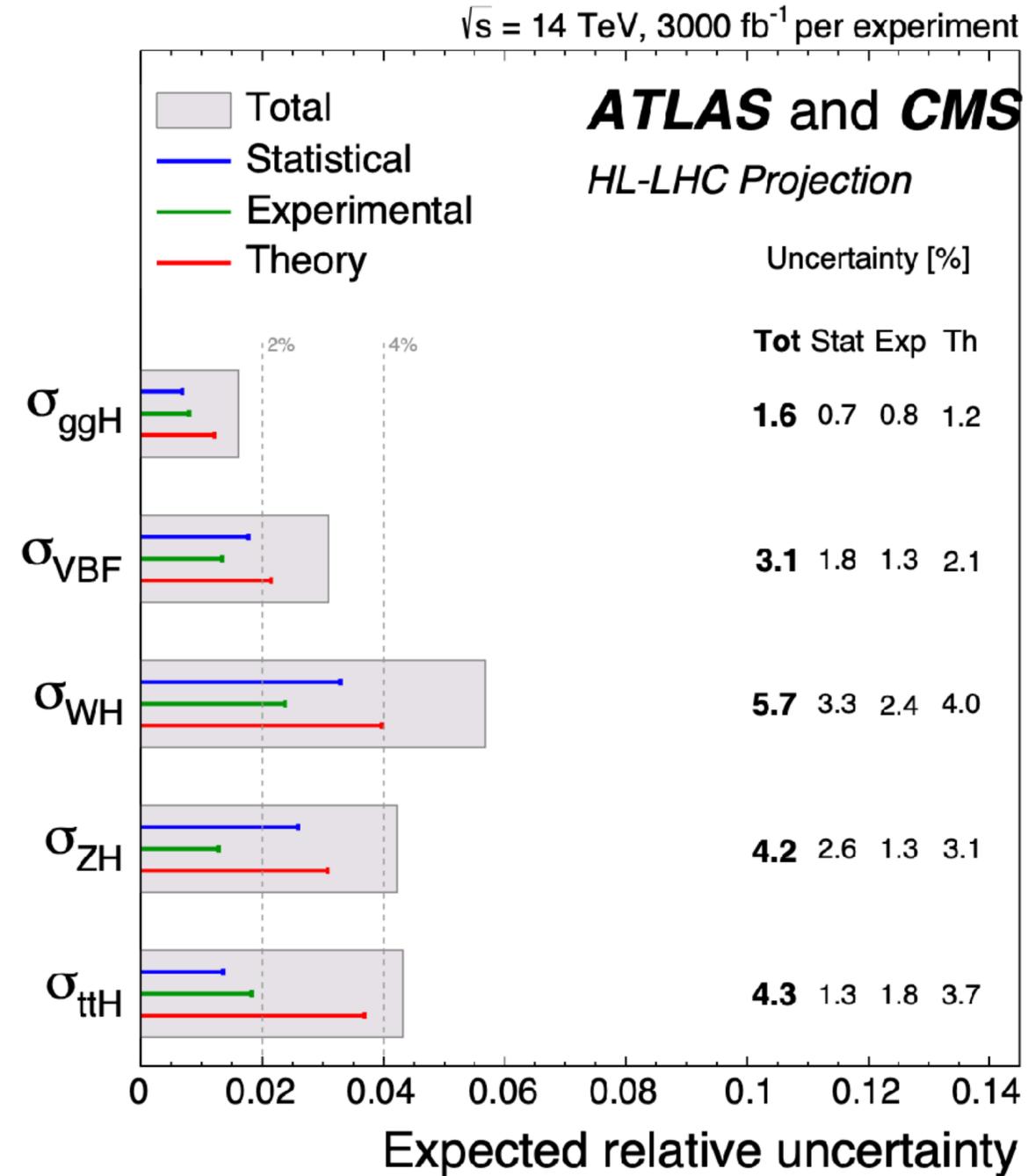
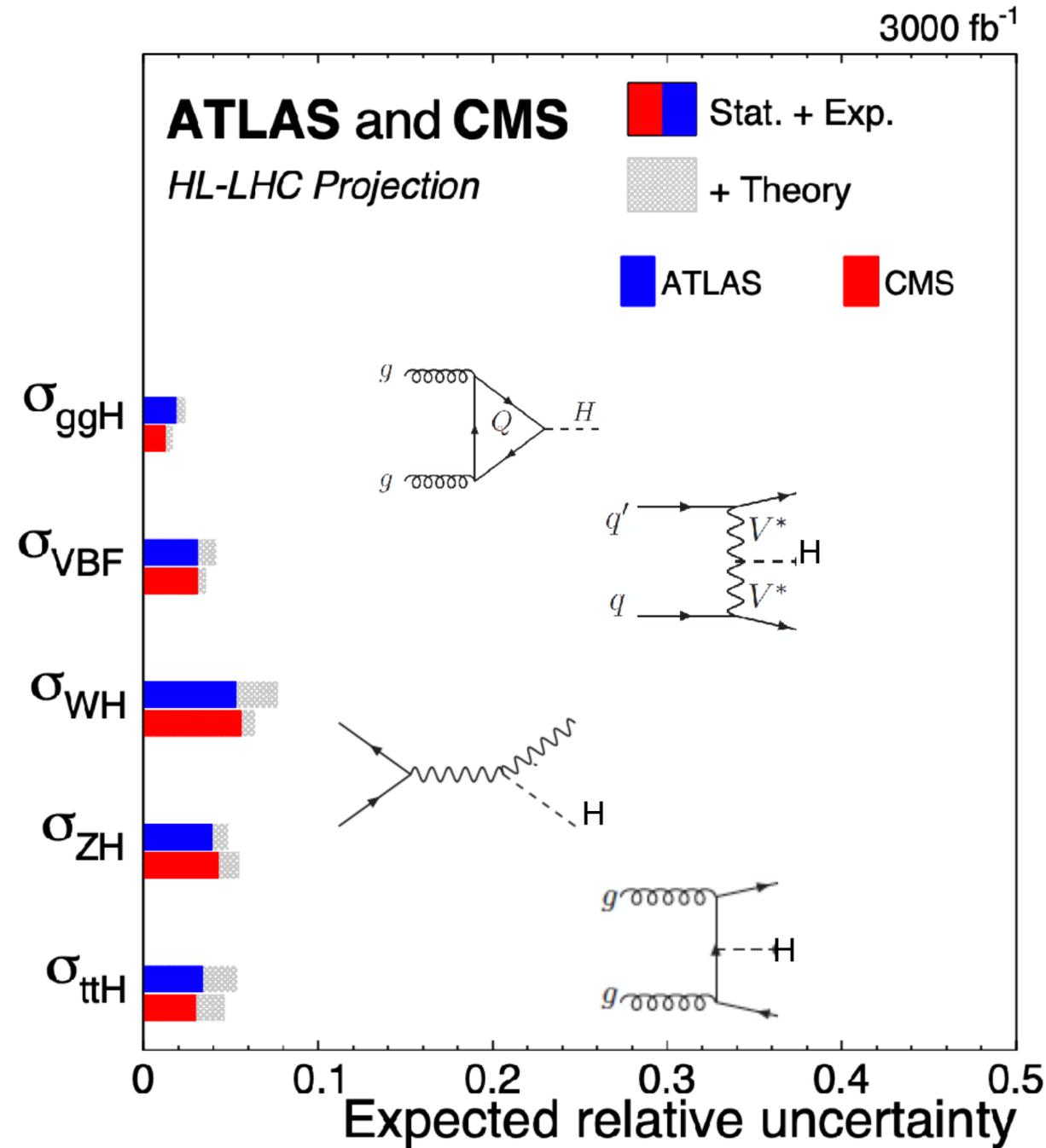


$$\text{rate } R = L \cdot \sigma(s)$$

# Low-luminosity LHC

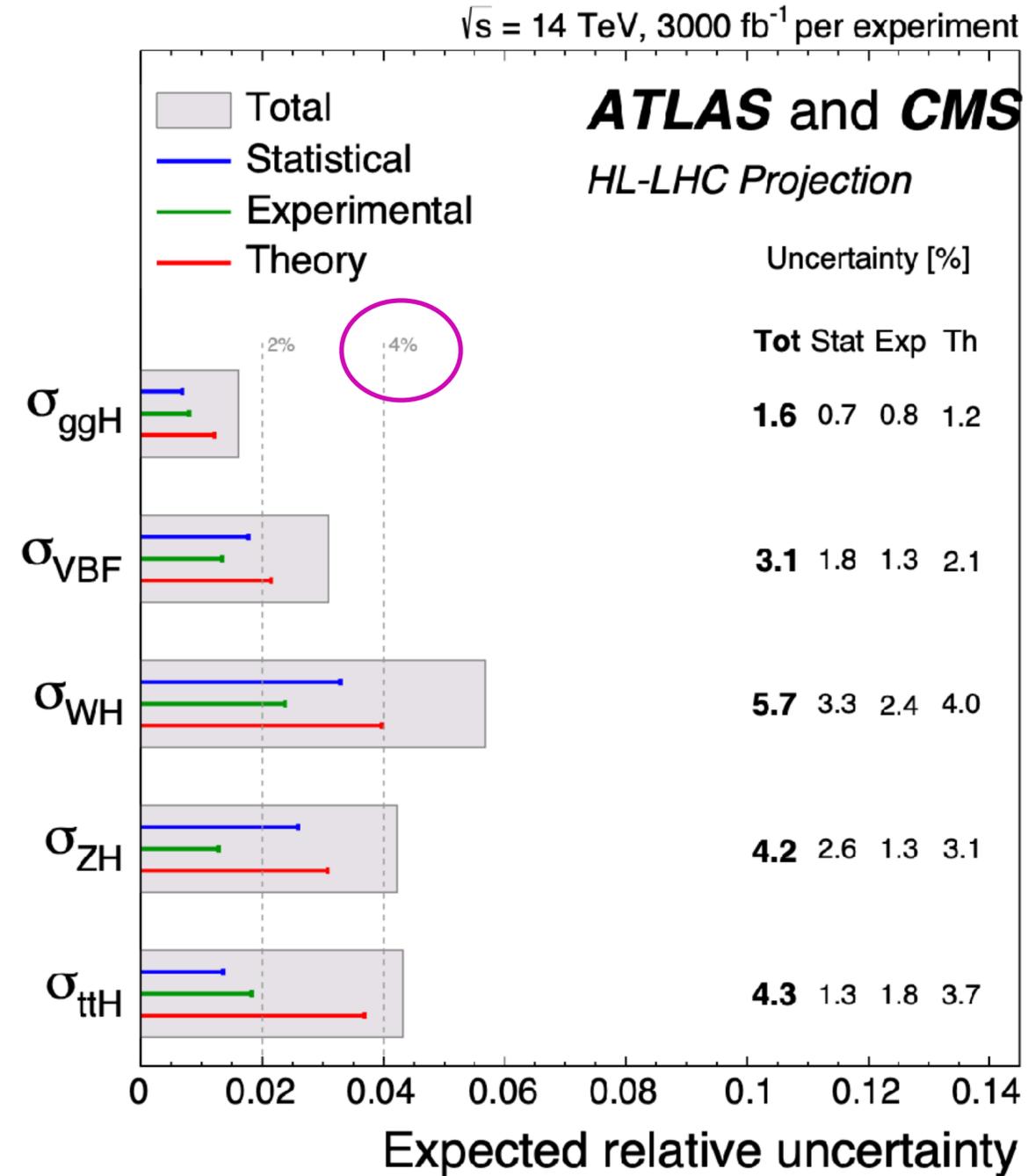
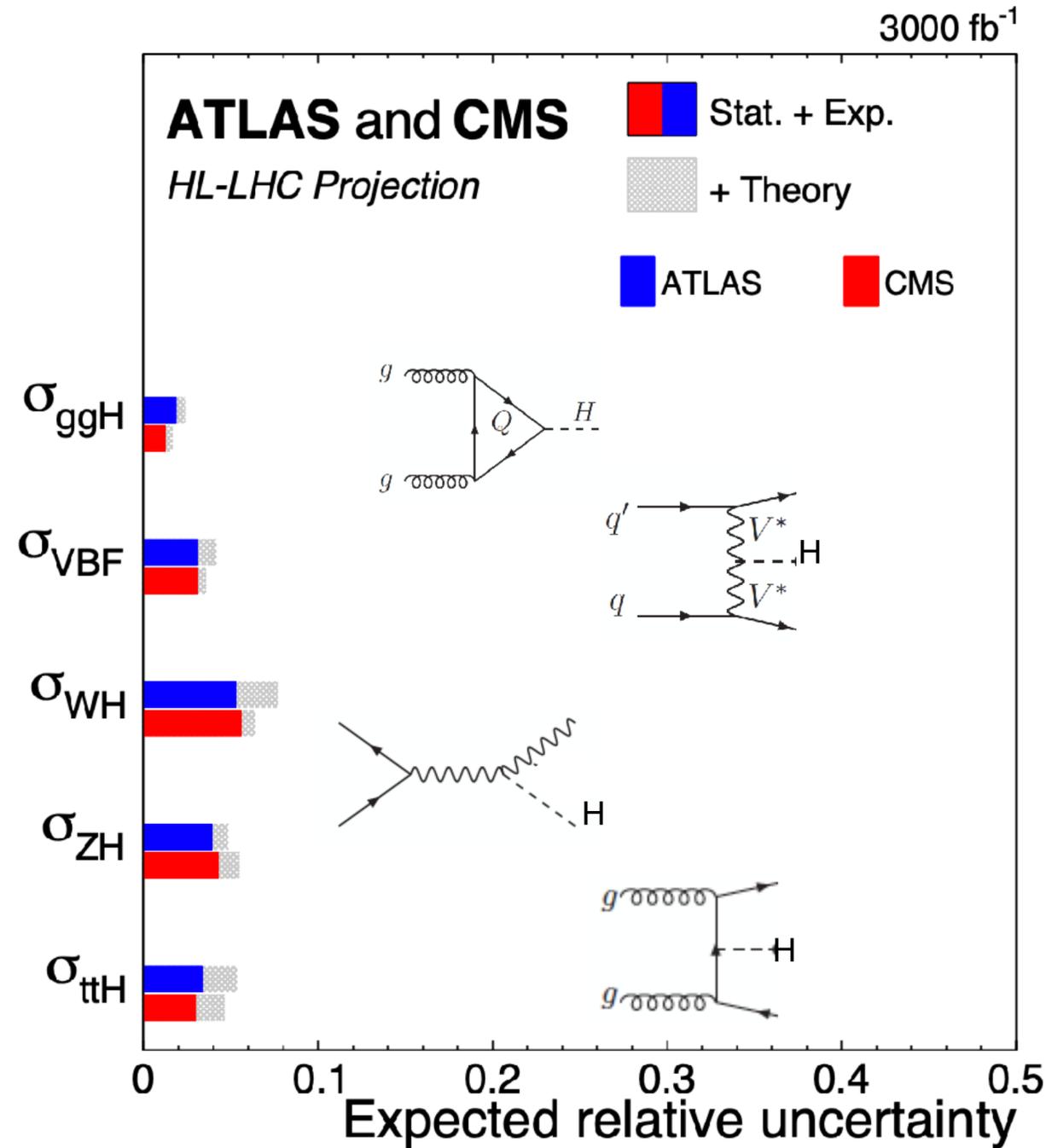


# Higgs production at HL-LHC: expected precision



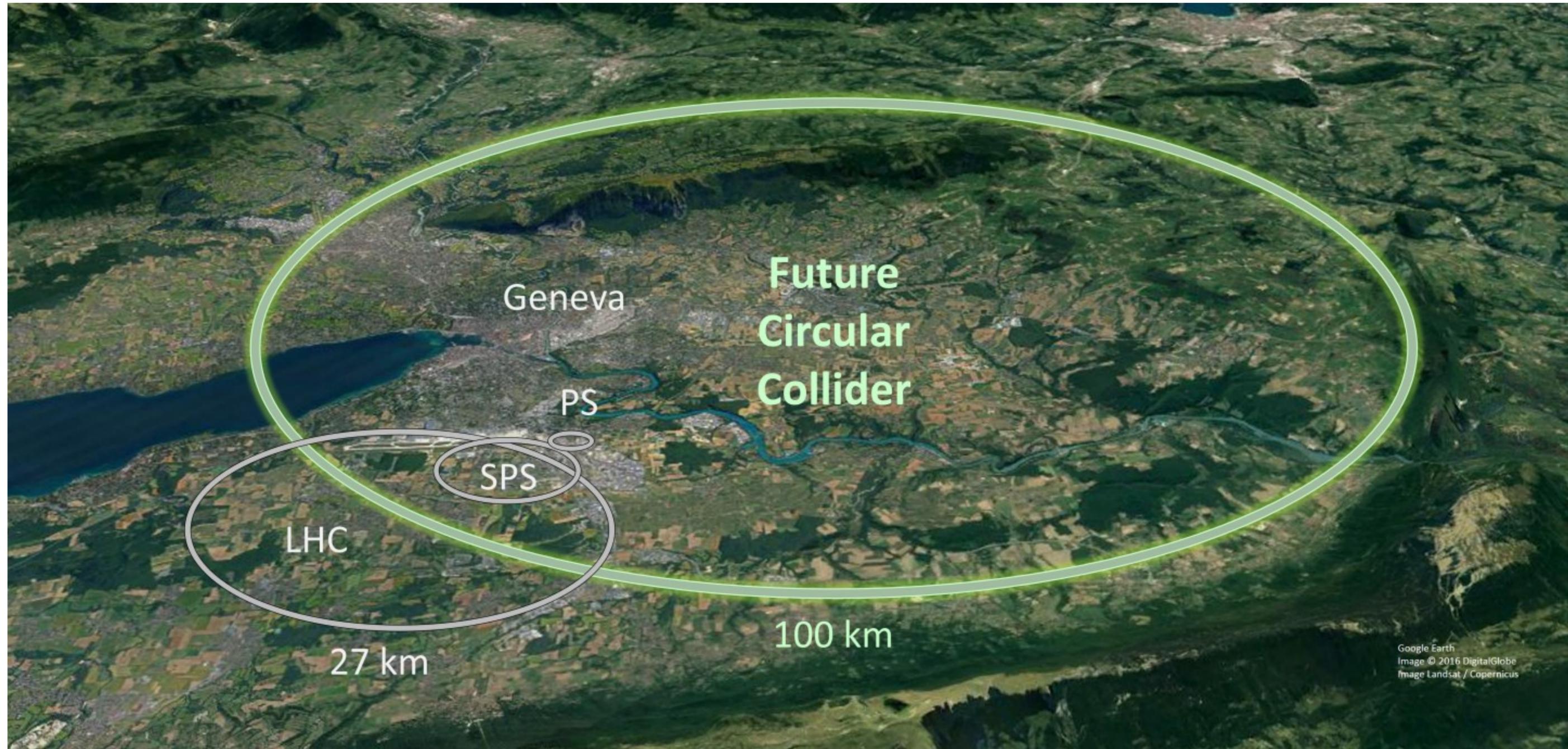
HL-HE CERN Yellow Report,  
1902.00134

# Higgs production at HL-LHC: expected precision



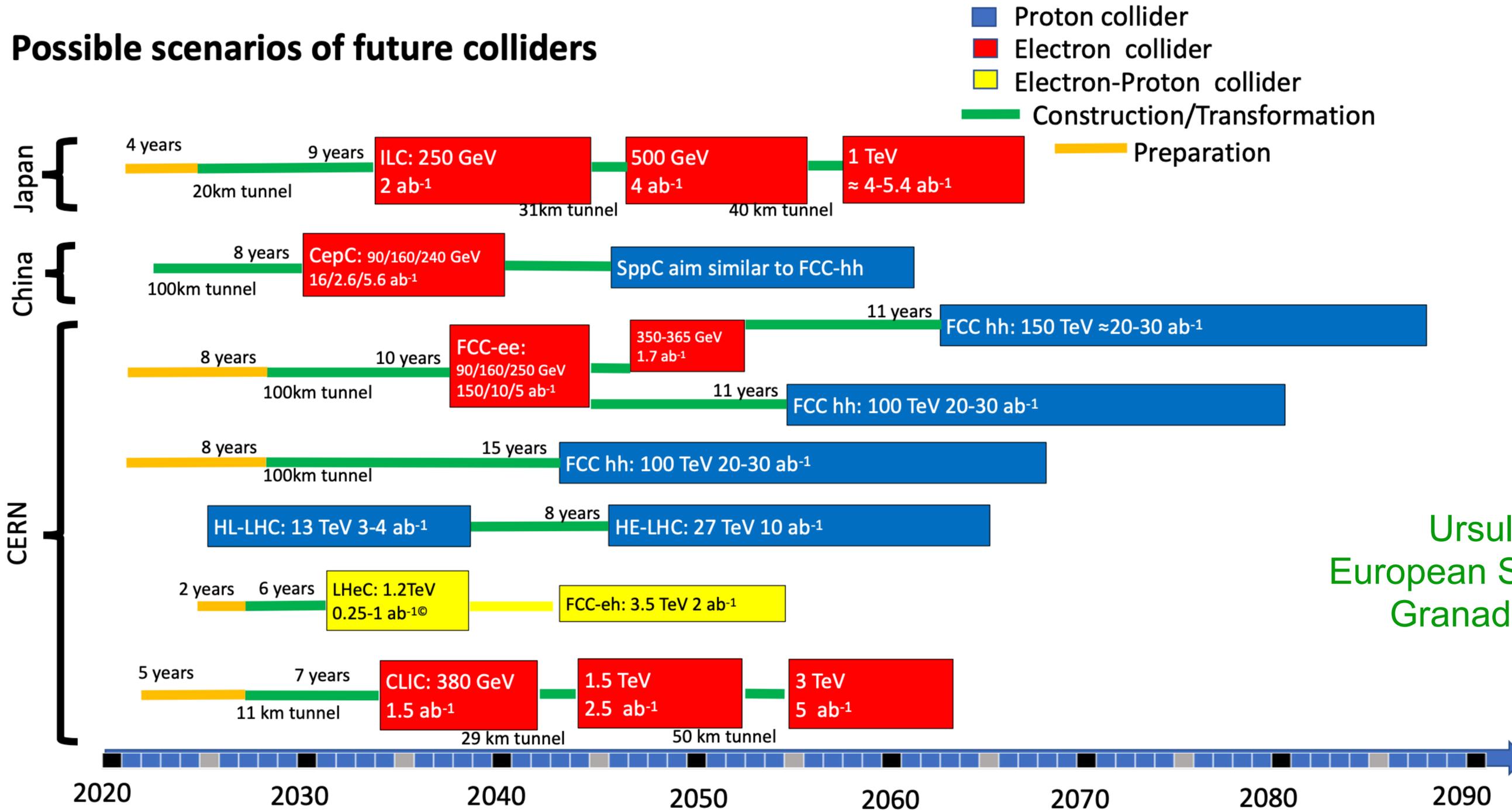
HL-HE CERN Yellow Report,  
1902.00134

# Science (no) fiction?



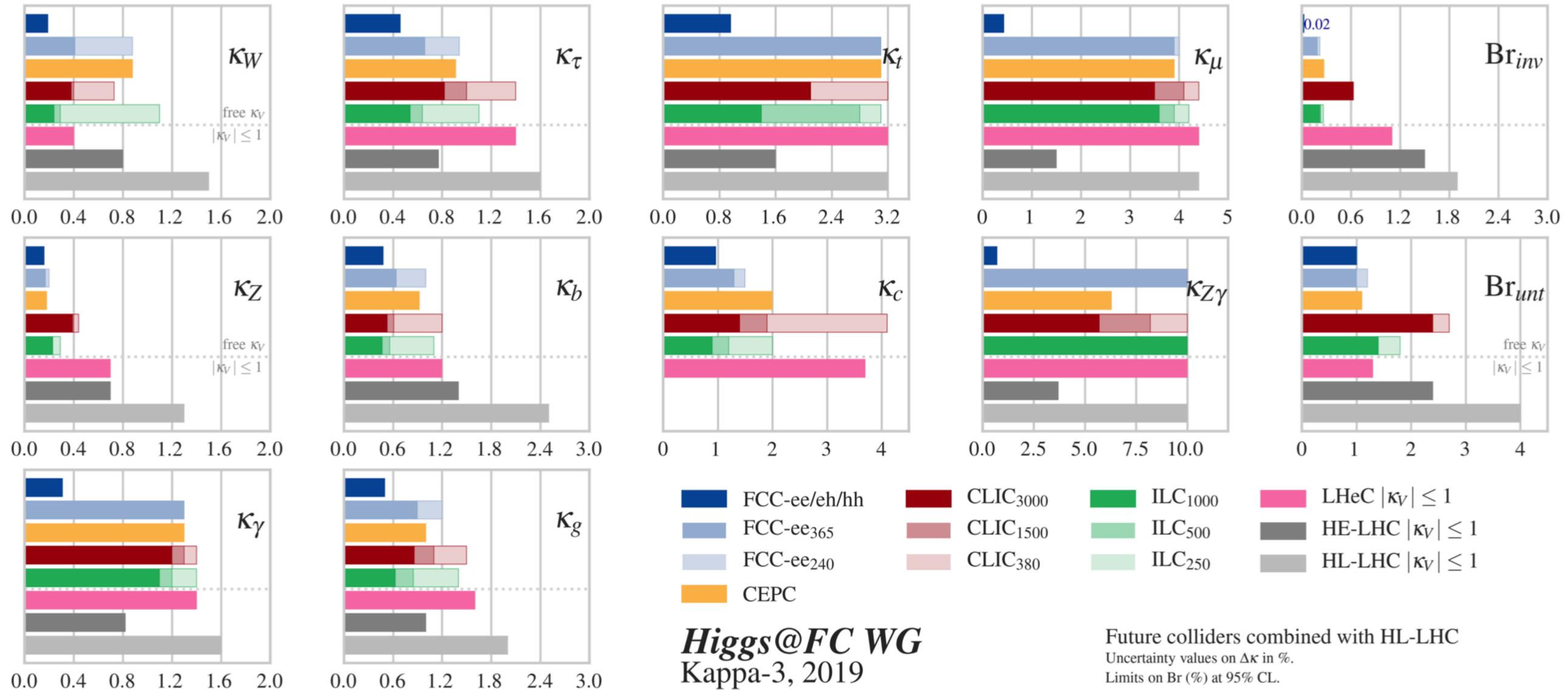
# Future collider plans

## Possible scenarios of future colliders



Ursula Bassler,  
European Strategy Meeting  
Granada, May 2019

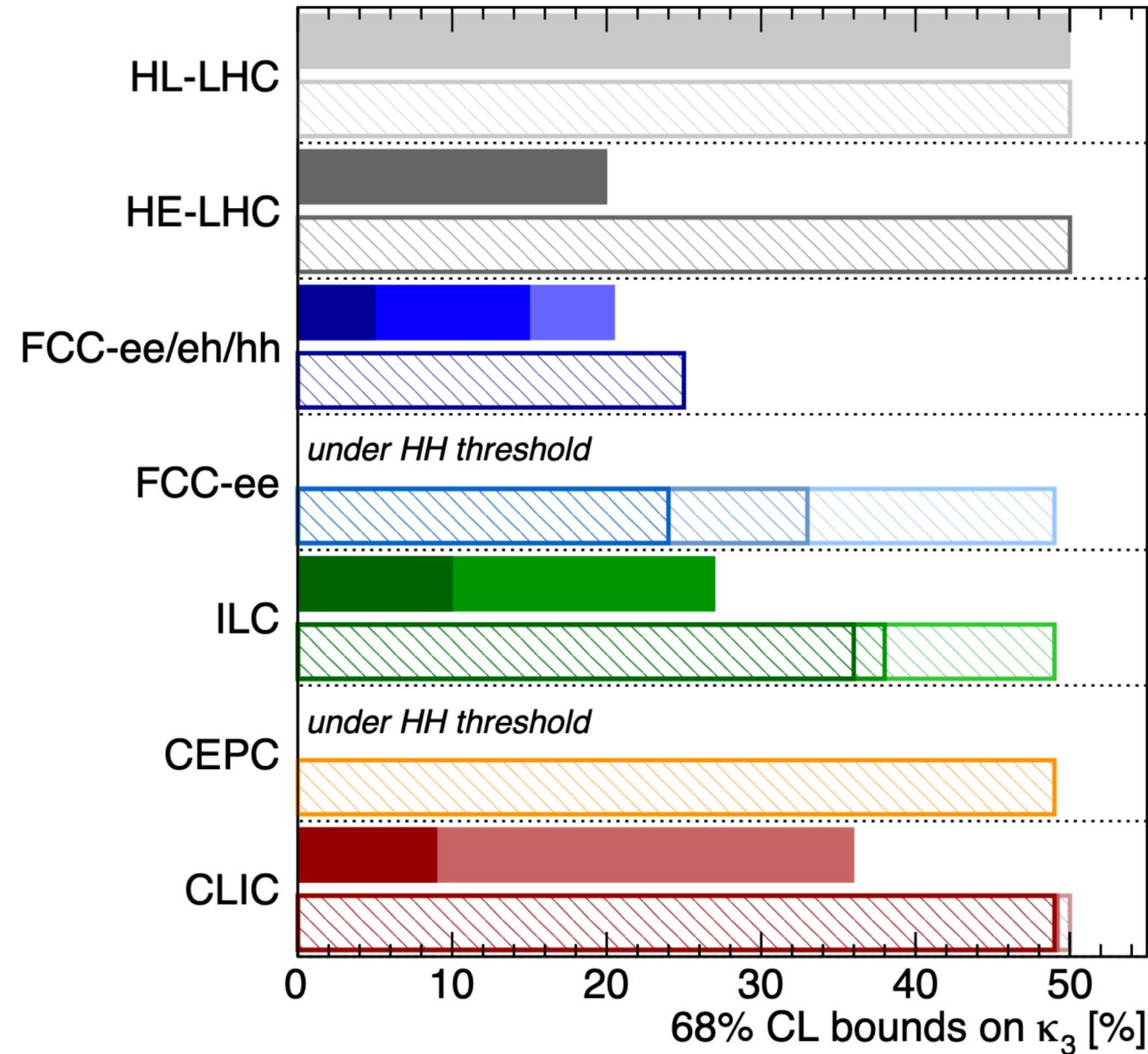
# Higgs couplings at future colliders



European Strategy Physics Briefing Book 1910.11775

# Higgs-boson self coupling

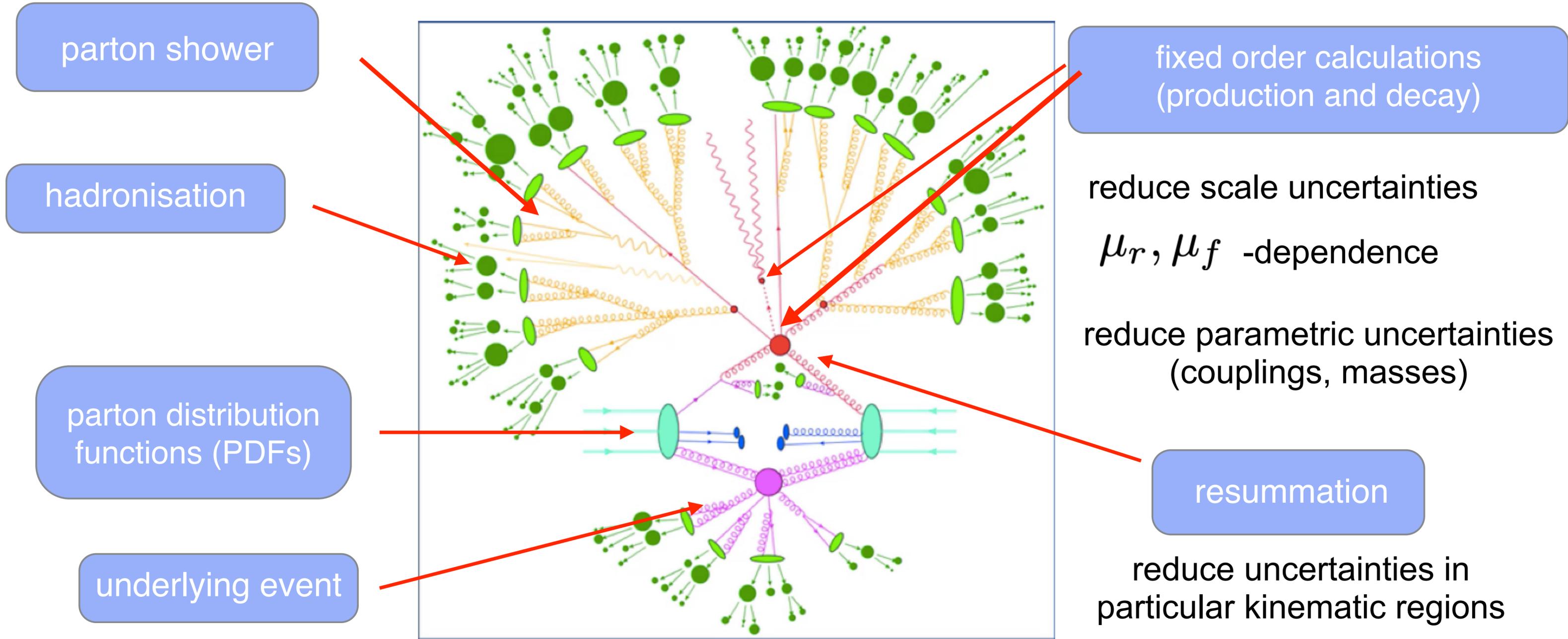
Higgs@FC WG September 2019



di-Higgs	single-Higgs
HL-LHC 50%	HL-LHC 50%
HE-LHC [10-20]%	HE-LHC 50%
FCC-ee/eh/hh 5%	FCC-ee/eh/hh 25%
LE-FCC 15%	LE-FCC n.a.
FCC-eh <sub>3500</sub> -17+24%	FCC-eh <sub>3500</sub> n.a.
	FCC-ee <sup>4IP</sup> <sub>365</sub> 24%
	FCC-ee <sub>365</sub> 33%
	FCC-ee <sub>240</sub> 49%
ILC <sub>1000</sub> 10%	ILC <sub>1000</sub> 36%
ILC <sub>500</sub> 27%	ILC <sub>500</sub> 38%
	ILC <sub>250</sub> 49%
	CEPC 49%
CLIC <sub>3000</sub> -7%+11%	CLIC <sub>3000</sub> 49%
CLIC <sub>1500</sub> 36%	CLIC <sub>1500</sub> 49%
	CLIC <sub>380</sub> 50%

All future colliders combined with HL-LHC

# How to increase the precision of the predictions?



artwork by G.Luisoni

# Perturbation theory

$$\begin{array}{cccc}
 & \text{leading order} & \text{next-to-leading order} & \text{next-to-next-to-leading order} \\
 & \downarrow & \downarrow & \downarrow \\
 \sigma = \alpha_s^k \left( \sigma^{LO} + \alpha_s \sigma^{NLO} + \alpha_s^2 \sigma^{NNLO} + \dots \right) \\
 \alpha_s(M_Z) \simeq 0.118 & \mathcal{O}(10\%) & \mathcal{O}(1\%) & 
 \end{array}$$

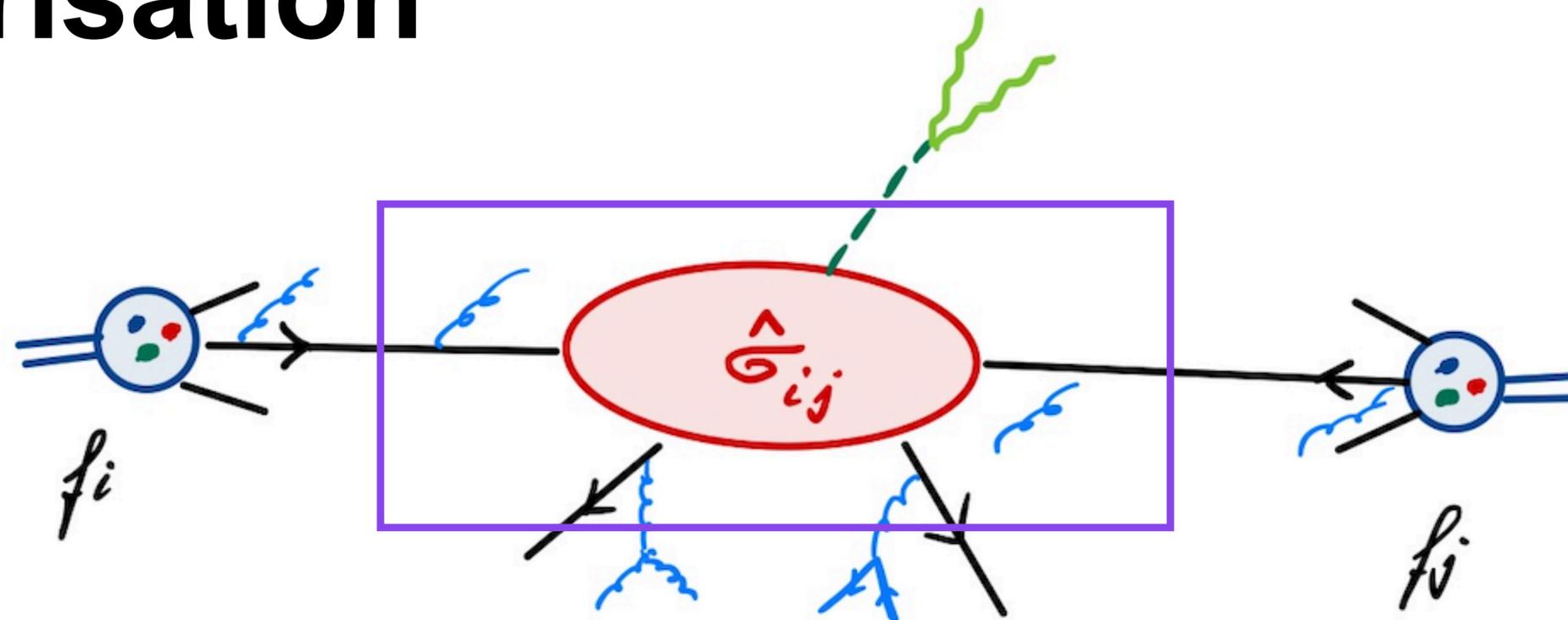
electroweak corrections:  $\alpha/\alpha_s \approx 0.1 \Rightarrow$  smaller, but beware of large terms like  $\log\left(\frac{M_Z^2}{\hat{s}}\right)$

**scale dependence:** due to truncation of perturbative series  $\longrightarrow$  measure of missing higher orders

$$\sigma = \alpha_s^k(\mu_r) \left( \sigma^{LO}(\mu_f) + \alpha_s(\mu_r) \sigma^{NLO}(\mu_r, \mu_f) + \alpha_s^2(\mu_r) \sigma^{NNLO}(\mu_r, \mu_f) + \dots \right)$$

$\uparrow$  renormalisation scale       $\uparrow$  factorisation scale

# Factorisation



$$d\sigma_{pp \rightarrow H+X} = \sum_{i,j} \int_0^1 dx_1 f_{i/p_a}(x_1, \alpha_s, \mu_f) \int_0^1 dx_2 f_{j/p_b}(x_2, \alpha_s, \mu_f) d\hat{\sigma}_{ij \rightarrow H+X}(x_1, x_2, \alpha_s, \mu_r, \mu_f) + \mathcal{O}\left(\frac{\Lambda}{Q}\right)^p$$

parton distribution functions (PDFs)
partonic cross section

non-perturbative

perturbative

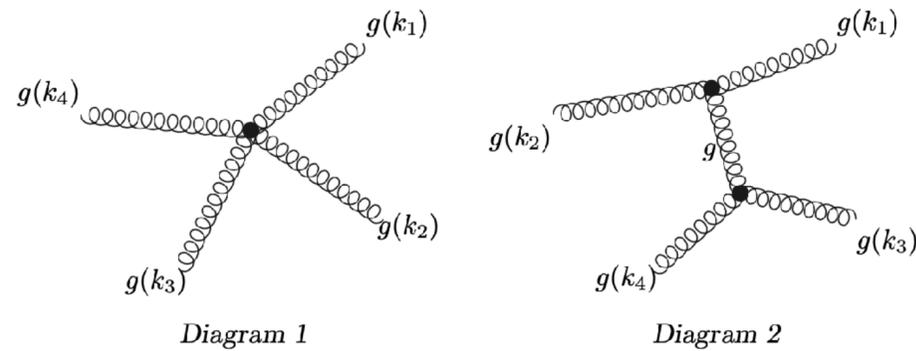
renormalisation scale

factorisation scale

# Higher orders in perturbation theory

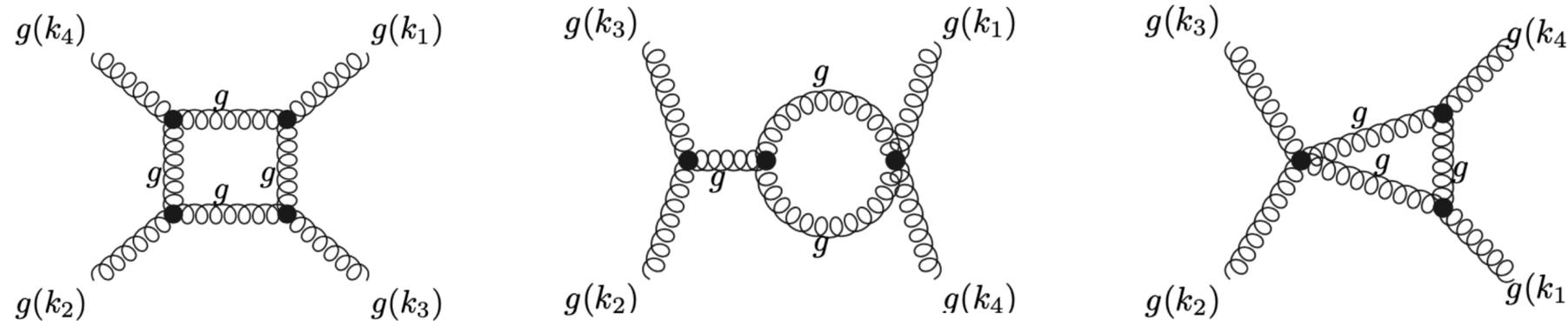
example  $pp$  to 2 jets: subprocess contributing at parton level:  $gg \rightarrow gg$

LO



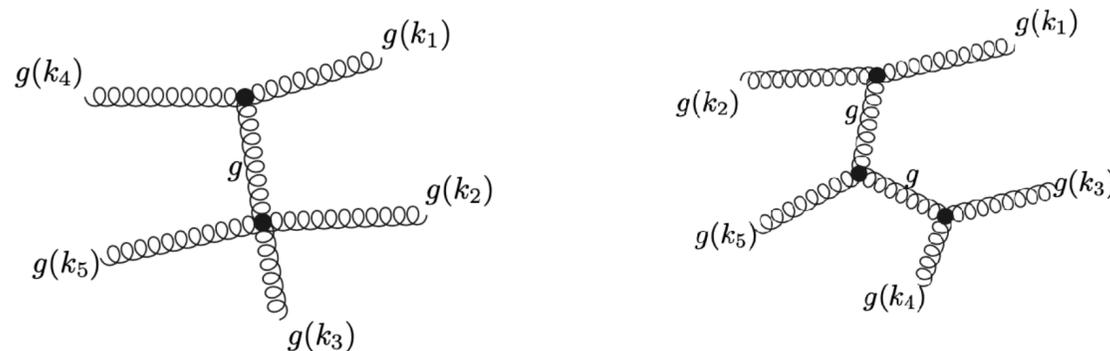
+ permutations (4 diagrams)

NLO virtual



+ ... (60 loop diagrams)

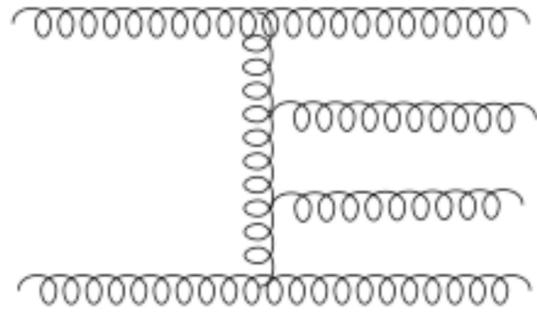
NLO real



+ ... (25 diagrams)

# Higher orders in perturbation theory

example NNLO:

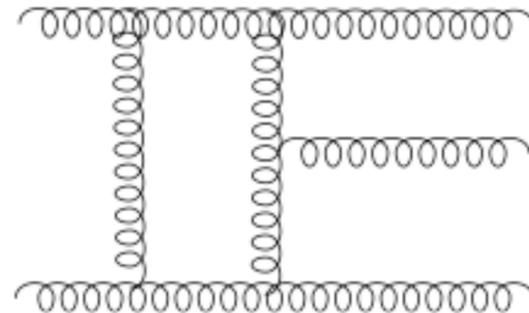


double real



implicit IR poles  
(phase space integration)

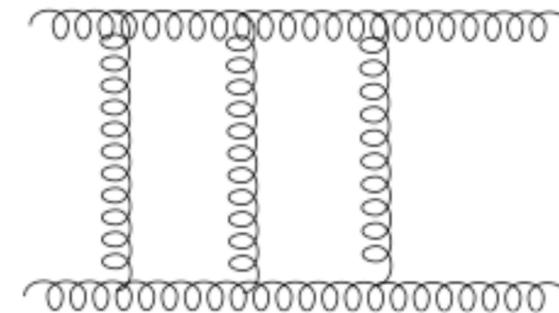
bottlenecks: IR subtraction



1-loop virtual  
⊗ single real



explicit and implicit poles



2-loop virtual

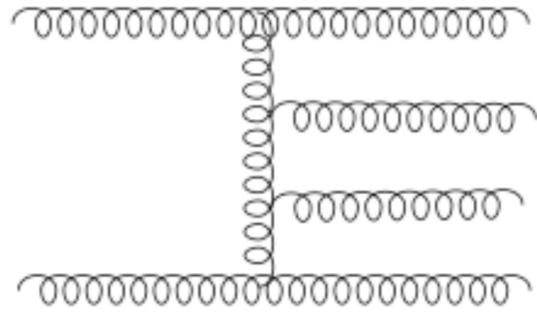


explicit poles  $1/\epsilon^{2L}$  ( $D = 4 - 2\epsilon$ )

(multi)-loop integrals

# Higher orders in perturbation theory

example NNLO:

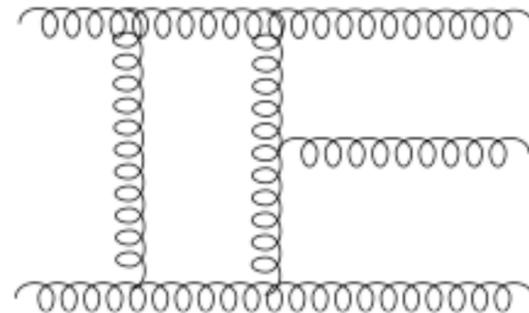


double real



implicit IR poles  
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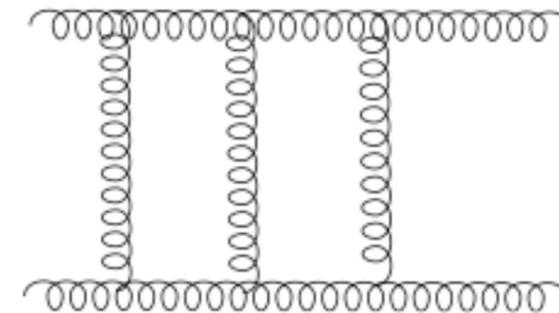
bottlenecks: IR subtraction



1-loop virtual  
⊗ single real



explicit and implicit poles



2-loop virtual



explicit poles  $1/\epsilon^{2L}$  ( $D = 4 - 2\epsilon$ )

(multi)-loop integrals

- current frontiers:**
- NNLO automation
  - N3LO coloured

- 2 loops, 4 legs with several mass scales
- 2 loops, 5 legs
- more than 2 loops

# Highlights

## Higgs Threshold Exp.

[Anastasiou, Duhr, Dulat, Herzog, BM, 15]

Higgs Jet Veto [Banfi, et al. 15]

Higgs VBF [Dreyer, Karlberg,16]

Higgs Diff. Threshold App. [Dulat, BM, A. Pelloni,17]

Higgs, [BM,18]

Higgs Diff. qT [Cieri,Chen, Gehrmann, Glover,Huss,18]

HH (VBF) [Dreyer, Karlberg,18]

Higgs (Y approx.) [Dulat, BM,Pelloni,18]

bb->H [Dulat, Duhr, BM,19]

ggF->HH [Chen,Li,Shoa,Wang]

Drell-Yan [Dulat, Duhr, BM,20]

bbH 4FS+5FS [Dulat, Duhr, Hirschi, BM,20]

CCDY [Dulat, Duhr, BM,20]

Fully differential Higgs -> 2Photons [Chen, BM, et al. 21]

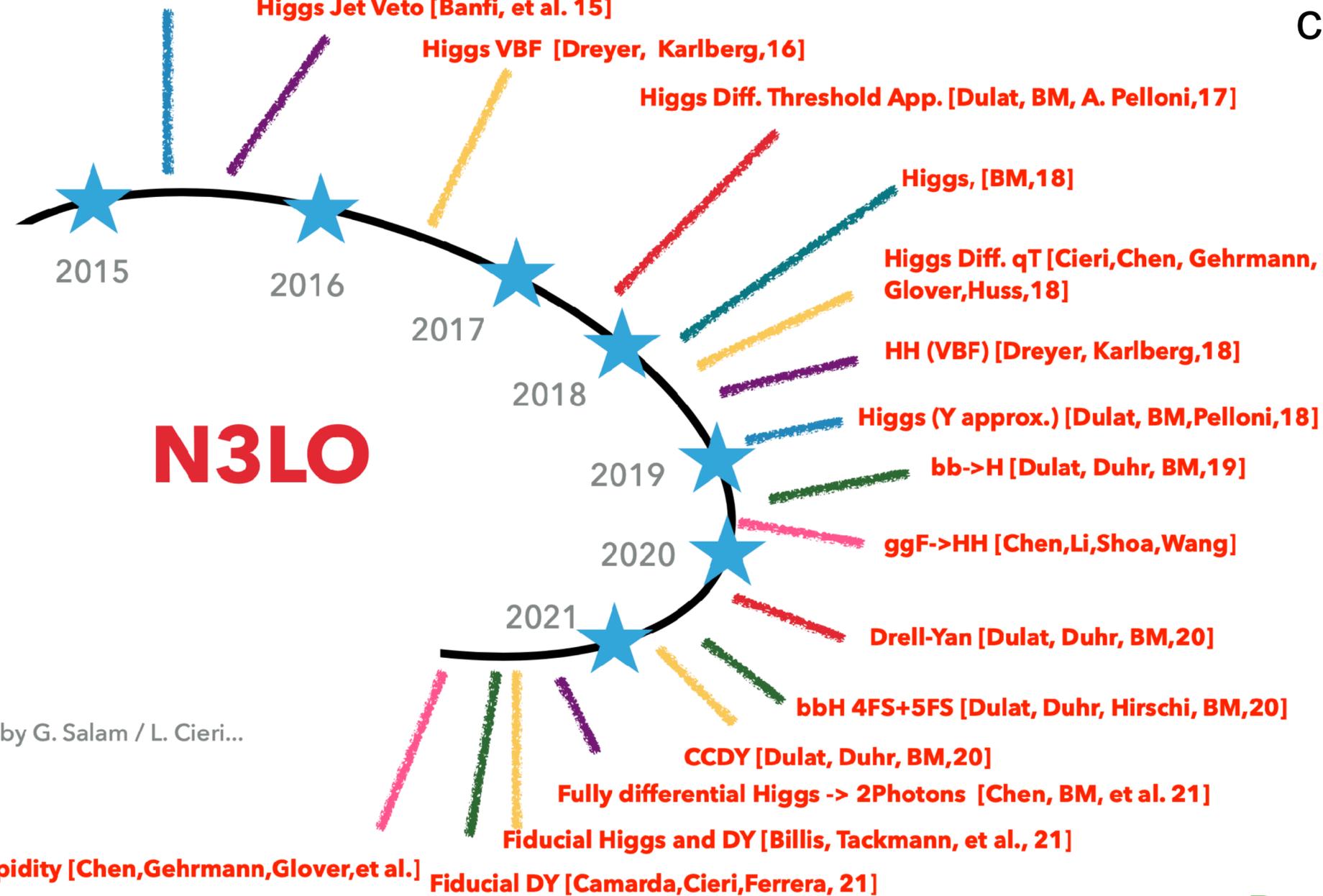
Fiducial Higgs and DY [Billis, Tackmann, et al., 21]

DY-Rapidity [Chen,Gehrmann,Glover,et al.]

Fiducial DY [Camarda,Cieri,Ferrera, 21]

colour singlet final state particles  
(H, Z, W)

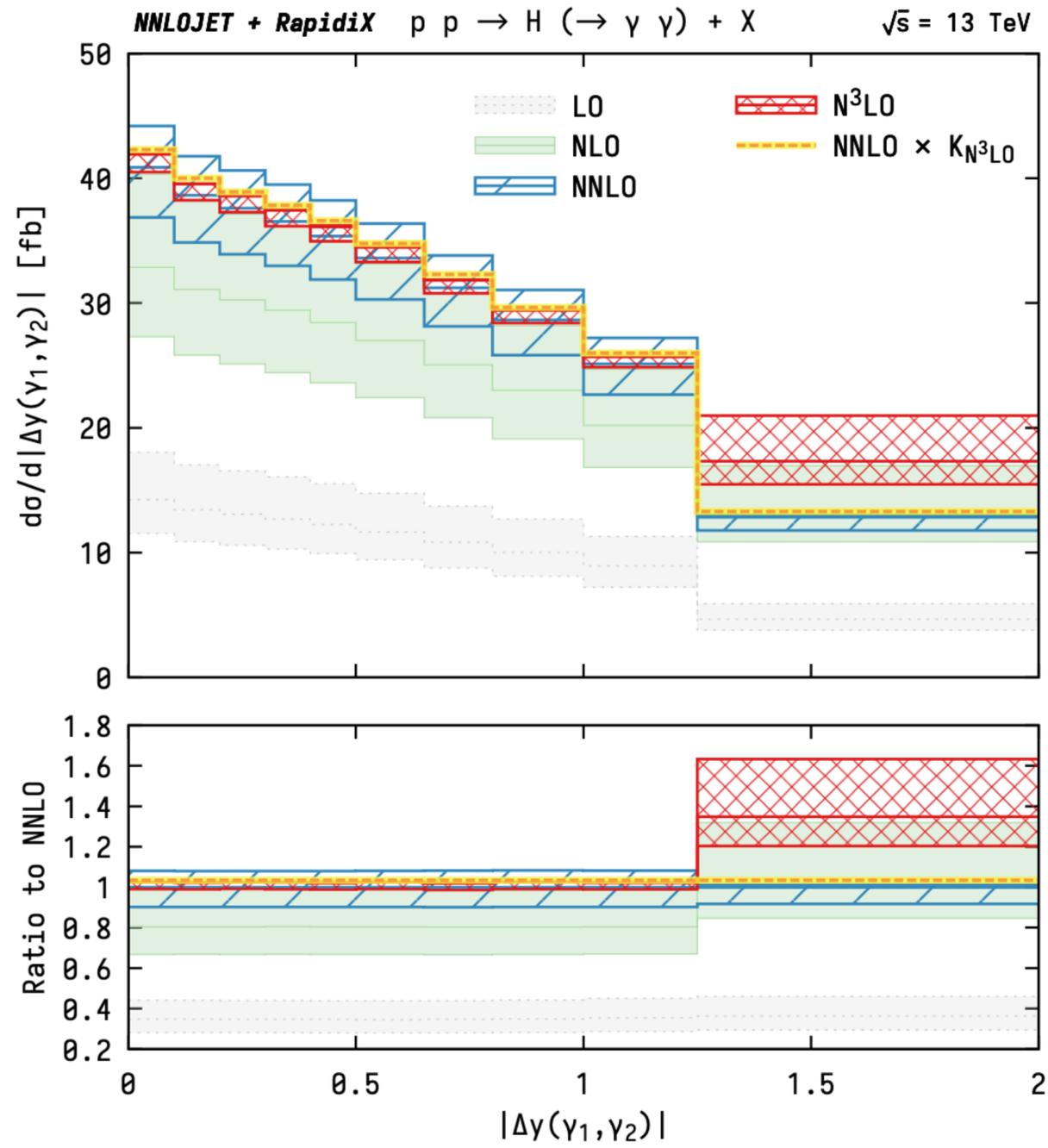
going more and more differential



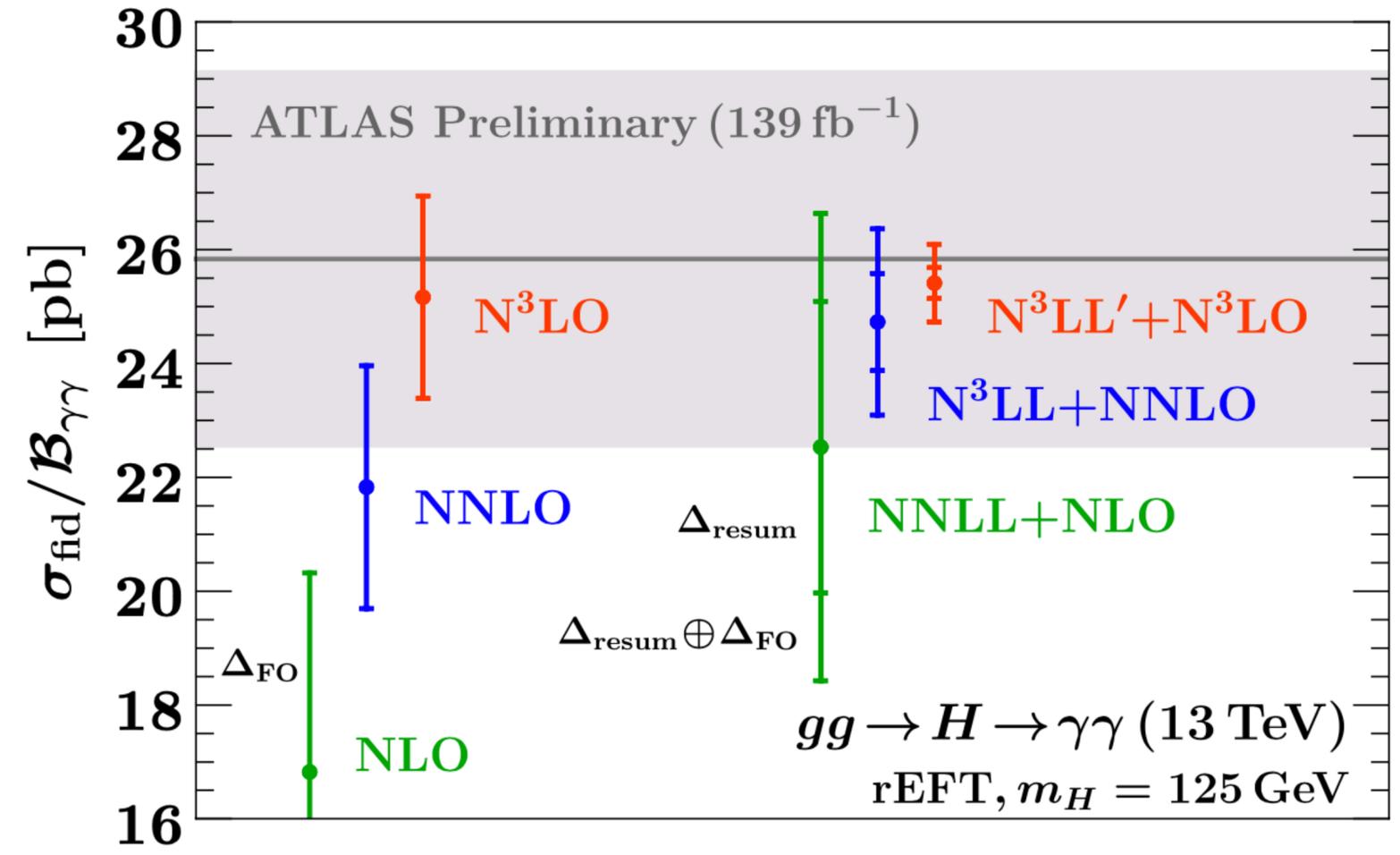
Slide inspired by G. Salam / L. Cieri...

Bernhard Mistlberger, Amplitudes 2021

# ggH@N3LO fiducial

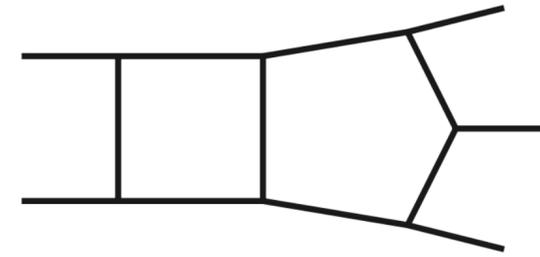


Chen, Gehrmann, Glover, Huss, Mistlberger, Pelloni, 2102.07607



Billis, Dehnadi, Ebert, Michel, Tackmann, 2102.08039

# Loop integrals: status 2-loop 5-point



massless:

$$pp \rightarrow \gamma\gamma\gamma$$

*Abreu, Page, Pascual, Sotnikov '20 (leading color amplitudes)*

*Chawdry, Czakon, Mitov, Poncelet '20 (leading color, full xs)*

*Kallweit, Sotnikov, Wiesemann '20 (leading color, full xs)*

$$pp \rightarrow \gamma\gamma j$$

*Chawdry, Czakon, Mitov, Poncelet '21 (leading color, full xs)*

*Agarwal, Buccioni, Manteuffel, Tancredi '21 (full color, amplitudes)*

$$gg \rightarrow \gamma\gamma g$$

*Badger, Brønnum-Hansen, Chicherin, Gehrmann, Hartanto '21 (amp)*

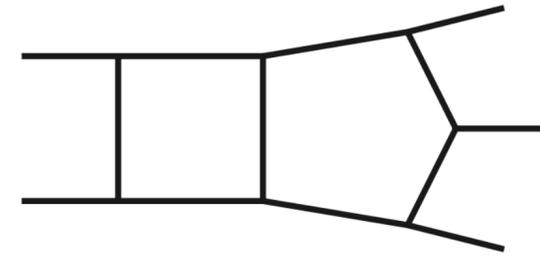
*Badger, Gehrmann, Marcoli, Moodie **today** (full xs)*

$$pp \rightarrow jjj$$

*Abreu, Febres Cordero, Ita, Page, Sotnikov '21 (leading color amp)*

*Czakon, Mitov, Poncelet '21 (full xs)*

# Loop integrals: status 2-loop 5-point



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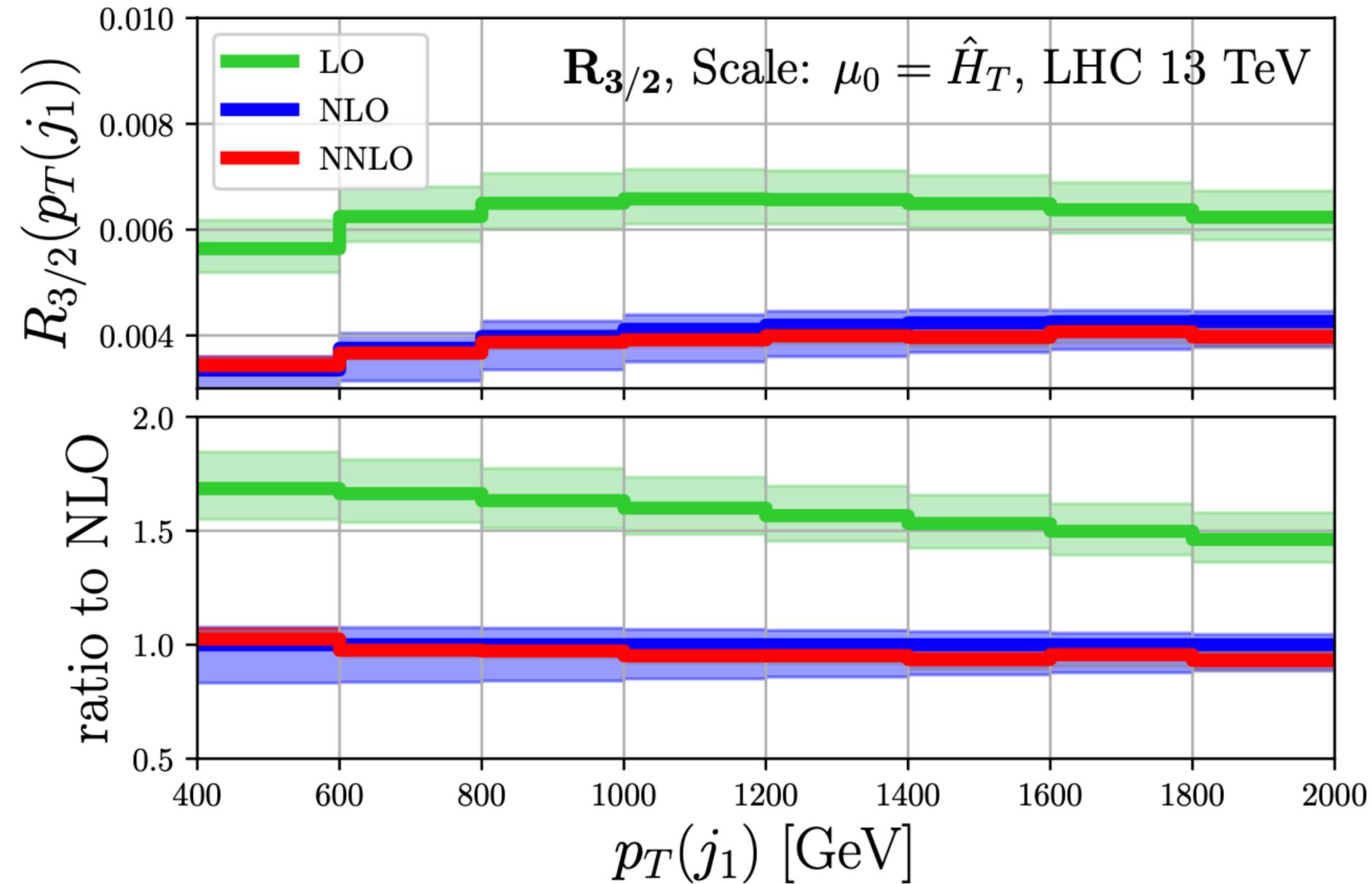
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*Abreu, Febres Cordero, Ita, Page, Sotnikov '21 (leading color amp)*

*Czakon, Mitov, Poncelet '21 (full xs)*

**important tool: pentagon functions in C++** *Chicherin, Sotnikov '21*

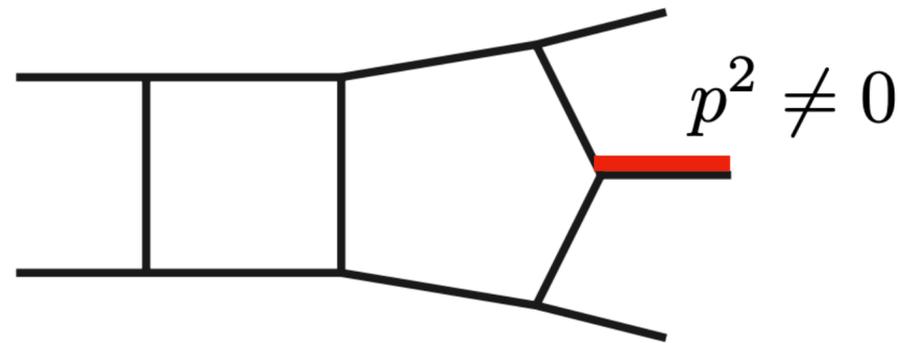
# 3-jet production at NNLO



3-jet/2-jet ratio

*Czakon, Mitov, Poncelet '21*

# 2-loop 5-point (one off-shell leg)



*Abreu, Ita, Moriello, Page, Tschernow '20 (planar)*

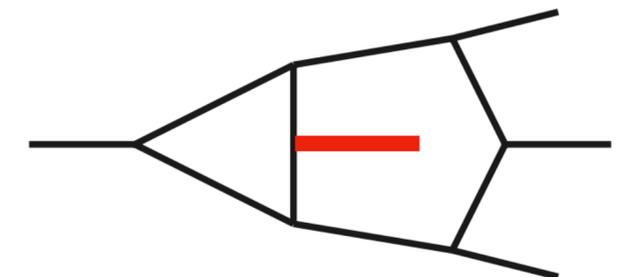
*Canko, Papadopoulos, Syrrakos '21 (planar, analytic)*

$W + 4$  partons *Badger, Brønnum-Hansen, Hartanto, Peraro '19 (planar, num. unitarity)*

$u\bar{d} \rightarrow W^+ b\bar{b}$  *Badger, Hartanto, Zoia '21 (planar, analytic)*

$pp \rightarrow b\bar{b}H$  *Badger, Hartanto, Kryz, Zoia '21 (leading colour)*

**non-planar:** *Abreu, Ita, Page, Tschernnov '21*  
*Liu, Ma '21*



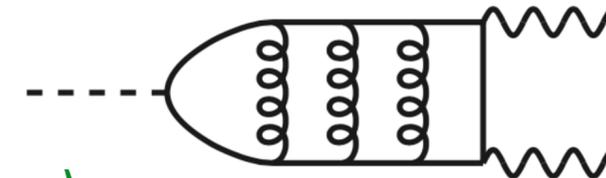
## 3-loop 4-point



$$pp \rightarrow \gamma\gamma \quad \text{Caola, Manteuffel, Tancredi '20}$$

$$q\bar{q} \rightarrow q\bar{q} \quad \text{Caola, Chakraborti, Gambuti, Manteuffel, Tancredi '21}$$

## 4-loop 3-point



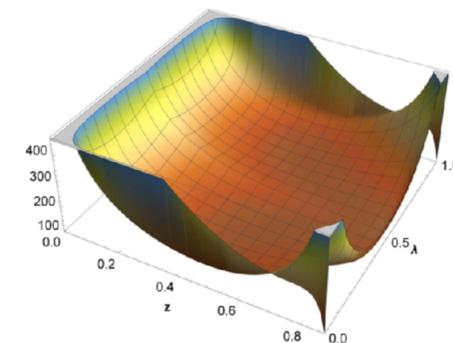
$$H \rightarrow \gamma\gamma \quad \text{Davies, Herren '21 (large } mt\text{-expansion)}$$

$$\text{form factors } \gamma^* \rightarrow q\bar{q} \quad \text{Agarwal, Manteuffel, Panzer, Schabinger '21, ...}$$

## 3-loop 3-point with **massive** propagators

$$gg \rightarrow H \quad \text{Czakon, Harlander, Klappert, Niggetiedt '21 (full cross section)}$$

semi-numerically



# 2-loop 4-point with massive propagators

**analytically:**  $H + j$  full set of master integrals *Frellesvig et al. '19*

mixed QCD-EW corrections to Higgs production *Bechetti et al. '20*

mixed QCD-EW corrections to Drell-Yan *Heller, von Manteuffel et al. '20*  
*Bonciani et al. '21*

2-loop 4-fermion scattering in QED *Bonciani et al. '21*

*Banerjee et al. '20, '21*

•  
•  
•

# 2-loop 4-point with massive propagators

numerically:

$$pp \rightarrow t\bar{t}$$

*Czakon, Mitov '13*

$$pp \rightarrow HH$$

*Borowka, Greiner, GH, Jones, Kerner, Schlenk, Schubert, Zirke '16*

*Baglio, Campanario, Glaus, Mühlleitner, Spira '18*

$$pp \rightarrow Hj$$

*Jones, Kerner, Luisoni '18*

$$pp \rightarrow W^+W^-$$

*Brønnum-Hansen, Wang '20*

$$pp \rightarrow HZ$$

*Chen, GH, Jones, Kerner, Klappert, Schlenk '20*

$$pp \rightarrow ZZ$$

*Agarwal, Jones, Manteuffel '20*

# Pro's and con's analytic/numerical

	analytic	numerical
pole cancellation	exact	with numerical uncertainty
fast evaluation	mostly	depends
control of integrable singularities	analytic continuation	less straightforward
extension to more scales/loops	difficult	promising
automation	difficult	less difficult

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often a combination can be beneficial,  
e.g. high energy limit analytically  
Davies et al. '19

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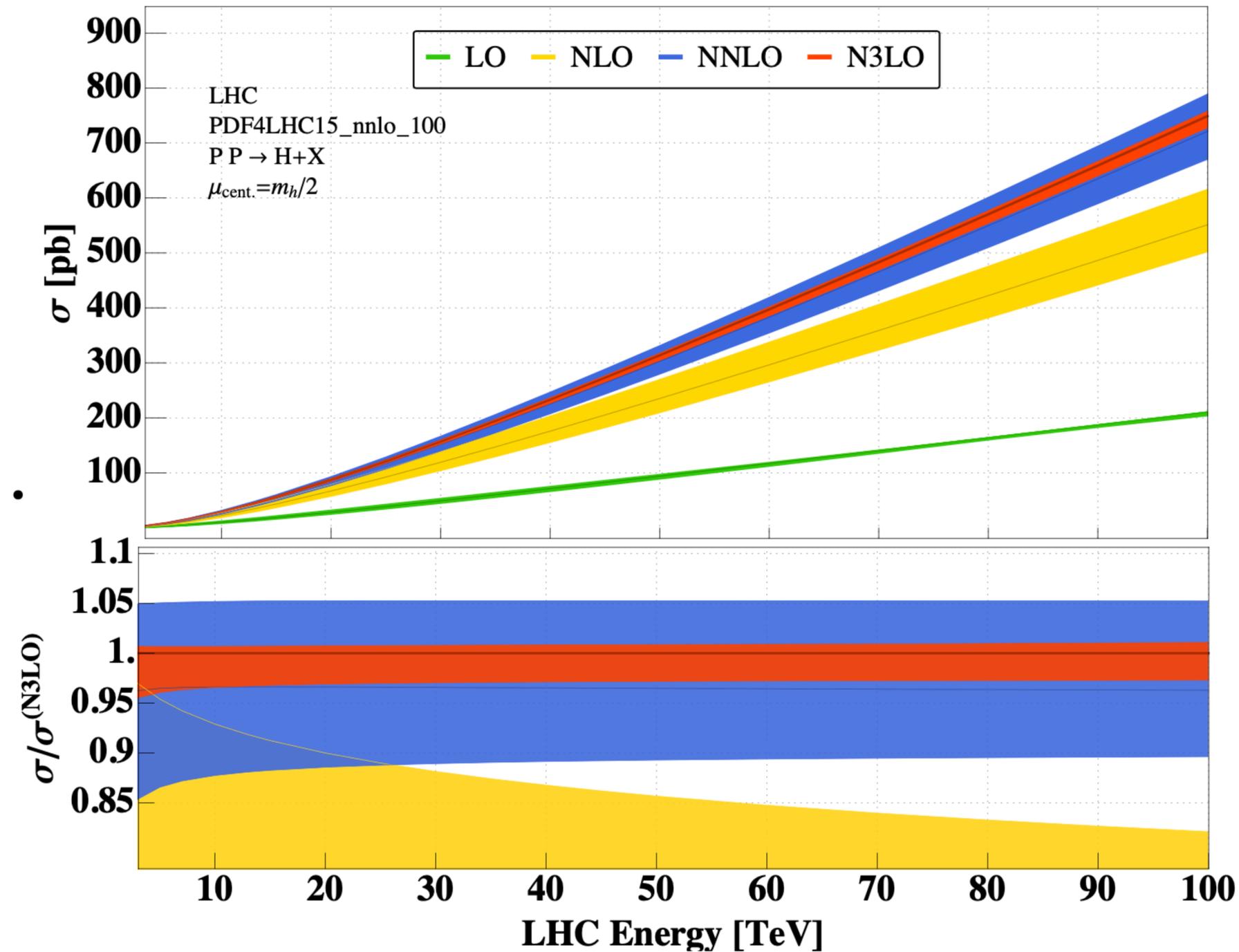
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# The Next Challenges

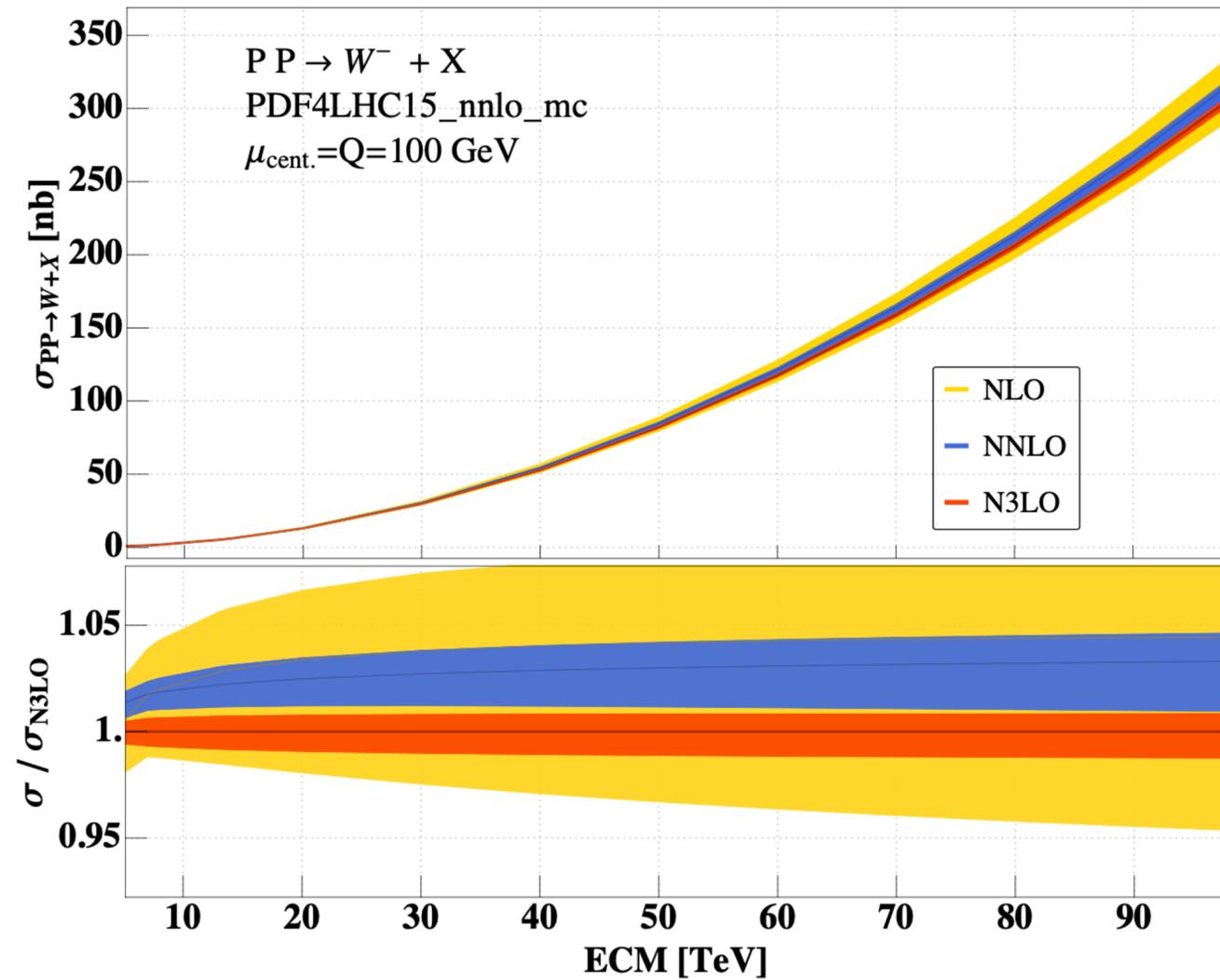
- scale uncertainties: how well do they estimate missing higher orders?
  - depends on choice of central scales, modes of variation, contributing partonic channels, ...
- electroweak corrections, mixed QCD-EW
- PDFs
- quark mass-related uncertainties: neglected masses, different renormalisation schemes
- parton shower uncertainties
- Effective Field Theories: truncation uncertainties, validity range

# Scale uncertainties: Higgs production in gluon fusion



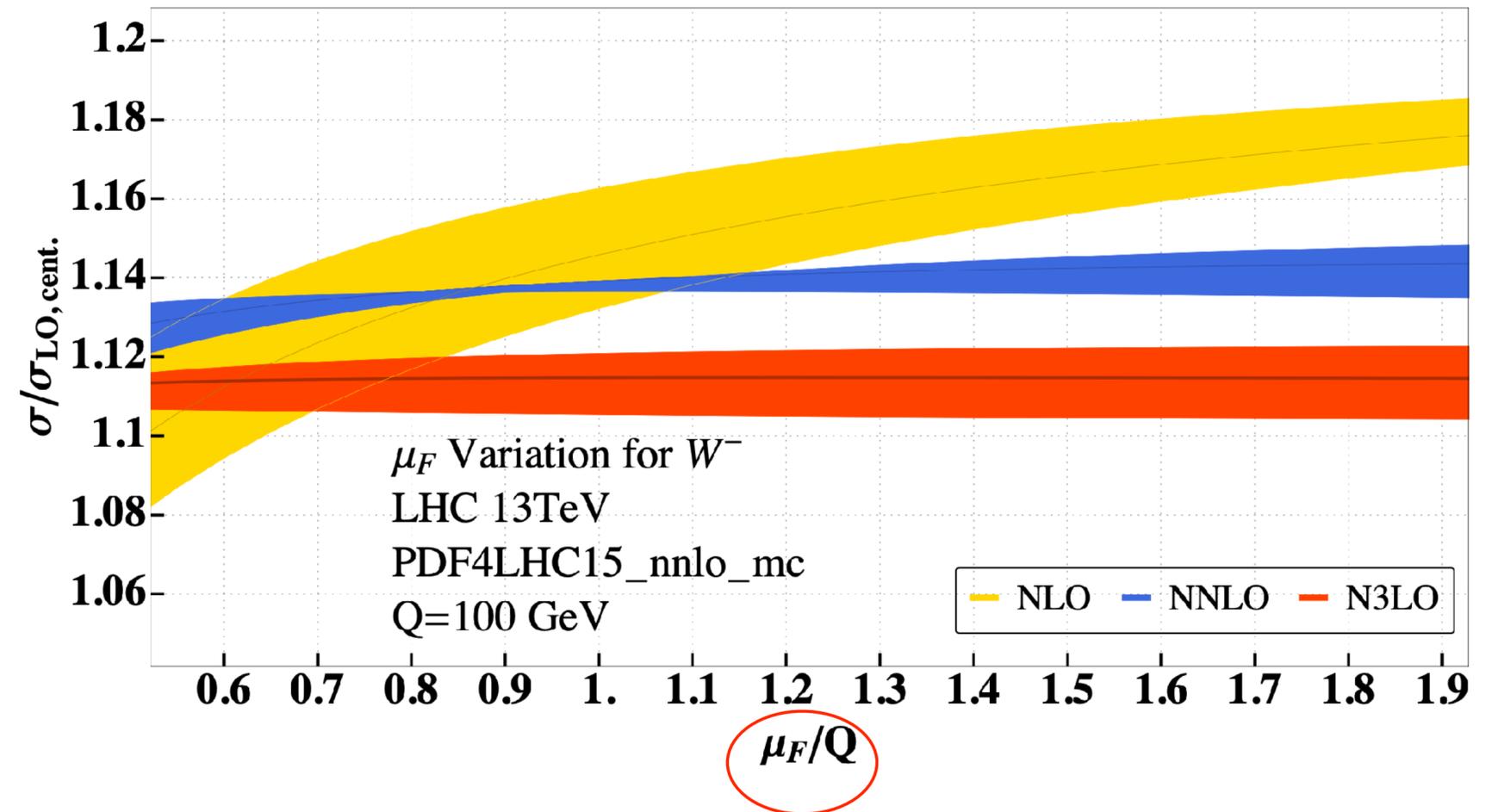
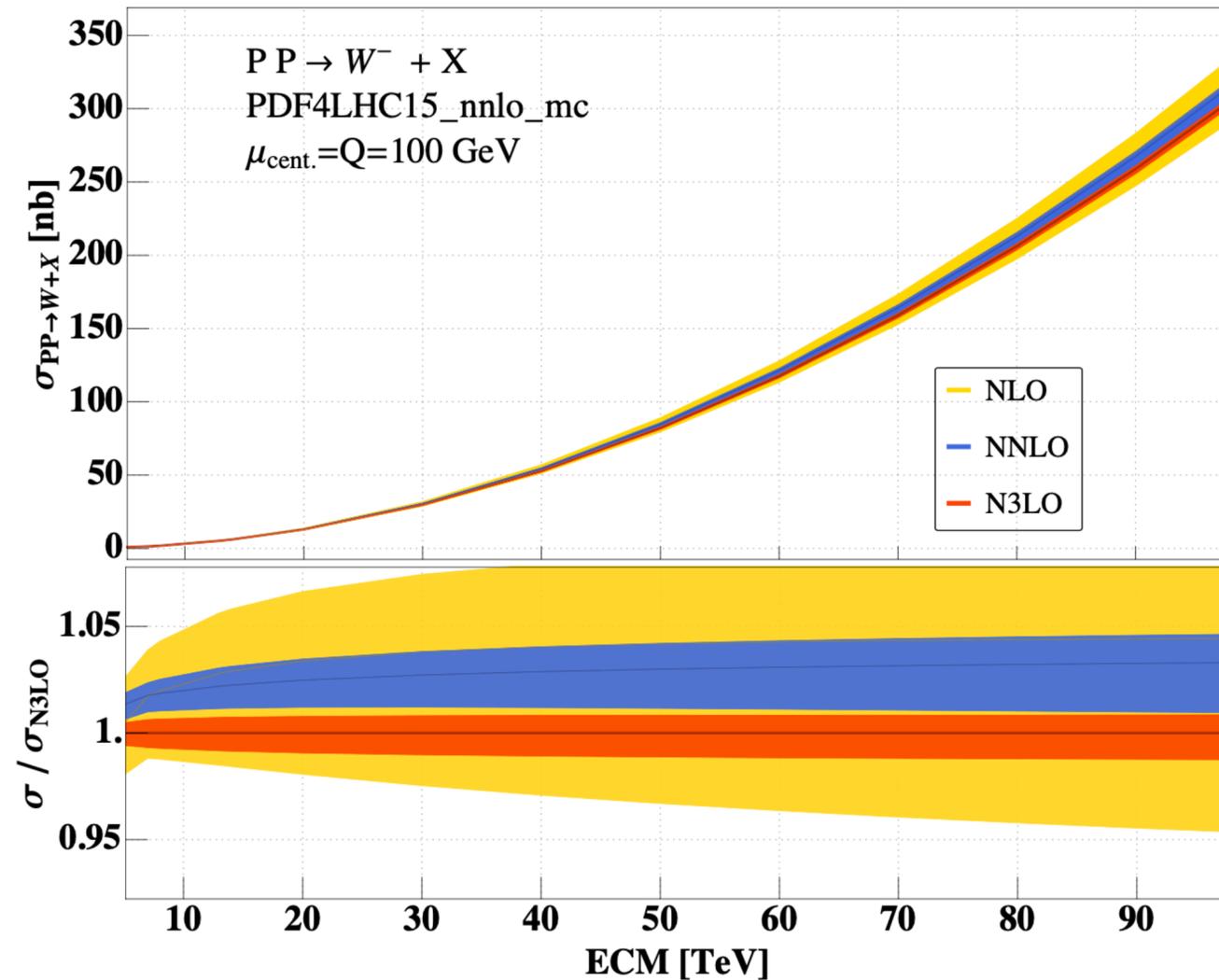
B. Mistlberger '18

# Scale uncertainties: Drell-Yan (W-production)



# Scale uncertainties: Drell-Yan (W-production)

Duhr, Dulat, Mistlberger '20

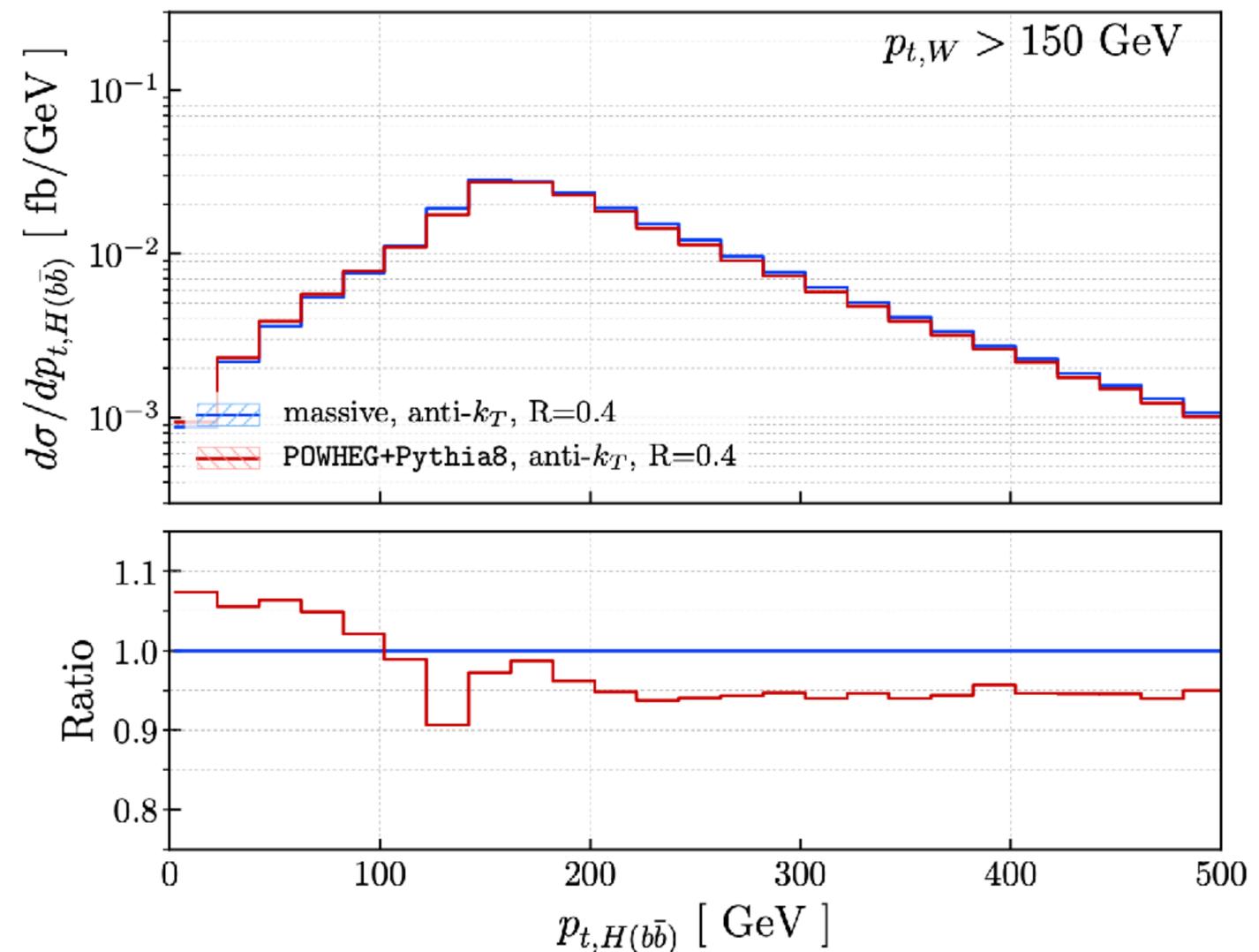
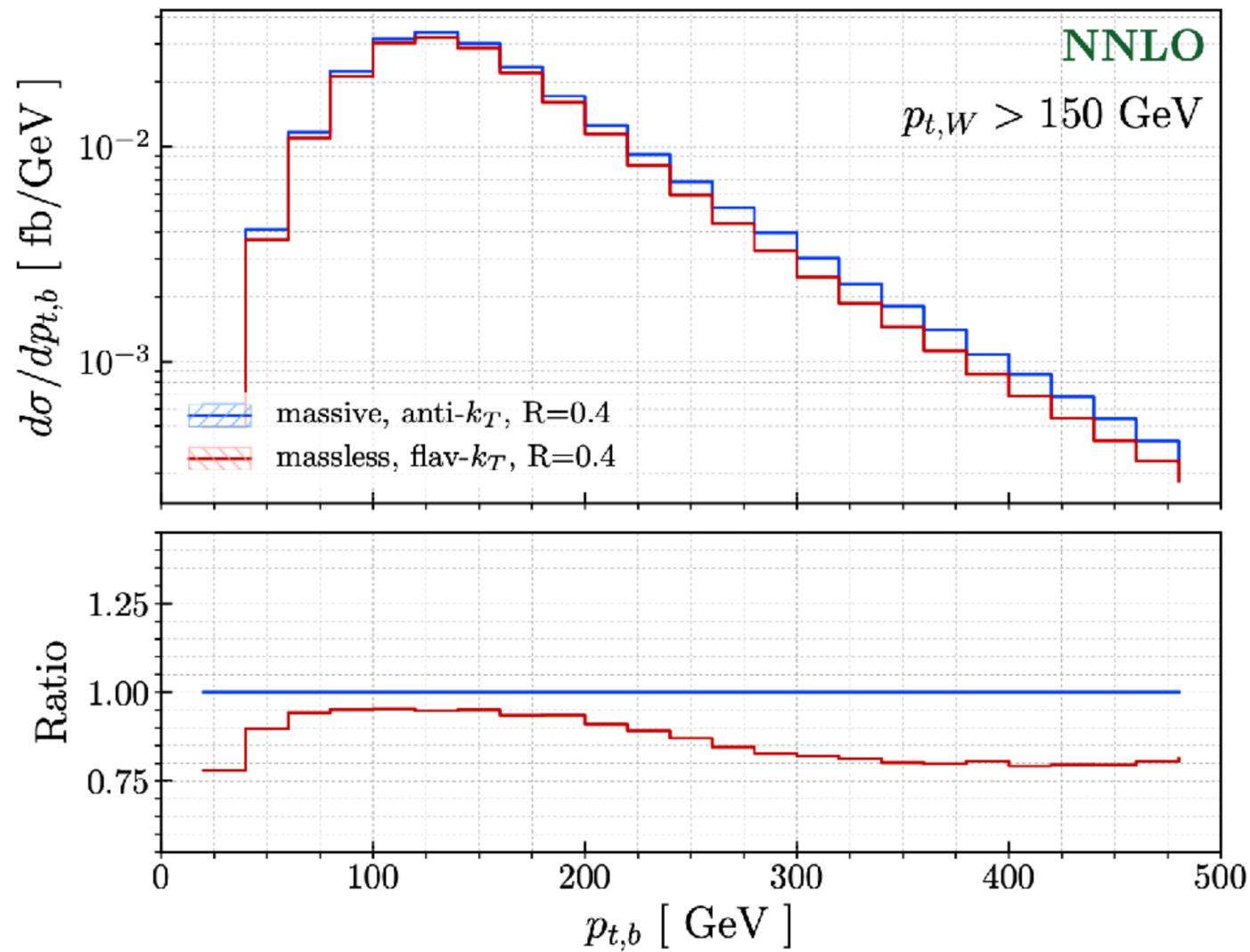


NNLO  $\mu_F$ -scale uncertainty bands do not properly reflect the uncertainty

# Mass effects, parton shower uncertainties

WH production at NNLO + decay  $H \rightarrow b\bar{b}$  with massive b-quarks

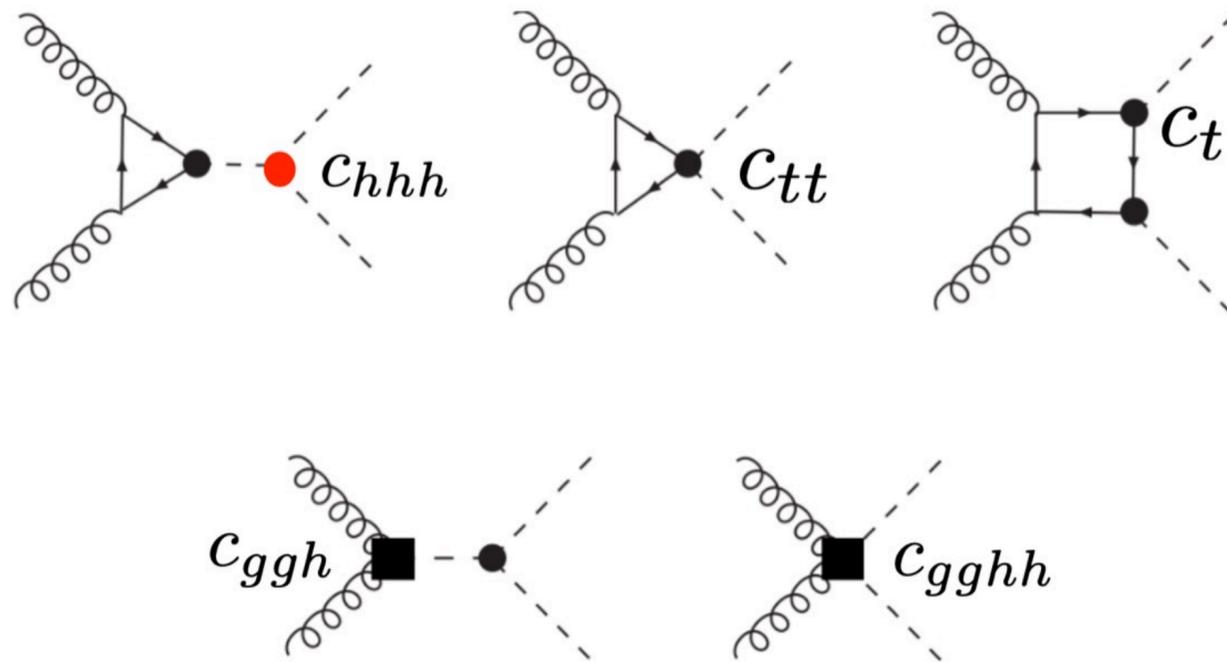
Behring, Bizon, Caola, Melnikov, Röntschi 2003.08321



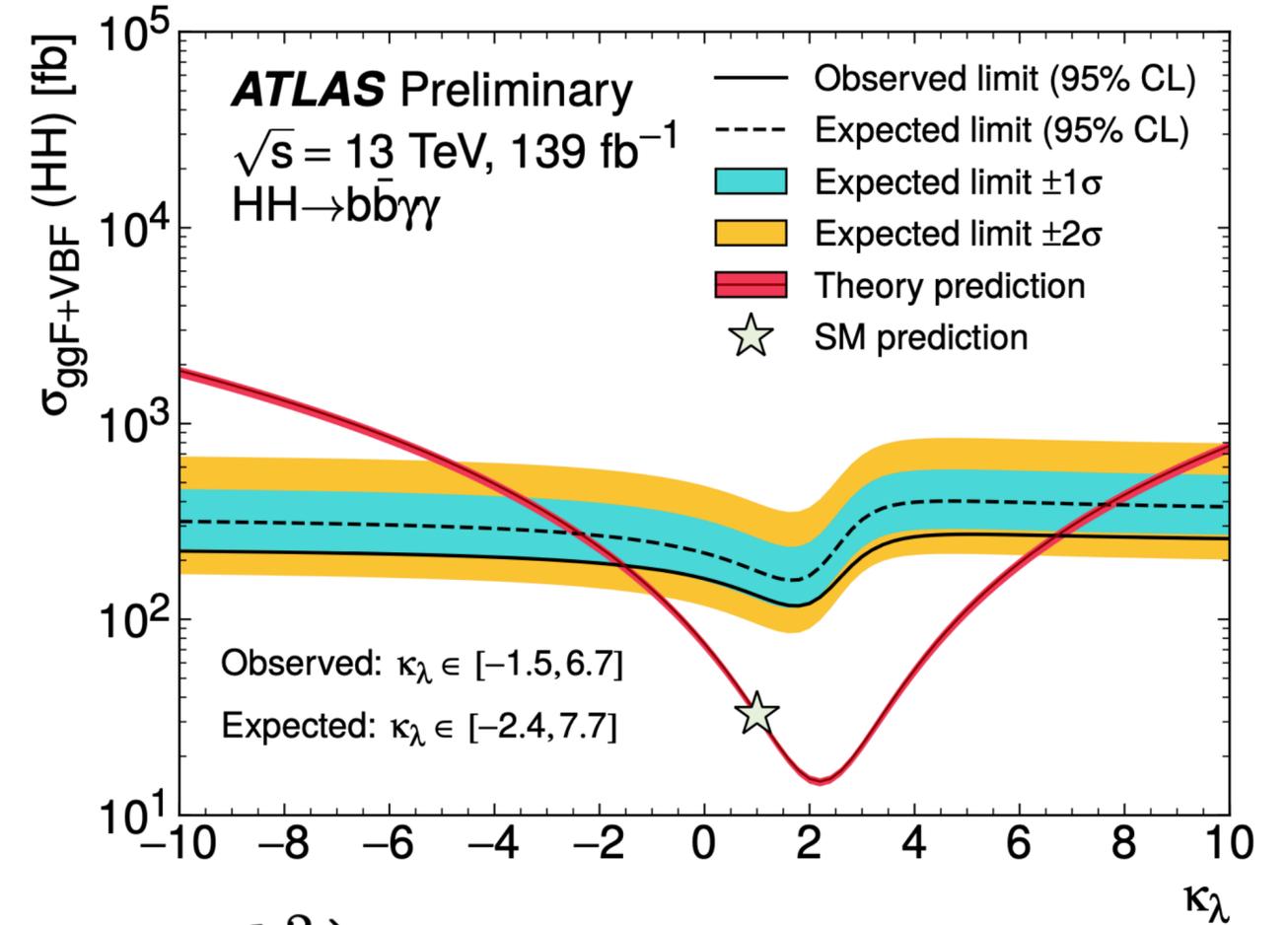
significant differences between massive and massless case and NNLO vs NLO+PS

# Exploring the Higgs potential

through Higgs boson pair production in gluon fusion



ATLAS-CONF-2021-016



$$\mathcal{L} \supset -m_t \left( c_t \frac{h}{v} + c_{tt} \frac{h^2}{v^2} \right) \bar{t}t - c_{hhh} \frac{m_h^2}{2v} h^3 + \frac{\alpha_s}{8\pi} \left( c_{ggh} \frac{h}{v} + c_{gghh} \frac{h^2}{v^2} \right) G_{\mu\nu}^a G^{a,\mu\nu} \quad \kappa_\lambda \equiv c_{hhh}$$

description of unknown interactions at high energies through Effective Field Theory

Standard Model:  $c_{tt} = 0, c_{ggh} = 0, c_{gghh} = 0$

# Higher order corrections: SM

**N3LO:** Chen, Li, Shao, Wang '19  
(HTL with top mass effects)

**NNLO:** De Florian, Mazzitelli '13  
Grigo, Melnikov, Steinhauser '14

**NNLO<sub>F</sub>T<sub>approx</sub>** Grazzini, Kallweit, GH, Jones,  
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inclusion of top quark mass dependence except in virtual  $\mathcal{O}(\alpha_s^3)$

**NLO full  $m_t$**

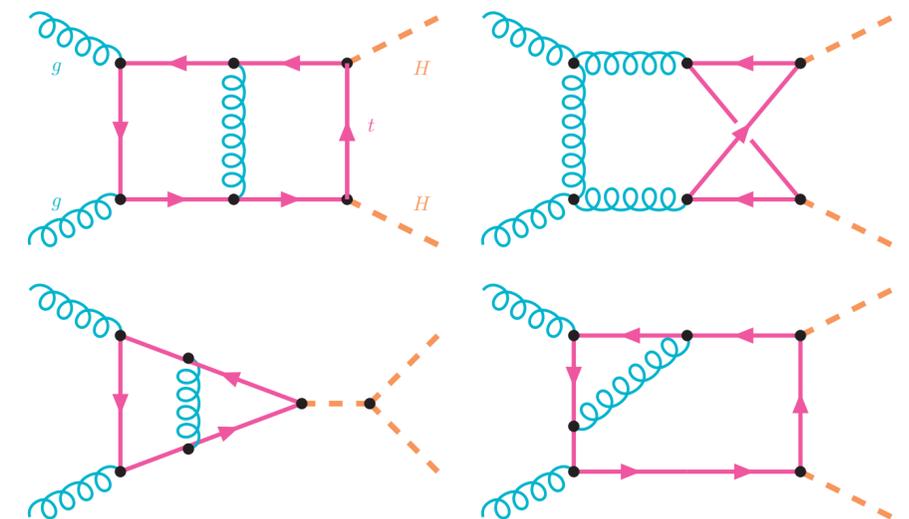
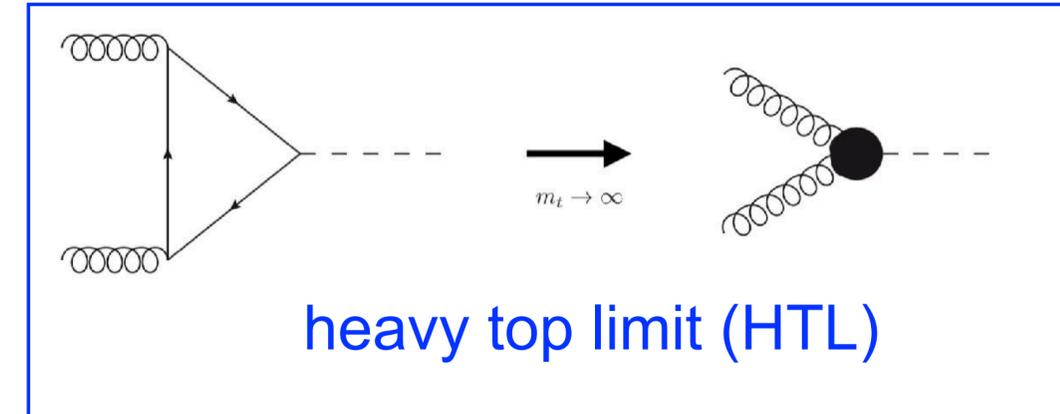
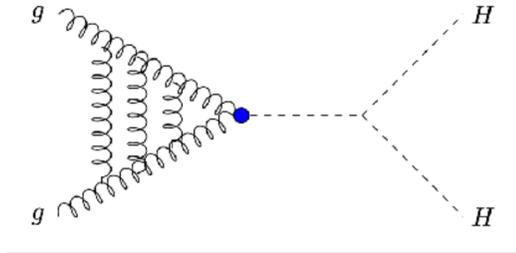
Borowka, Greiner, GH, Jones, Kerner, Schlenk et al. '16

Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher '18

Davies, GH, Jones, Kerner, Mishima, Steinhauser, Wellmann '19

top quark mass scheme uncertainties: pole mass versus  $\overline{\text{MS}}$  mass

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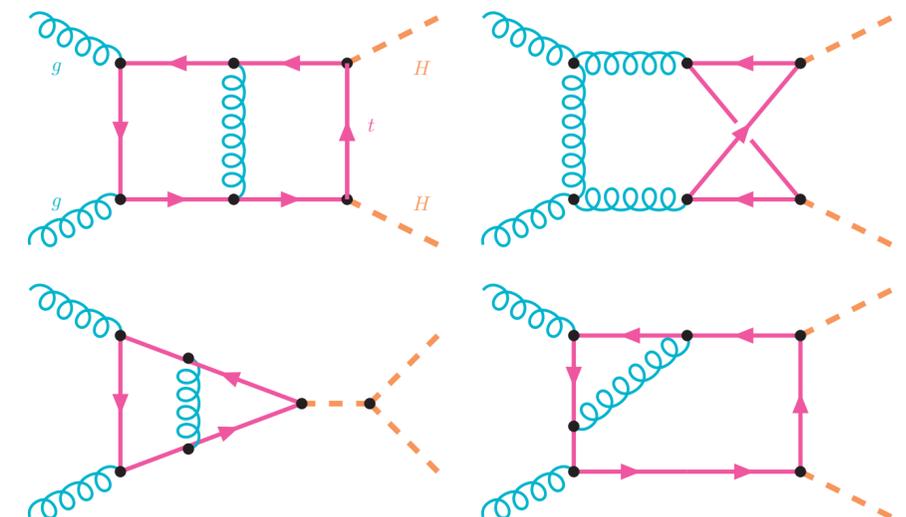
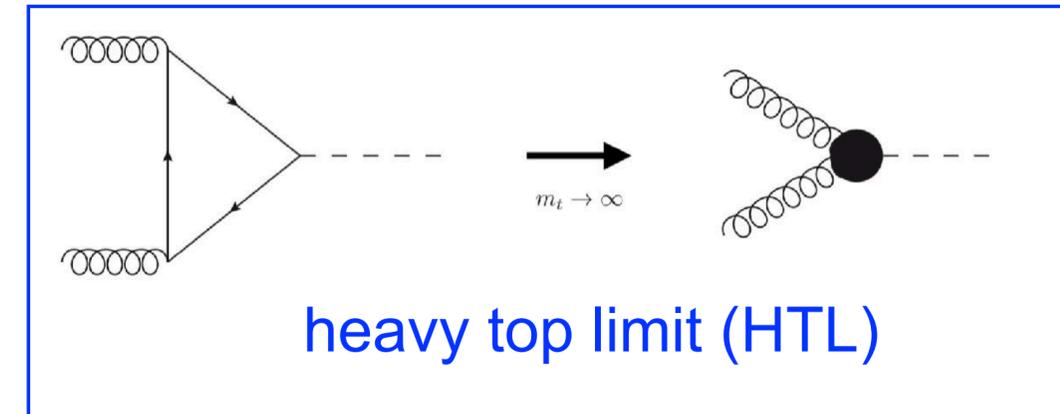
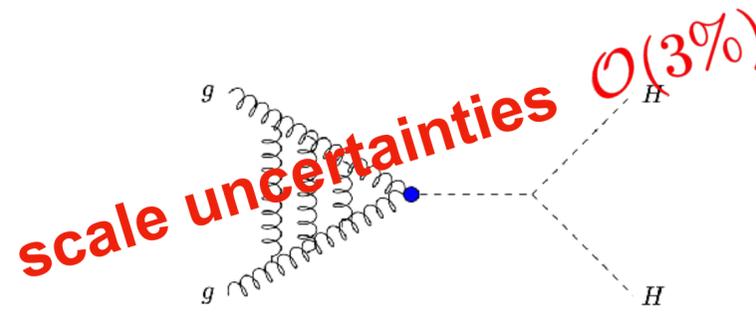
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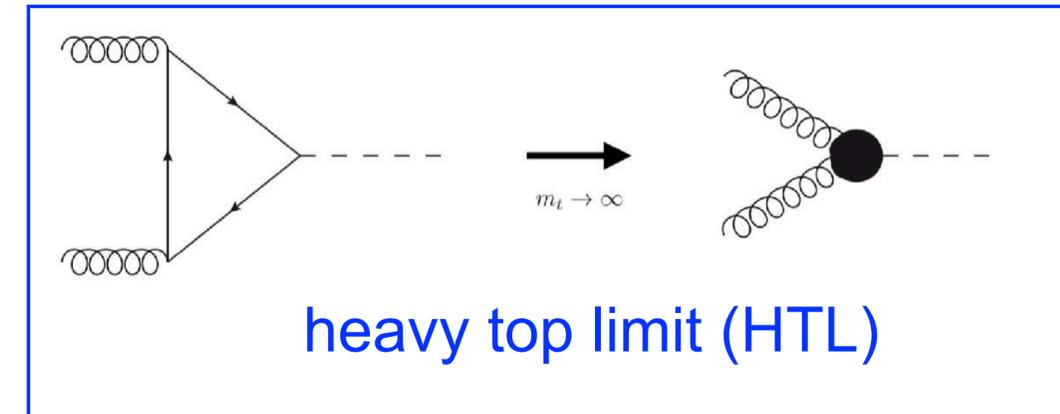
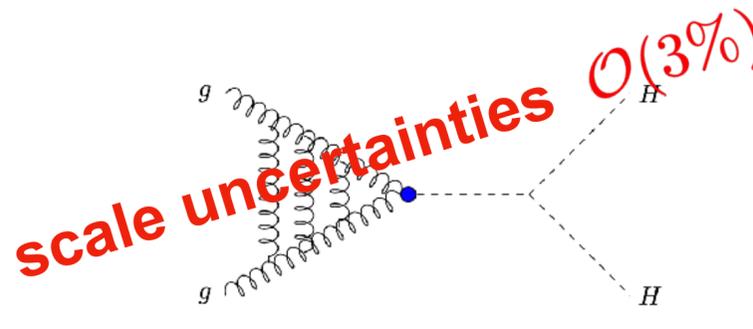
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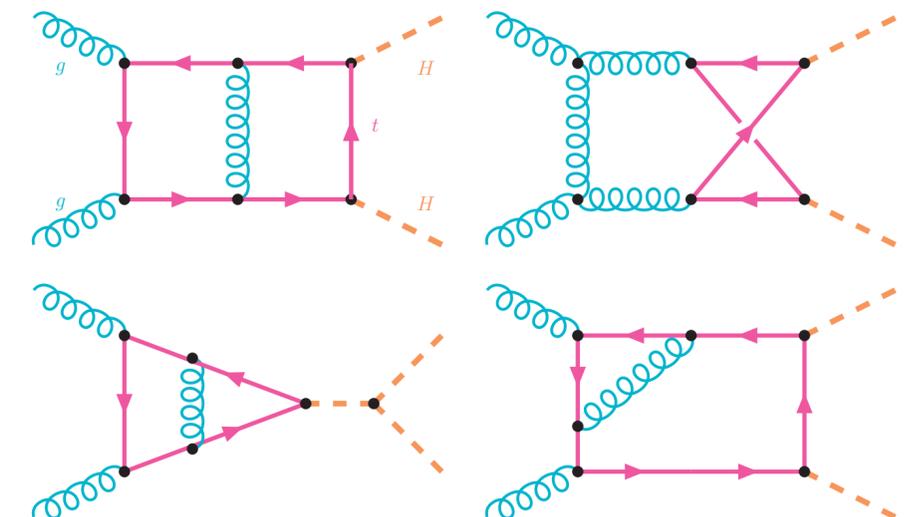
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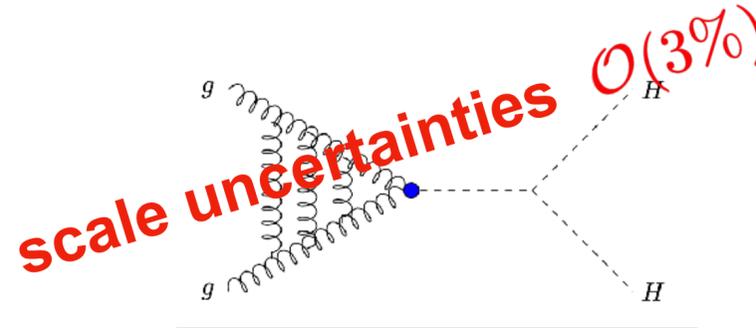


residual missing top mass effects estimated to  $\mathcal{O}(5\%)$

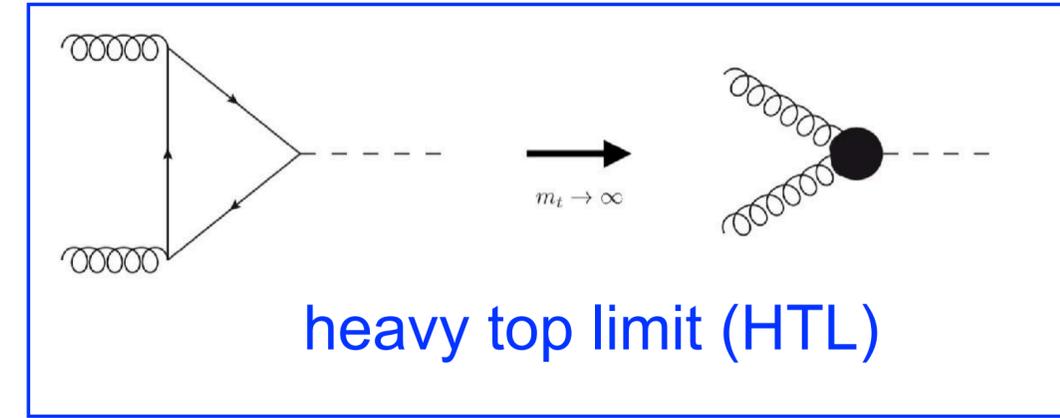


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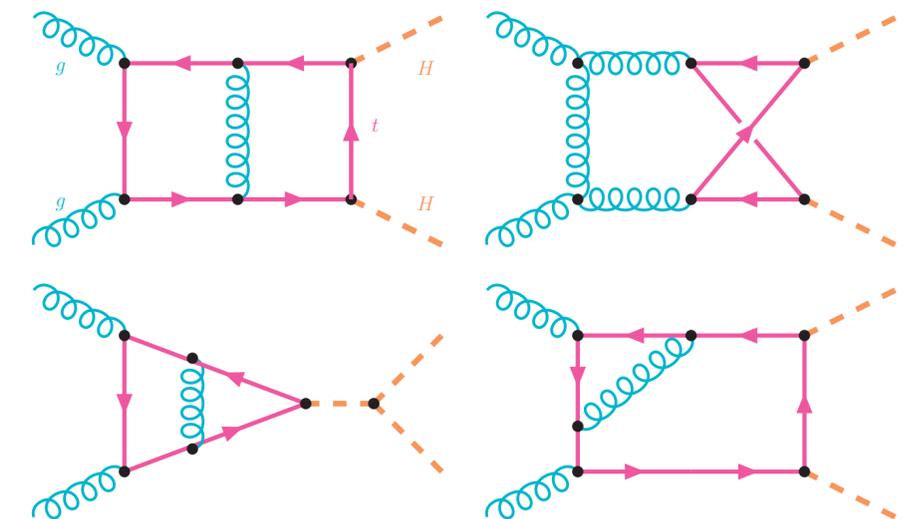
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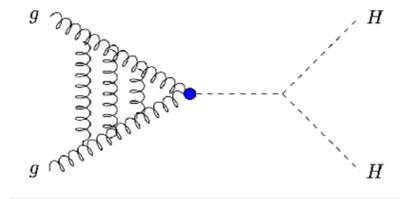
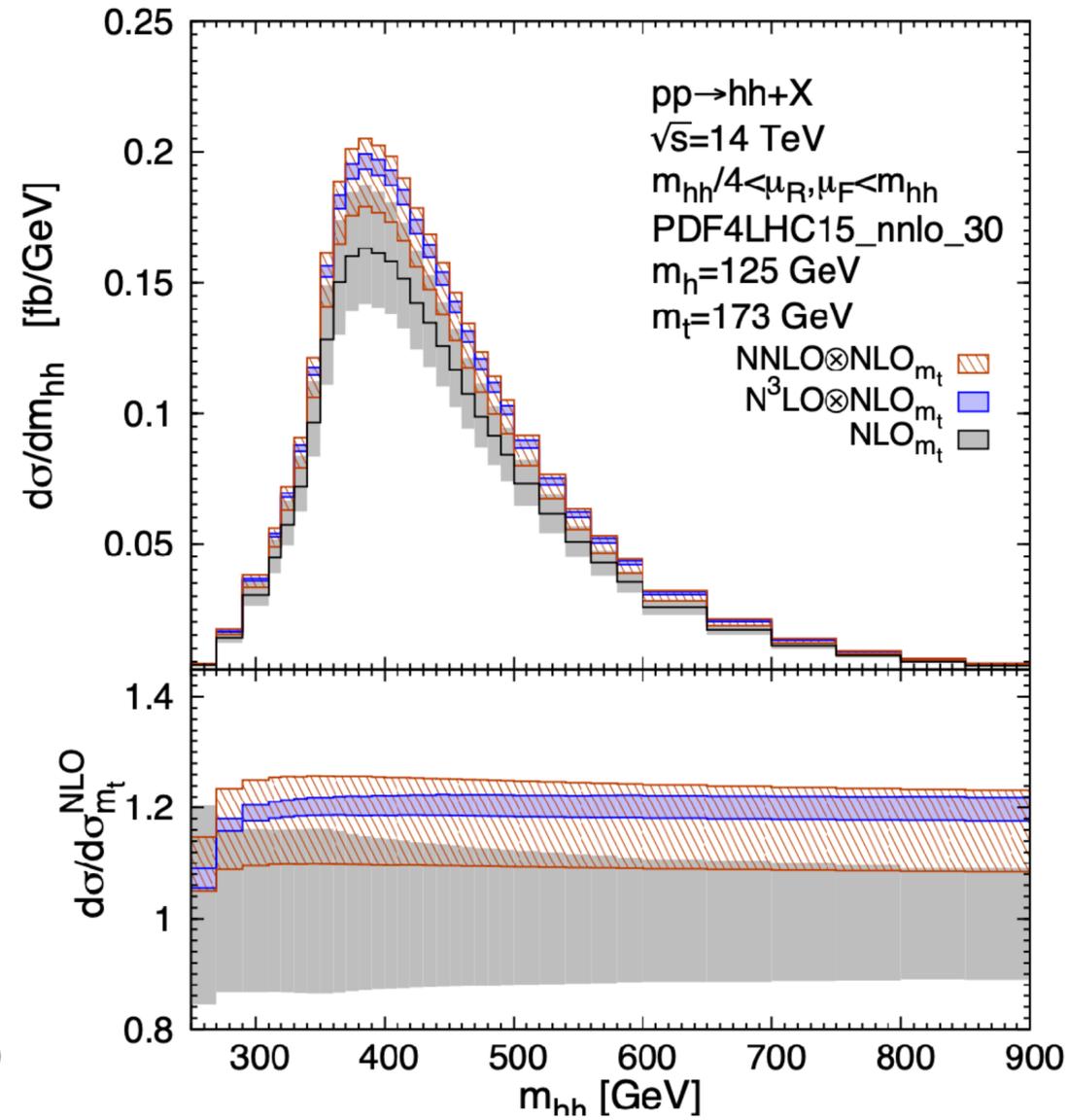
Baglio, Campanario, Glaus, Mühlleitner, Rorner, Spira '18, '20



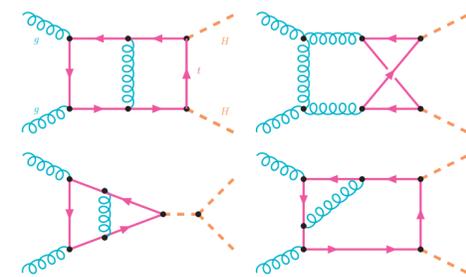
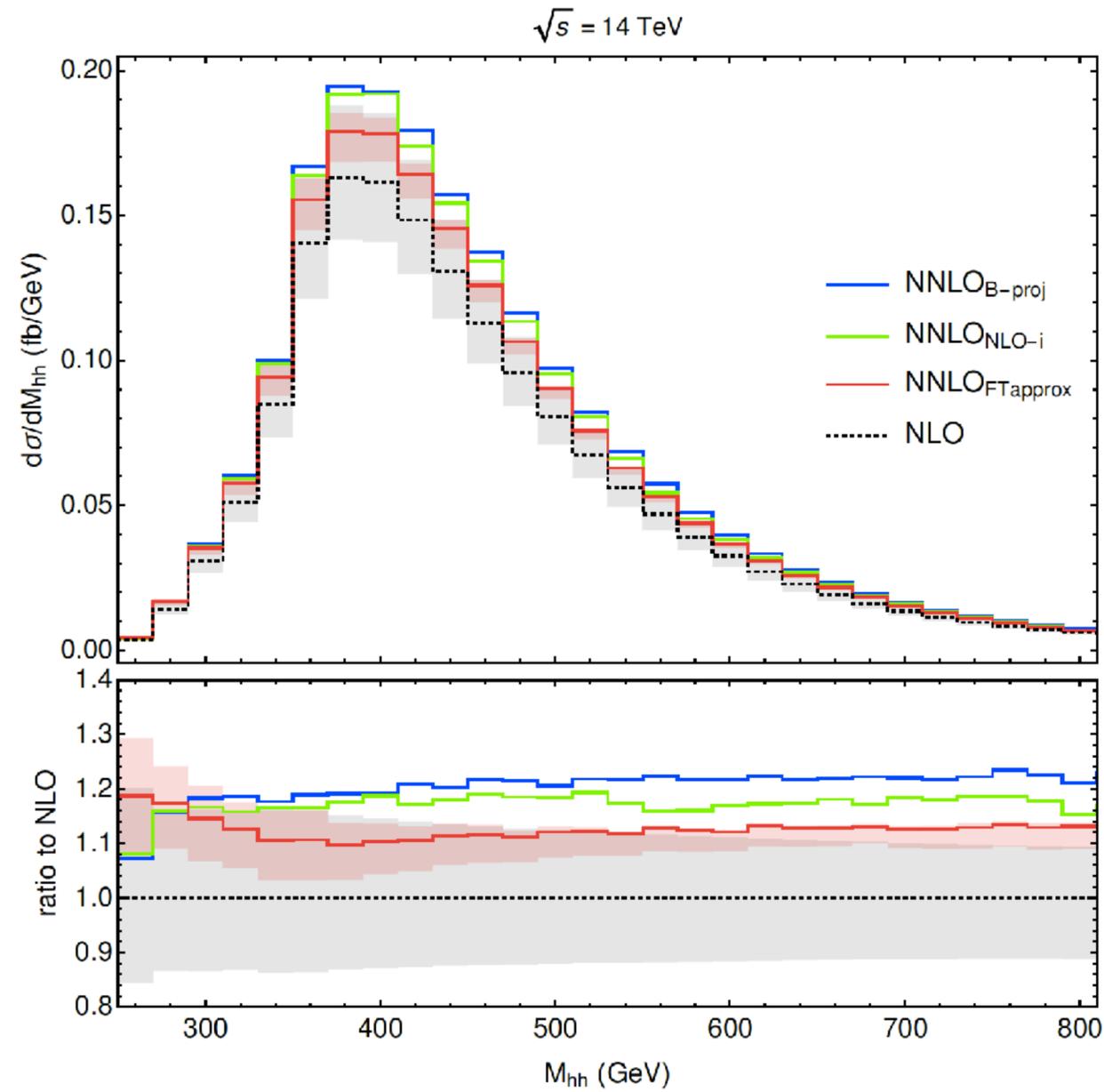
uncertainty due to top mass scheme  $\mathcal{O}(20\%)$

# Highest perturbative orders (SM)

Chen, Li, Shao, Wang 1912.13001



Grazzini, Kallweit, GH, Jones, Kerner, Lindert, Mazzitelli 1803.02463

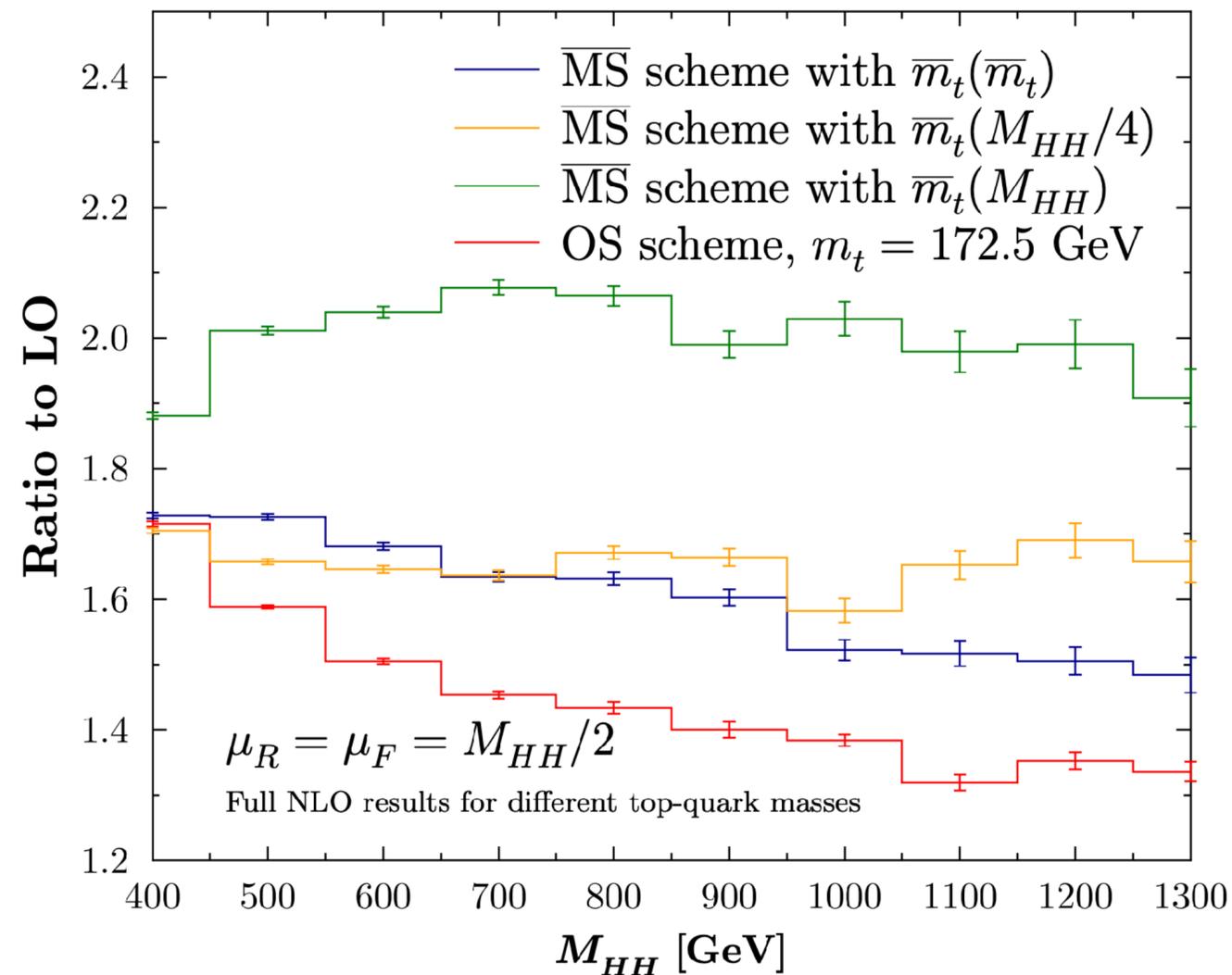


# Top quark mass renormalisation scheme uncertainties

$$\bar{m}_t(m_t) = \frac{m_t}{1 + \frac{4}{3} \frac{\alpha_s(m_t)}{\pi} + K_2 \left( \frac{\alpha_s(m_t)}{\pi} \right)^2 + K_3 \left( \frac{\alpha_s(m_t)}{\pi} \right)^3}$$

relation between pole mass and  $\overline{\text{MS}}$  mass

$gg \rightarrow HH$  at NLO QCD |  $\sqrt{s} = 13$  TeV | PDF4LHC15



Baglio, Campanario, Glaus Mühlleitner, Ronca, Spira 2003.03227, 2008.11626

also present in other heavy quark loop induced processes

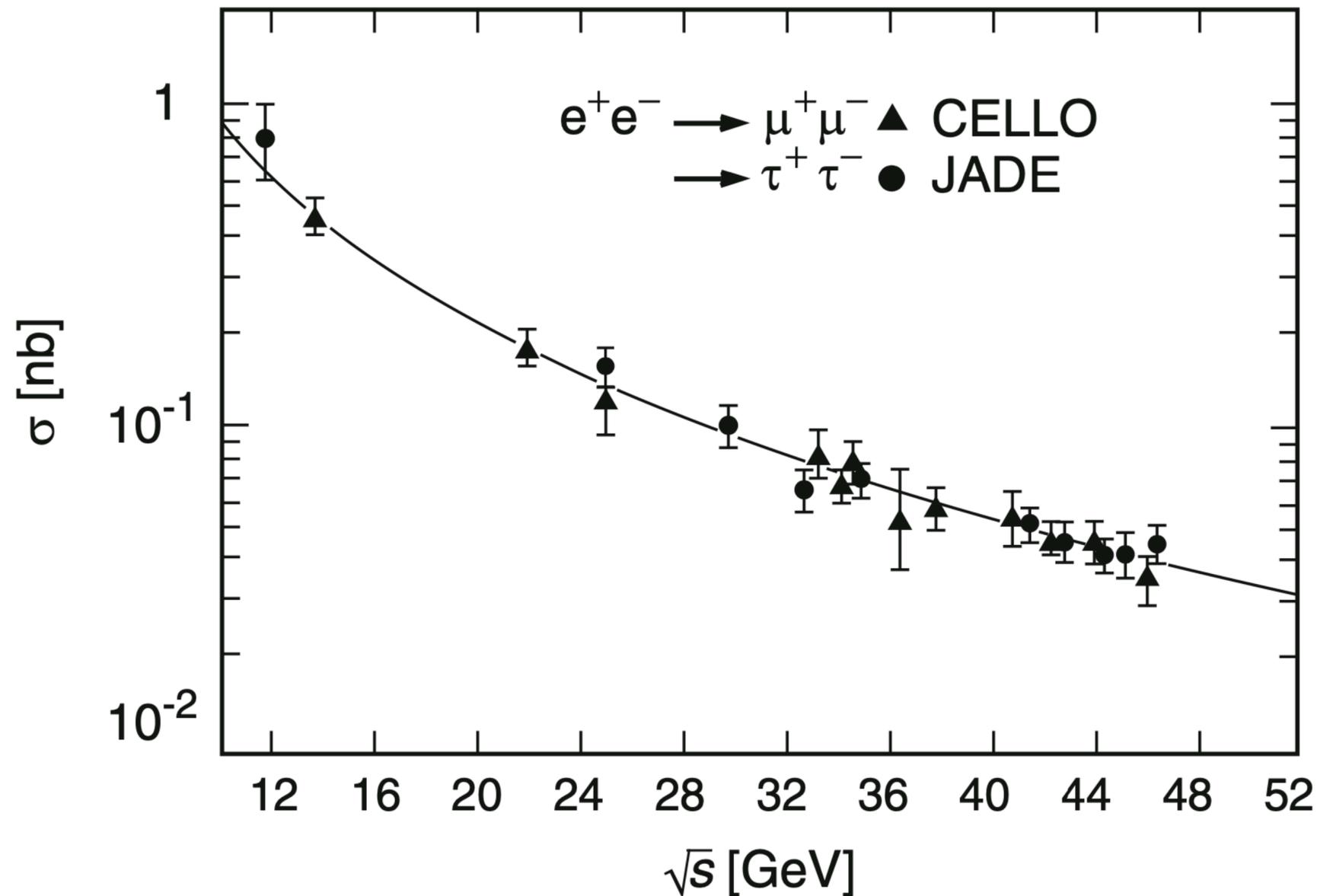
# Effective Field Theory parametrisation of New Physics



“Standard Model Effective Field Theory” (SMEFT)

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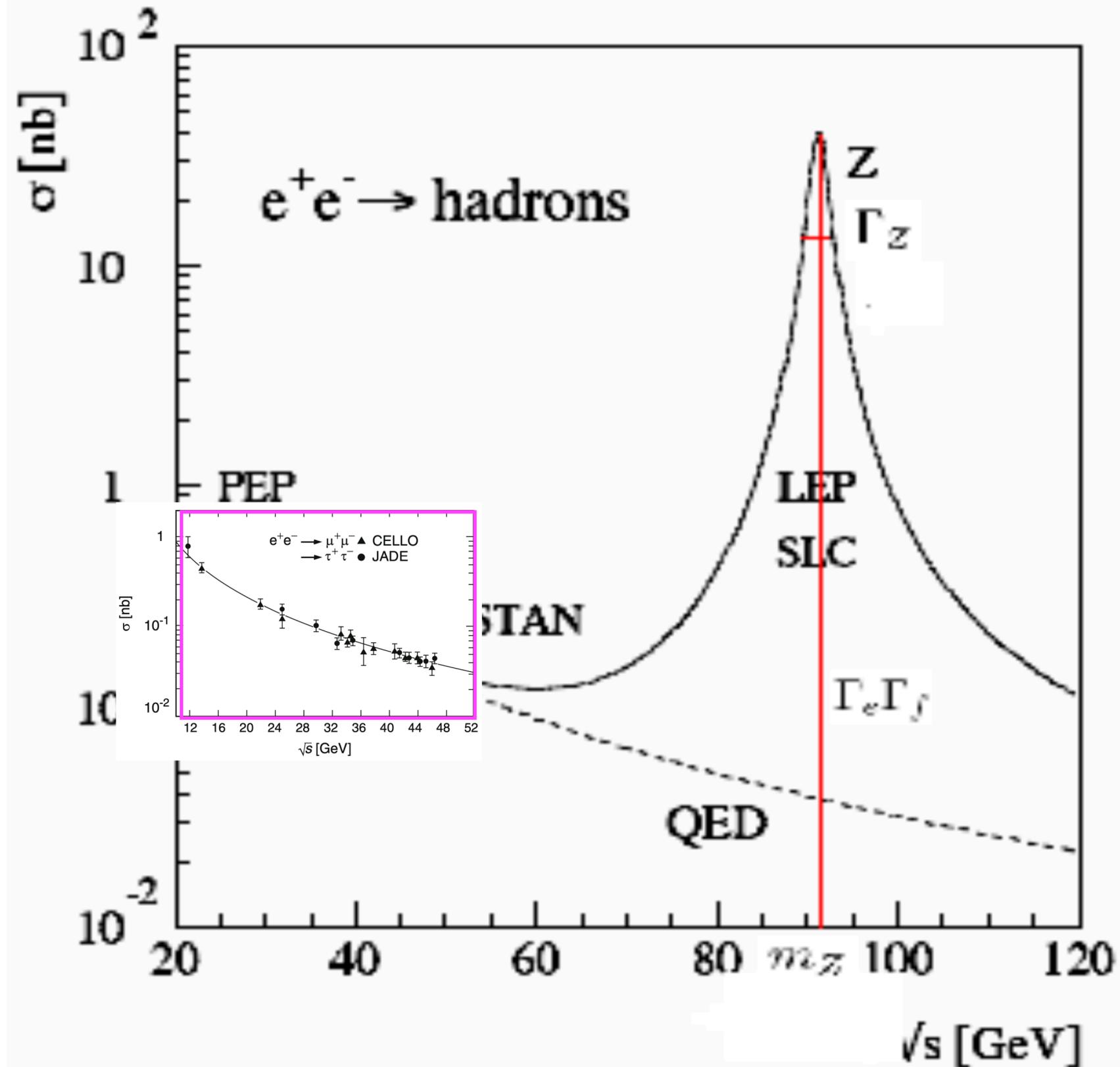


**QEFT (QED-Effective Field Theory)**

tests of QED about 40 years ago ...

$$\sigma \sim 1/s$$

# More complete picture



$$|M|^2 = \left| \begin{array}{c} \text{Diagram with } \gamma \text{ exchange} \\ + \\ \text{Diagram with } Z \text{ exchange} \end{array} \right|^2$$

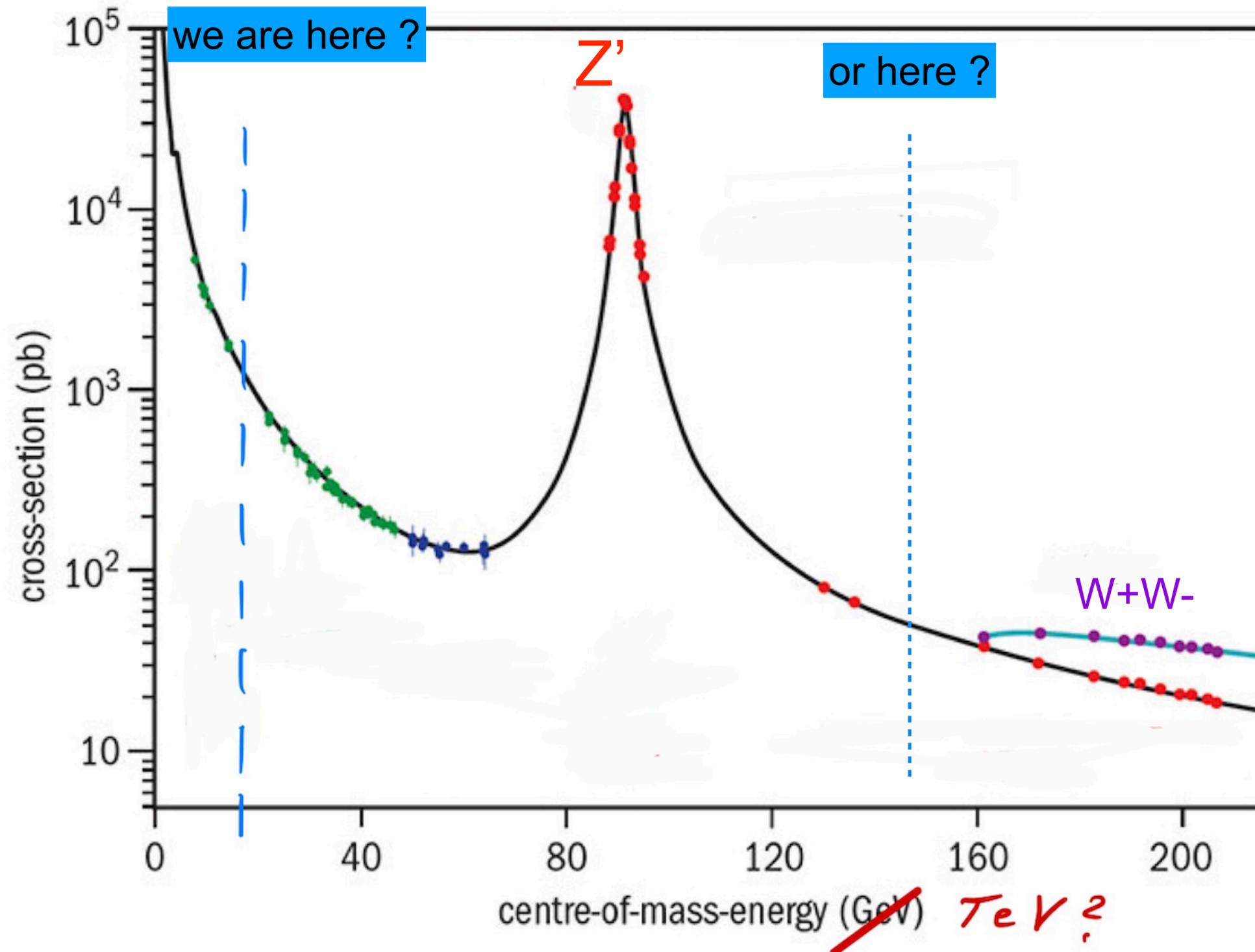
$$M \sim 1/q^2$$

$$M \sim 1/[q^2 - m_Z^2 + im_Z\Gamma_Z]$$



$$M \sim 1/m_Z^2 \text{ for } q^2 \ll m_Z^2$$

# Low energy picture



# Effective Field Theory expansion schemes

SMEFT (Standard Model Effective Field Theory):

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{C_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{\text{dim6}} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right)$$

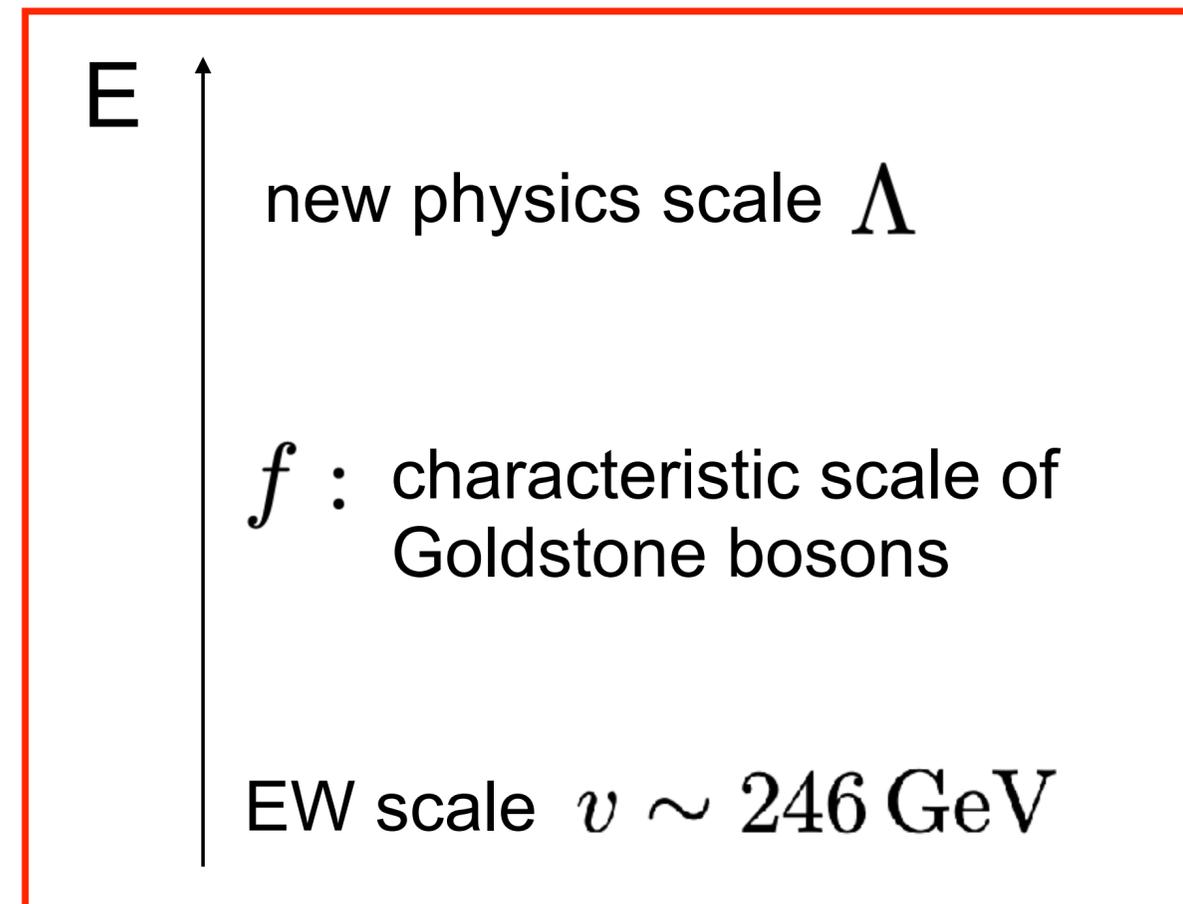
canonical dimension counting

HEFT (Higgs Effective Field Theory):

$$\mathcal{L}_{\text{HEFT}} = \mathcal{L}_0 + \sum_{L=1}^{\infty} \sum_i \left(\frac{1}{16\pi^2}\right)^L c_i^{(L)} \mathcal{O}_i^{(L)}$$

counting of loop orders, expansion parameter:  $f^2/\Lambda^2 \approx 1/(16\pi^2)$

(similar to chiral perturbation theory)



# Lagrangians relevant for HH production

## SMEFT:

$$\Delta\mathcal{L}_{\text{dim6}} = \frac{\bar{c}_H}{2v^2} \partial_\mu(\phi^\dagger\phi)\partial^\mu(\phi^\dagger\phi) + \frac{\bar{c}_u}{v^2} y_t(\phi^\dagger\phi\bar{q}_L\tilde{\phi}t_R + \text{h.c.}) - \frac{\bar{c}_6}{2v^2} \frac{m_h^2}{v^2} (\phi^\dagger\phi)^3$$

$$+ \frac{\bar{c}_{ug}}{v^2} g_s(\bar{q}_L\sigma^{\mu\nu}G_{\mu\nu}\tilde{\phi}t_R + \text{h.c.}) + \frac{4\bar{c}_g}{v^2} g_s^2\phi^\dagger\phi G_{\mu\nu}^a G^{a\mu\nu}$$

$\bar{c}_i = C_i^{(6)} \frac{v^2}{\Lambda^2}$

(SILH basis/Warsaw)

Giudice et al. hep-ph/0703164

Grzadkowski et al. 1008.4884

Gröber et al. 1504.06577

## HEFT:

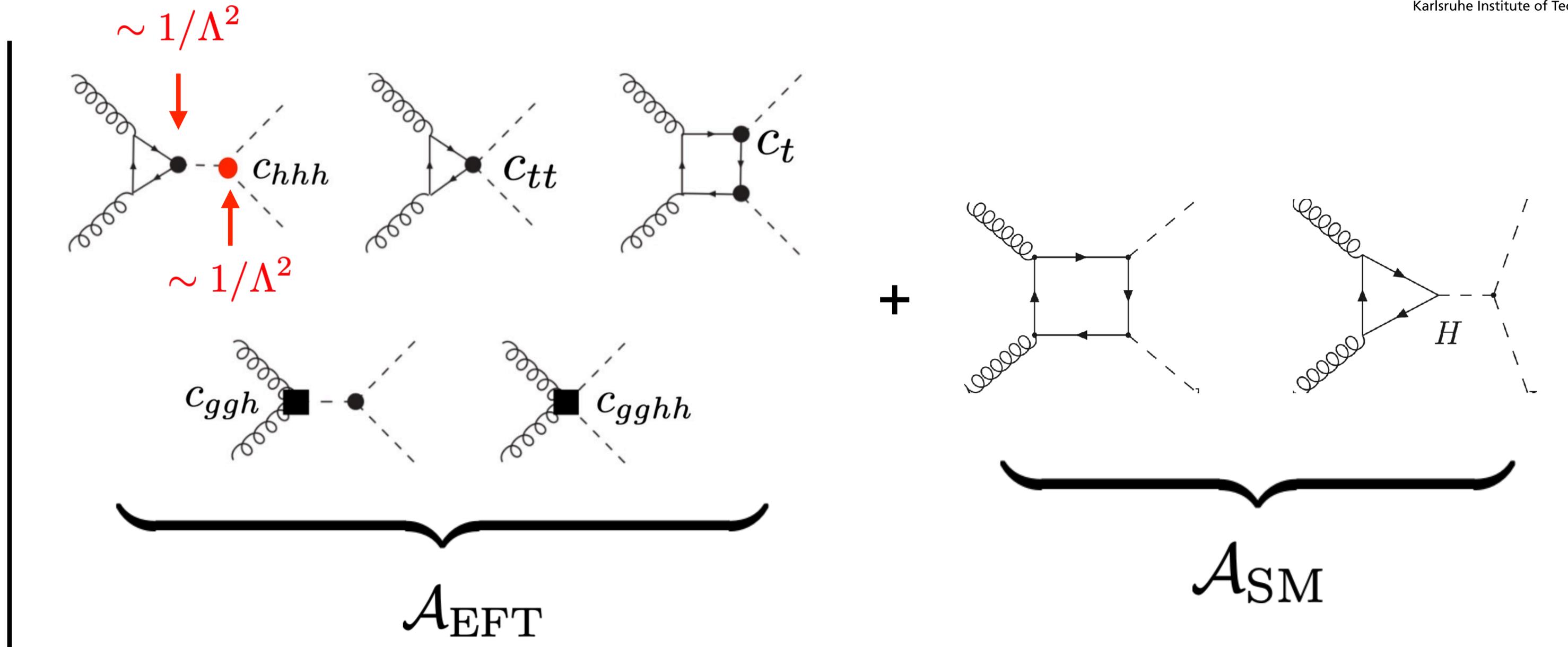
$$\mathcal{L} \supset -m_t \left( c_t \frac{h}{v} + c_{tt} \frac{h^2}{v^2} \right) \bar{t}t - c_{hhh} \frac{m_h^2}{2v} h^3 + \frac{\alpha_s}{8\pi} \left( c_{ggh} \frac{h}{v} + c_{gghh} \frac{h^2}{v^2} \right) G_{\mu\nu}^a G^{a,\mu\nu}$$

coupling relations at Lagrangian level:  $c_t = 1 - \bar{c}_H/2 - \bar{c}_u$  ,  $c_{tt} = -(\bar{c}_H + 3\bar{c}_u)/2$

$$c_{ggh} = 2 c_{gghh} = 128\pi^2 \bar{c}_g \quad , \quad c_{hhh} = 1 - \frac{3}{2}\bar{c}_H + \bar{c}_6$$

# SMEFT at amplitude squared level

2



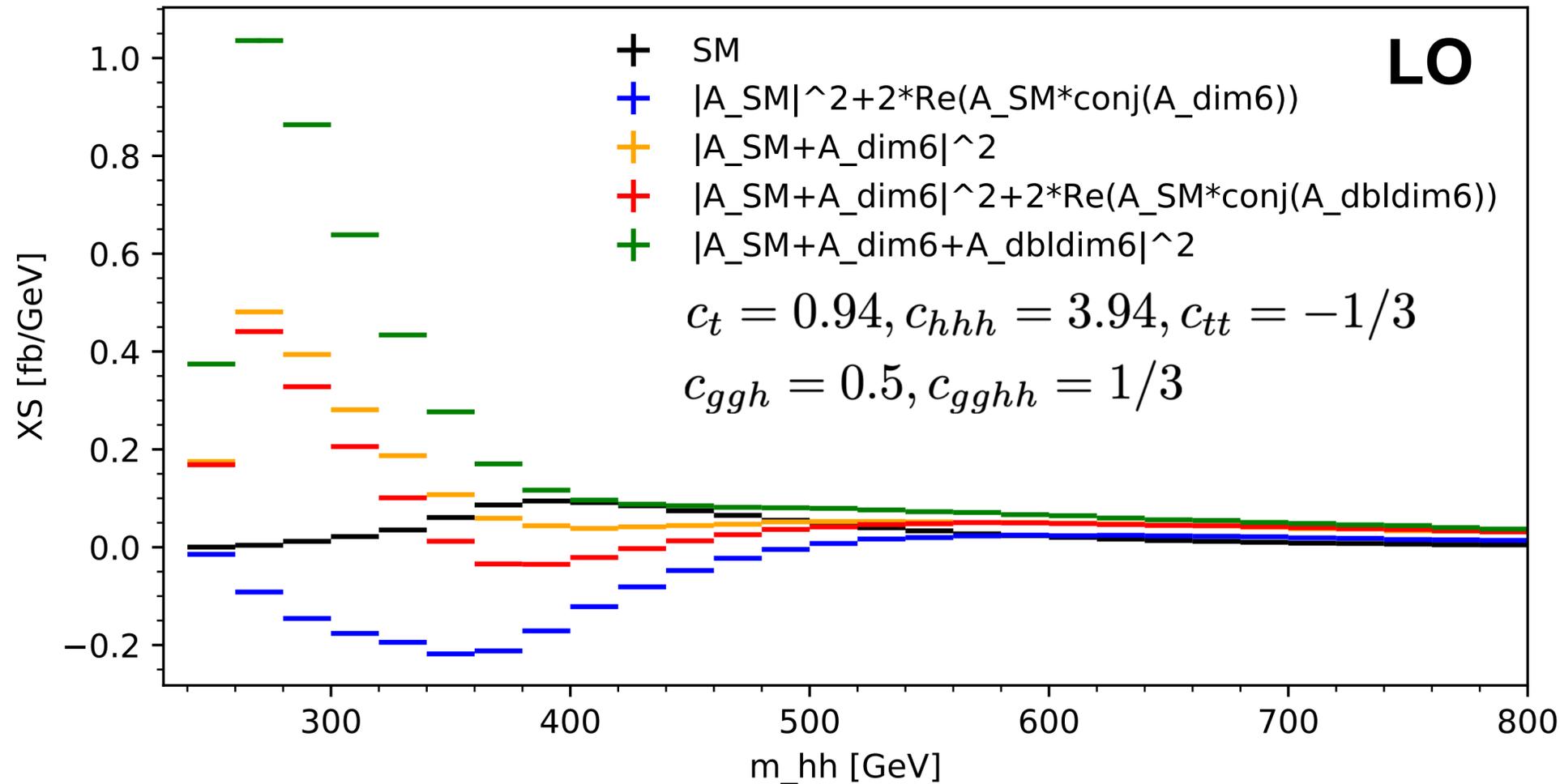
terms  $\sim 1/\Lambda^4$  same order as dim 8 operators (which are not included)

# SMEFT at amplitude squared level

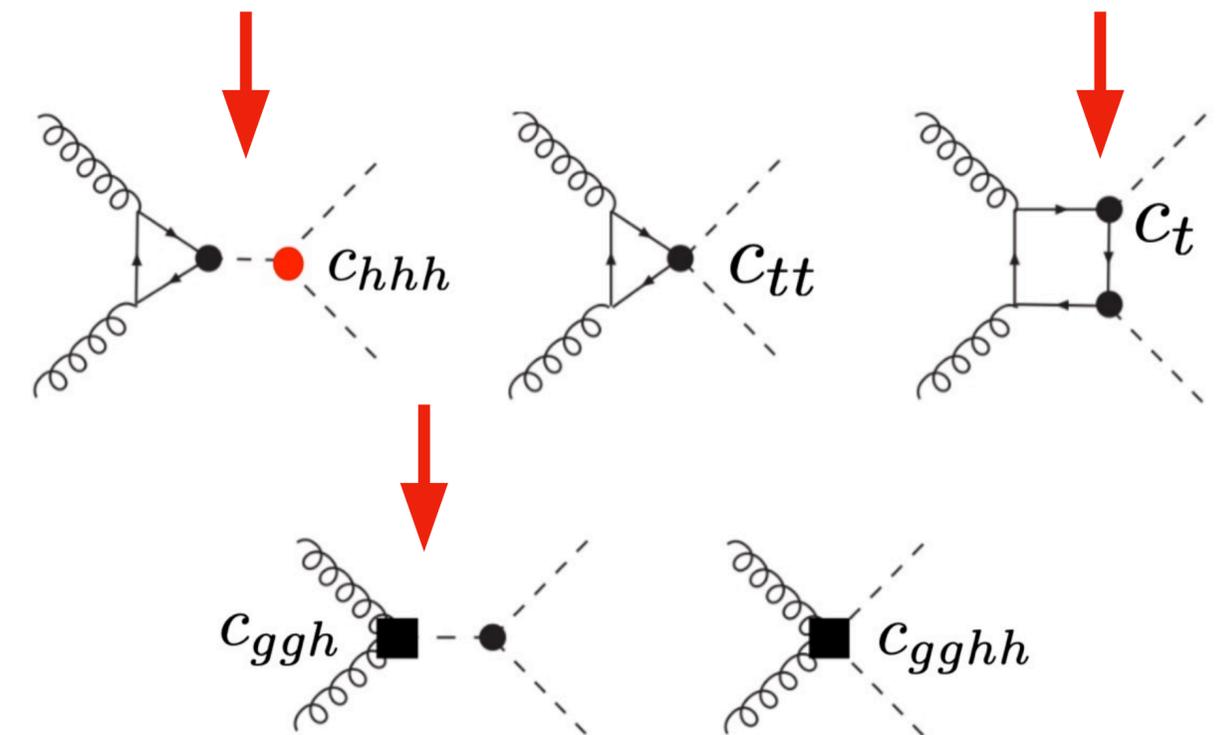
canonical dimension counting  $\rightarrow$  how to treat  $|\text{dim6}|^2$  versus  $\text{dim8}$  ?  
 $\rightarrow$  how to treat double operator insertions?

figure: Jannis Lang

Benchmark point 1  $\Lambda = 1 \text{ TeV}$



two operators in one diagram



# Summary & Outlook

- Indirect signs of New Physics: precision is the key
- Increasing the precision at the percent level has many facets:  
missing higher orders (QCD/EW), parton shower uncertainties, PDFs,  
heavy quark mass effects/scheme dependence, non-perturbative effects, ...
- Testable hypotheses of New Physics:
  - Concrete models -> model dependence
  - Effective field theories -> dependence on counting scheme, truncation, unitarity

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efinger-consulting.de

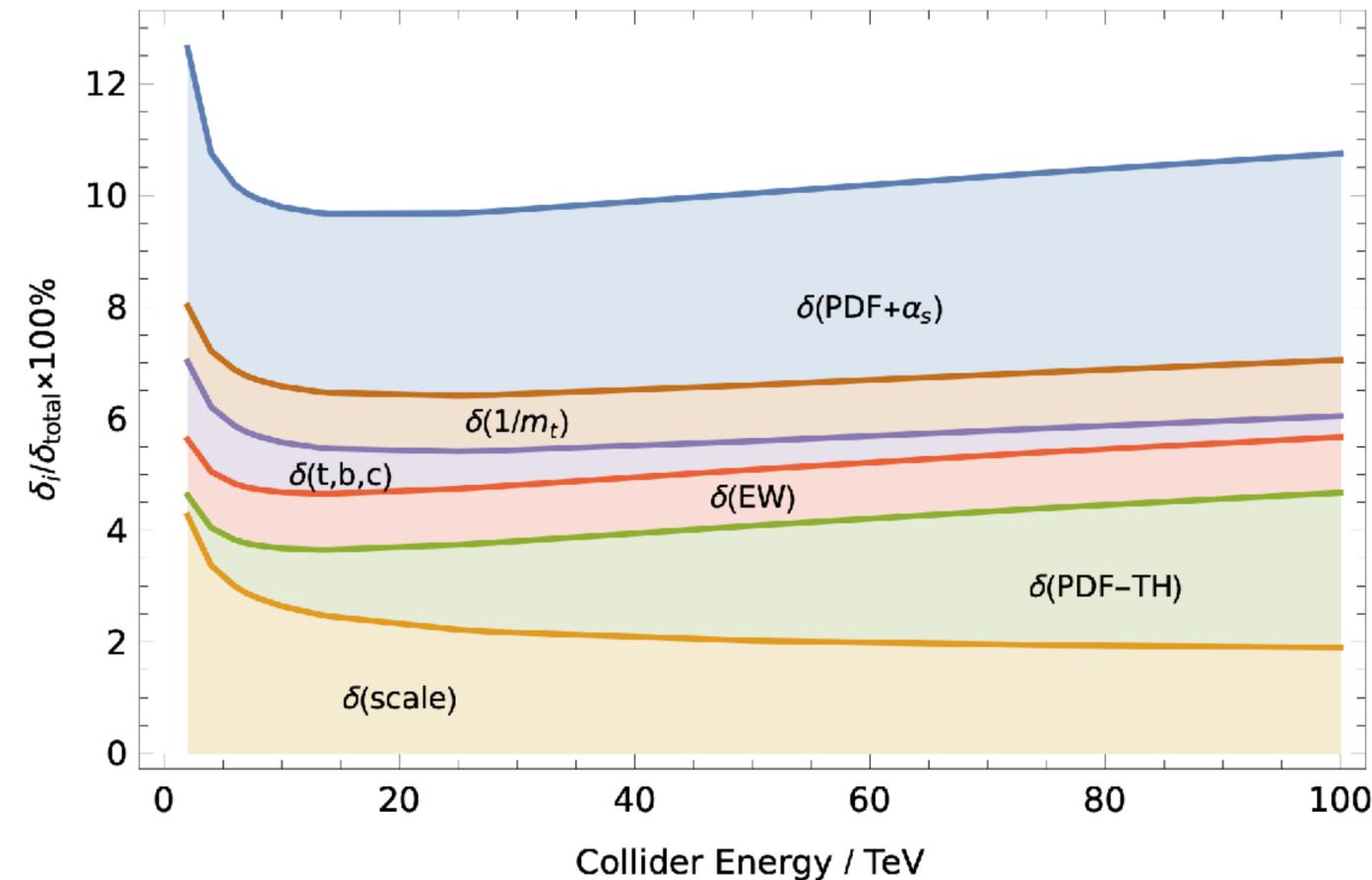
joint efforts needed to work on all the different aspects!

# Higgs production in gluon fusion: uncertainties

$\delta(\text{scale})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$	$\delta(\text{PDF})$	$\delta(\alpha_s)$
+0.10 pb -1.15 pb	$\pm 0.56$ pb	$\pm 0.49$ pb	$\pm 0.40$ pb	$\pm 0.49$ pb	$\pm 0.89$ pb	+1.25 pb -1.26 pb
+0.21% -2.37%	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$	$\pm 1.85\%$	+2.59% -2.62%

scale uncertainties no longer the dominant uncertainties

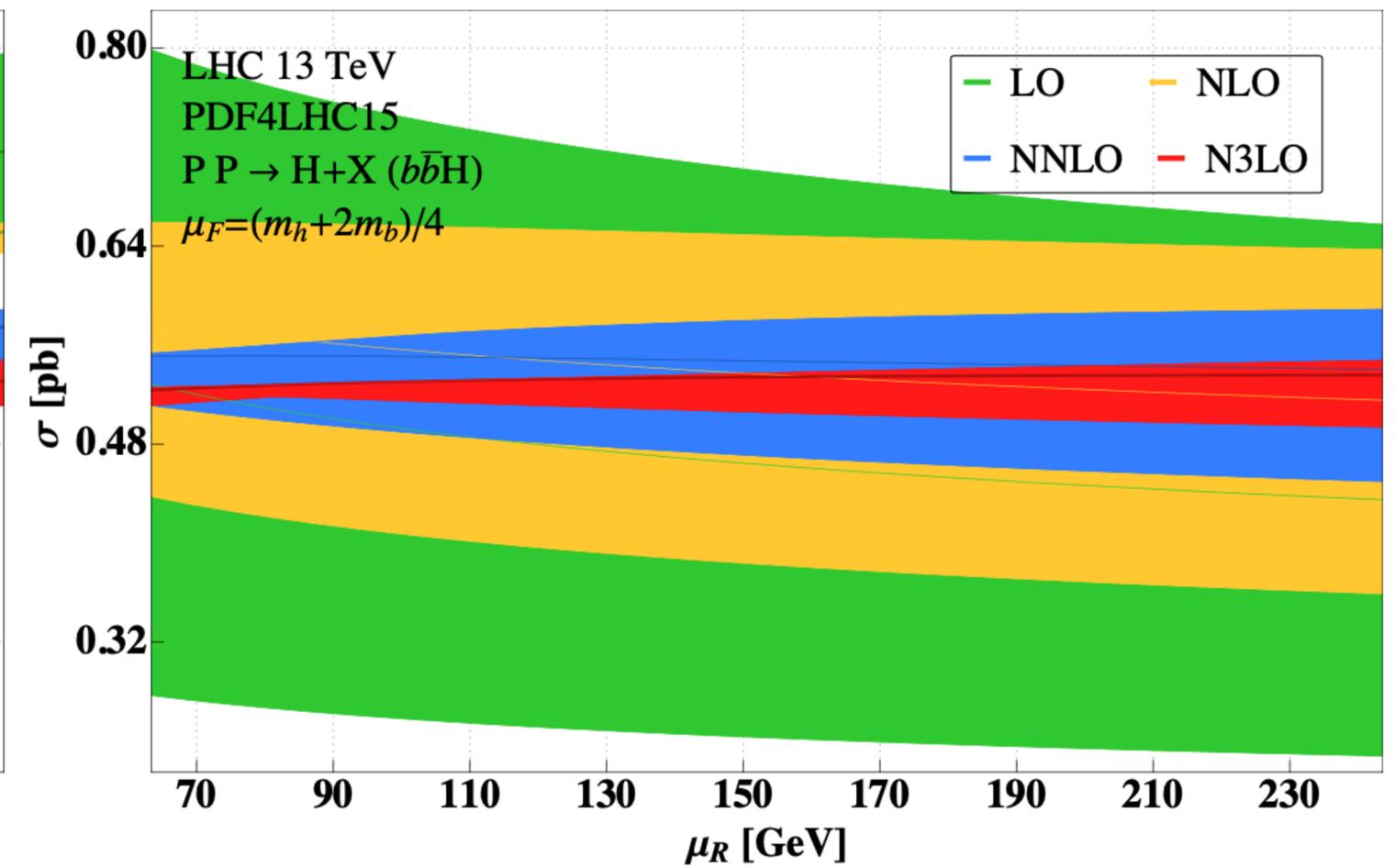
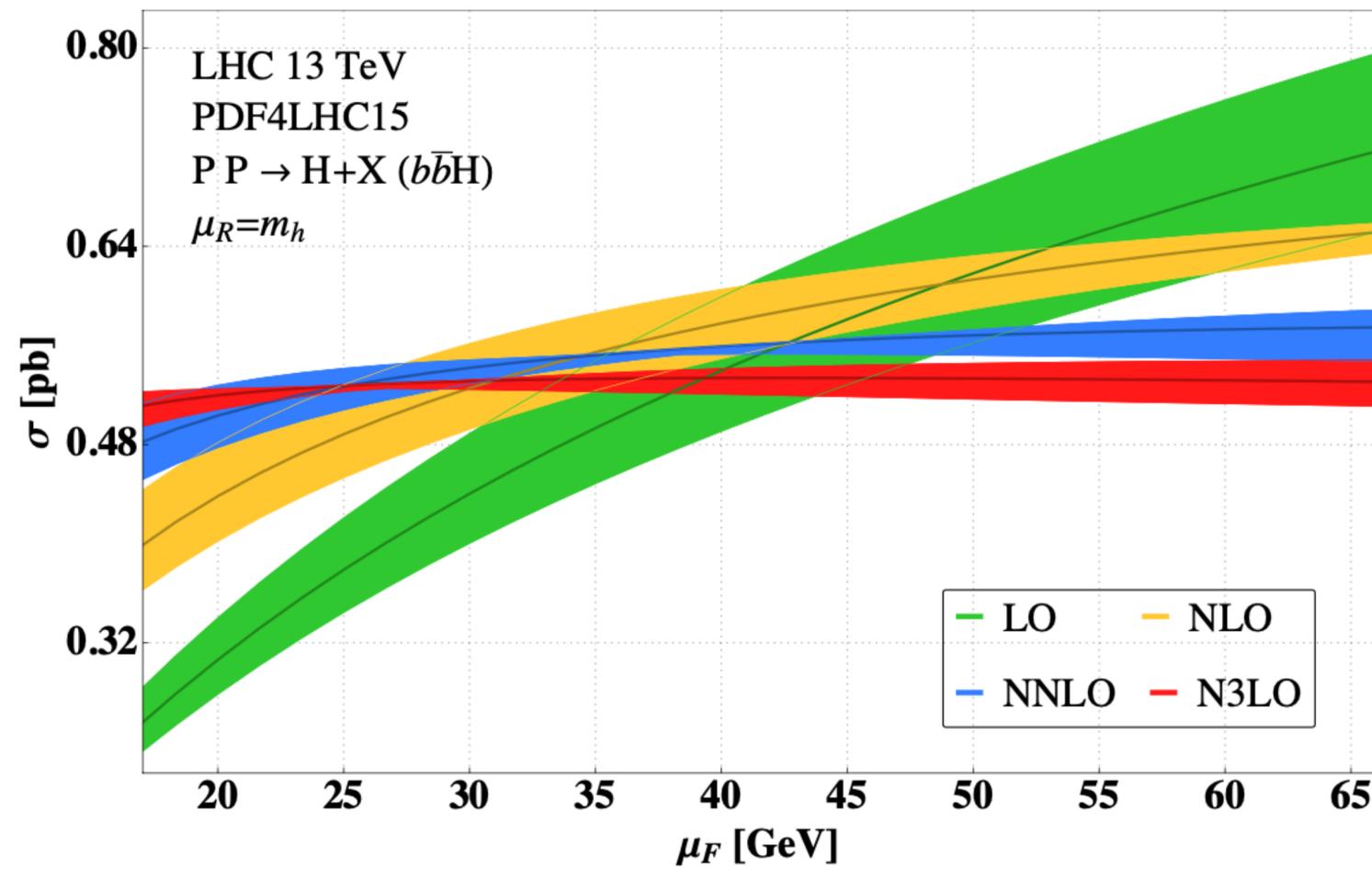
2009.00516



NNLO PDFs with  
 $N^3\text{LO } \sigma$

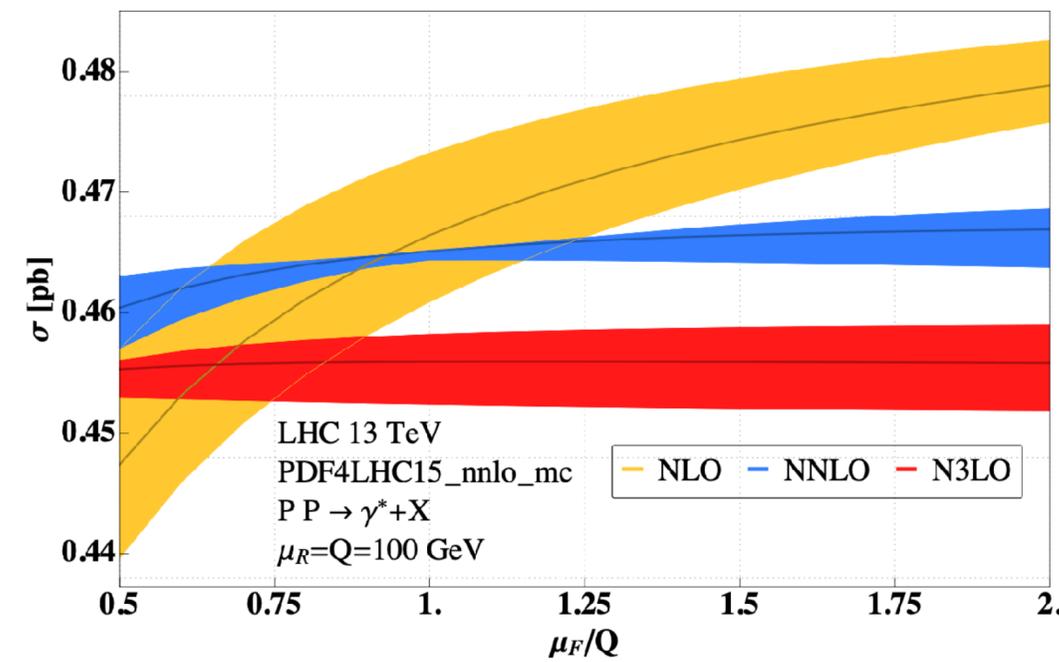
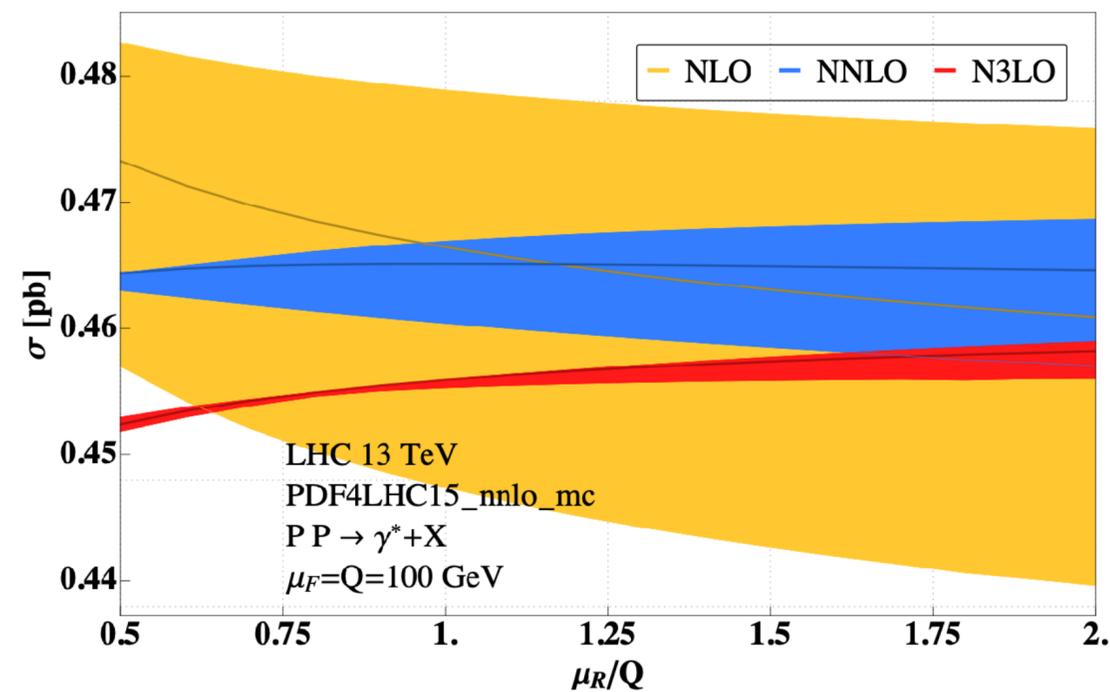
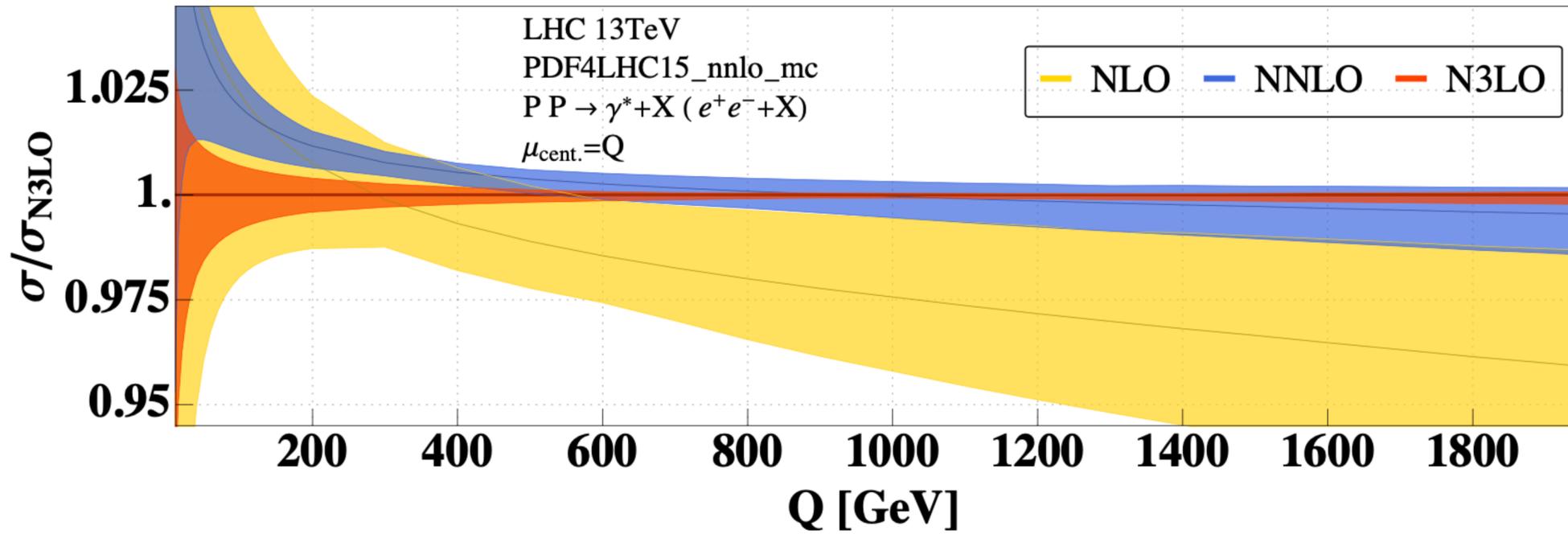
1902.00134

# bbH

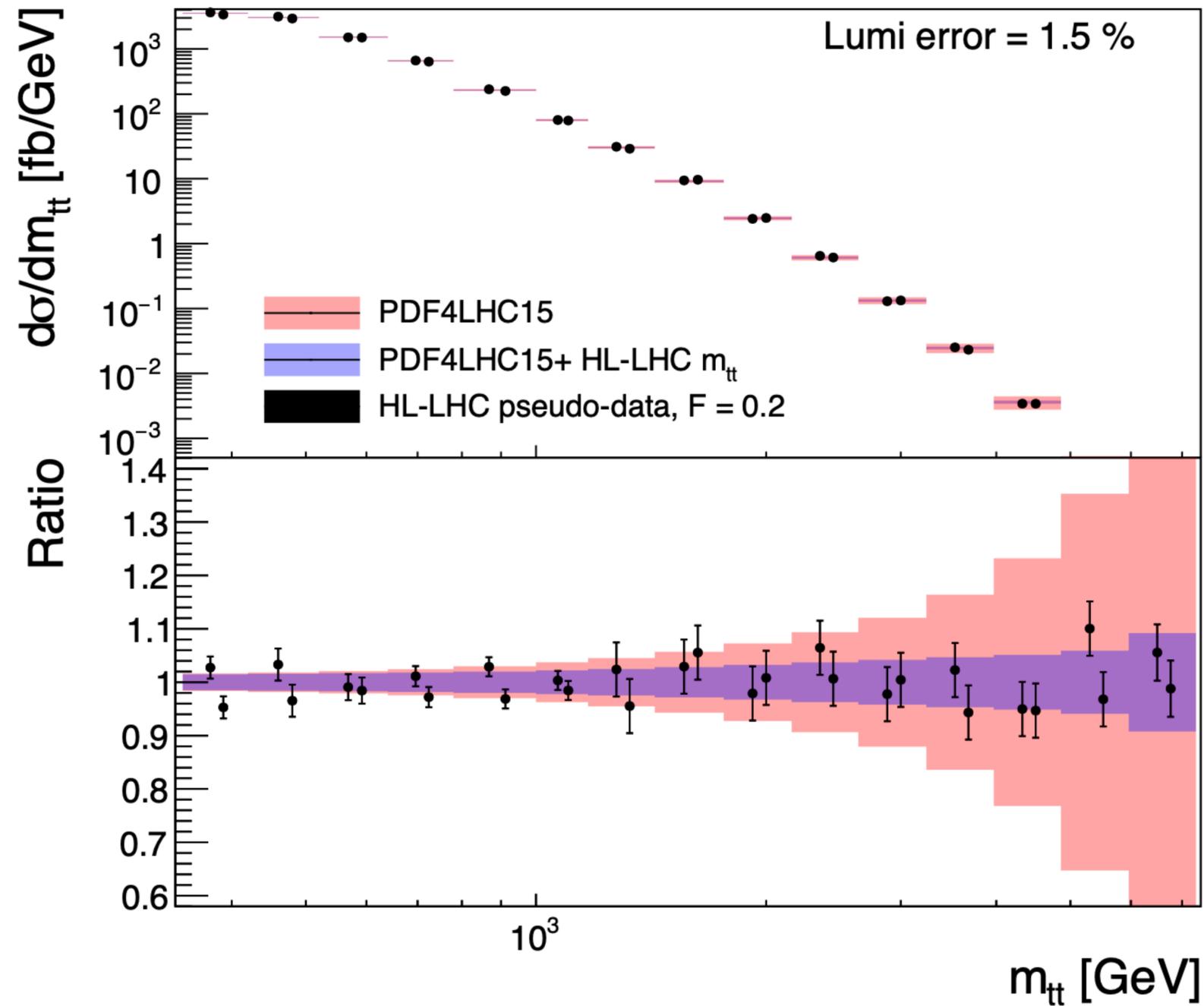


# Drell-Yan (NC)

Duhr, Dulat, Mistlberger  
2001.07717



## Projected invariant $t\bar{t}$ mass data



R. Khalek et al,  
1810.03639

# Counting schemes

HEFT (EWChL): “loop expansion”

based on chiral dimension  $d_\chi = 2L + 2$   $L$ : “Loop”

with  $d_\chi(A_\mu, \varphi, h) = 0$ ,  $d_\chi(\partial, \bar{\psi}\psi, g, y) = 1$

↑  
expansion in  
canonical  
dimension  $1/\Lambda^2$

**SMEFT**

$$\xi = v^2/f^2$$

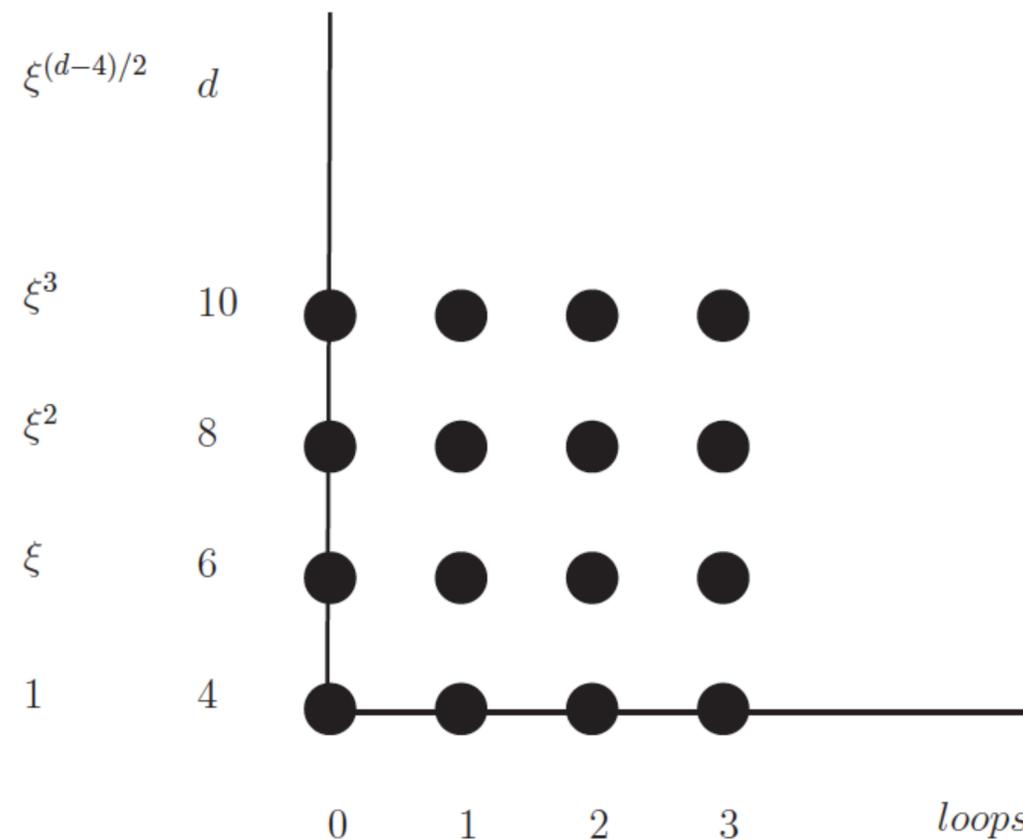


figure: G.Buchalla

loop expansion



**HEFT**