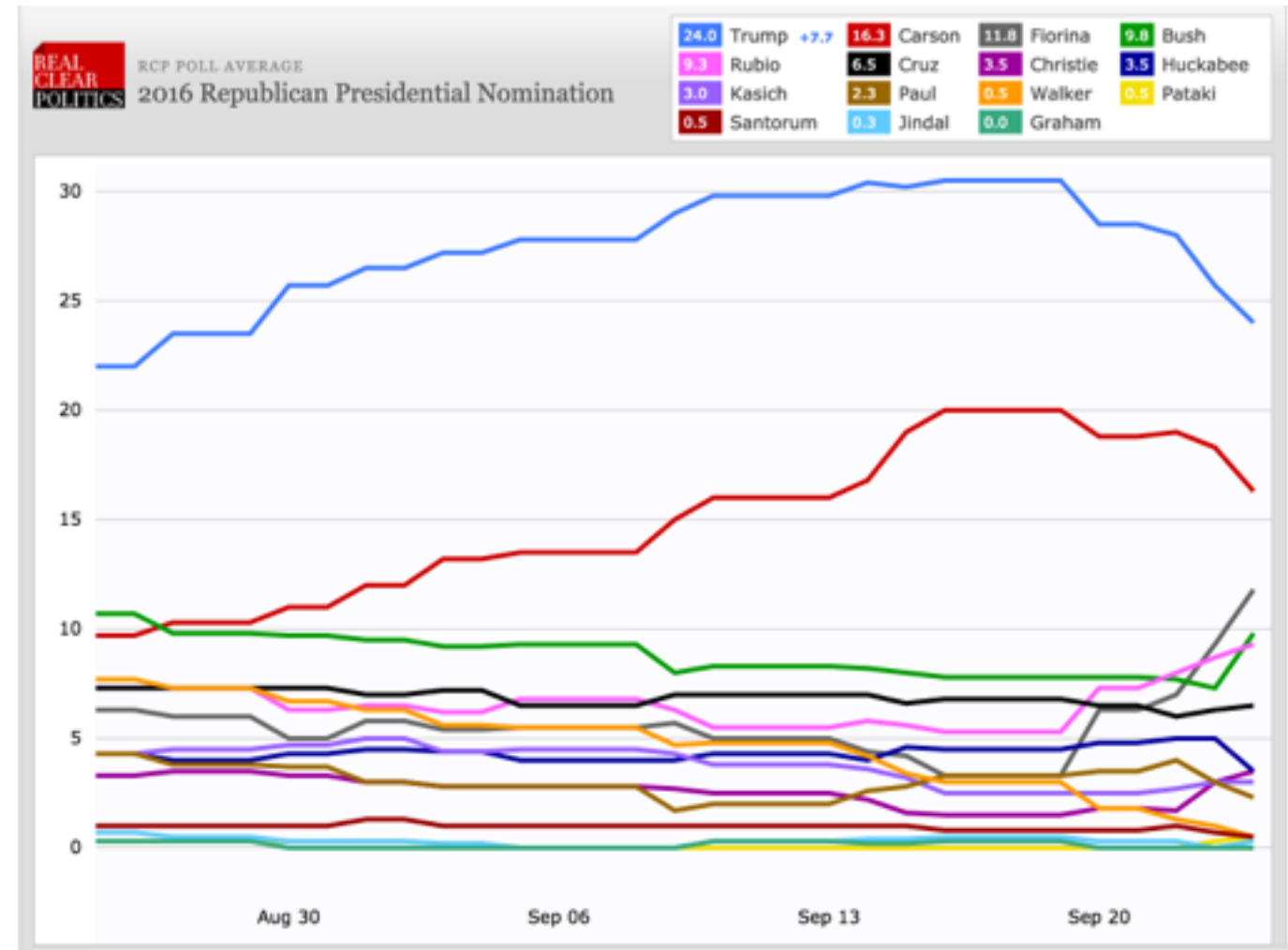
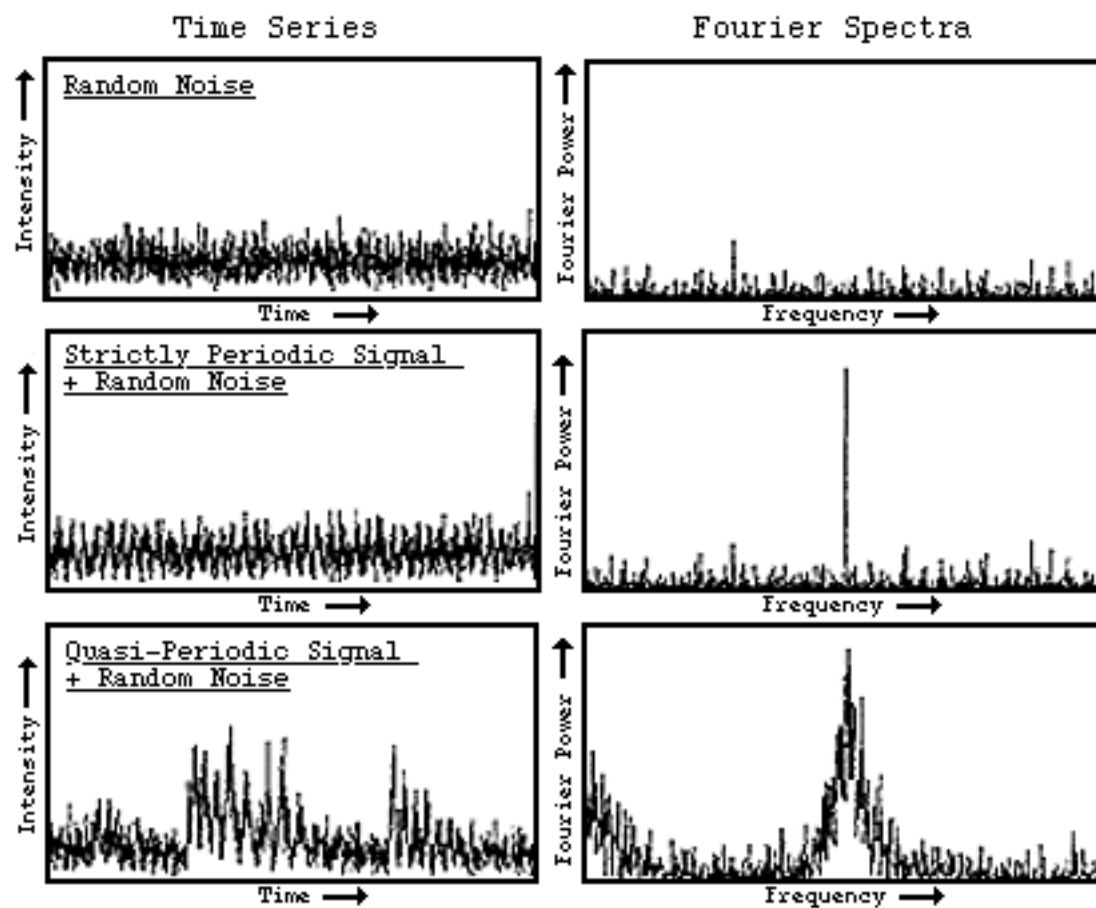


# (High Energy) Astrophysics with Novel Observables



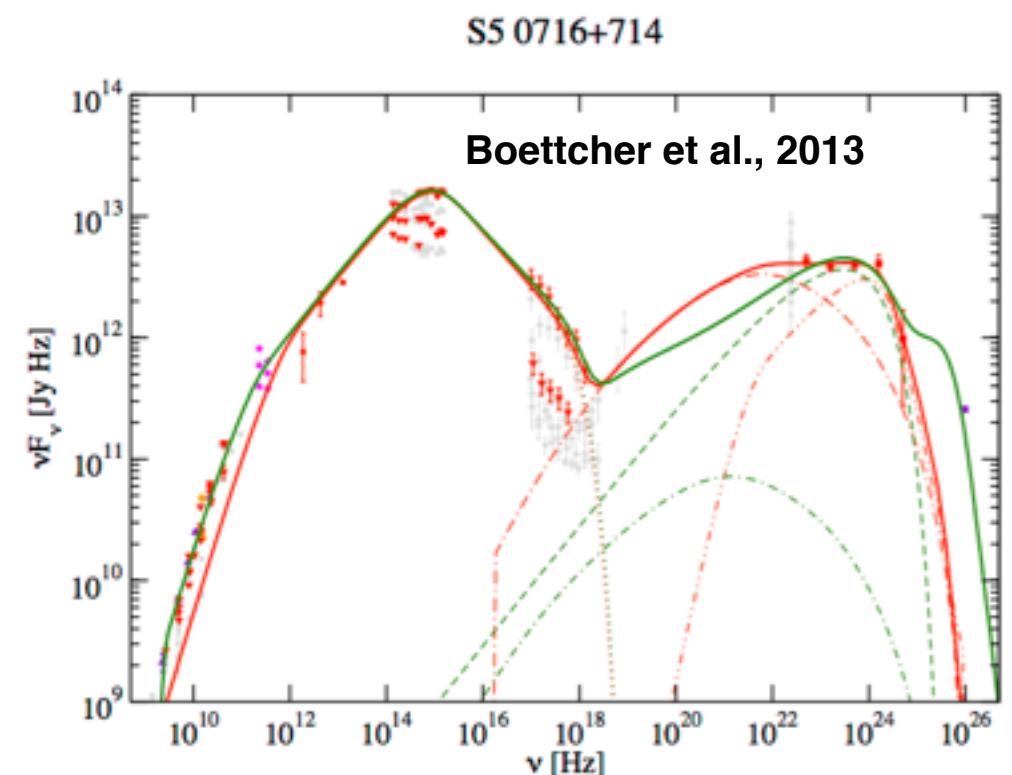
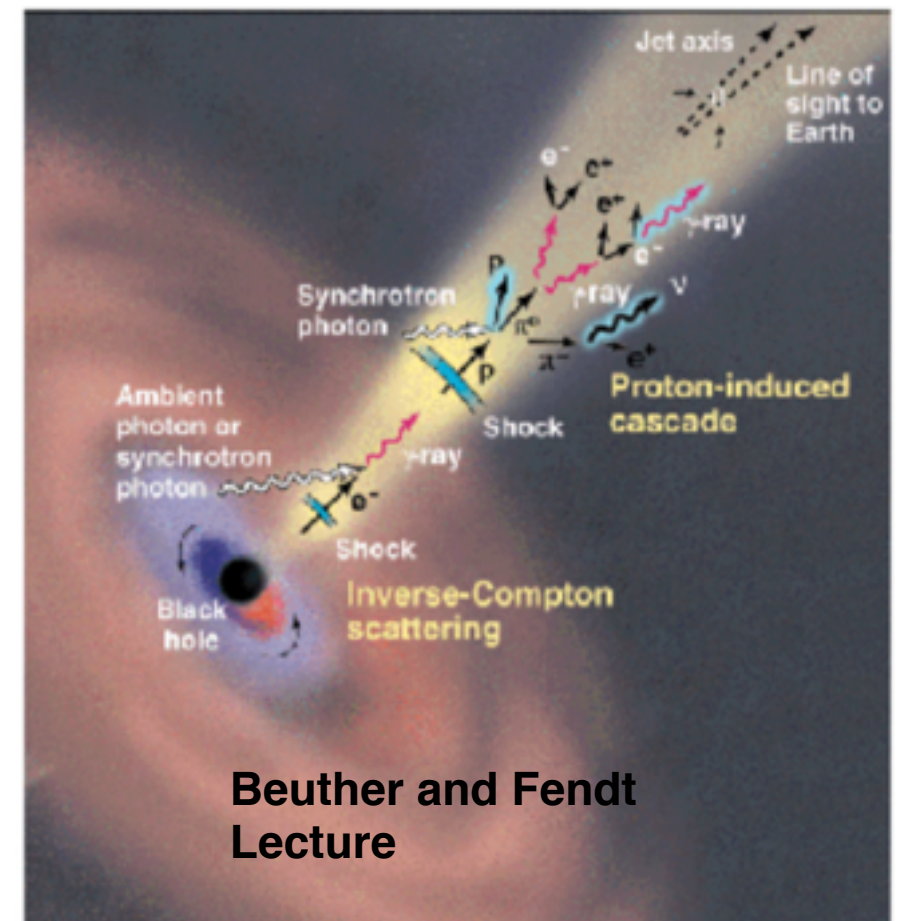
Nachiketa Chakraborty,  
HAP Workshop, 8th December, 2016 Cochem



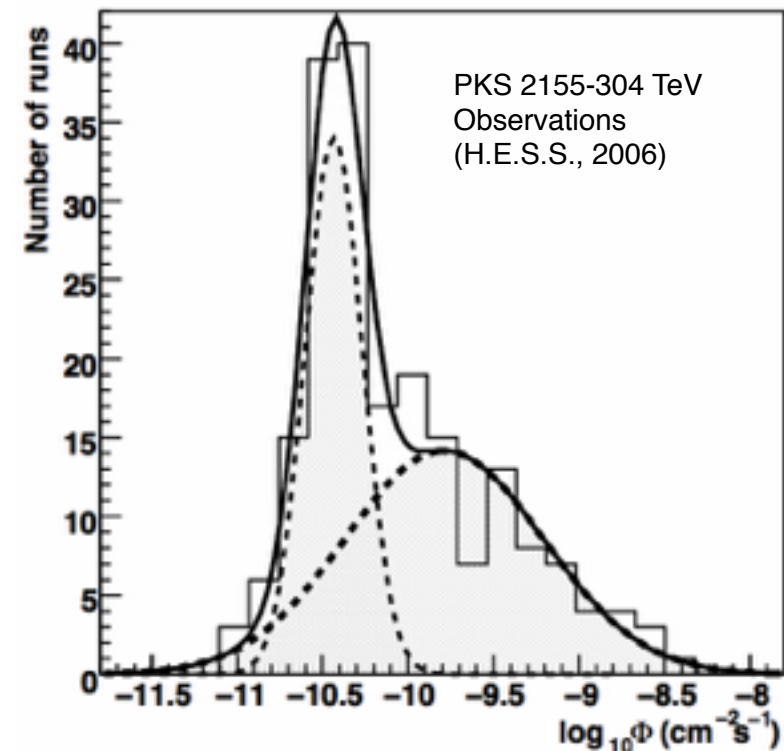
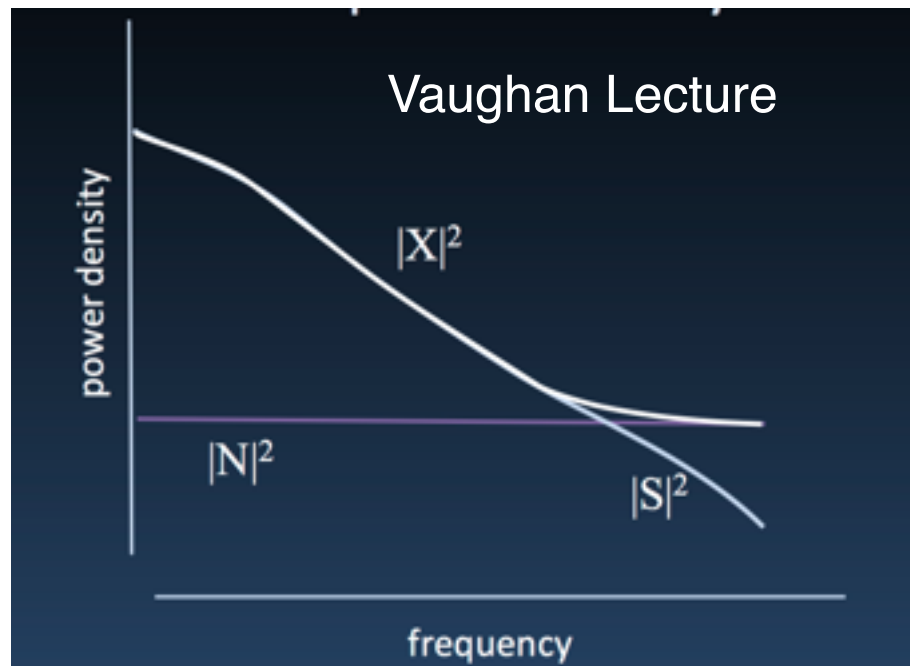
Alexander von Humboldt  
Stiftung/Foundation

# Motivation

- Complexity of physical processes and environment lead to degeneracies (AGNs, GRBs, etc)
- Standard SED modeling, morphology, “eyeballing” lightcurves insufficient - extract more from MWL LCs ?
- Need **newer and novel “observables”** for sharper understanding
- Large datasets  $\Leftrightarrow$  Statistical Methods (both **individual** and population) e.g. time series methods



# Additional Observables ? : PSD and PDF



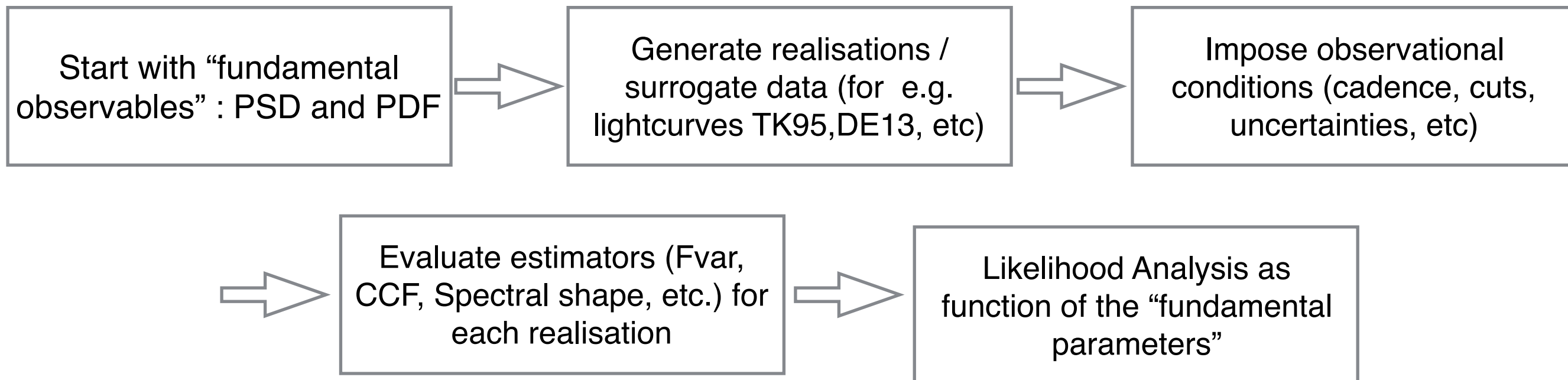
- **Power spectral density** or PSD *encodes temporal structure* - "power distribution in timescales"
- Time :  $x = s + n$  (Vaughan Lecture)  
Fourier :  $X = S + N$   
 $|X|^2 = |S|^2 + |N|^2 + \text{Cross}$   
 $\text{PSD}(f) = \langle |S|^2 \rangle = \langle |X|^2 \rangle - \langle |N|^2 \rangle$
- Formally (for AGNs and others)  
Time :  $\text{Lightcurve}(t) = \text{Dynamical}(t) \times \text{Acceleration}(t) \times \text{Radiation}(t) \times \text{Observation}(t)$  [**Product**]
- Fourier :  $\text{Lightcurve}(f) = \text{Dynamical}(f) * \text{Acceleration}(f) * \text{Radiation}(f) * \text{Observation}(f)$  [**Convolution**]
- First **2 moments** - mean and variance

- **Probability Distribution Function** or PDF *probes the fundamental form of the physical processes*
- Default assumption is Gaussian ;  
evidence for lognormality =>  
Multiplicative (Lyubarskii 97, Uttley et al., 2005)  
or Cascade like processes (exception see Biteau and Giebels, 2012)
- Contains the **skewness and kurtosis** of the underlying data

# General Approach

- Observed Emission
  - Function of **time (lightcurve)**, space (morphology), energy (energy spectrum) **How tells us why**
  - Individual sources : physical mechanisms at emission sites
  - Population : general trends
- **Timing analysis** : Observed light curve is 1 sample or realisation -> we need to “repeat” to get significant results  
(Timmer and Koenig, 1995, Emmanoulopoulos, McHardy and Papadakis, 2013)
- Signal coupled with noise
  - Either disentangle **deterministic** signal from **random** fluctuations (for eg. detecting periodic/QPOs)
  - Or the interesting signals are random fluctuations themselves (for eg. flaring vs quiescence)
- **Observational Irregularities** : Allocation, satellite cycles, visibility, competing targets, etc
  - gaps
  - coarse or uneven sampling
  - length of observation limited

Emmanoulopoulos et al., 2013, Allevato et al., 2013, Chakraborty & Biteau (In prep)





# Fvar and VED

$$Fvar = \frac{\sqrt{S^2 - \sigma^2}}{\phi_{\text{mean}}}$$

- Increasingly used for MWL studies
- Simple yet *not unbiased estimator*
- Energy / wavelength dependent Fvar => VED

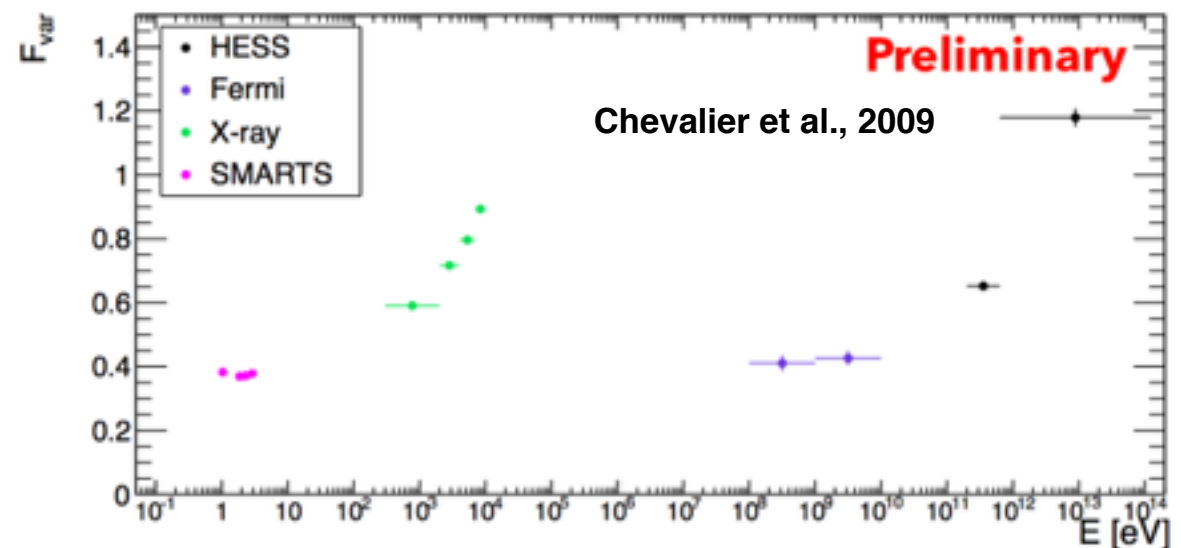
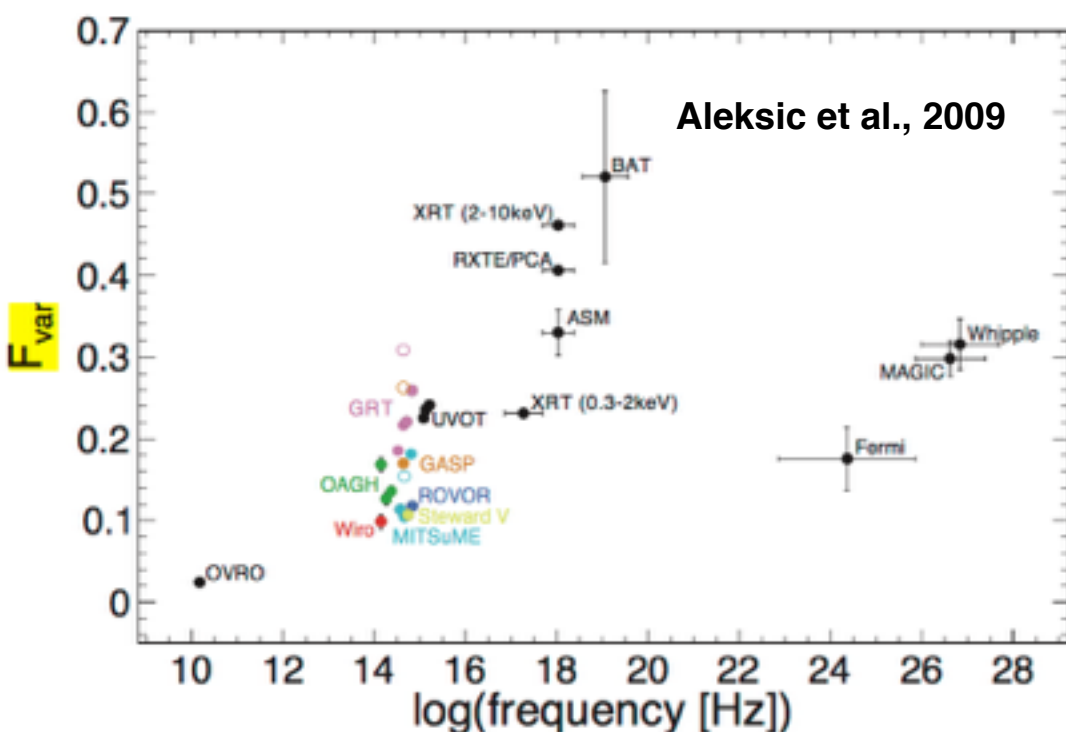
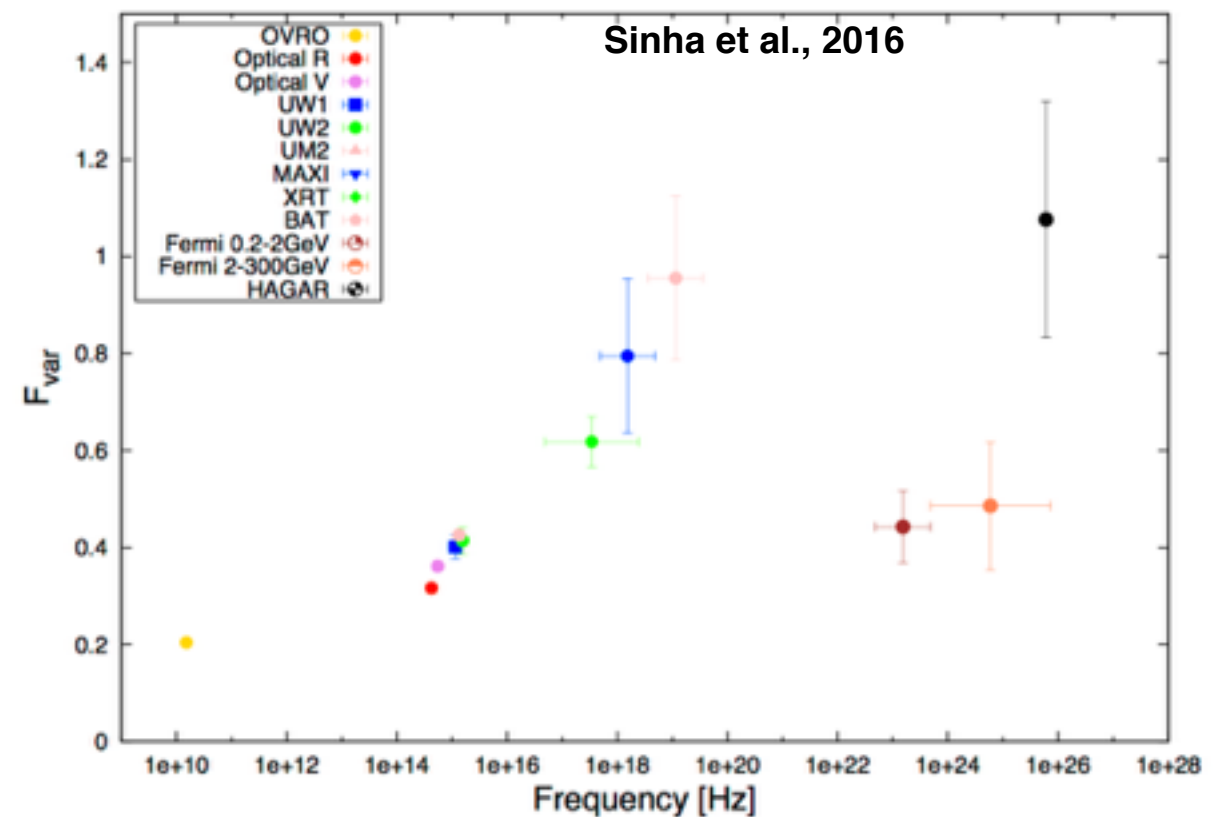
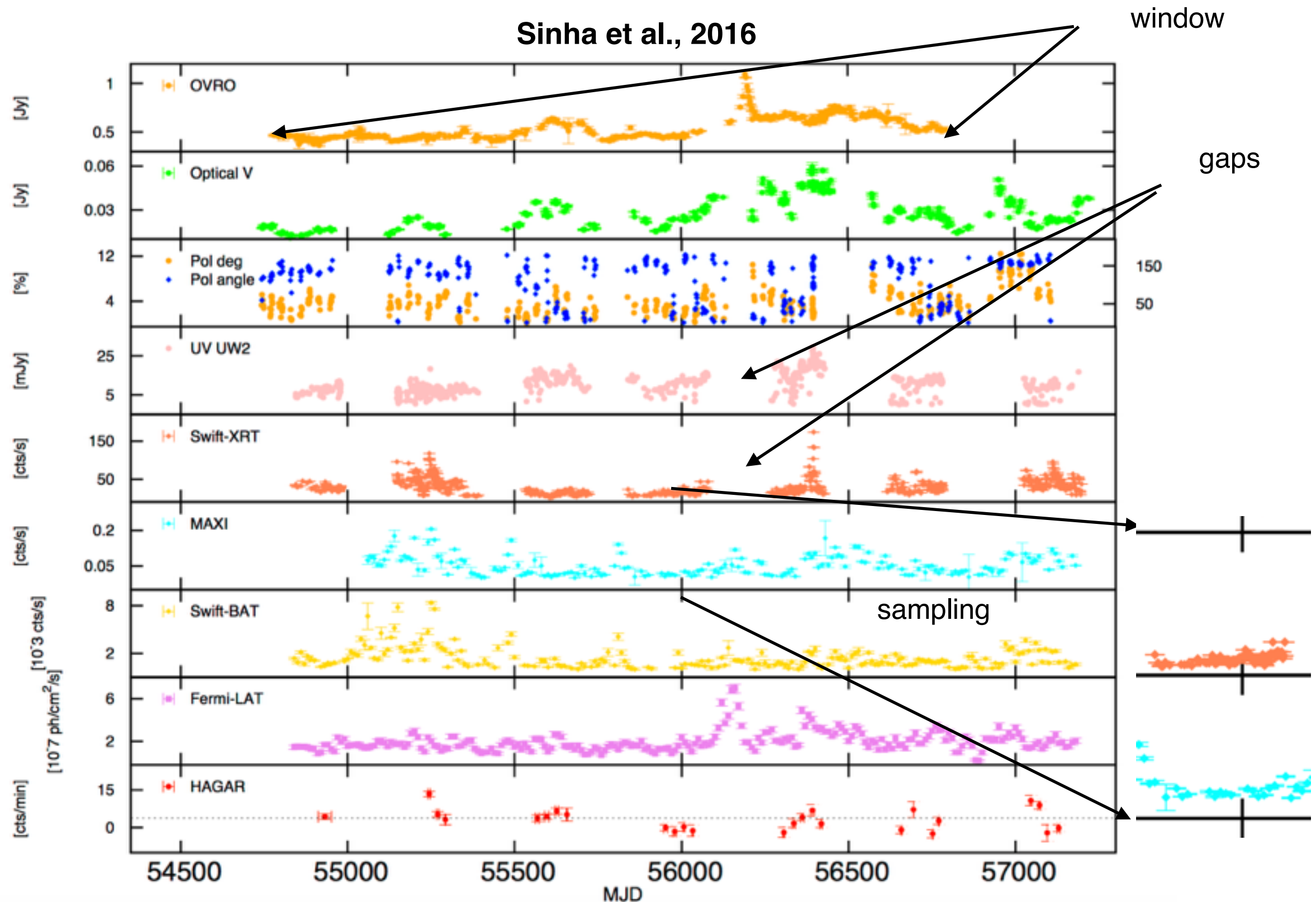


Figure 3: VED of PKS 2155-304.

- Lightcurve(f) = Dynamical(f) \* Acceleration(f) \* Radiation(f) \* **Observation(f)**

# MWL Observations of Mrk 421



# Method to estimate $F_{\text{var}}$

Start with “fundamental observables” : PSD (**PL**) and PDF (**Gaussian**)

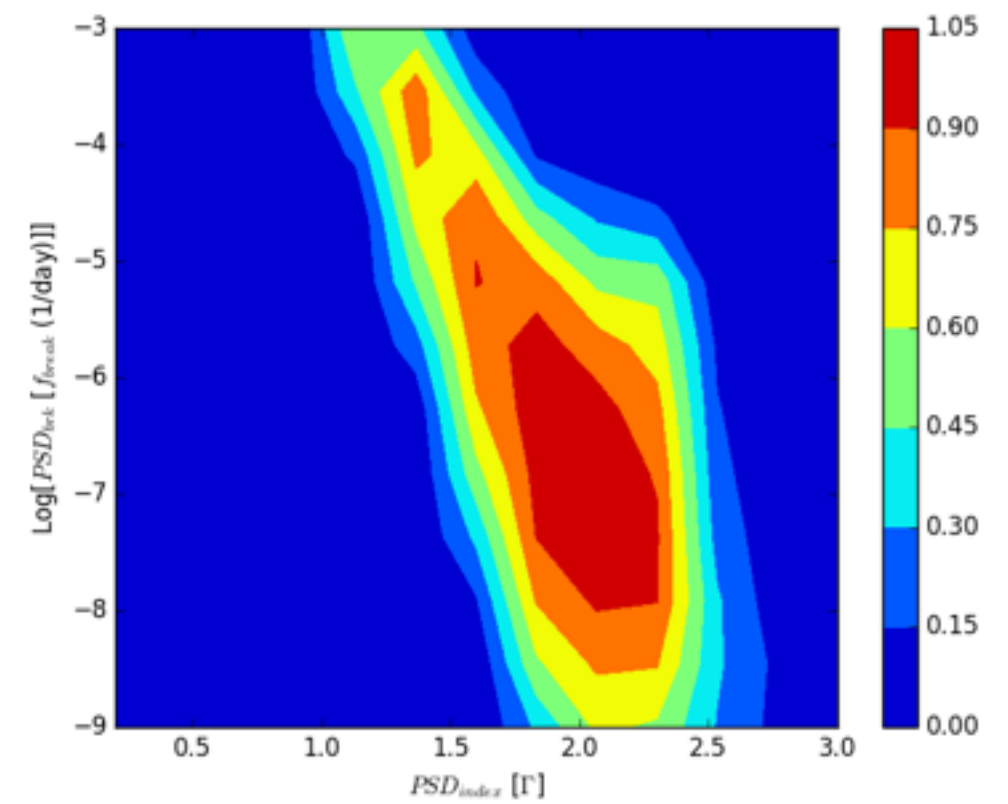
Generate realisations / surrogate data (for e.g. lightcurves **TK95**, DE13, etc)

Impose observational conditions (**cadence**, cuts, uncertainties, etc)

Evaluate estimators ( **$F_{\text{var}}$** , CCF, Spectral shape, etc.) for each realisation

Likelihood Analysis as function of the “fundamental parameters” (**Map of index and norm**)

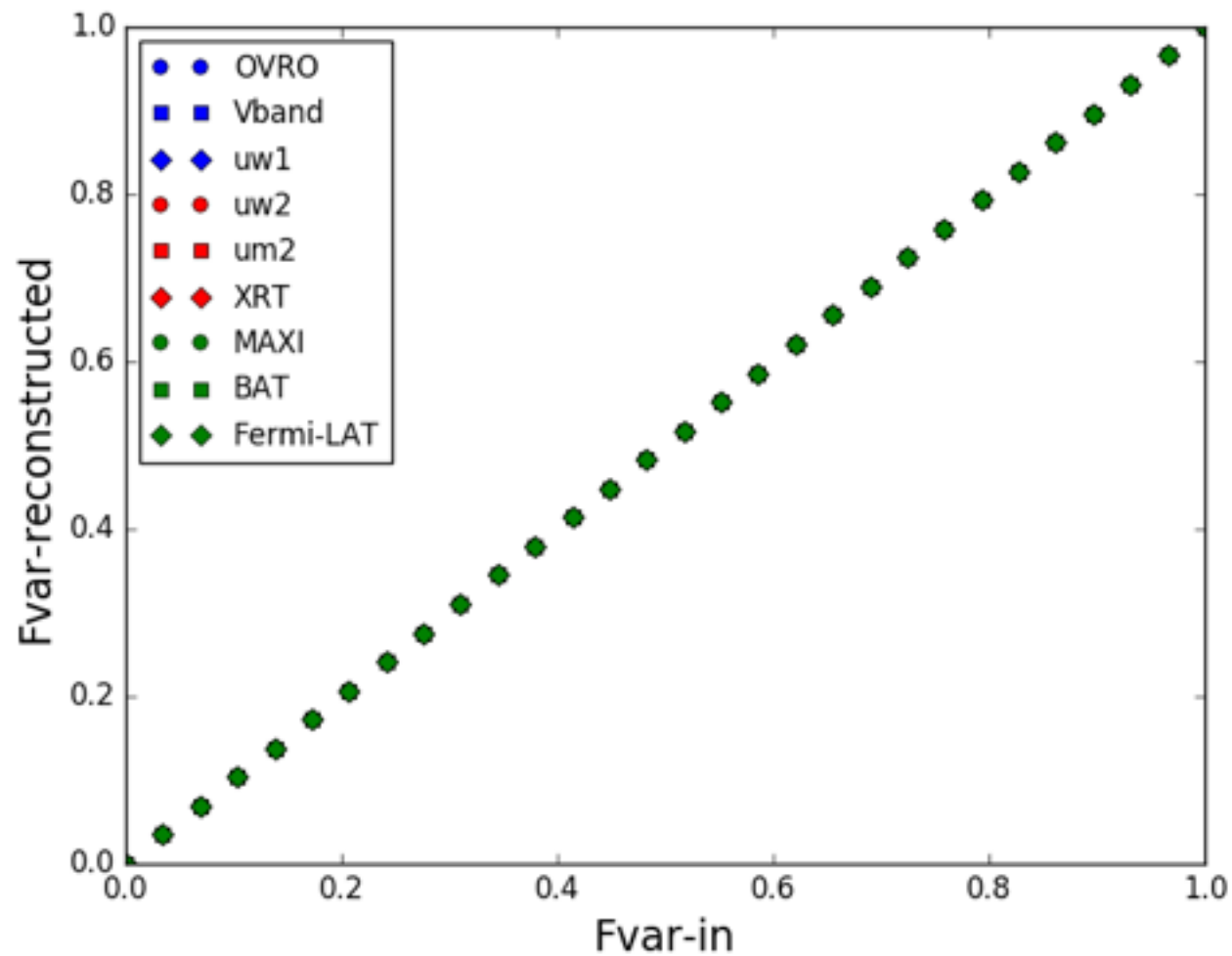
Sinha et al., 2016



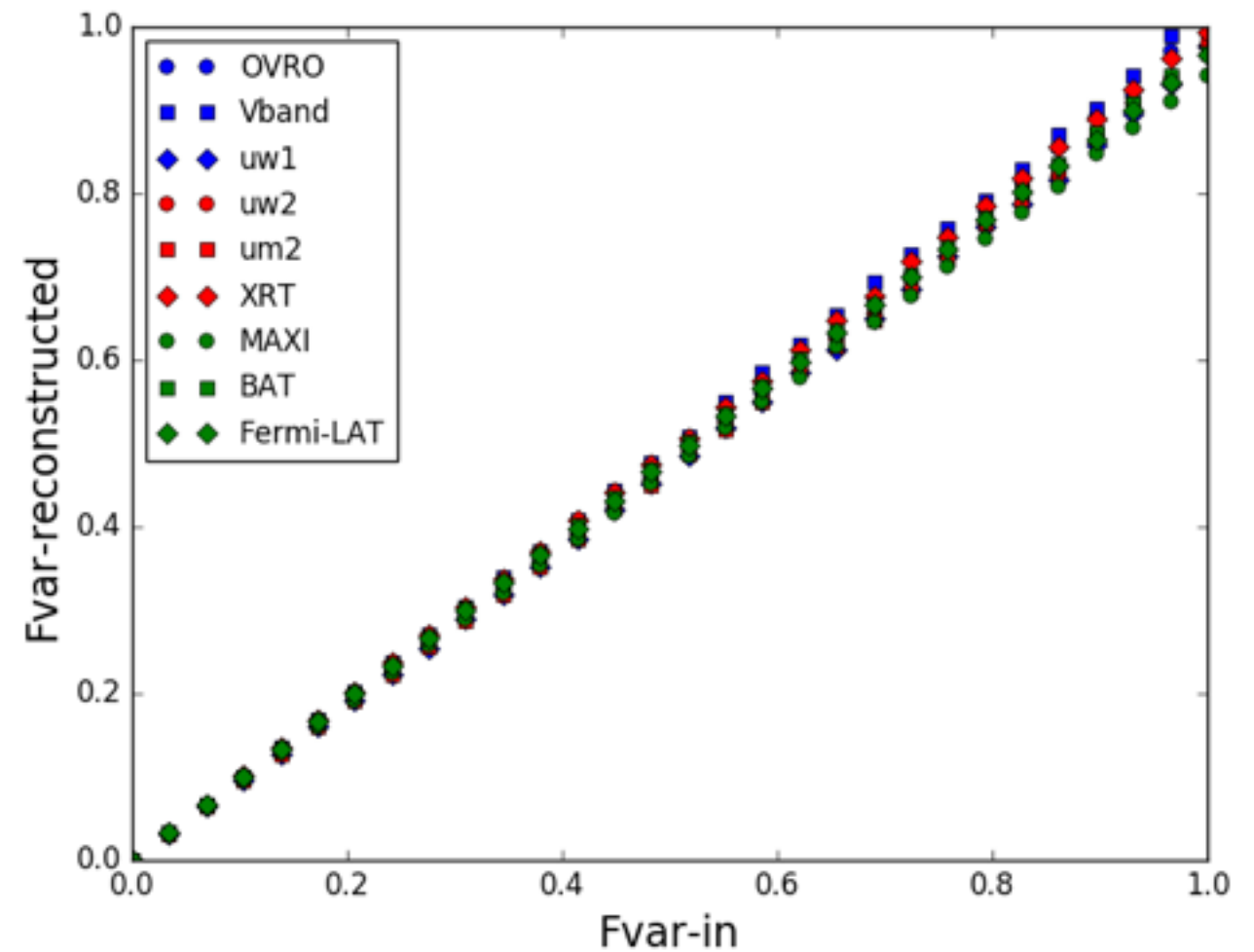
# Fvar reconstruction

Red Noise : Index = 2.0

“Ideal” Cadence



Observed Cadence

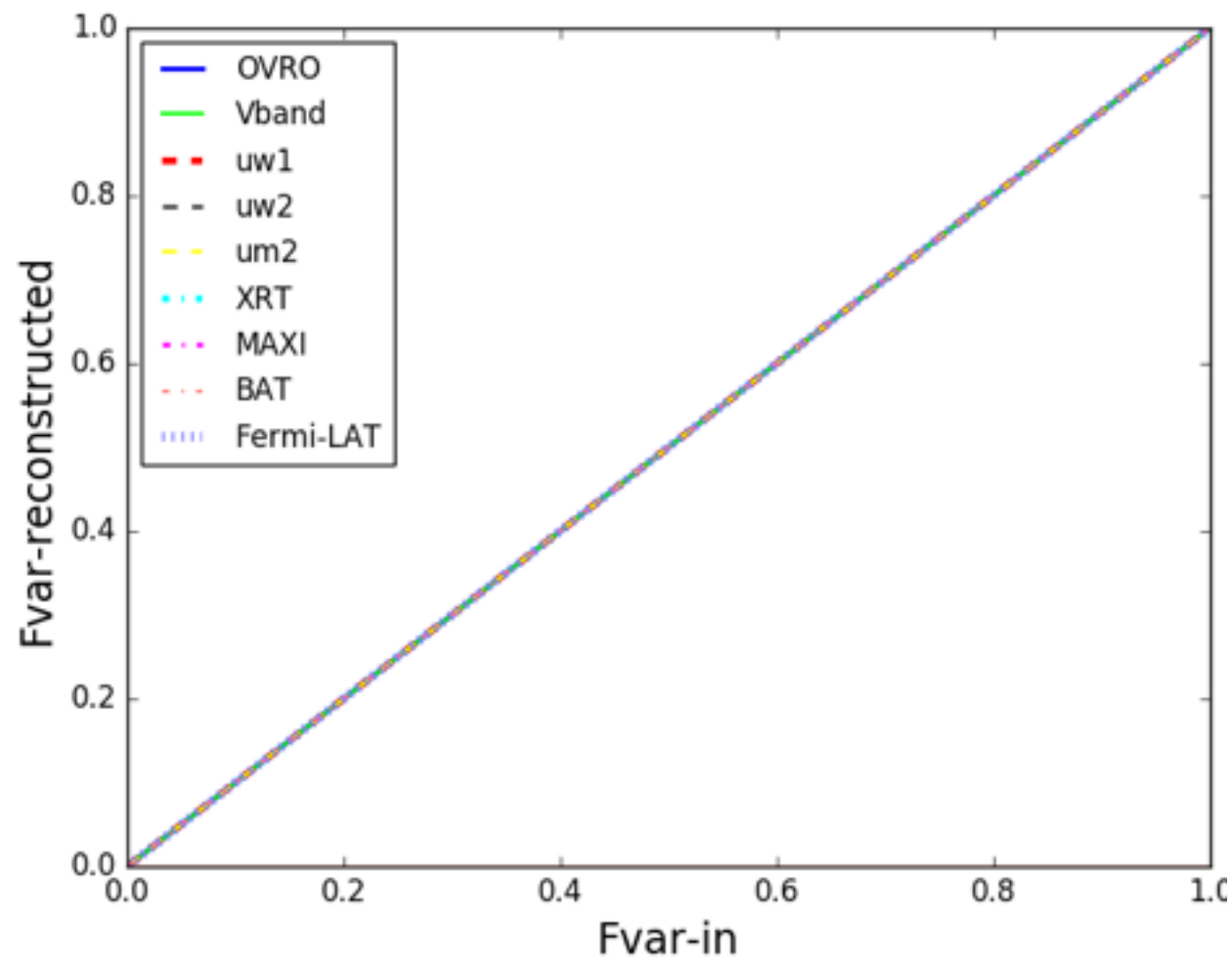




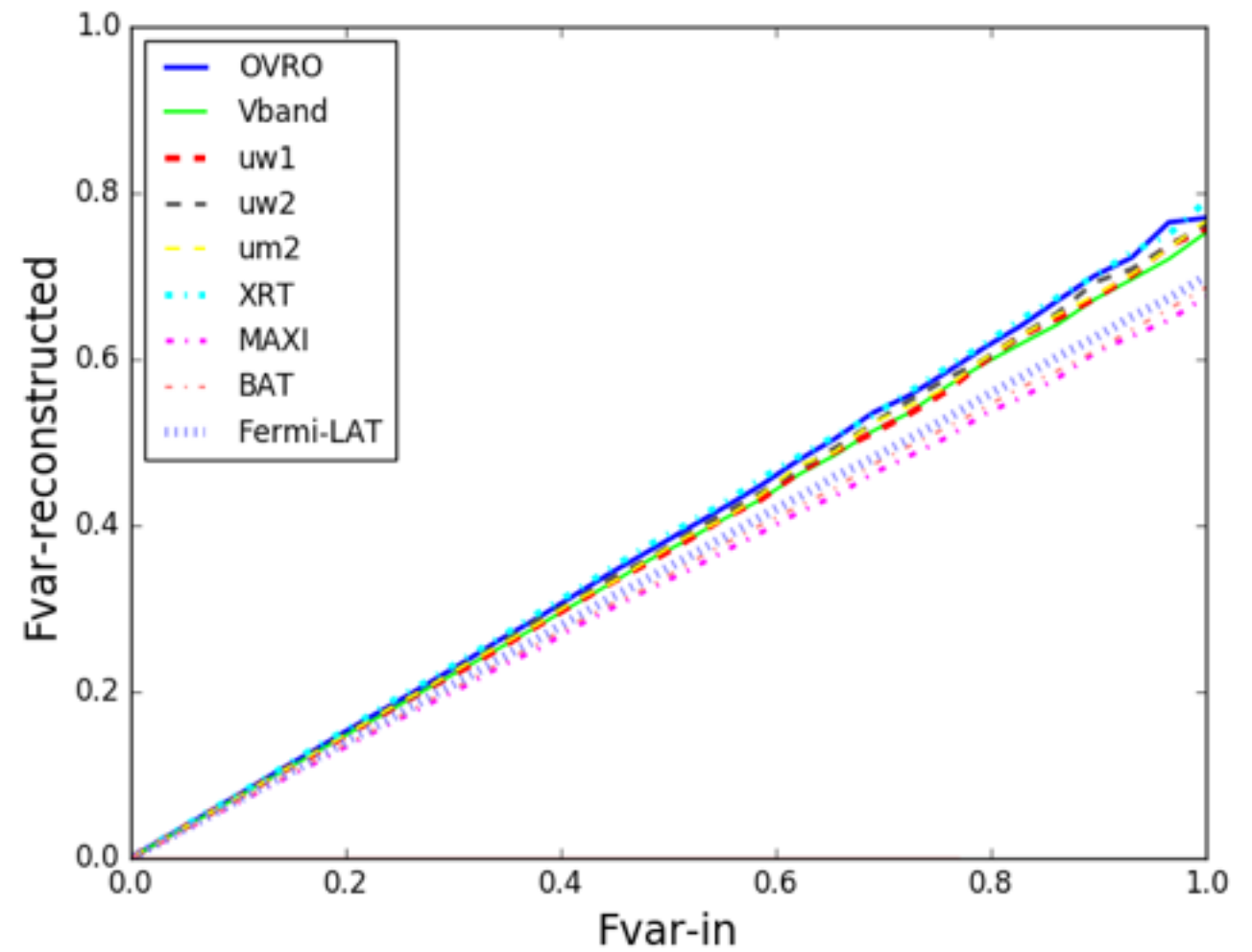
# Fvar reconstruction

Pink Noise : Index = 1.0

“Ideal” Cadence



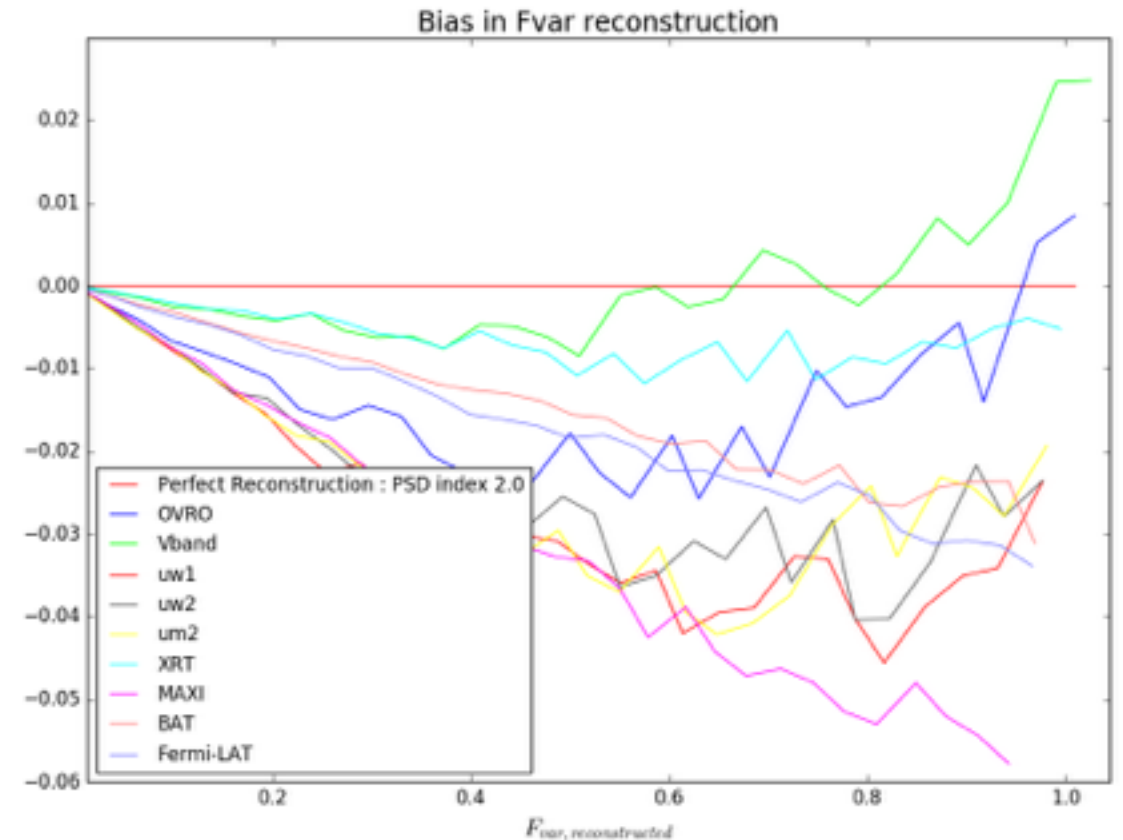
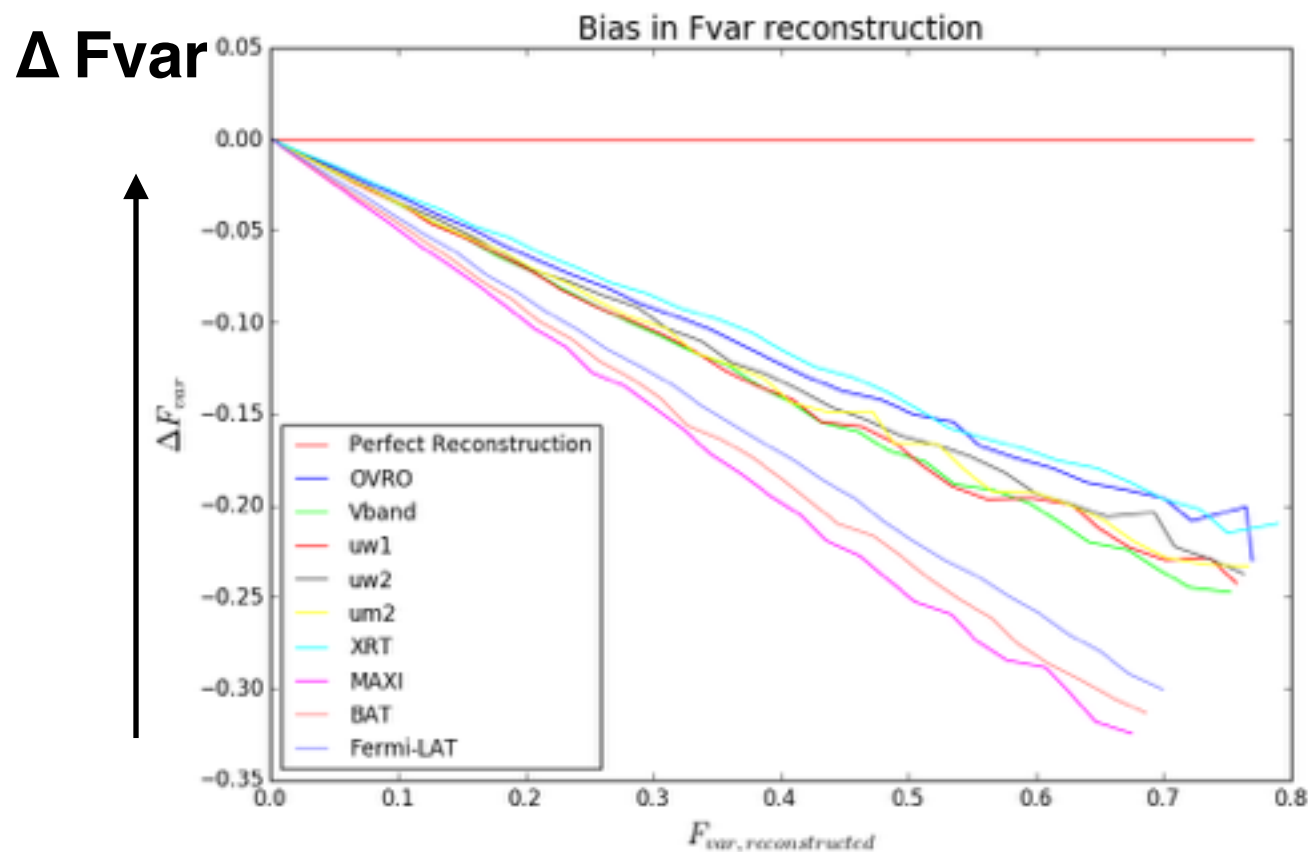
Observed Cadence



# Fvar reconstruction

simulation PSD index = 1.0

simulation PSD index = 2.0



**Fvar,obs** →

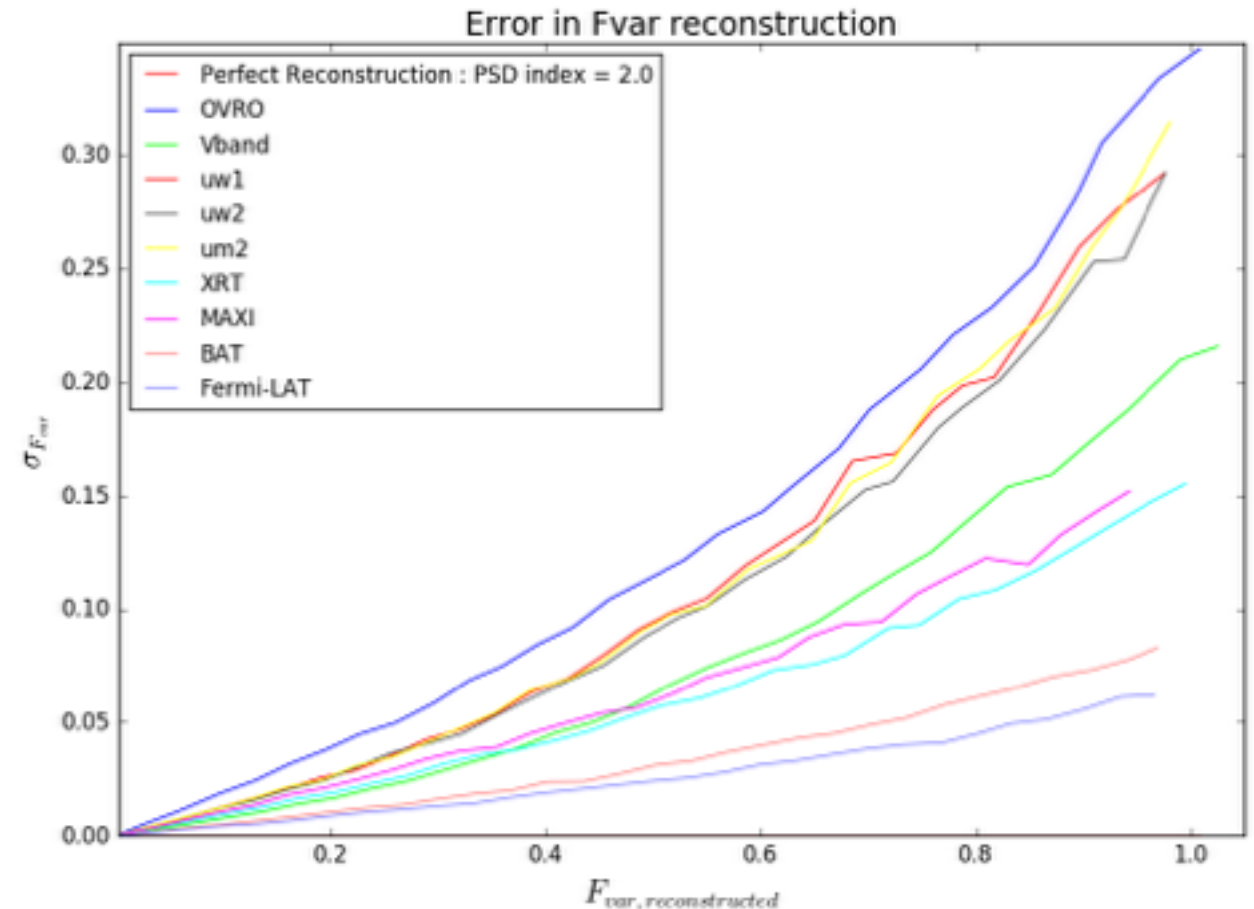
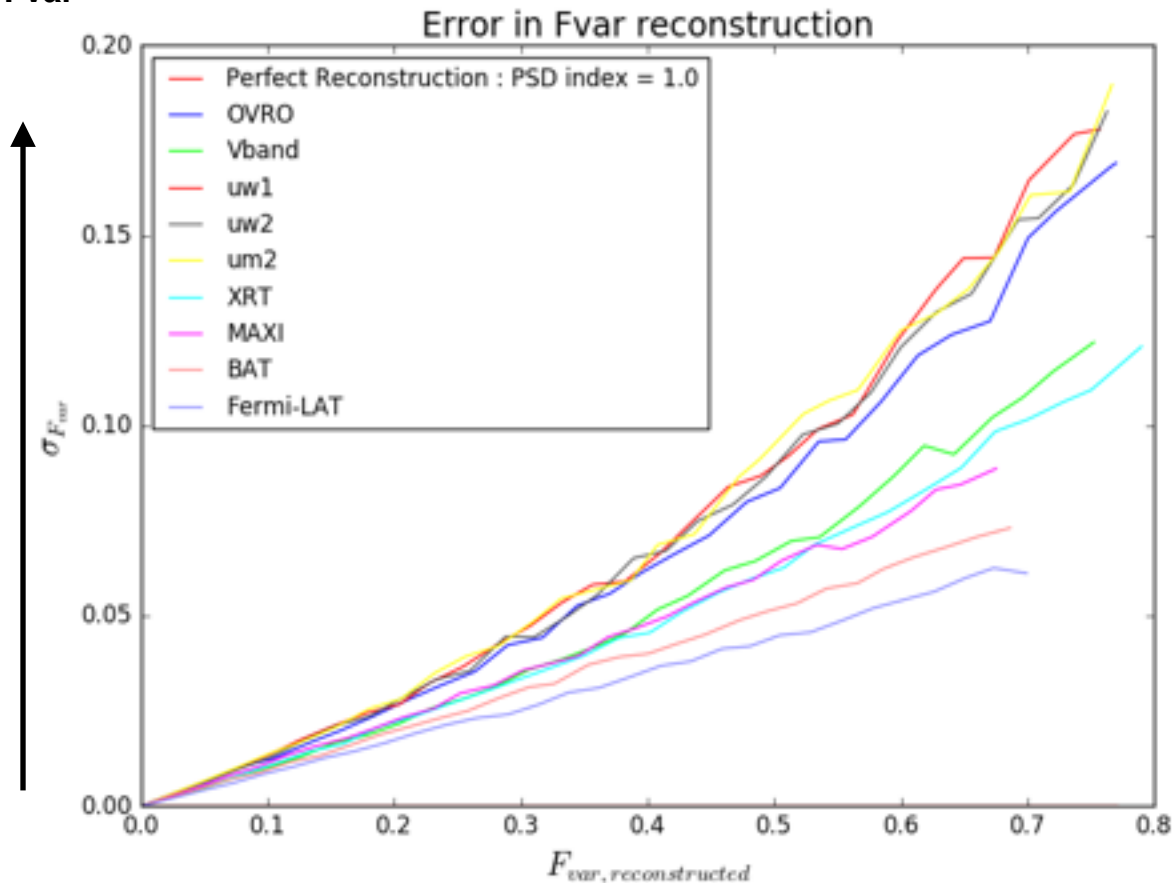
- Bias due to observational effects - larger for harder PSD (brown vs red) -> sampling effects ?
- Relatively, best reconstructions for finely sampled, least “gapped” (OVRO, Vband)
- Length of observational window less important for long enough durations and slow variations

# Fvar reconstruction....

simulation PSD index = 1.0

simulation PSD index = 2.0

$\sigma_{Fvar}$

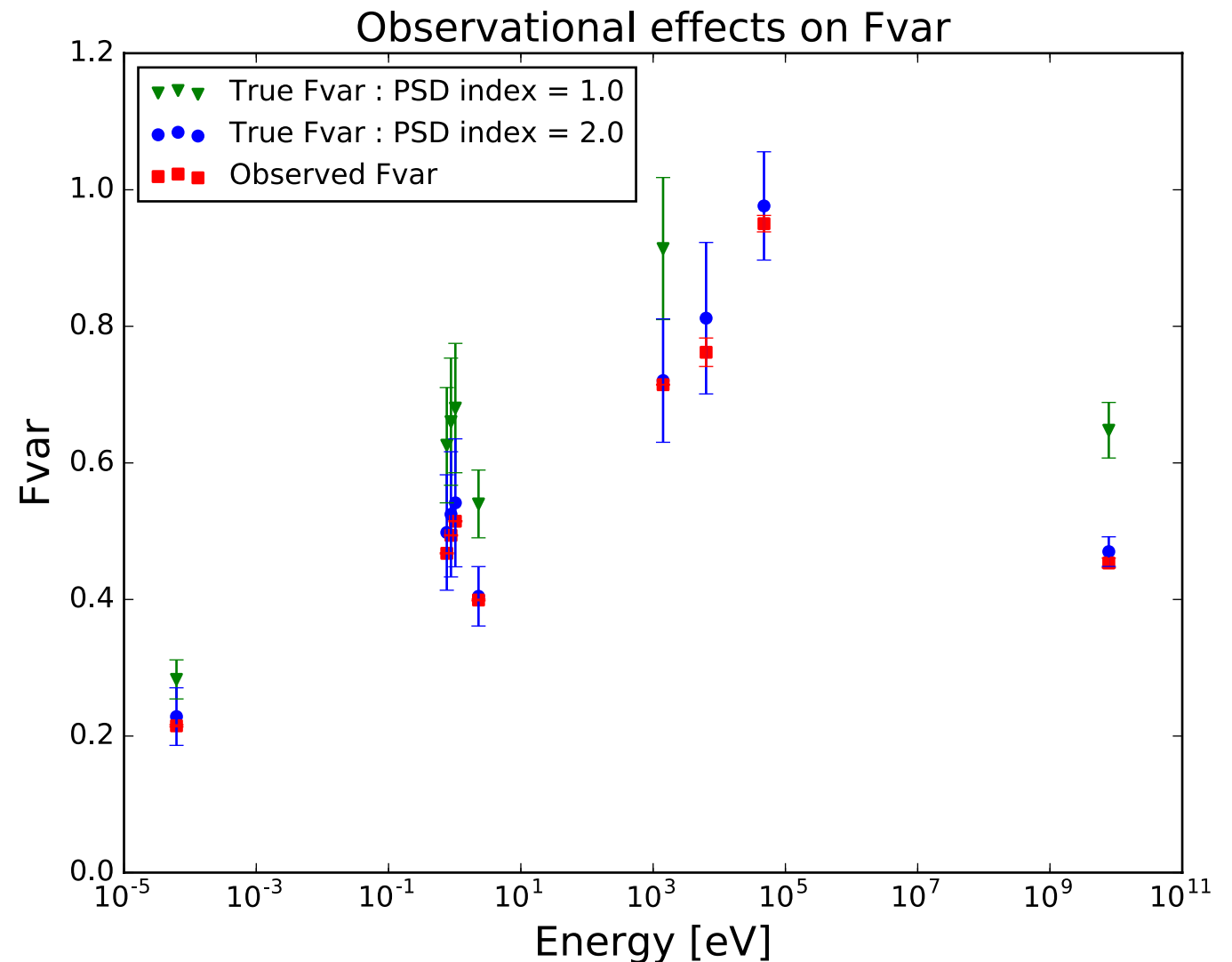


**Fvar,obs** →

- Uncertainty in Fvar comparable for brown vs red noise
- Relative uncertainty larger for longer wavelengths - larger dispersion ( $\sigma$  **does not** include flux errors)

# Variability Energy Distribution

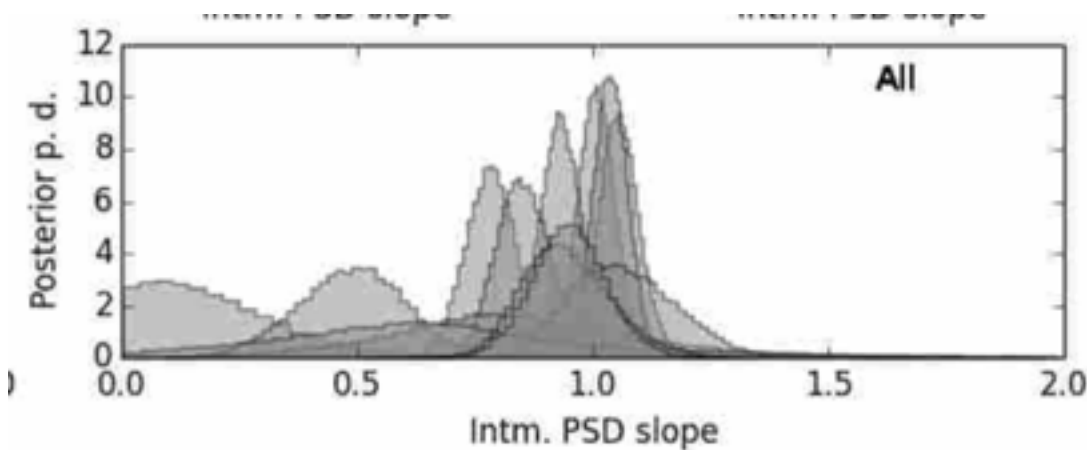
- Even with red noise, both the **uncertainty and bias due to observational effects are non-trivial**
- Correct estimate of variability necessitates incorporating these systematic uncertainties
- Crucial to have coordinated observational cadence across wavelengths
- Further work - **non-Gaussian PDFs**, tests for stationarity



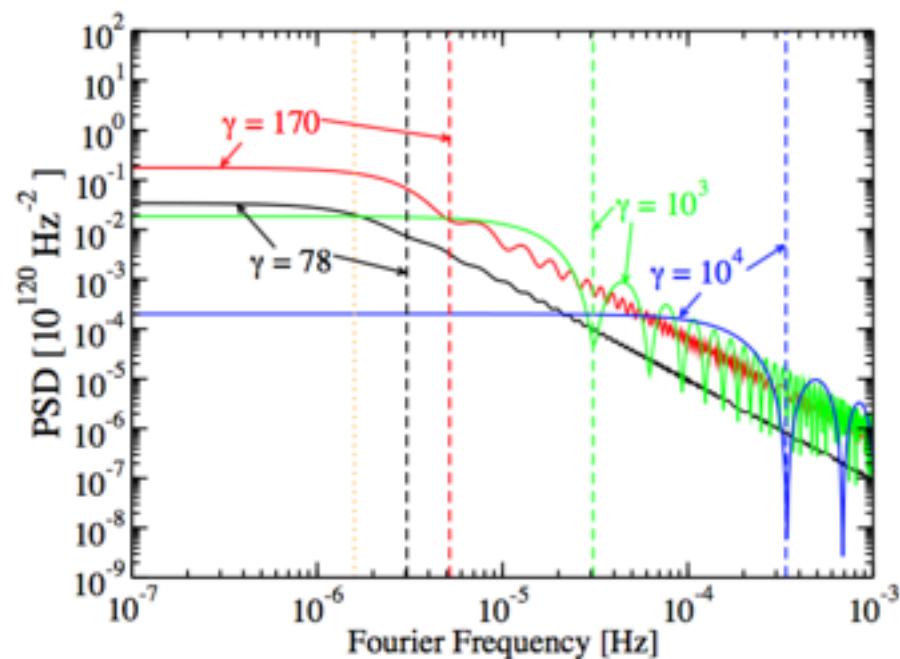
- *Several applications with simulated LCs*
  - Other estimators like CCF, doubling times, etc. (previous talks, Vaughan, Emmanoulopoulos et al)
  - Polarisation variability (Blinov - RoboPol first season results)
  - Estimation of flaring in AGNs
- *etc.....*

# Origin of Power-laws

- $\text{Lightcurve}(f) = \text{Dynamical}(f) * \text{Acceleration}(f) * \text{Radiation}(f) * \text{Observation}(f)$



LAT : 100 MeV - 300 GeV LCs, 4 years  
Sobolewska et al., 2014



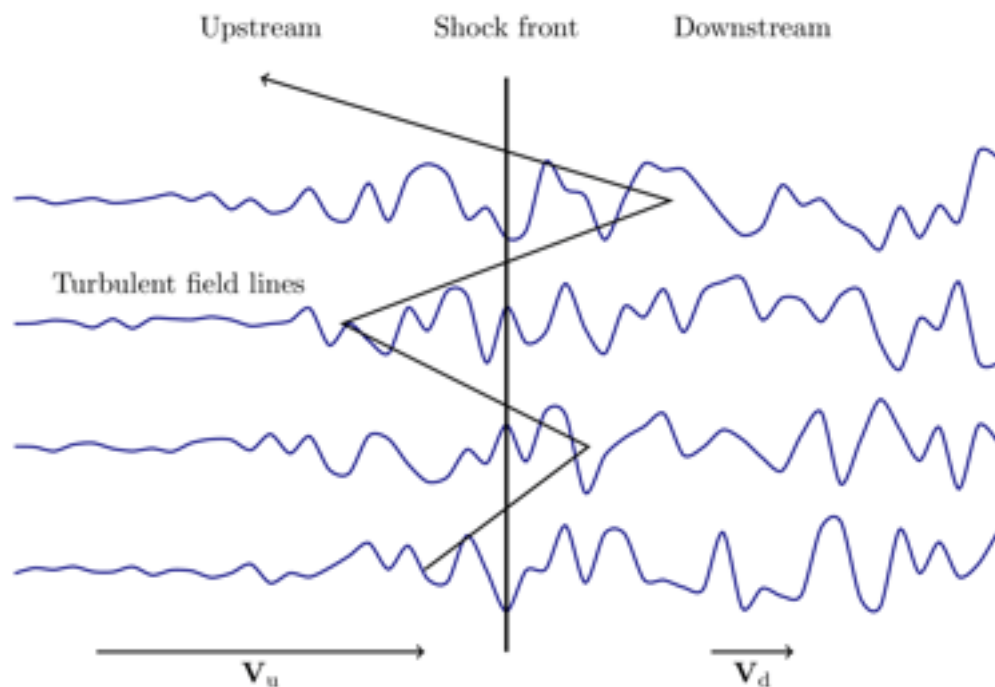
Finke et al., 2014

- Attempts at deeper theoretical understanding of timing characteristics (Lyubarskii et al., 1997, Rieger and Volpe 2010, Finke et al., 2014, 2015, Pollack et al. 2016)
- Understanding origin of temporal structure of fluctuations (PSD)
  - why power-law PSDs ?
  - fluctuations in injection - but what is the source ?
  - fluctuations in accretion flow -> flicker noise (PSD index 1 - 2)
  - jet-disk connection **cannot account** for **minutes** timescales in TeVs (no Doppler)
  - MHD turbulence -> shortest timescales

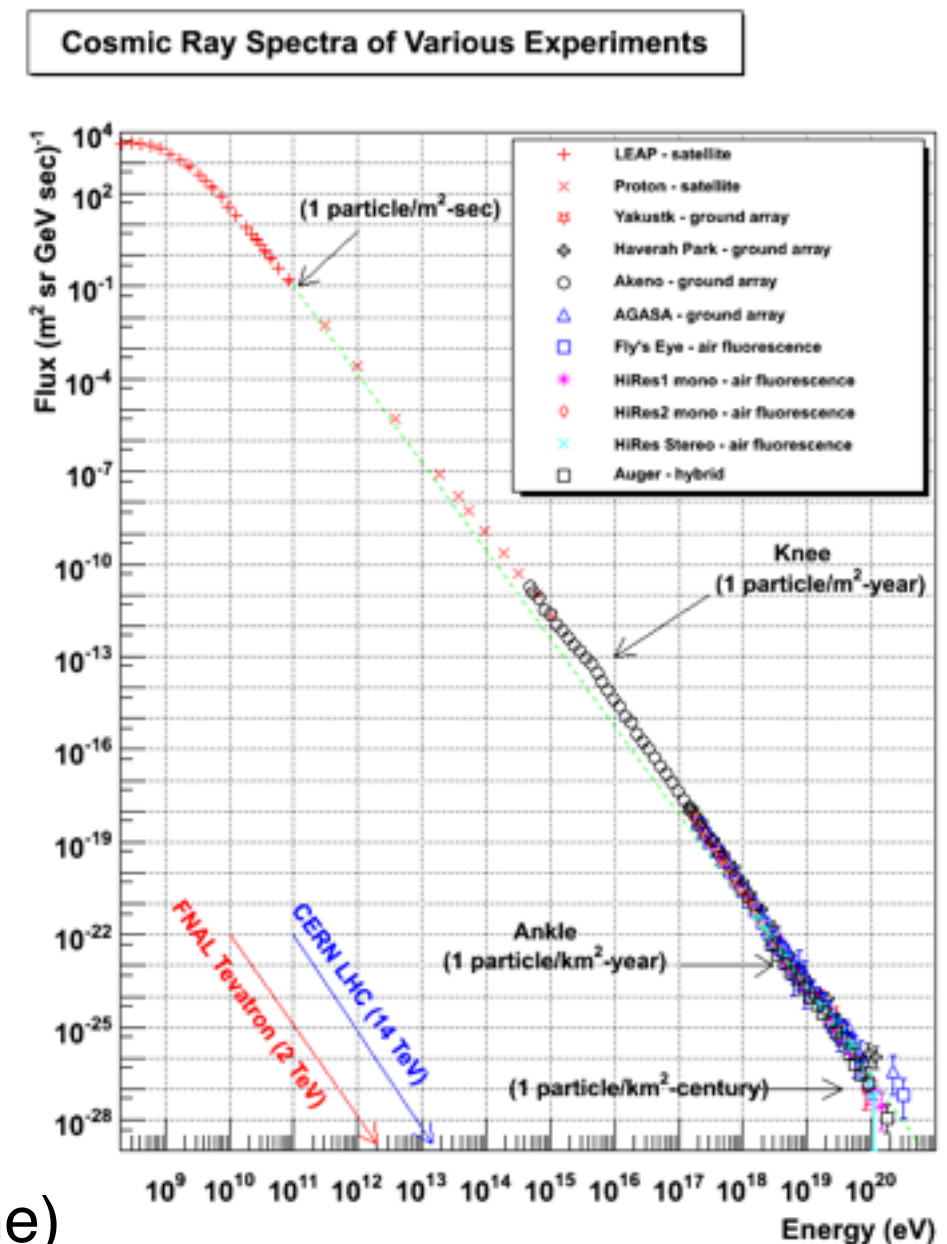


# Particle Acceleration -> Power-Laws

- Lightcurve(f) = Dynamical(f) \* **Acceleration(f)** \* Radiation(f) \* Observation(f)



⇒



Could they have same origin ?  
(Analytical / simulations with Simone Giacche)

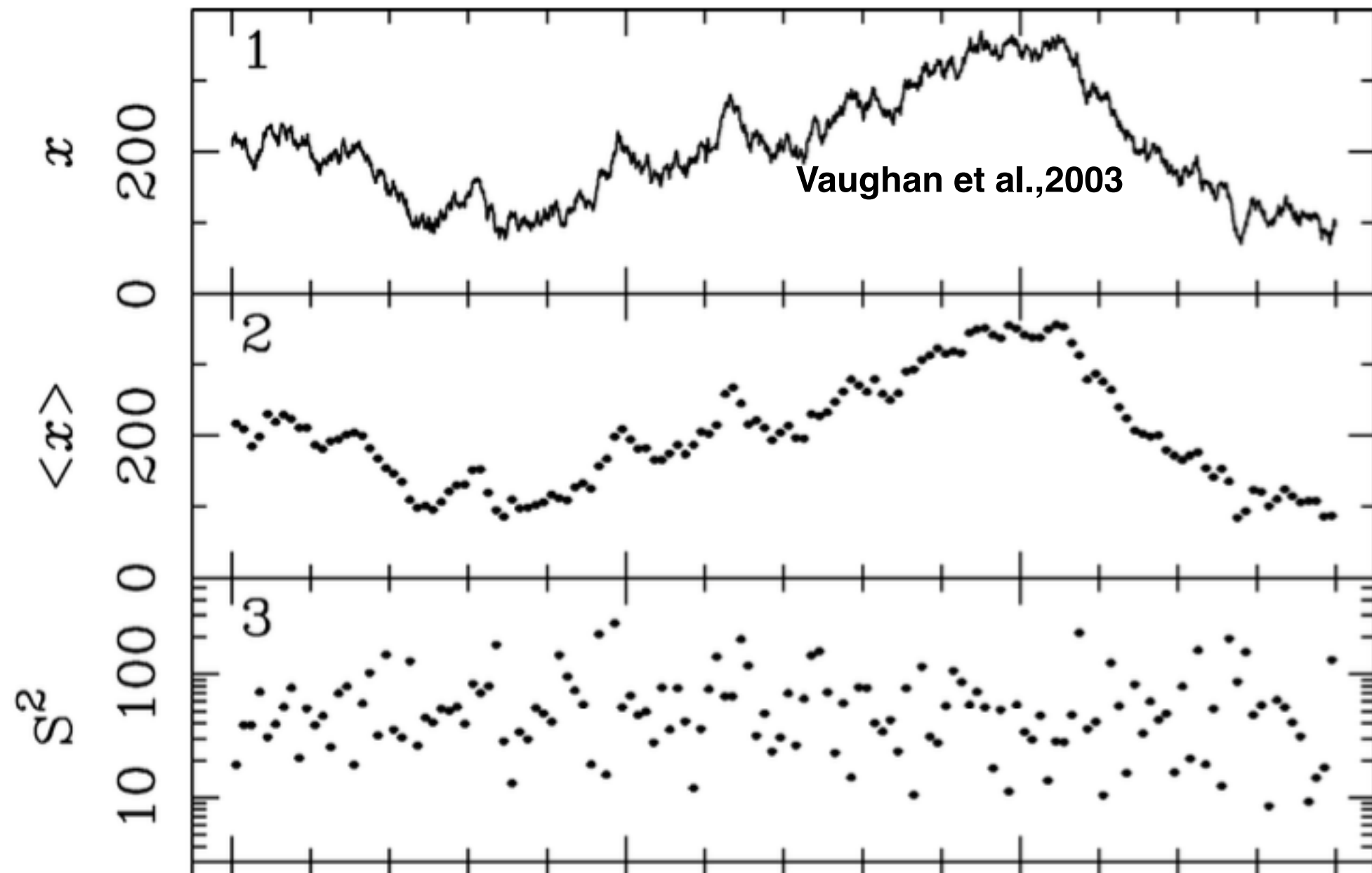
# Conclusions

- Complexity of AGN processes and environment necessitates “novel observables”
- Statistical methods may provide these via PSD and PDF  
=> naturally emerge from big datasets
- Estimates of variability require simulations - uncertainties and biases related to cadence are important
- Estimates of observables from simulations
- Reaffirms need for coordinated MWL observations
- Increasing theoretical understanding of PSD and PDF in terms of physical processes

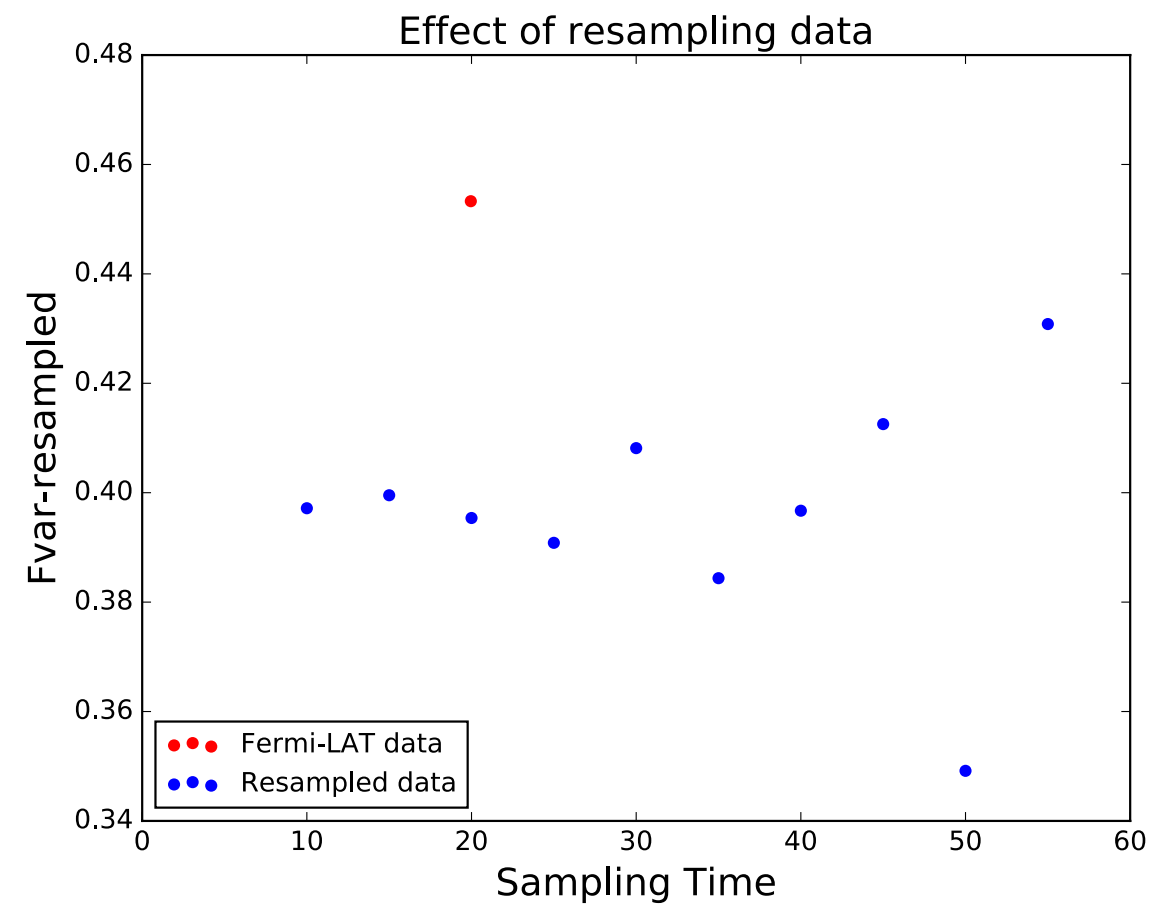
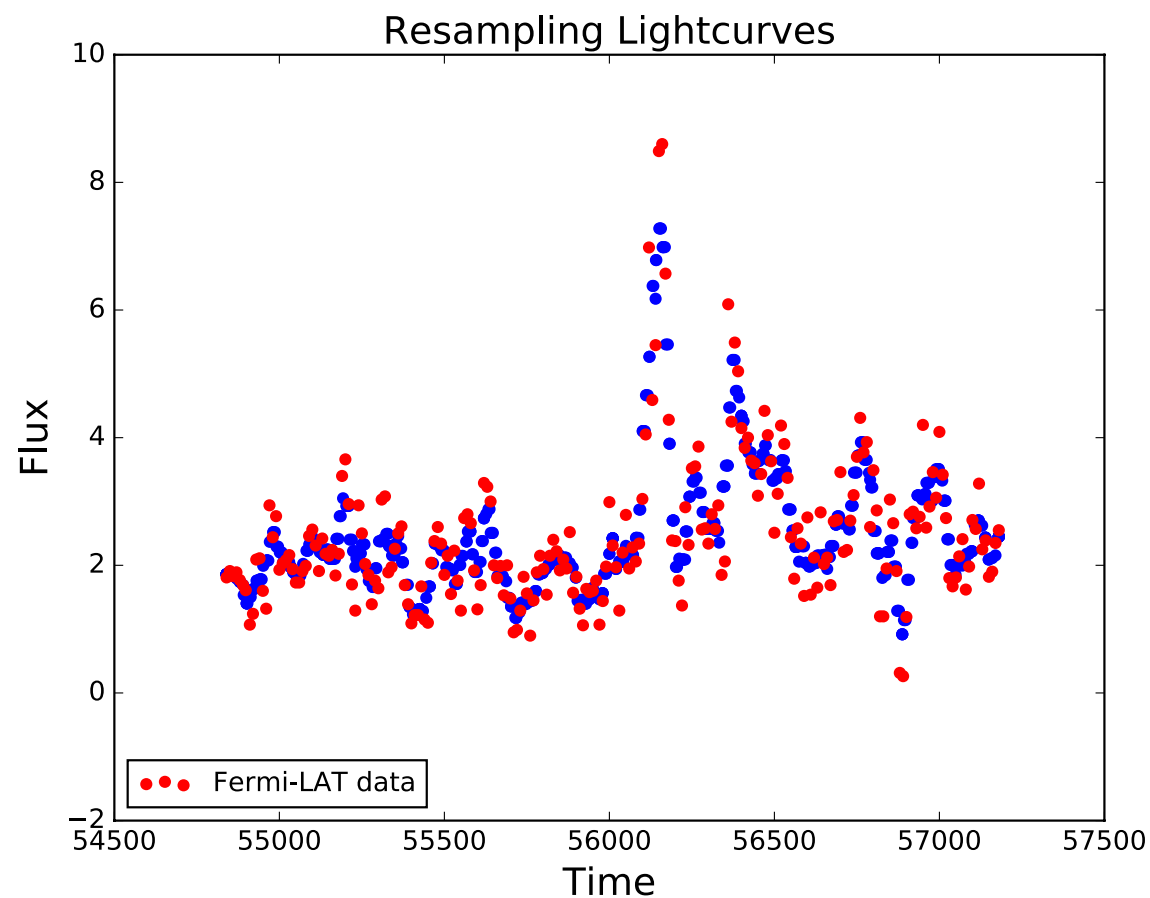
# THANK YOU

- In collaboration with
  - Frank Rieger, Simone Giacche (MPIK)
  - Jonathan Biteau (IPNO)
  - Paul Morris, Garret Cotter (Oxford)

# Backup

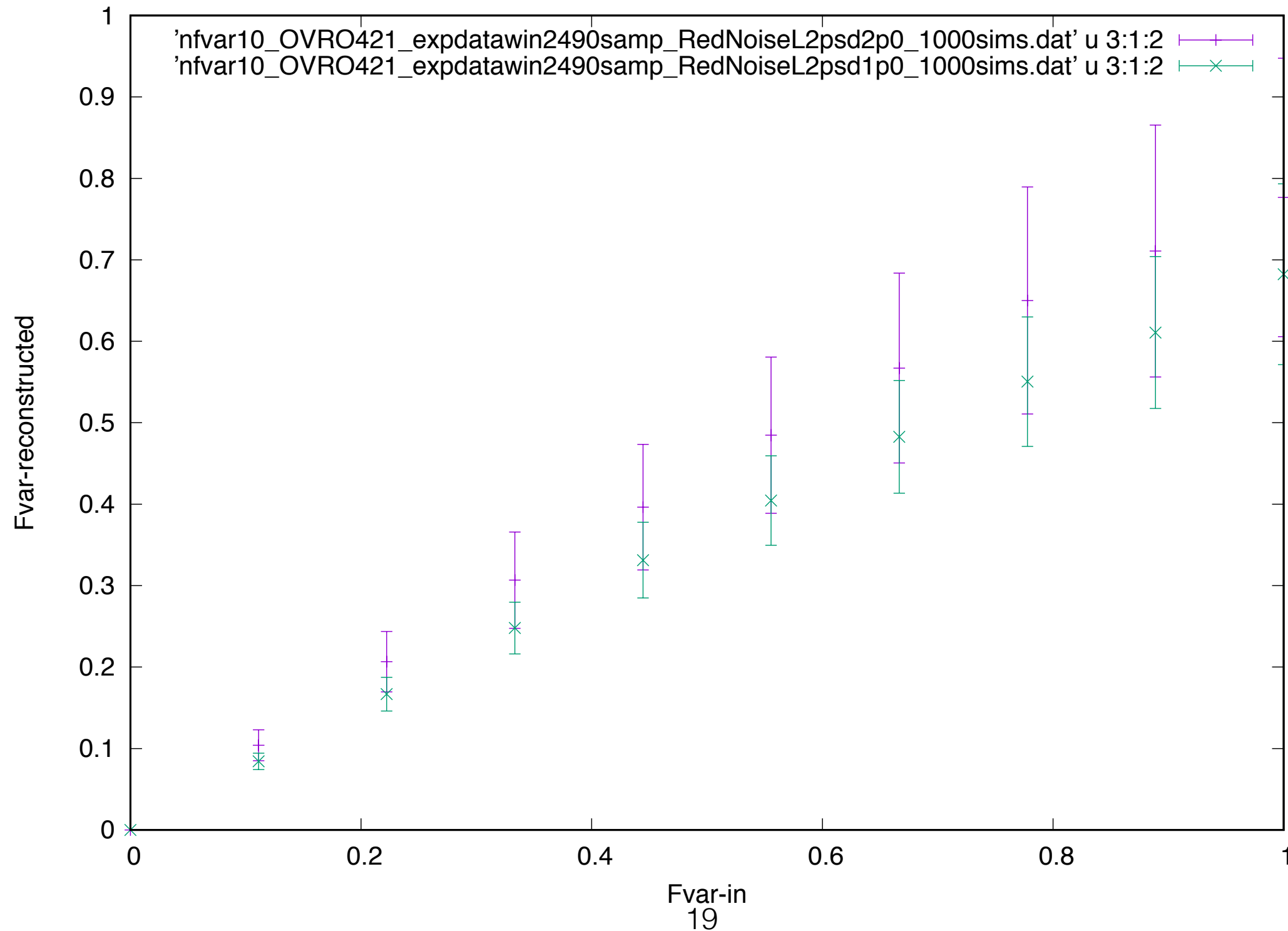


# Simple Resampling Effects





# Non-gaussian PDF

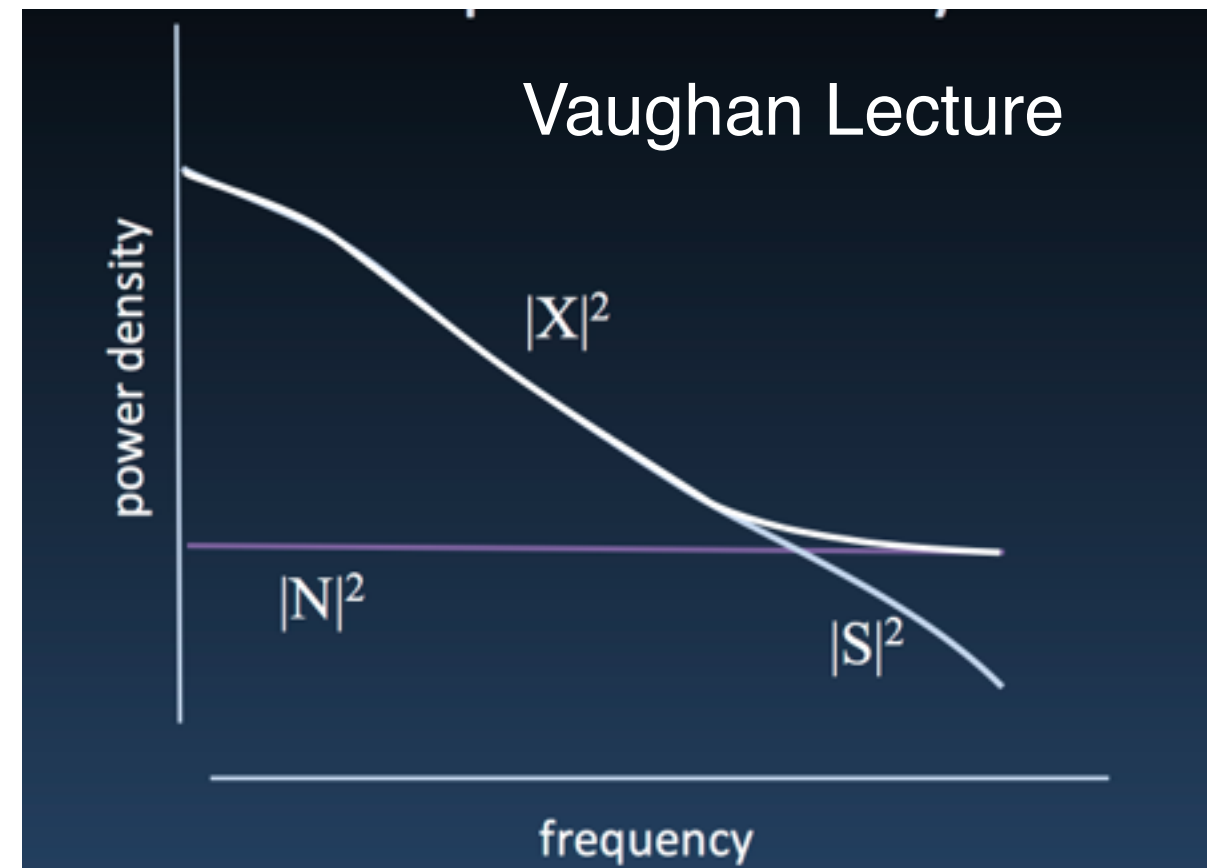


# Motivation

- Sources vary with time ! **How tells us why**
  - Individual sources : physical mechanisms at emission sites
  - Population : general trends
- Unlike other experiments we cannot manipulate or repeat exactly the same way
- Observed light curve is 1 sample or realisation -> we need to **“repeat” to detect**
- Signal coupled with noise
  - Either disentangle **deterministic** signal from **random** fluctuations
  - Or the interesting signals are random fluctuations themselves
- **Observational Irregularities : Allocation, satellite cycles, visibility, competing targets, etc**
  - gaps
  - coarse or uneven sampling
  - length of observation limited

# Power Spectral Density

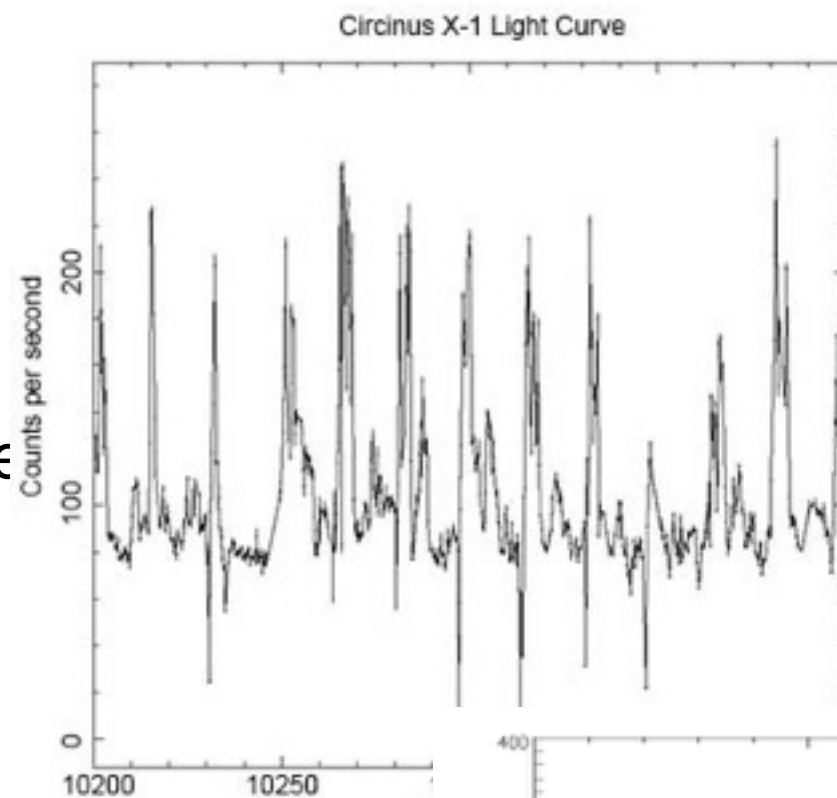
- Power spectral density or PSD is the “distribution of timescales”
- Frequency  $\leftrightarrow$  timescales
- Time :  $x = s + n$   
 Fourier :  $X = S + N$   
 $|X|^2 = |S|^2 + |N|^2 + \text{Cross}$   
 $\text{PSD}(f) = \langle |S|^2 \rangle = \langle |X|^2 \rangle - \langle |N|^2 \rangle$   
 $\Leftrightarrow$  Related to the variance
- Formally (for AGNs and others)  
 Time :  $\text{Lightcurve}(t) = \text{Dynamical}(t) \times \text{Acceleration}(t) \times \text{Radiation}(t) \times \text{Observation}(t)$  [**Product**]
- Fourier :  $\text{Lightcurve}(f) = \text{Dynamical}(f) * \text{Acceleration}(f) * \text{Radiation}(f) * \text{Observation}(f)$  [**Convolution**]



- Dynamical  $\rightarrow$  Periodic, slow variations  
 Acceleration  $\rightarrow$  Stochastic / Shocks  
 (Sironi et al., 2015, Giacche and Chakraborty, in progress)  
**Radiation  $\rightarrow$  (LC simulations  $\leftrightarrow$  “Observables”)**  
**Observation  $\rightarrow$  Potential (CTCs, others)**

# Types of lightcurves

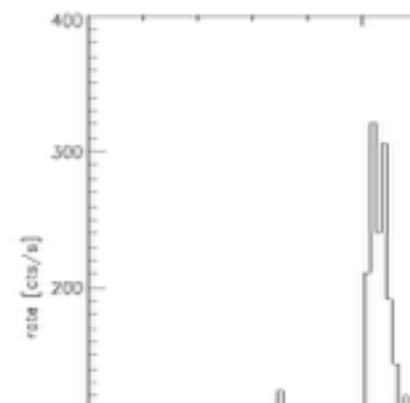
- **Periodic** - differentiate deterministic from noisy background



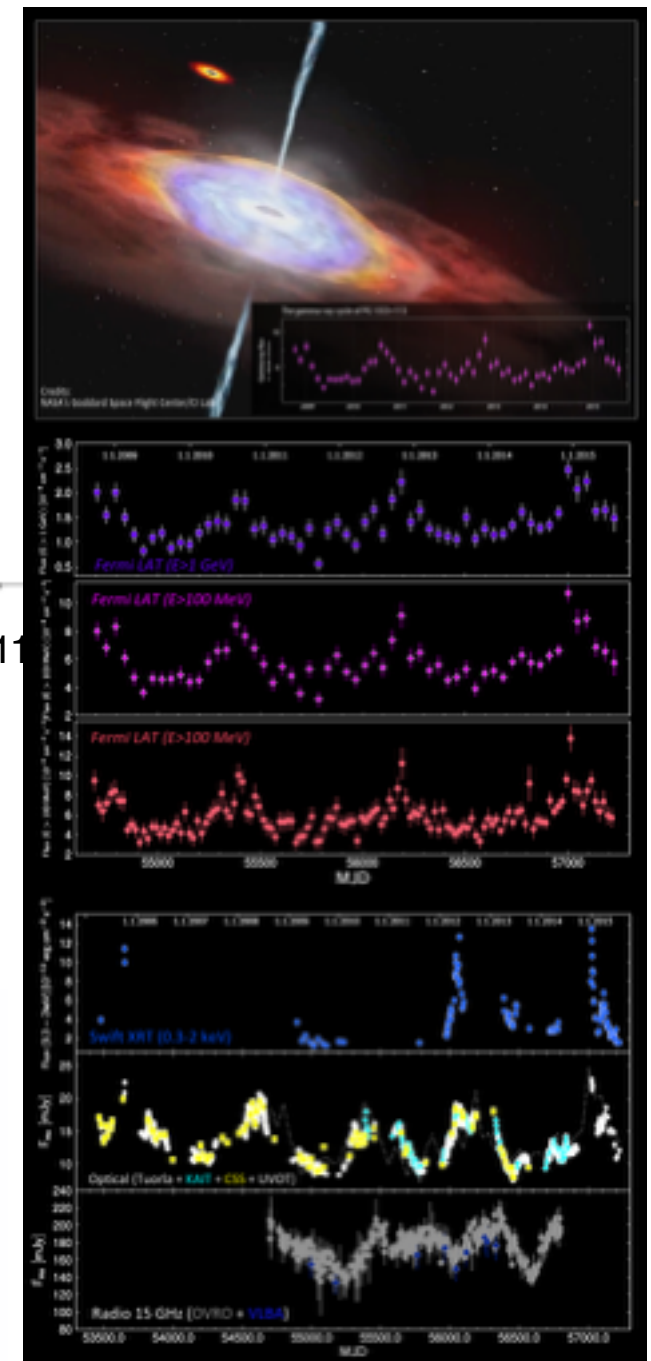
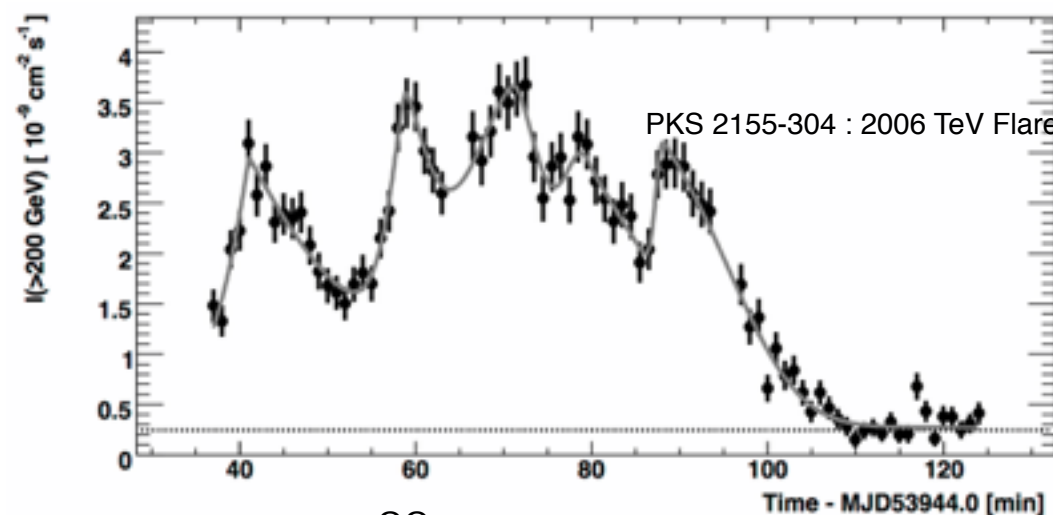
- **Transient** - differentiate deterministic from noisy background

P ~ 17 d  
<http://imagine.gsfc.nasa.gov>

GRB 11

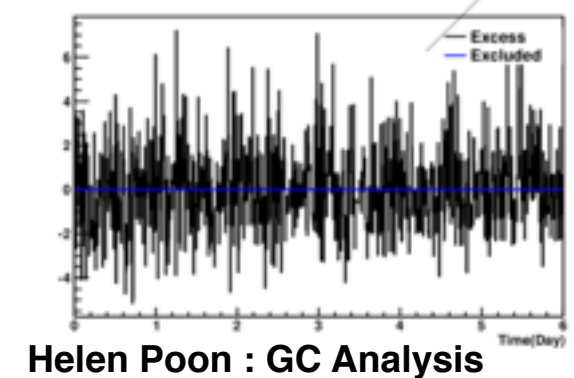
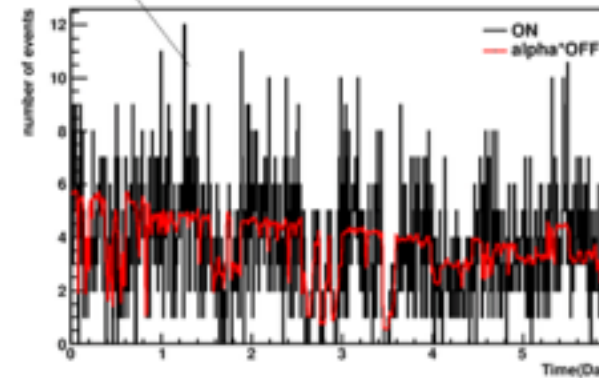
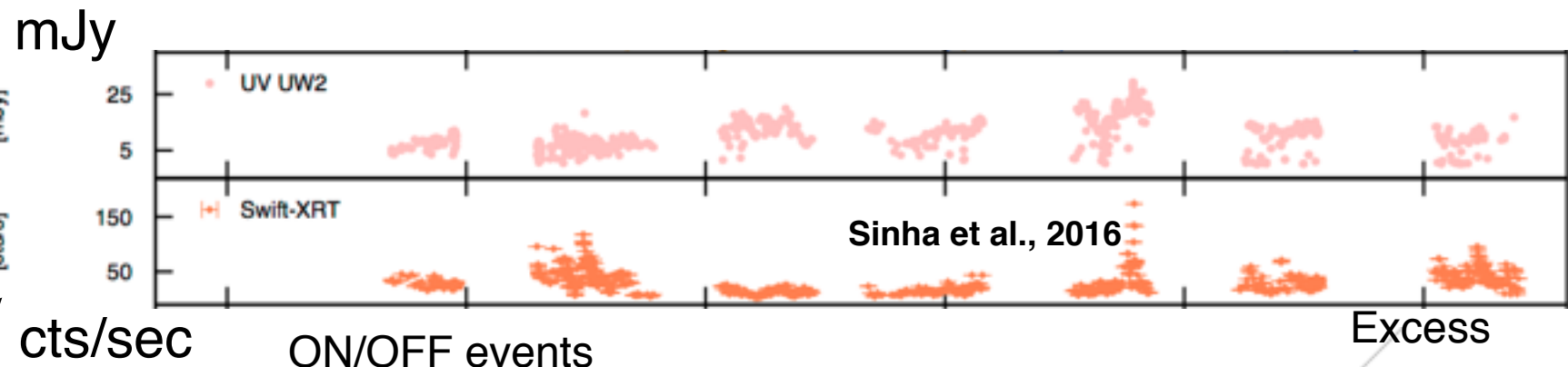


- **Stochastic** - noisy (from noisy background ?)



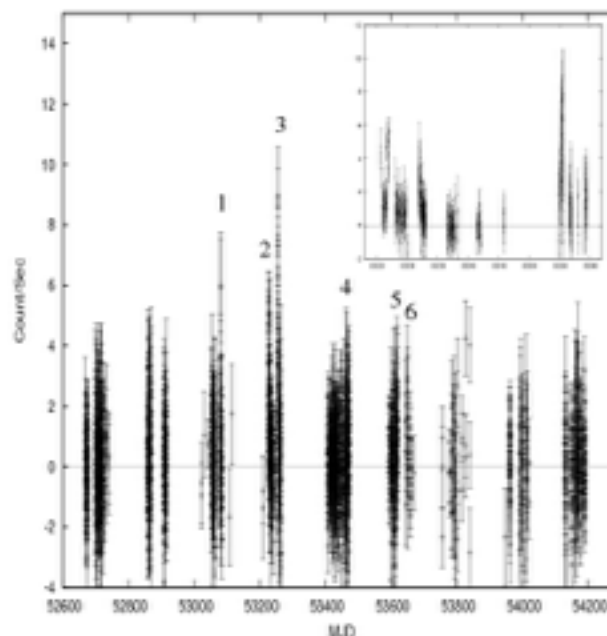
# Types of data analyses

- Depending on the wavelength
  - (quasi-)continuous, binned signals or fluxes
  - discrete : time tagged events
  - discrete : counts per time bins

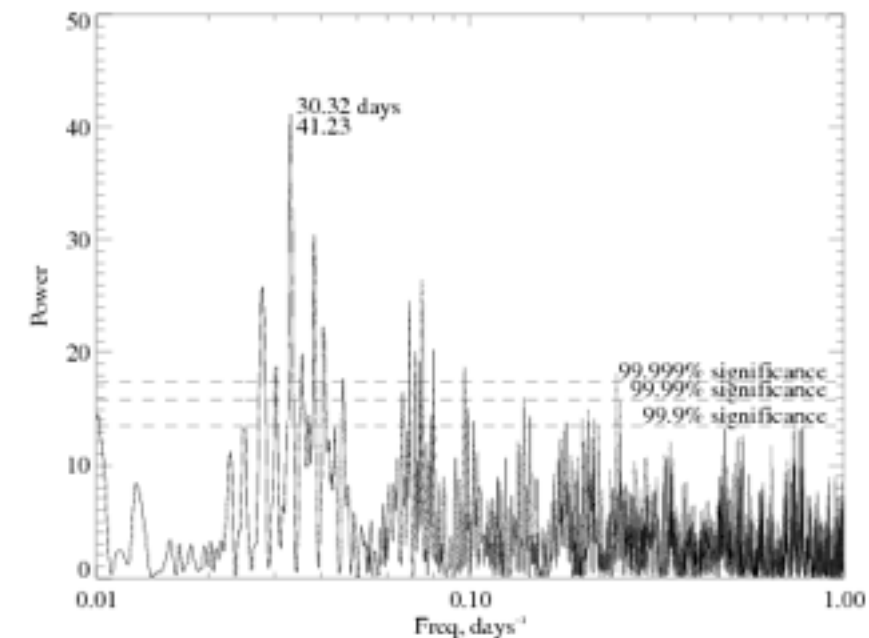


Helen Poon : GC Analysis

## Time vs Frequency domain



$\Leftrightarrow$

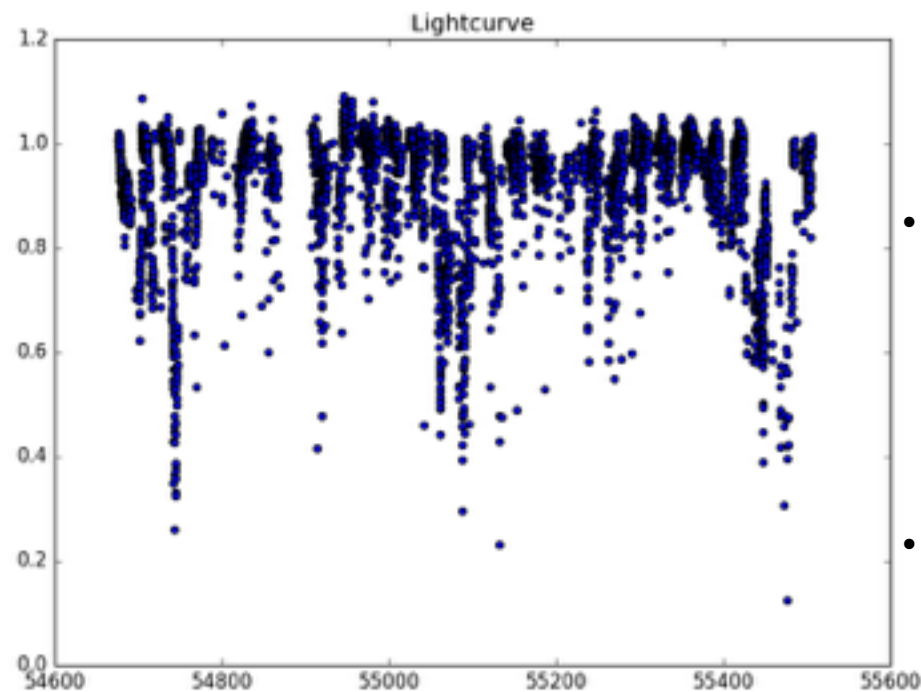
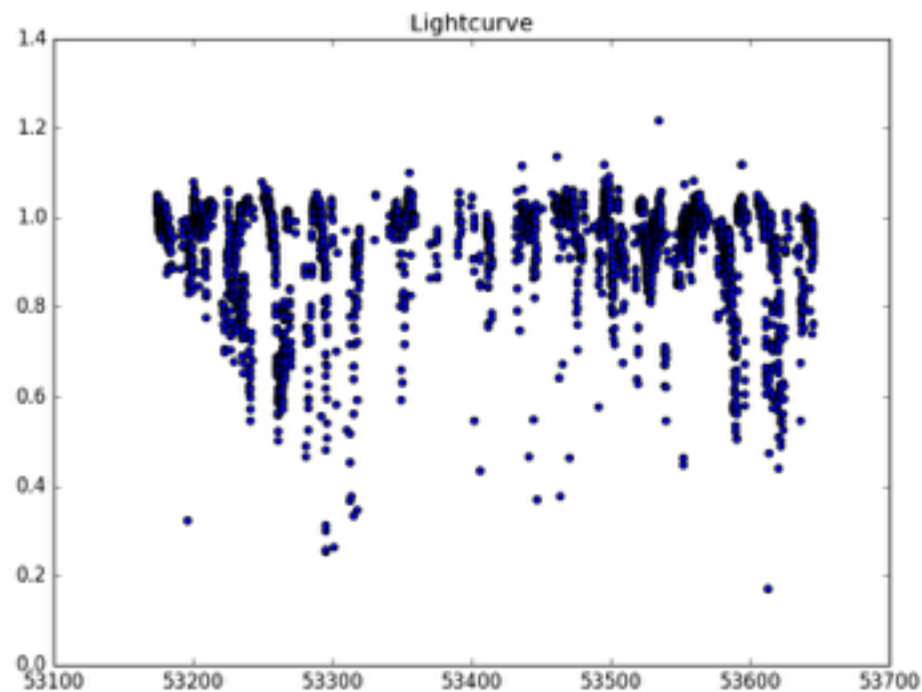


- Naturally analyses methods are also different(ly used)
- Temporal vs Fourier Analyses ; mixed

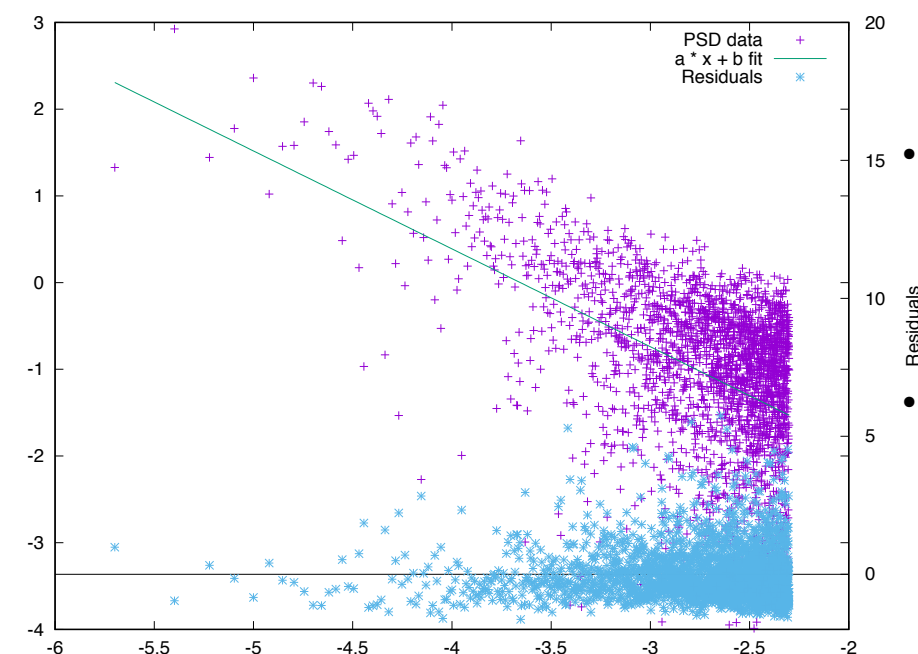
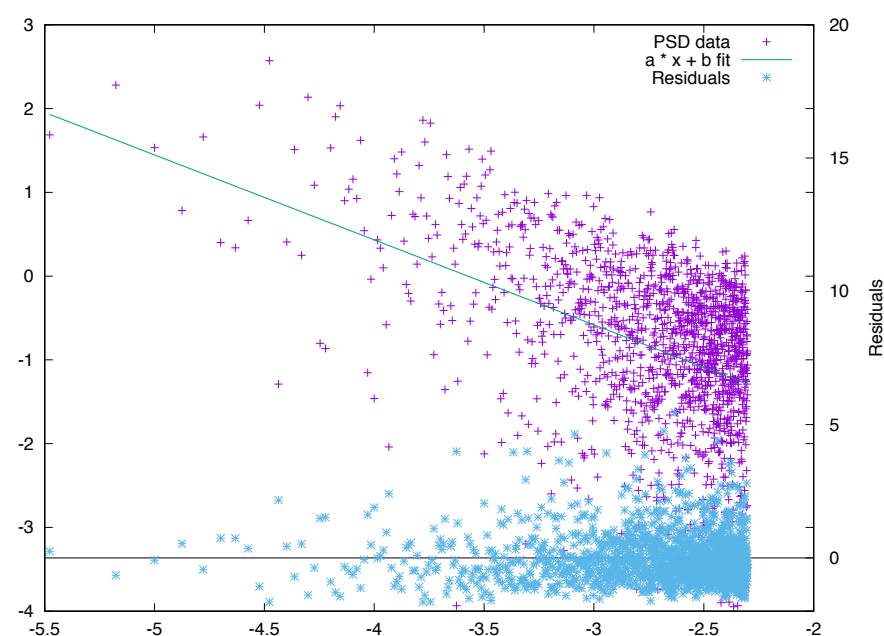


- $\text{Lightcurve}(f) = \text{Dynamical}(f) * \text{Acceleration}(f) * \text{Radiation}(f) * \mathbf{Observation}(f)$

## Applications for foreground diagnostics



- Source of variations -> Foreground contamination
- eg. Atmospheric transparency coeff themselves have structure - brown noise (1.0)



- Either correct directly (better) or model
- Could use PSD as discriminator