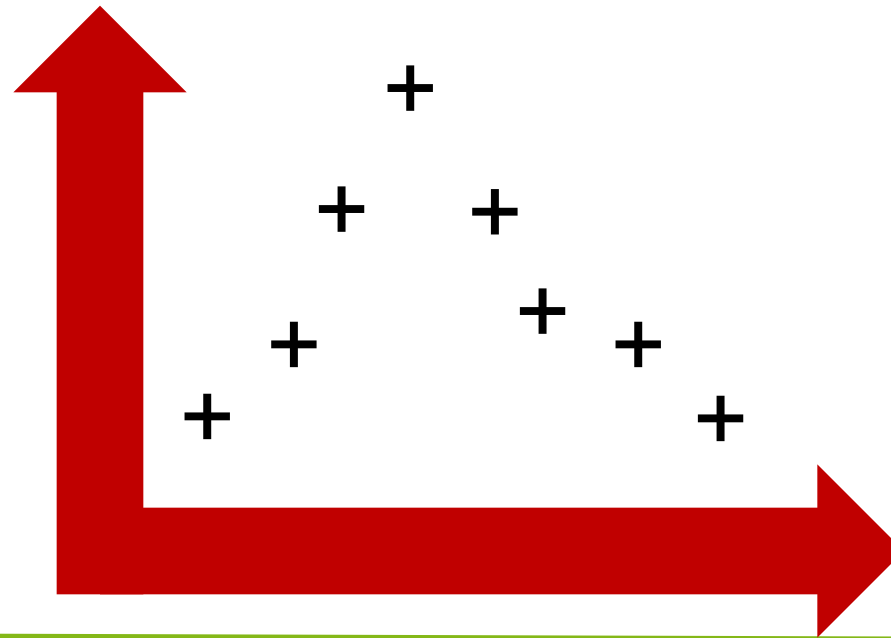




DSEA – A Data Mining Approach to Unfolding

Outline

- Why unfold?
- The Dortmund Spectrum Estimation Algorithm (DSEA)
- Performance Studies using Toy MC simulation
- Summary & Outlook

SFB 876 Providing
Information by Resource-
Constrained Data Analysis



Other people who contribute to DSEA:

Max Wornowizki, Tobias Voigt, Mathis
Börner, Martin Schmitz

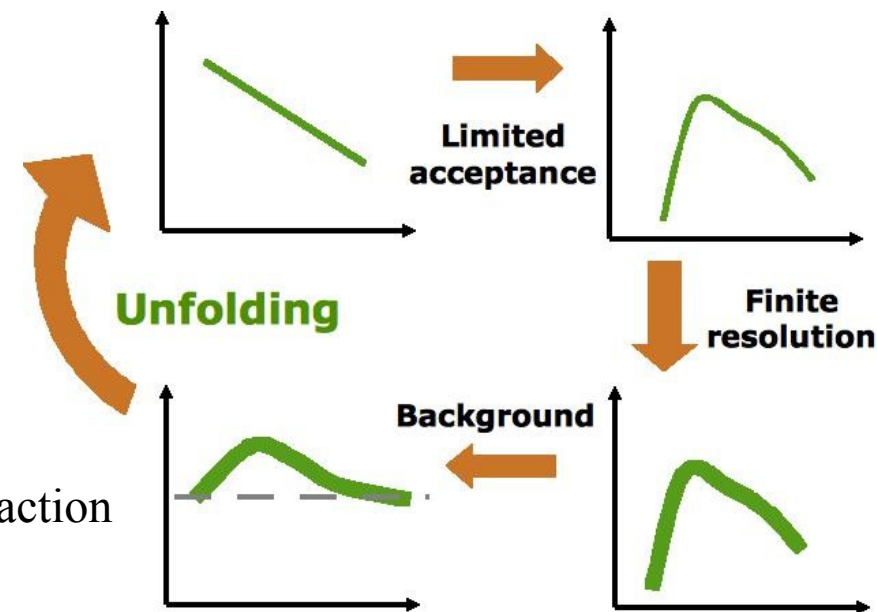
Why Unfold?

The production of muons from muon neutrinos is a stochastic process:

$$\frac{dN_{\mu}}{dE_{\mu}} = \int_{E_{\mu}}^{\infty} dE_{\nu} \left(\frac{dN_{\nu}}{dE_{\nu}} \right) \left(\frac{dP(E_{\nu})}{dE_{\mu}} \right)$$

Neutrino spectrum

Physics of neutrino interaction



Additional smearing due to limited acceptance and finite resolution.



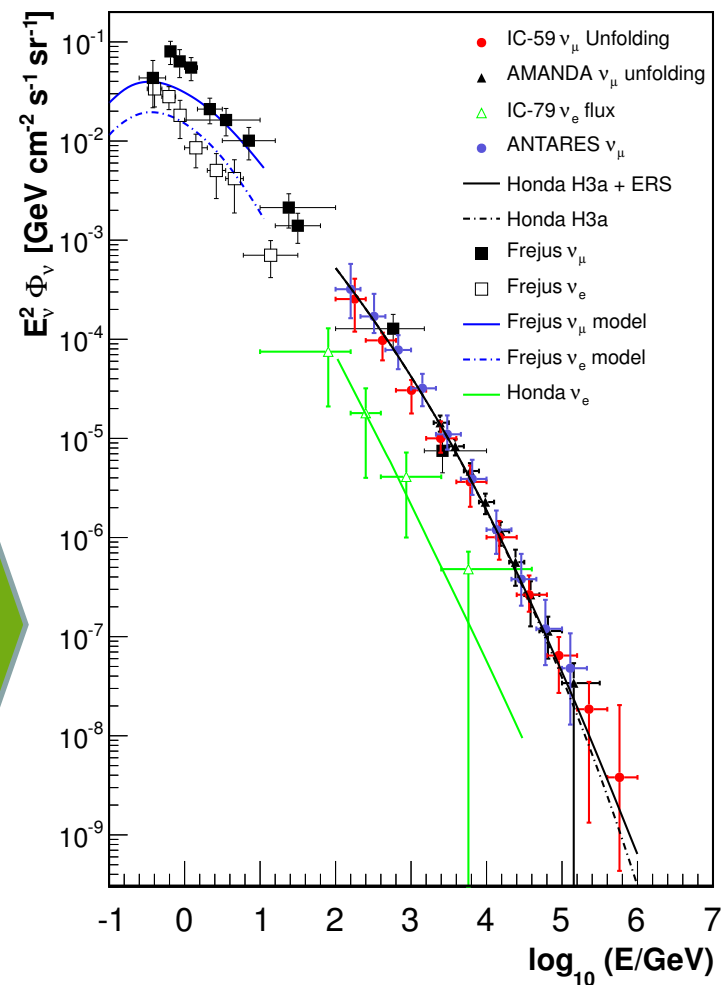
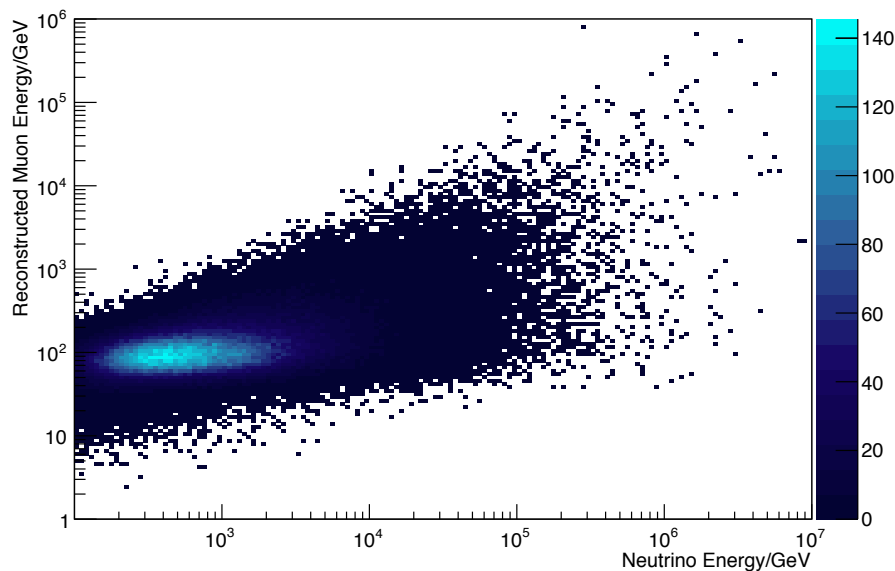
$$g(y) = \int_{E_{\min}}^{E_{\max}} A(E, y) f(E) dE$$

Fredholm Integral equation of the first kind

Unfolding Spectra of Atmospheric Neutrinos

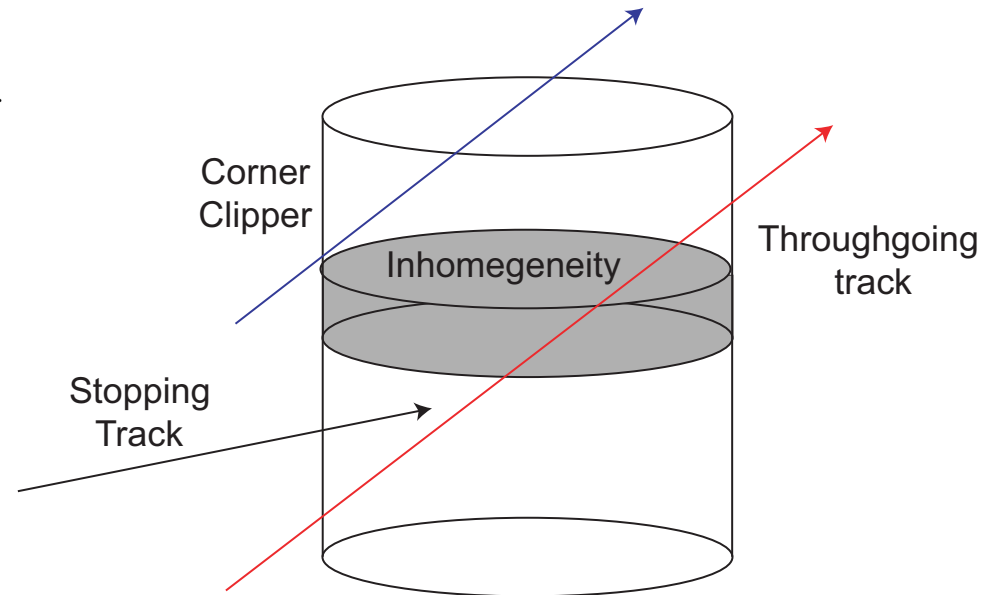
Example taken from atm. ν_μ measurement with IceCube.

Aartsen et al., EPJC 75, 116 (2015)



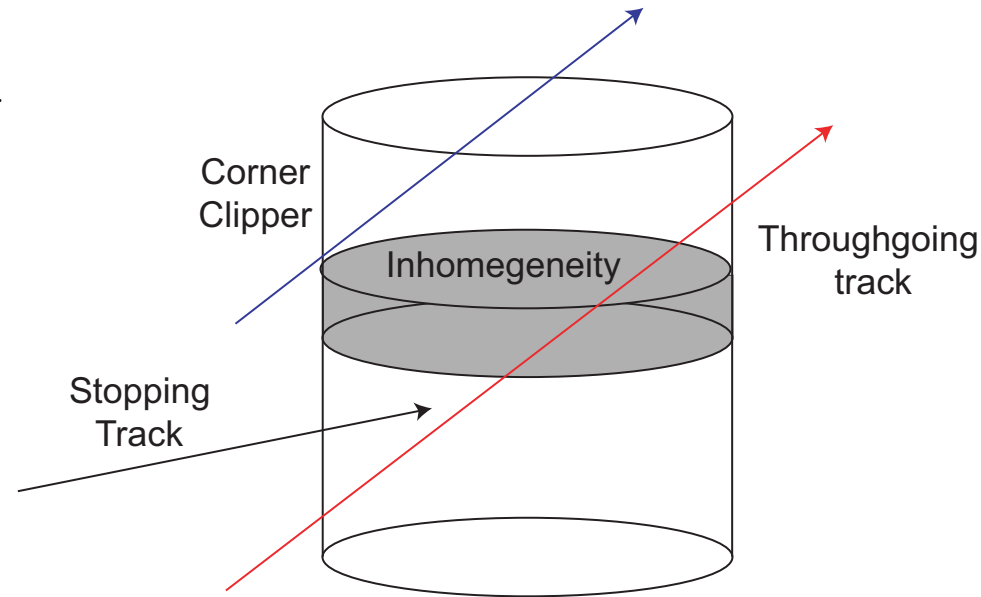
Why do we need to improve on existing algorithms?

- Events with identical energy may cause very different patterns inside the detector
- Geometrical information will increase precision of the measurement
- Existing algorithms are limited in the number of input variables (“curse of dimensionality“)
- Algorithms return spectra accurately, but information on individual events is lost
- Generally require a certain amount of unfolded events to obtain a spectrum



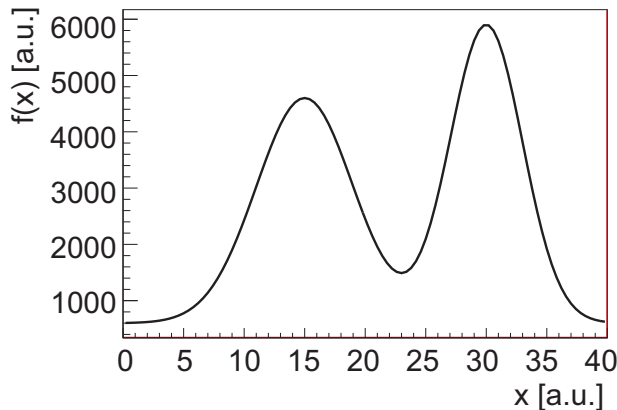
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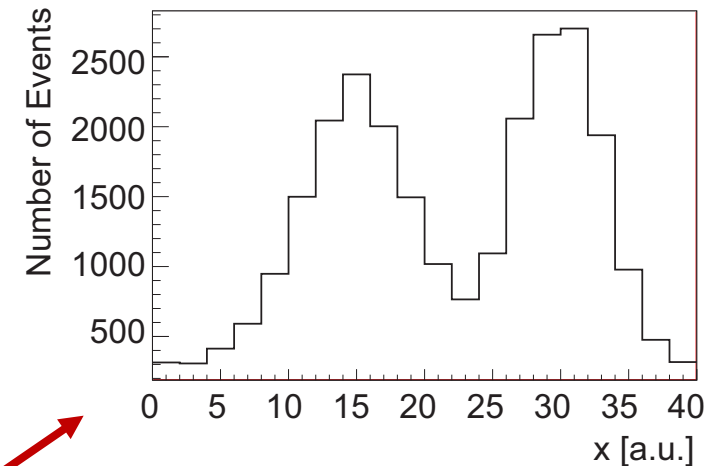


We need algorithms that can utilize an arbitrary number of input variable and fully retain the information on individual events.

DSEA – The General Idea



Discretize



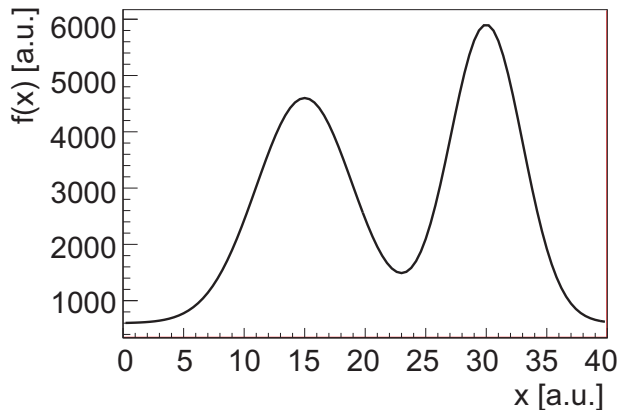
Classify



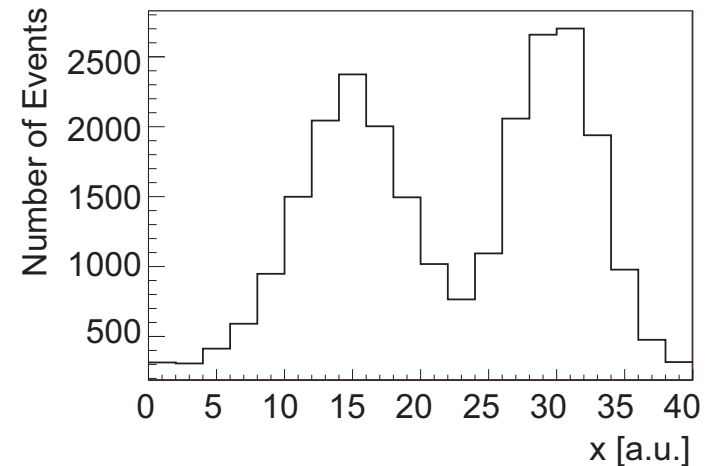
Inverse Problem is transformed
into a multinomial classification
task that can be solved by an
arbitrary classifier.

Really beautiful spectrum

DSEA – The General Idea



Discretize



Classify

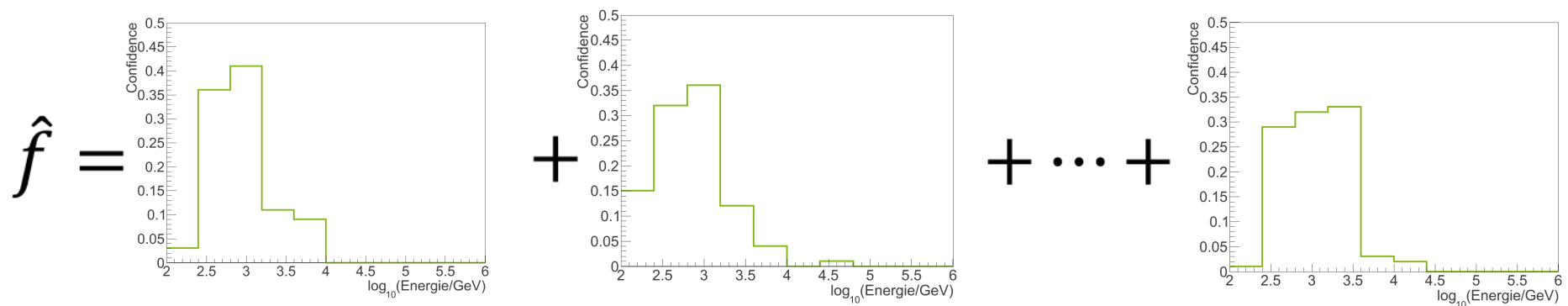


Really beautiful spectrum

- Arbitrary number of input variables
- Information on individual events is fully retained

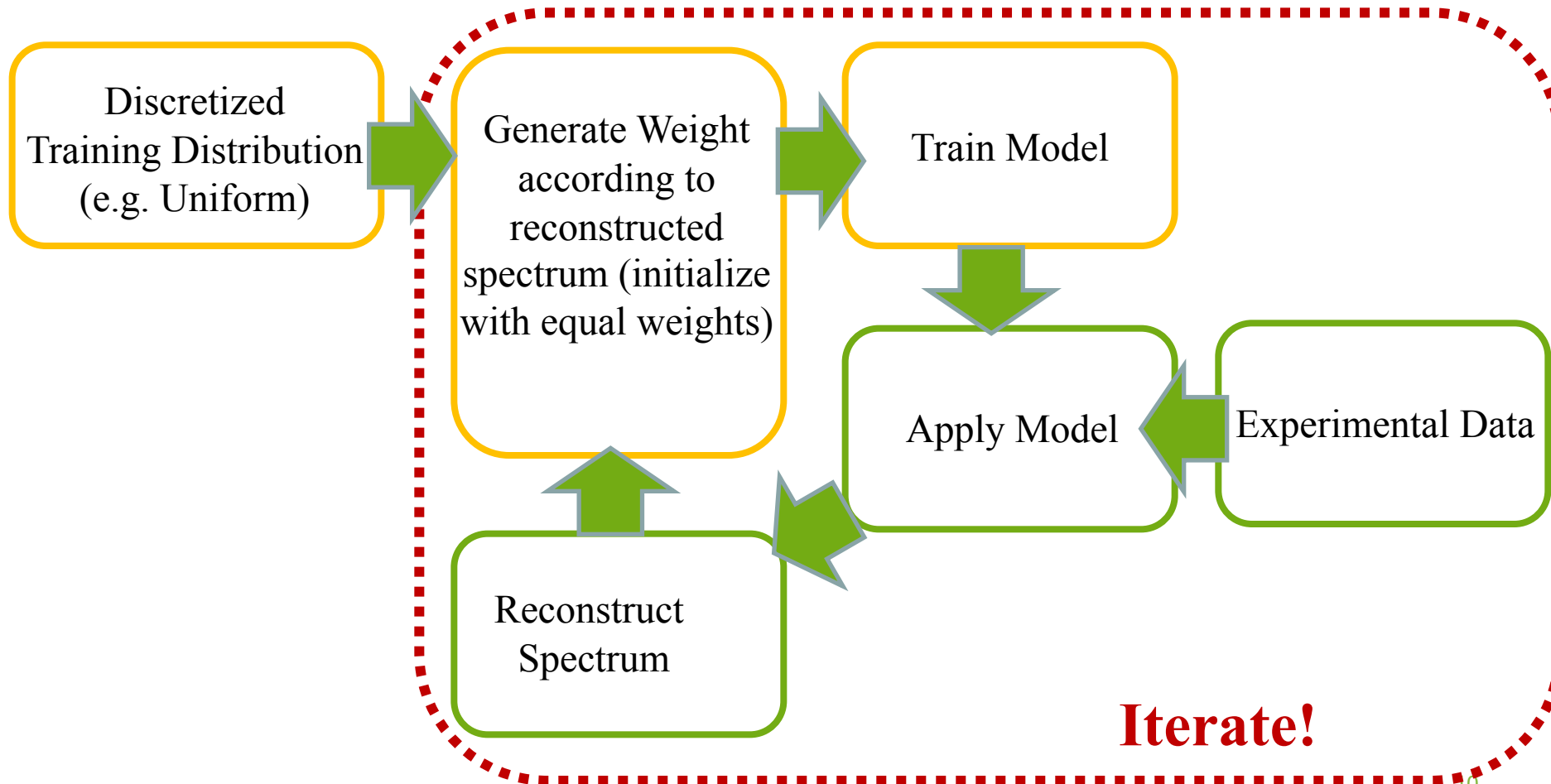
However, it is not really that simple...

- Maximum of confidence distribution generally not very distinct
- Therefore, classification also not very distinct
- Results in poorly reconstructed spectrum
- Solution: Interpret confidence distribution as estimation of pdf



Don't you only get out what you put in?

NO!



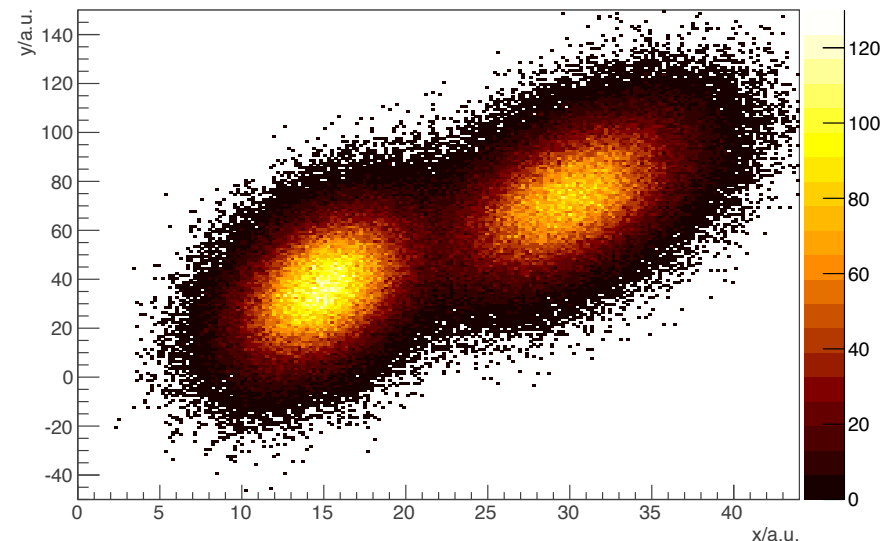
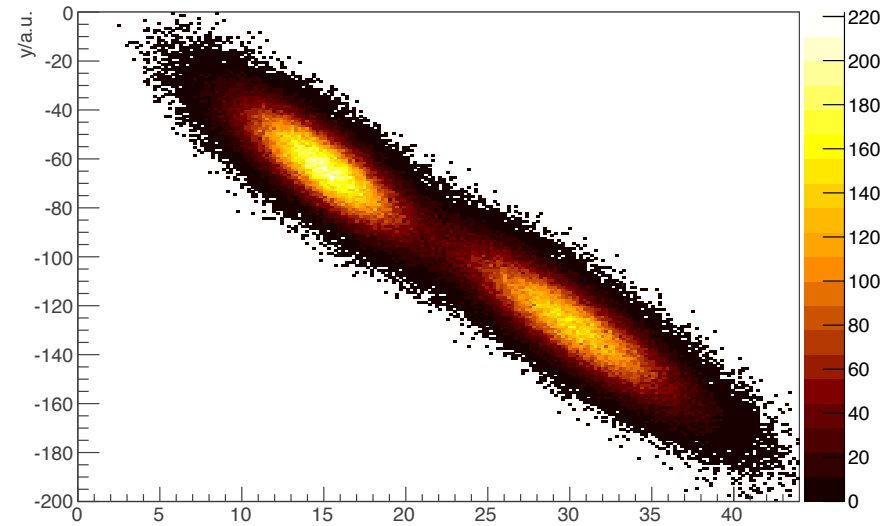
DSEA – Full Size Technical Description

1. **Discretize** $f(x) \mapsto \vec{f}(x) = (f_1, \dots, f_m)$. (**Initialize**)
2. **Train Model** A subset of n examples $(\underline{A}, W, L) = \{(\vec{a}, w, l)_1; \dots; (\vec{a}, w, l)_n\}$ is used to train a model $M(\underline{A}, W, L)$. Each example consists of a label l , a weight w and h attributes $\vec{a} = (a_1, \dots, a_h)$.
3. **Apply Model** The Model $M(\underline{A}, W, L)$ is applied to a set of $\tilde{n}$ unlabeled examples $\tilde{\underline{A}} = (\vec{a}_1, \dots, \vec{a}_{\tilde{n}})$ yielding a confidence $c_{i,j} = g(M(\underline{A}, W, L), \vec{a}_i)$ for the i -th example to belong to the j -th bin in $\vec{f}(x)$.
4. **Reconstruct Spectrum** For the k -th iteration, the bin content $\hat{f}_{j,k}$ of the j -th bin is estimated as $\hat{f}_{j,k} = \sum_{i=1}^{\tilde{n}} c_{i,j}$.
5. **Update weights** The example weights for the $(k + 1)$ -th iteration are updated according to $w_{i,k+1} = \frac{\hat{f}_{k,l_i}}{\tilde{n}}$. (**Continue with Step 2**)



Performance Studies using Toy MC

- Generate function with two-peak structure (2 Gaussian with different mean and width, test set)
- Generate uniform distribution using identical settings (training set)
- Generate 10 correlated variables, apply Gaussian smearing (amount of smearing is randomized within pre-defined range, but kept constant during simulation)
- Statistical uncertainties are obtained by running DSEA 10 times, varying the random seed for the sampling of the training set



Convergence – when to stop iterating?

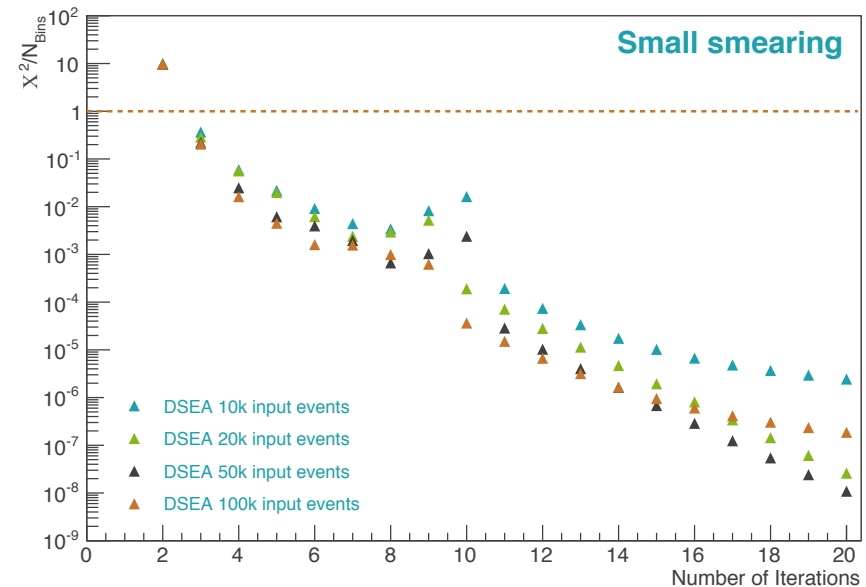
General rule from Iterative Bayesian
Unfolding:

$$\frac{\chi^2}{m} \leq 1$$

Where

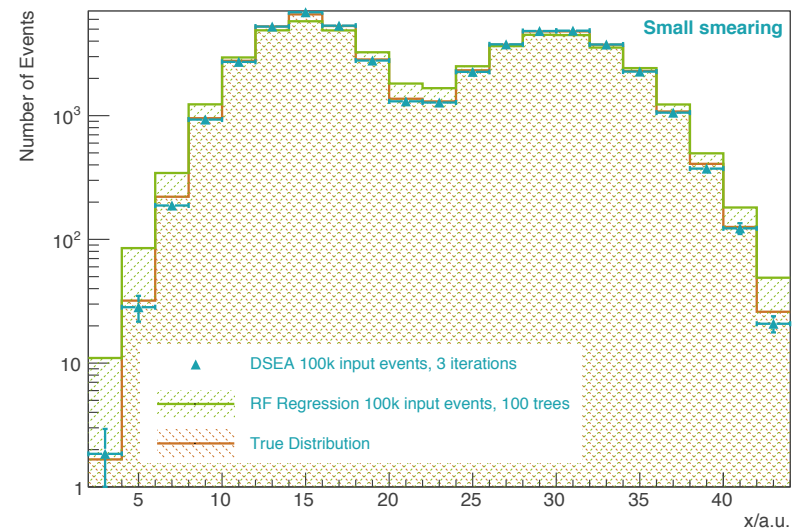
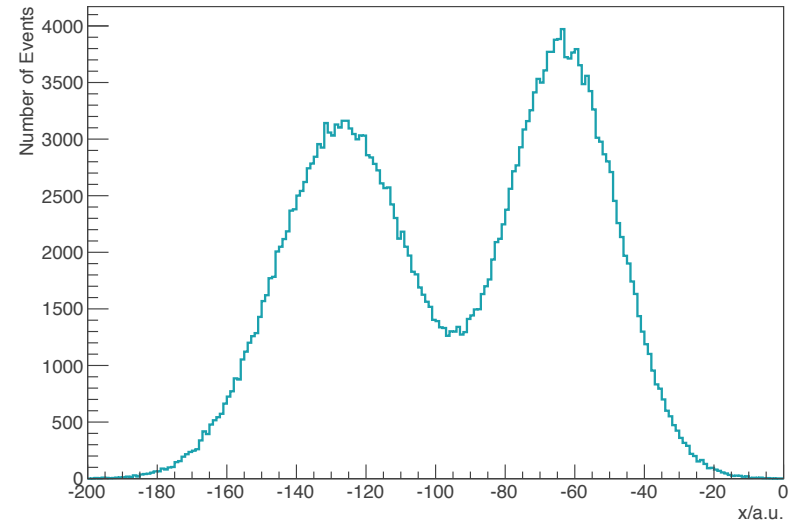
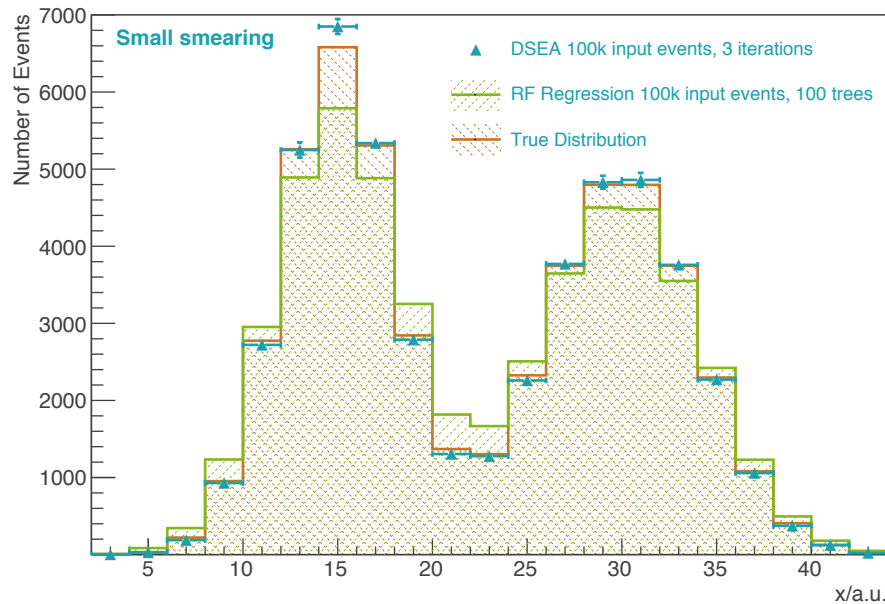
$$\chi^2 = \sum_{j=1}^m \left(\frac{\hat{f}_{j,i-1} - \hat{f}_{j,i}}{\sqrt{\hat{f}_{j,i-1}}} \right)^2$$

- Convergence criterion reached after 3 – 5 iterations
- Some dependence on the number of input examples



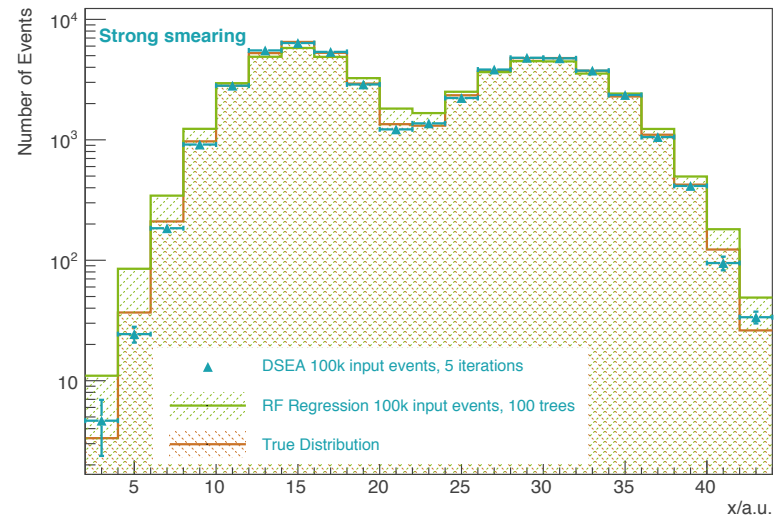
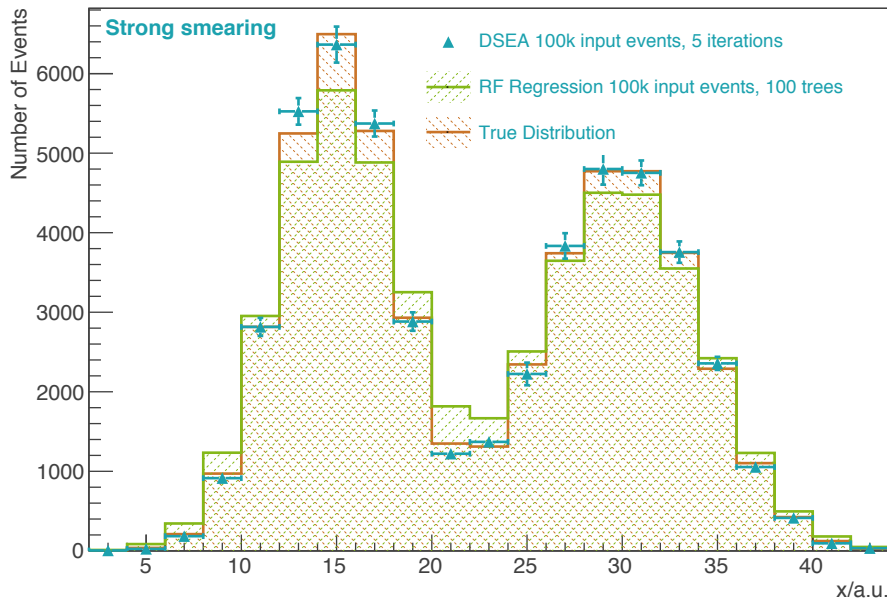
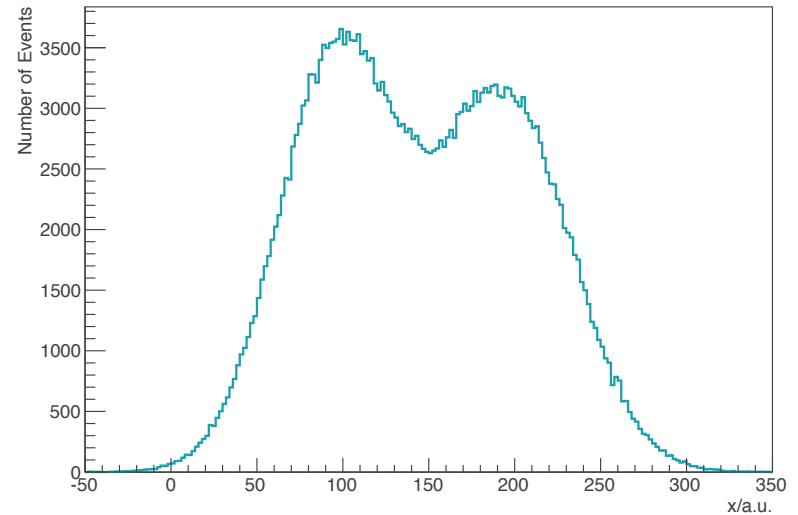
Performance – Spectral Reconstruction

Spectral Reconstruction for small smearing using DSEA (blue), compared to a Random Forest regression (green).



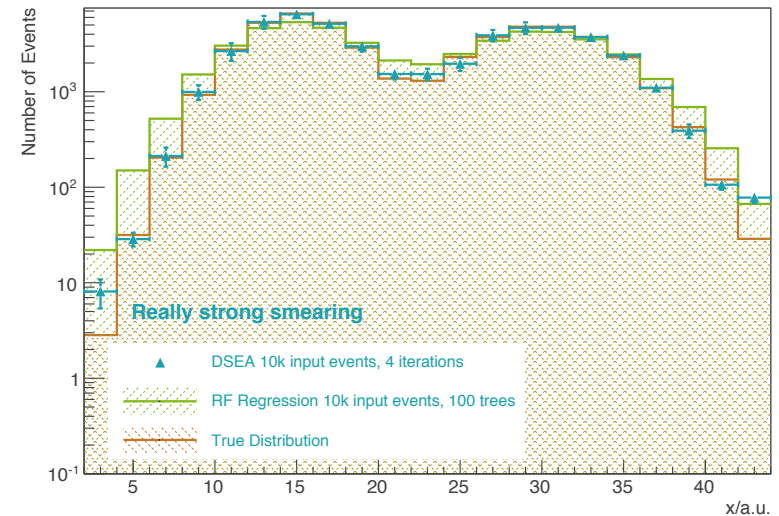
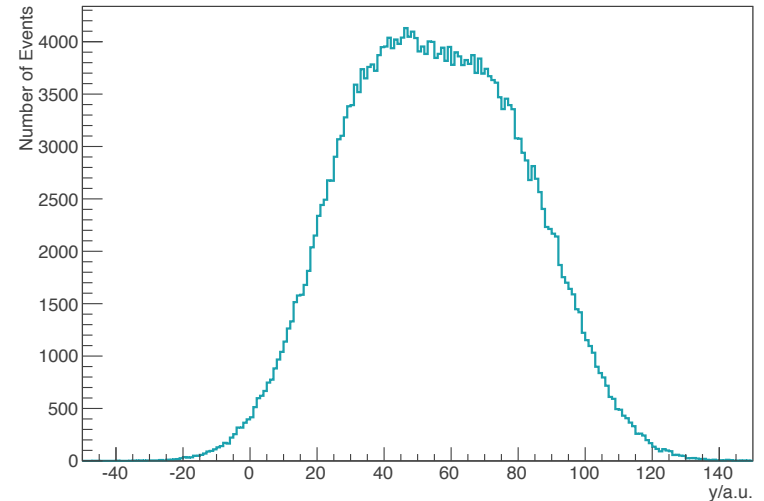
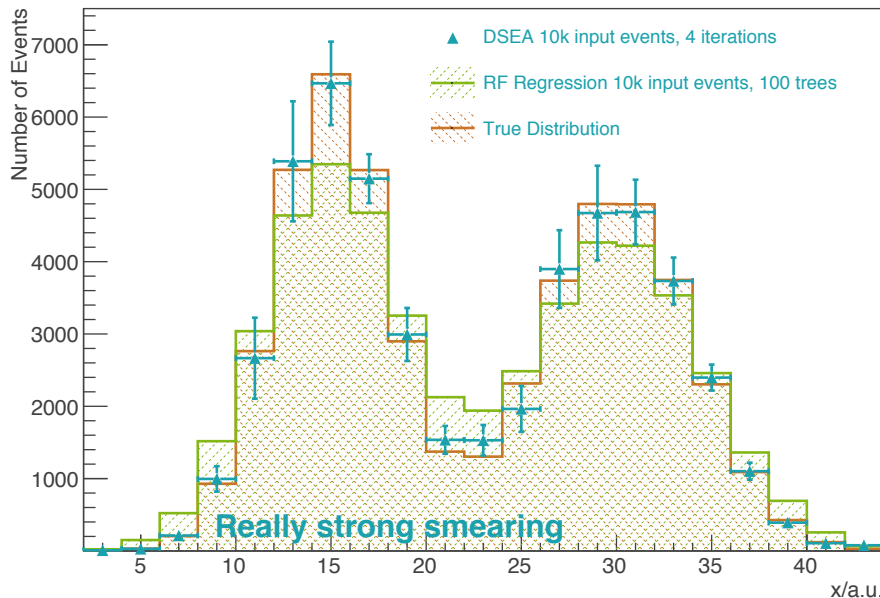
Performance – Spectral Reconstruction

Spectral Reconstruction for strong smearing using DSEA (blue), compared to a Random Forest regression (green).

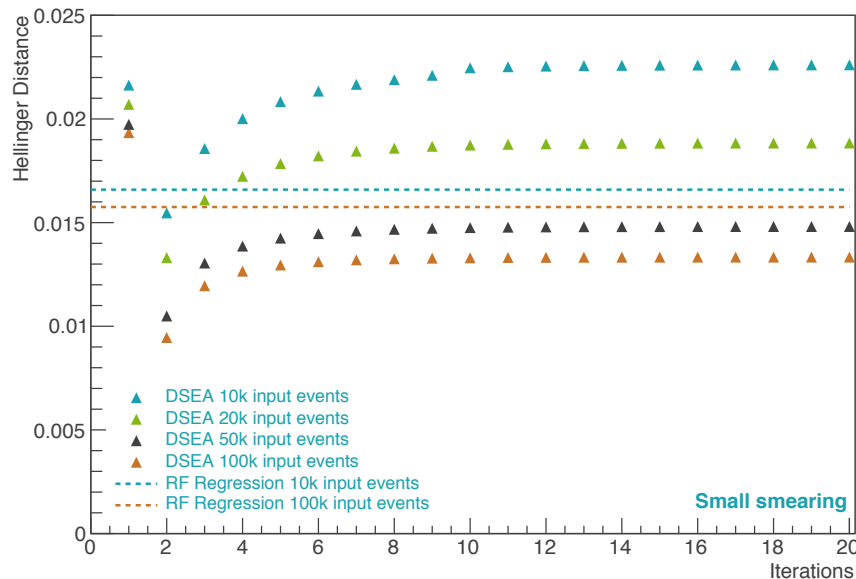


Performance – Spectral Reconstruction

Spectral shape (two peaks) no longer visible in input variables, but spectrum correctly reconstructed using only 10k examples!



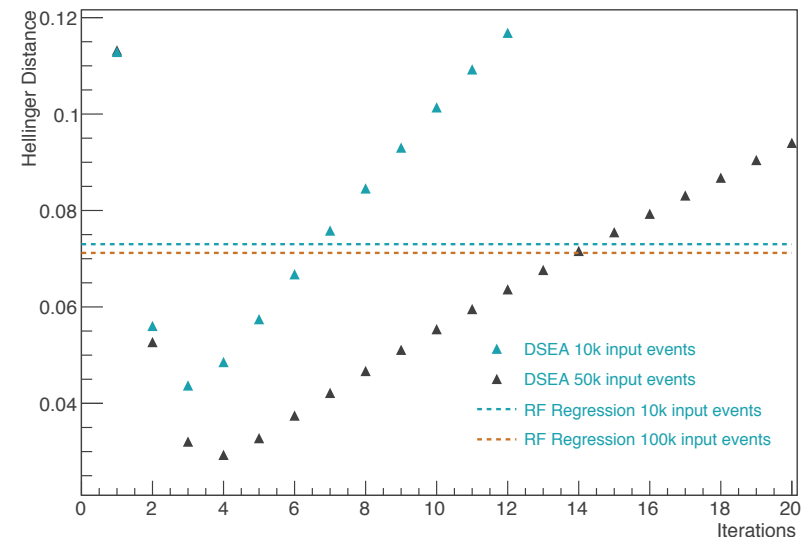
Performance – Agreement with Underlying Distribution



Agreement tends to be optimal for 2 to 5 iterations, gets worse if too many iterations are used.

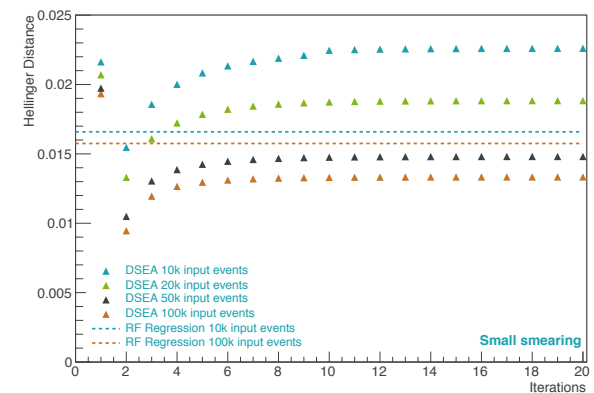
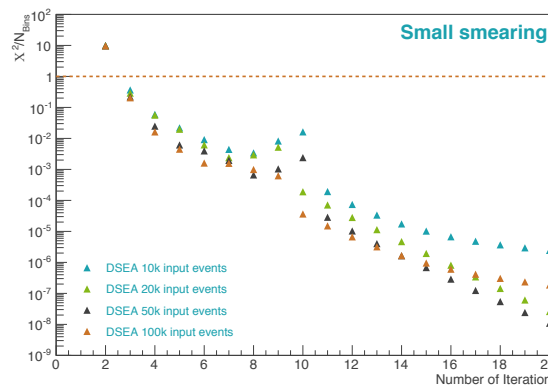
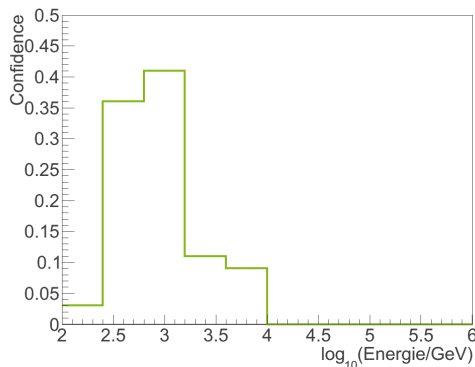
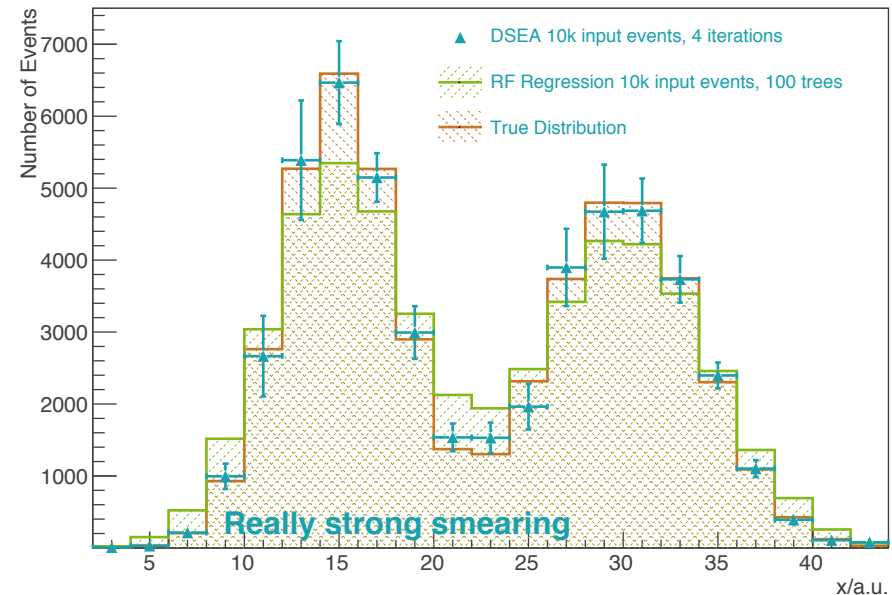
Hellinger Distance:

$$H^2(f, \hat{f}) = \frac{1}{2} \sum_{j=1}^m \sqrt{f_j} - \sqrt{\hat{f}_j}$$



Summary and Outlook

- Apply DSEA to other types of function (saw tooth, steeply falling, steeply rising,...)
- Obtain fair comparison to existing approaches
- Apply DSEA in spectral measurement on simulated experimental data



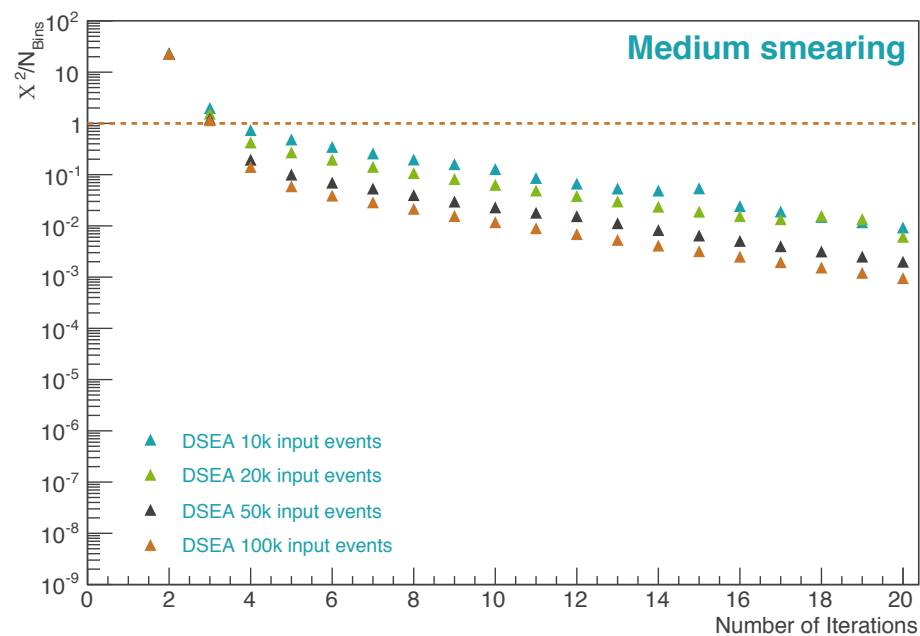
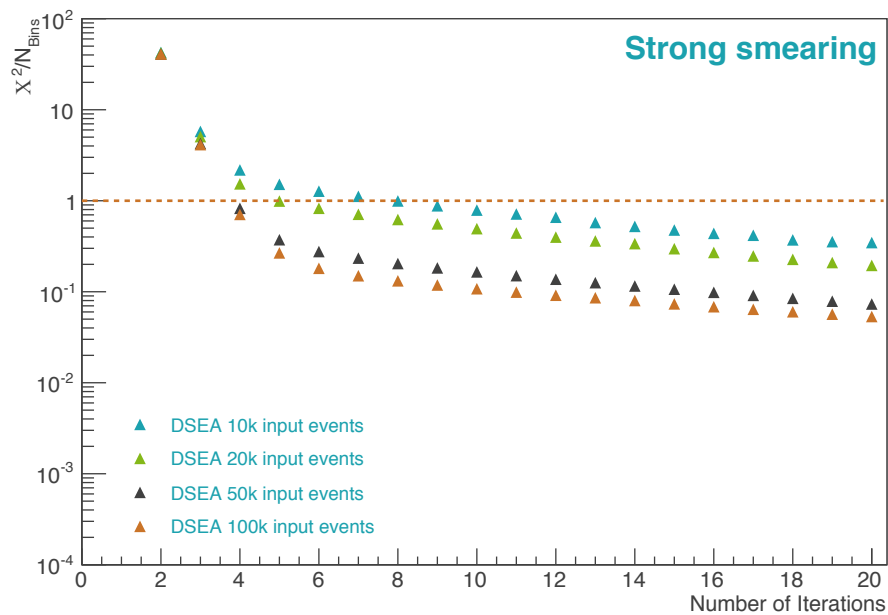
Backup Slides

Here be dragons.

Overlap with Existing Algorithm

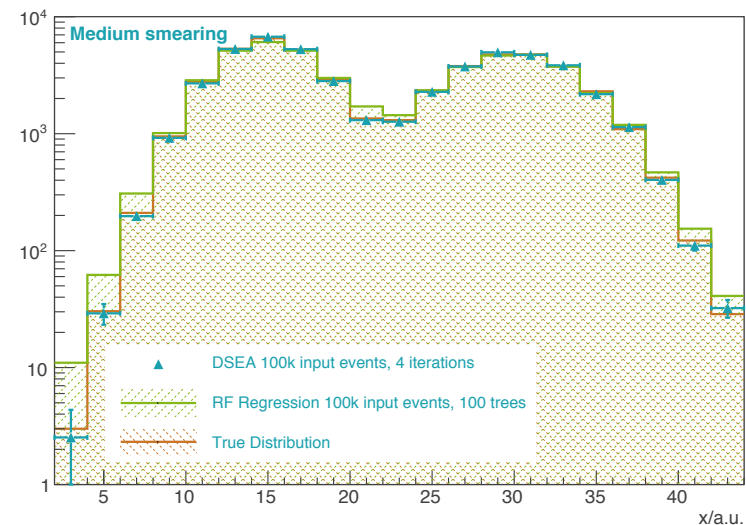
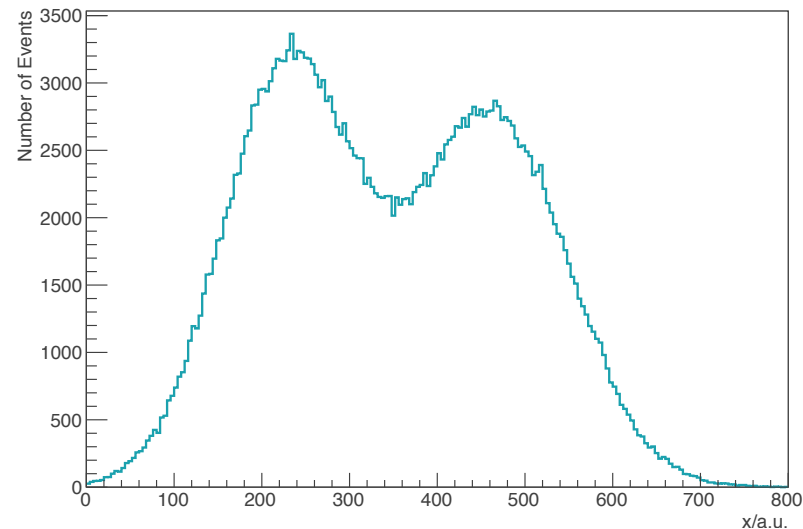
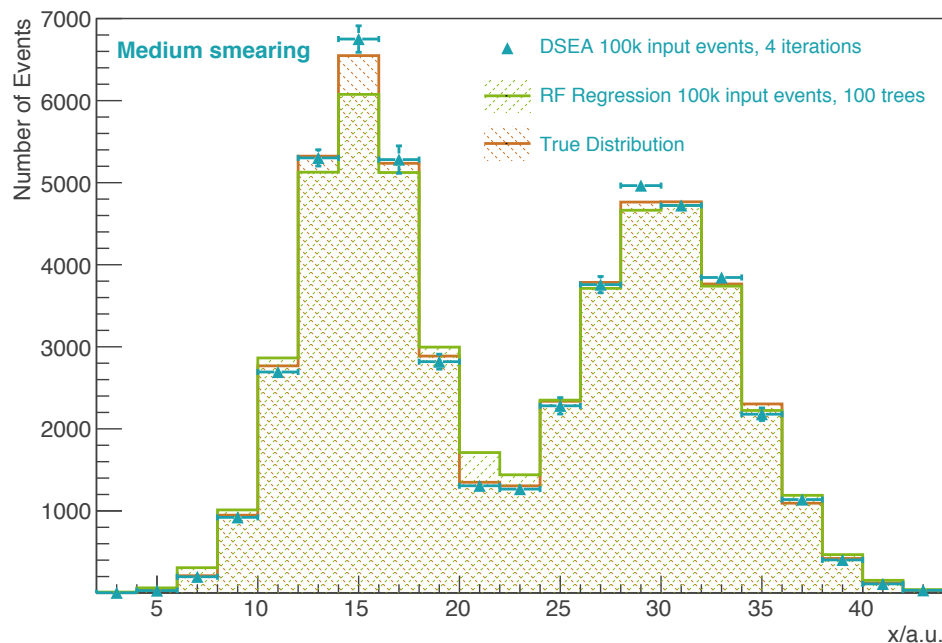
- Some overlap with Kernel Density Estimation, but...
 - ... Kernel function not predefined, so confidence distribution can be anything
 - ... „Kernel“ in DSEA is discrete
- Some overlap with Iterative Bayesian Unfolding, especially if Naive Bayes is used as a classifier, but...
 - ... Event-by-event, rather than bin-by-bin
 - ... Fully retains information on individual events

Convergence for Strong and Medium Smearing

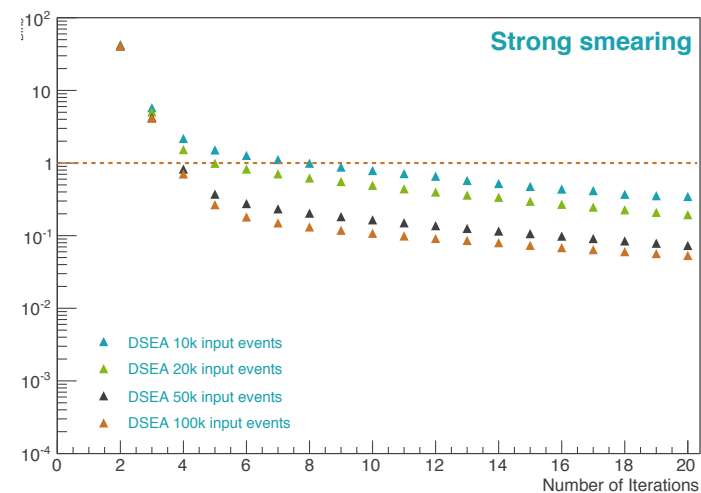
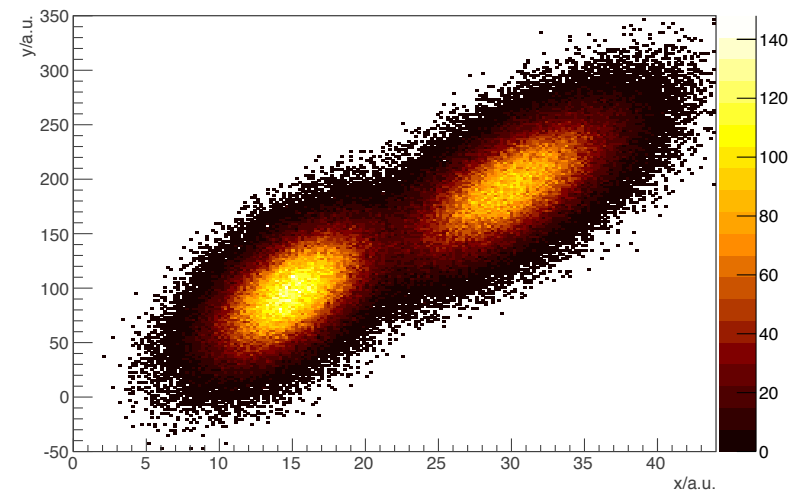
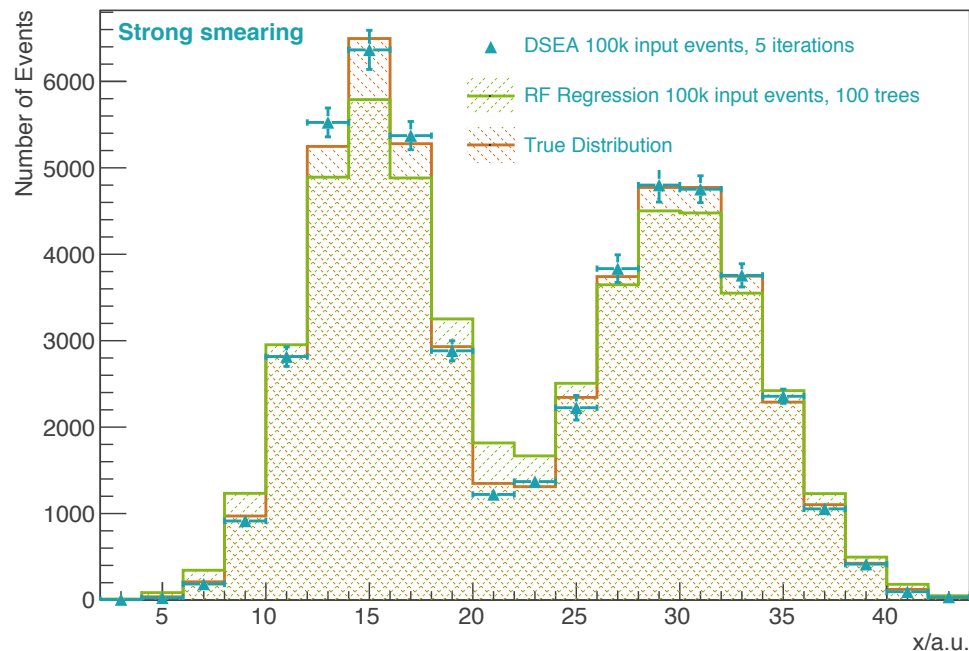


Performance – Spectral Reconstruction

Spectral Reconstruction for strong medium using DSEA (blue), compared to a Random Forest regression (green).

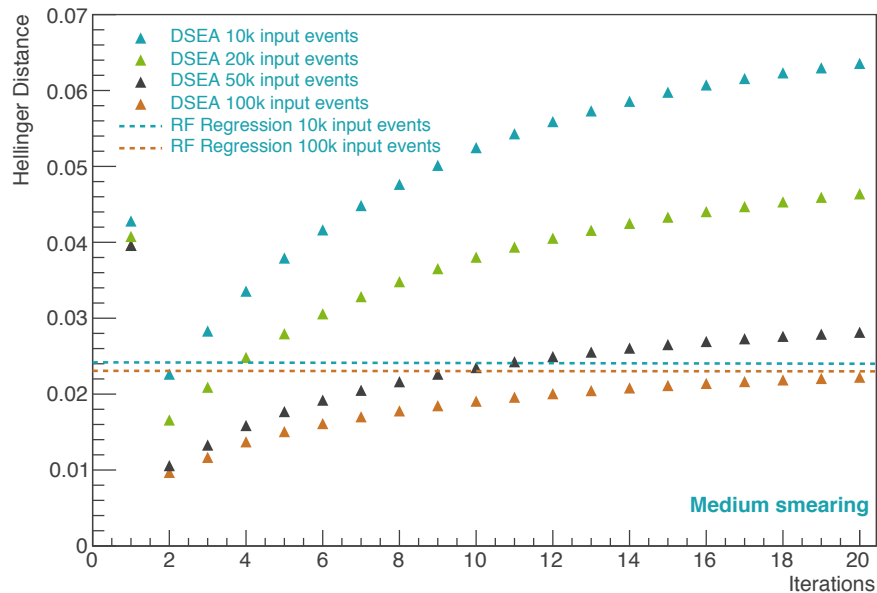


The Dortmund Spectrum Estimation Algorithm (DSEA)

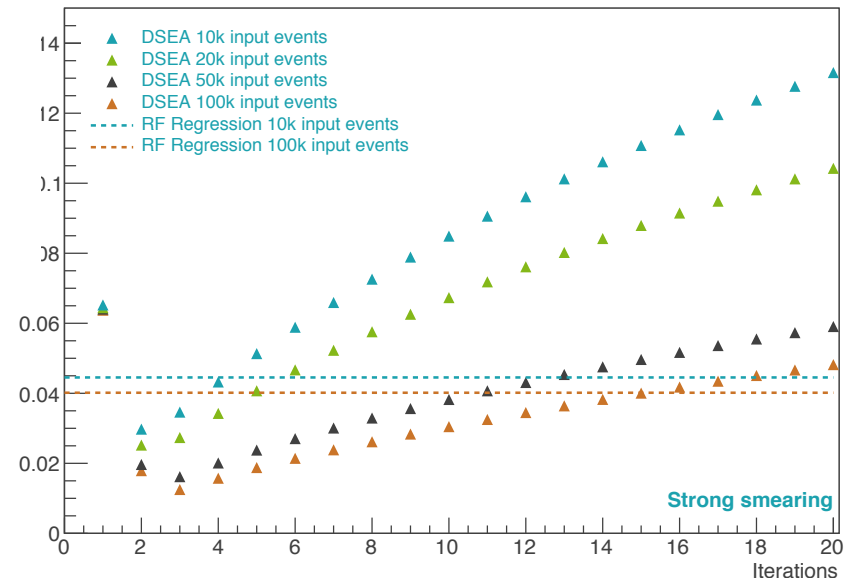


T. Ruhe et al., Proc. of the ADASS XXVI (2016)

Performance – Agreement with Underlying Distribution



Hellinger distance for strong and medium smearing.



More Information is Good for You!

