

On the direct correlation between γ -rays and neutrinos from blazars

Shan Gao

Collaborators: Martin Pohl, Walter Winter

arXiv: 1610. 05306

Dec. 9, 2016
HAP workshop,
Cochem, Germany



Outline

- Motivation

Why blazars / MWL & Multi-Msg. / $L_v \sim L_\gamma$?

- Methods and modeling

What's special on PKS B1424-418 / our analysis ?

- Results and implications

What's new to consider in a future analysis ?

Blazars

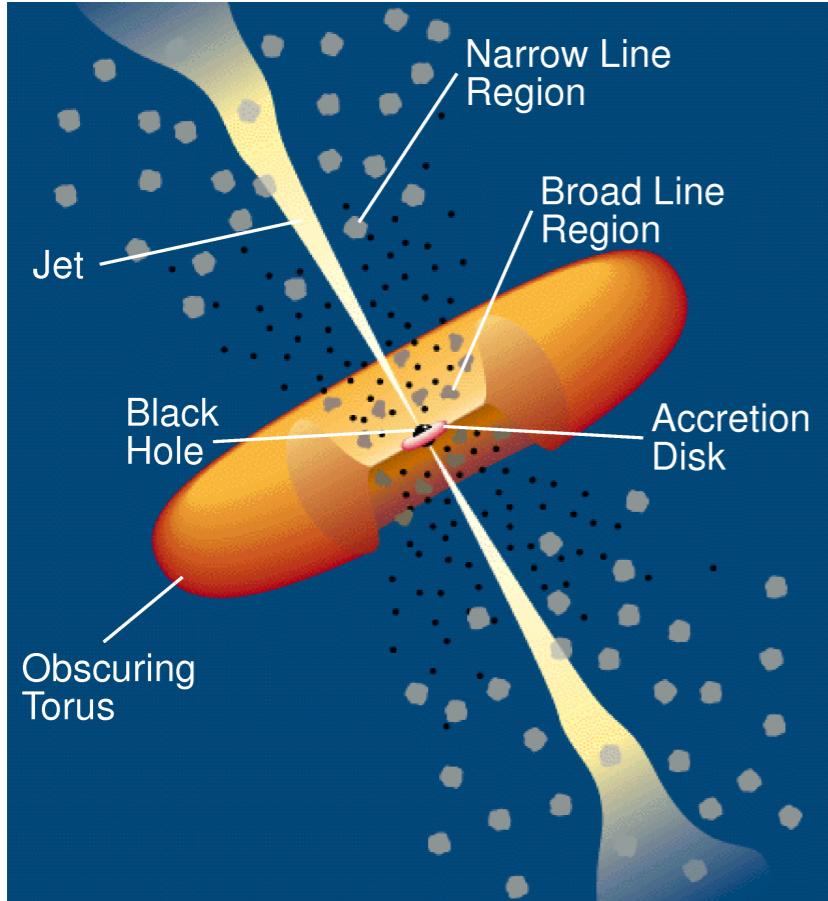
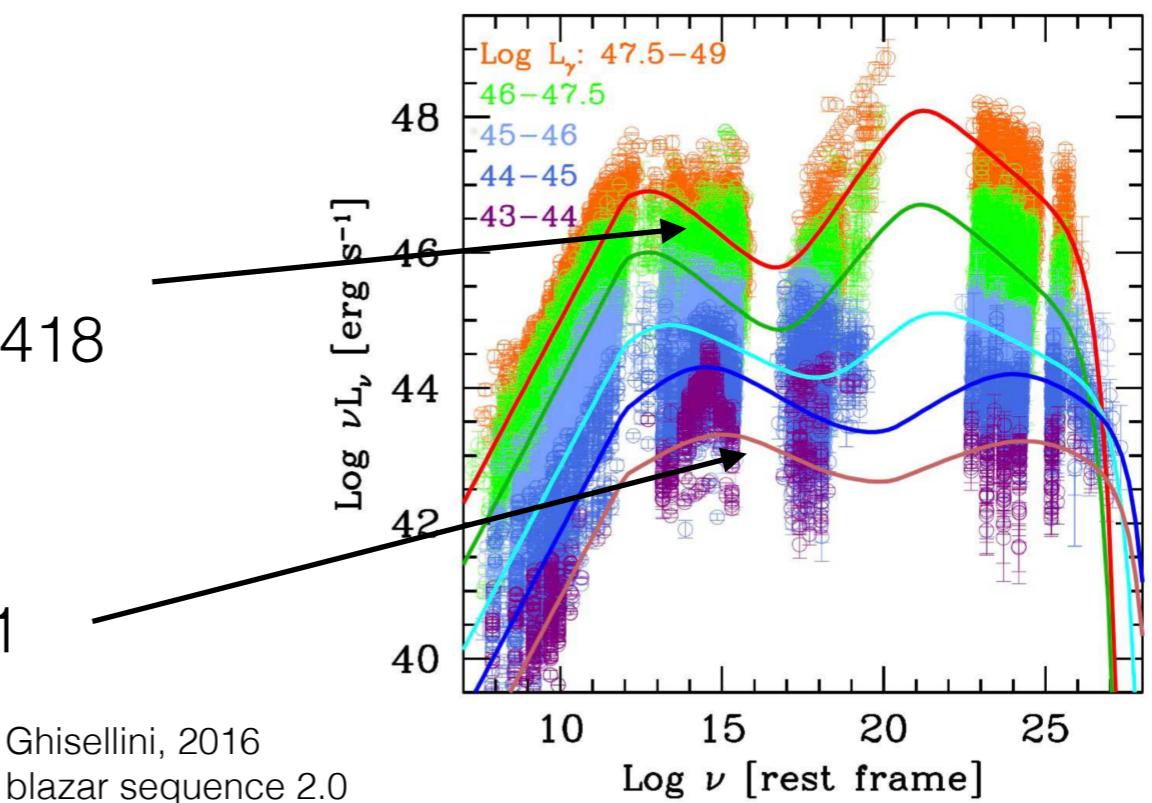


Figure: blazar, Urry & Padovani 95

- Relativistic jets & Doppler boosting;
- Power from SMBH
- Spectrum: non-thermal double hump
- Variable on all time scales
- Population: 745 (3LAC catalog)
- Distribution: isotropic
- Luminosity range $\sim 10^{44-49}$ erg/s.
- Jet Component: unknown - leptonic, hadronic, magnetic, ...

FSRQ, LBL
e.g. PKS B1424-418

HBL
e.g. Mrk 421



neutrino production

Dissipation in the jet



Proton acceleration (Diffusive shock acc., stochastic acc., mag. reconn. ...)

see talks by [Asano](#),

[Nalewajko](#)



Interacting with a target photon or another proton



γ-rays and neutrinos

$$p + \gamma(p) \rightarrow \pi + p(n)$$

$$\pi^0 \rightarrow \boxed{\gamma + \gamma}$$

$$\pi^+(\pi^-) \rightarrow \nu_\mu(\bar{\nu}_\mu) + \mu^+(\mu^-) \rightarrow \boxed{\nu_\mu + \bar{\nu}_\mu + \nu_e(\bar{\nu}_e)} + \boxed{e^+(e^-)}$$

They have comparable energy budgets

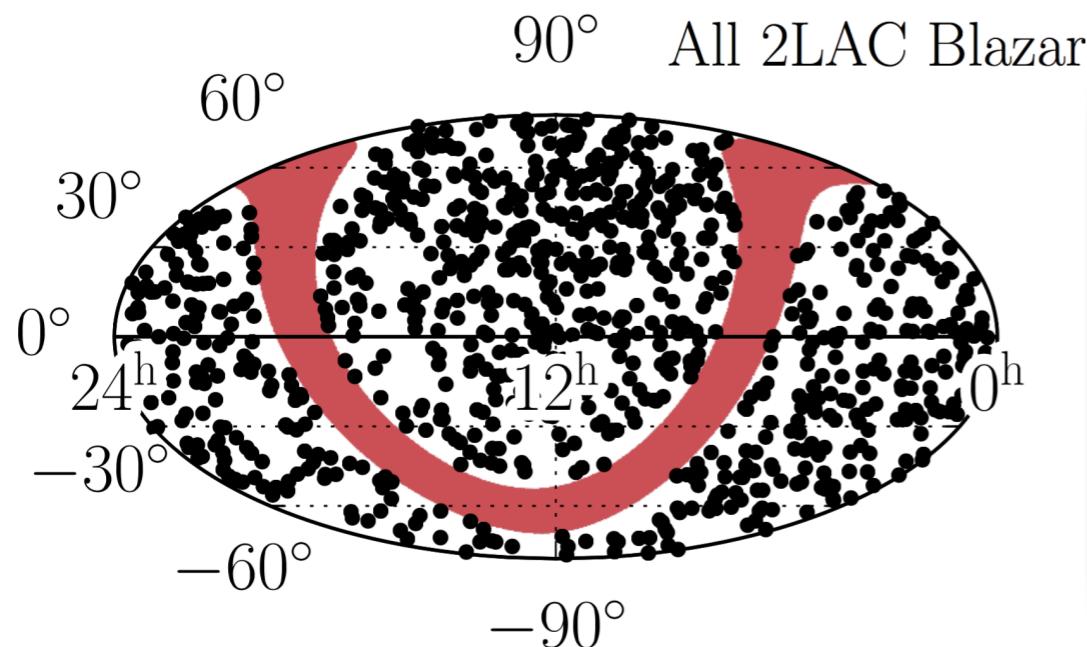
Blazars significantly contribute to EGRB*



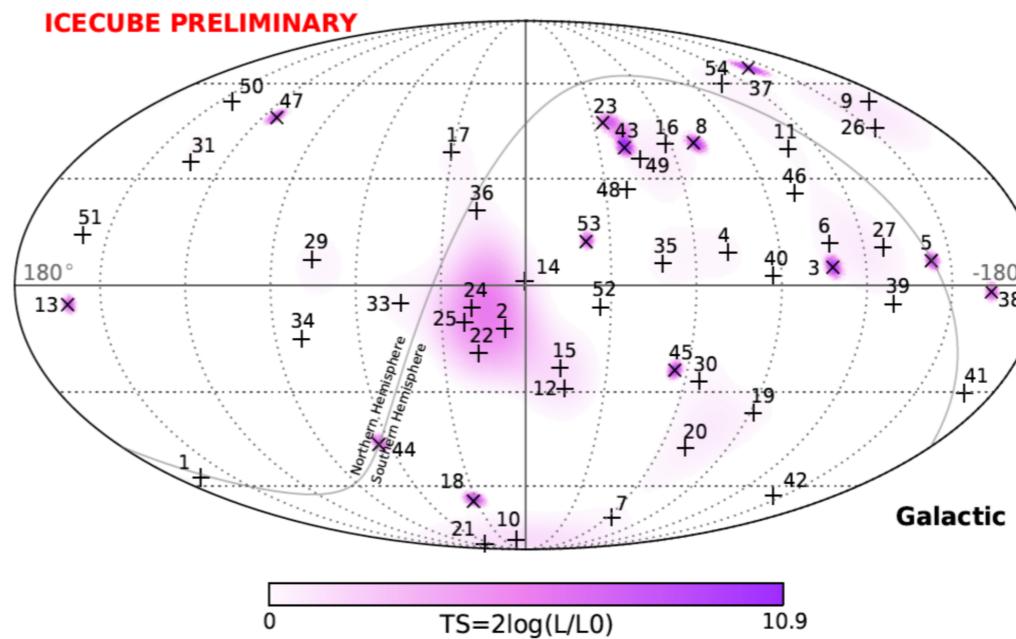
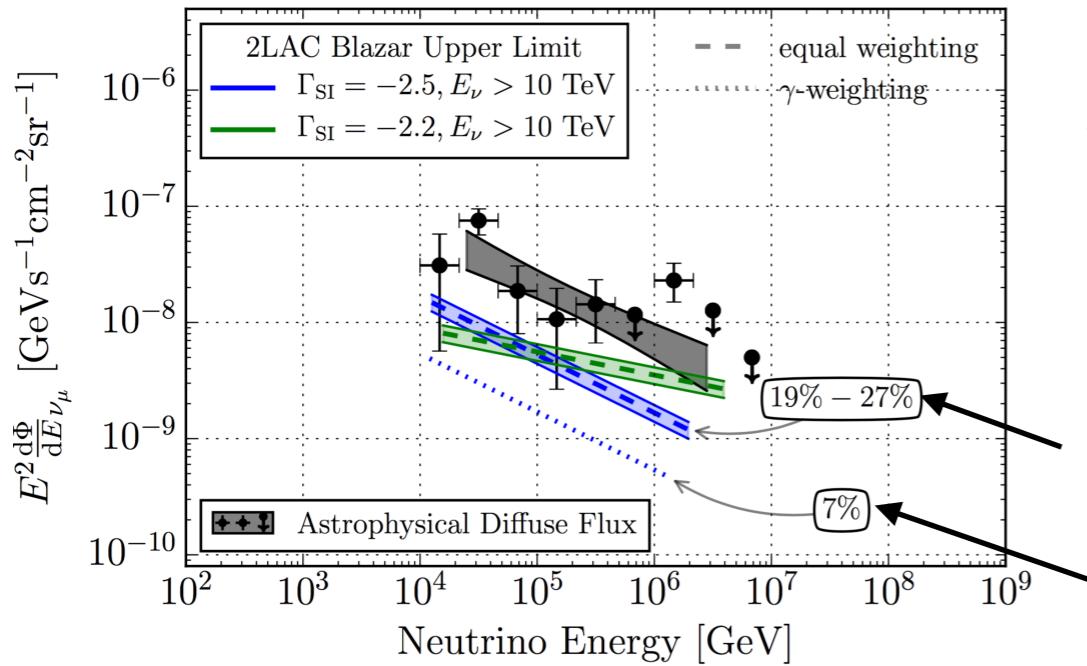
promising candidate as
IceCube neutrino source

*Ajello et al. *Astrophys.JL* 2015

IceCube analysis 2LAC blazars



IceCube collaboration, arXiv: 1611.03874



All 2LAC blazars (862 objects, FSRQ,LBL,IBL,HBL)

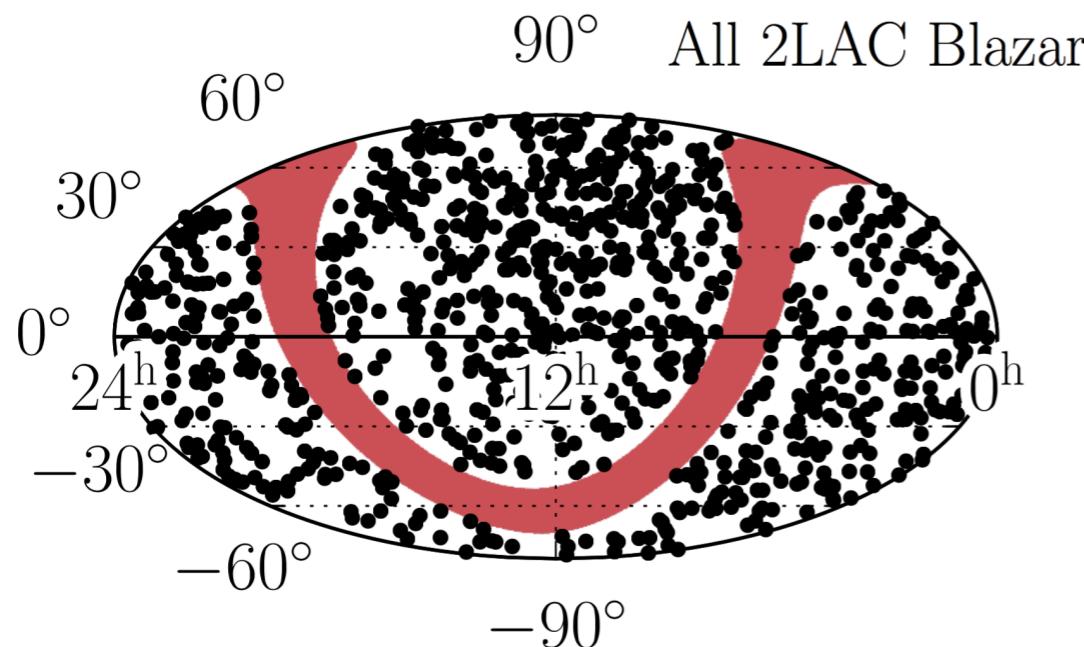
equal weighting

γ -weighting

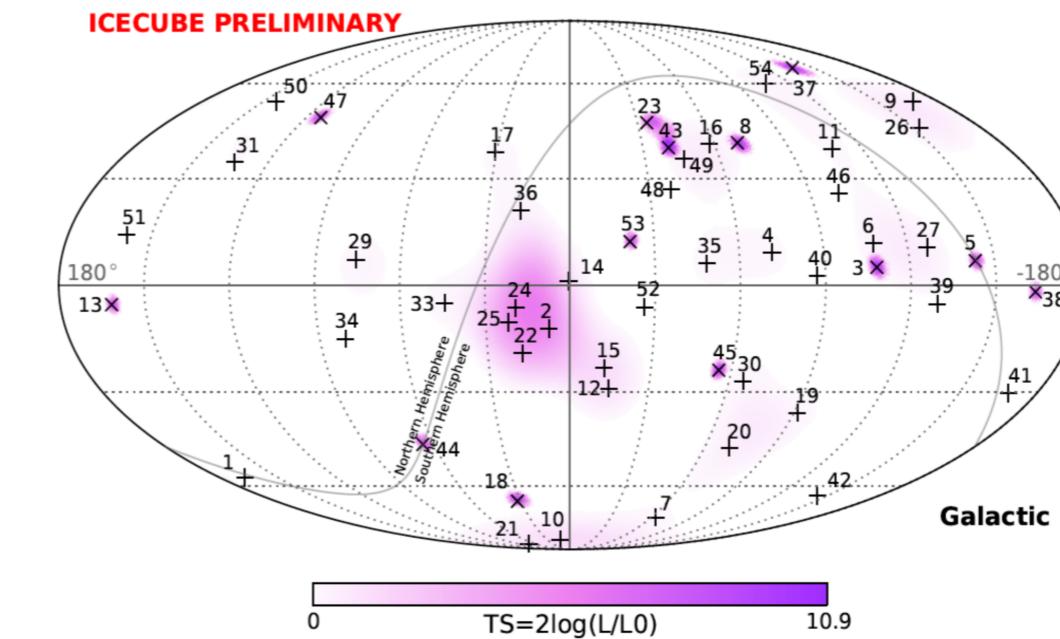
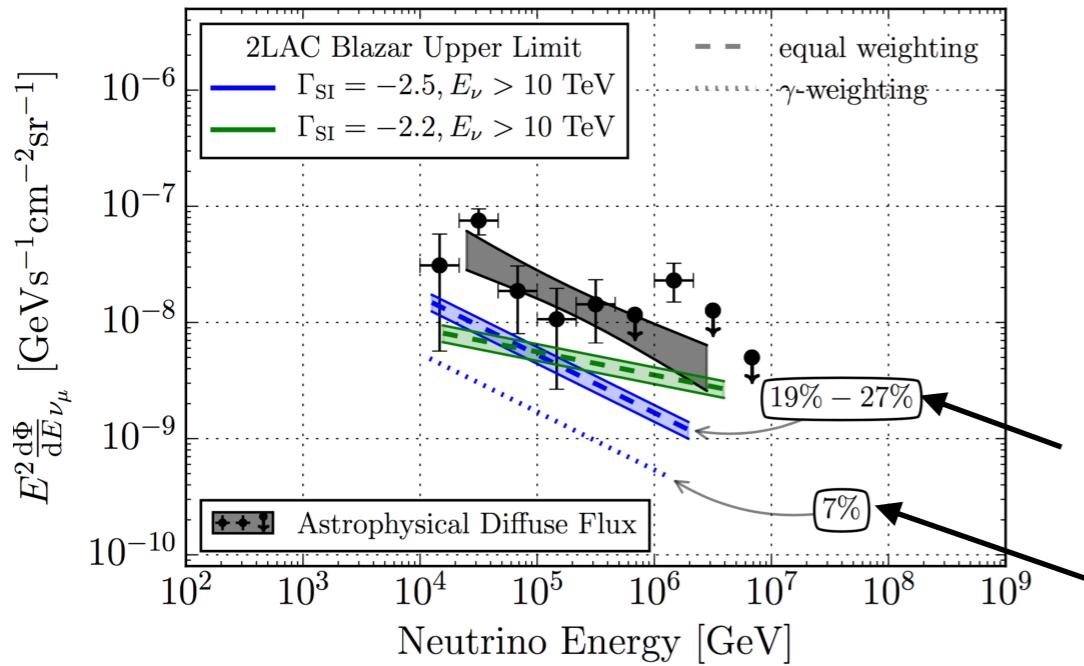
γ -weighting: $L_\nu = L_\gamma$ for each source

equal weighting: dN/dS follows the same as γ -rays; No correlation for individual source

IceCube analysis 2LAC blazars



IceCube collaboration, arXiv: 1611.03874



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γ -weighting

$L_{\nu} \sim L_{\gamma}$ relation is crucial for any kind of analysis

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No. of para. & No. of data points

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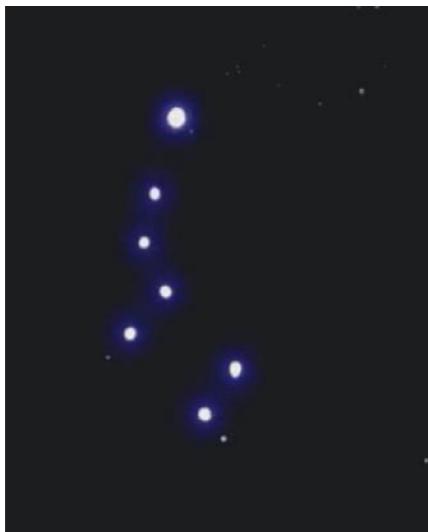
	Group	Symbol	Definition
Parameters	Global	R'_{blob}	Comoving radius of blob, fixed to 7.5×10^{17} cm
		f_{esc}	e^\pm and p escape fraction, fixed to 1/10
		Γ_{bulk}	bulk Lorentz factor of the blob fixed to 35
	Leptonic	B'	Magnetic field strength, blob frame
		$L_{e,\text{inj}}$	Injection luminosity of primary e^- , AGN frame
		$\gamma'_{e,\text{min}}$	Minimum Lorentz factor of primary e^- , blob frame
		$\gamma'_{e,\text{max}}$	Maximum Lorentz factor of primary e^- , blob frame
		$\alpha'_{e,\text{idx}}$	Power law index of injected primary e^-
	Hadronic	$\alpha'_{p,\text{idx}}$	Power law index of injected protons, fixed to -2.0
		η_b	Luminosity ratio p to e^- at injection, <i>i.e.</i> , $\eta_b \equiv L_{p,\text{inj}}/L_{e,\text{inj}}$
		$E_{p,\text{max}}^{\text{ob}}$	Maximal energy of injected protons, observer frame

big blazar parameter table for the simplest hadronic model :
one-zone + single power-law injections

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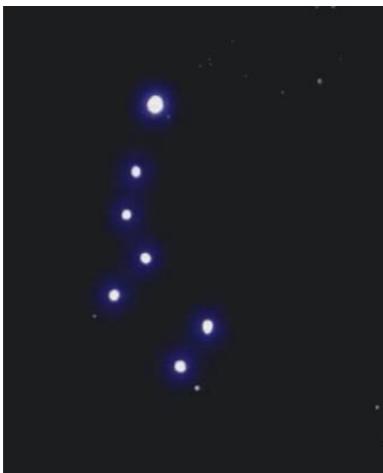
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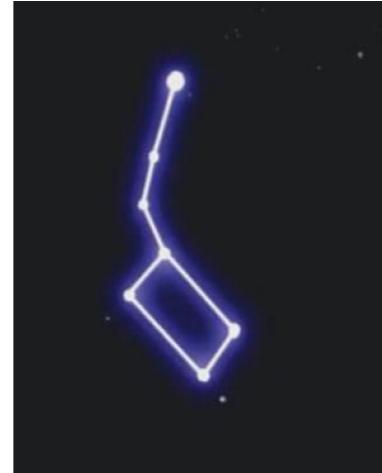
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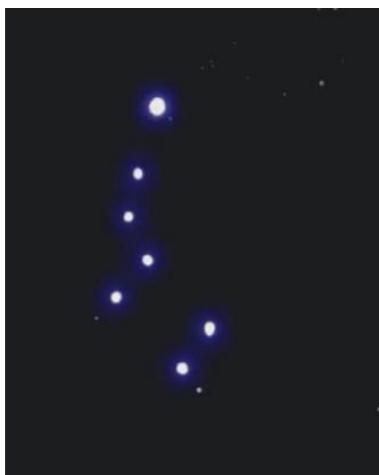
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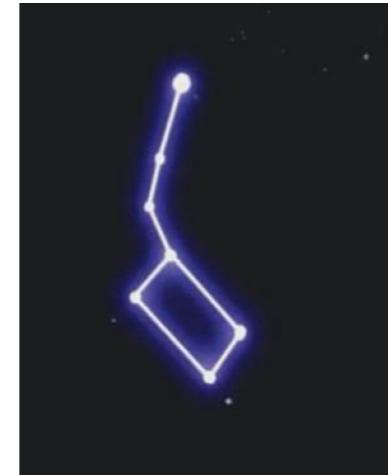
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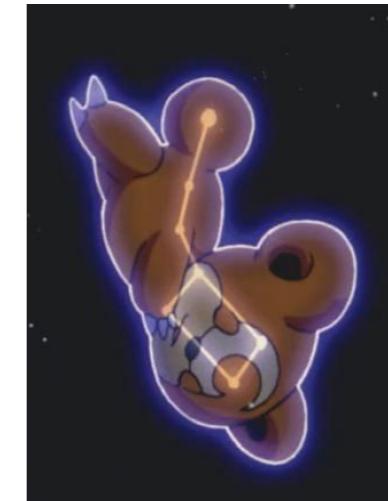
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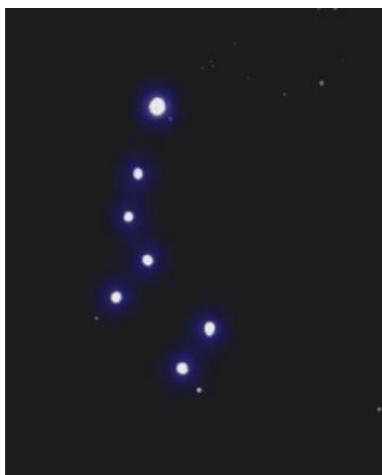
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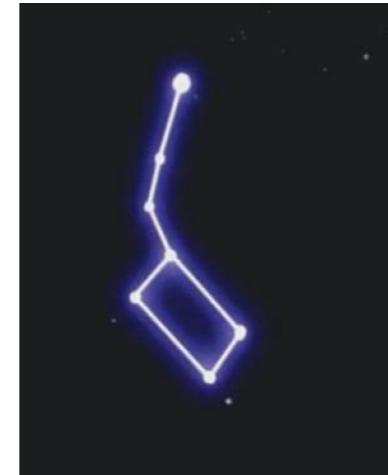
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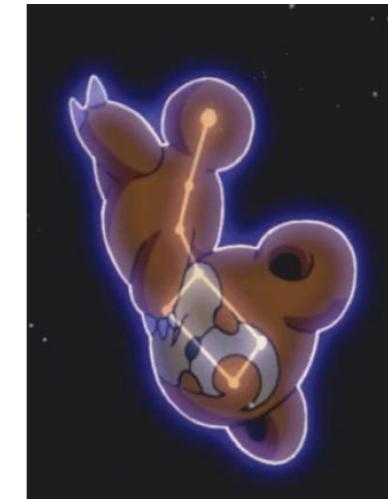
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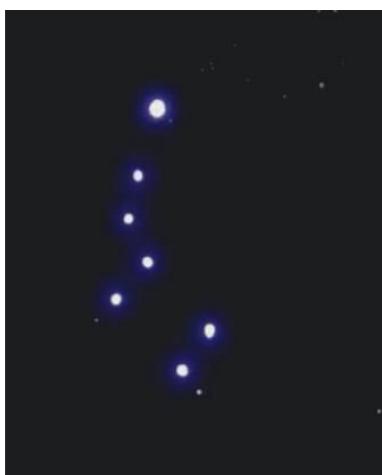
data (e.g. ν)



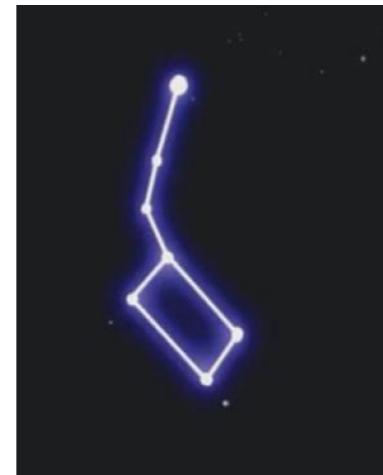
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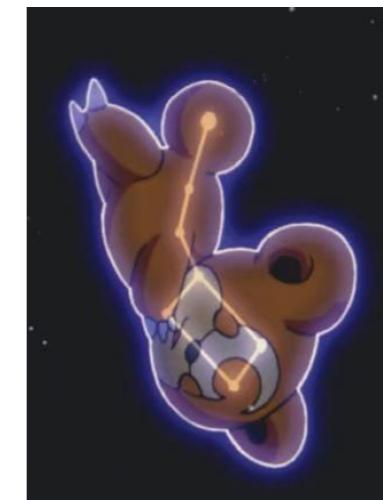
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besides, there are other novel observables:

- time series — PSD , PDF ... See 8 talks presented in “variability” section
- polarization See talk by [Böttcher](#)
- ...

model & methods

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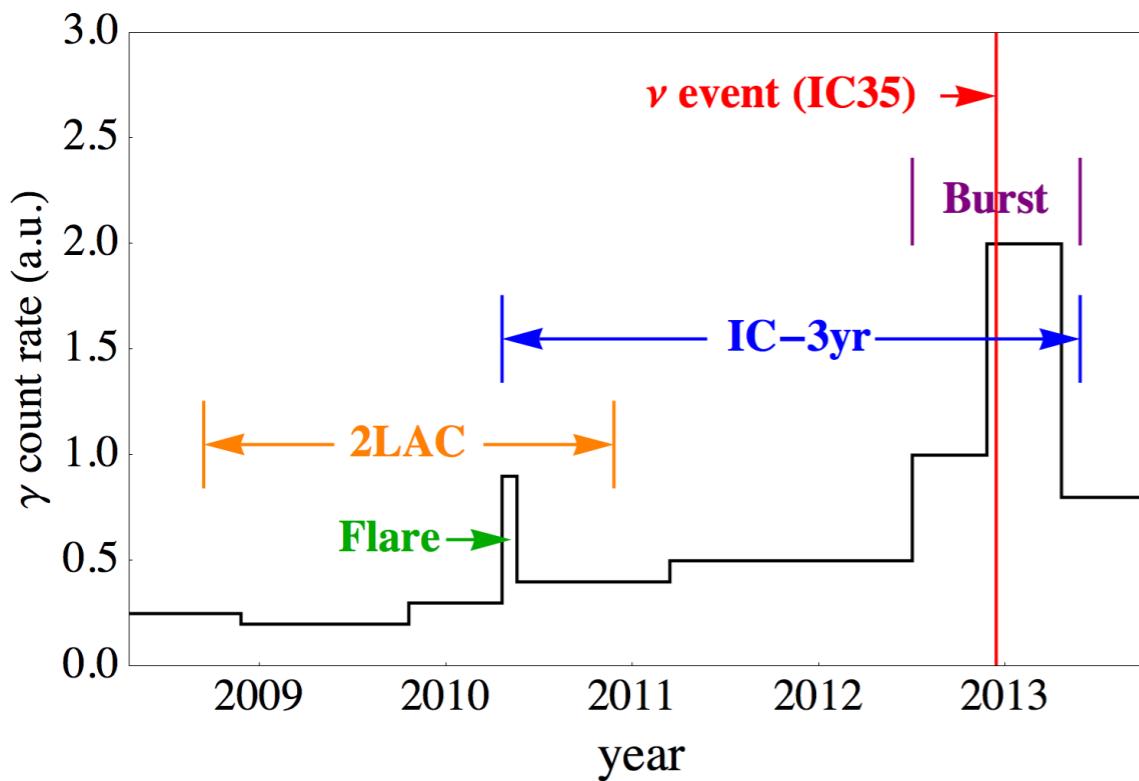
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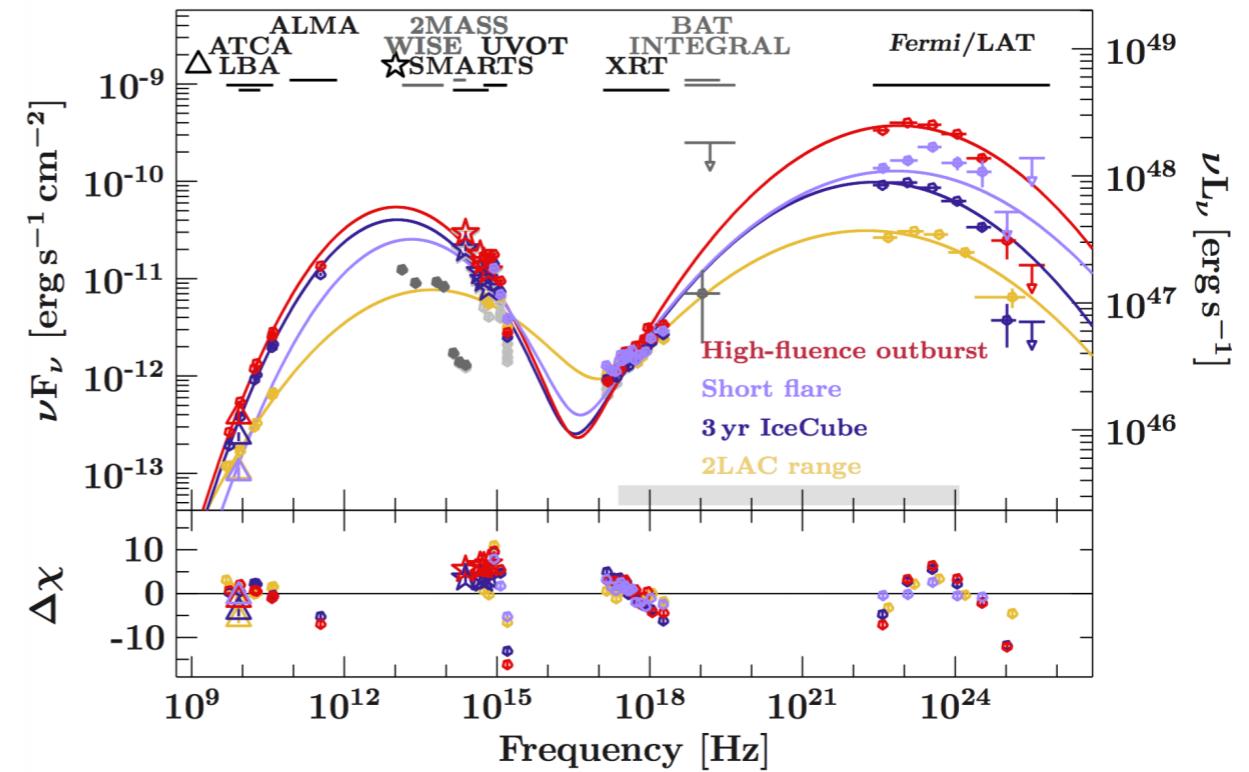
t-dependent, full particle interactions
(syn + IC + pg + BH ...), coupled
diff-int Fokk-Plk eqn., and efficiency

PKS B1424 418

$z=1.522$ FSRQ



SG,Pohl,Winter arxiv:1610.05306



Kadler et al. NatPhys 2016

- Positional and temporal correlation with “big-bird” event (IC35, 2PeV)
- Sufficient energy in γ -rays → if all converted to ν → multiple events
- Low background coincidence probability

for PKS B1424 418

	1st peak (eV-keV)	middle range	2nd peak (MeV-TeV)	Example
Pure Leptonic	L primary e-syn	L Synchrotron-Self Compton (ssc)	L SSC or External-IC	can explain most blazars
LH-SSC	L primary e-syn	H secondary lep emission	L SSC	PKS B1424-418
LHπ	L primary e-syn	H secondary lep emission	H π^0 decay or secondary lep	Mrk 421
LHs	L primary e-syn	H secondary lep emission	H proton syn	3C 279
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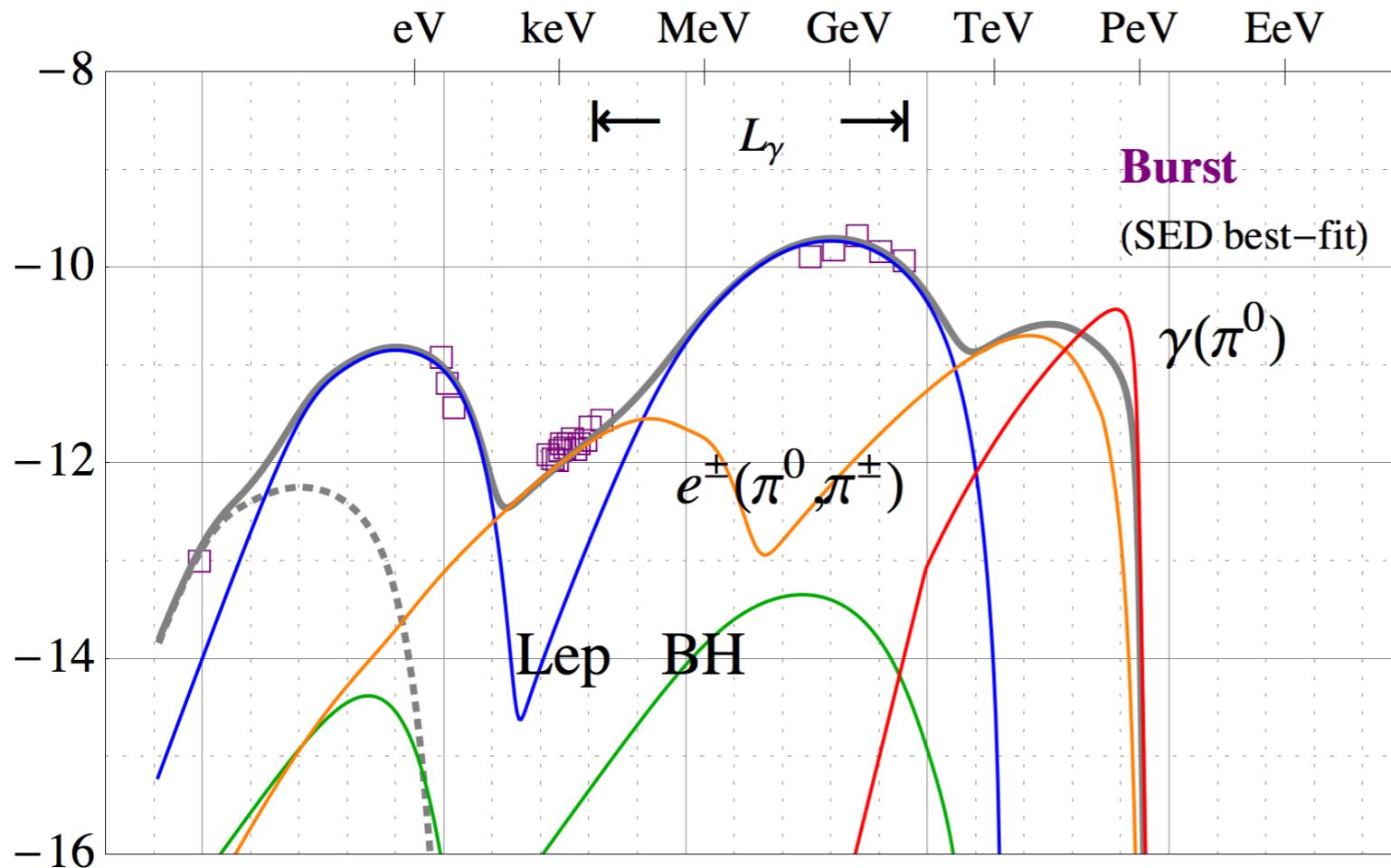
Analytical calculation: E_{peak} , L_{peak} , E_v must be consistent with observation; BH, psyn not overshooting SED, etc.

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Components of the SED

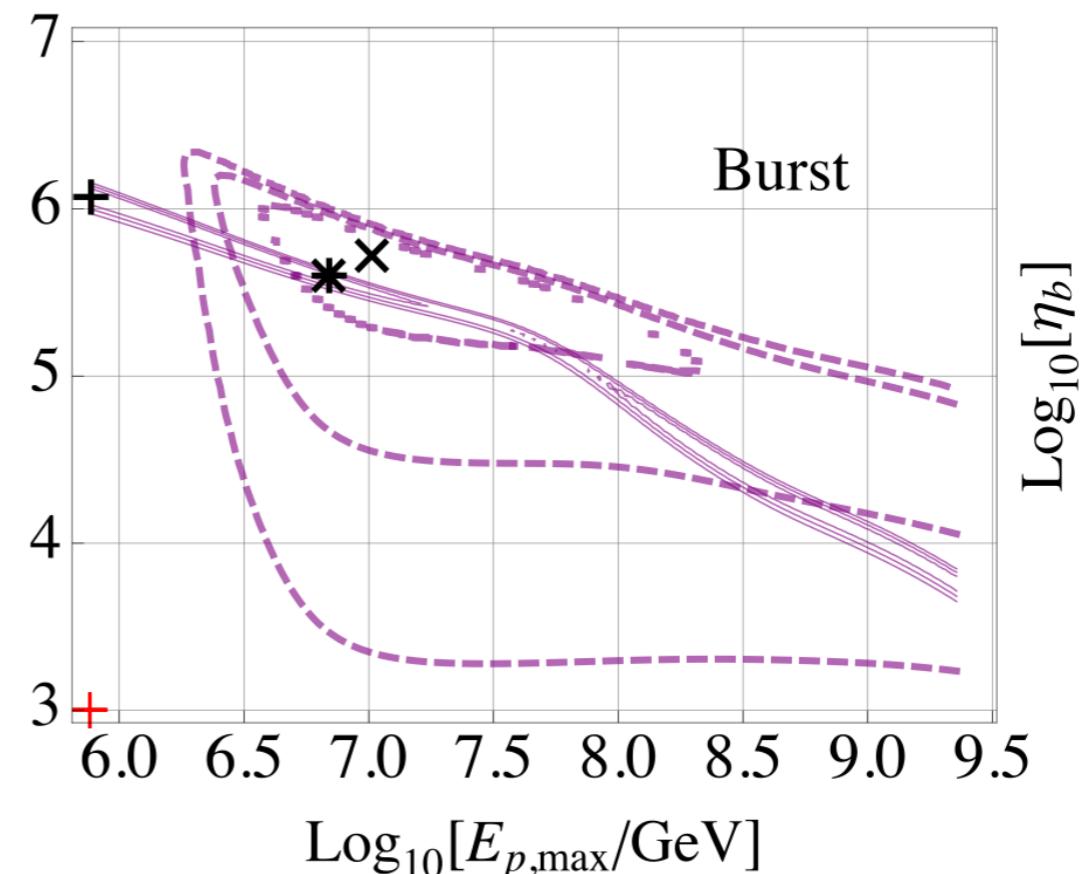
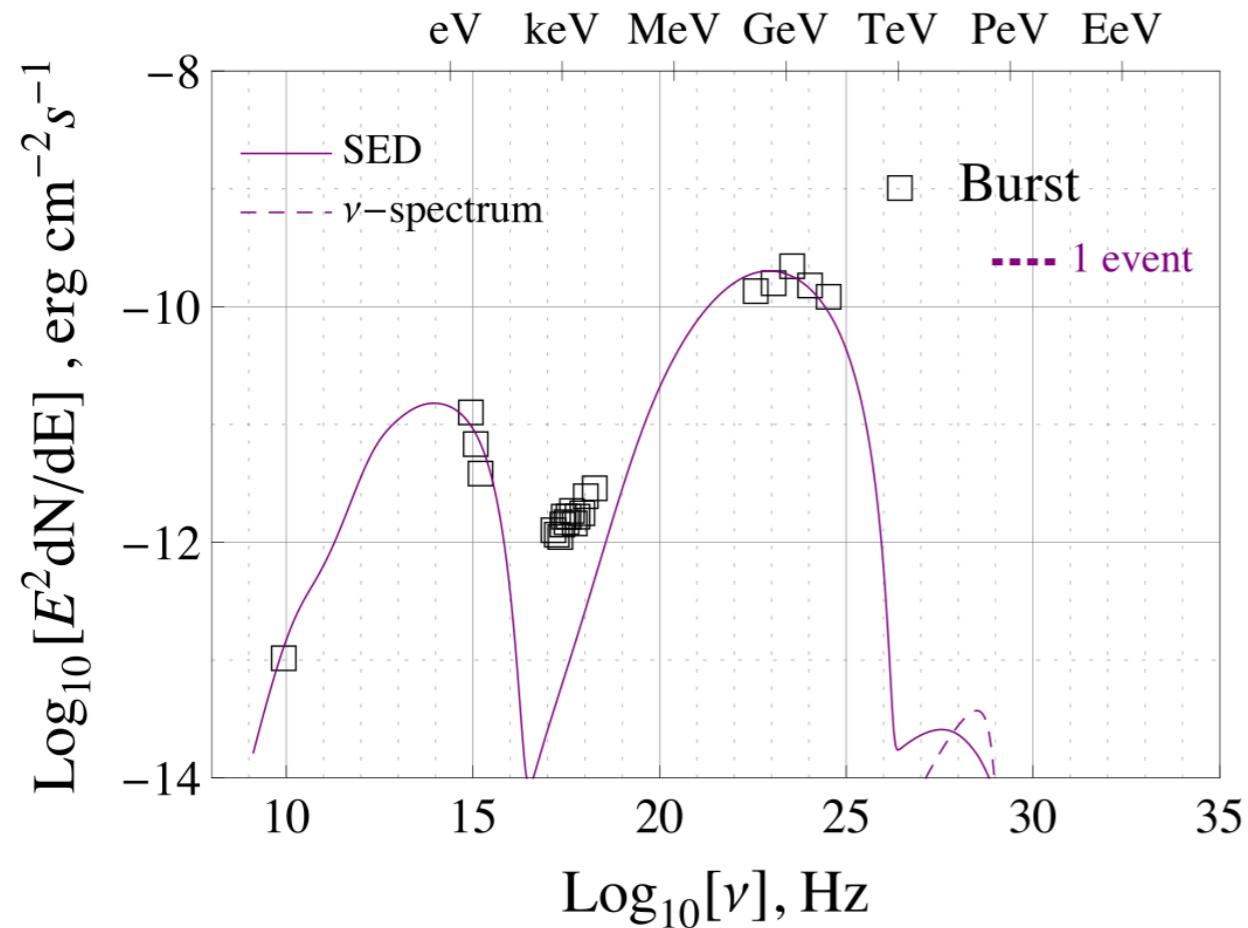


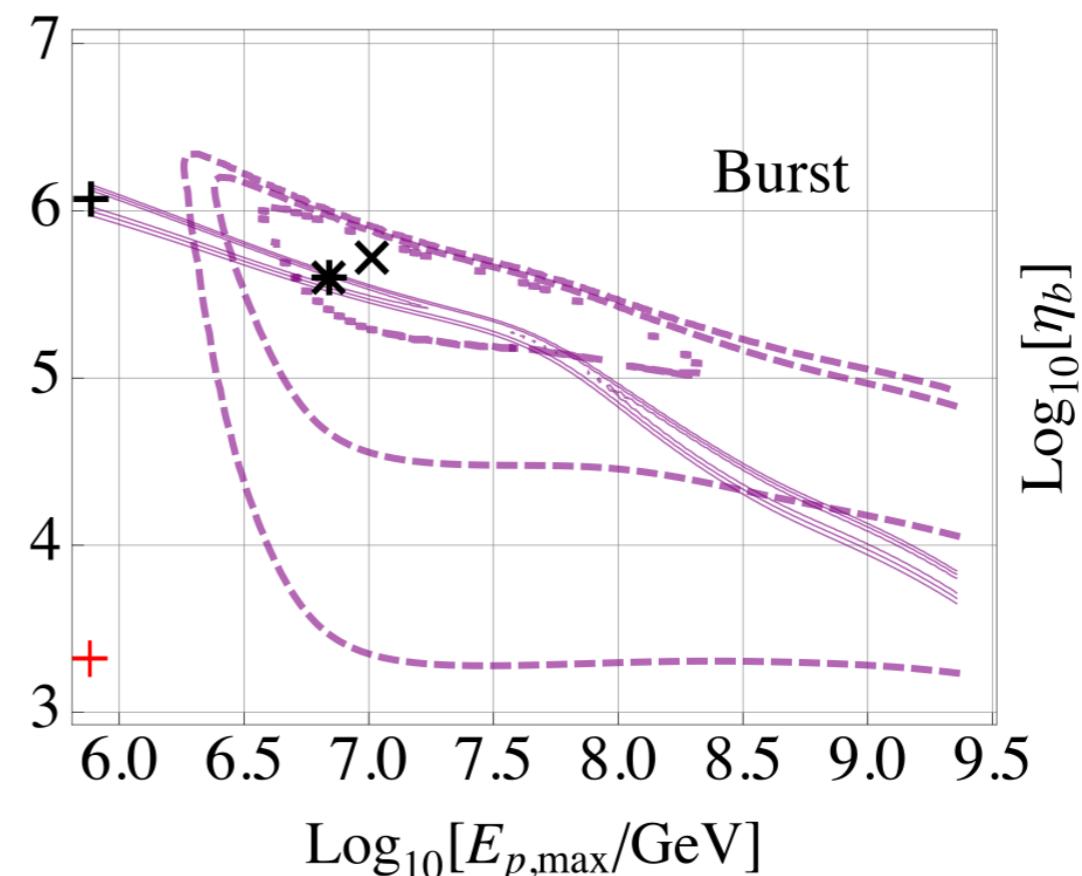
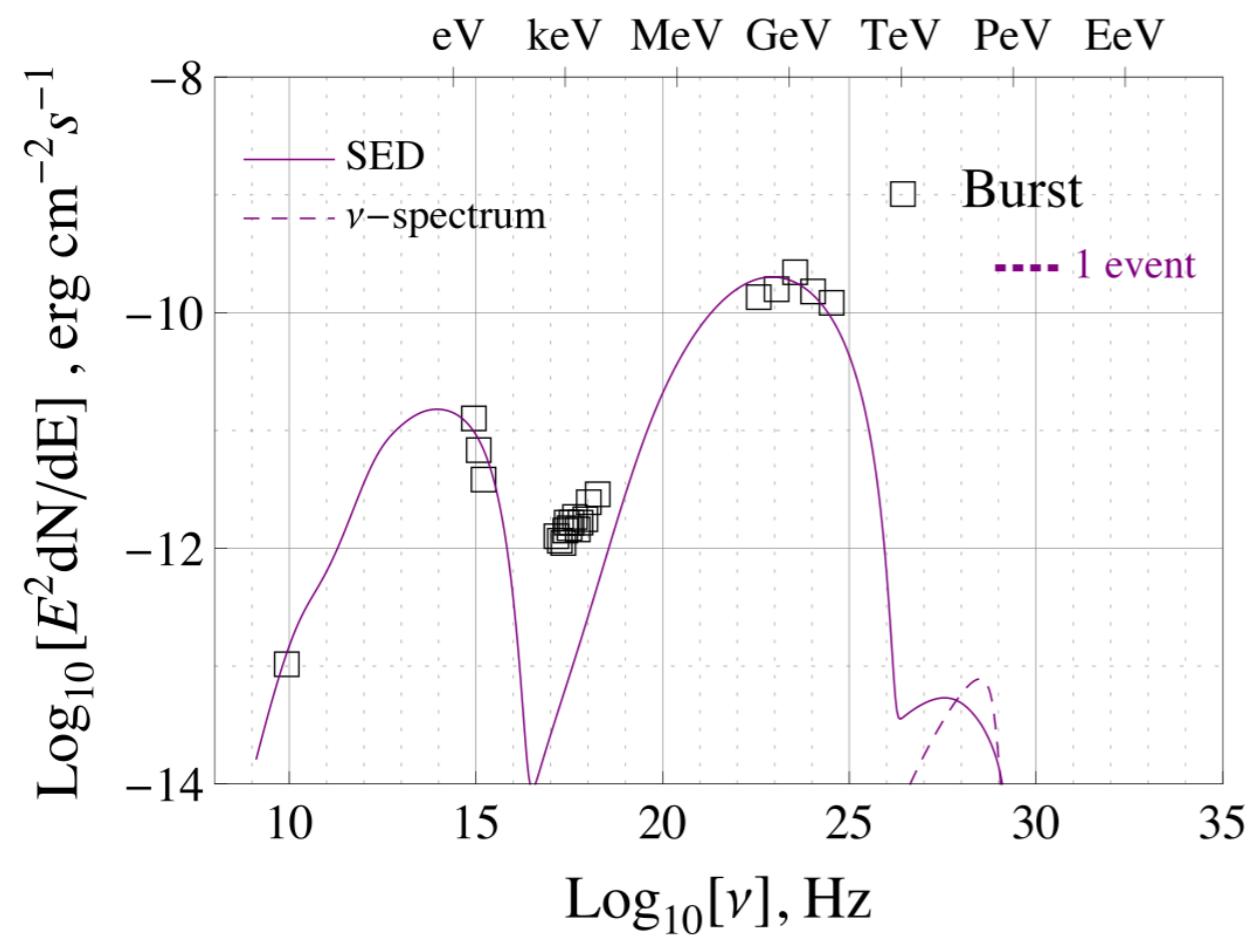
Hadronic X-rays

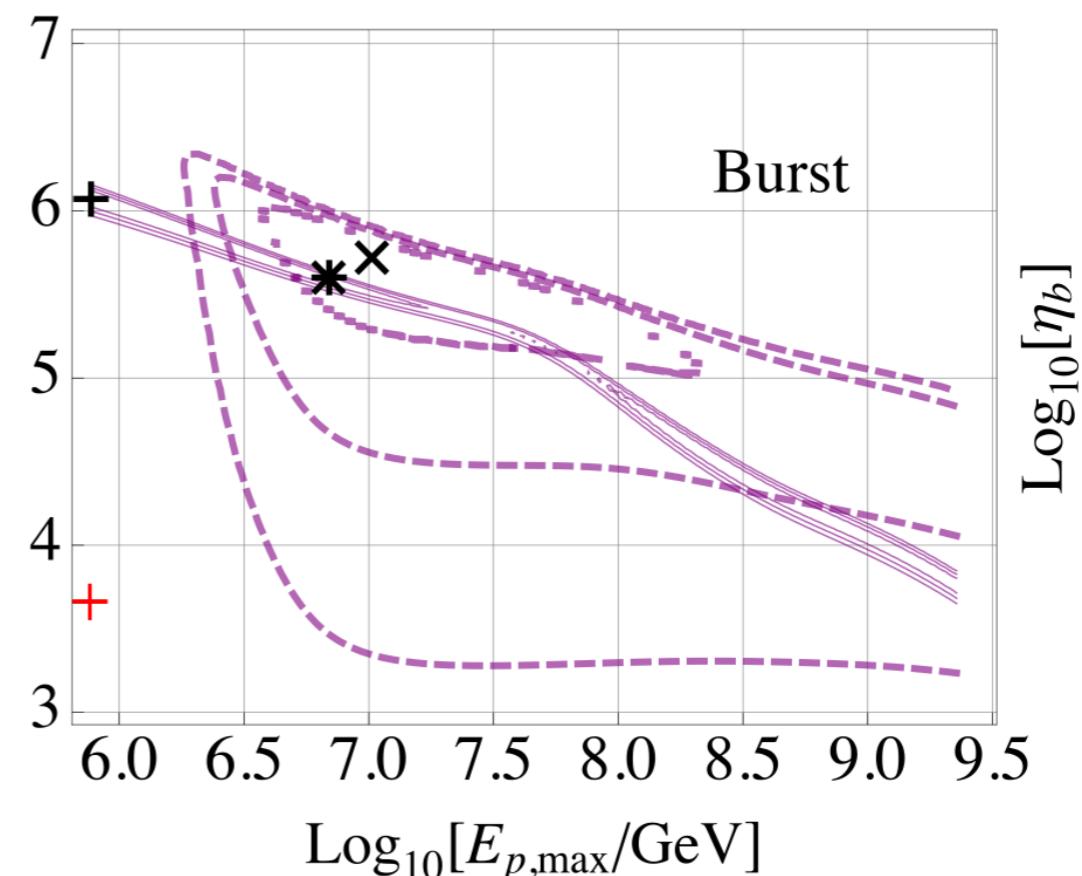
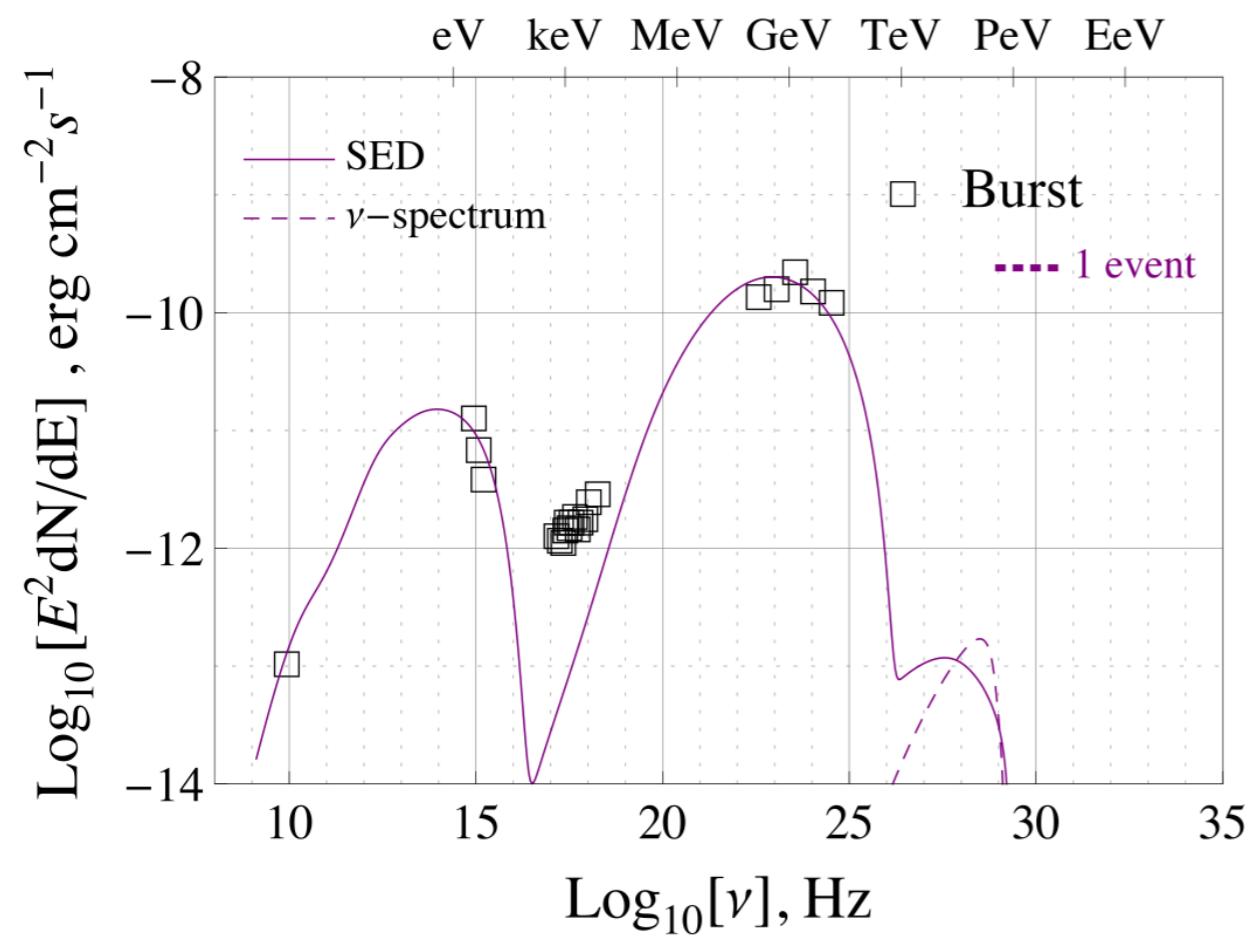
SG,Pohl,Winter arxiv:1610.05306

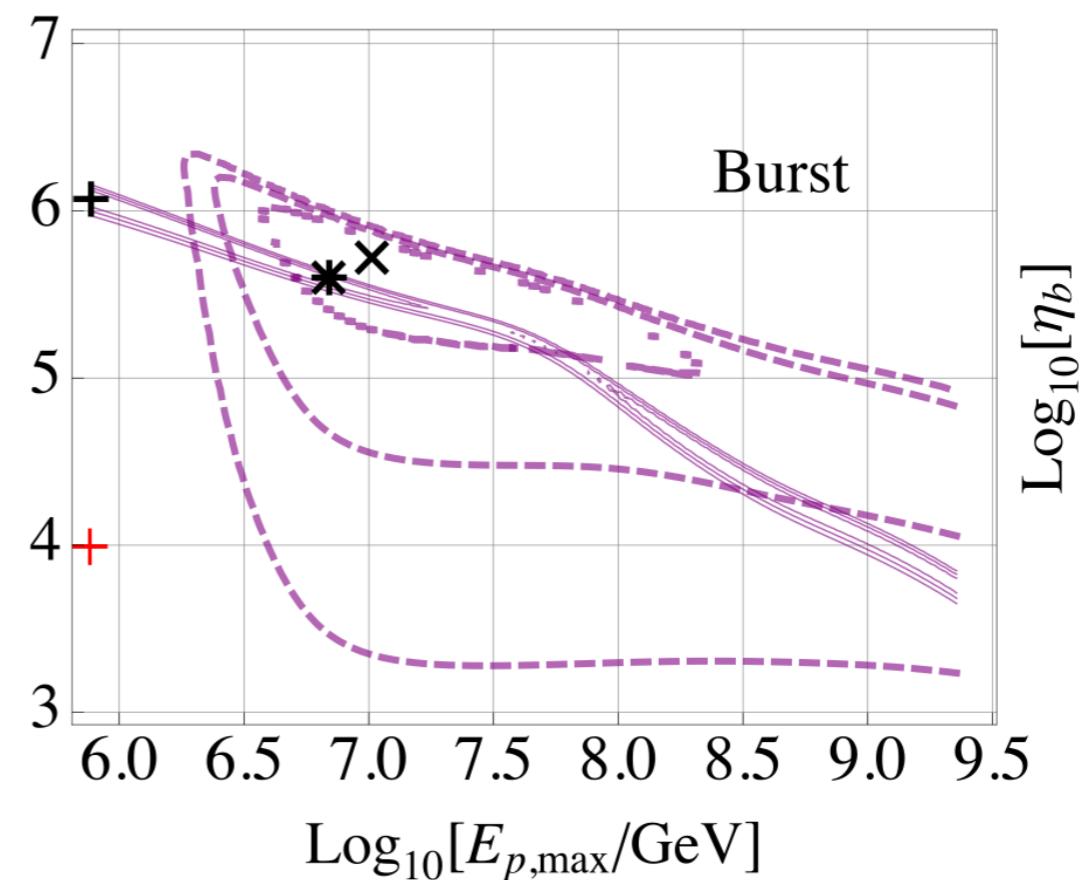
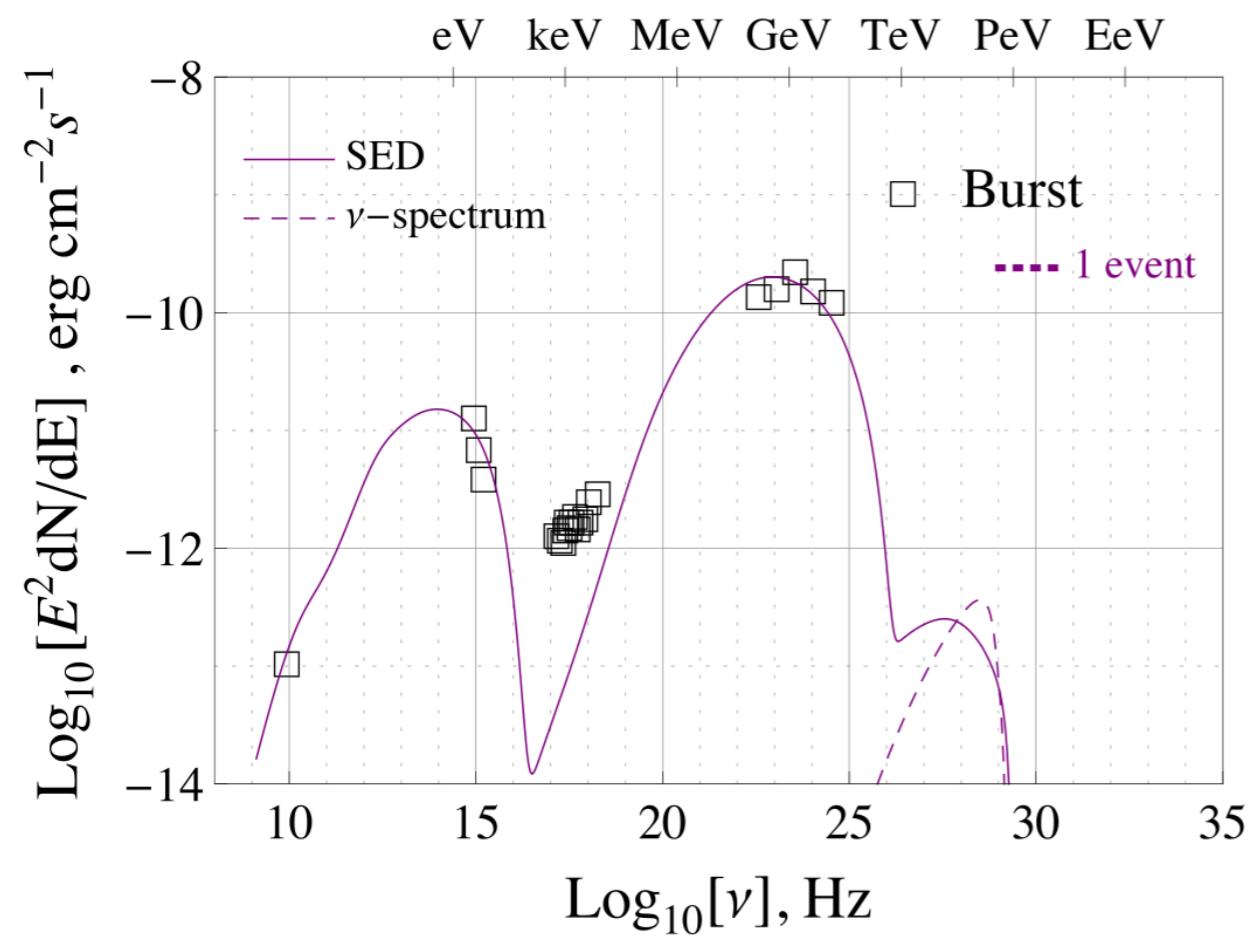
Suggesting $L_{\nu} \neq L_{\gamma}$

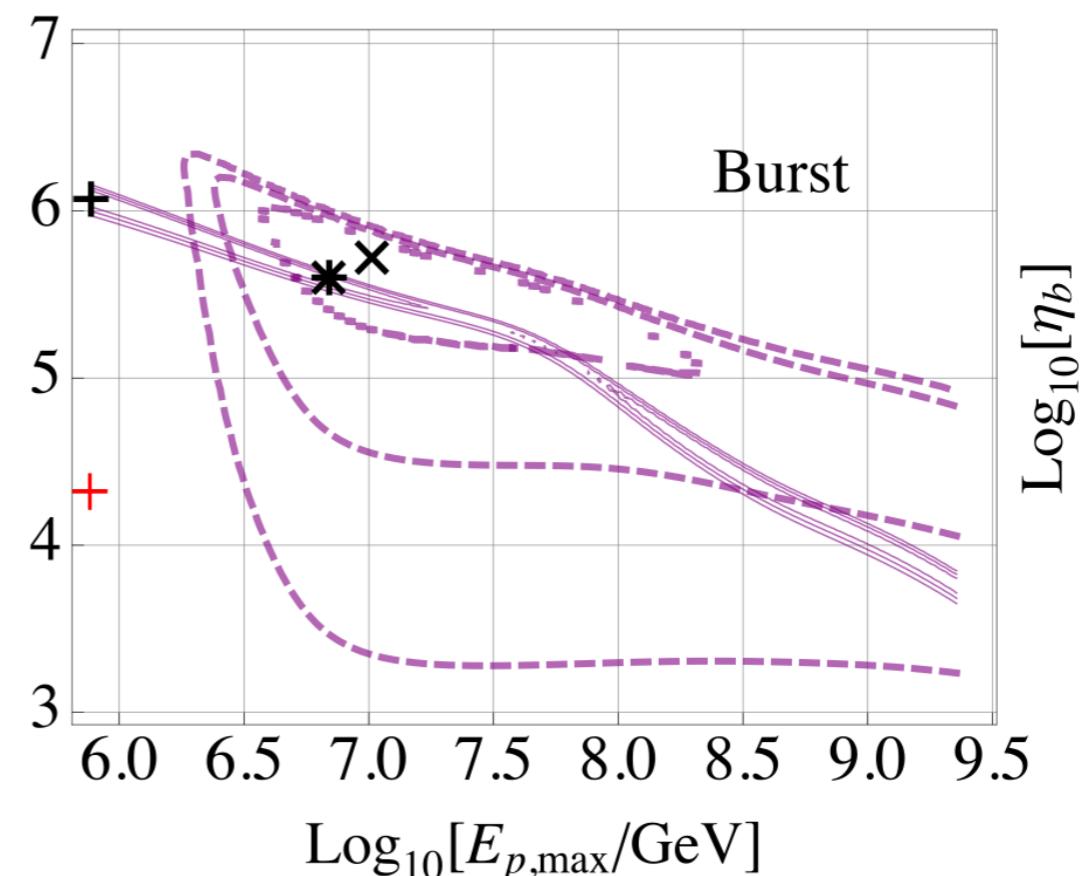
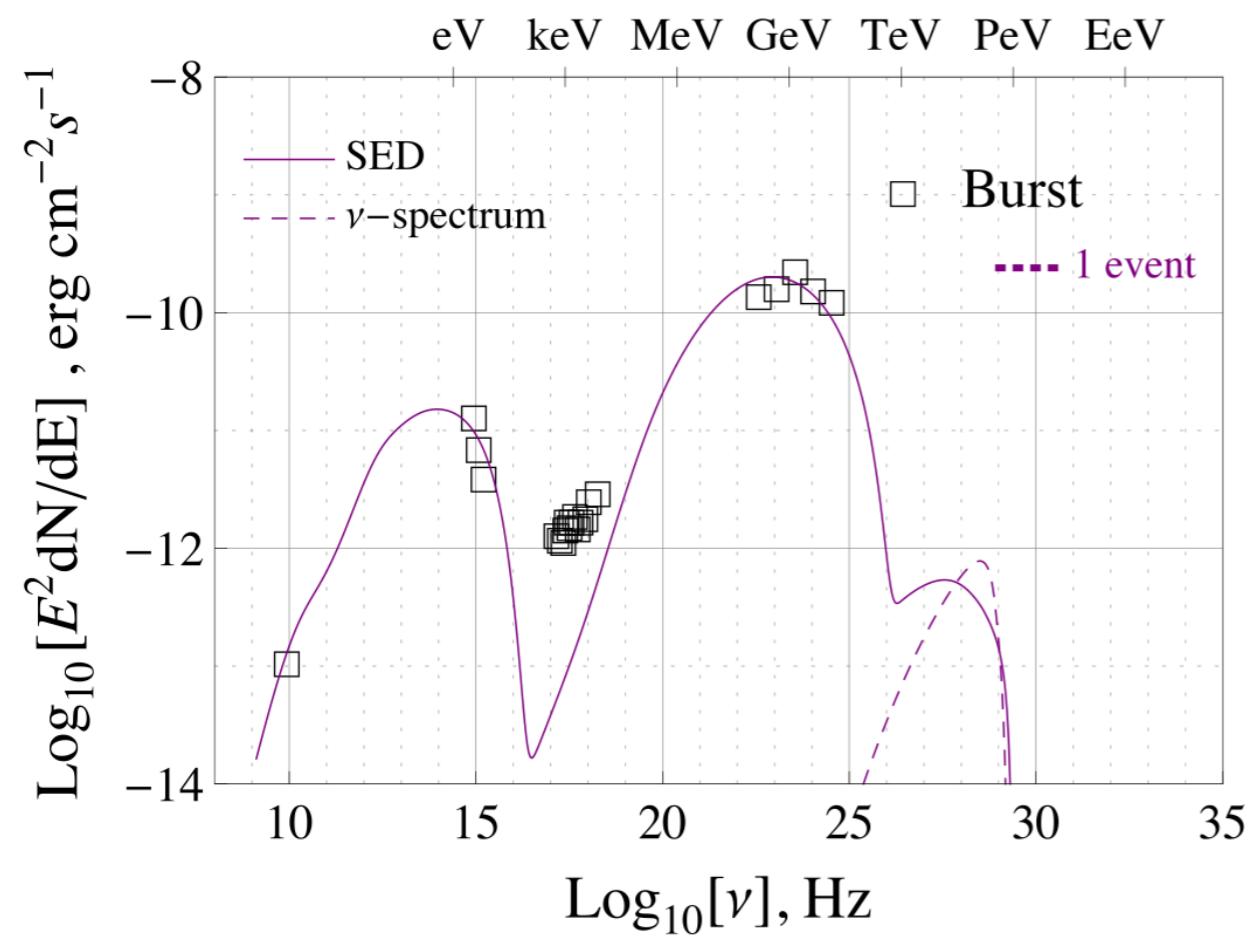
parameter space scan

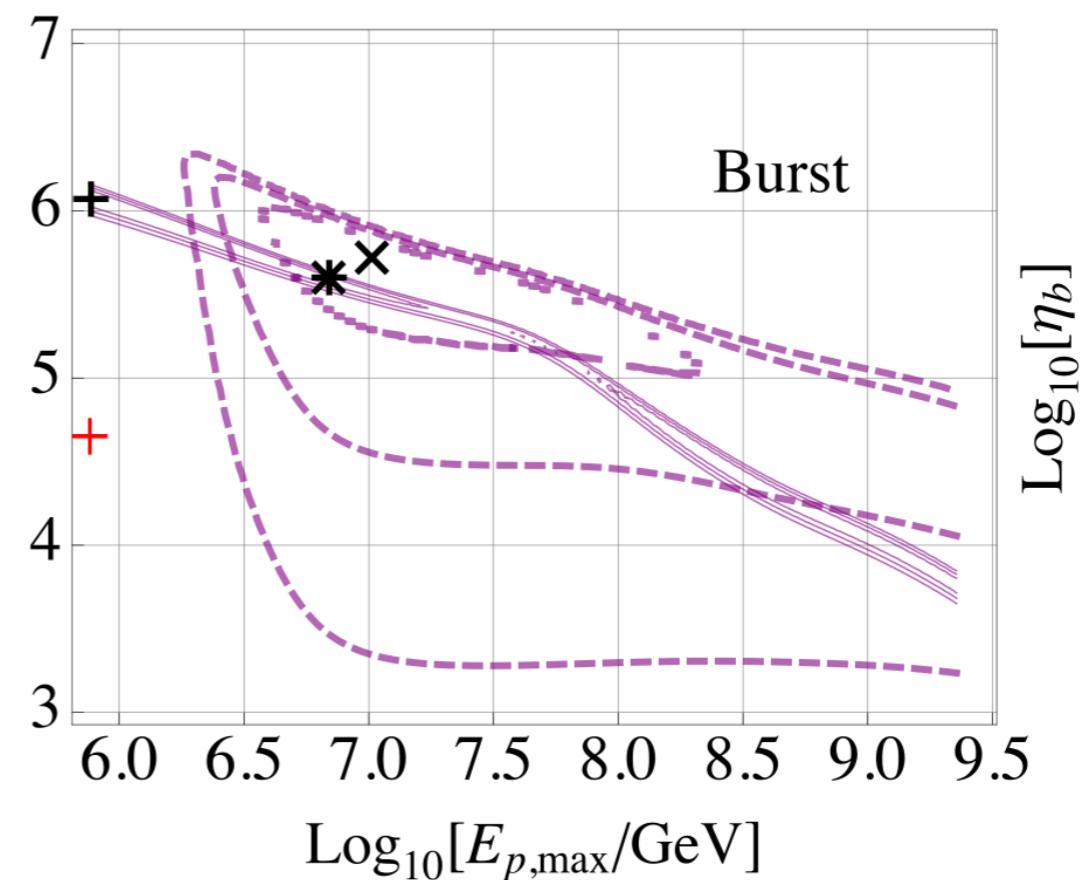
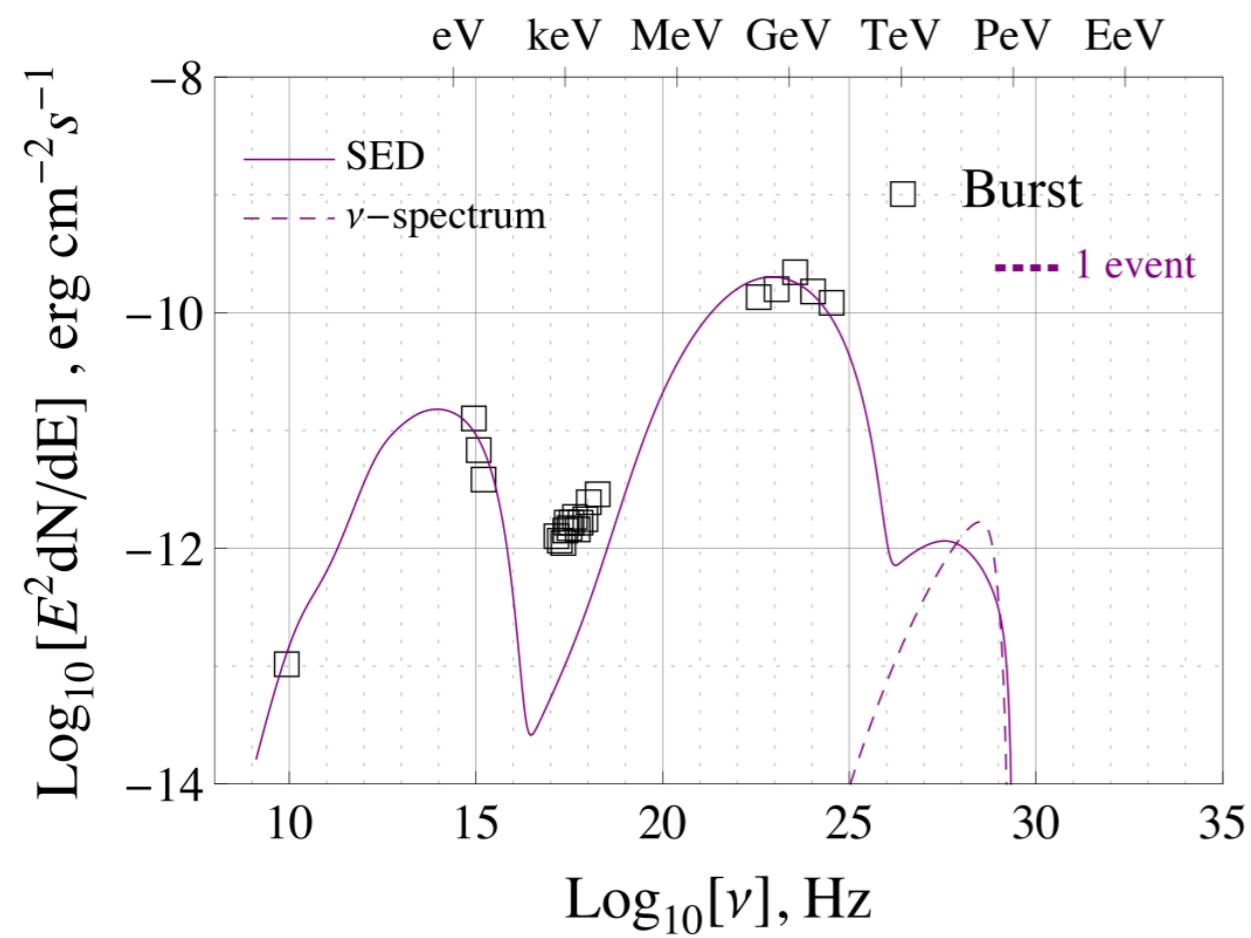


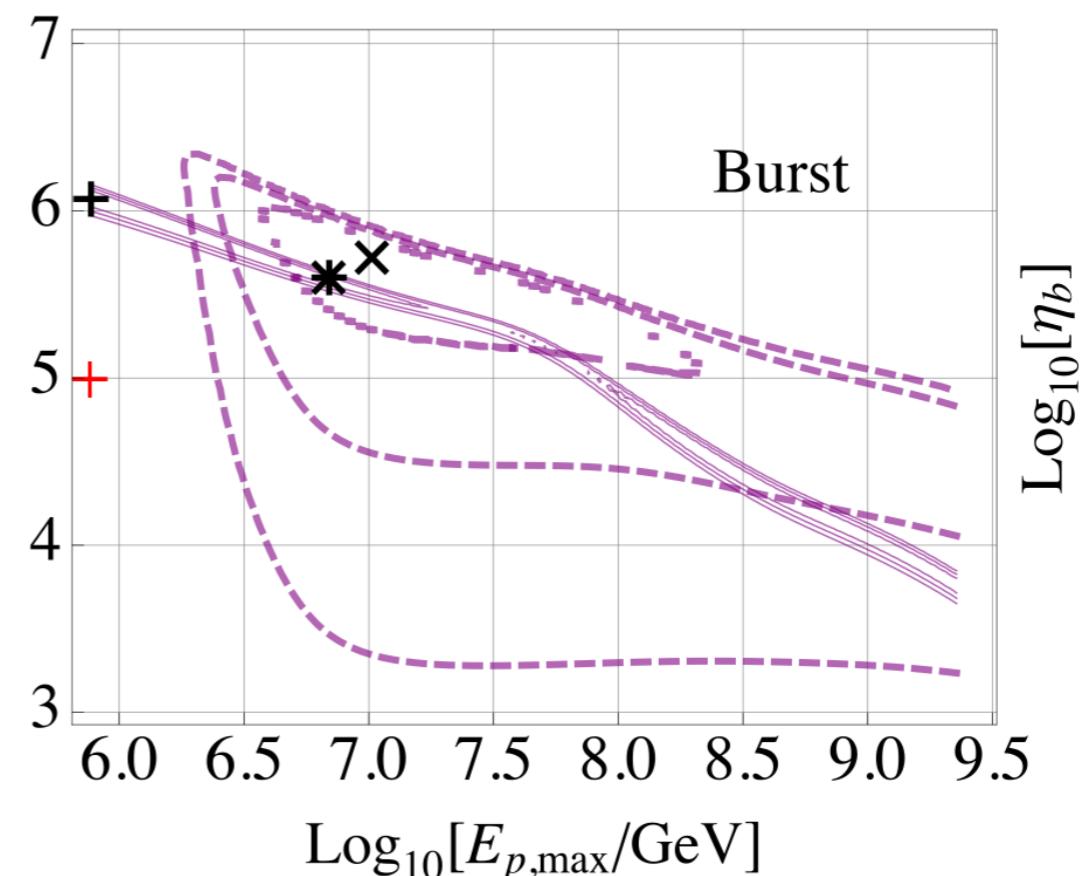
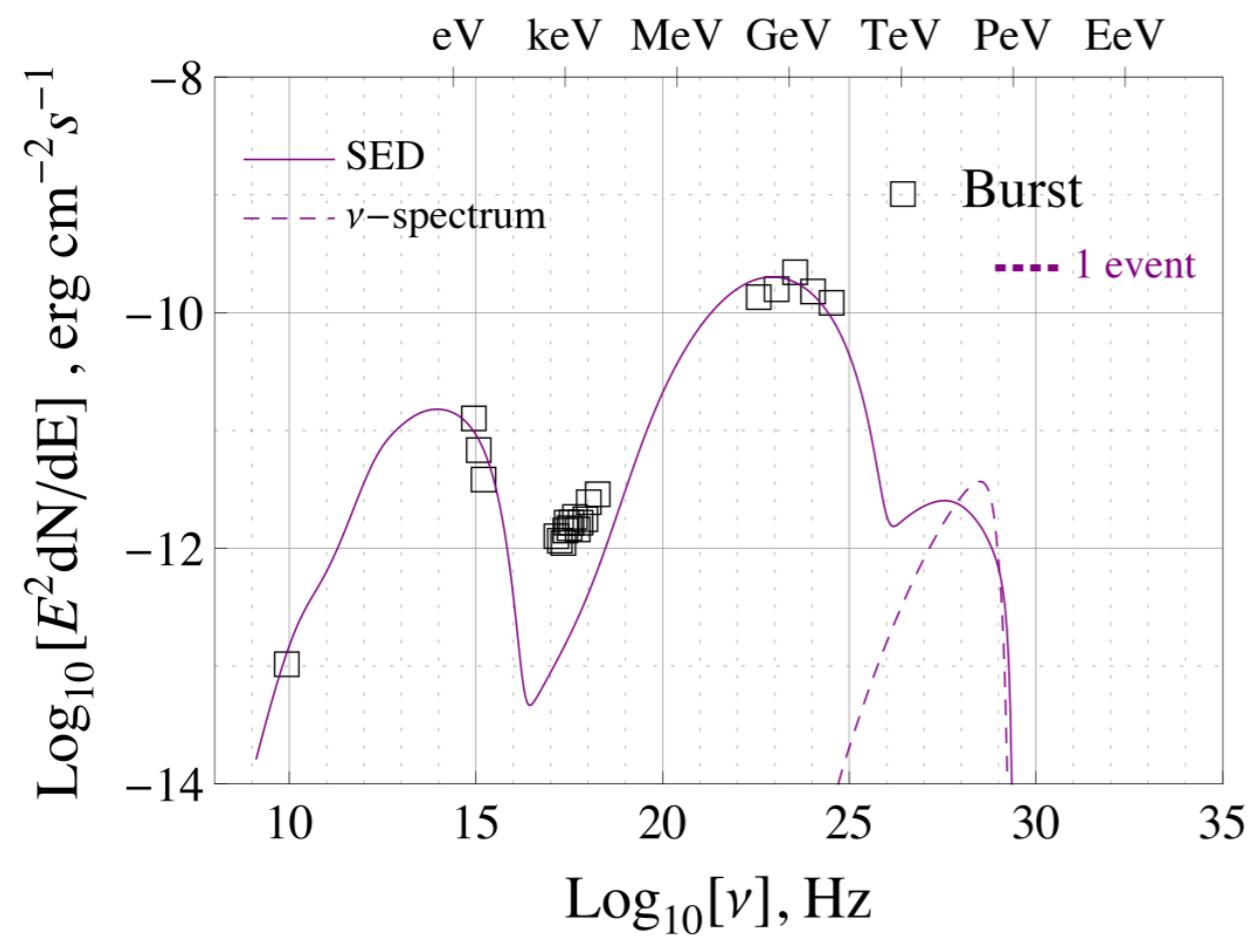


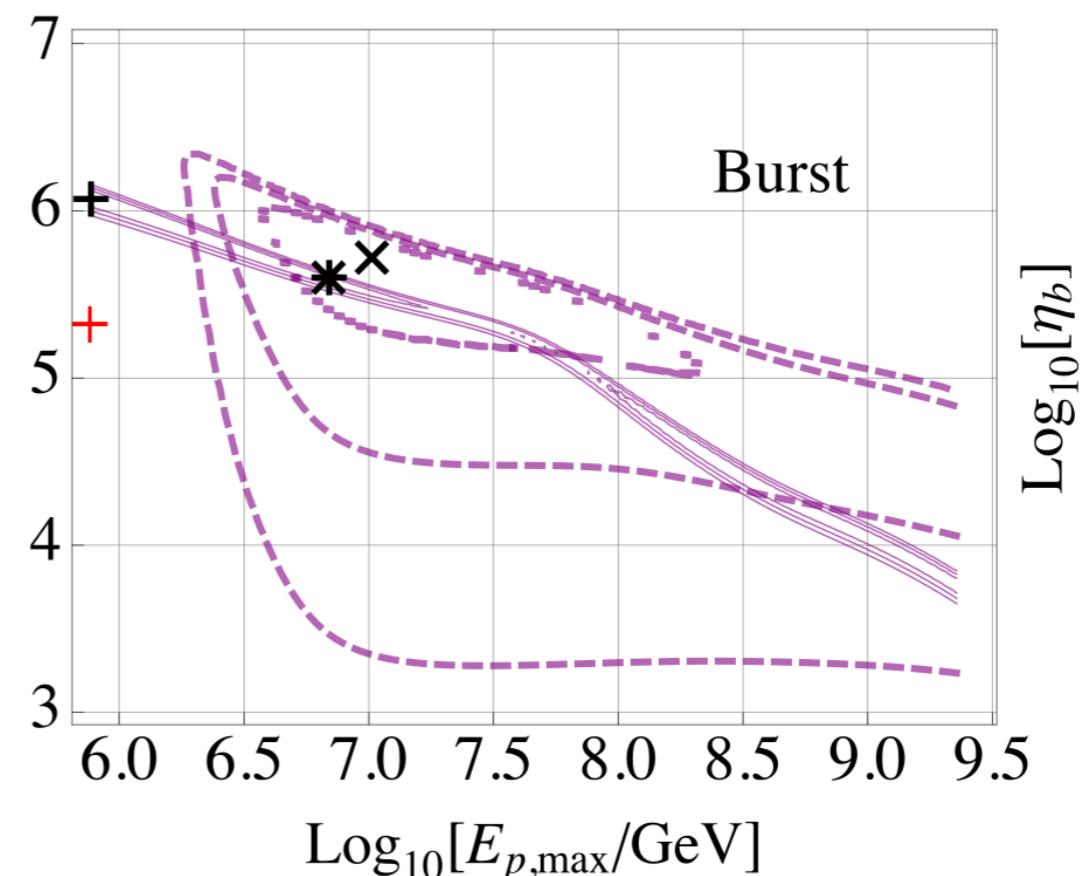
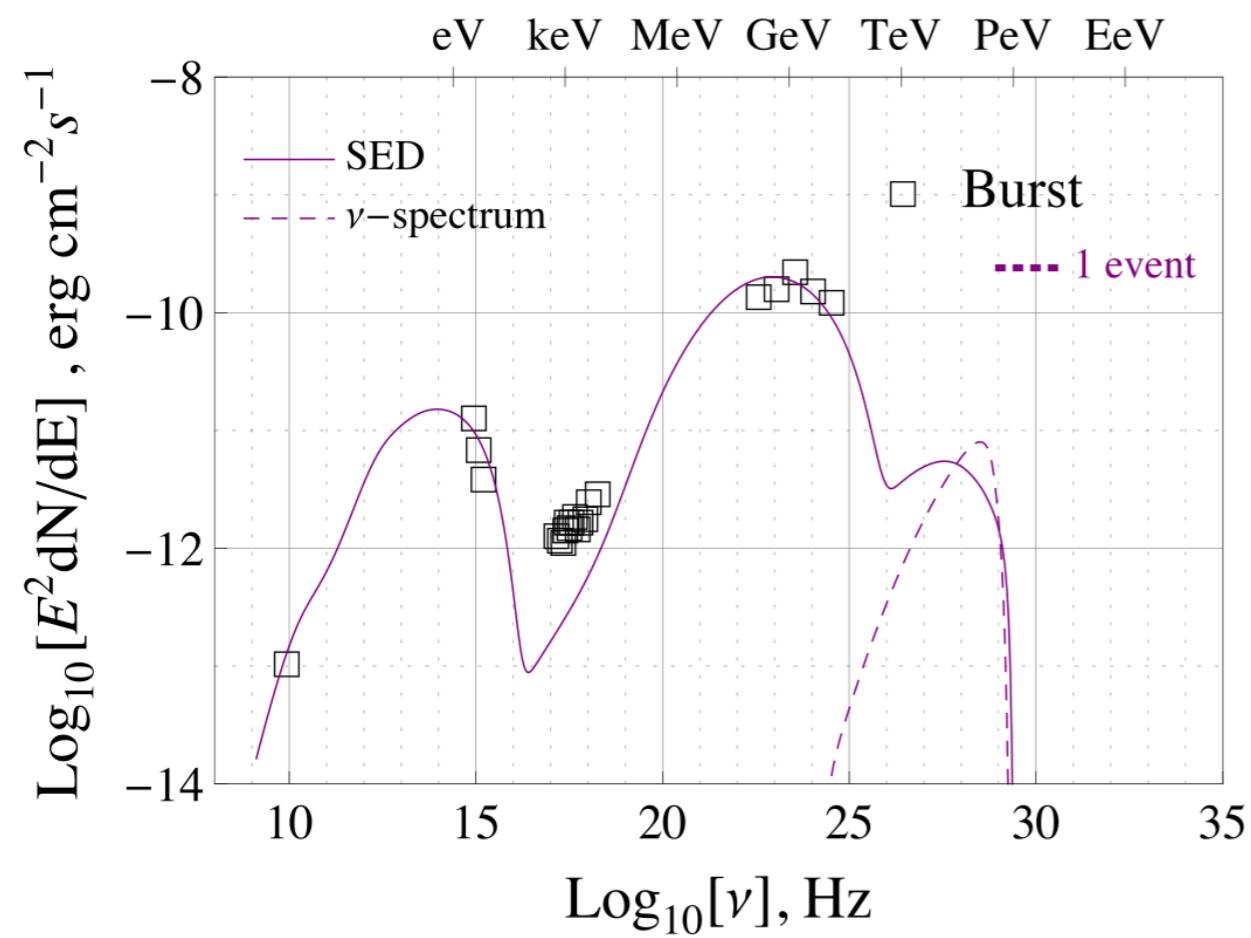


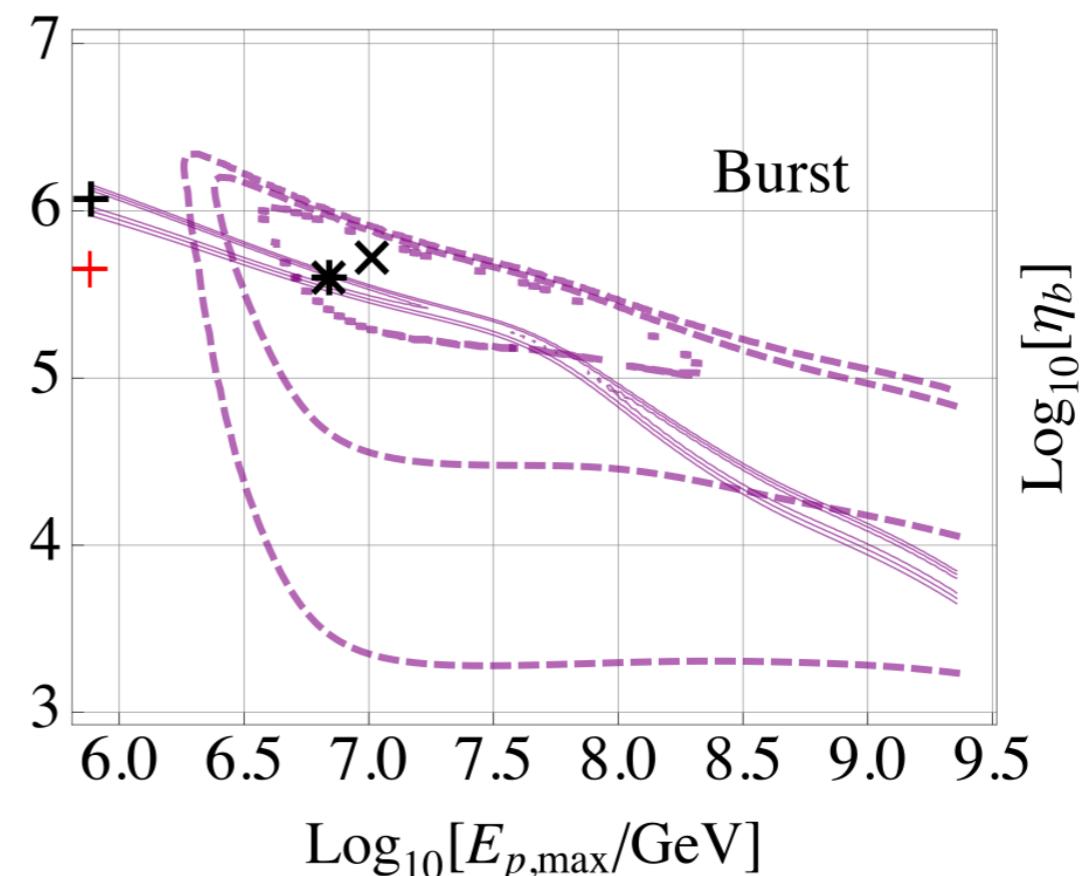
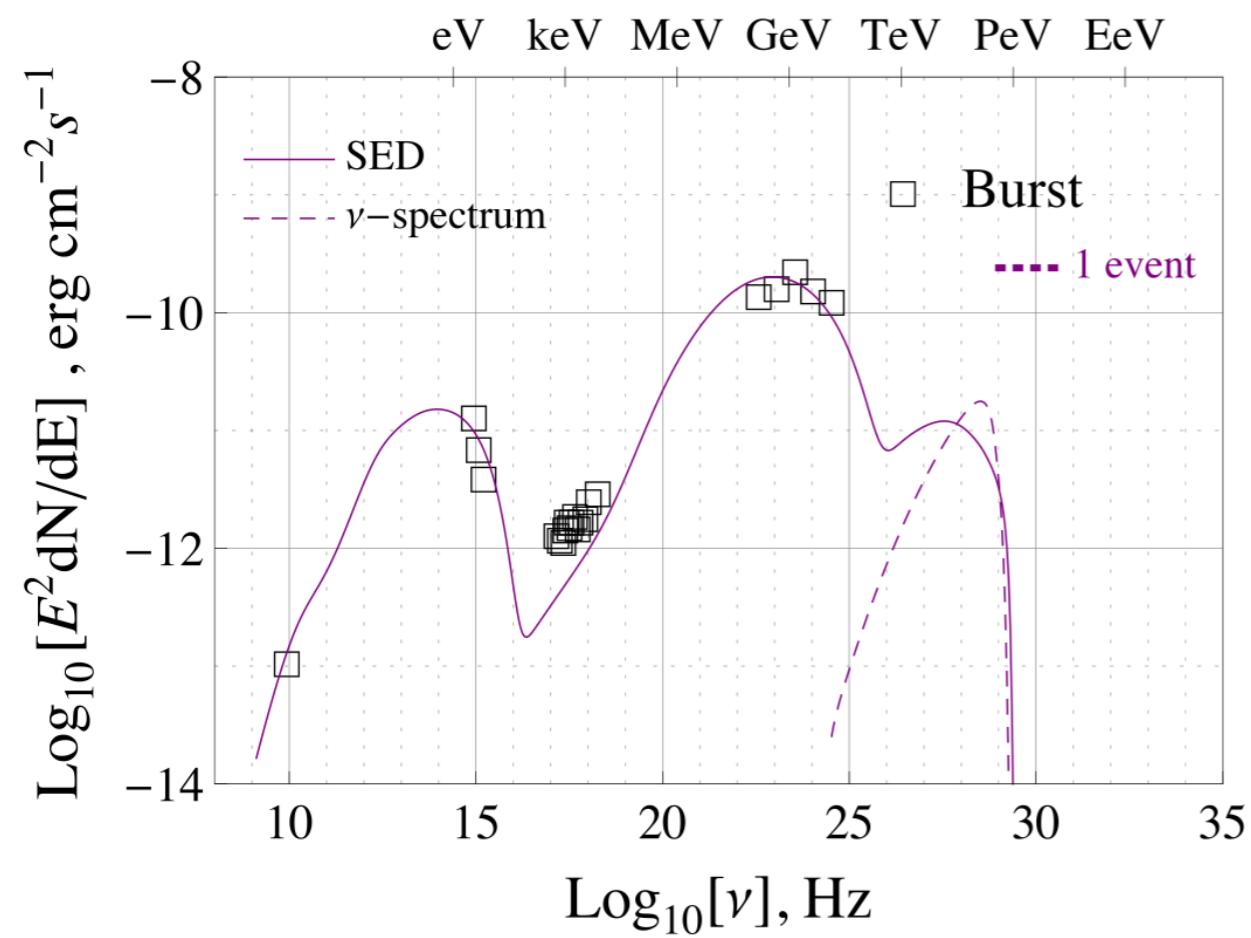


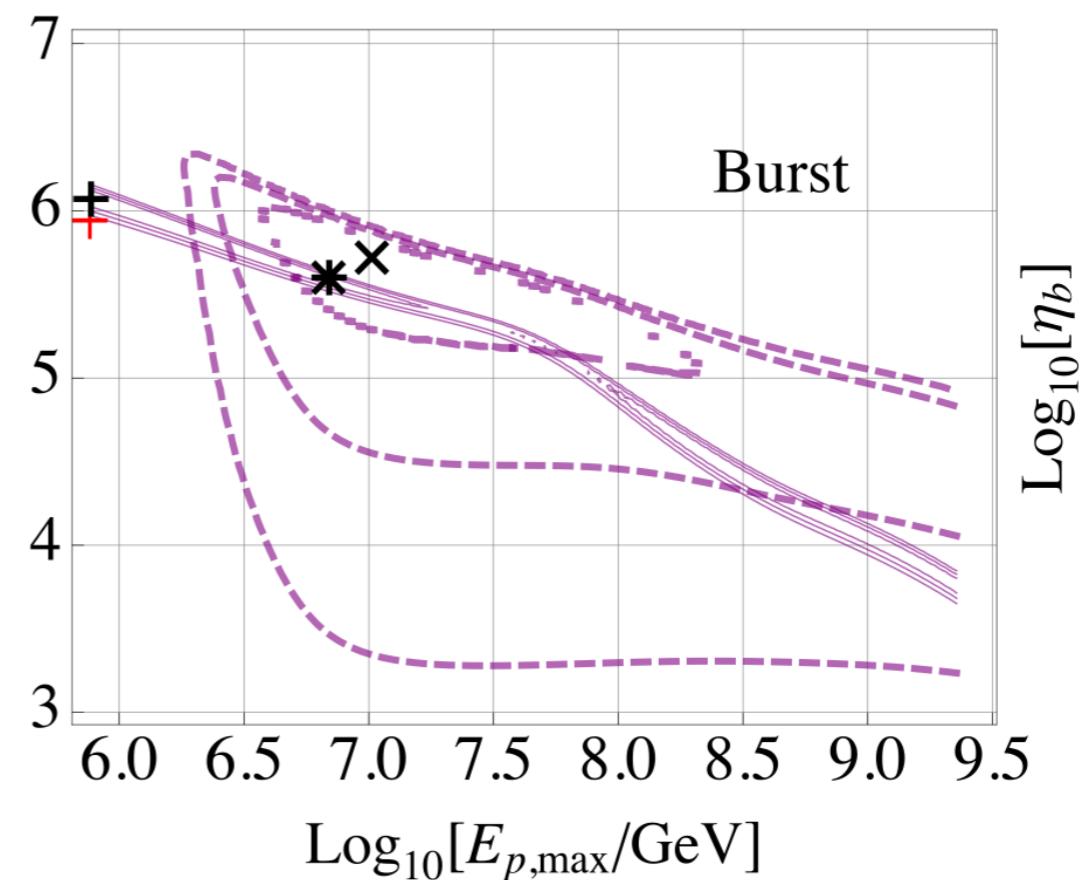
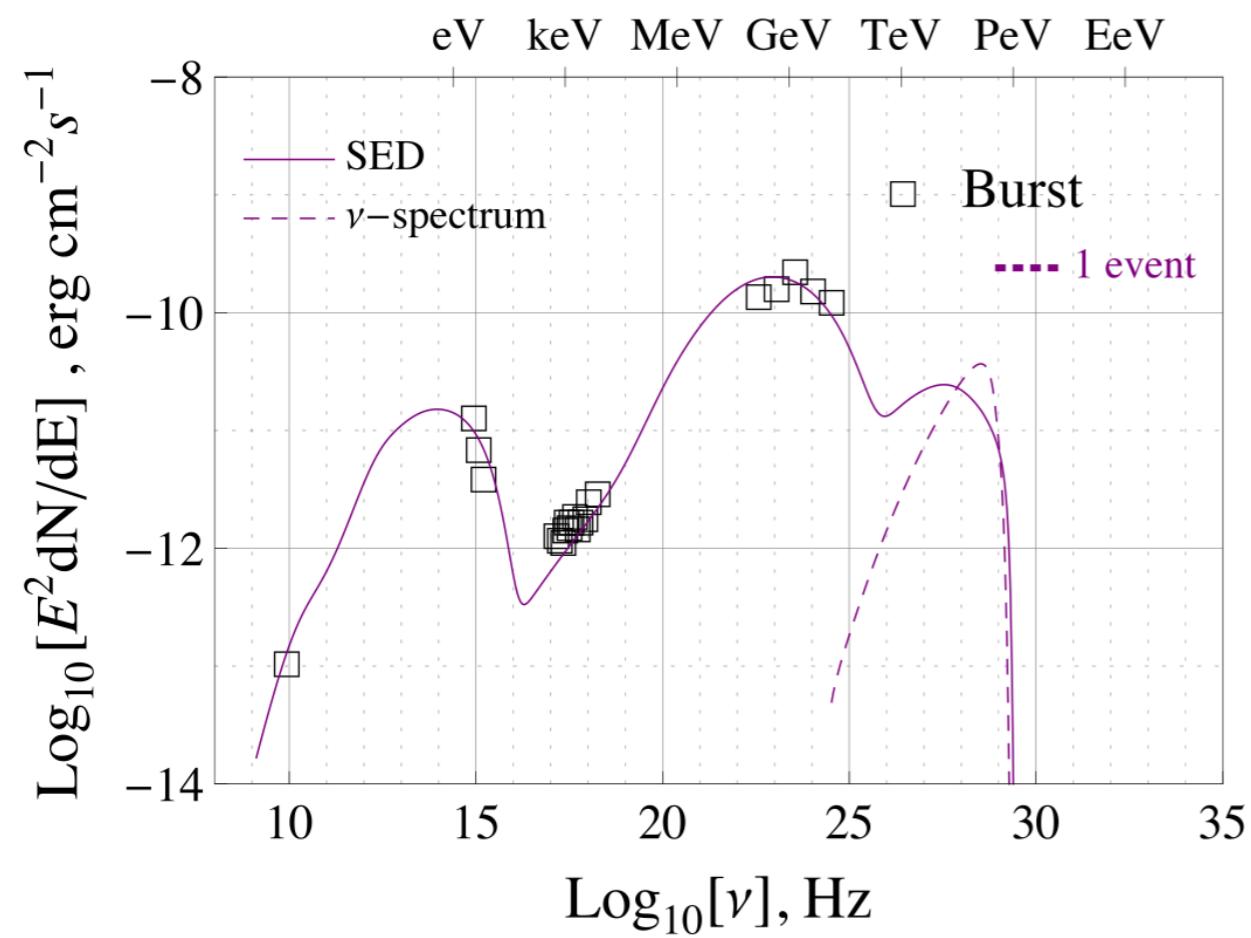


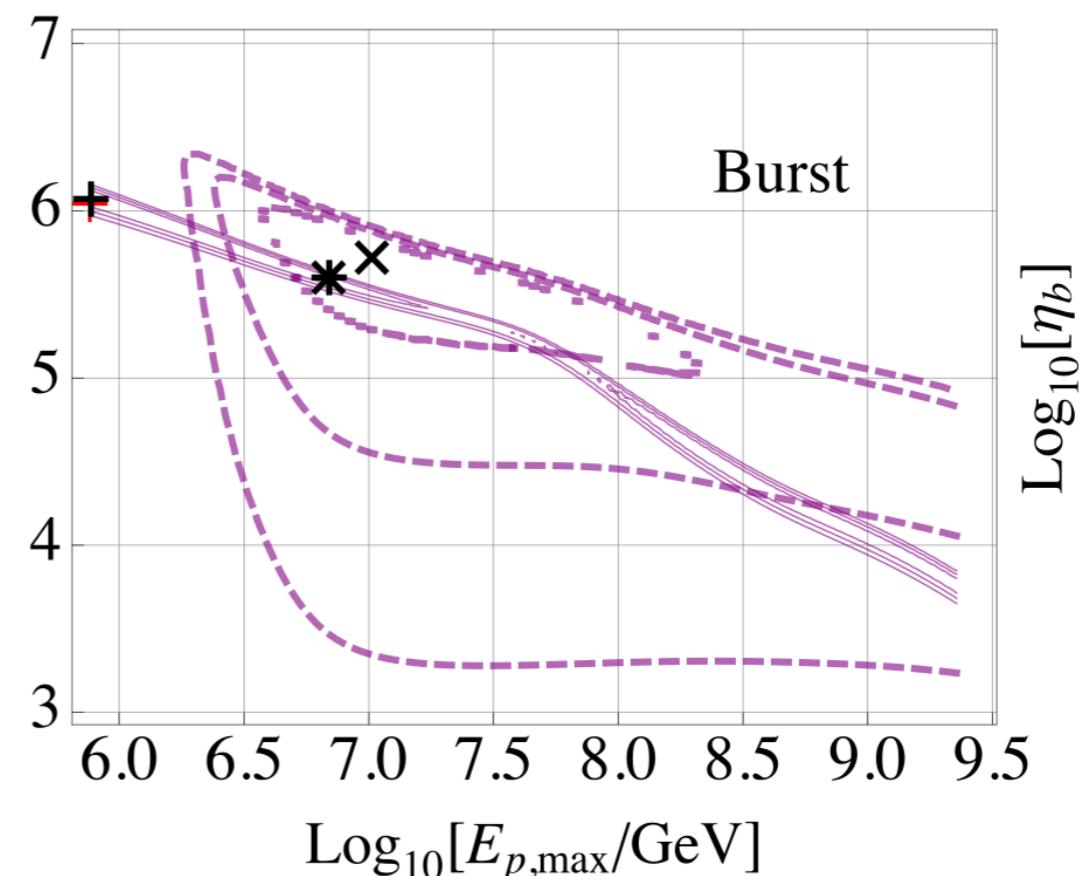
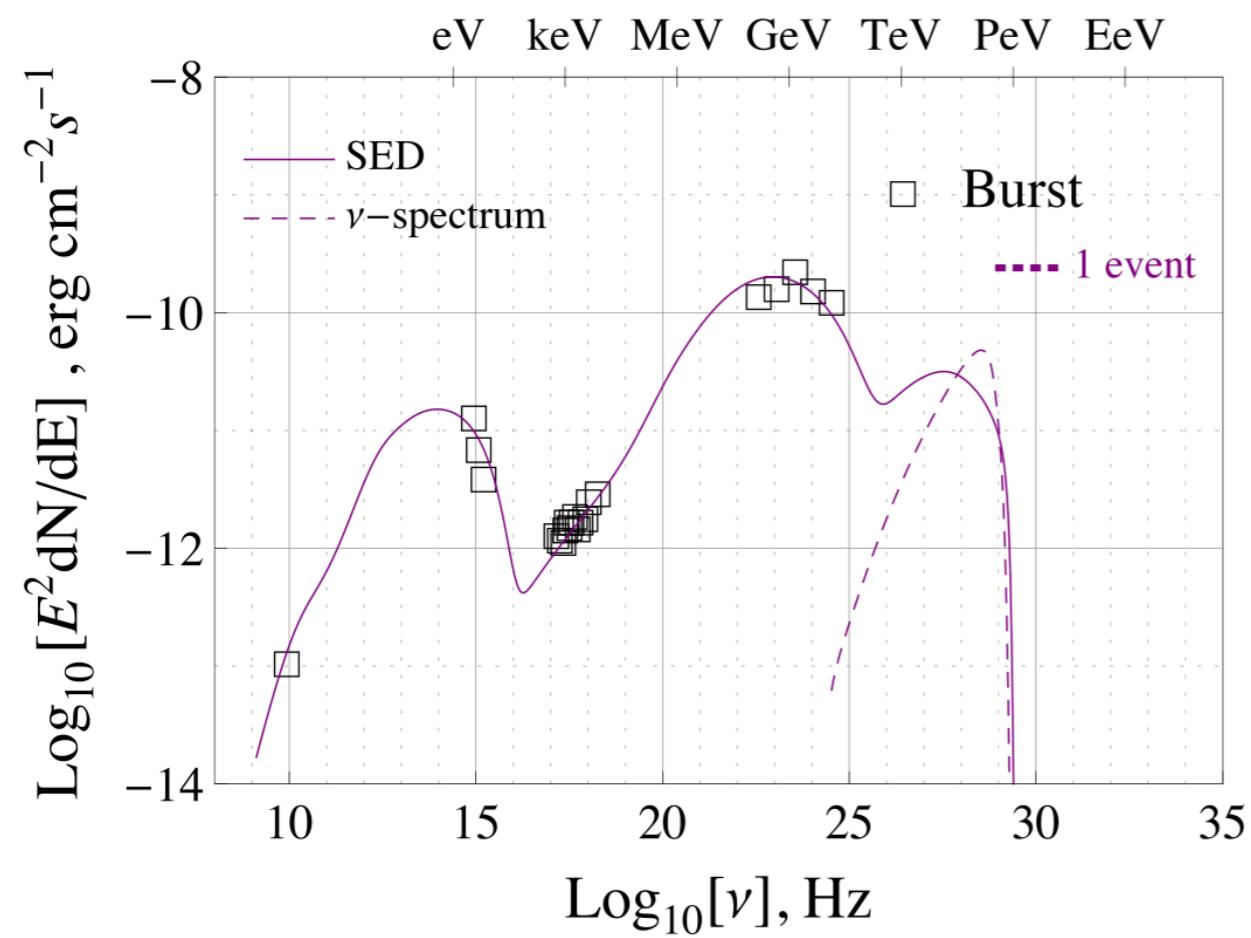


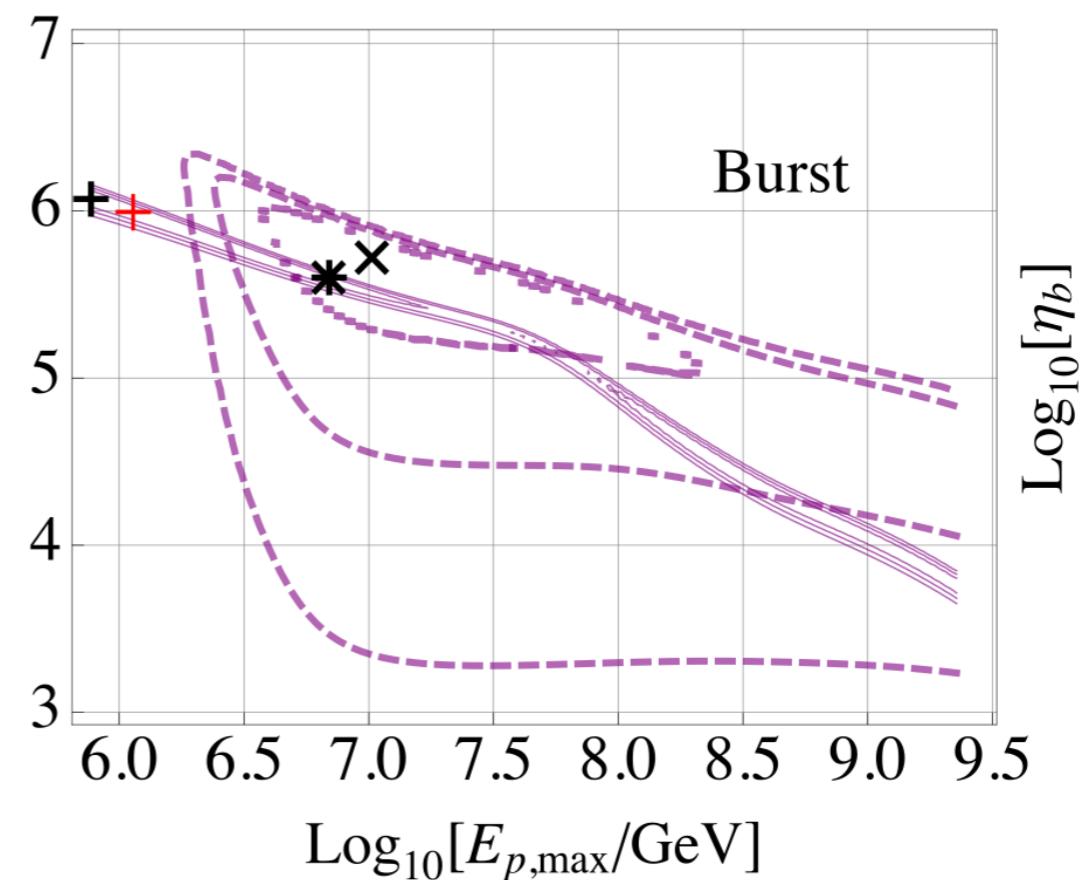
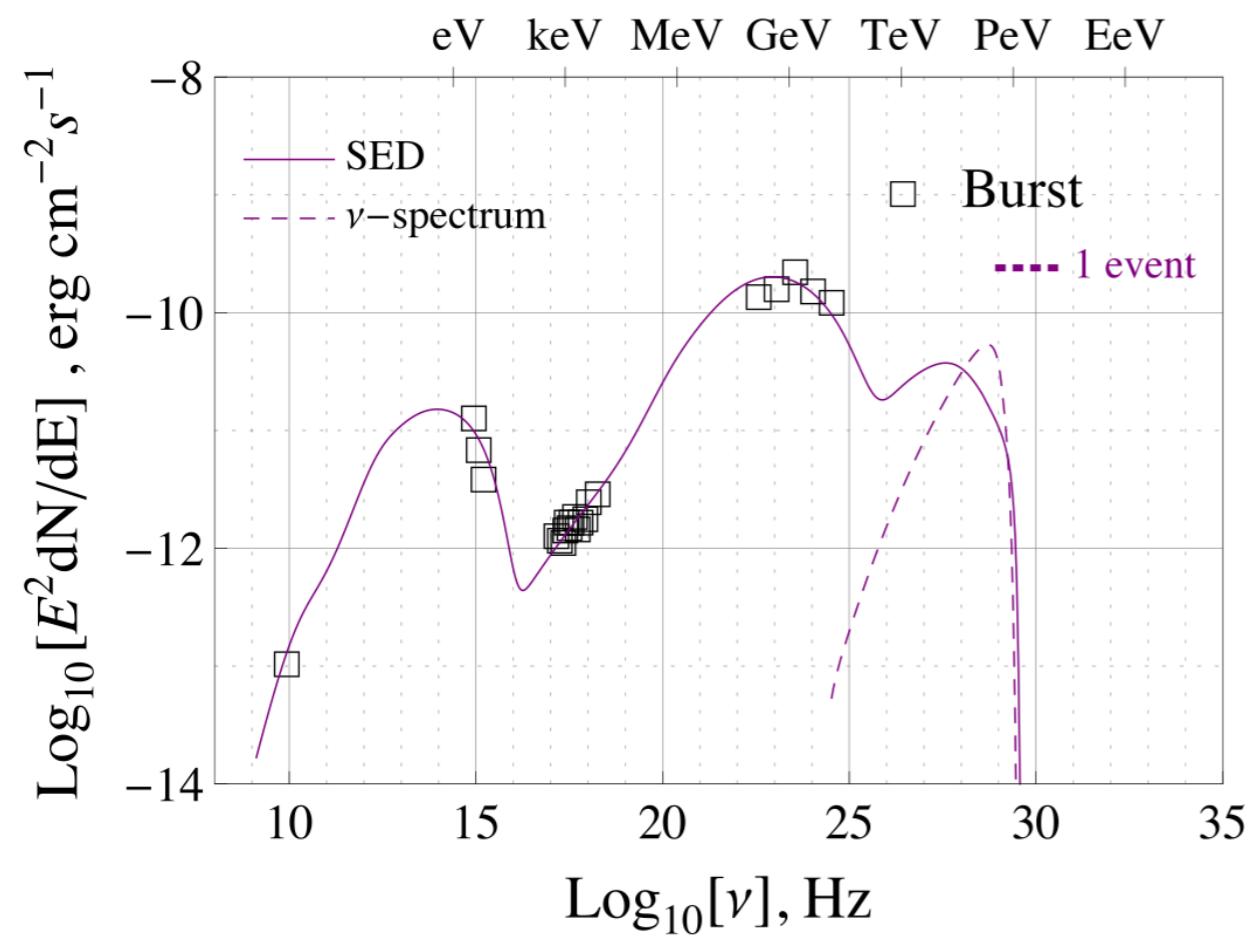


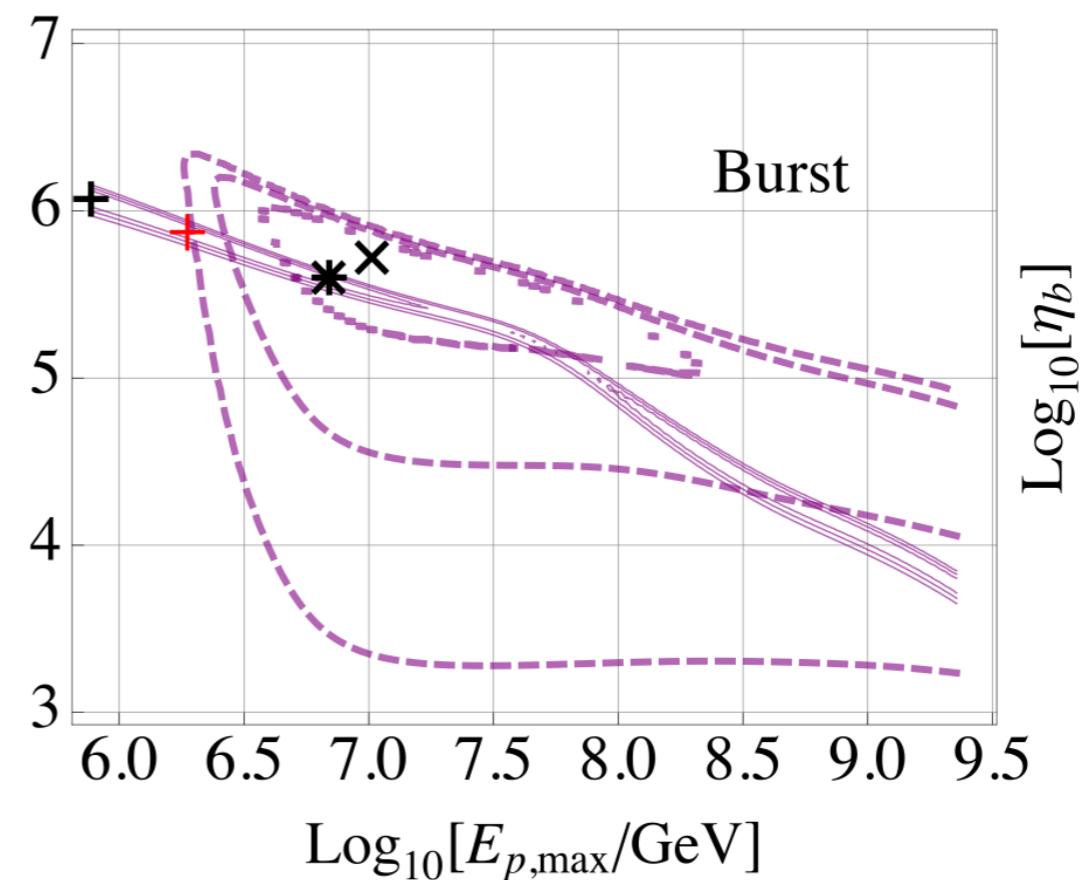
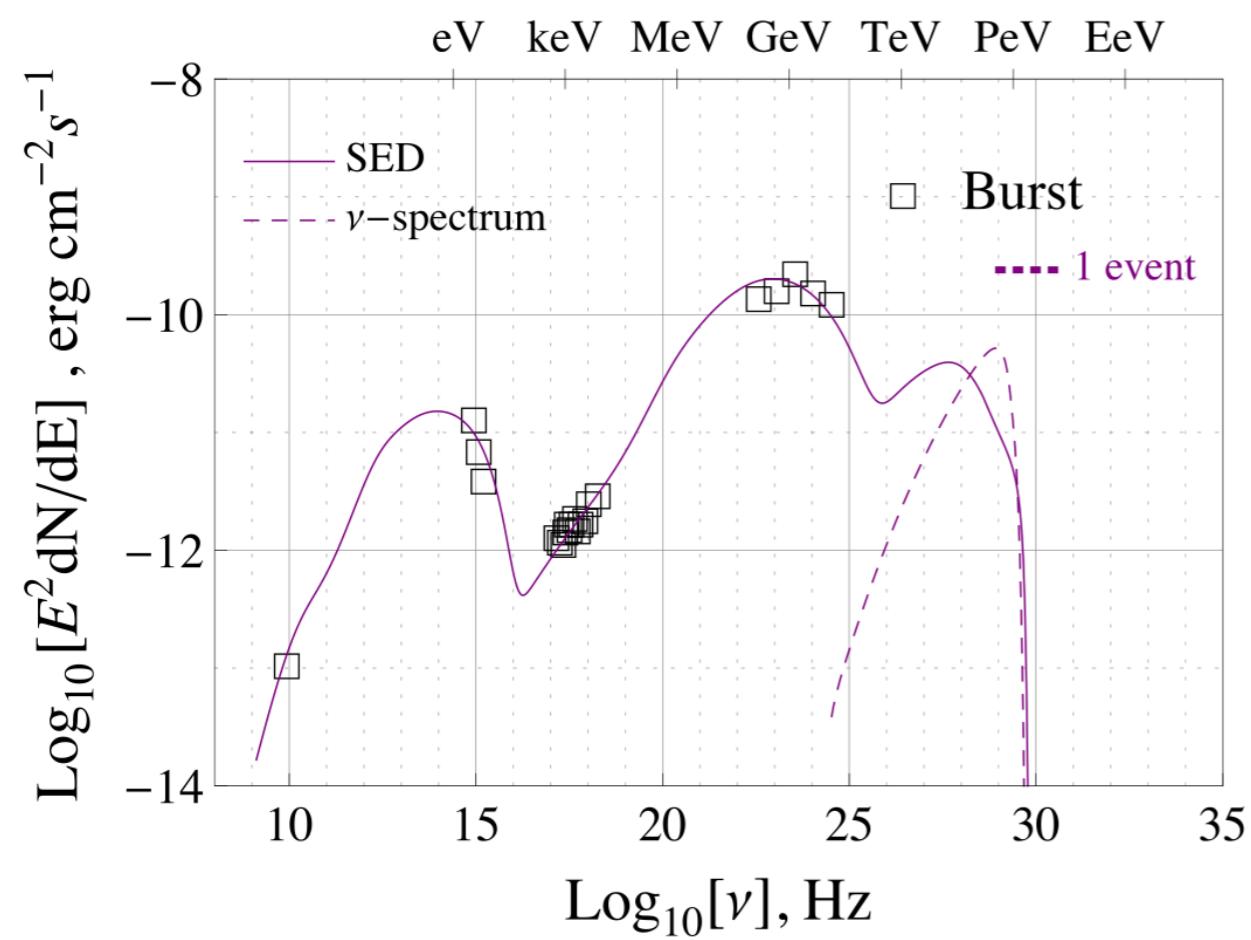


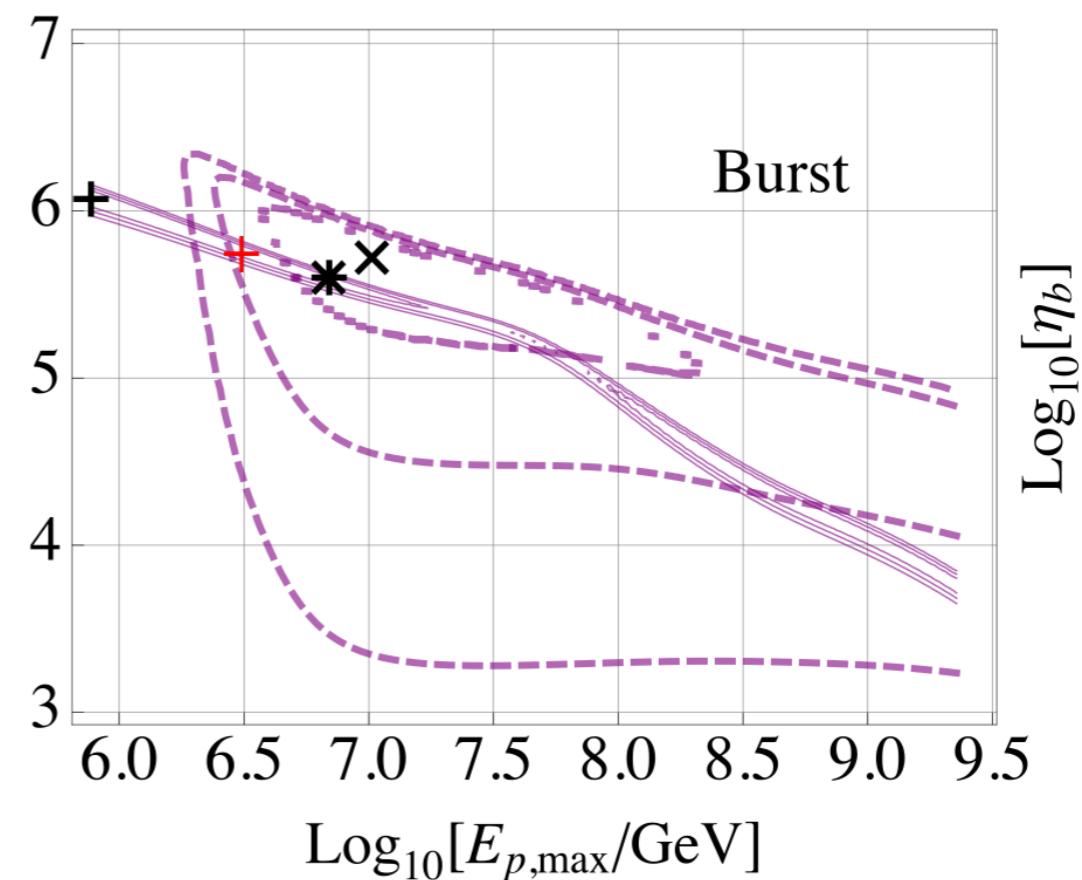
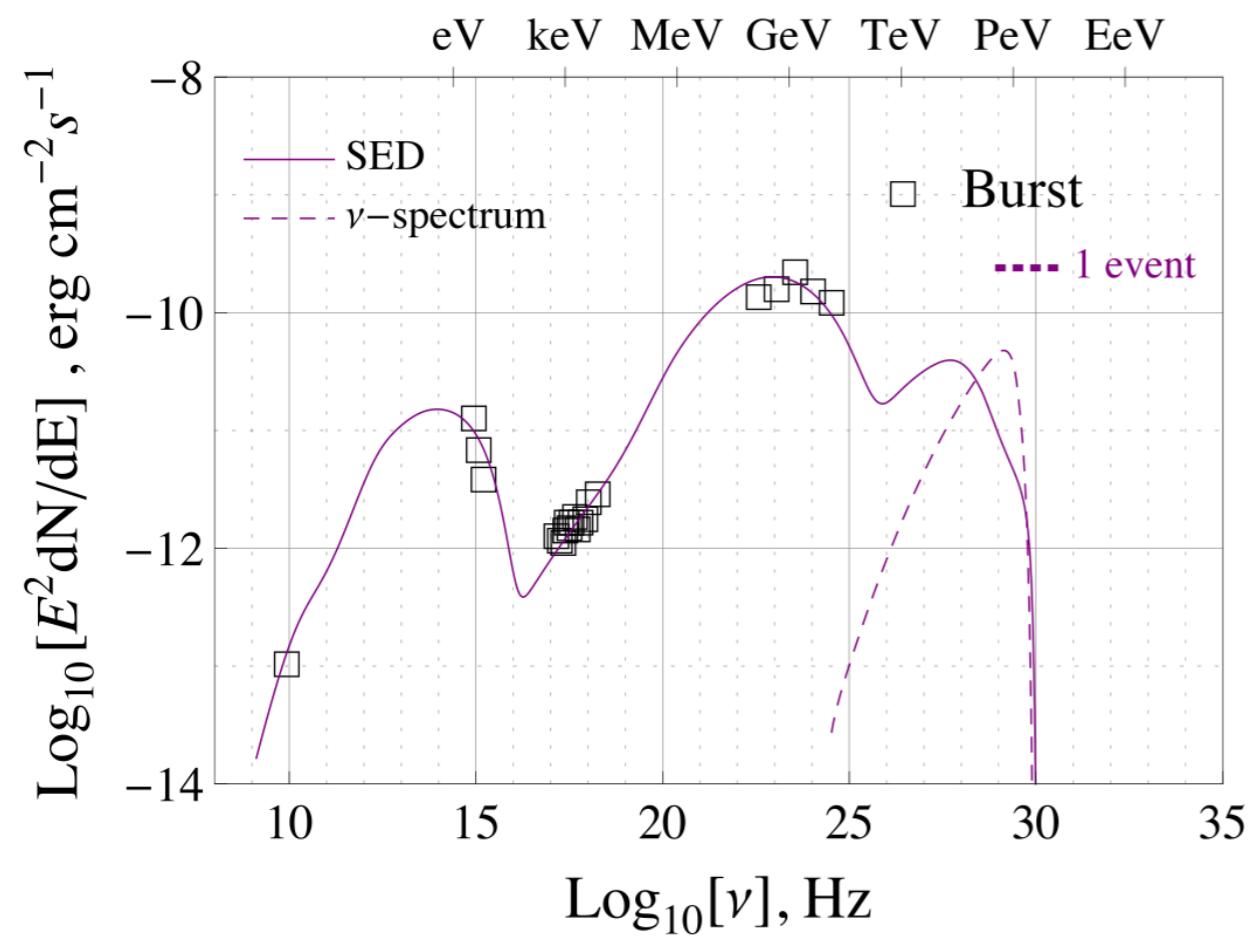


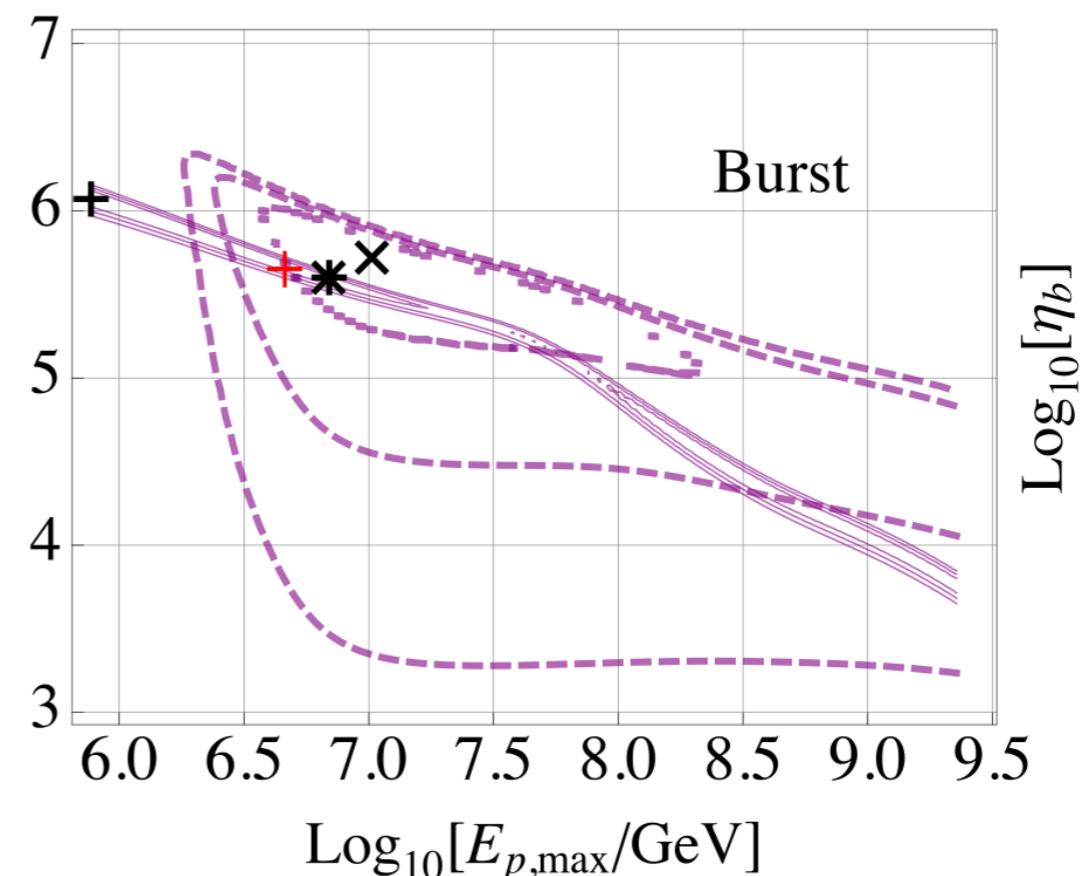
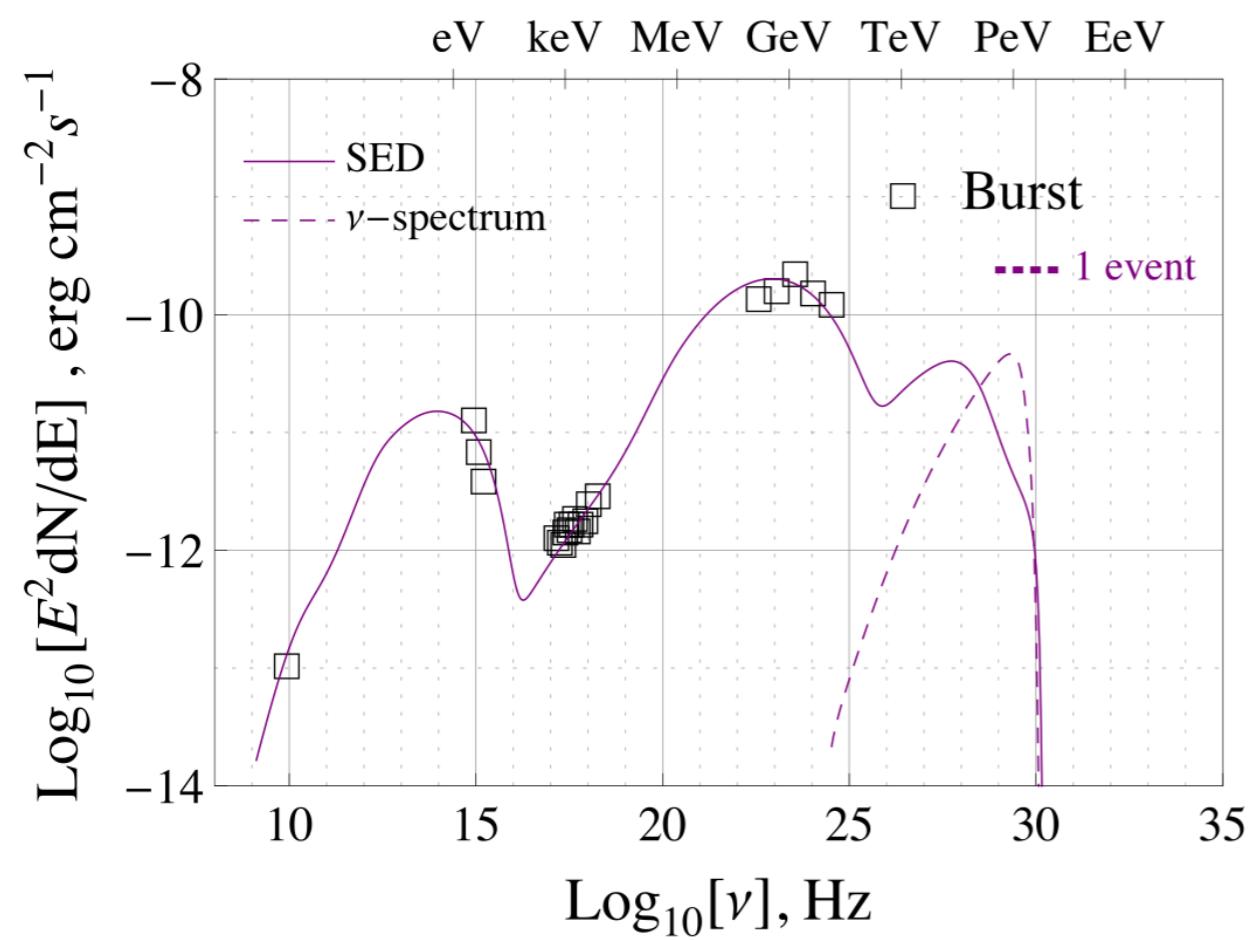


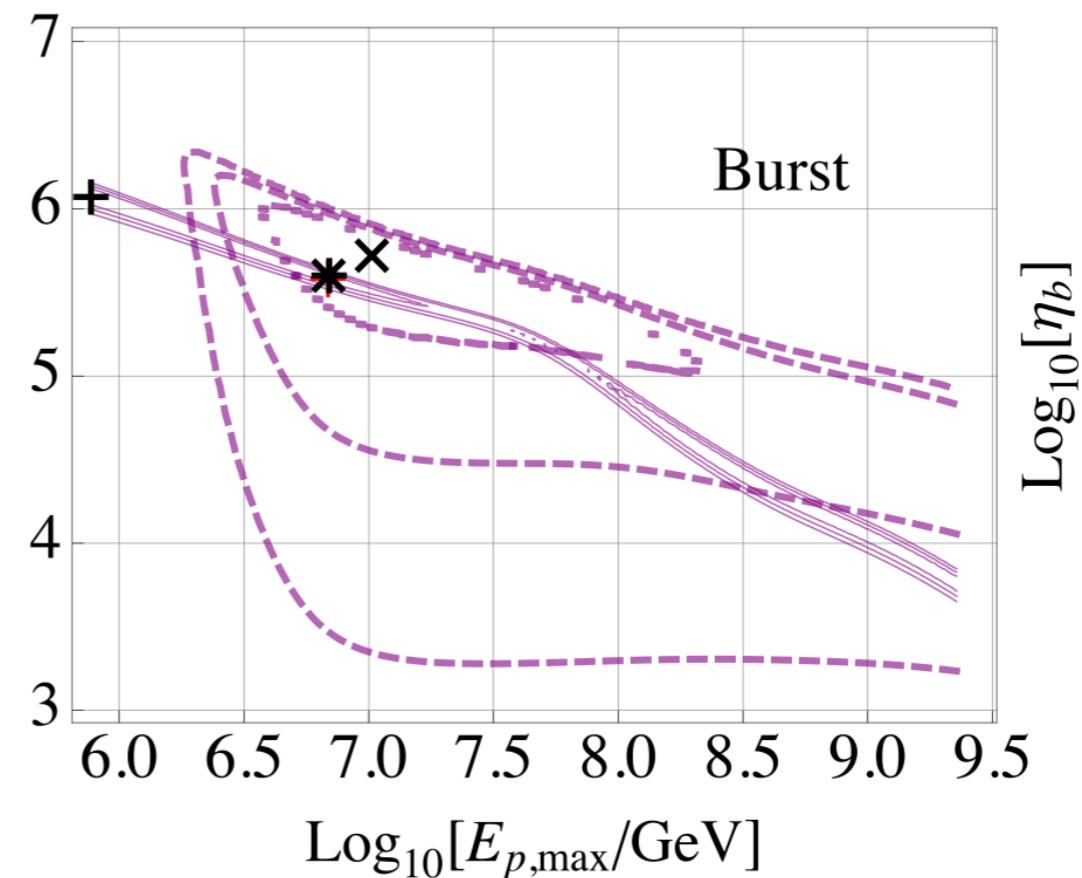
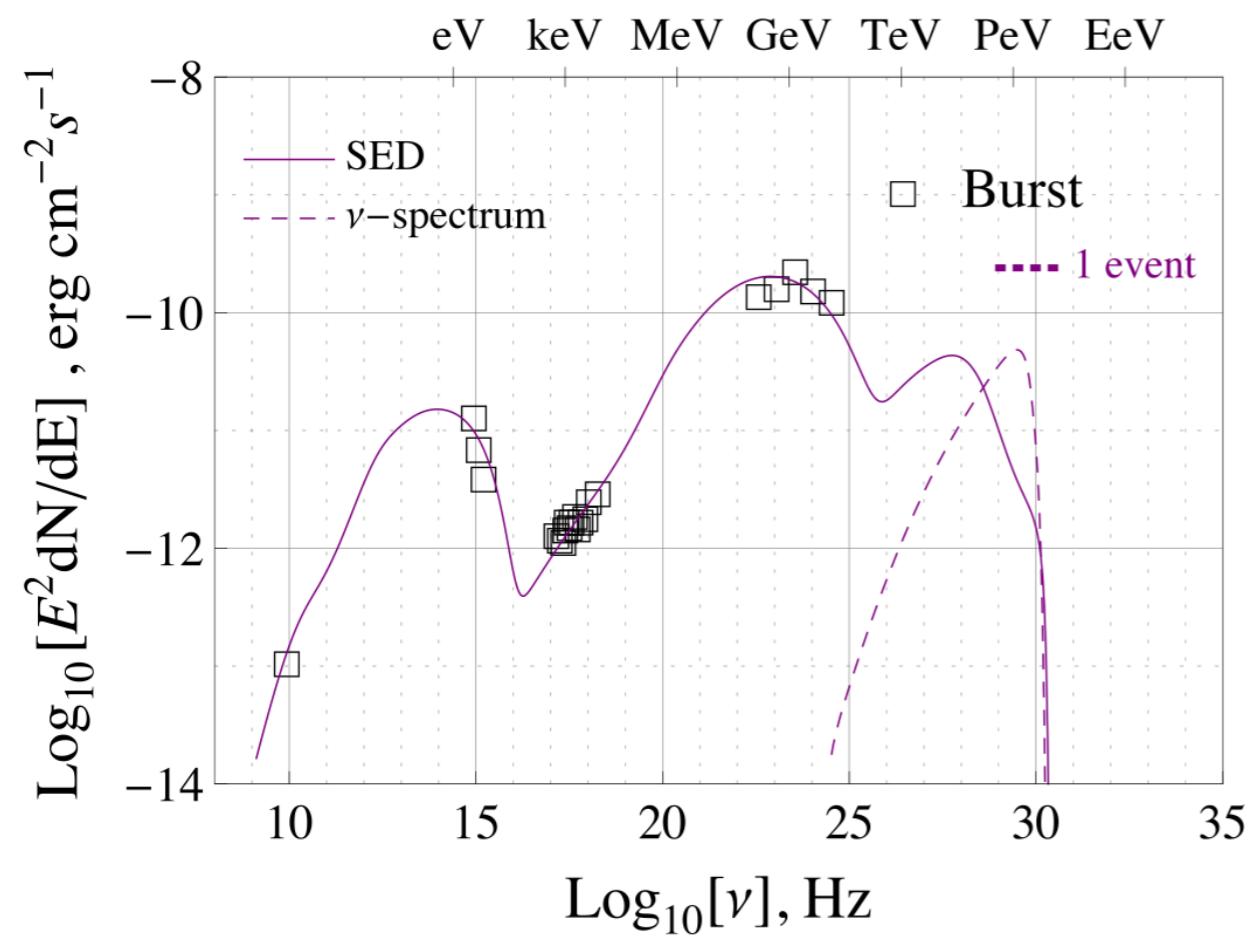


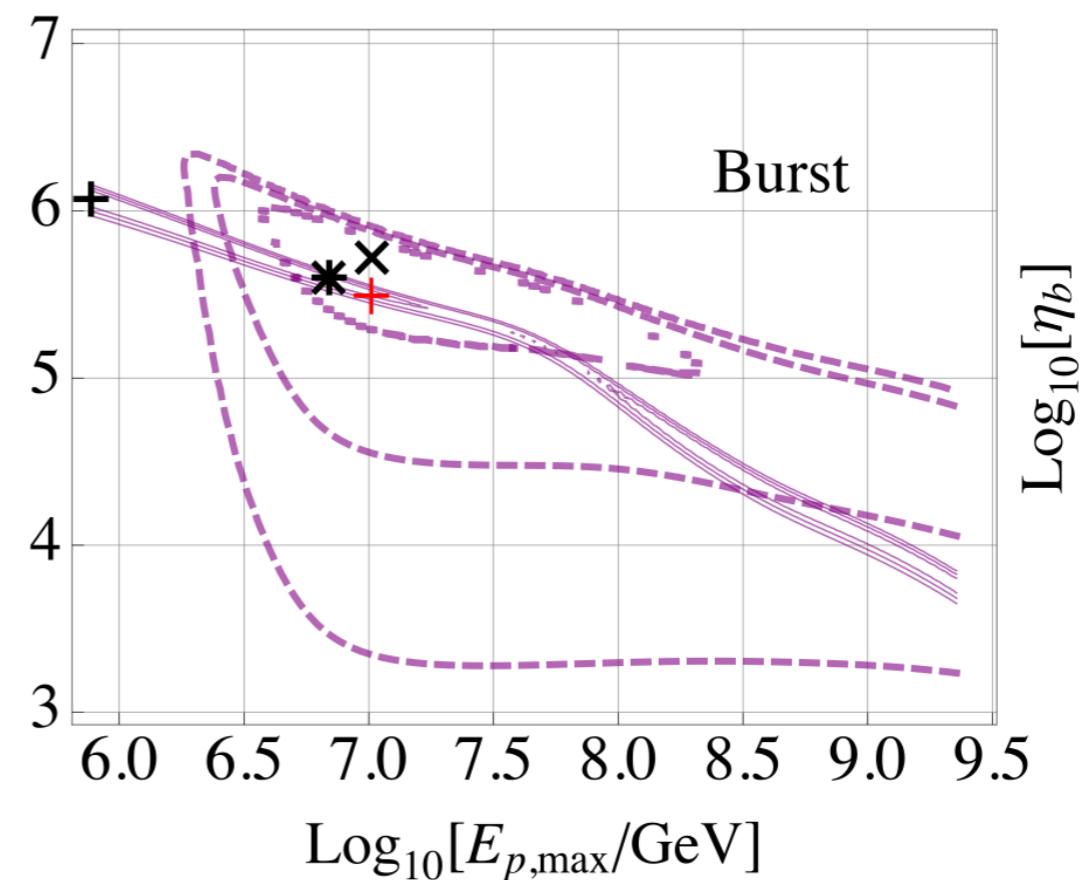
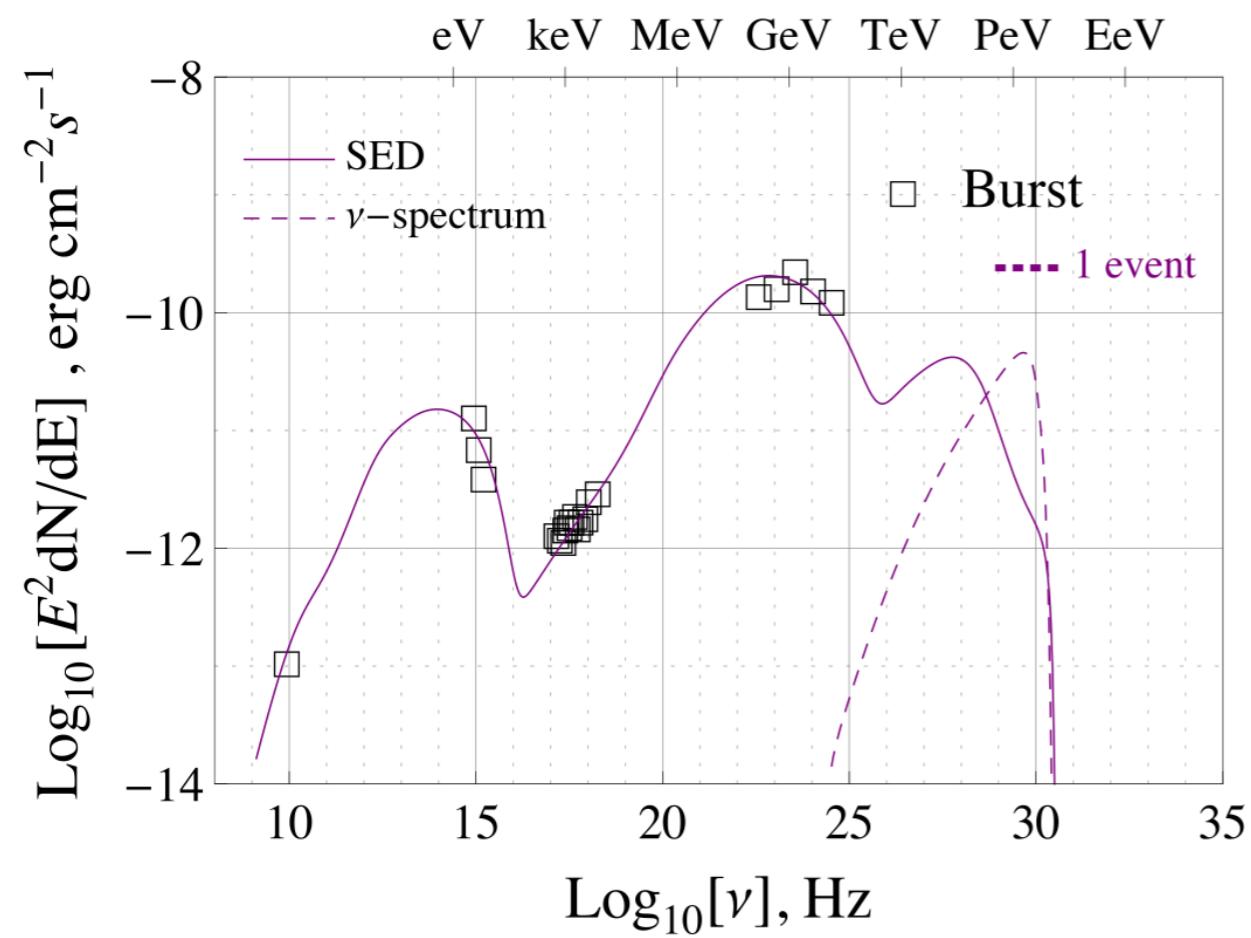


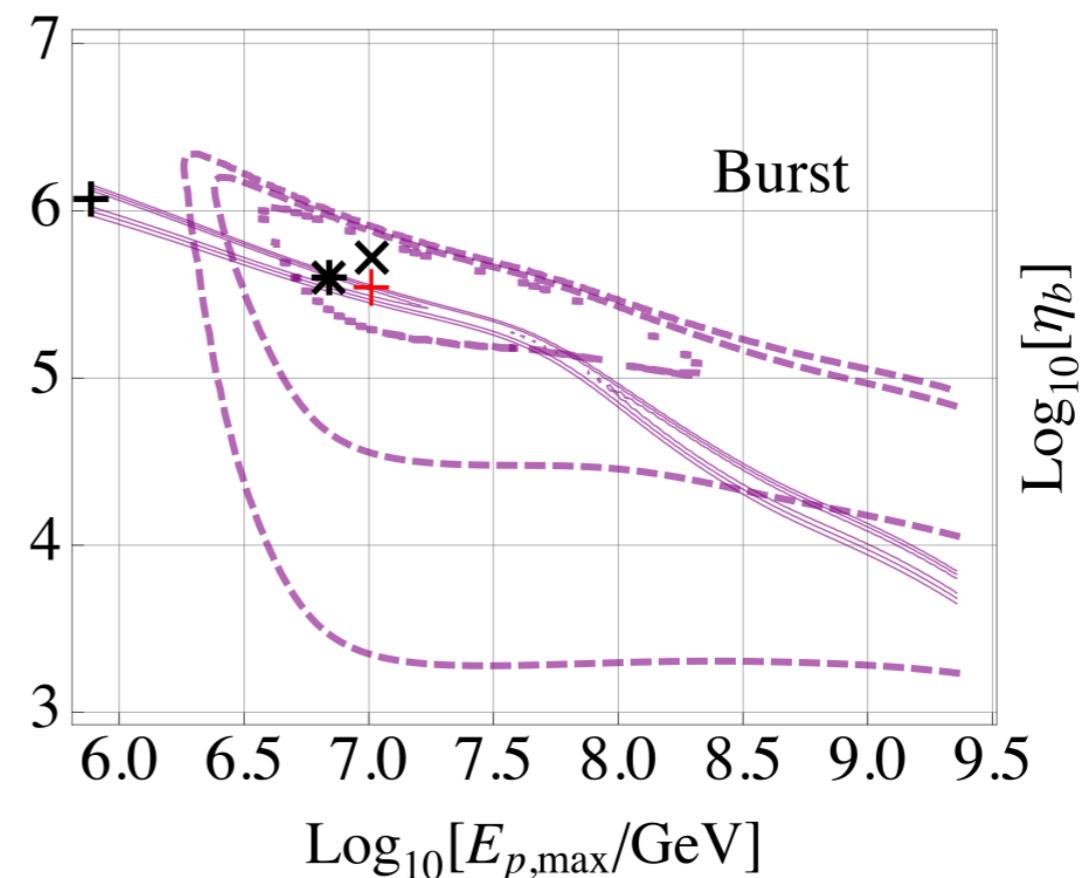
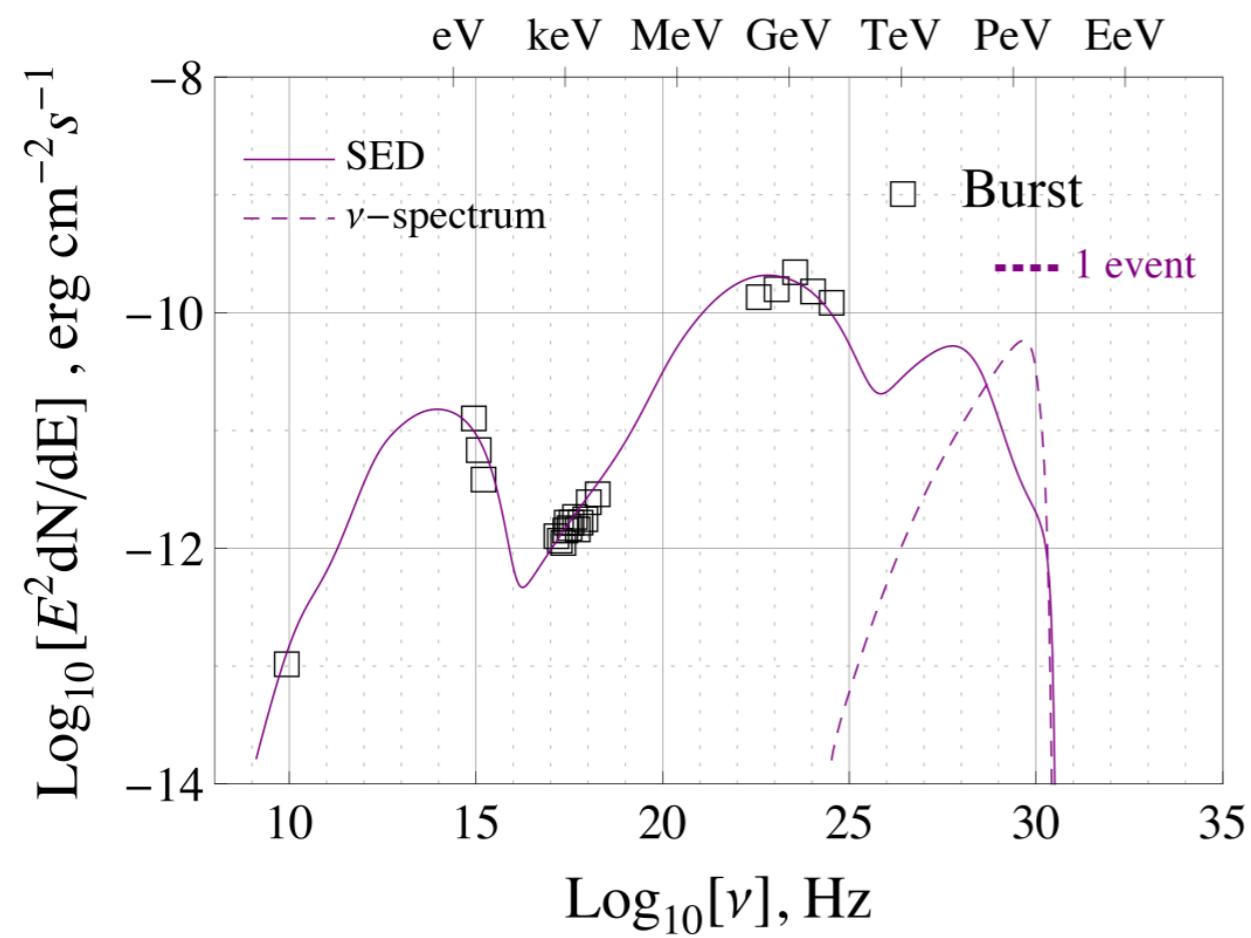


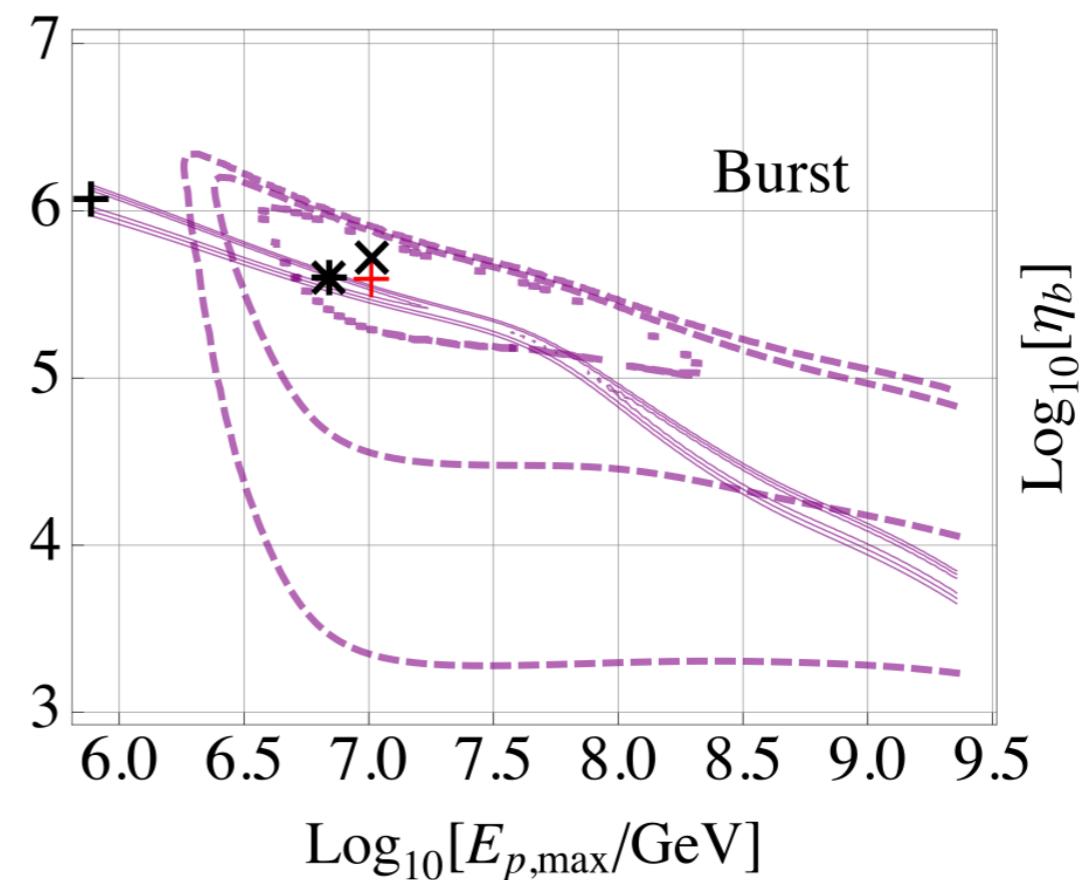
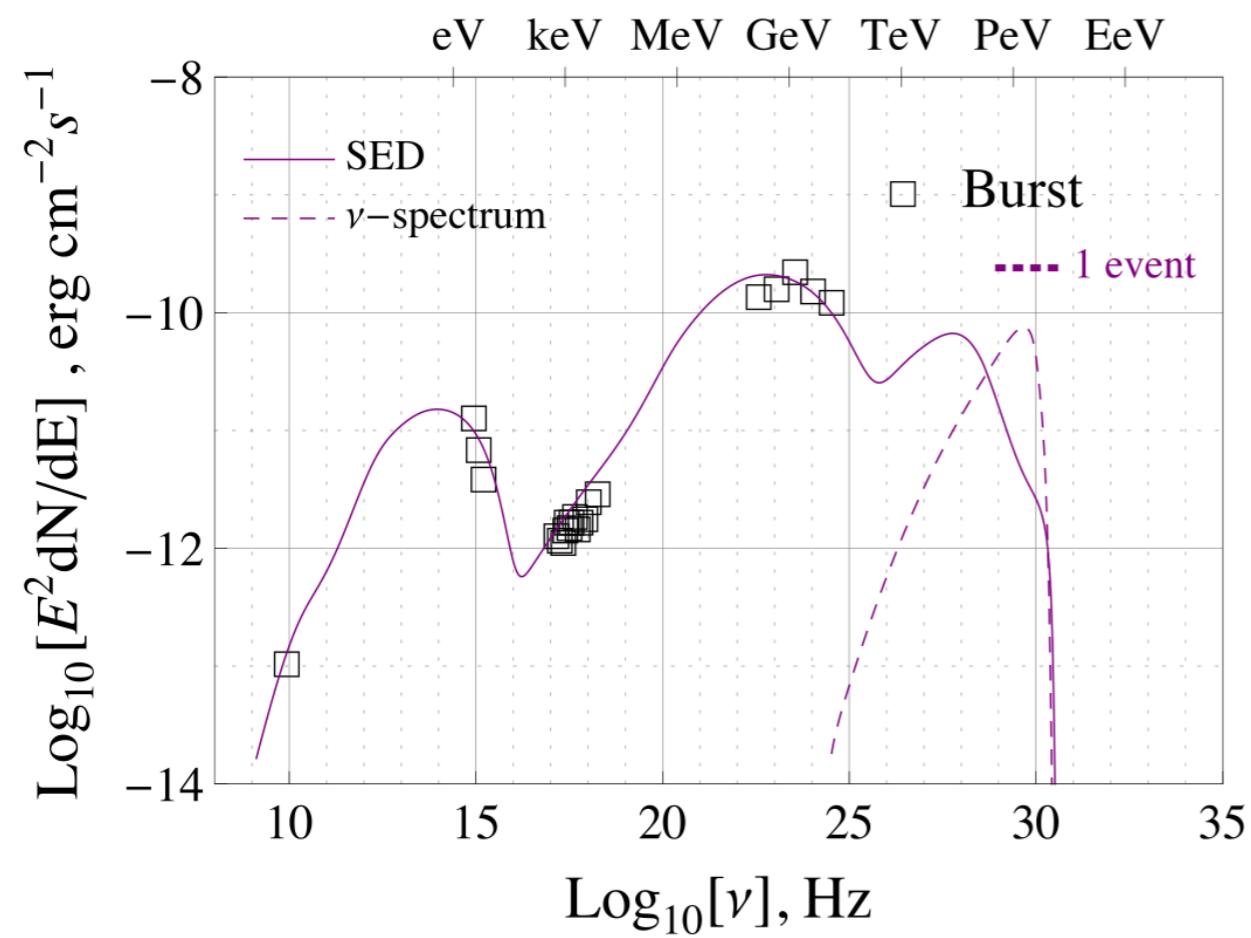


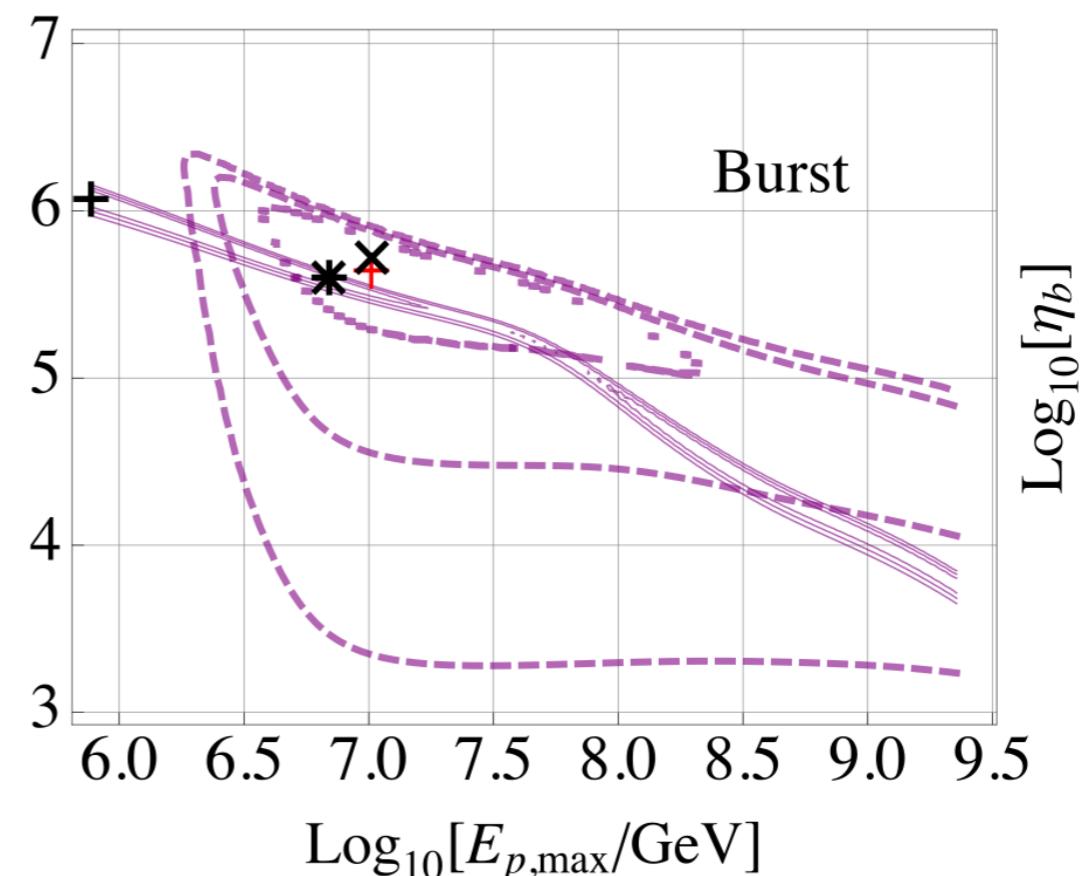
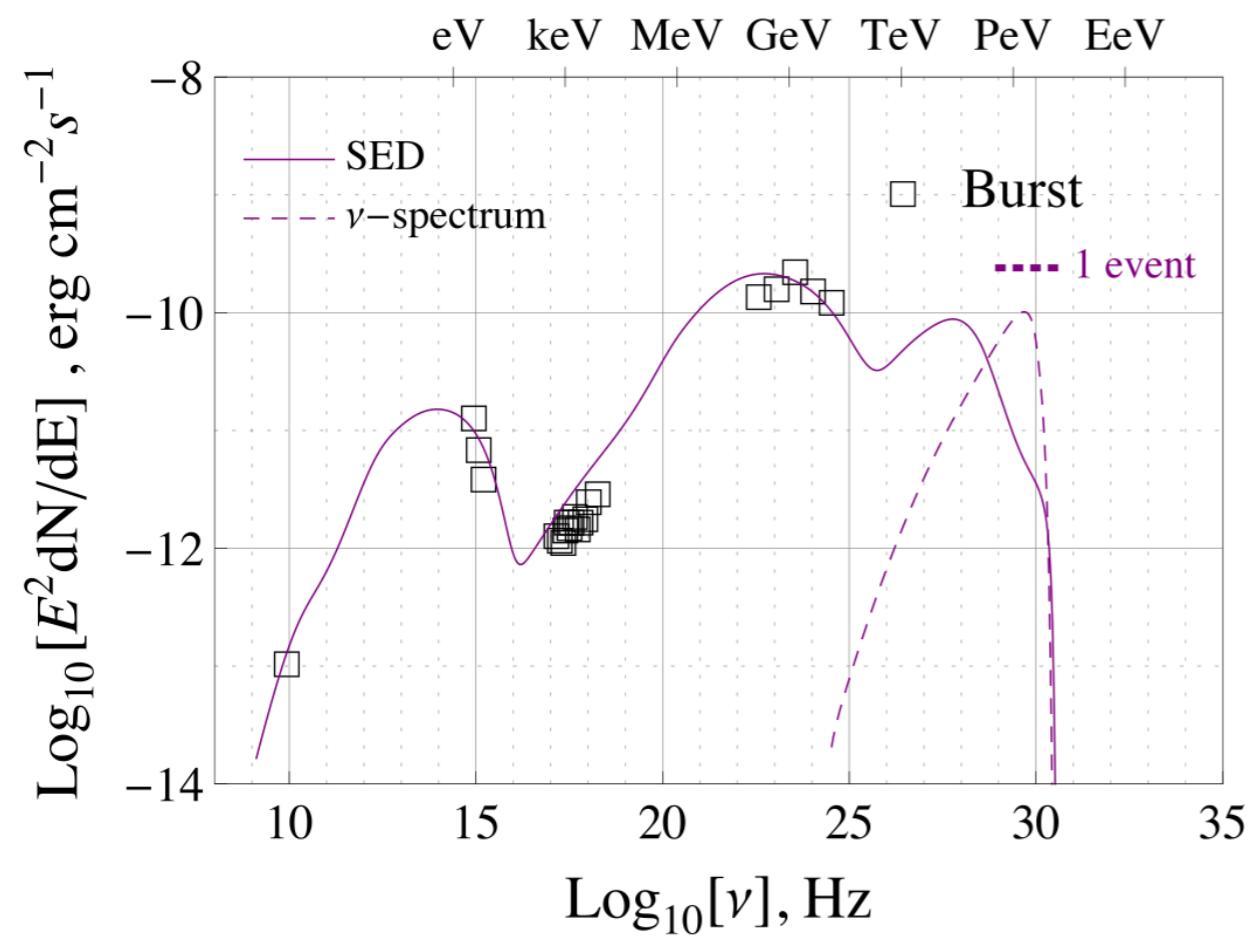


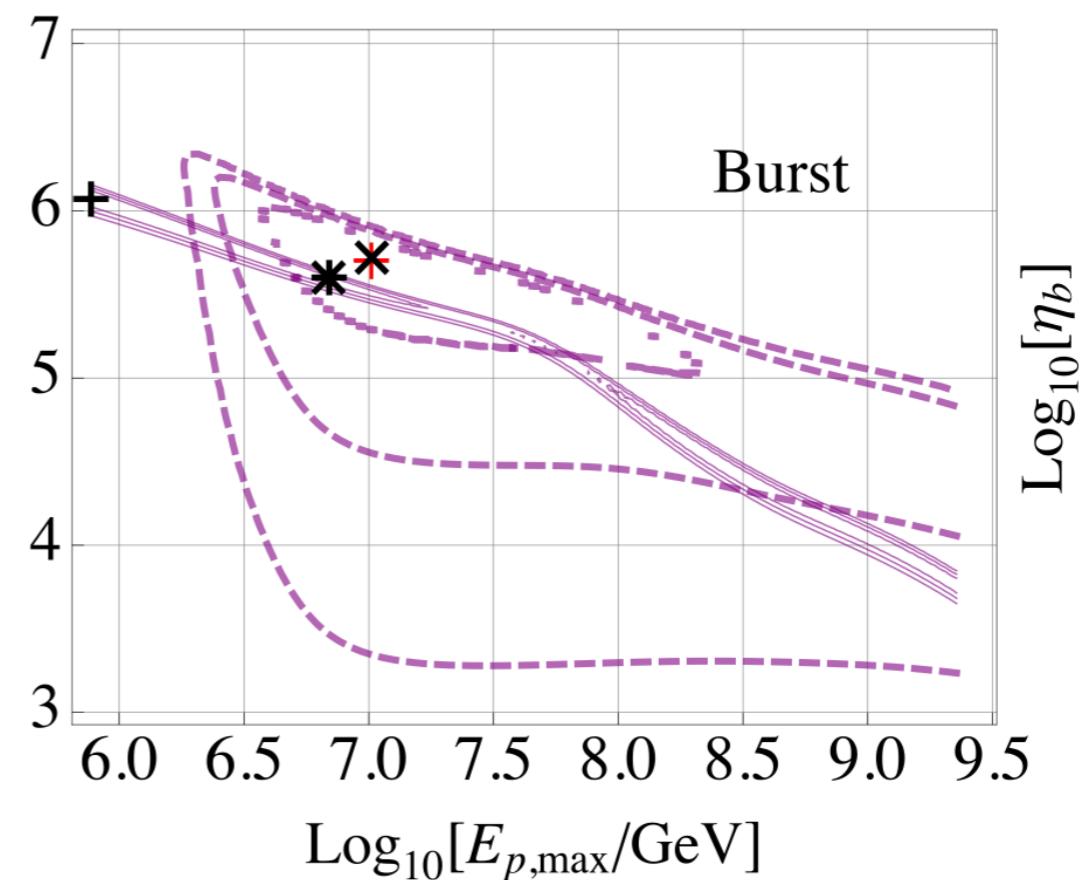
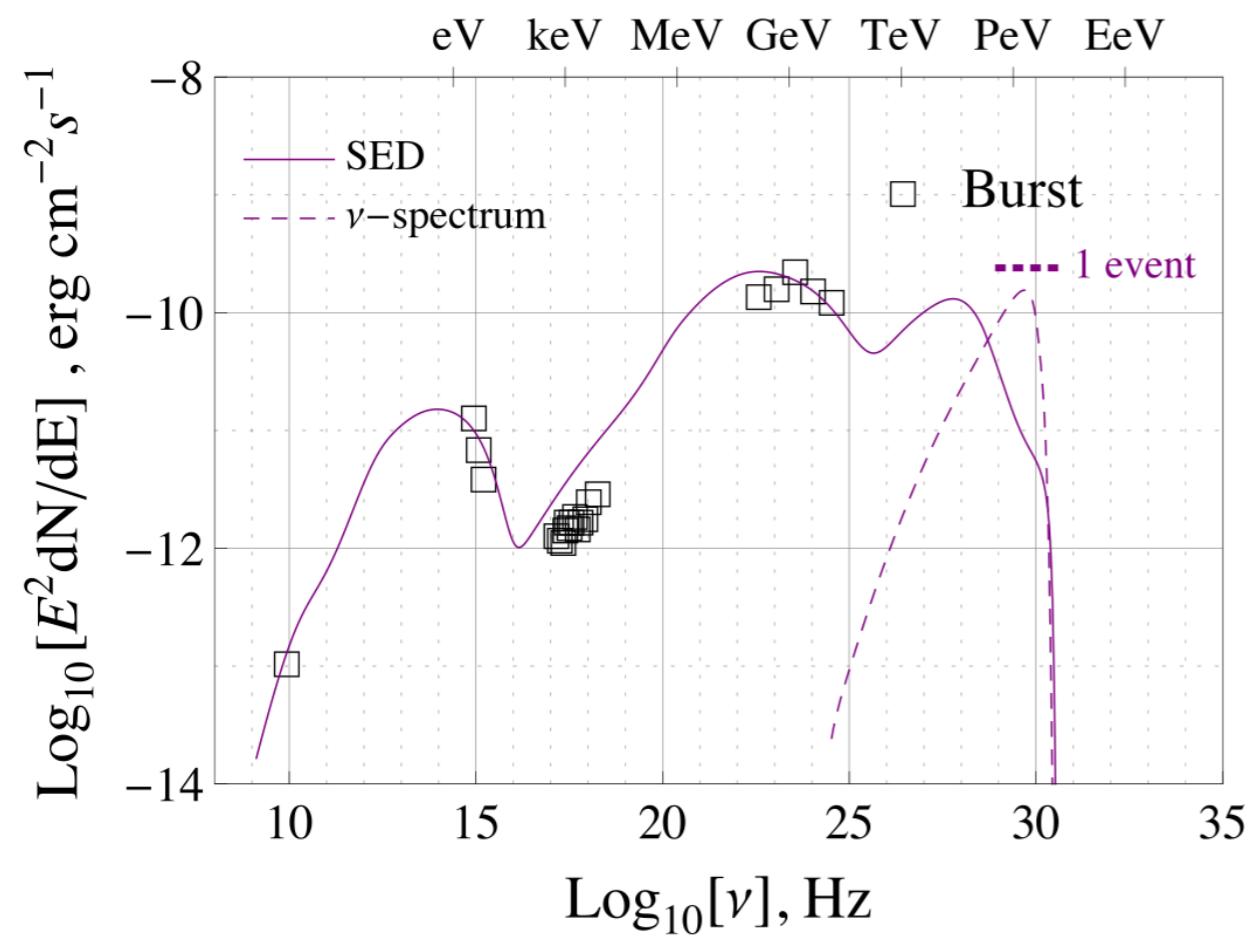


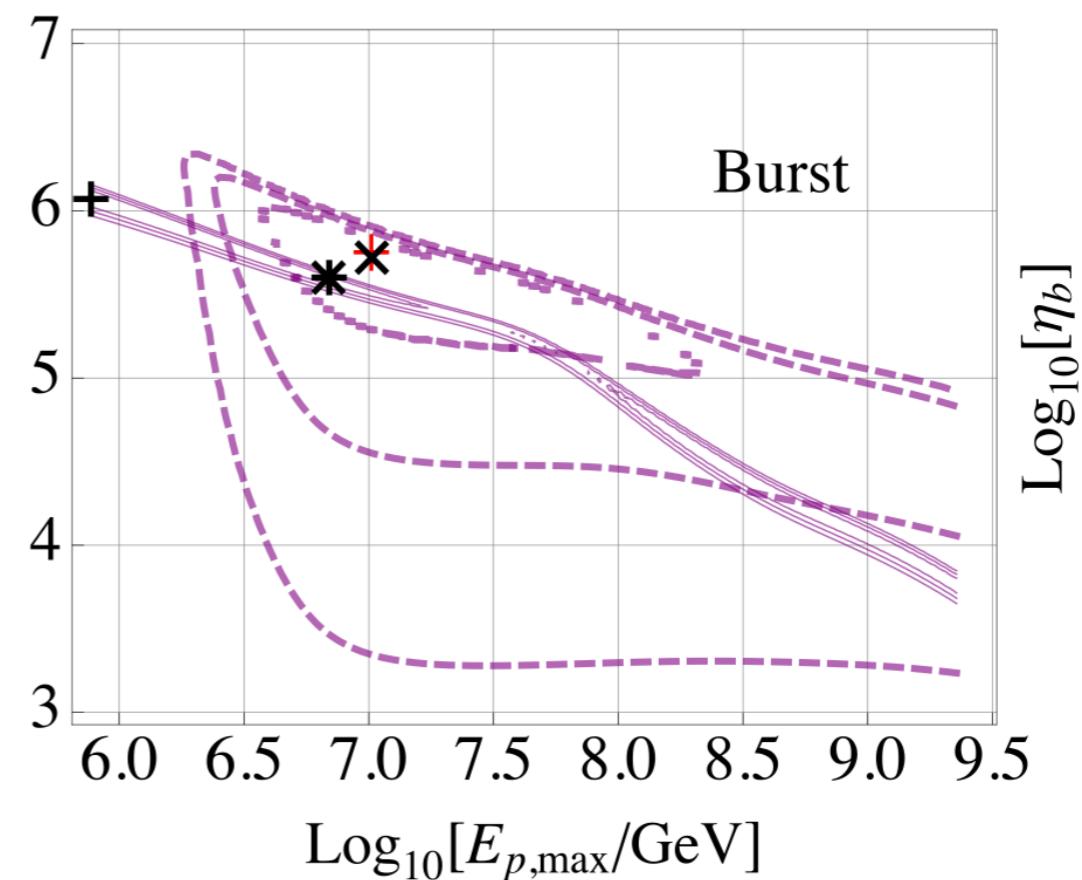
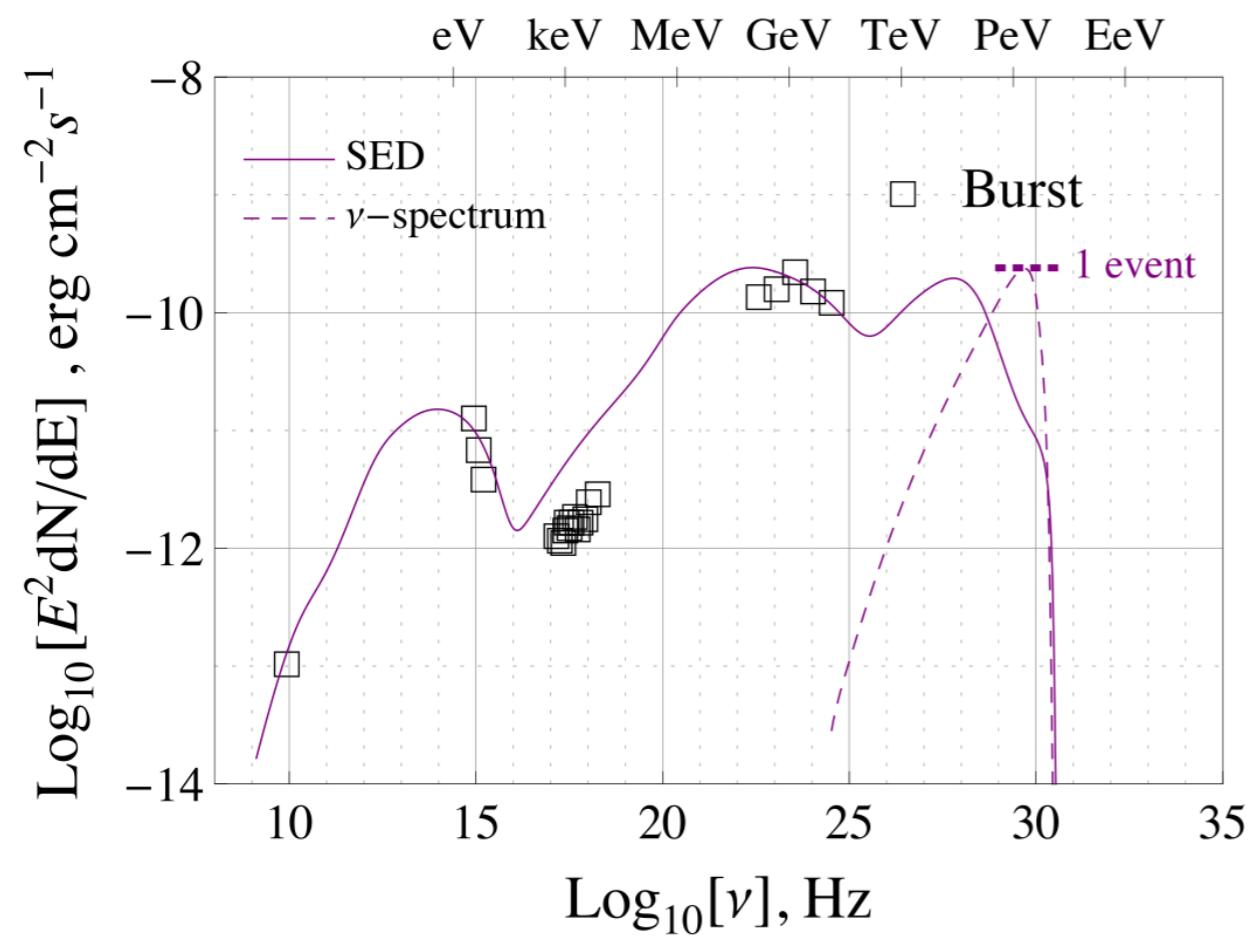


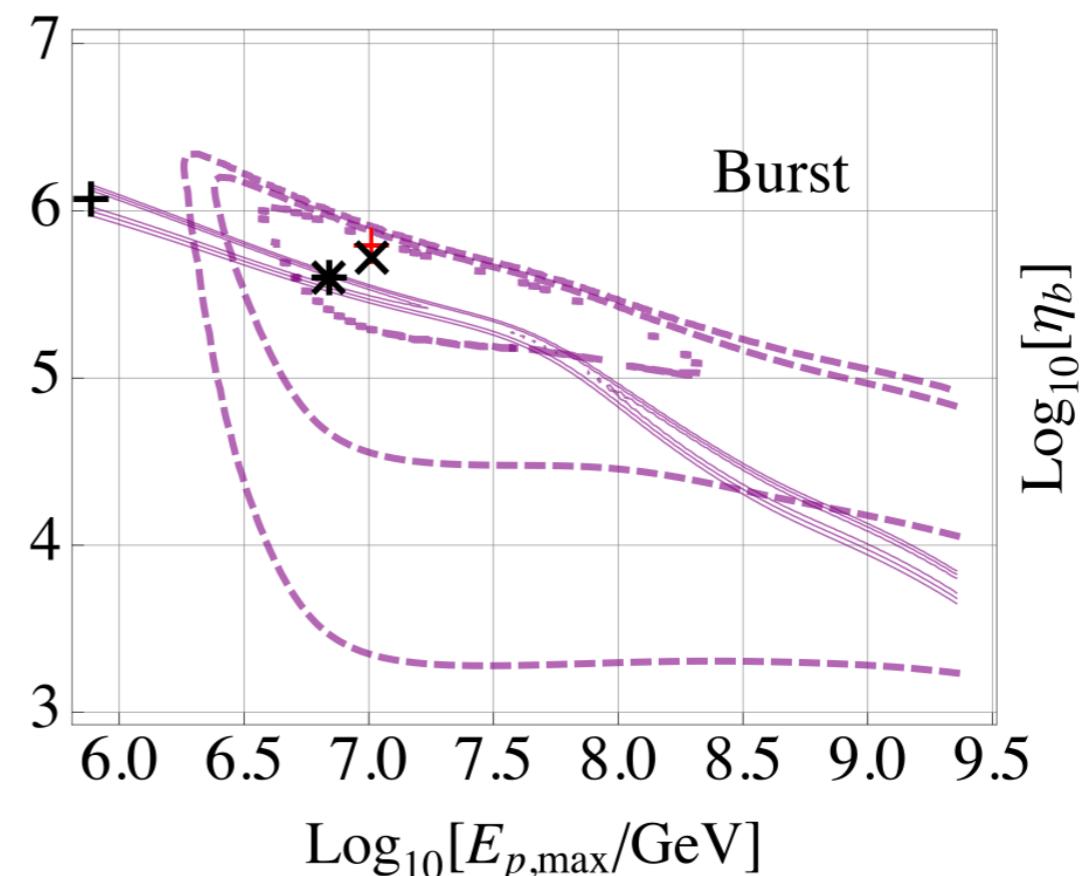
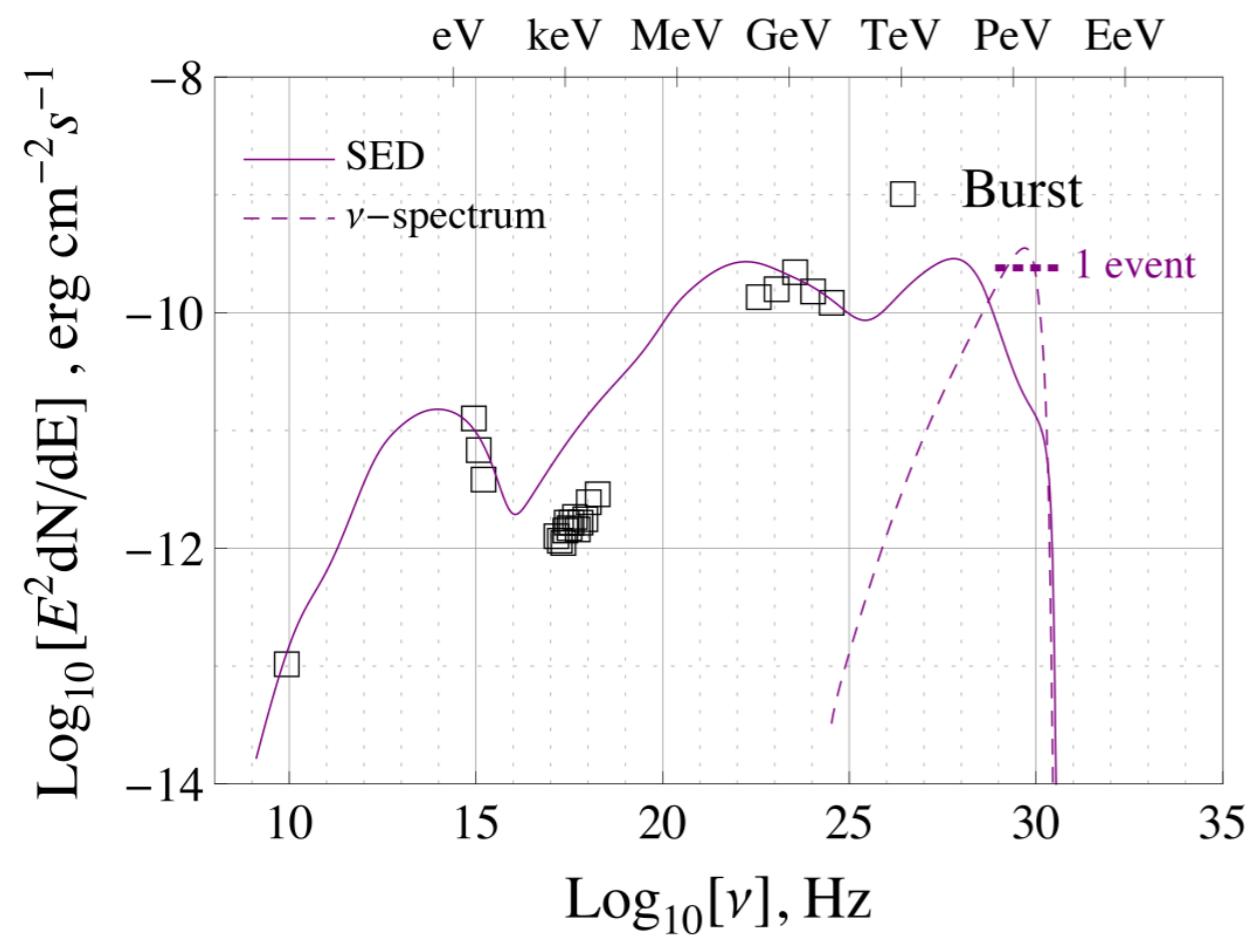


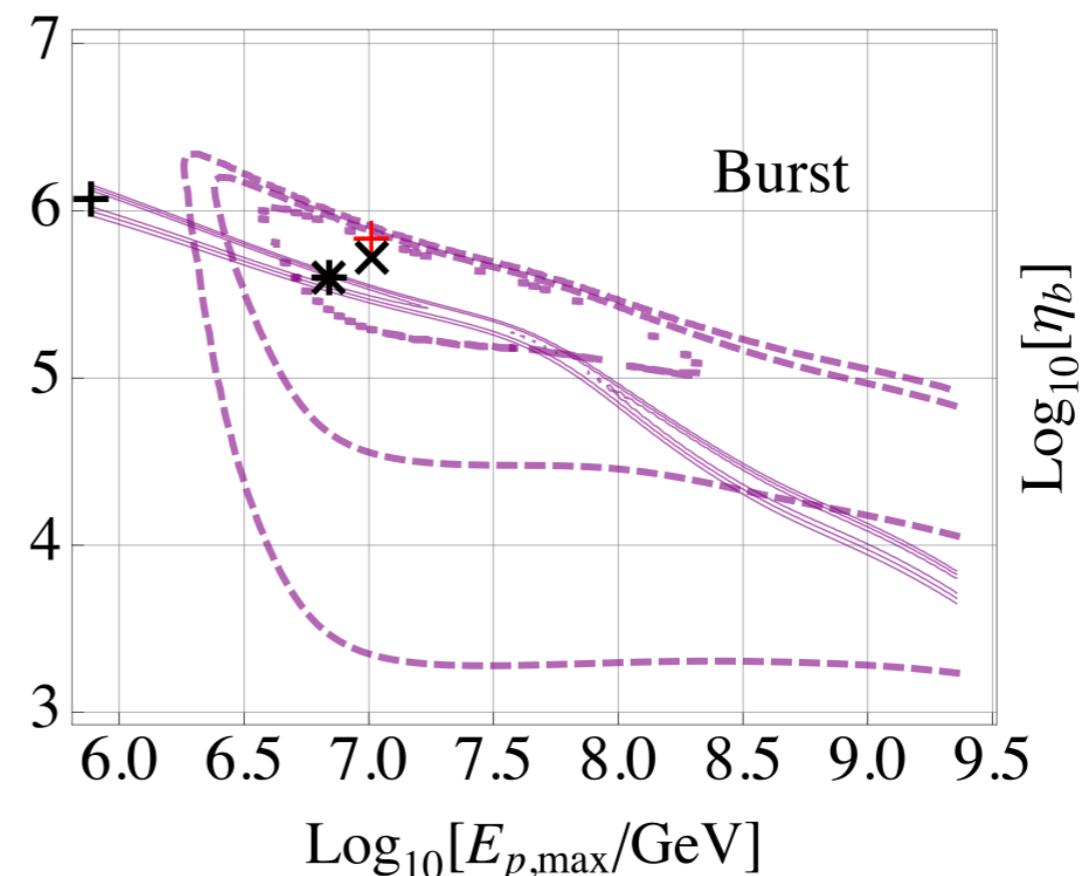
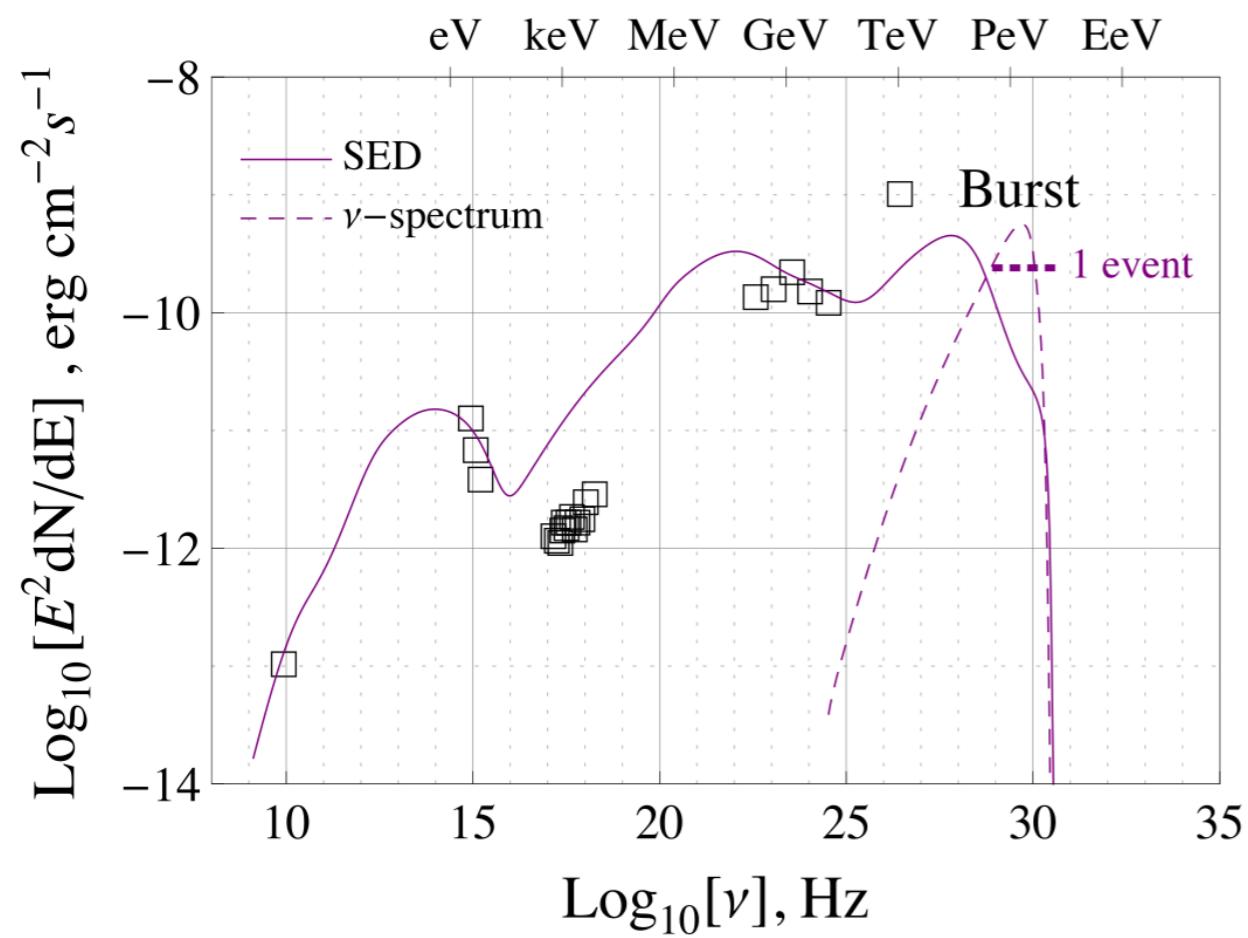


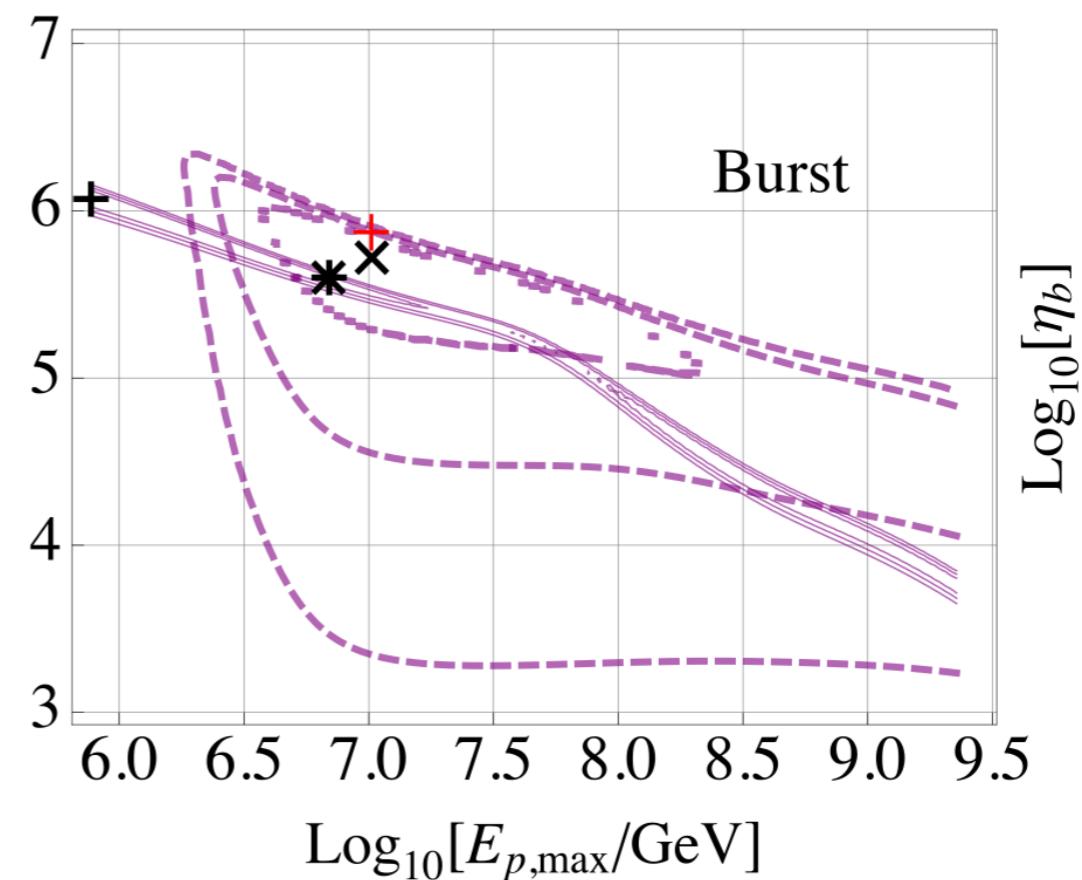
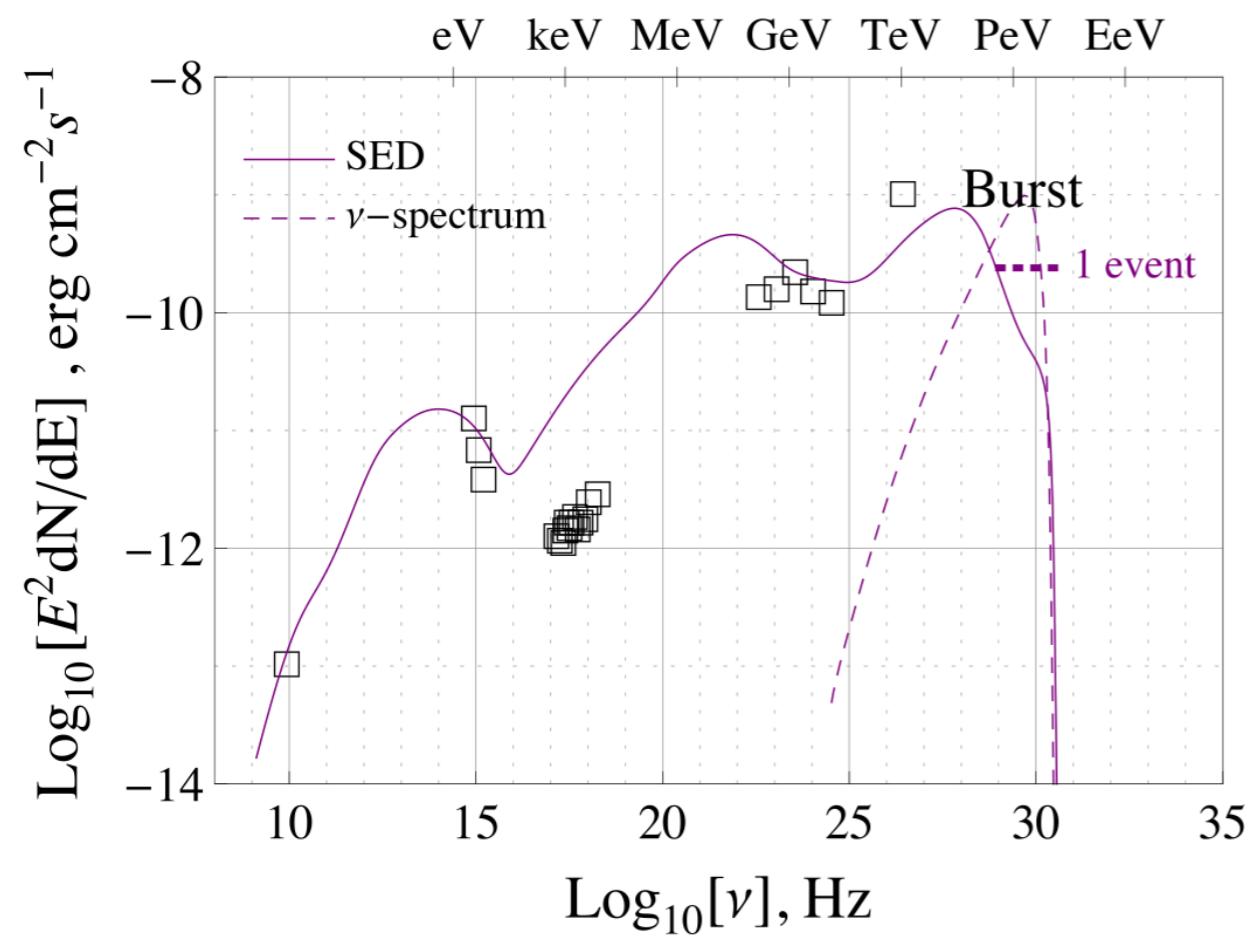


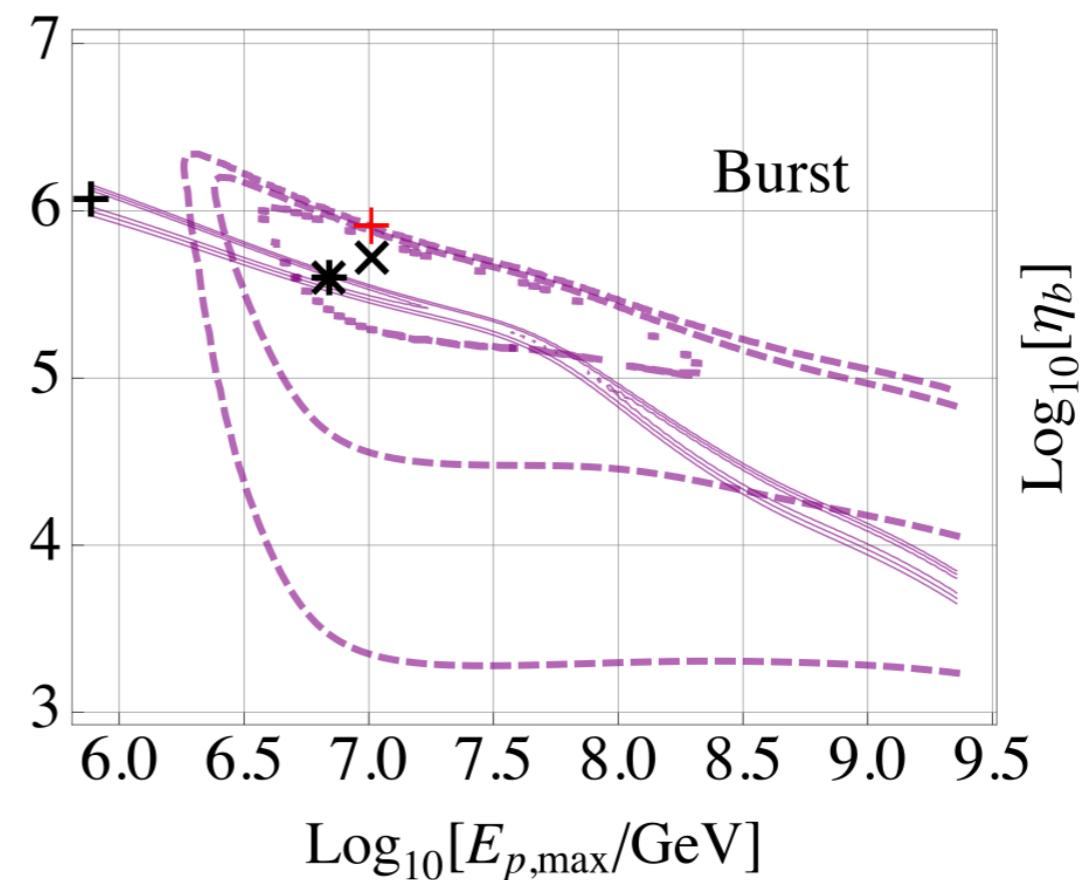
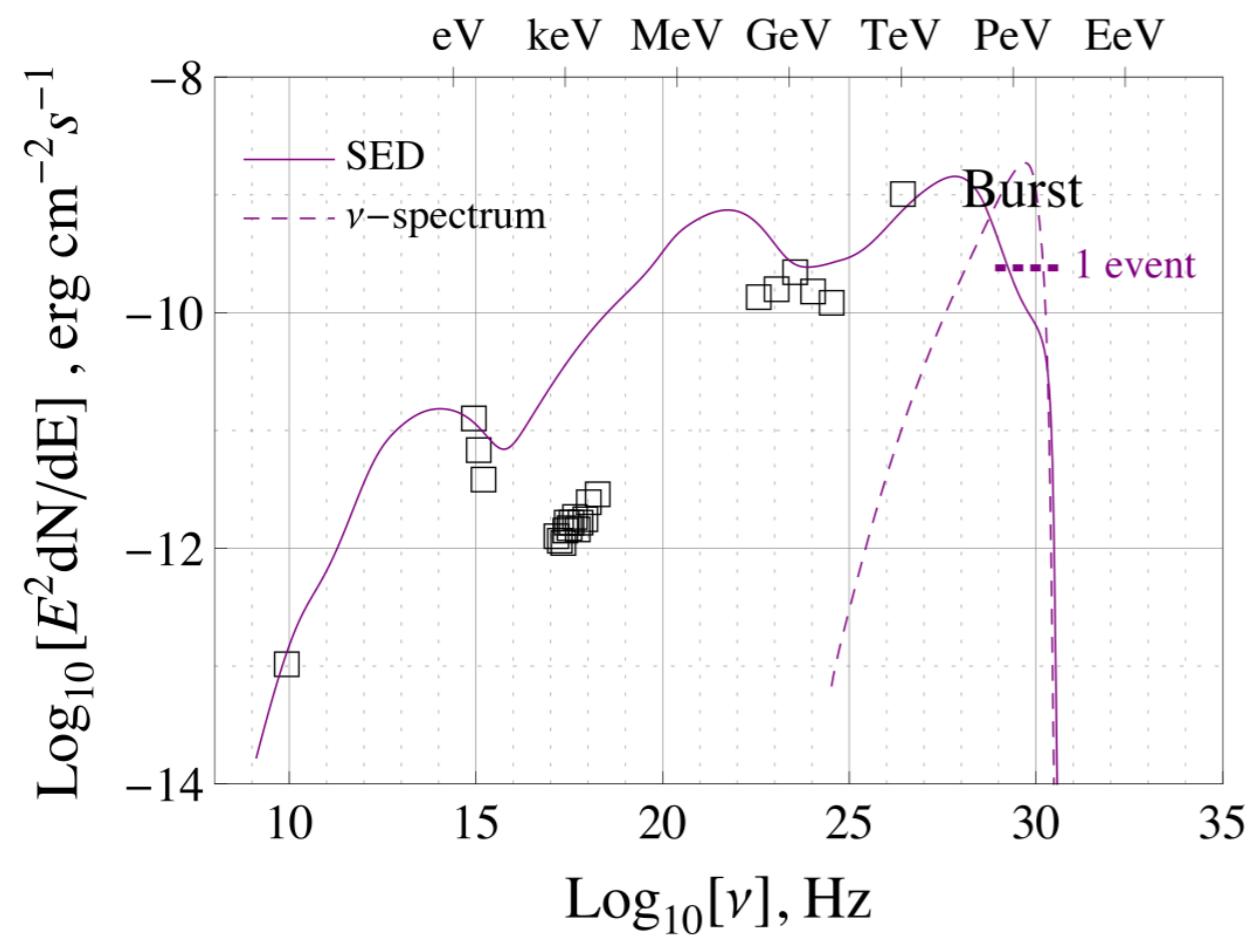


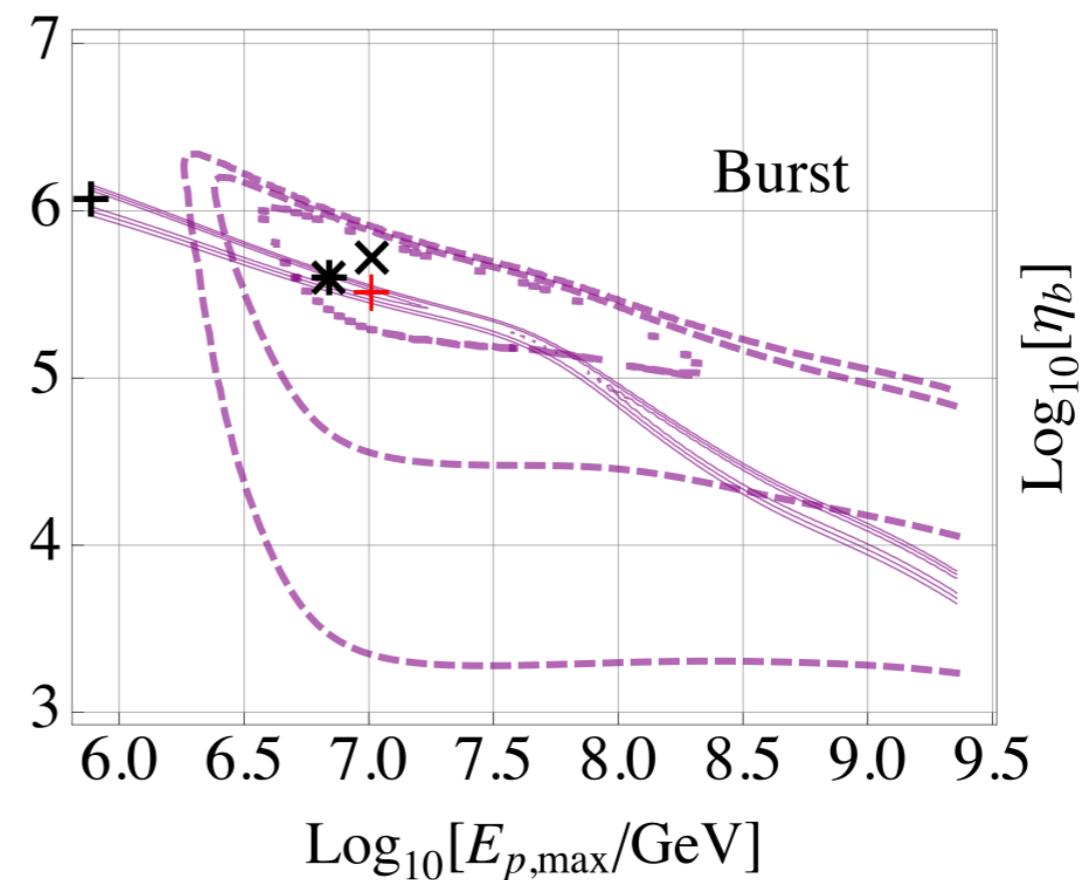
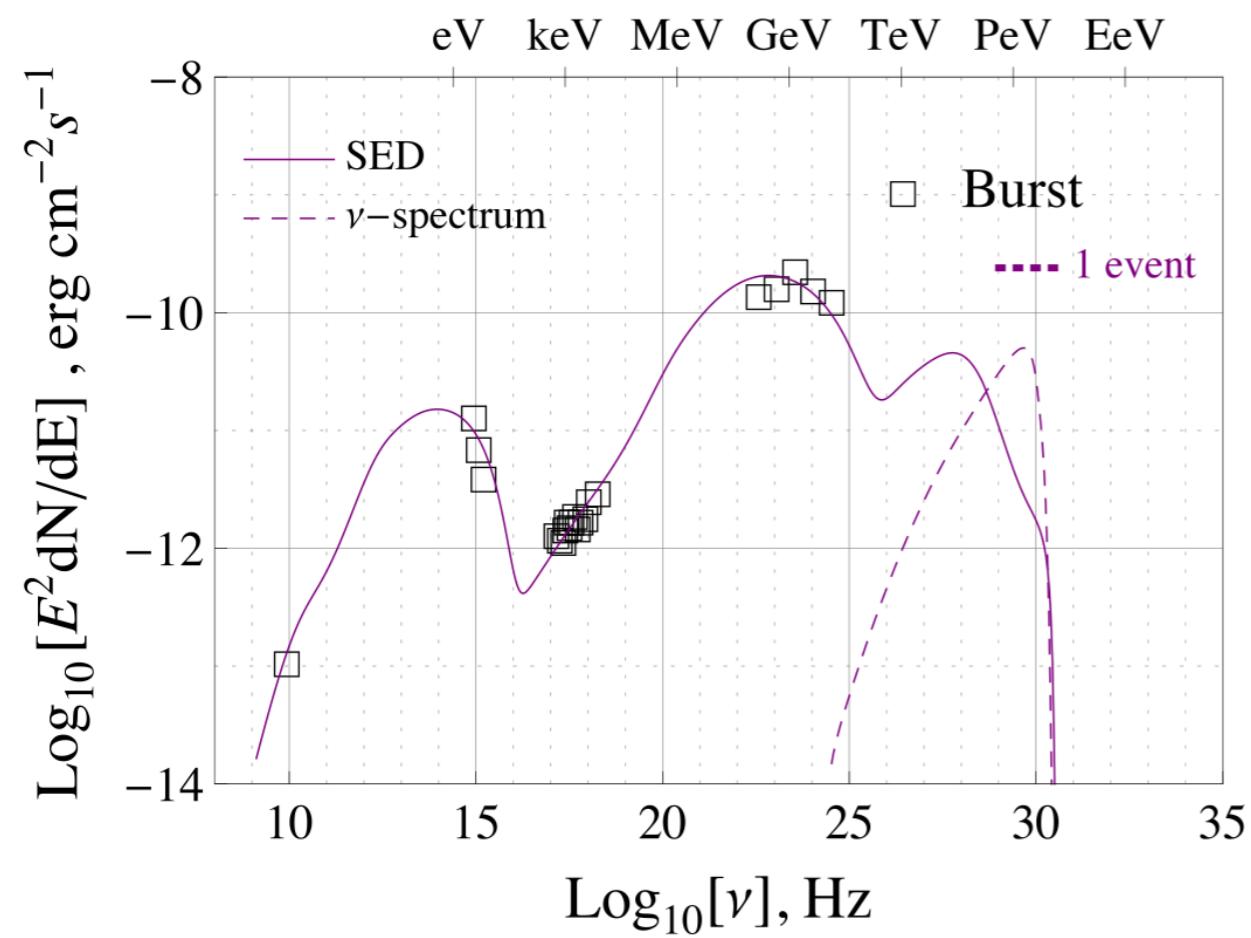


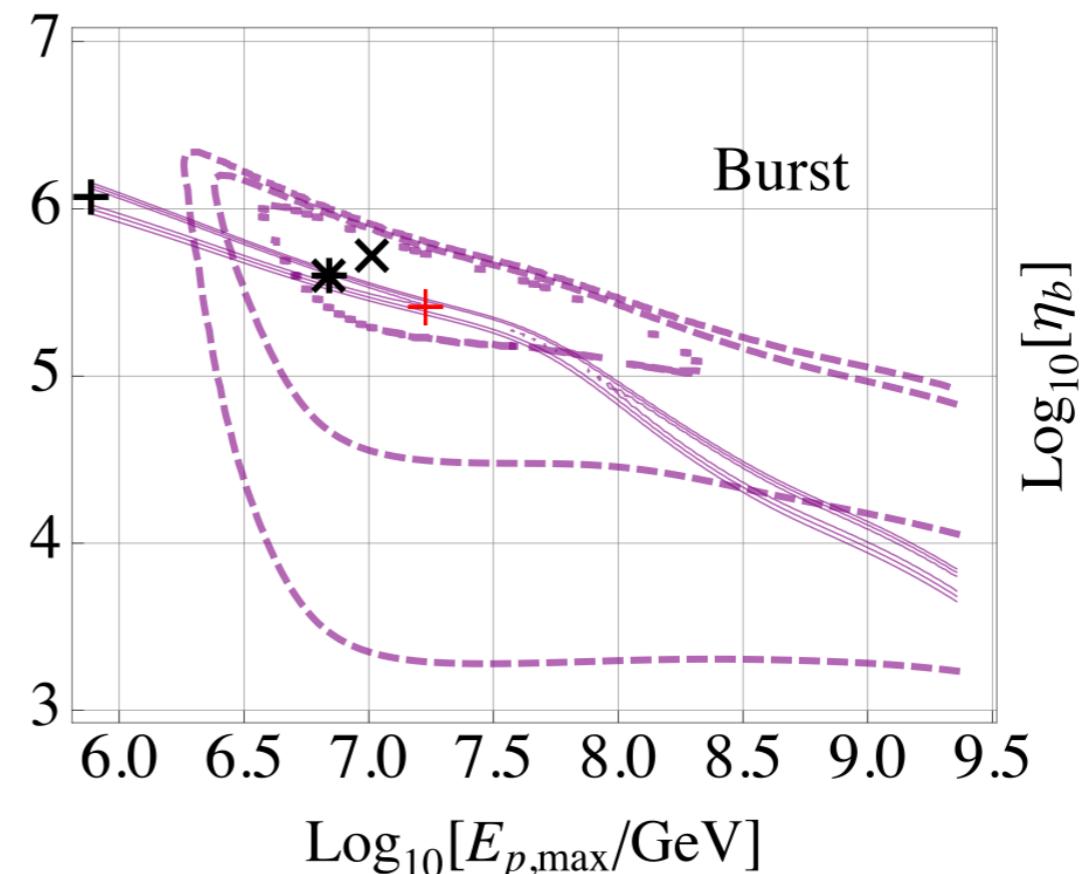
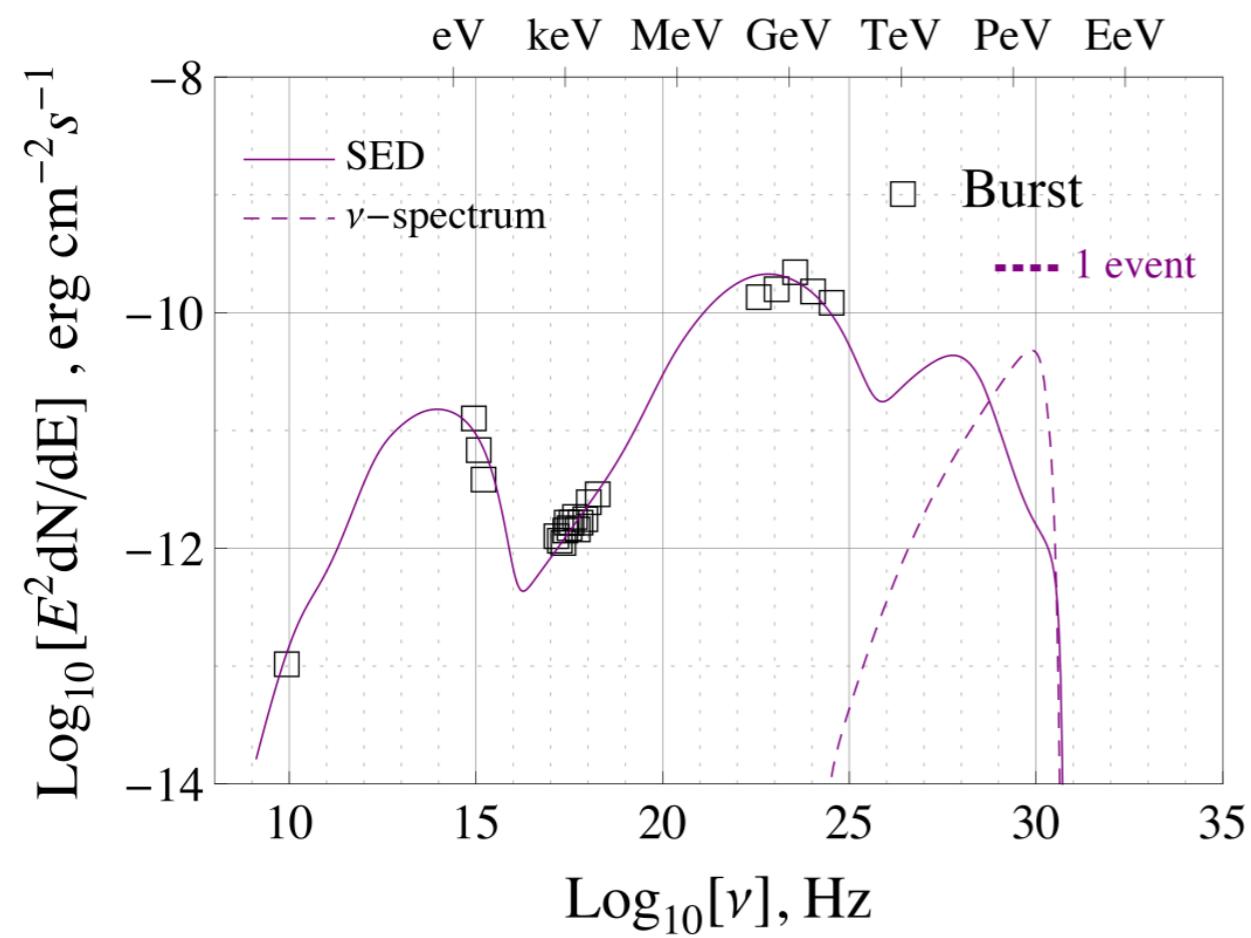


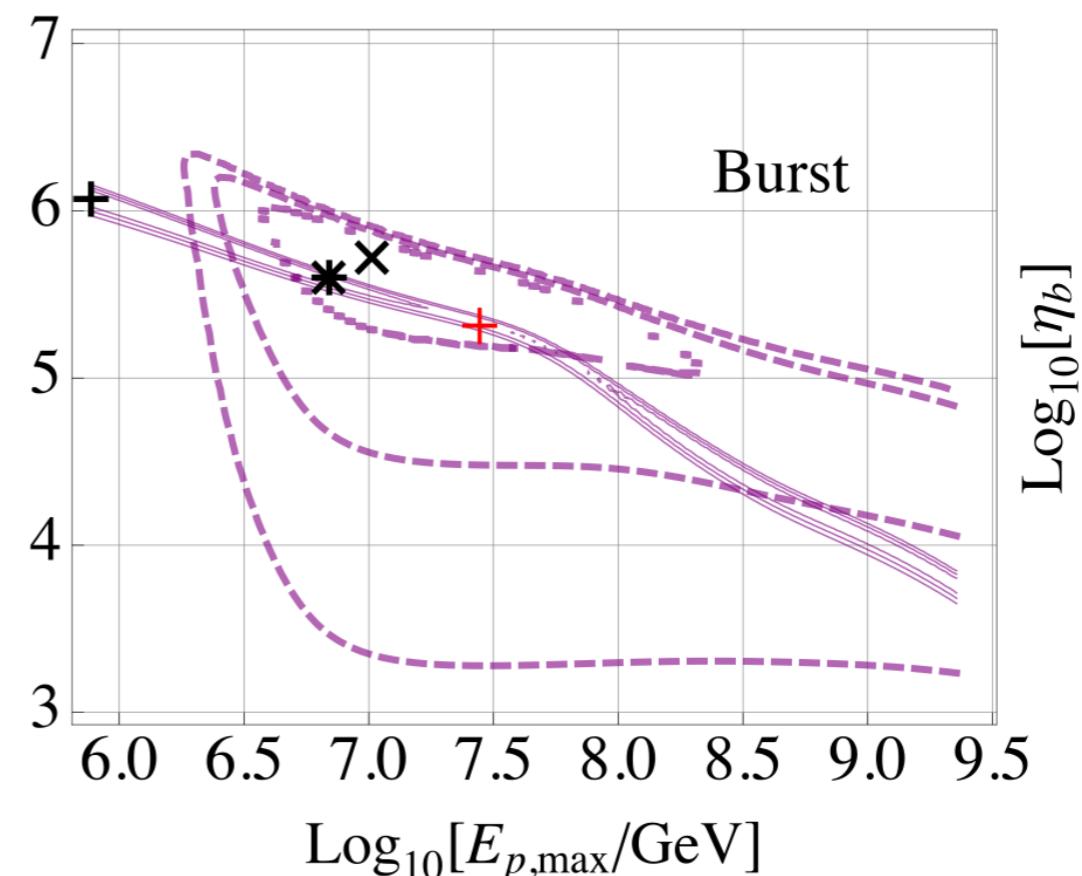
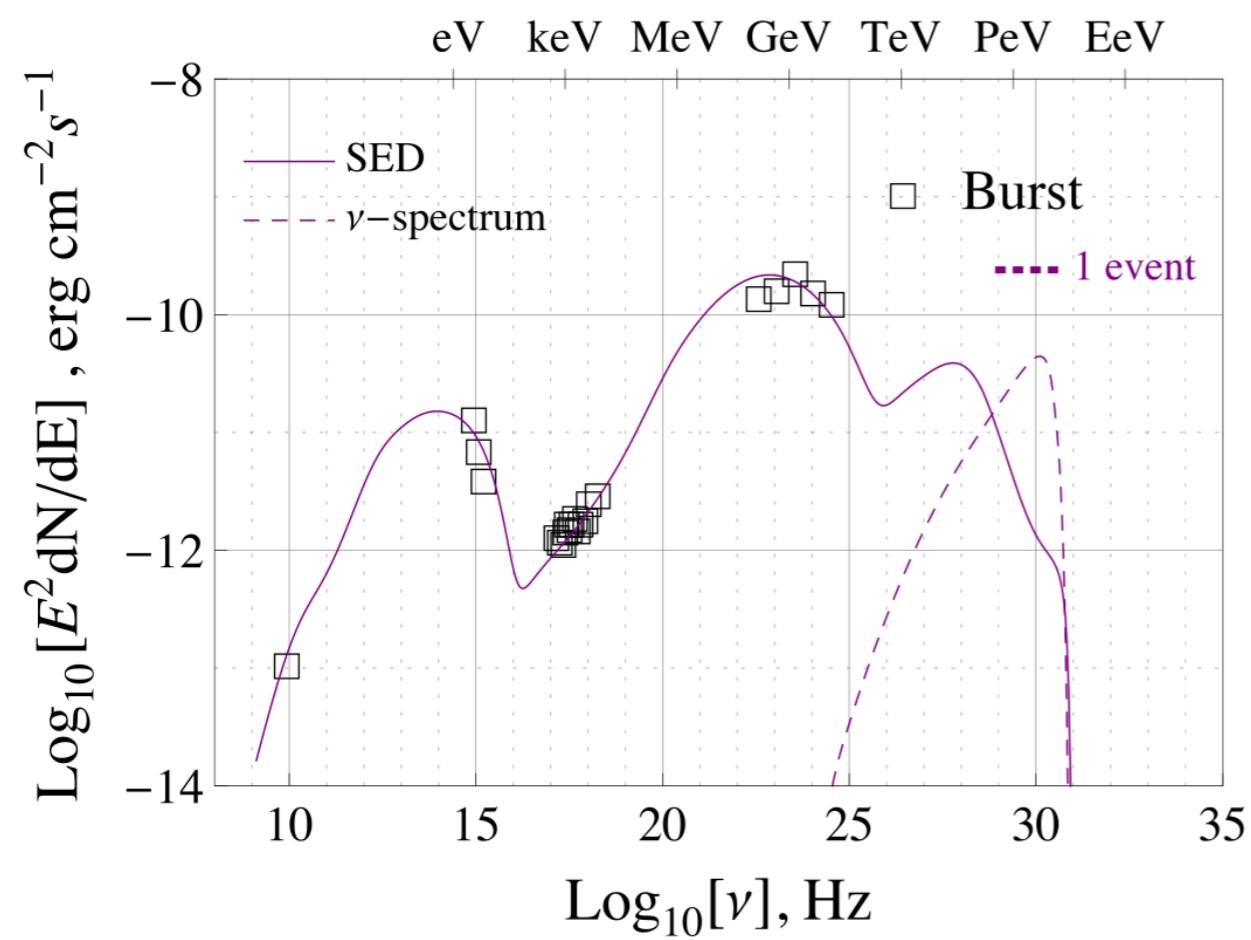


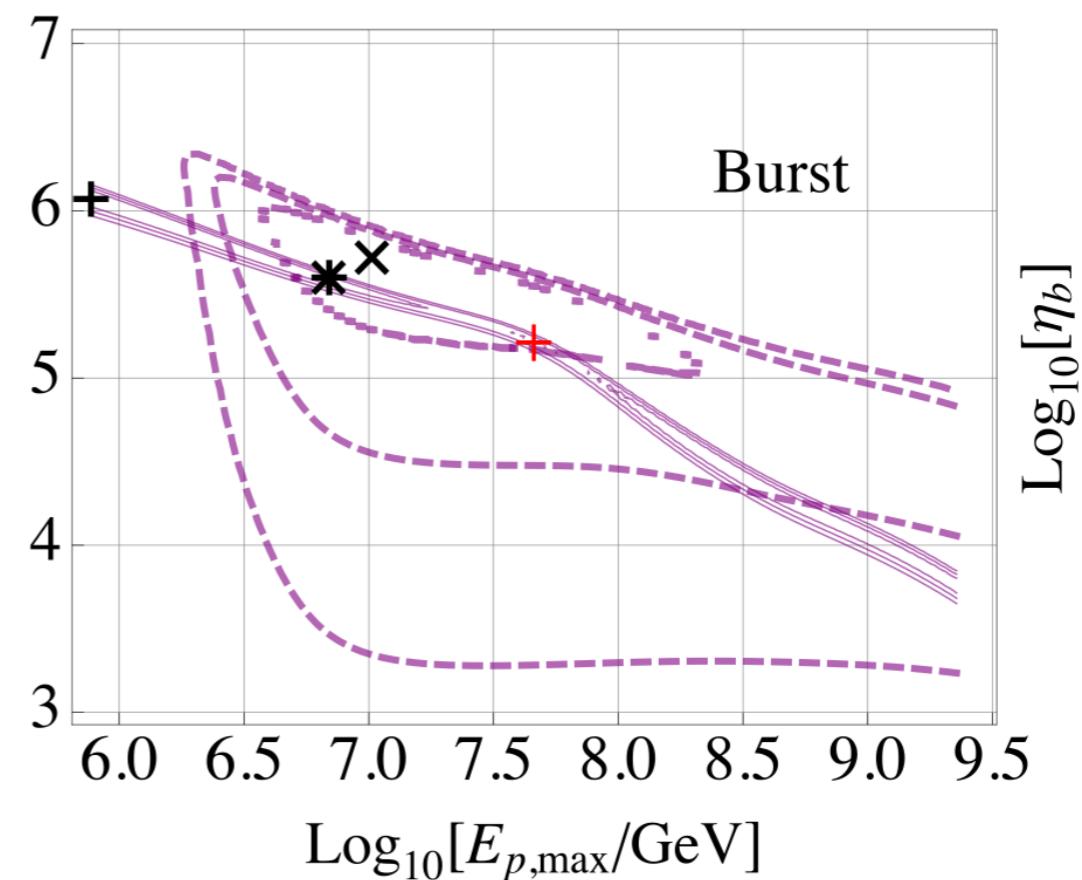
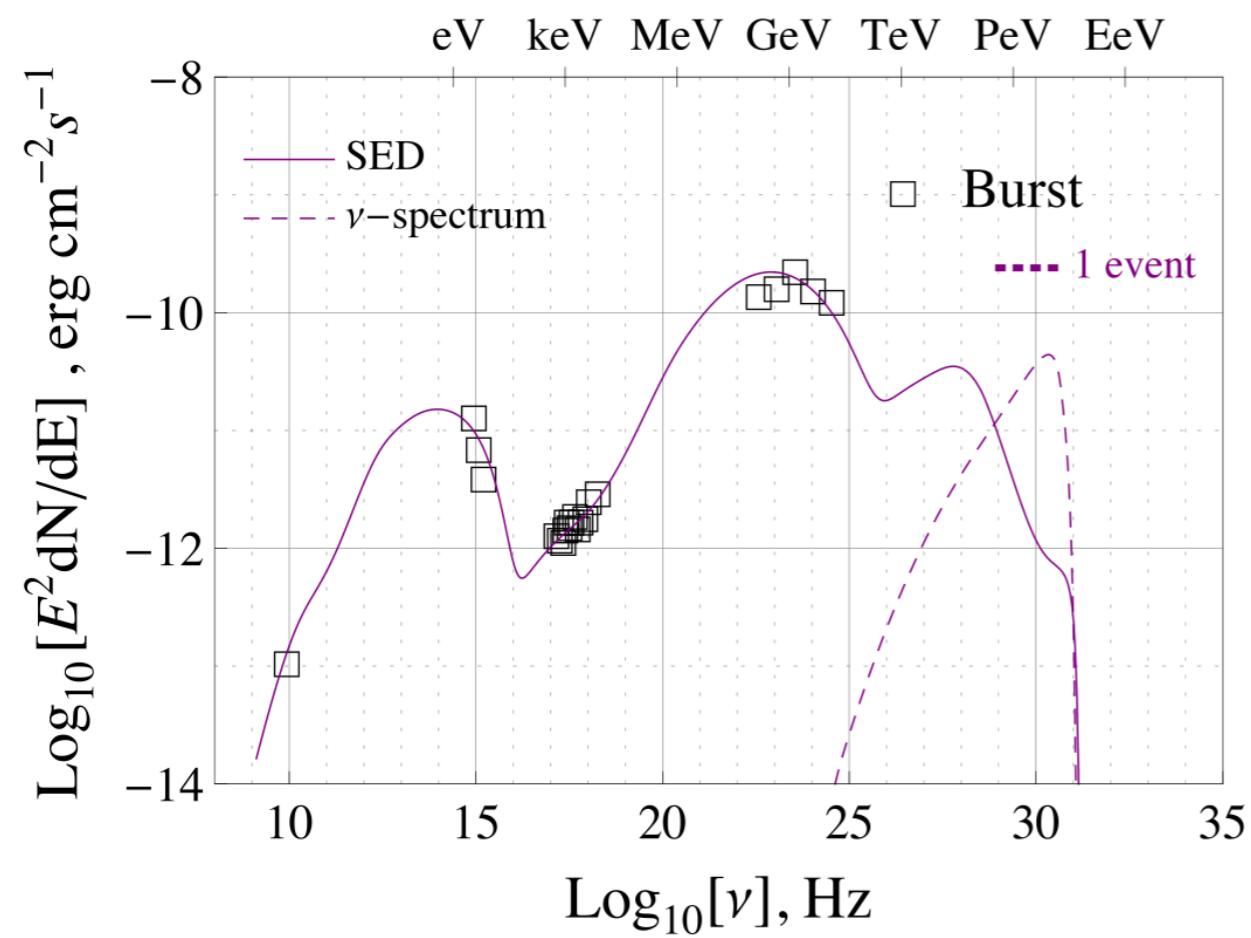


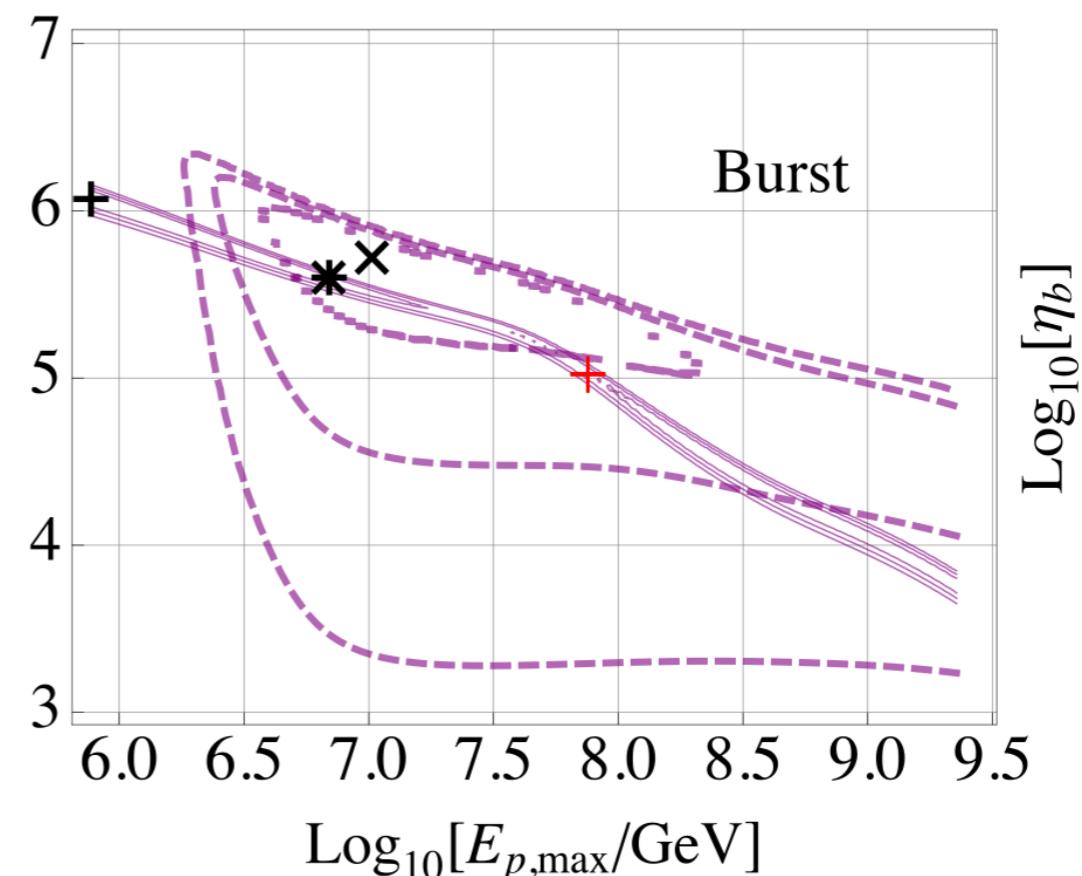
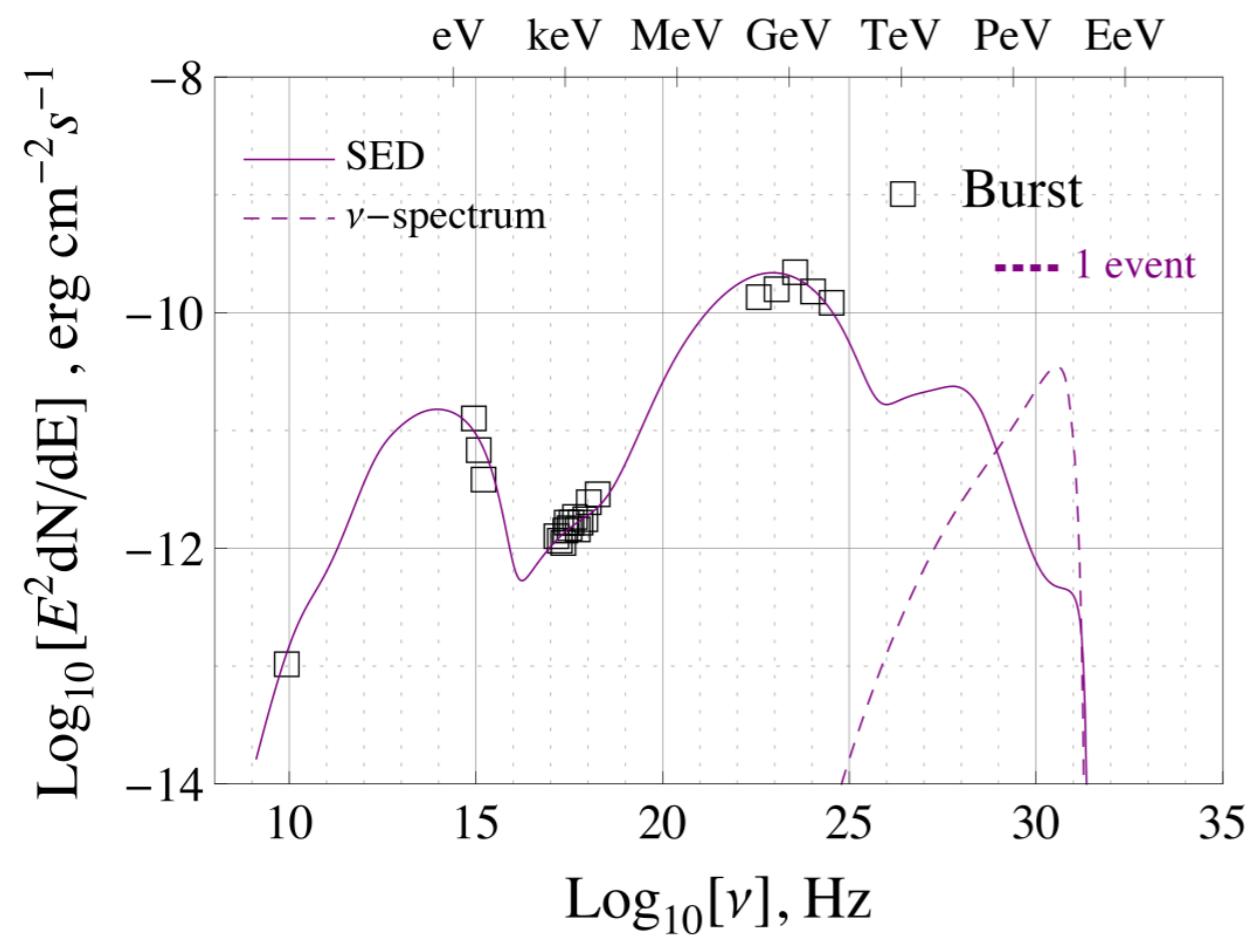


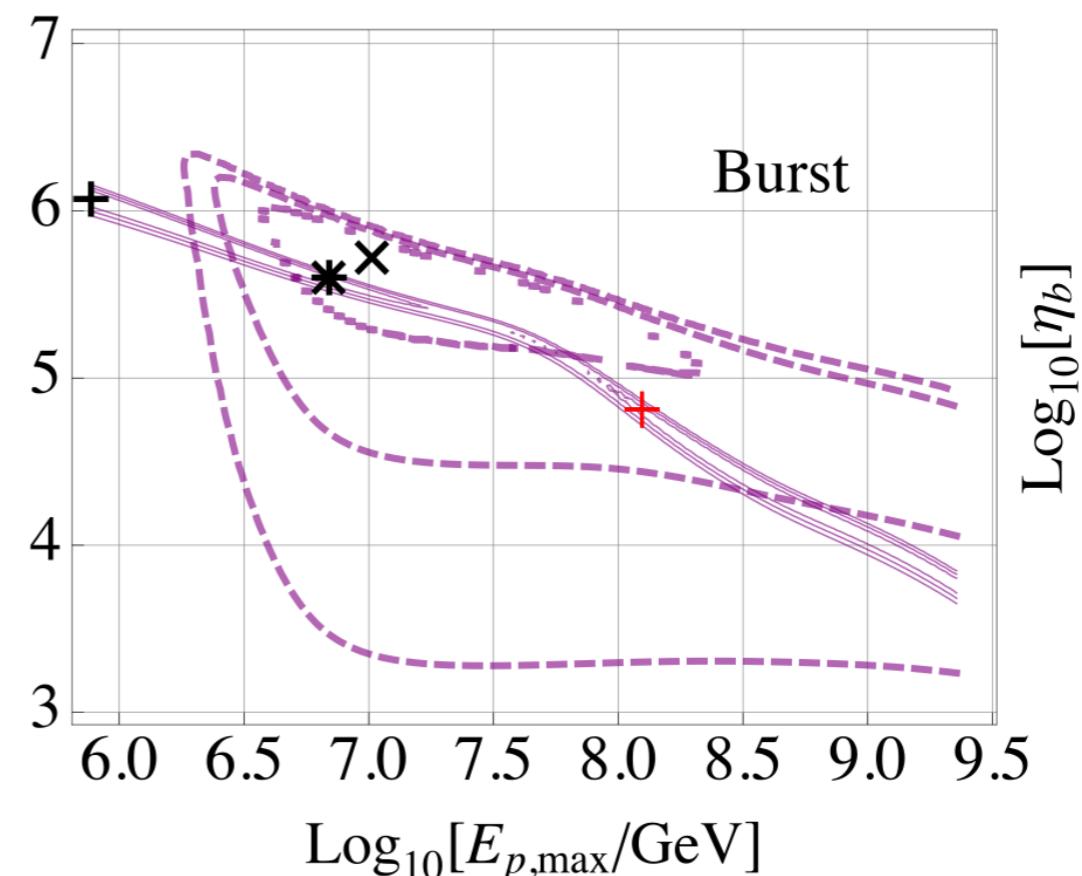
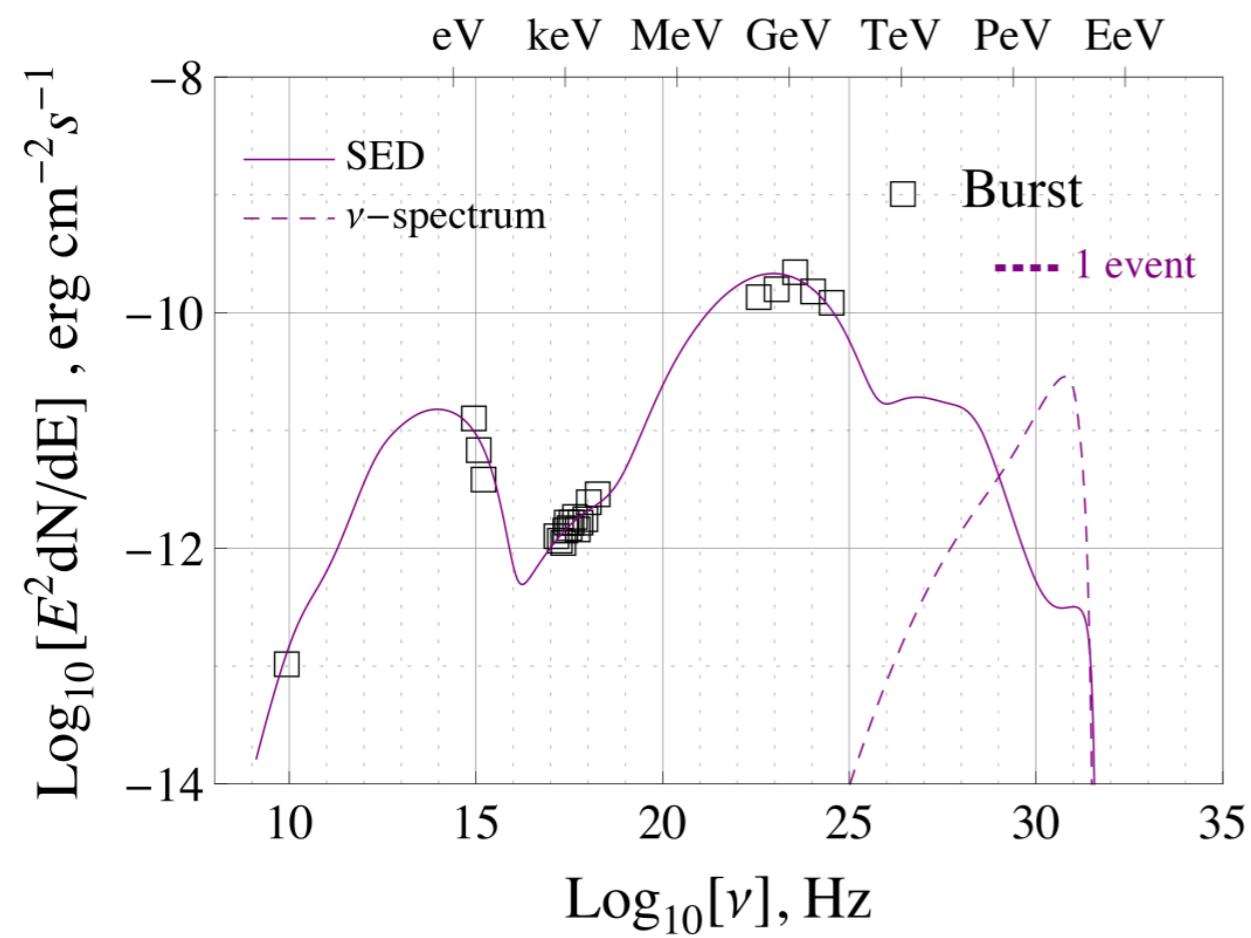


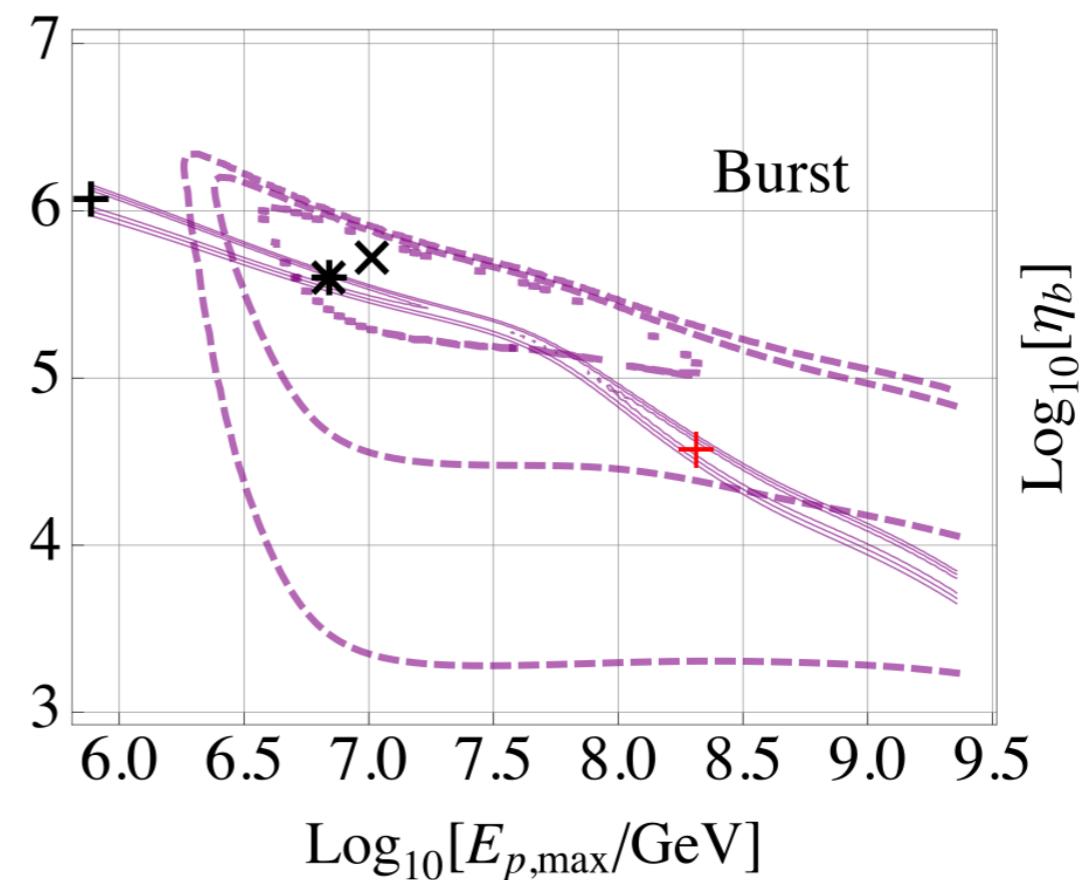
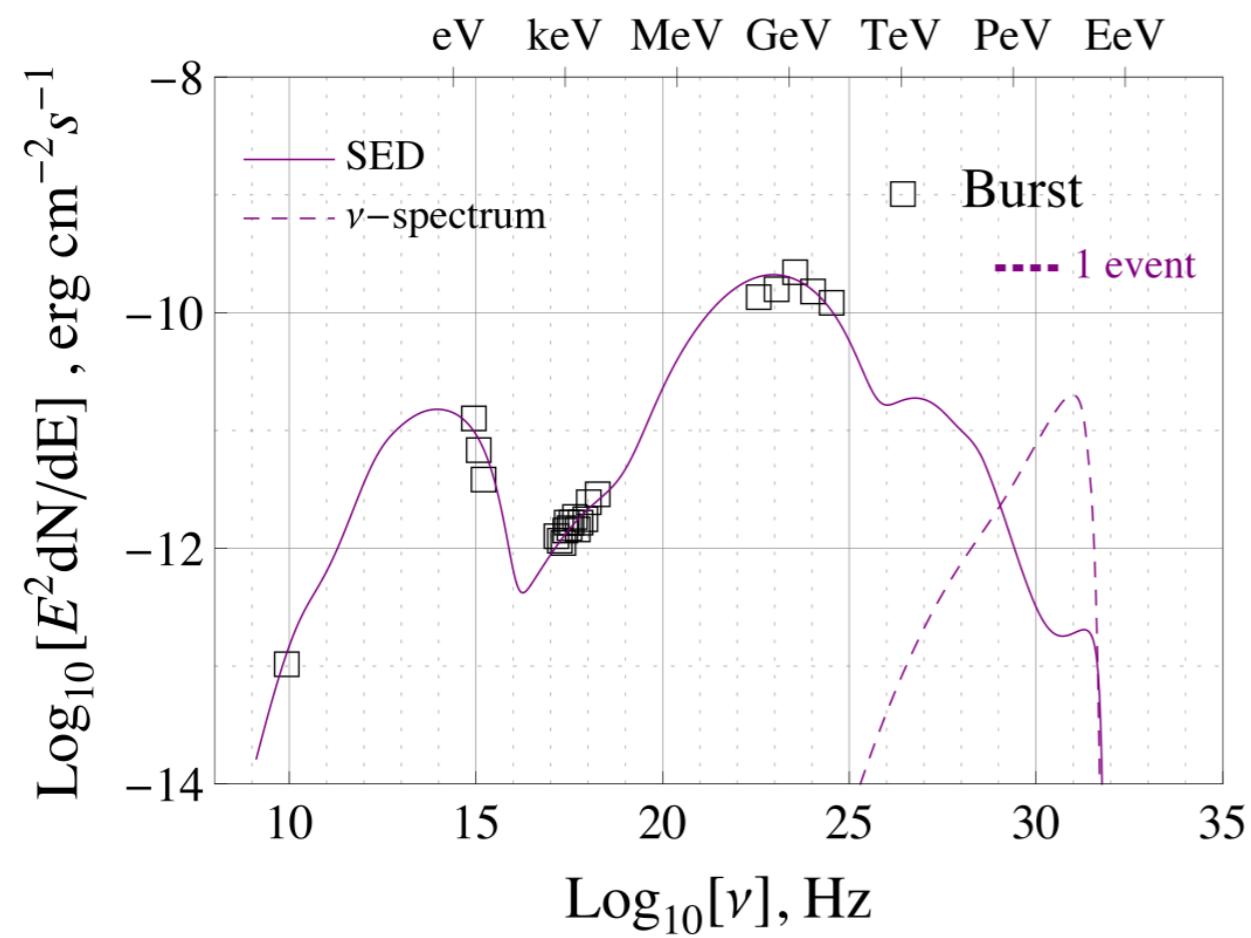


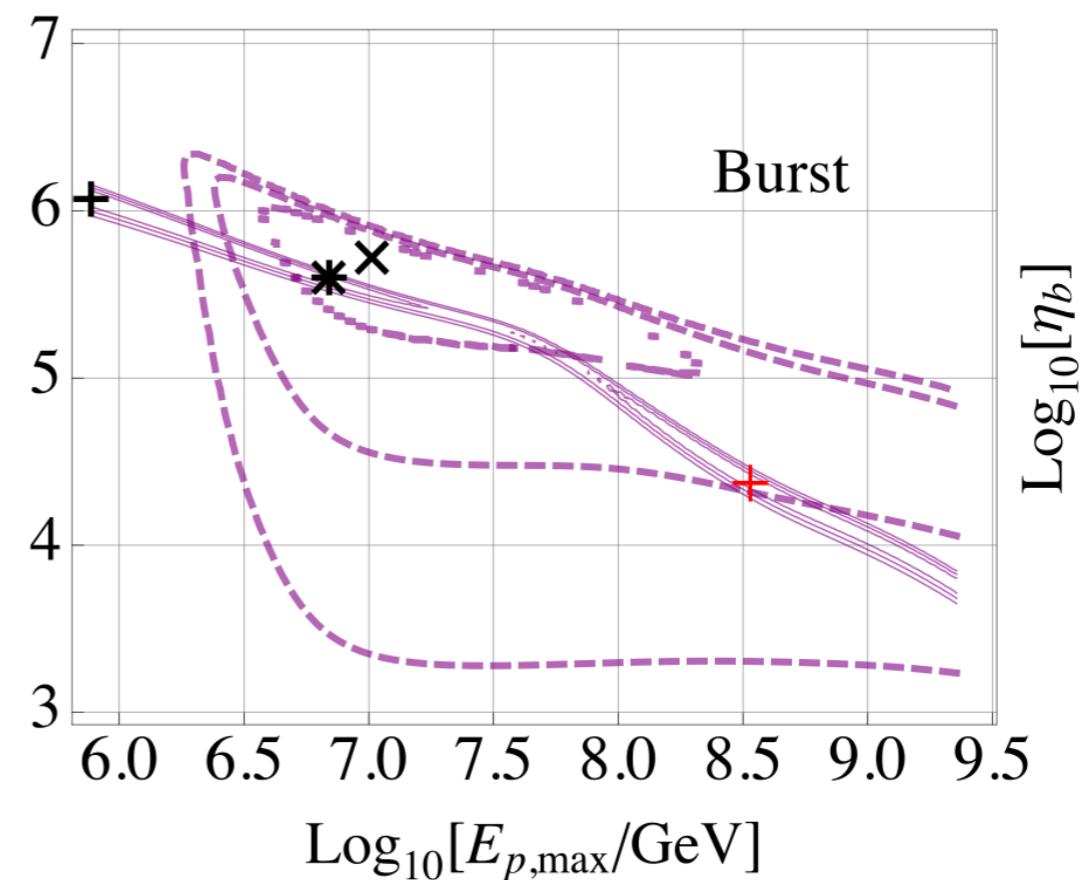
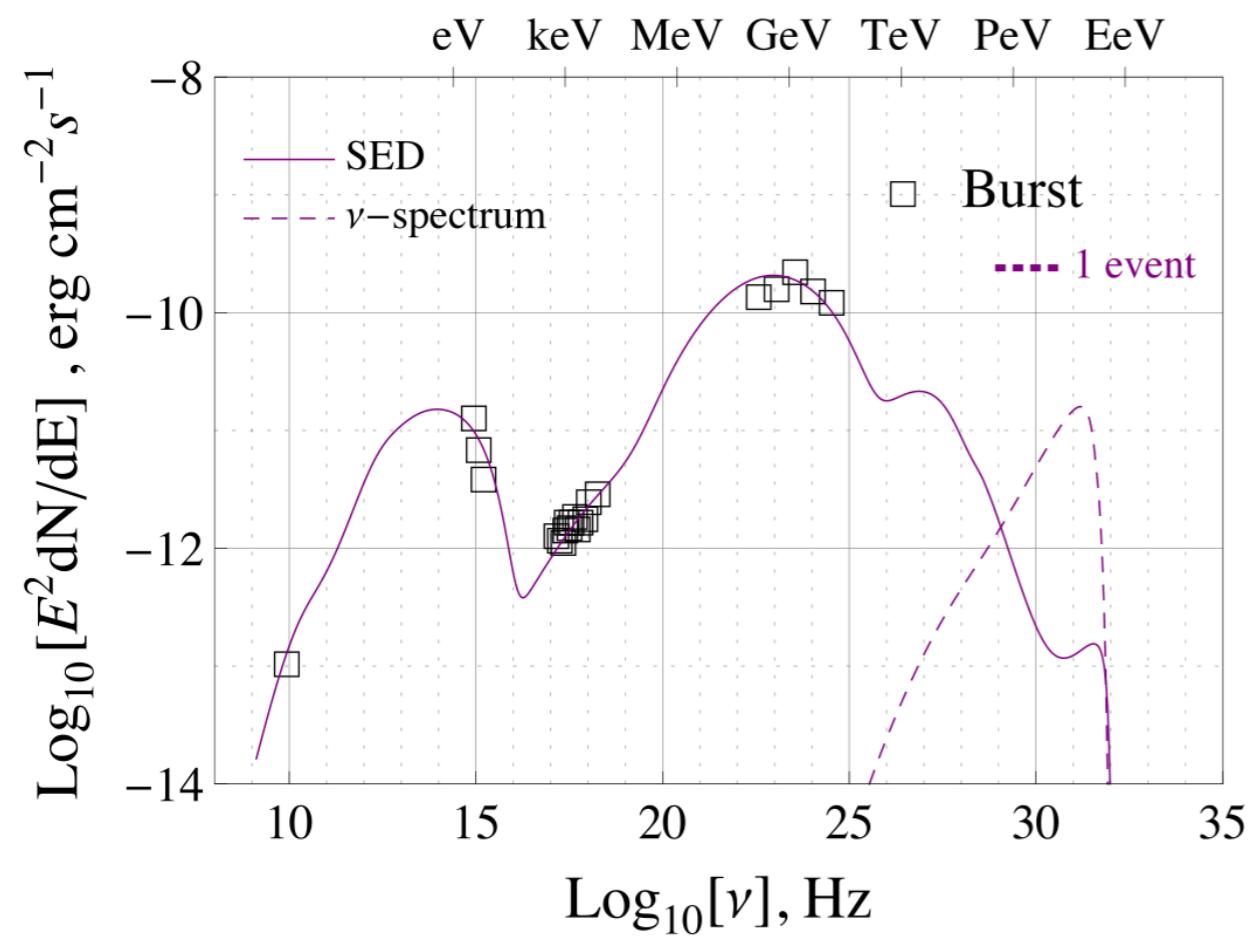


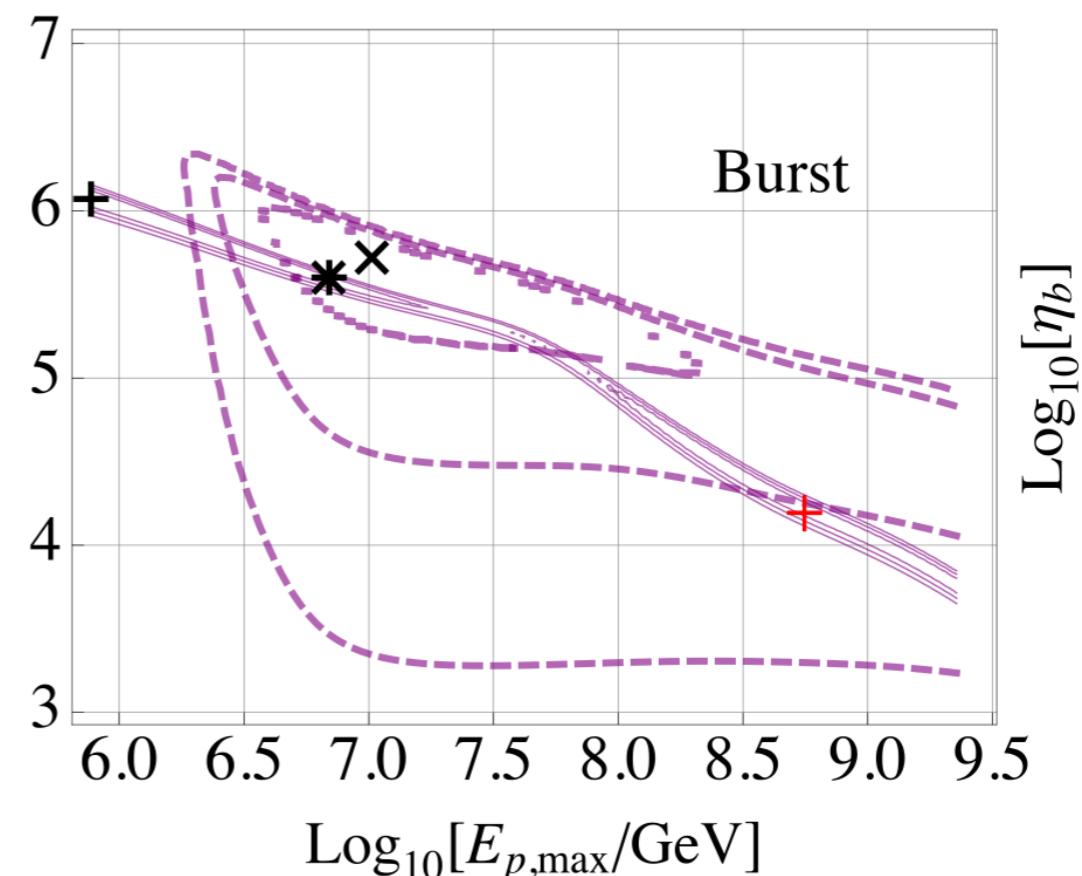
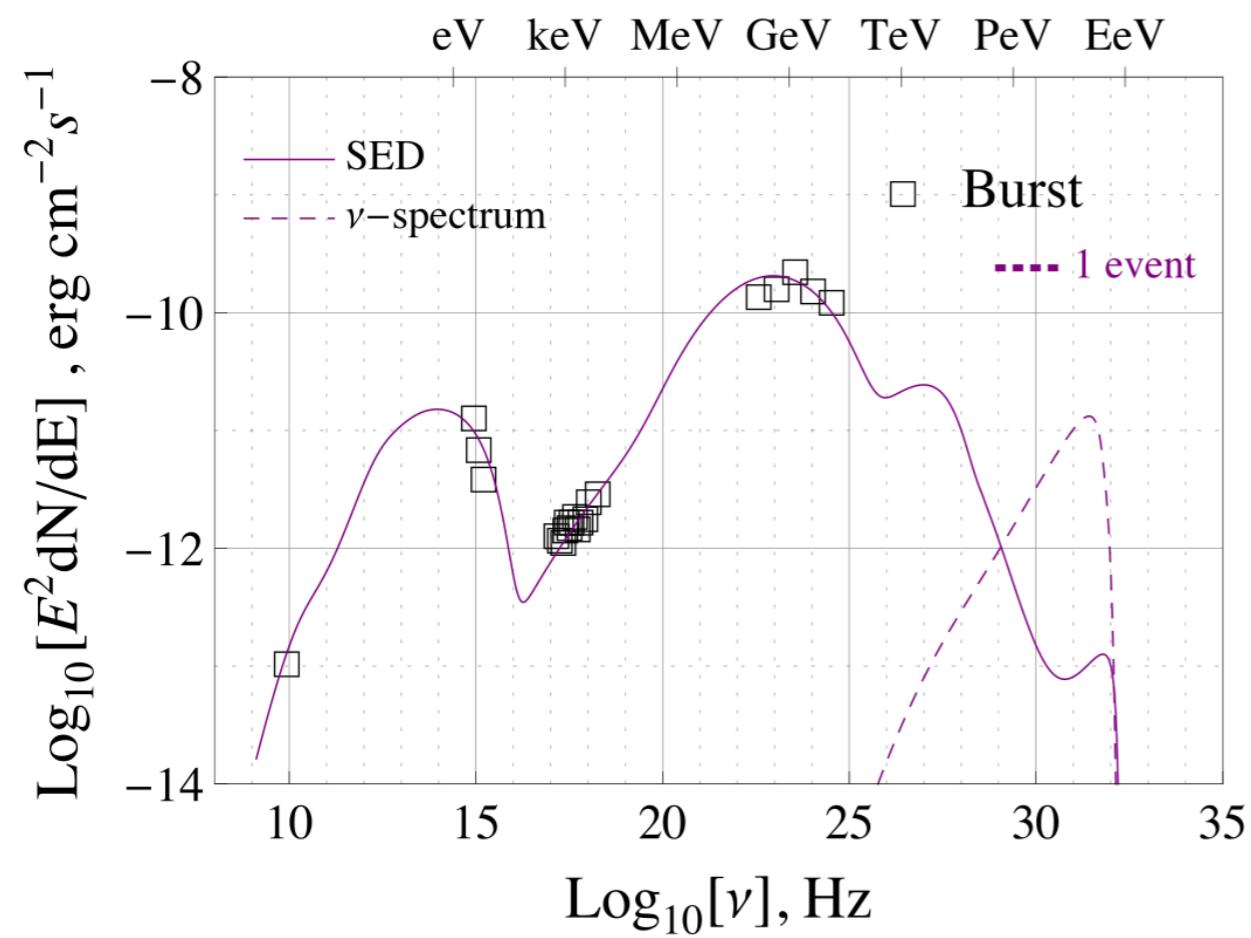


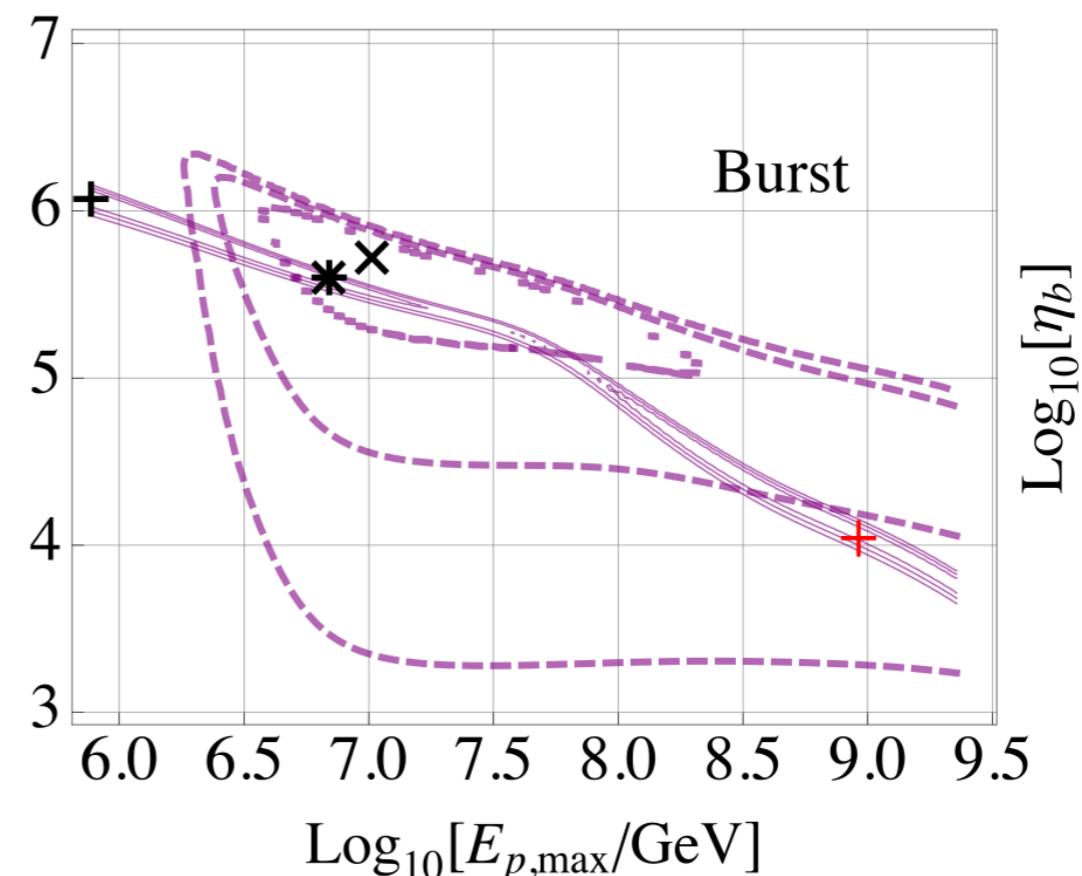
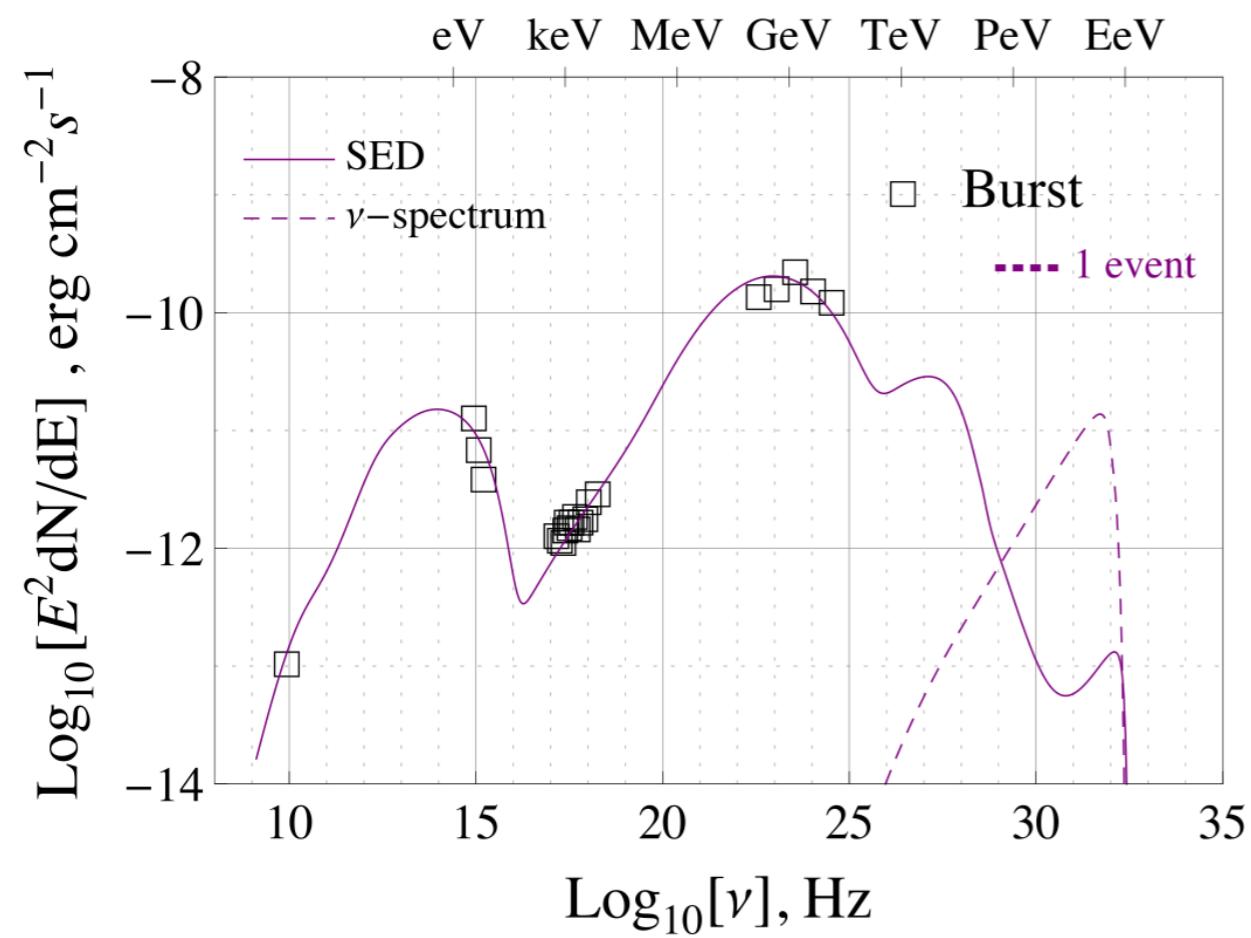


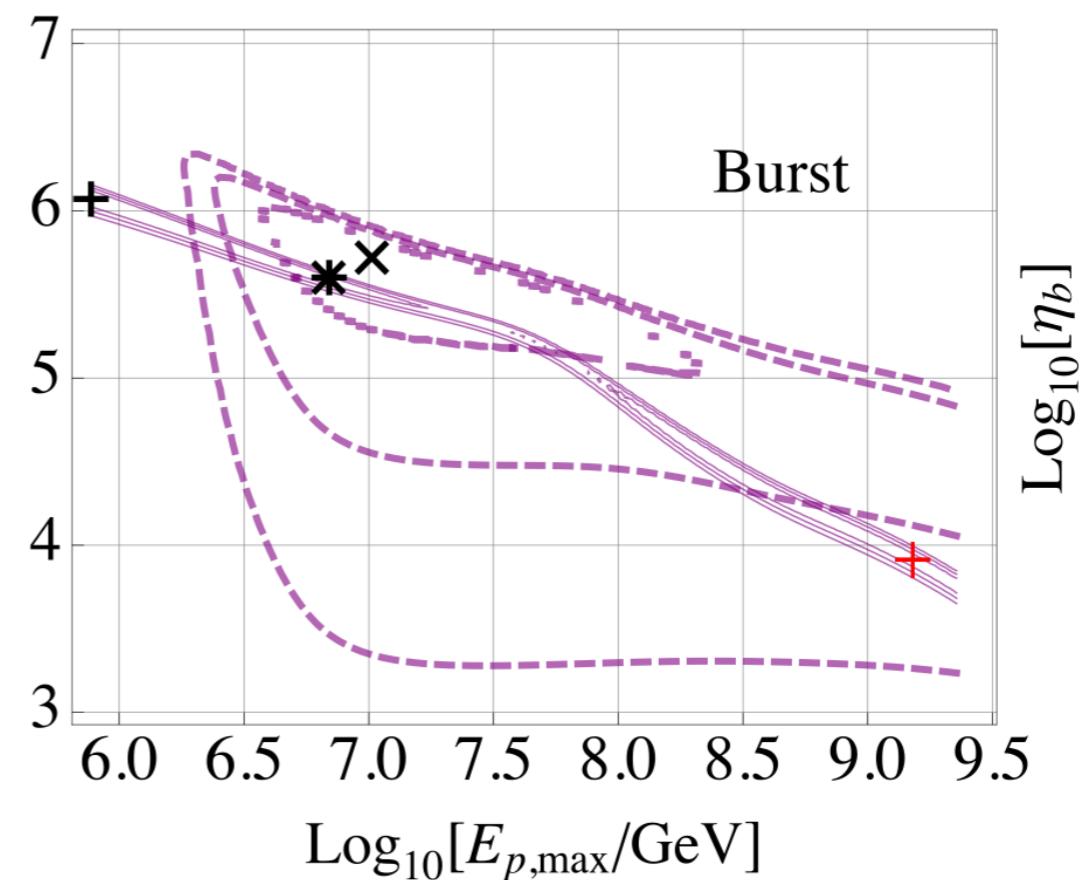
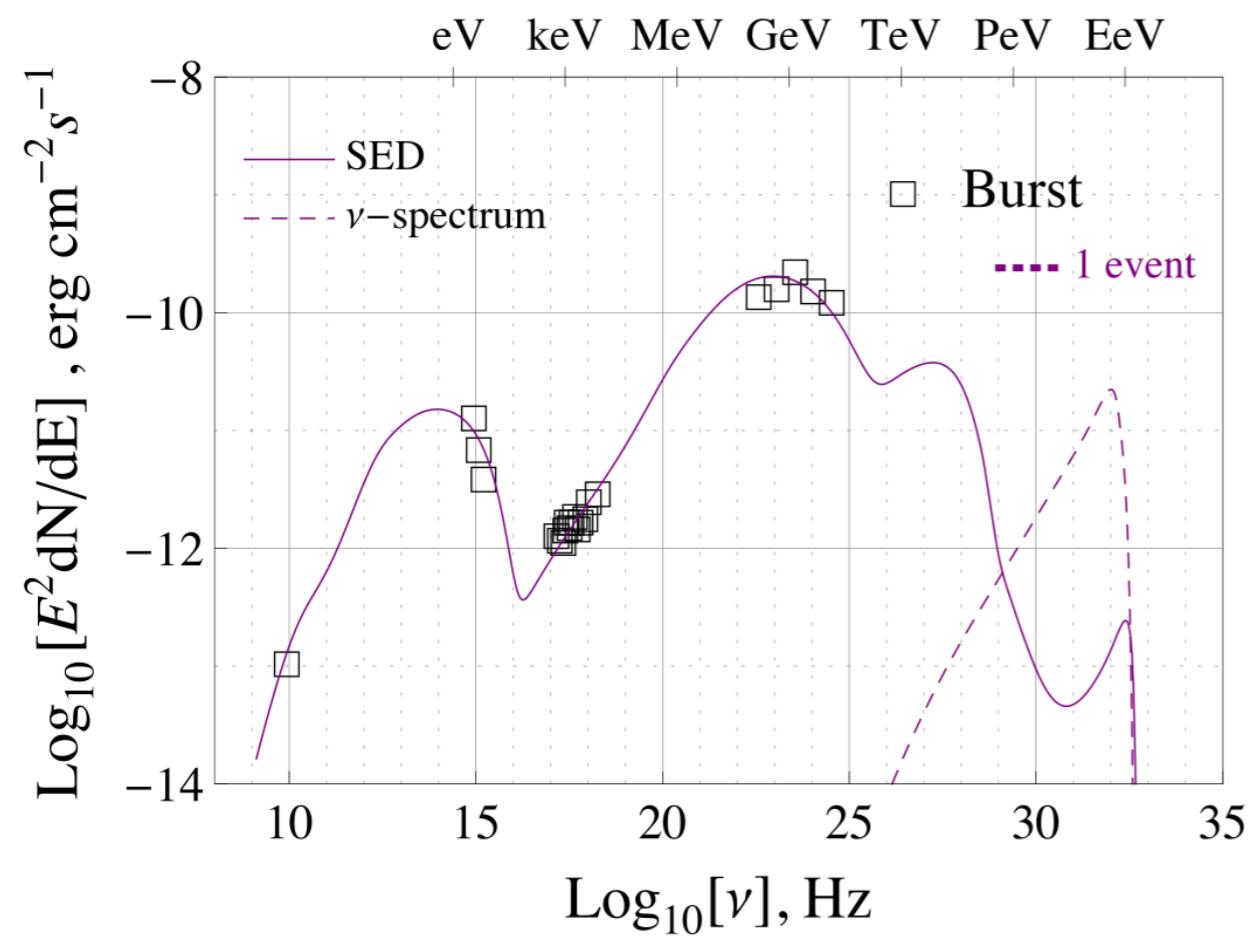


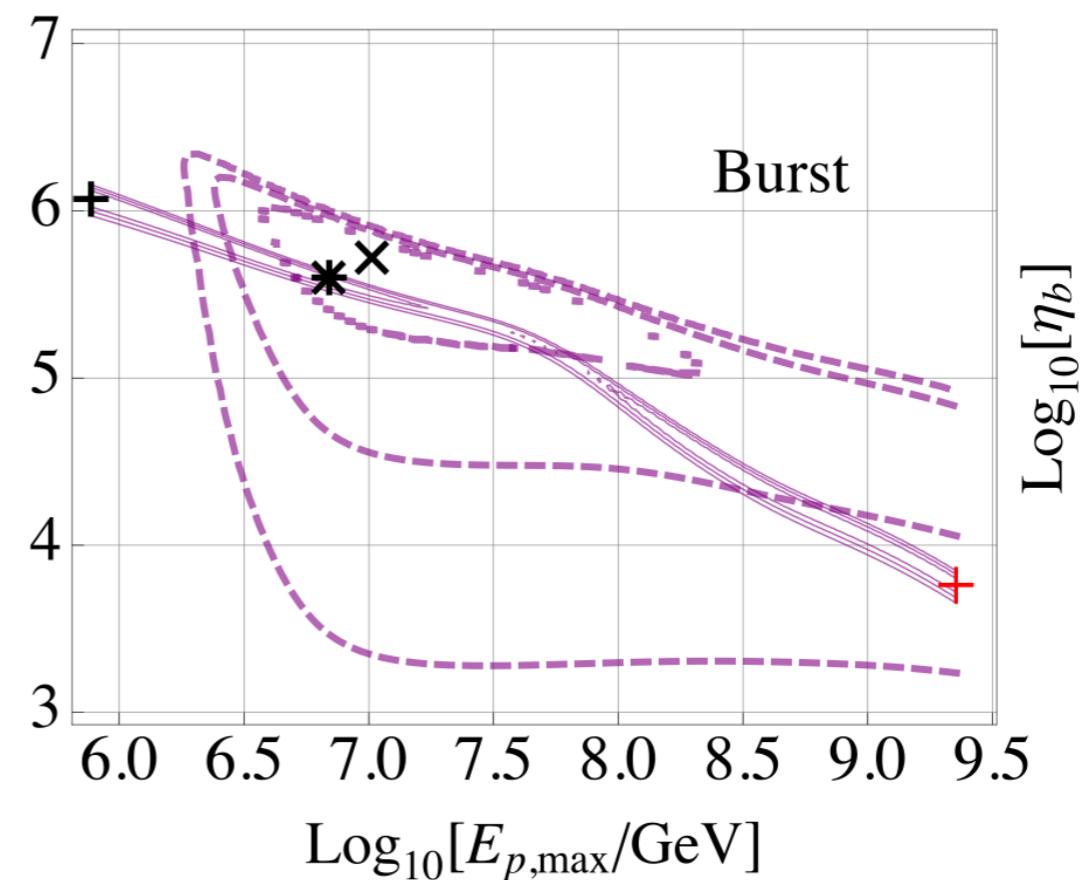
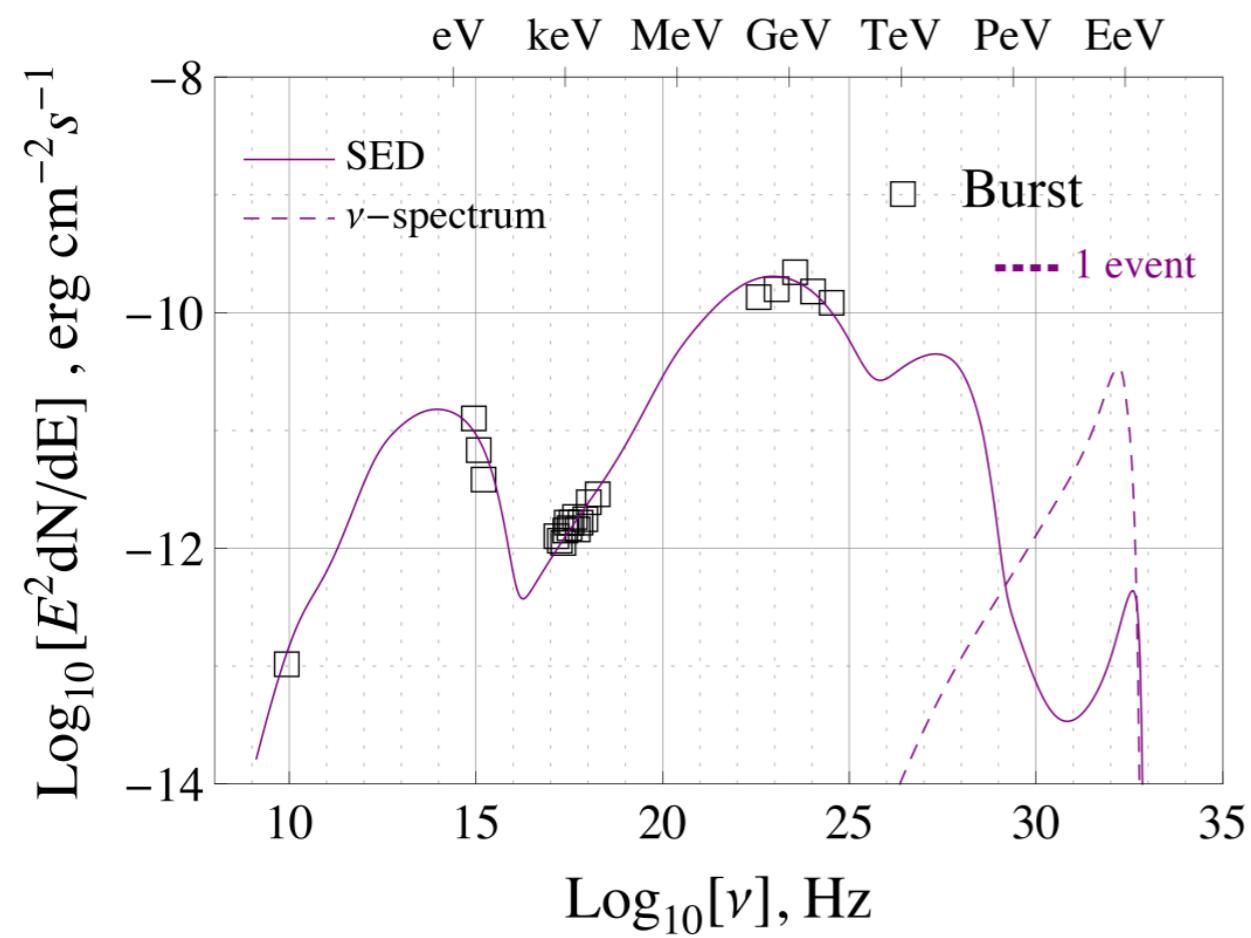




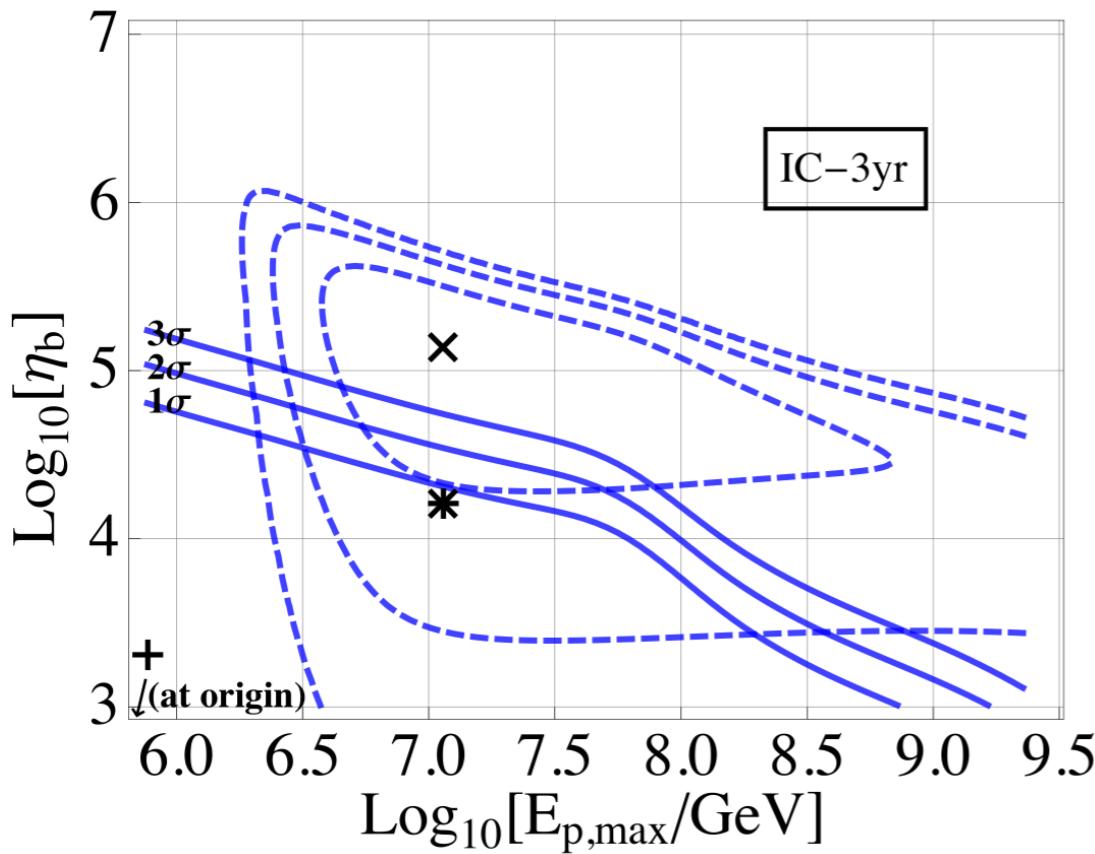




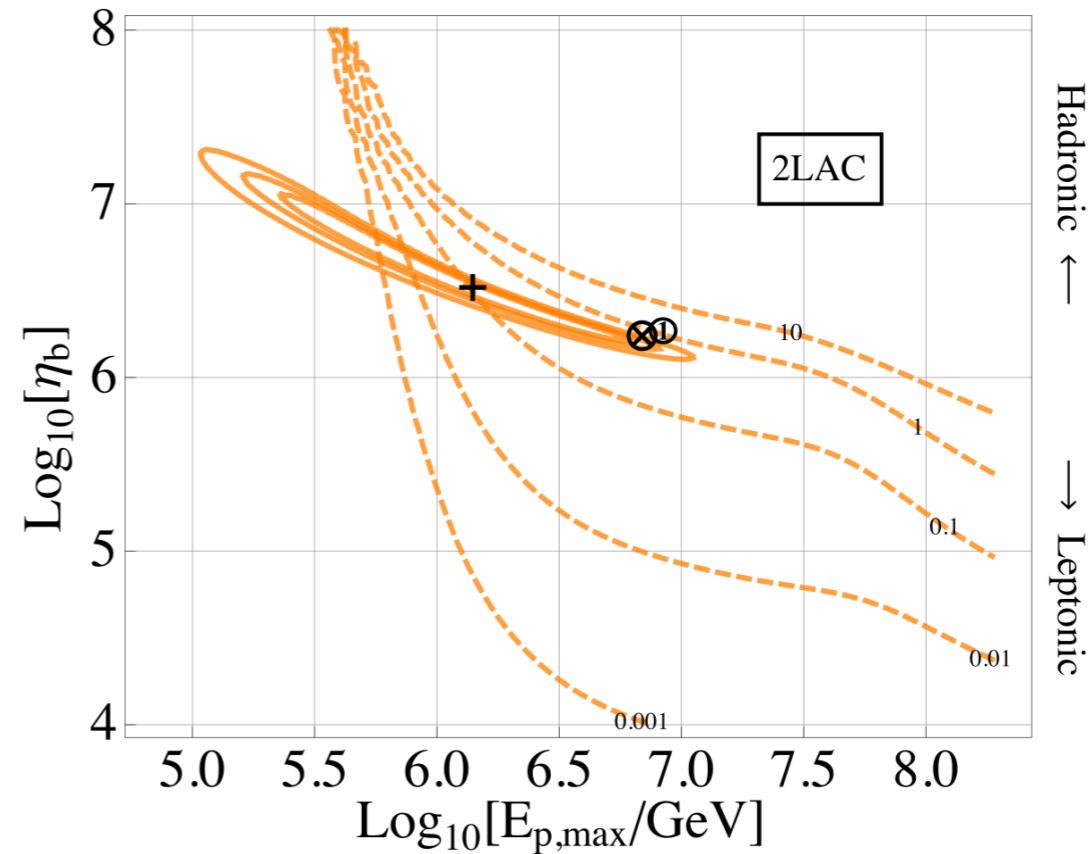




Other phases

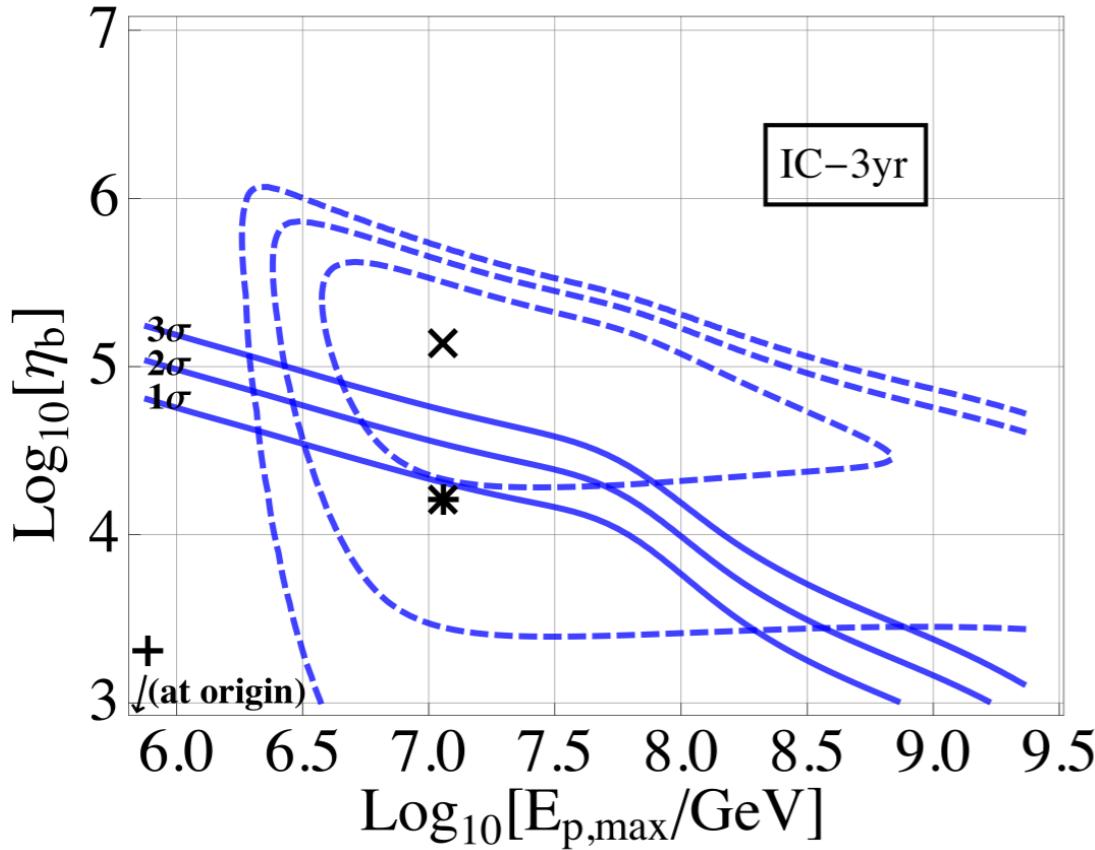


Hadronic \longleftrightarrow Leptonic



Hadronic \longleftrightarrow Leptonic

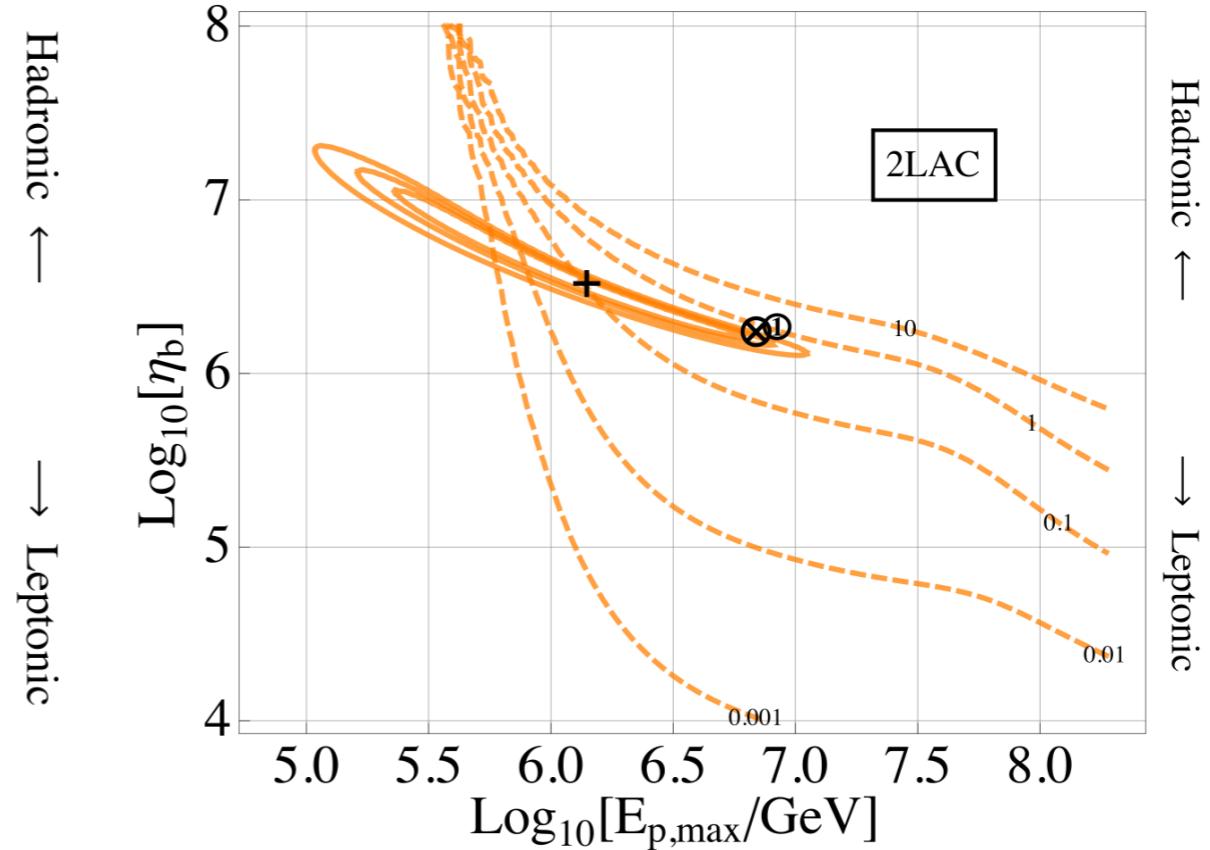
Other phases



SED best-fit: Leptonic SSC

Question of how many protons it can tolerate.

v best fit in tension with SED



IC 40 + 59 strings

No neutrinos

SED best fit consistent with this

Conclusions

- Caution: $L_\gamma \sim L_\nu$ OK for LH π ; Invalid for LHs or LH-SSC models — additional correction factor from theory.
- Degeneracy is large; $\nu +$ more MWL observation breaks it significantly.
- PKS B1424-418: able to reproduce “big-bird” event ($P \sim 5\%$) during both burst & IC-3yr phase.

- backup

Phase	2LAC			IC-3yr			Burst		
Time	2008.9–2010.9			2010.5–2013.5			2012.5 – 2013.5		
$R_{\text{blob}}/\text{cm}$				7.5×10^{17}					
Γ_{bulk}				35					
B'/mG	3.0			3.7			2.5		
$L_{\text{e,inj}}/L_{\text{edd}}$	5.9×10^{-6}			1.7×10^{-5}			1.7×10^{-5}		
$\gamma'_{\text{e,min}}$	1.6×10^3			1.5×10^3			3.3×10^3		
$\gamma'_{\text{e,max}}$	1.5×10^5			1.1×10^5			1.6×10^5		
$\alpha'_{\text{e,idx}}$	-2.2			-2.3			-2.1		
$\alpha'_{\text{p,idx}}$				-2.0					
Fit symbol	+	\otimes	①	+	*	\times	+	*	\times
Fit	SED	Tab. 2	Tab. 2	SED	joint	ν	SED	joint	ν
$\eta_{\text{b}}/10^5$	32	17	18	0	0.16	1.3	12	3.9	5.1
$E_{\text{p,max}}^{\text{ob}}/\text{PeV}$	1.67	8.3	10.1	-	13.7	13.7	0.92	8.3	12.4
$N_{\nu}, 0.5\text{--}1.6\text{ PeV}$	0.11	0.51	0.74	0	0.066	0.69	0.008	0.25	0.68
$N_{\nu}, 1.6\text{--}2.4\text{ PeV}$	0	0.10	0.18	0	0.017	0.18	0	0.050	0.19
$N_{\nu}, > 2.4\text{ PeV}$	0	0.038	0.10	0	0.071	0.17	0	0.017	0.15
$P_{0,1,0}(E_{\text{p,max}}, \eta_{\text{b}}), \%$	-	-	-	0	1.6	6.4	0	3.6	6.7
photon SED $\chi^2/\text{d.o.f.}$	1.0	1.6	5.6	1.0	1.09	3.9	1.0	1.06	33

Pure Hadronic Model

$$E_\nu \approx 0.05 E_p$$

$$\gamma'_p = 5 \times 10^6 \Gamma_{10}^{-1} E_{\nu, \text{PeV}}^{\text{ob}}$$

$$h \nu'_{\text{pk1}} / m_e c^2 = (m_e / m_p) (B / B_{\text{crit}}) \gamma'^2_p$$

$$B = 7 \times 10^{-4} \left(\frac{\nu_{\text{pk1}}}{10^{14} \text{ Hz}} \right) \left(\frac{\Gamma}{10} \right) \left(\frac{E_\nu^{\text{ob}}}{\text{PeV}} \right)^{-2}$$

NU E is ~5% of parent proton

Derived p Lorentz factor

Freq. of 1st peak by p-syn

Required B field

$$\gamma'_{e|\text{p}\gamma} m_e \approx 0.05 m_p \gamma'_p$$

$$h \nu'_{\text{pk2}} / m_e c^2 = (B / B_{\text{crit}}) \gamma'^{-2}_{e|\text{p}\gamma}$$

$$B = 3 \times 10^{-2} \left(\frac{\nu_{\text{pk2}}^{\text{ob}}}{10^{23} \text{ Hz}} \right) \left(\frac{\Gamma}{10} \right) \left(\frac{E_\nu^{\text{ob}}}{\text{PeV}} \right)^{-2}$$

Secondary e+- E is ~5% of parent proton

2nd peak by synchrotron emission of secondaries

Required B field

Requires contradictory B field values >> Pure Hadronic Model not viable

Leptonic and LH-SSC model

$$\gamma^2 \nu_{\text{sy}} = \nu_{\text{IC}}$$

$$\gamma_{\text{KN}} h \nu'_{\text{sy}} = m_e c^2$$

Thomson to KN scattering transition

$$\frac{\gamma}{\gamma_{\text{KN}}} = 0.006 \left(\frac{\nu_{\text{sy}}}{10^{14} \text{ Hz}} \frac{\nu_{\text{IC}}}{10^{23} \text{ Hz}} \right)^{1/2} \left(\frac{\Gamma}{10} \right)^{-1}$$

2nd peak by Th. , not KN

Cutoff due to $E_{e,\text{max}}$, or absorption
by EBL (not discussed)

$$l_* \equiv \left(\frac{L'}{R} \right) / \left(\frac{4\pi m_e c^2}{\sigma_T} \right) \approx 0.03 \left(\frac{L_{\text{ob}}}{10^{-11} \text{ erg cm}^{-2} s^{-1}} \right) \left(\frac{\Gamma}{10} \right)^{-4} \left(\frac{R}{10^{15} \text{ cm}} \right)^{-1}$$

compactness for gamma-rays

GeV - TeV γ can escape source

Leptonic and LH-SSC model

$$\gamma'_e{}^2 \approx \nu'_{\text{sy}} / \nu'_{\text{IC}}$$

Thomson scattering

$$h \nu'_{\text{sy}} = m_e c^2 (B'/B_{\text{crit}}) \gamma'_e{}^2$$

Synchrotron, ~ 1st peak

$$\nu' = \nu^{\text{ob}} (1 + z) / \Gamma$$

$$u'_{\text{ph}} = \left(\frac{d_{\text{pks}}}{R_{\text{blob}}} \right)^2 \left(\frac{1 + z}{\Gamma^2} \right) \frac{\nu F_\nu}{c}$$

comoving phot density

$$Y_{\text{SSC}} \approx \frac{u'_{\text{ph}}}{u'_B} \approx \frac{L(\nu_{\text{sy}})}{L(\nu_{\text{IC}})}$$

Y_{SSC} related to relative heights
of the two peaks of SED

$$X = 10^i X_i$$

$$R_{18} \Gamma_{10} \approx 1.4 \left(\frac{L(\nu_{\text{sy}})}{10^{-11} \text{ erg cm}^{-2} \text{ s}^{-1}} / Y_{\text{SSC}} \right)^{1/2} \left(\frac{\nu_{\text{sy}}^{\text{ob}}}{10^{14} \text{ Hz}} \right)^{-2} \left(\frac{\nu_{\text{IC}}}{10^{23} \text{ Hz}} \right)$$

Expressed in all observed quantities

Requires either large R or Γ values

Numerical Calculation

Diff-integral Equations

$$\frac{\partial n(E)}{\partial t} = -\frac{\partial}{\partial \ln E} \left[A(E) - B(E) \frac{\partial}{\partial \ln E} \right] n(E) - \alpha n(E) + \epsilon$$

$$n(E) \equiv \frac{dN}{dV d \ln x} = x \frac{dN}{dV dE}$$

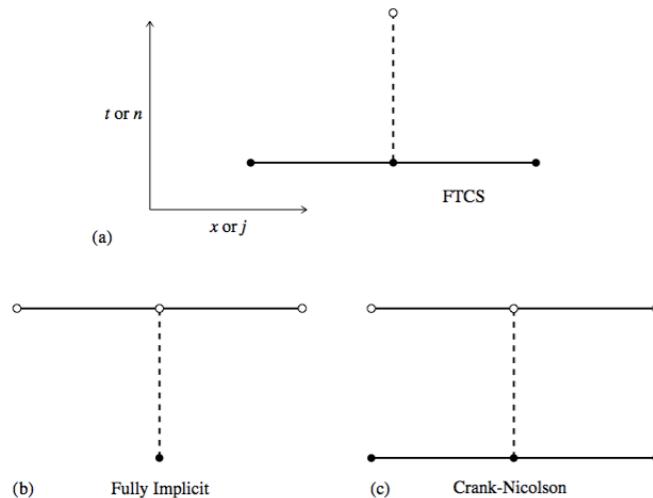
$$\alpha(E) = \sum_{IT} \int c \sigma_{IT} n_{IT}(E_1) dE_1$$

$$\epsilon(E) = \sum_{IT} \int R(E \leftarrow E_1) d n_{IT}(E_1)$$

Solving time-dependent coupled kinematic equations
for $e^-, e^+, p, n, \gamma, v$

Coefficients derived from physics

Numerical Scheme : Finite Difference



Chang & Cooper for E

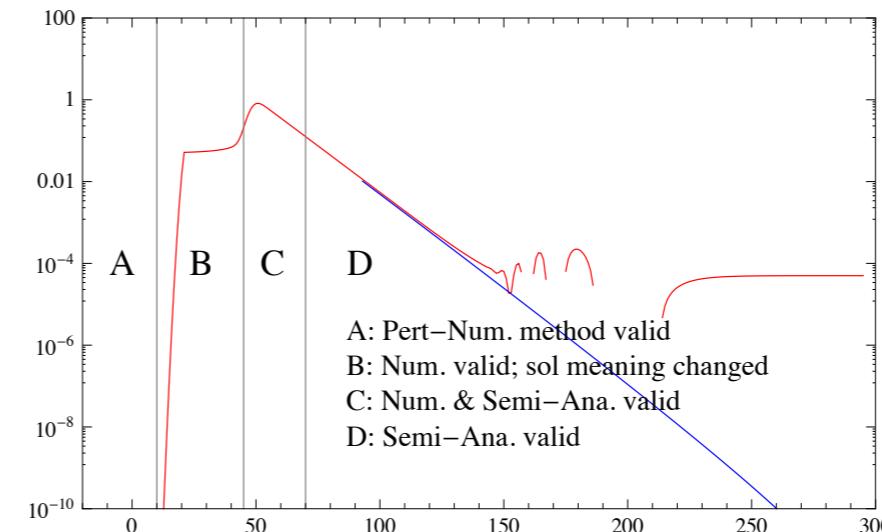
Crank & Nicolson for t

Stability + Energy conservation + Positive spectrum
(even when dt and dN/dE is large)

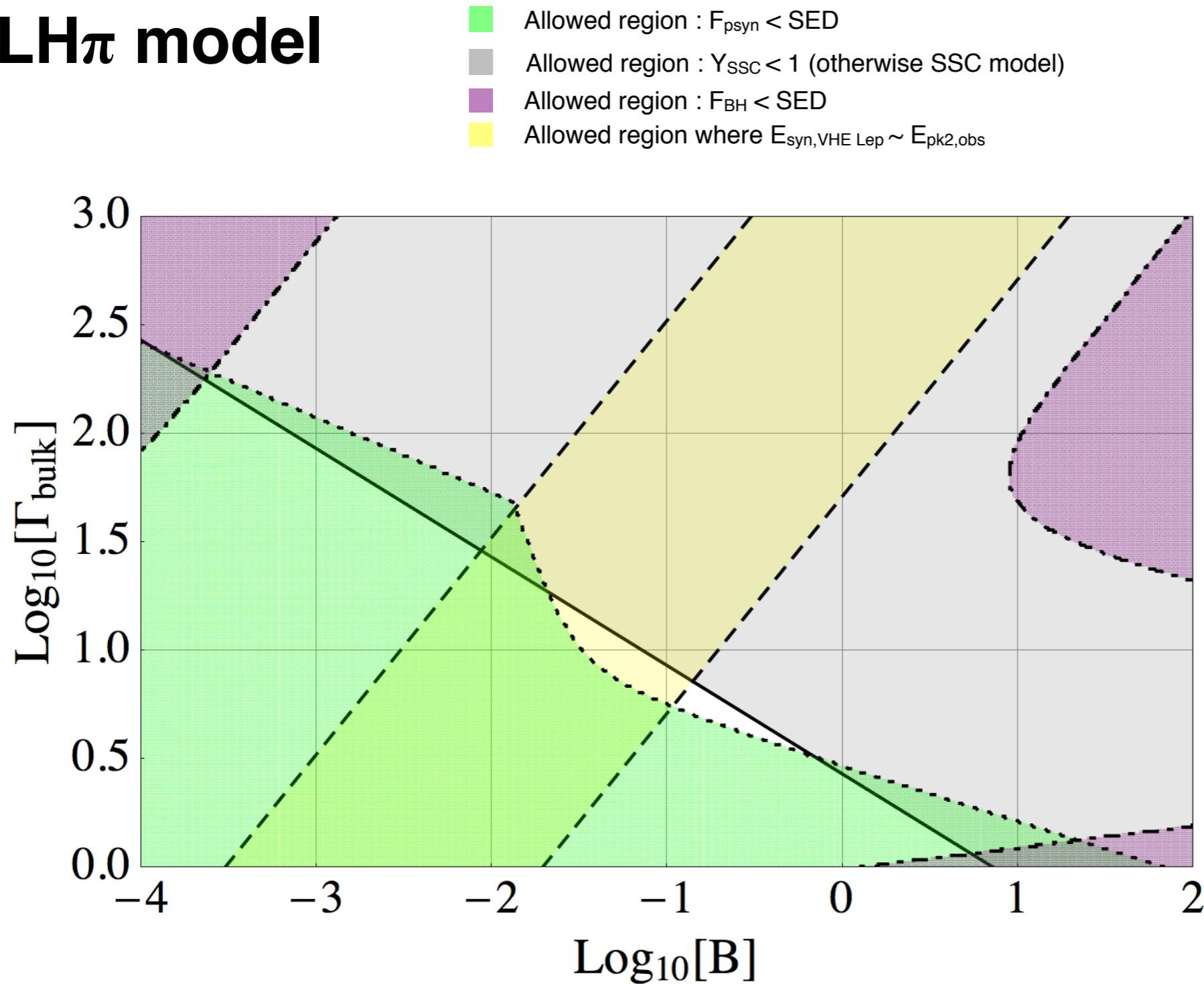
Approximation

Semi-analytical solution for VHE e
quasi-steady states within a step Δt

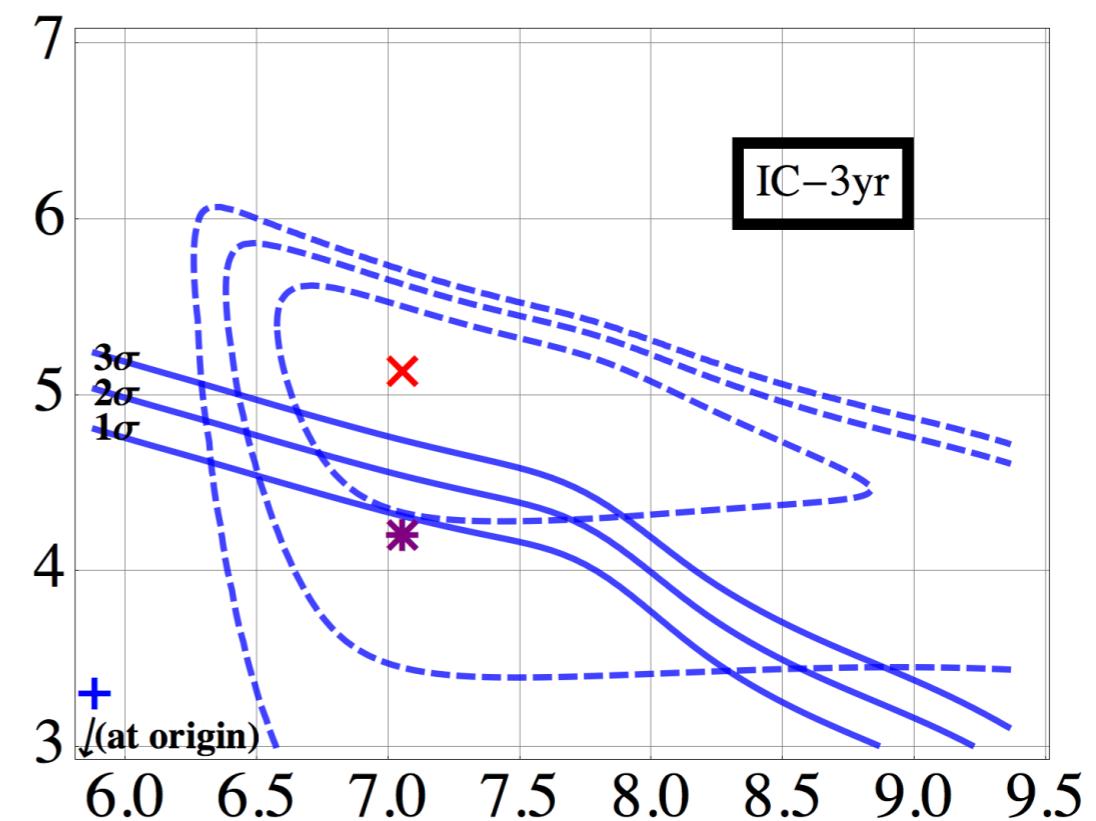
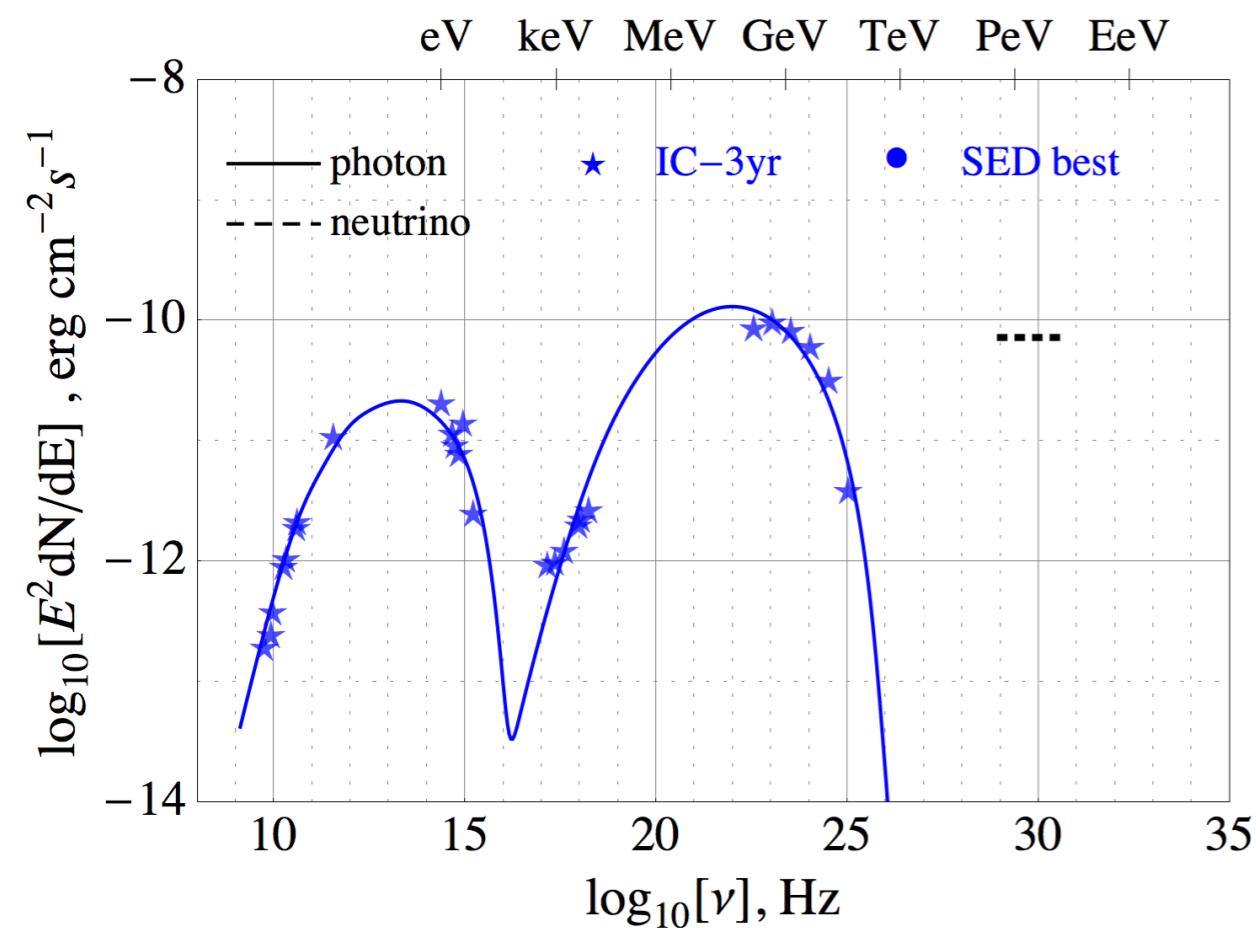
>> reasonable Δt and high efficiency
resolving the stiffness problem at VHE



LH π model

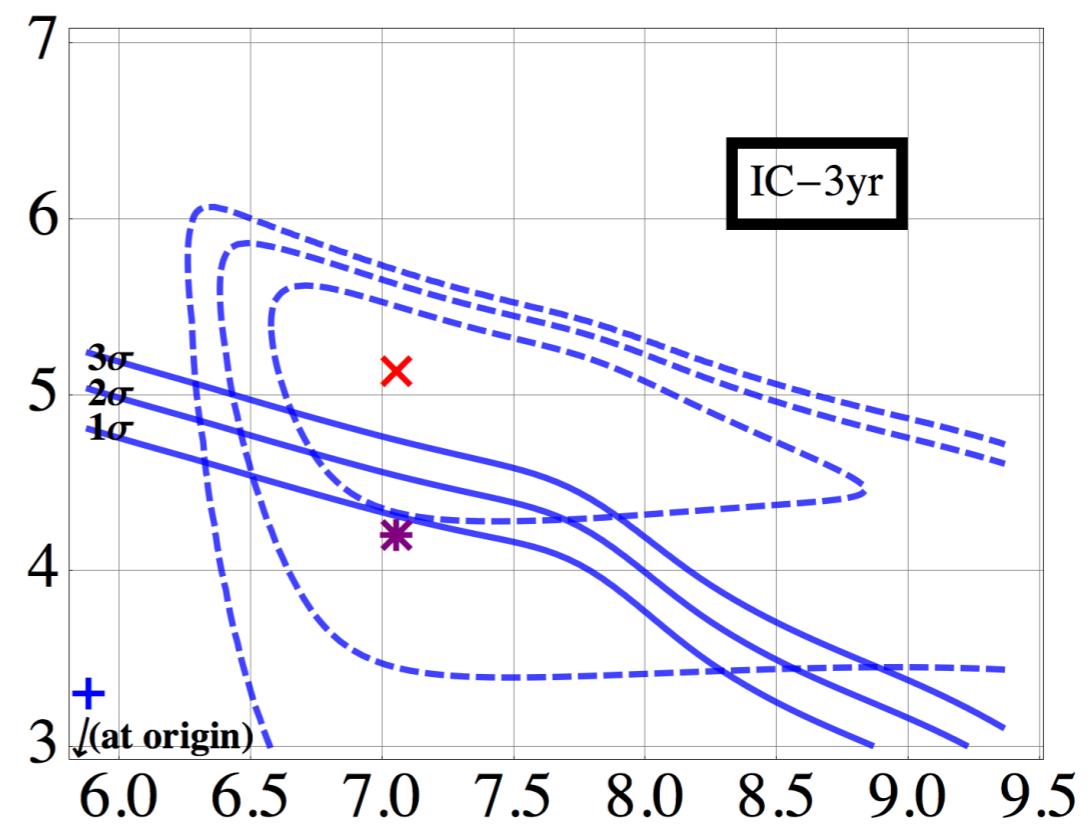
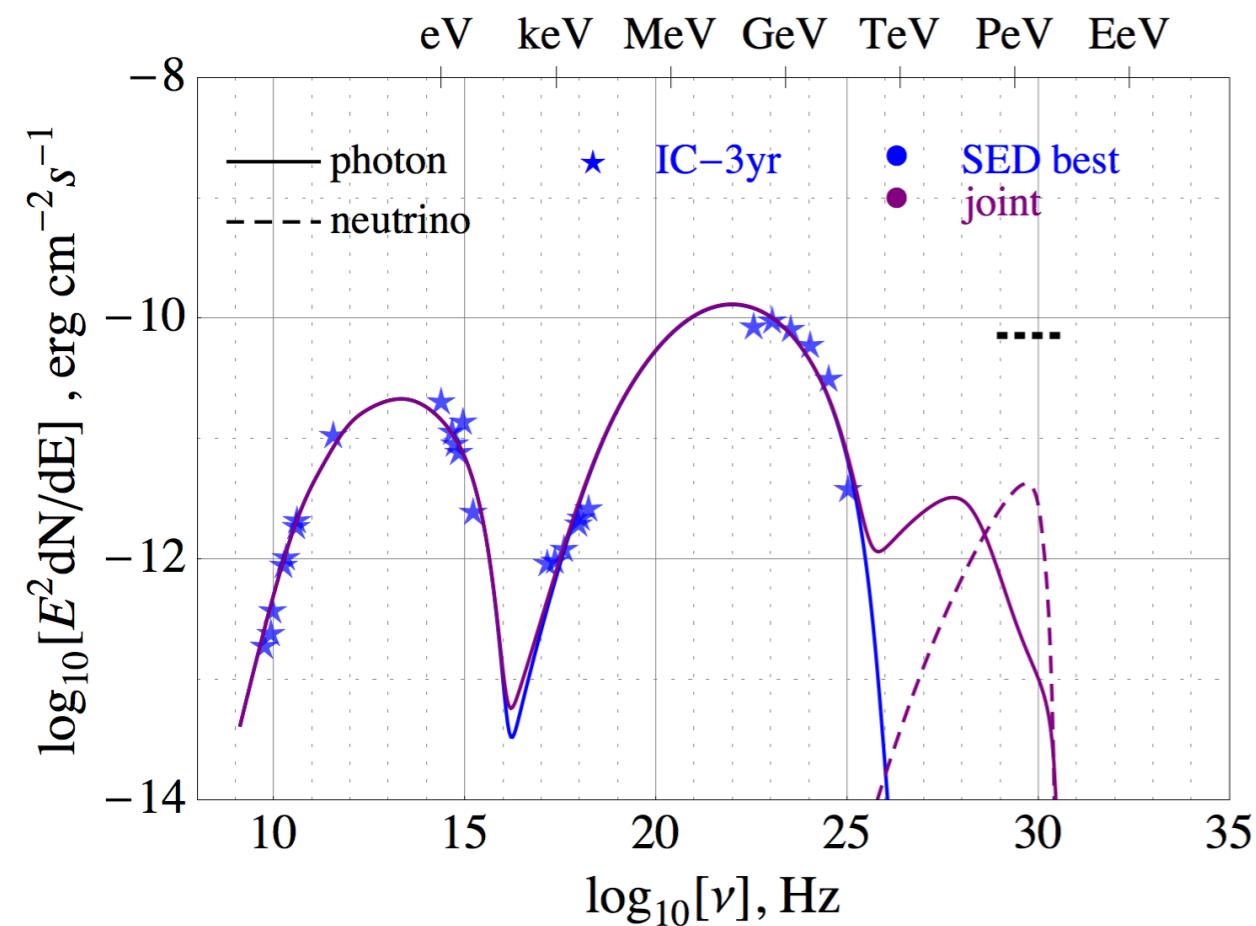


IC-3yr phase



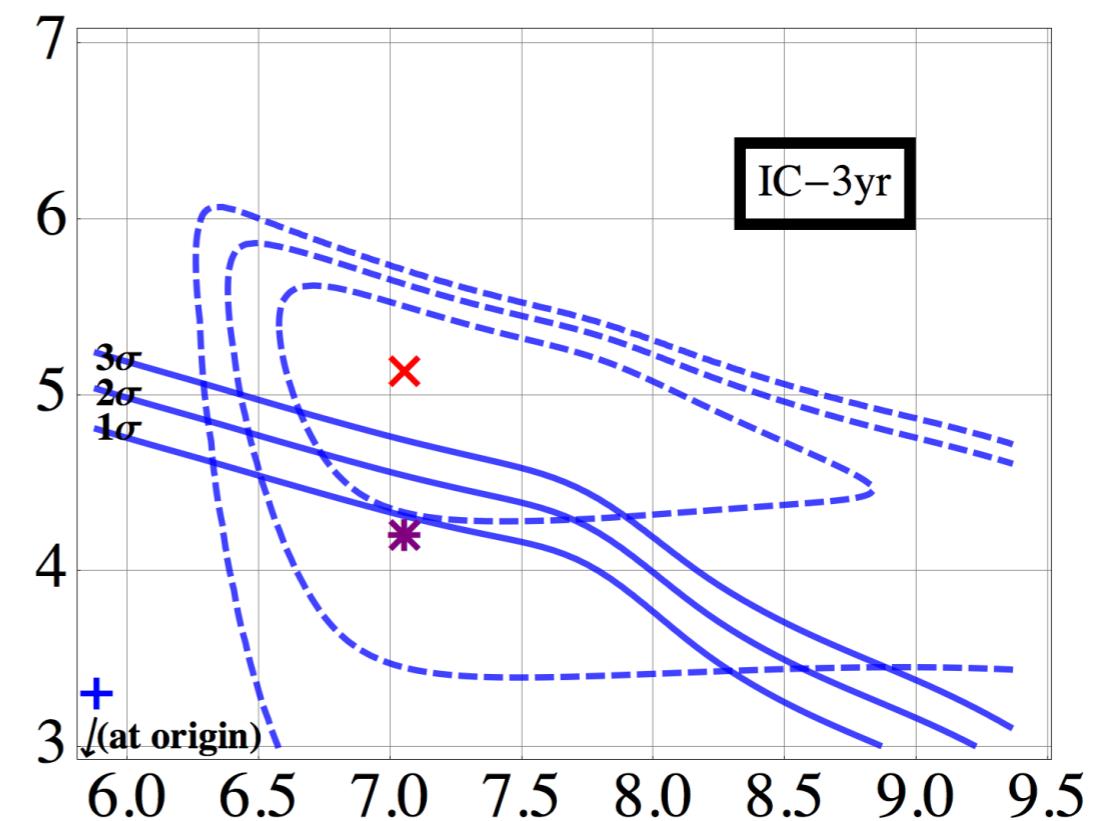
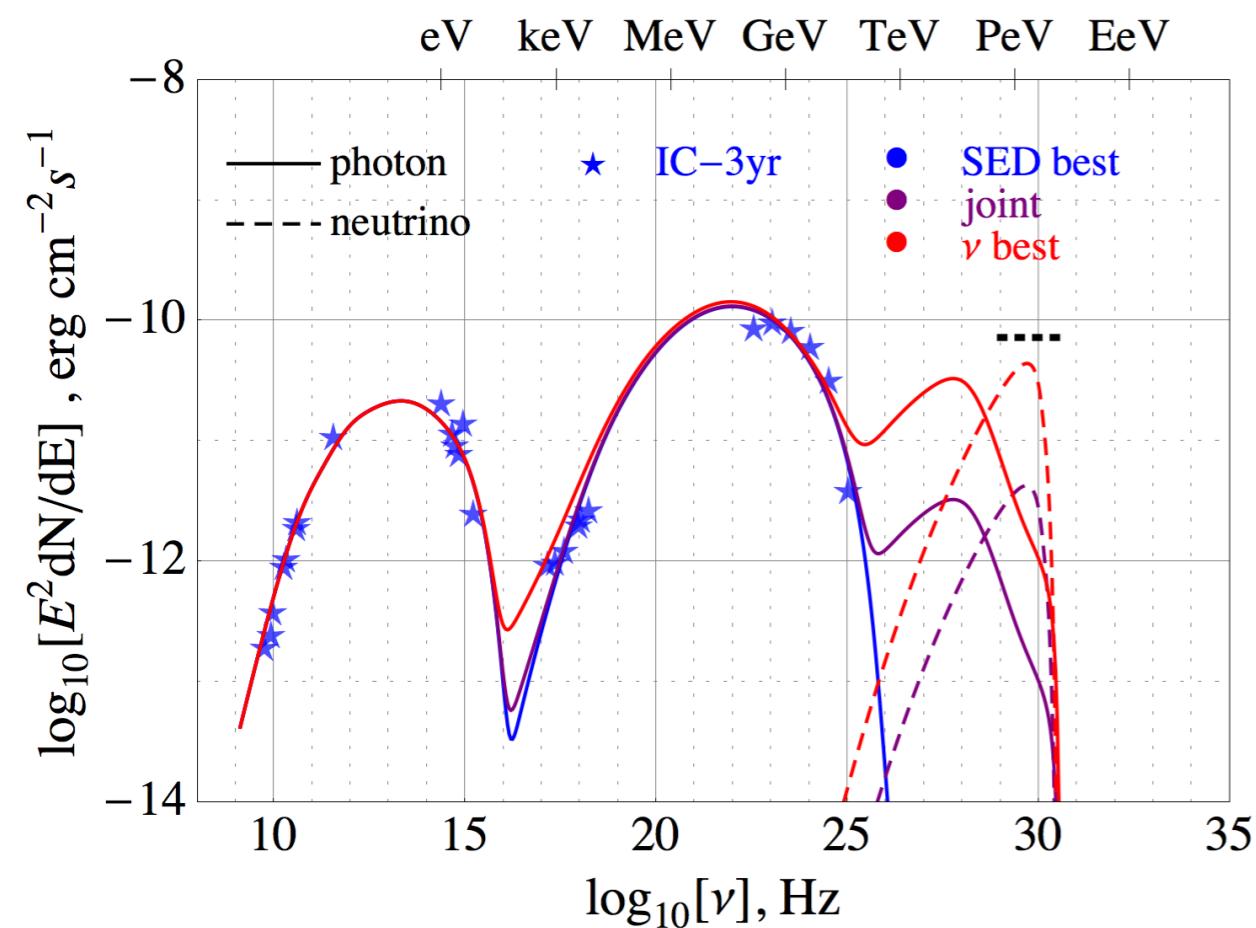
SED best fit, a leptonic SSC-model

IC-3yr phase



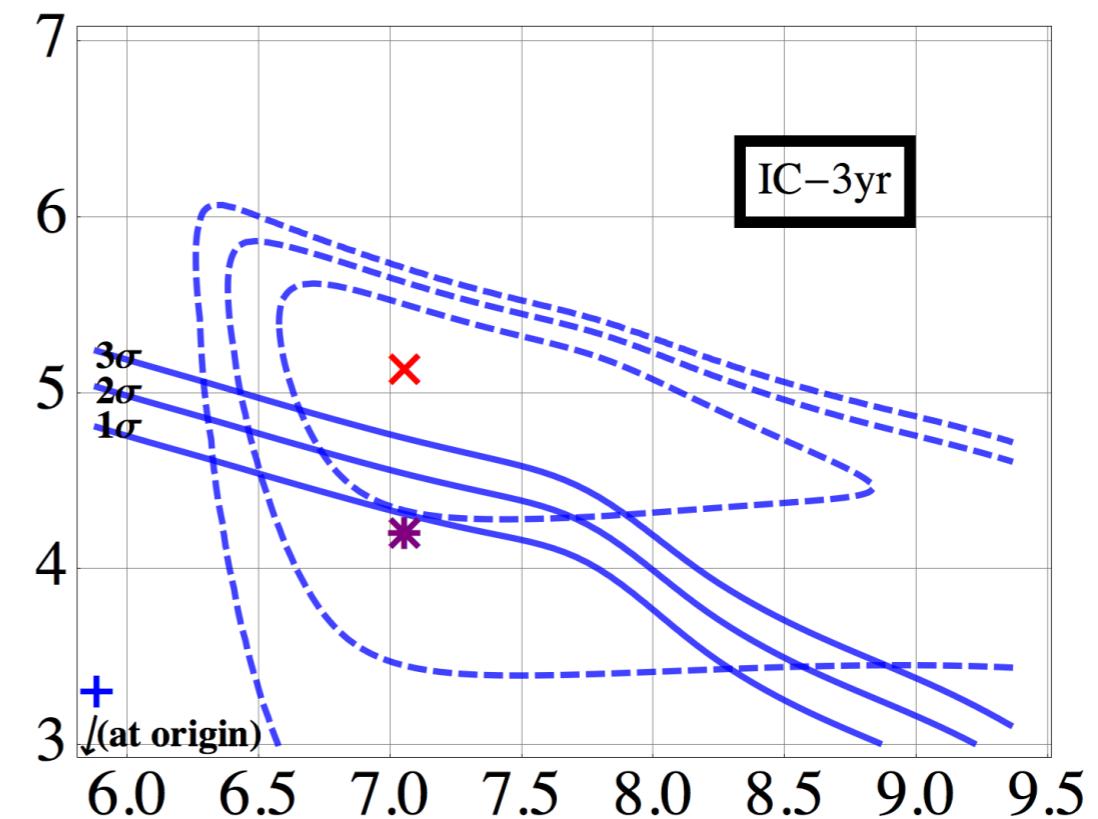
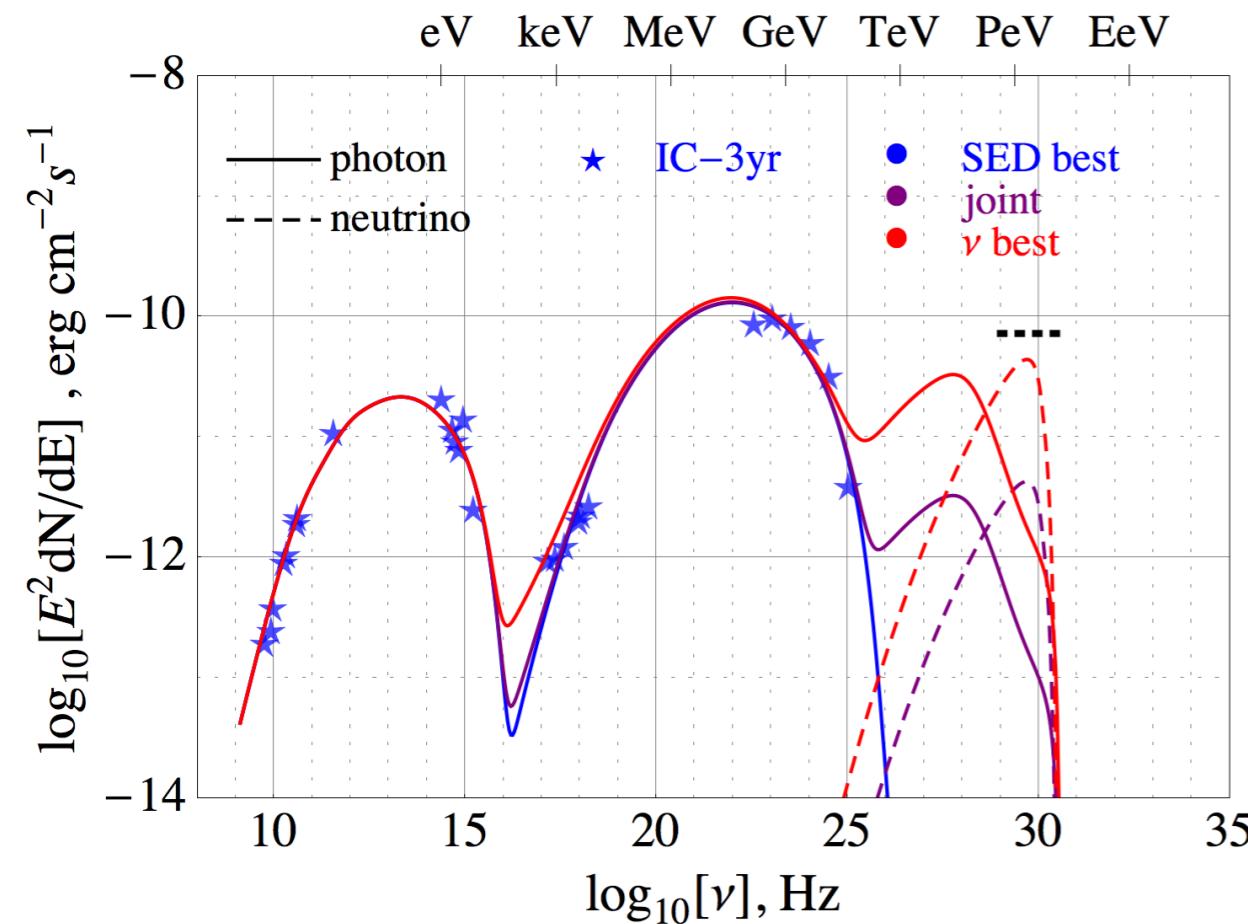
SED - neutrino joint best-fit, $L_p/L_e \sim 10^4$

IC-3yr phase



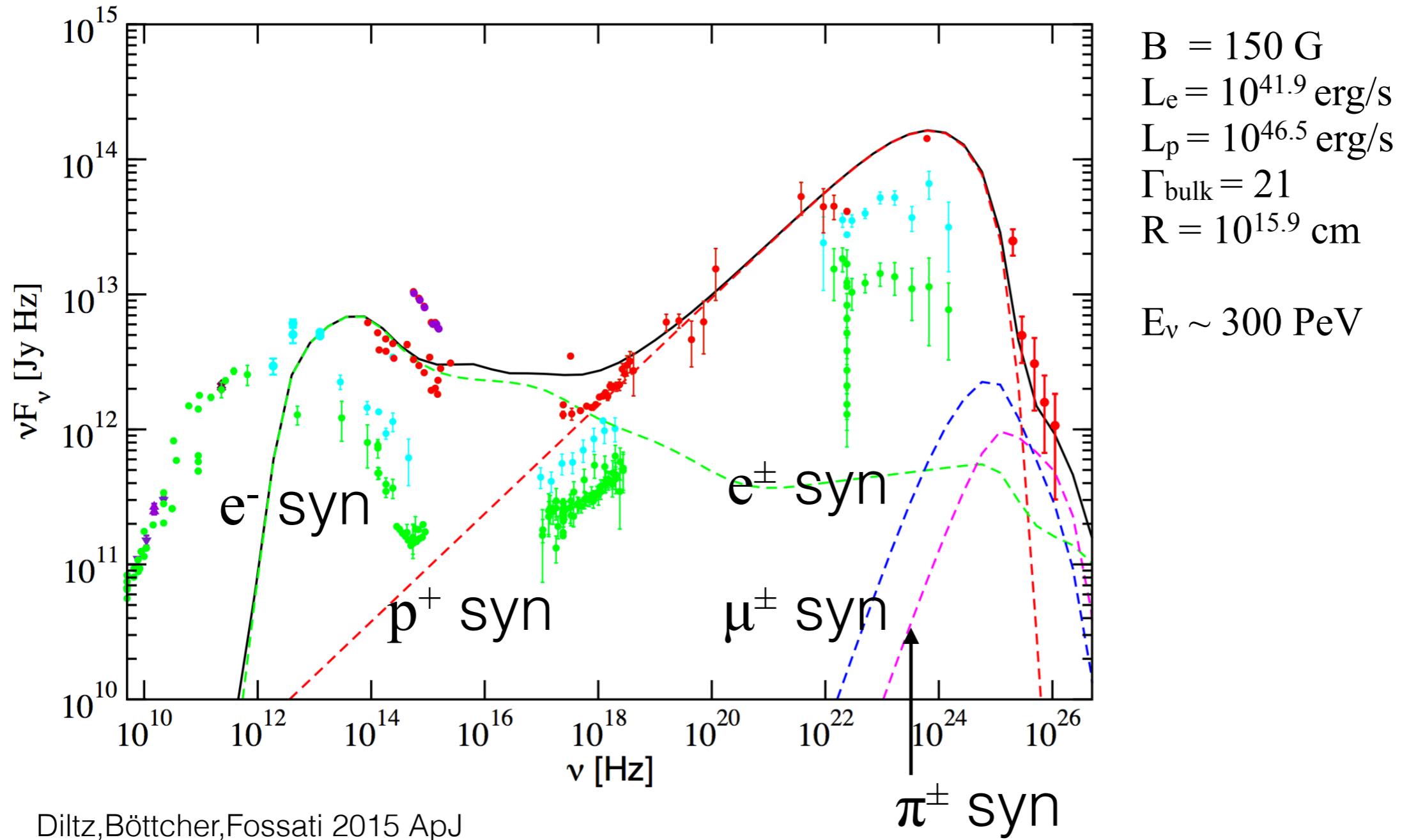
neutrino best-fit, $L_p/L_e \sim 10^5$

IC-3yr phase



Max amount hadrons can a leptonic model tolerate
NU best-fit is in tension with SED best-fit (overshooting X-ray band)
Joint-fit gives ~5% probability to reproduce “big-bird” within this phase

3C 279, Steady-state, proton-synchrotron model



Diltz, Böttcher, Fossati 2015 ApJ

Mrk 421

