

# Detector backscattering systematics

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Tristan Workshop 2022



# Outline

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- **Backscattering shape in monochromatic and Tritium spectra**
- Backreflection in the KATRIN environment
- Test of the model with KATRIN data
- Preliminary impact on Tritium spectrum
- Conclusions

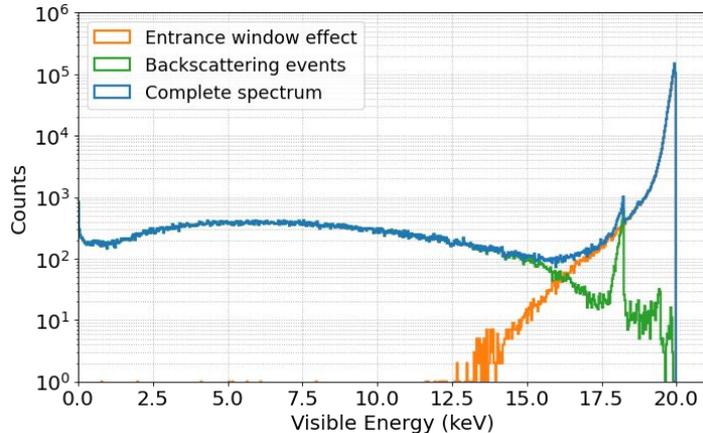
# How to model backscattering

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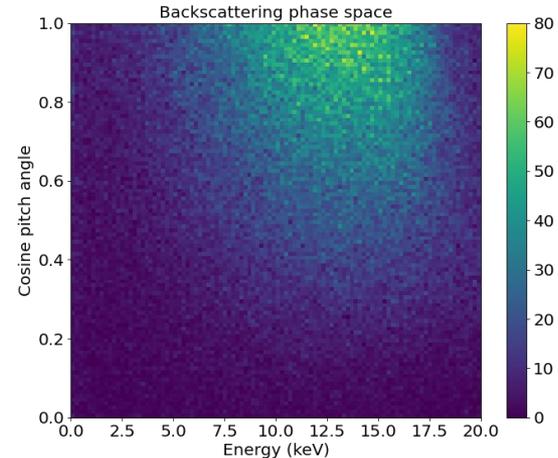
- Backscattering depends only on the electron scattering in Silicon → **simulated in Geant4**
- electrons will arrive at the detector with different energies and incidence angles → need to do simulations at different energies and angles
- Shoot electrons on the detector: both the **energy deposited in the active volume** and the **energy-angle of the backscattered electrons** are saved
  
- Example: Geant4 simulation of  $10^6$  electrons with 20 keV and  $0^\circ$  incident angle (normal incidence) → an empirical model for the DL is applied

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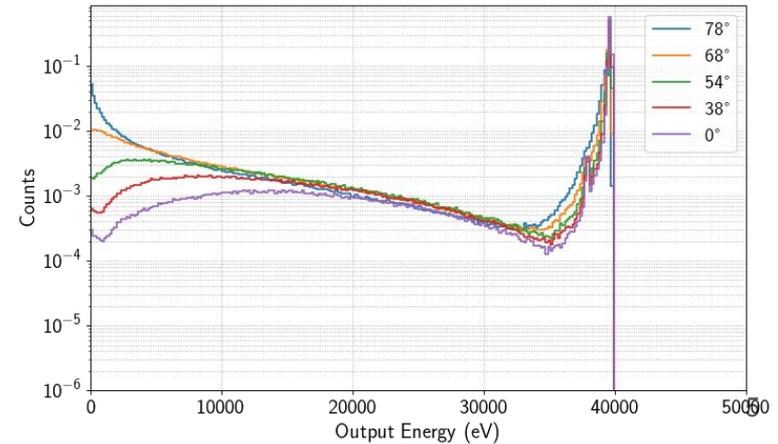
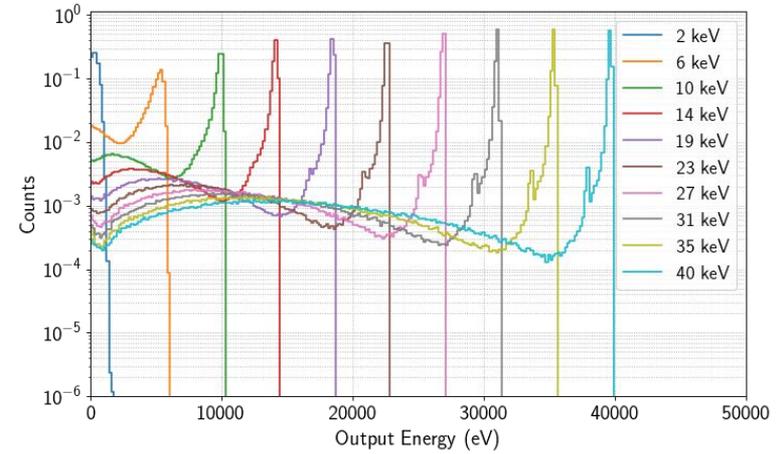
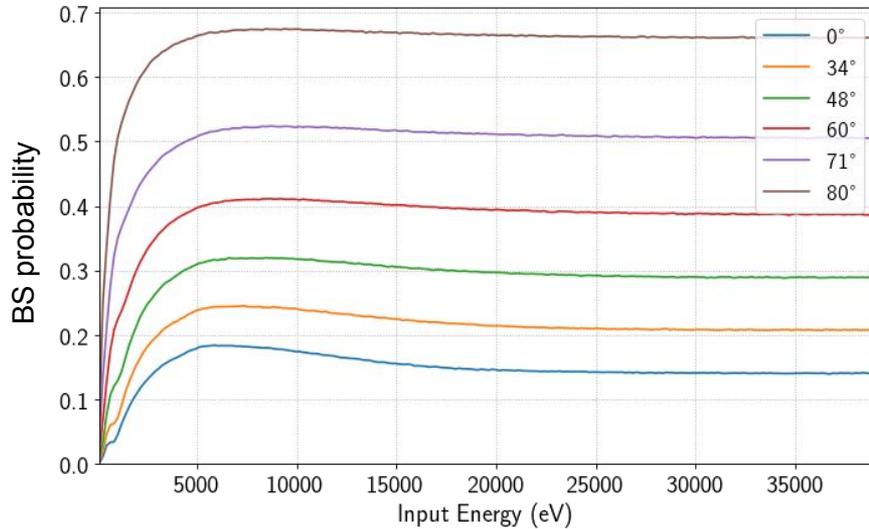
**Detector response**



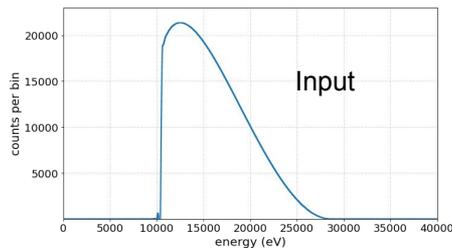
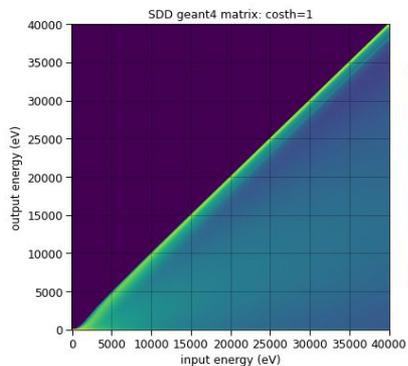
**Backscattering response**

# The effect of different energies and angles

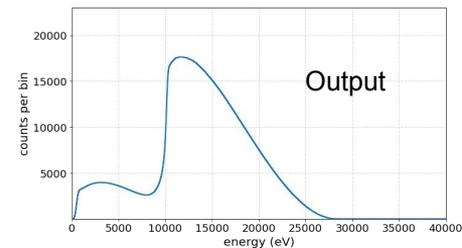
**Backscattering probability increases a lot with the angle and slightly decreases with the energy**



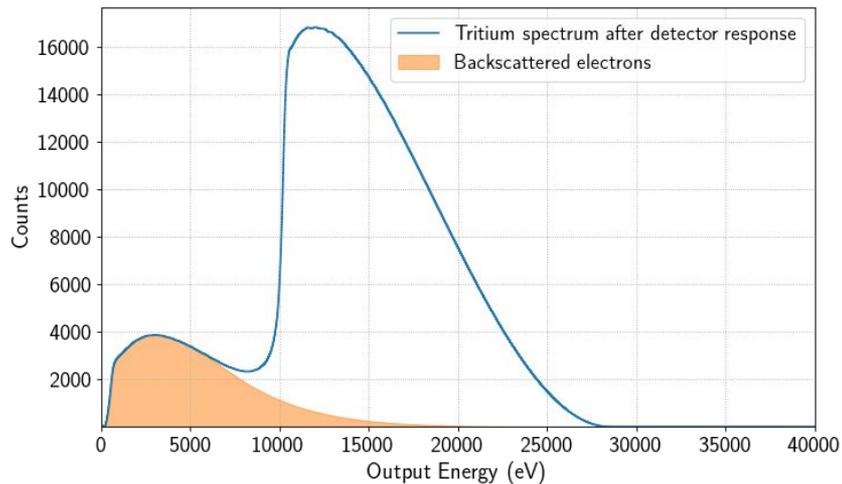
# Impact on Tritium spectrum



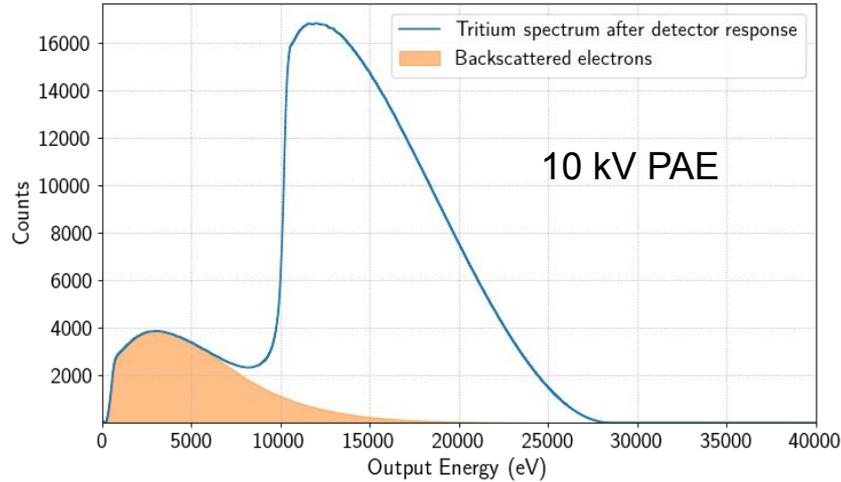
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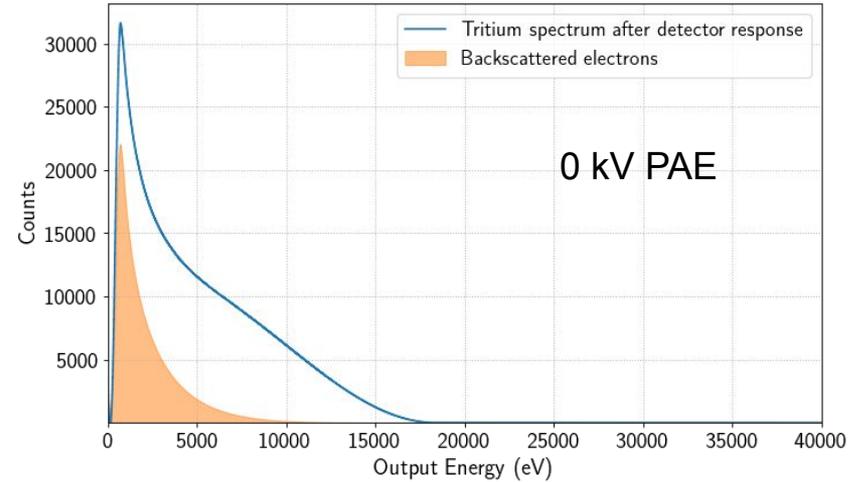
**17% backscattering probability**



# Impact of PAE



17% backscattering probability,  
mainly outside the ROI



28% backscattering probability,  
completely inside the ROI

- PAE: →
- **higher energies** → slightly less BS
  - **collimated electrons** → less BS towards 0°
  - move **BS spectrum outside of the ROI**

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# Backreflection in KATRIN

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  - post-acceleration potential
  - pinch magnet
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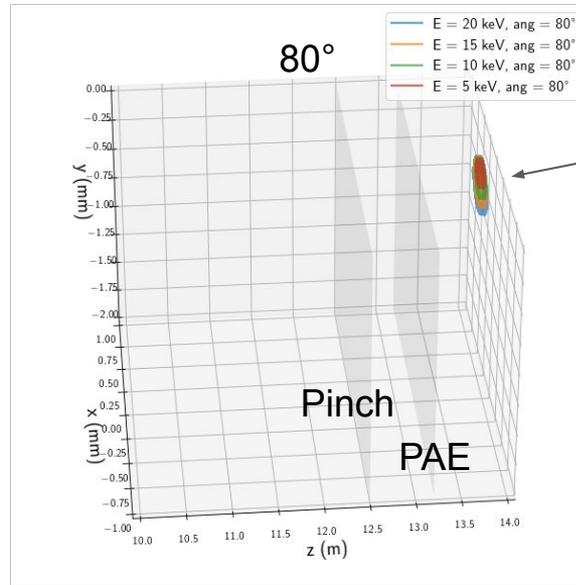
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PAE = 10kV, nominal B-fields



electrons generated at the detector position

electrons with **ang**>75° are reflected by the detector magnet

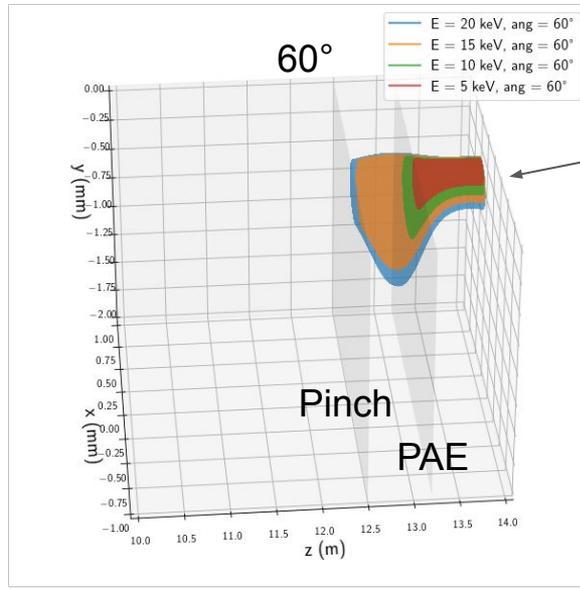
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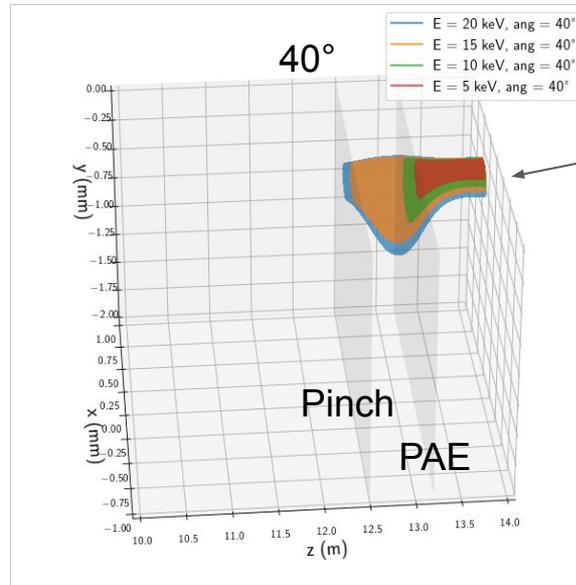
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electrons with **large angles** can also be reflected by the pinch

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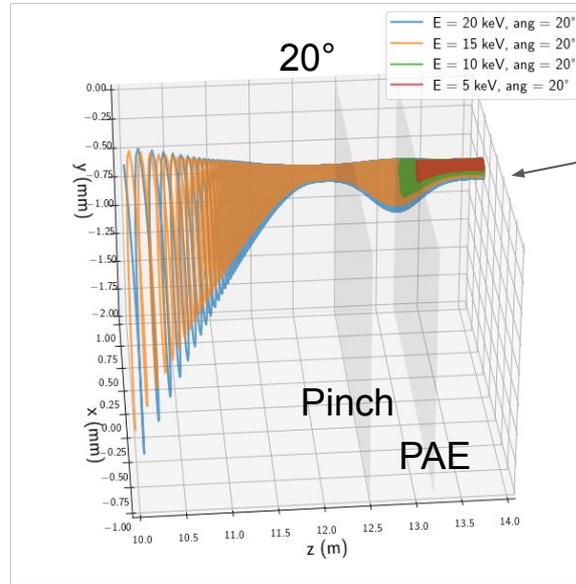
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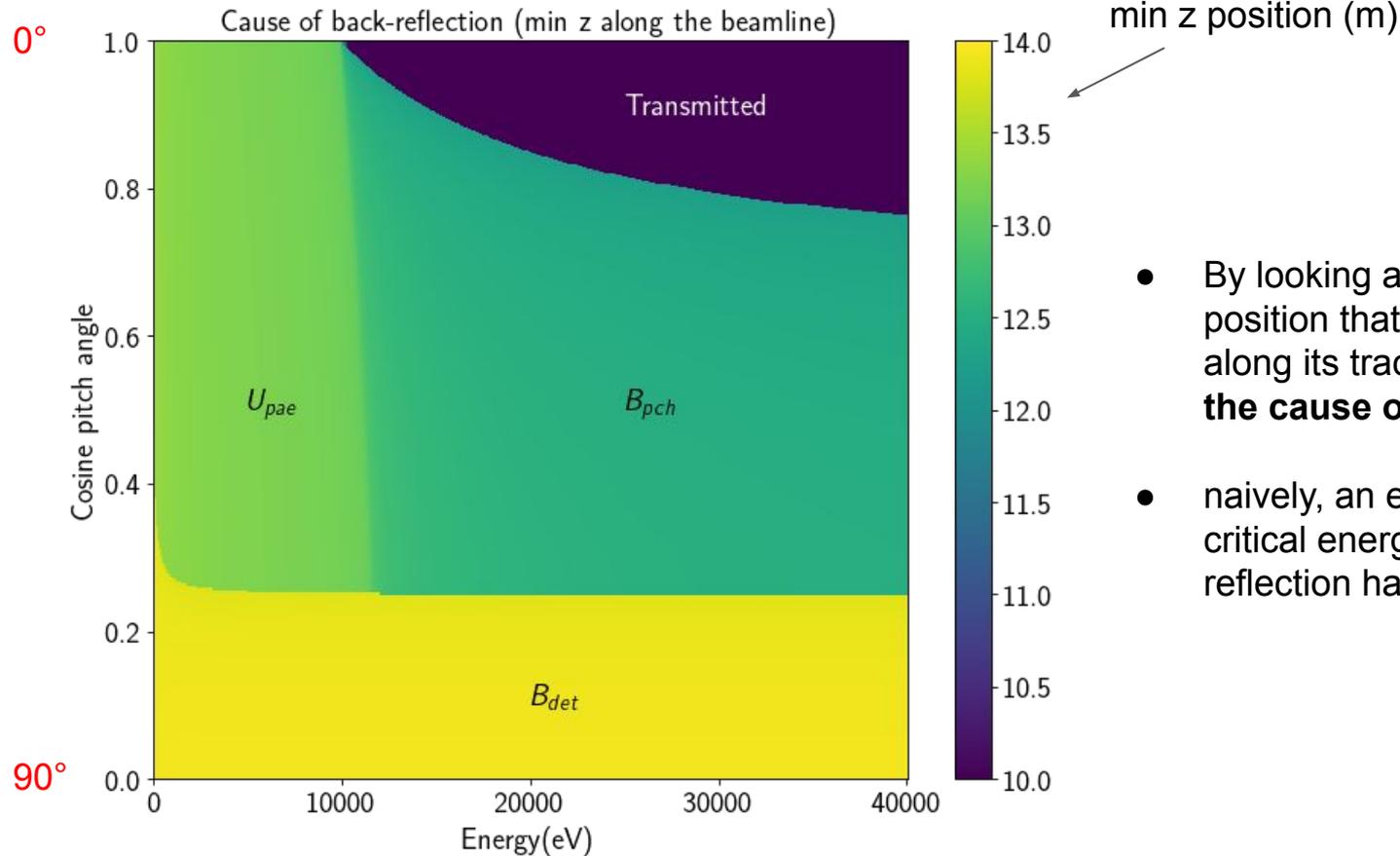
PAE = 10kV, nominal B-fields



electrons generated at the detector position

electrons with **E > 10 keV** and **small angles** are transmitted

# Cause of the backreflection



- By looking at the minimum z position that the electron reaches along its tracking, **we can identify the cause of the backreflection**
- naively, an electric reflection has a critical energy, while a magnetic reflection has a critical angle

# Two types of backreflection

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- **some electrons will return back in a time long enough** that the detector can distinguish the new event with respect to the primary one → I will call this **slow reflection**
  - this will lead to **two different events**, and therefore this kind of reflection can be handled in the TRModel

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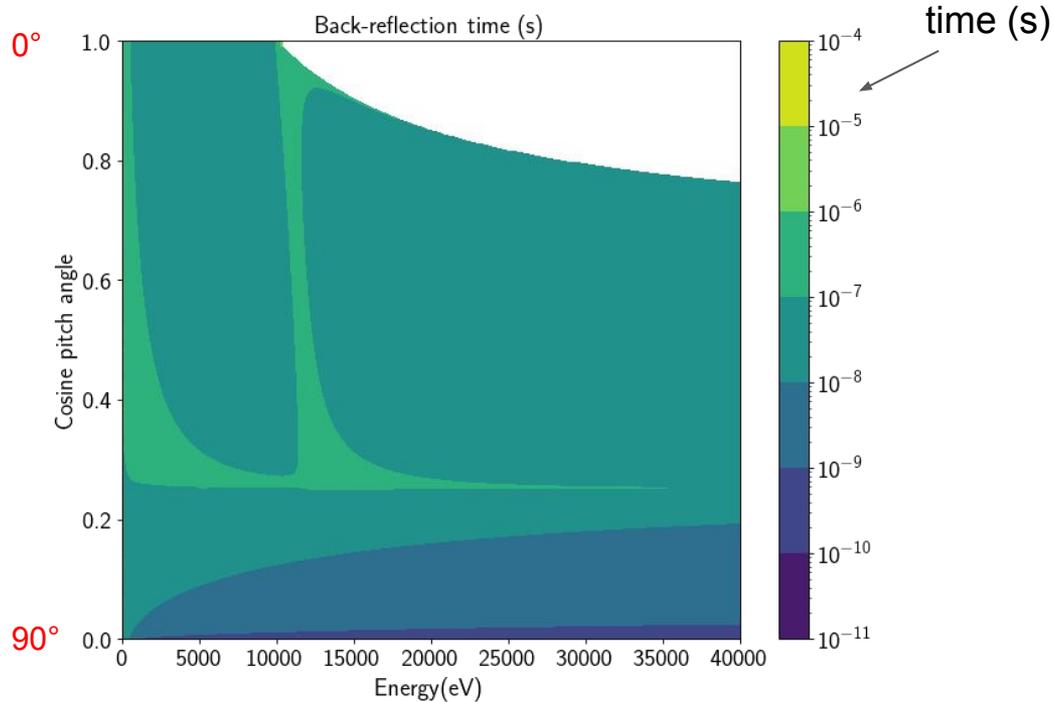
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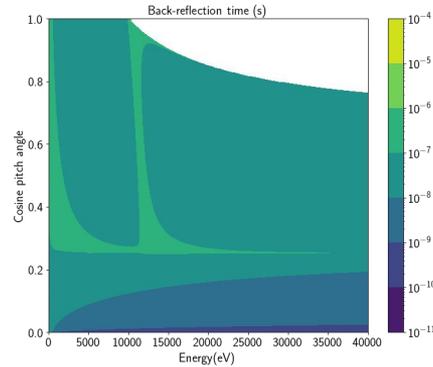
The time required to return back to the detector **depends on the energy and angle of the backscattered particle and on EM fields**

# Time required to return back at the detector

By fixing the EM fields (e.g. Scenario 1 fields) we can have this information by **shooting electrons in Kassiopeia with different energies and angles**:



# A model for the fast backreflection

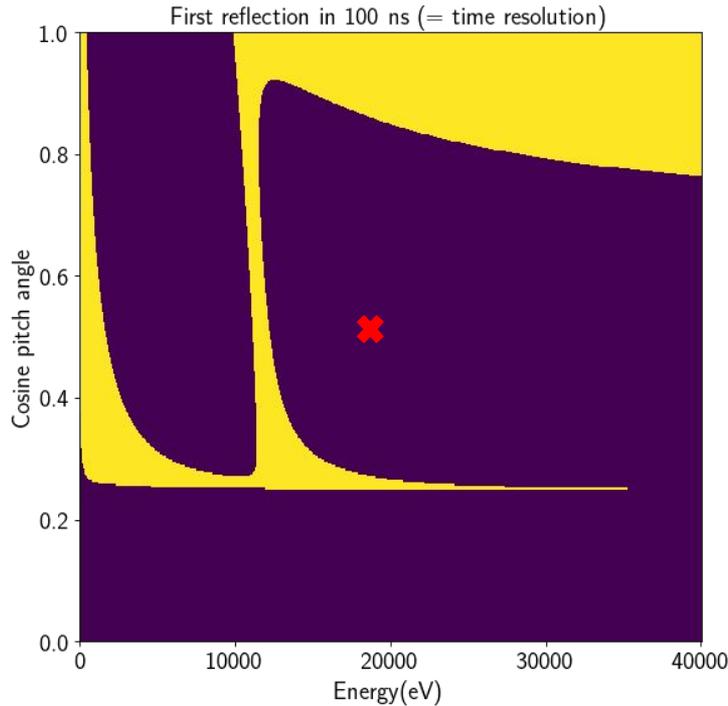


Idea:

1. the time plot is loaded in Geant4 main and passed to the class that handles the tracking
2. for every backscattered electron the time required to return back is evaluated
3. **if there is enough time available this electron is manually inverted in Geant4** and it is re-propagated in the detector
4. this procedure is iterative (multiple backscattering and backreflections inside the given time window)

# Example

Let's suppose we have a **100 ns time window** → fast backreflection can only happen in **dark areas**



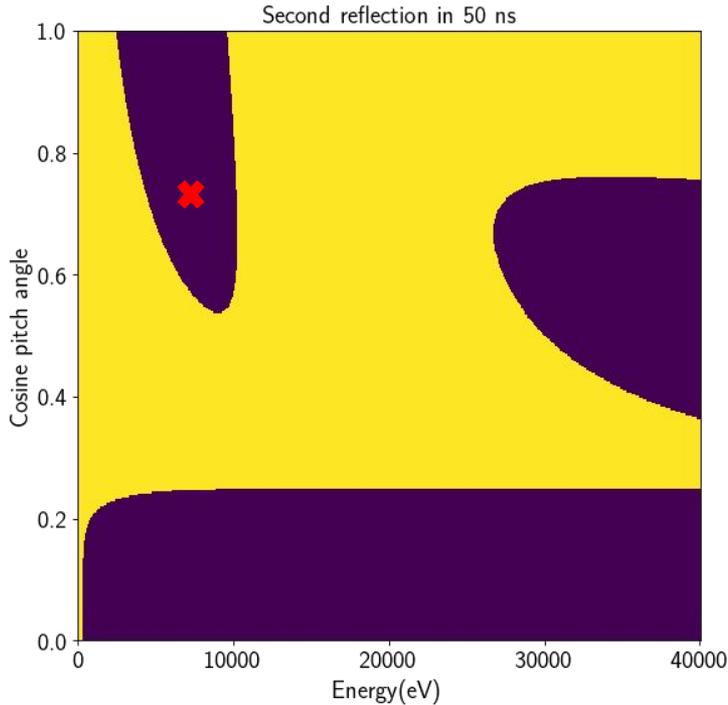
Consider a backscattered electron with an energy/angle for which the **time required to return back is 50 ns**



It is **flipped in Geant4** and its tracking continues!

# Example

Let's suppose that electron is **backscattered again** → since the time resolution is 100 ns, but it spent 50 ns for the first reflection, it now has **50 ns available** → fast backreflection can only happen in **dark areas**



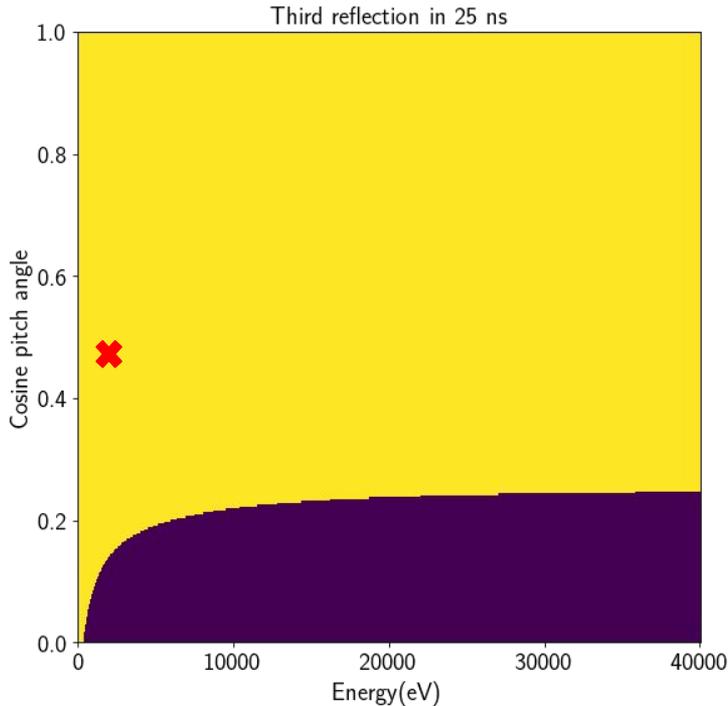
Consider an electron with an energy/angle for which the **time required to return back is 25 ns**



It is **flipped in Geant4** and its tracking continues!

# Example

**Another backscattering** → since the time resolution is 100 ns, but it spent 75 ns for the first two reflections, it now has **25 ns available** → fast backreflection can only happen in **dark areas**



Consider an electron with an energy/angle for which the **time required to return back is bigger than 25 ns**

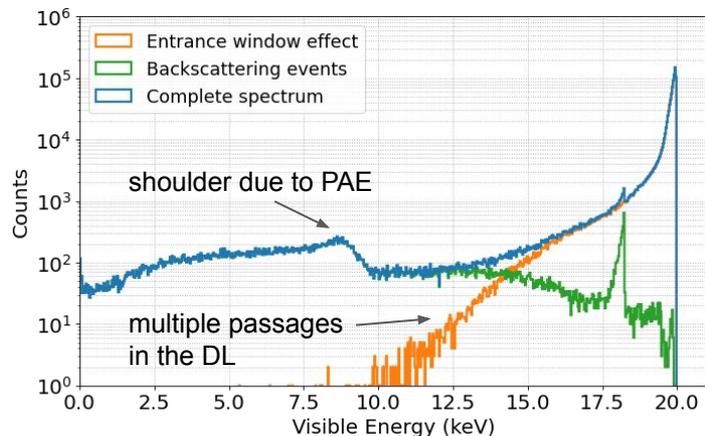
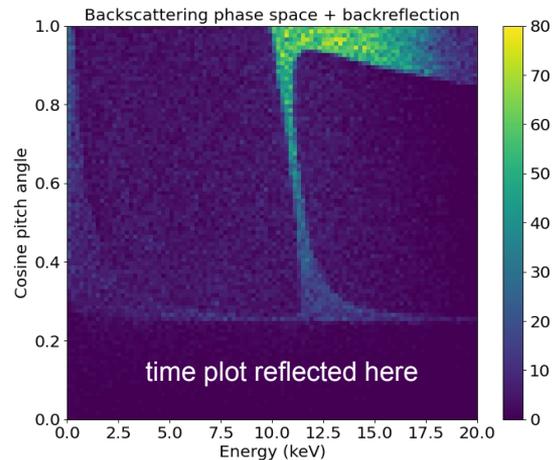


Its **tracking in Geant4 is finished** and its energy-angle are saved, together with the total energy deposited in the detector!

# Output of the simulation: 20 keV and 0°

with the energy-angle saved we fill the **backscattering response** (electrons that will be re-propagated in the TRModel)

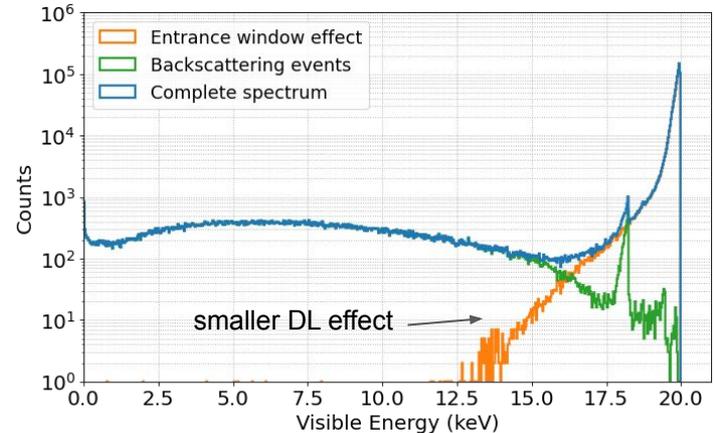
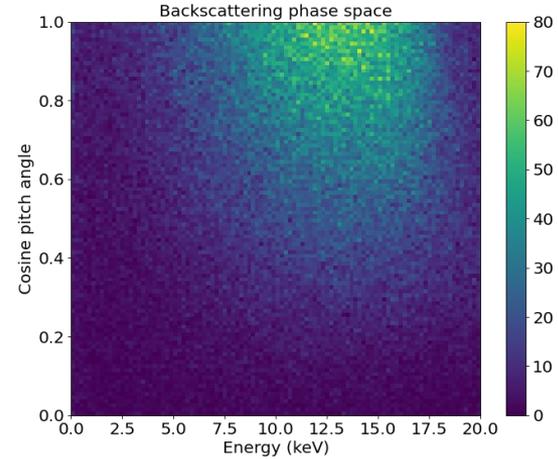
with the energy deposited in the detector we apply the DL model and fill the **detector response**



# To be compared with

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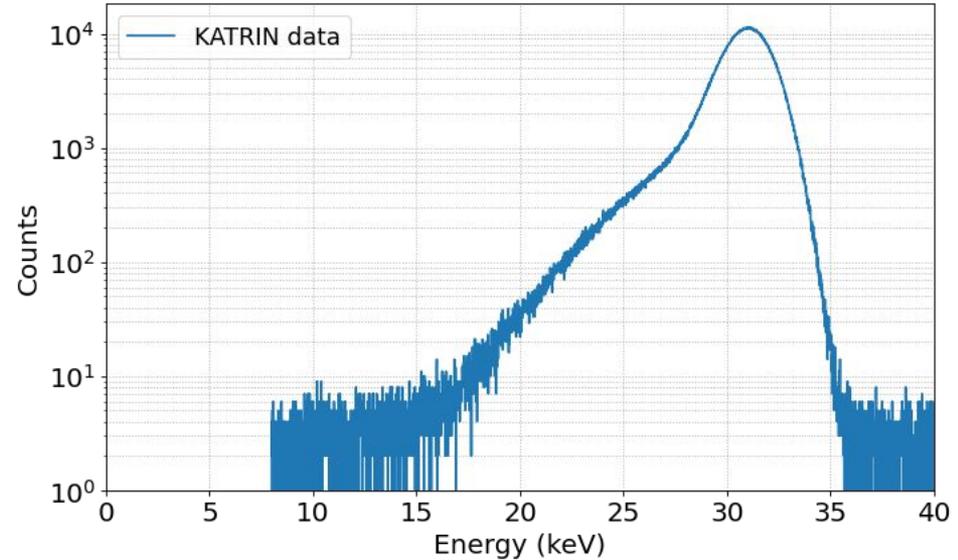
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# Fit to monochromatic spectra in KATRIN environment

- **Monochromatic 21.15 keV electrons** from an e-gun, 40° incidence angle
- **Nominal EM fields** (like Scenario 1), but retarding potential at -20.15 kV
- **excellent test for the fast reflection model**, since the FPD is slower than SDDs (1 order of magnitude) and the spectrum is totally dominated by this effect
- DL thickness and an horizontal gain are left free during the fit:



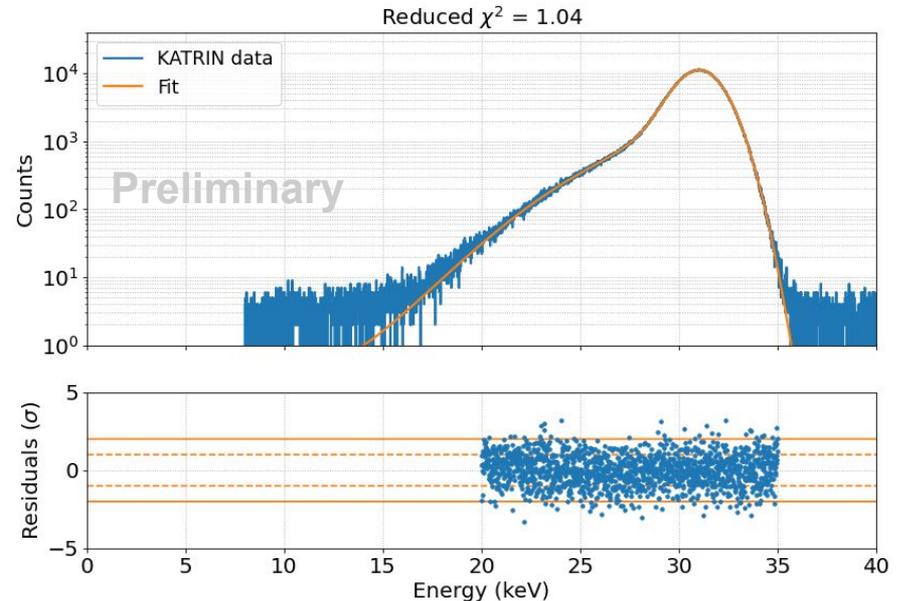
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- DL thickness and an horizontal gain are left free during the fit:

**DL~110nm** and gain~1

- A very good agreement can be seen between data and simulation!

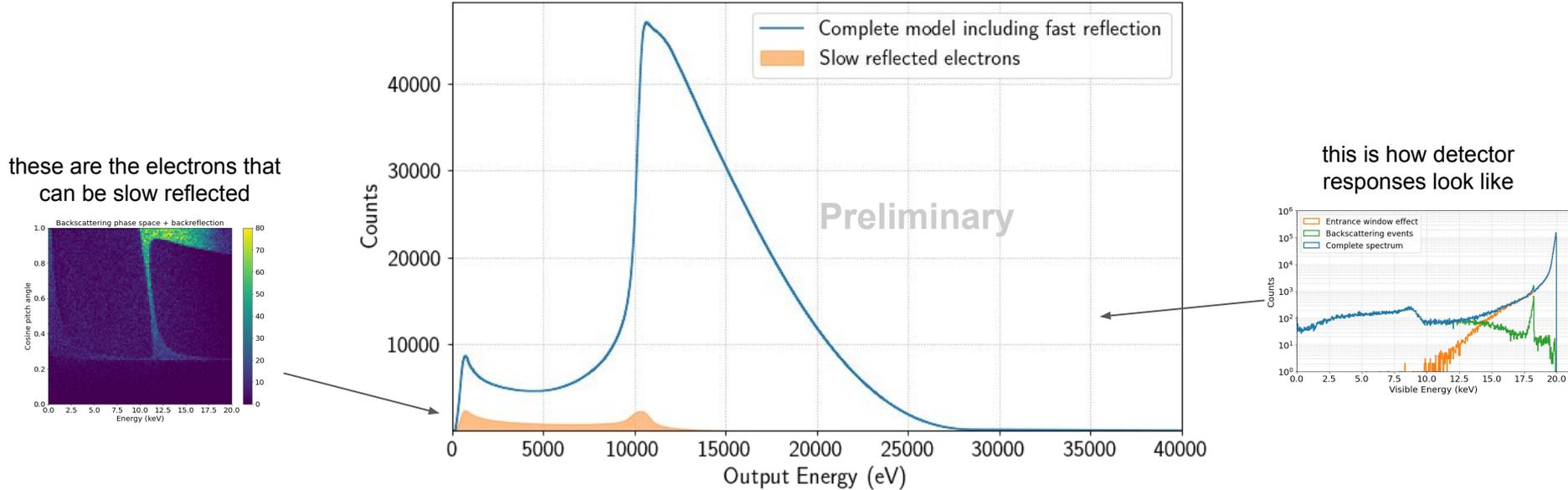


# Outline

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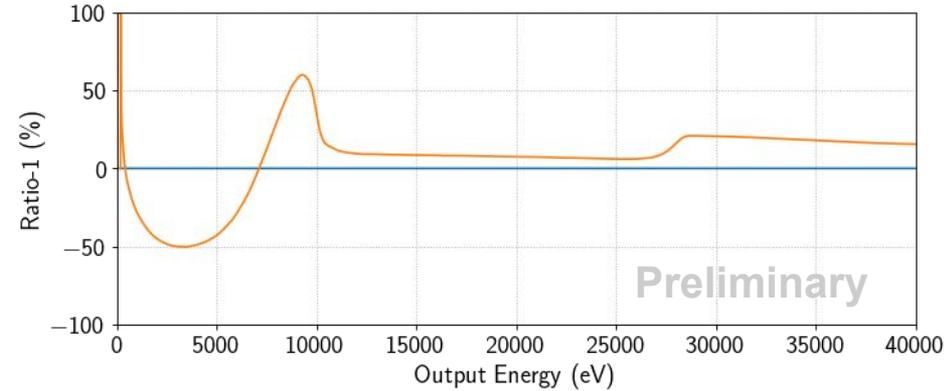
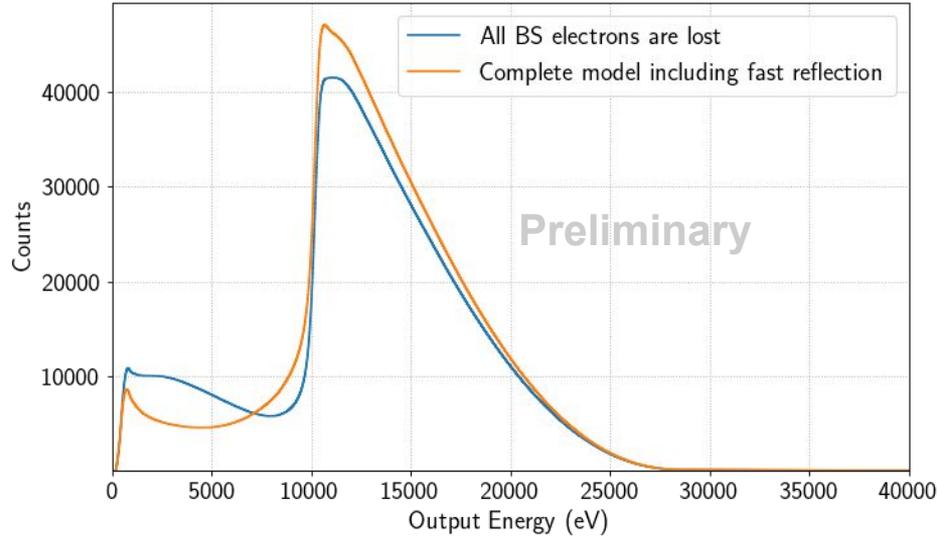
- Backscattering shape in monochromatic and Tritium spectra
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# Backreflection impact on Tritium spectrum



- very low backscattering tail with completely different shape
- only **few electrons are slowly reflected** → cause of the peak-like structure

# Backreflection impact on Tritium spectrum



- very low backscattering tail with completely different shape
- **smooth ~10% difference in the ROI**

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# Conclusions

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- a Geant4 simulation was developed to **produce detector and backscattering responses** ✓
- these responses were **successfully implemented in the TRMoc** ✓
- an **integration between Geant4 and Kassiopeia** was done in order to **describe the fast reflection** due to EM fields ✓
- this model well describes differential monochromatic spectra acquired from the FPD ✓
- The impact on Tritium spectrum is shown thanks to the integration in the TRModel, the **next step is to evaluate the impact on sensitivity**

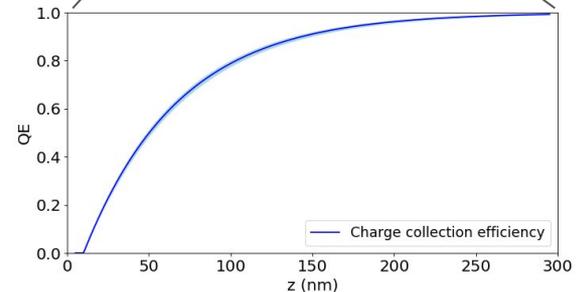
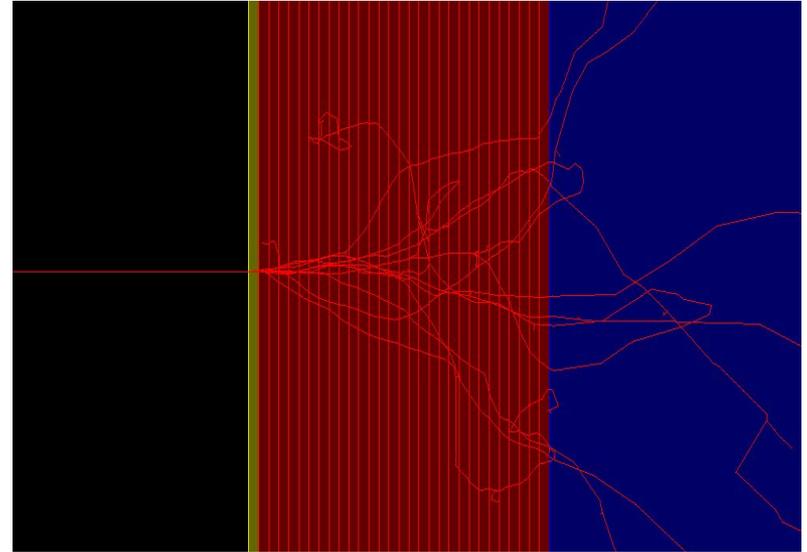


**THANK YOU FOR YOUR ATTENTION!**

Backup slides

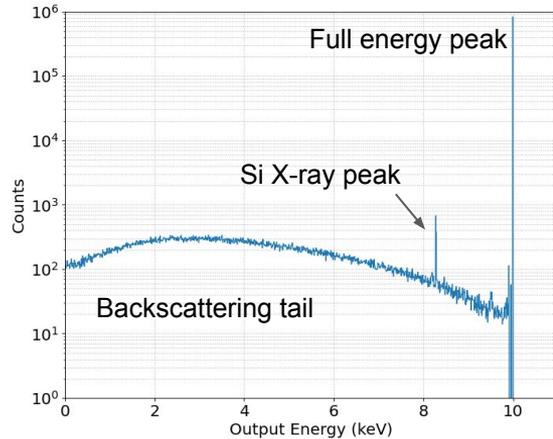
# Backscattering and dead layer

- Starting point: **Geant4 simulation**
- **Backscattering already included** in the physics list
- **Dead layer effects added through an empirical model:**
  - first 10nm: SiO<sub>2</sub>
  - other 29 Si layers, 10nm each one
  - bulk
  - the energy deposited in every region is saved
  - the visible energy is the weighted sum, where weights follow an exponential with **parameter  $\lambda$**



# Response to monochromatic electrons

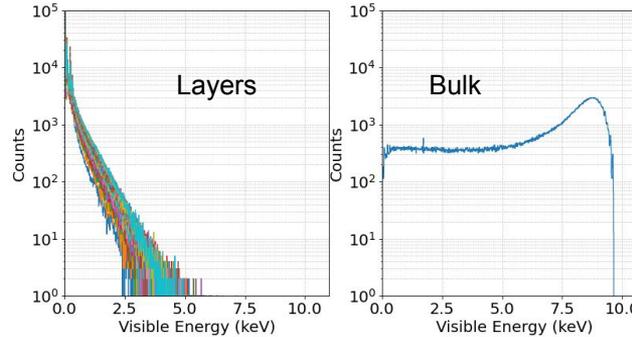
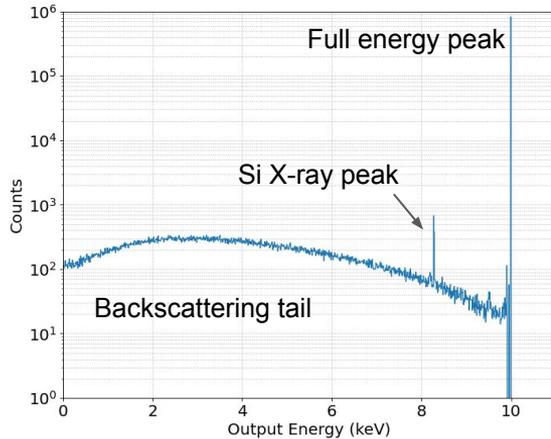
$10^6$  electrons with  $E=10\text{keV}$  and normal incidence



Raw spectrum: **total energy deposited**  
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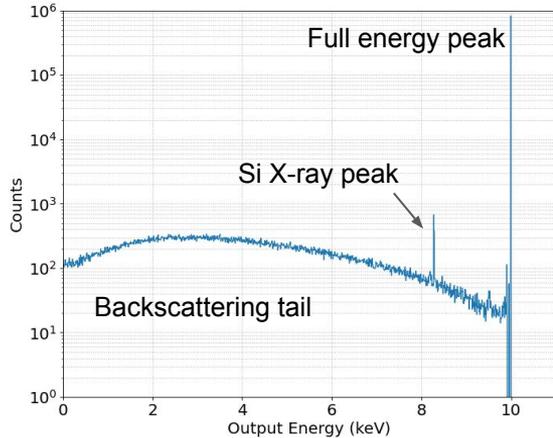


contributions from  
bulk and layers

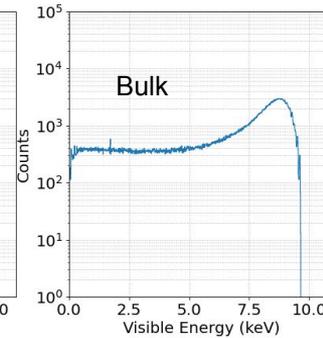
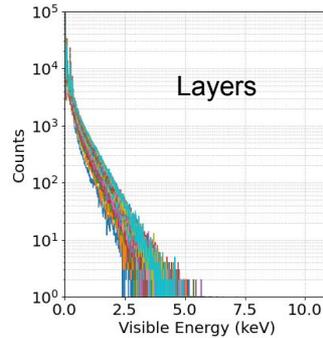
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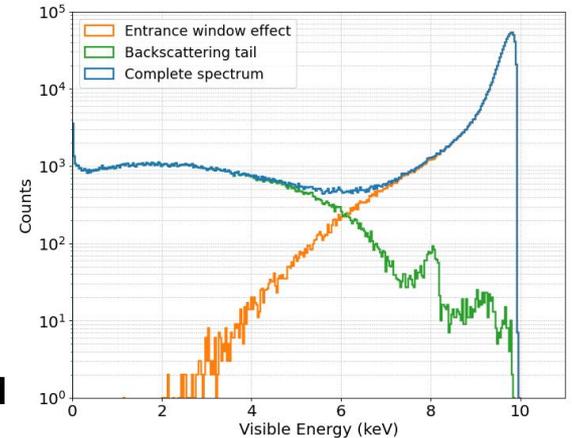


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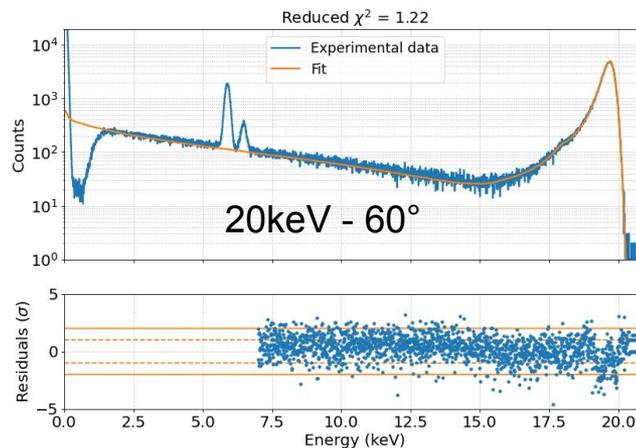
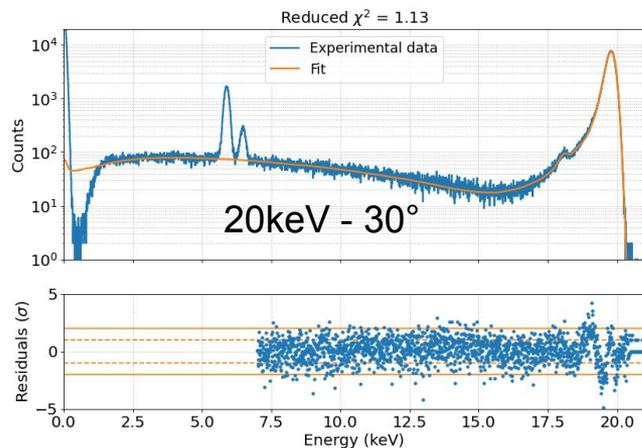
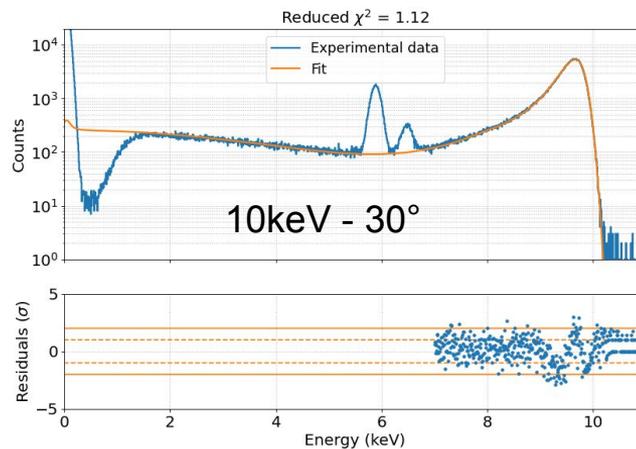
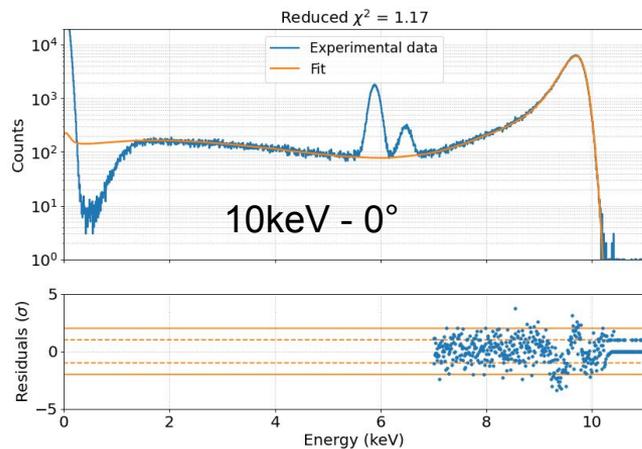


contributions from bulk and layers

Spectrum with QE applied



# Comparison with data

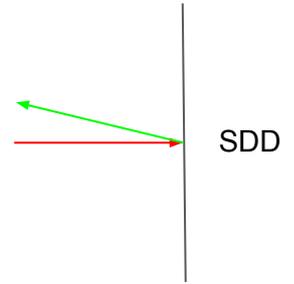
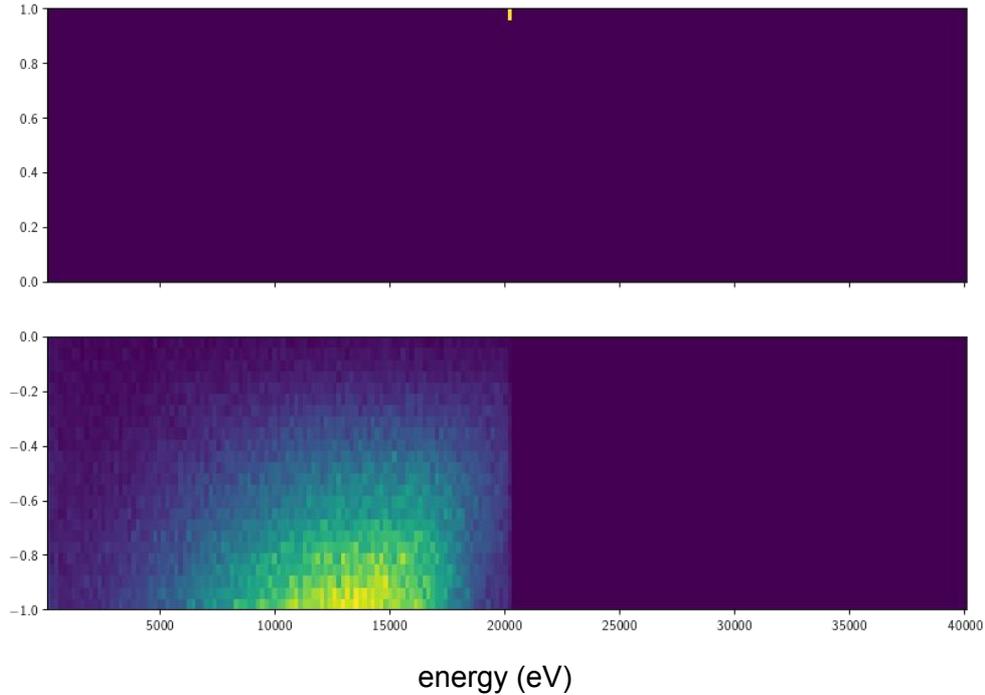


- monochromatic and collimated electrons from a SEM
- different energies and angles
- **good agreement so far**

# Some checks

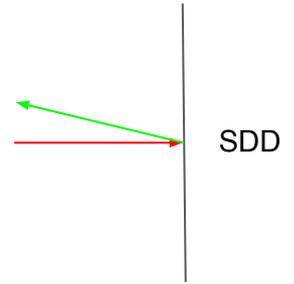
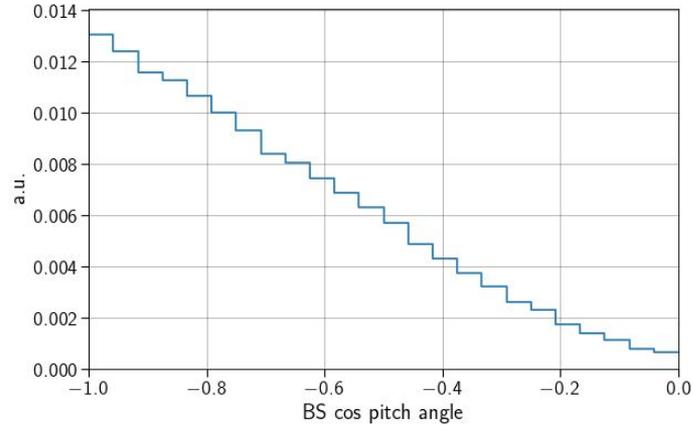
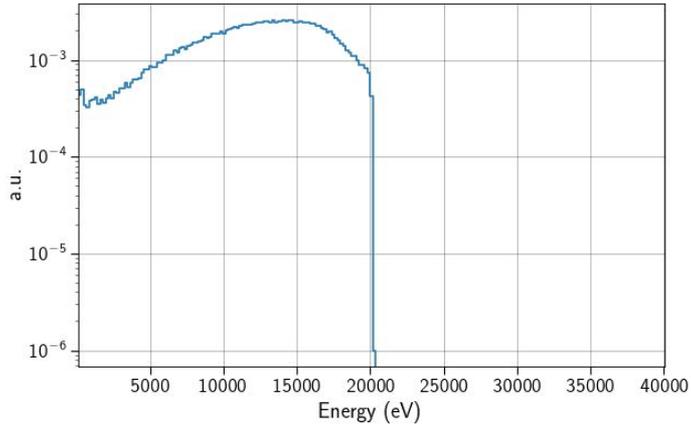
input energy near 20 keV, input angle near  $0^\circ$  ( $\cos=1$ )

input cos (from 0 to 1)  
= input ang (from  $90^\circ$  to  $0^\circ$ )



# Some checks

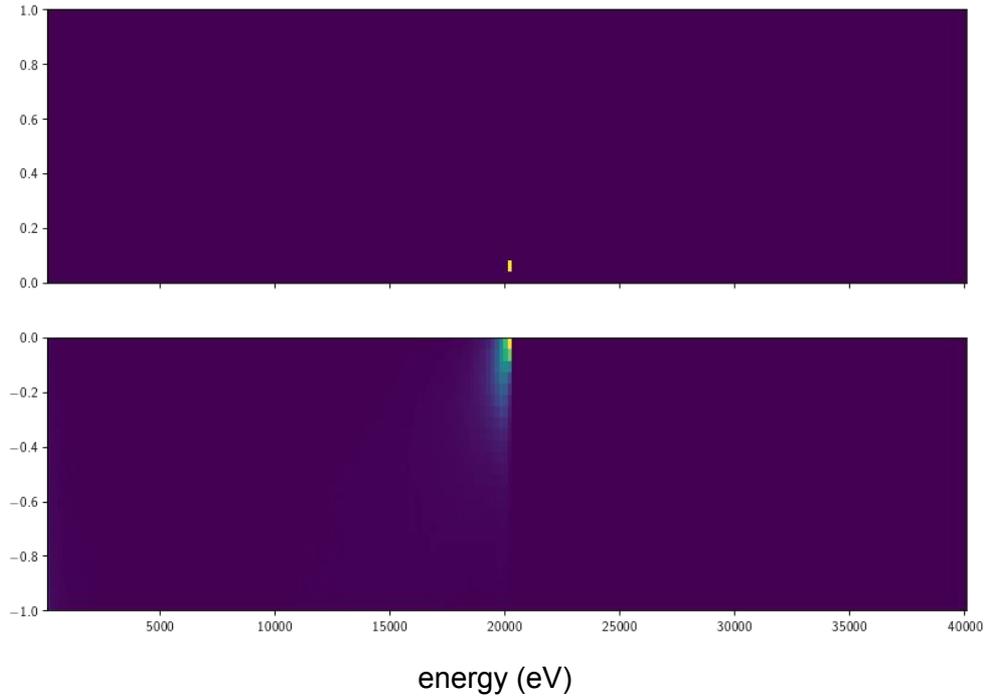
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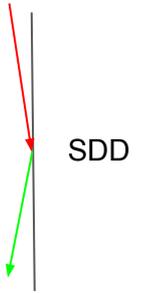
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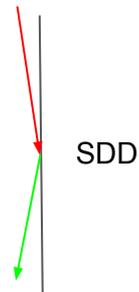
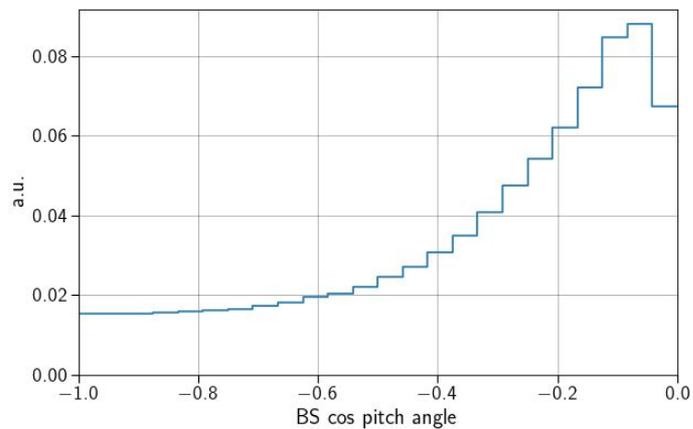
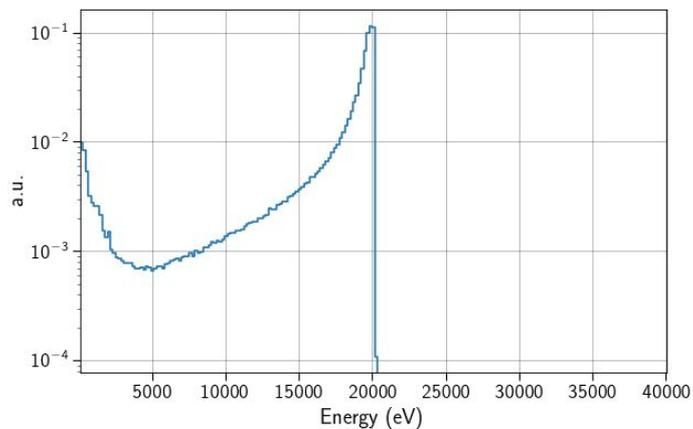


output cos (from -1 to 0)  
= output ang (from  $180^\circ$  to  $90^\circ$ )



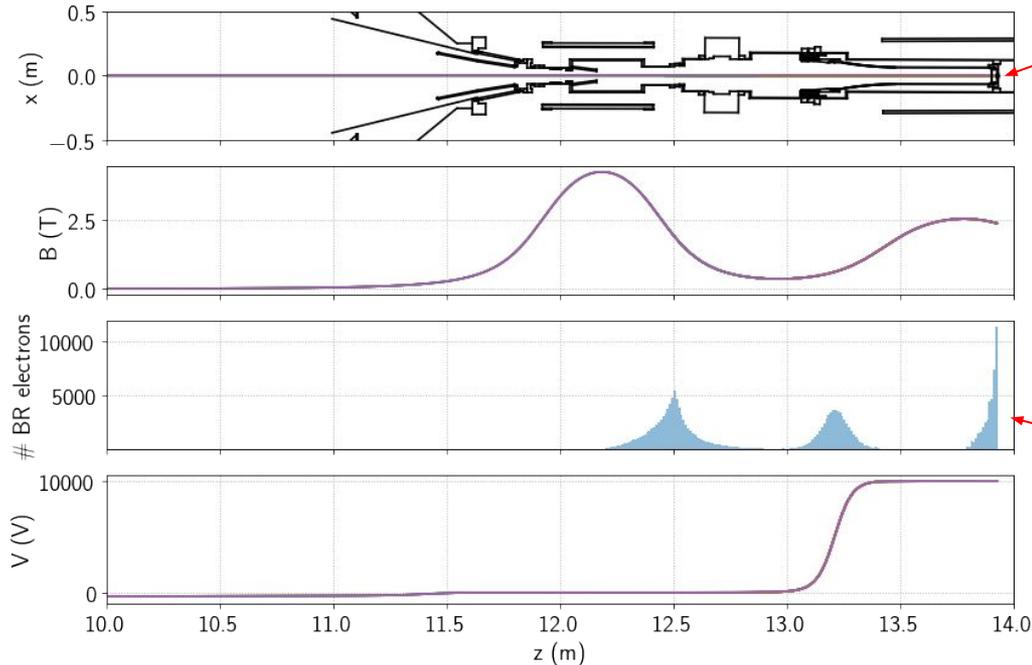
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# Backreflection simulation

- In order to know if the backreflection is fast or slow we need to know the time required to return back to the detector
- this can be **simulated with Kassiopeia**



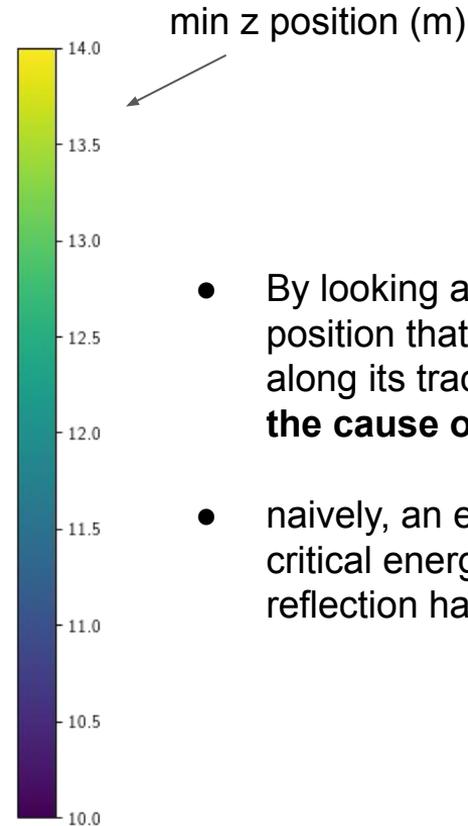
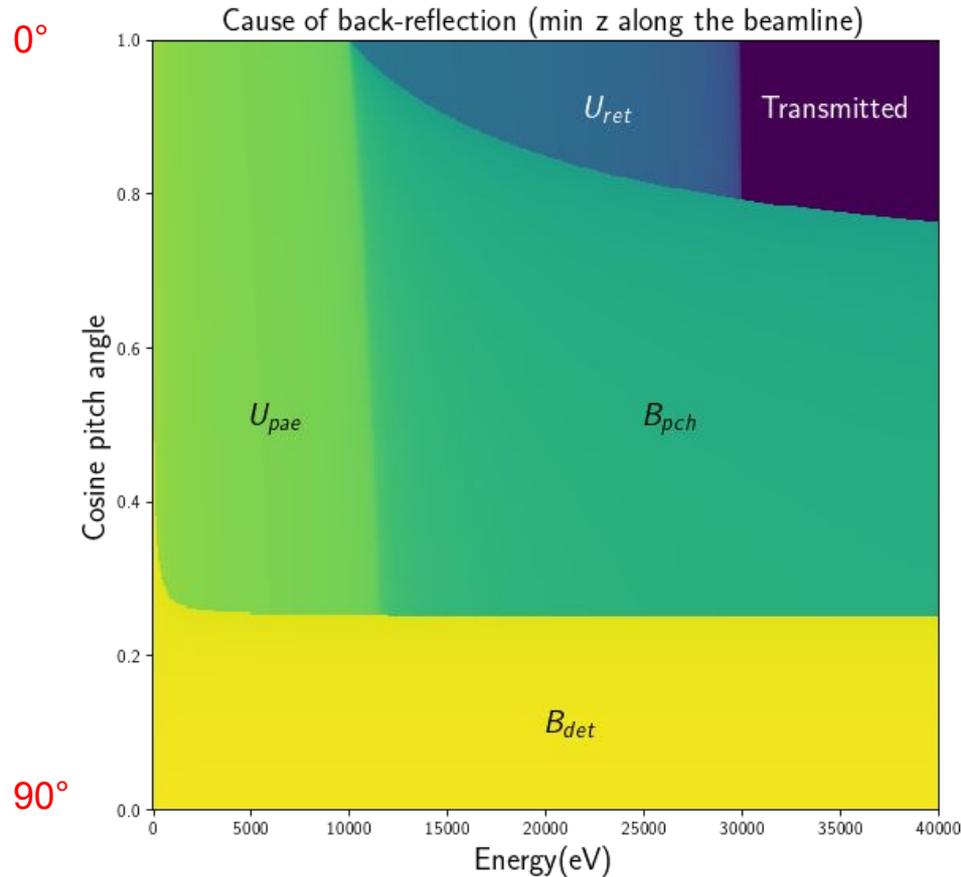
- **Electrons generated at the detector**  
→ directed towards the source
- grid scan in energy and angle

- configuration:

- $B_{\text{det}} = 2.52$  T
- $U_{\text{pae}} = 10$  kV
- $B_{\text{pch}} = 4.2$  T

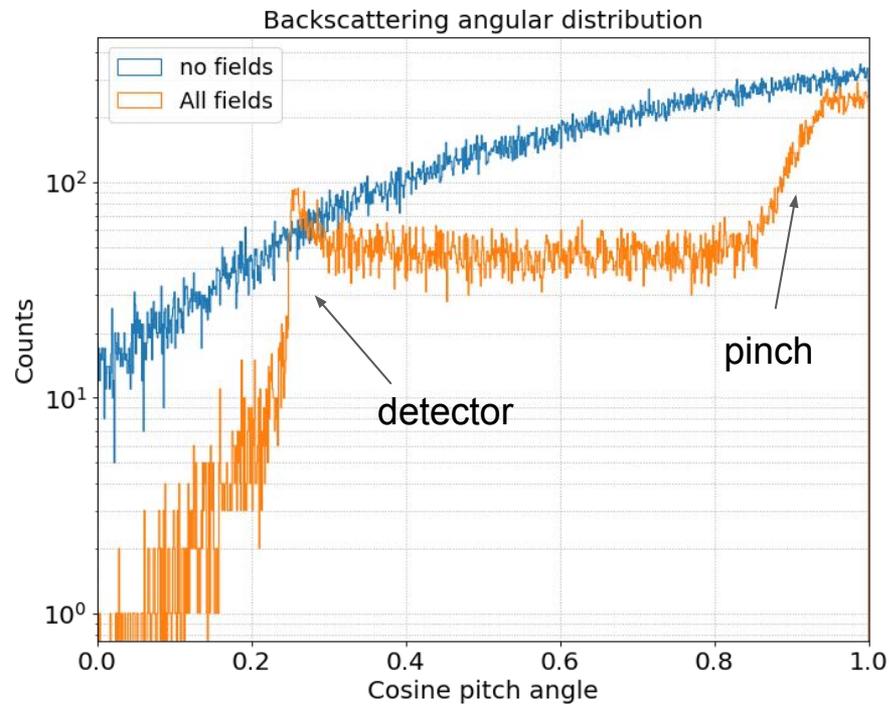
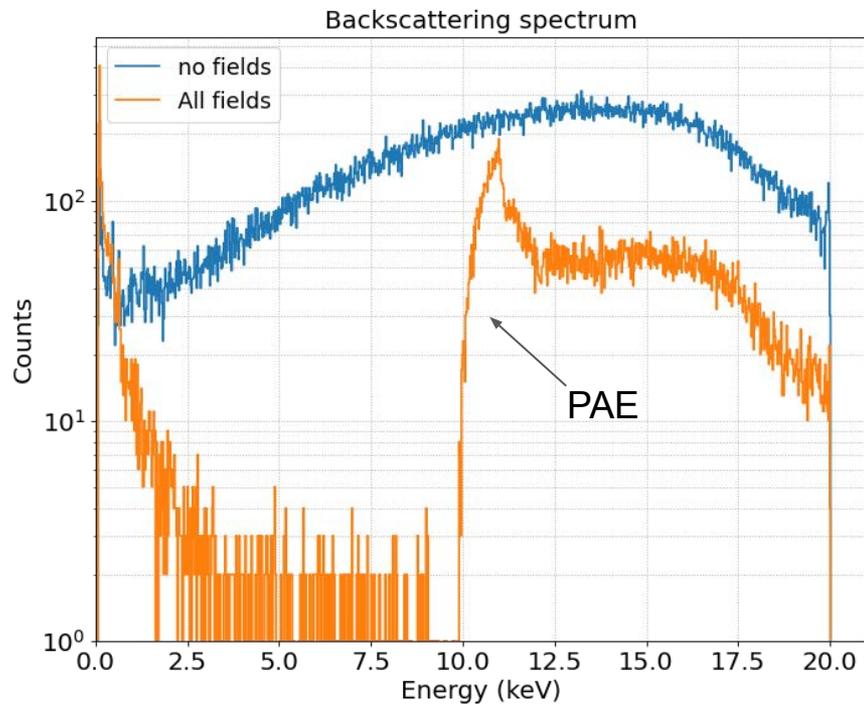
- the blue histogram represents the point where the backreflection happens ( $B_{\text{det}}, U_{\text{pae}}, B_{\text{pch}}$ )

# Cause of the backreflection

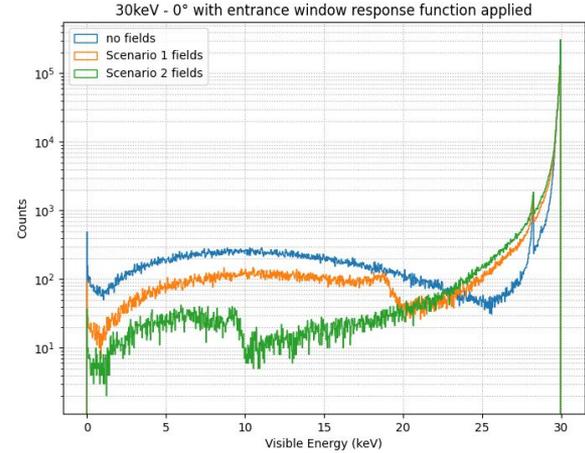
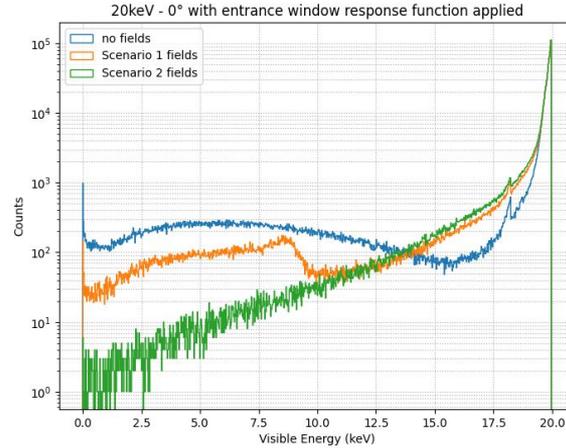
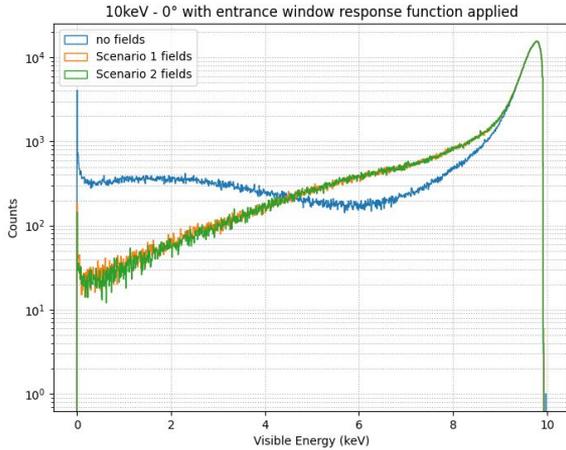


- By looking at the minimum z position that the electron reaches along its tracking, **we can identify the cause of the backreflection**
- naively, an electric reflection has a critical energy, while a magnetic reflection has a critical angle

# A look at the backscattering response



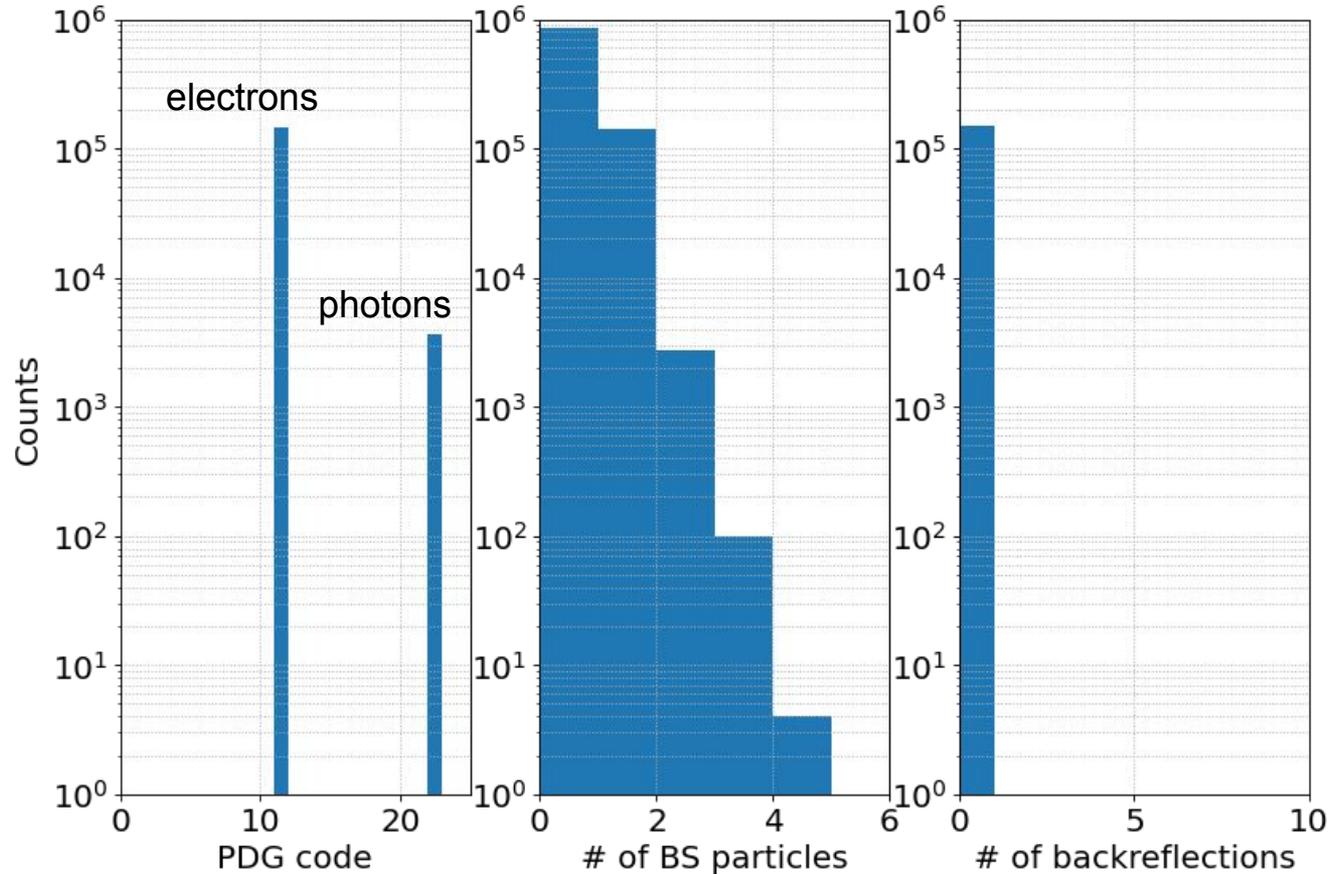
# BR for different energies



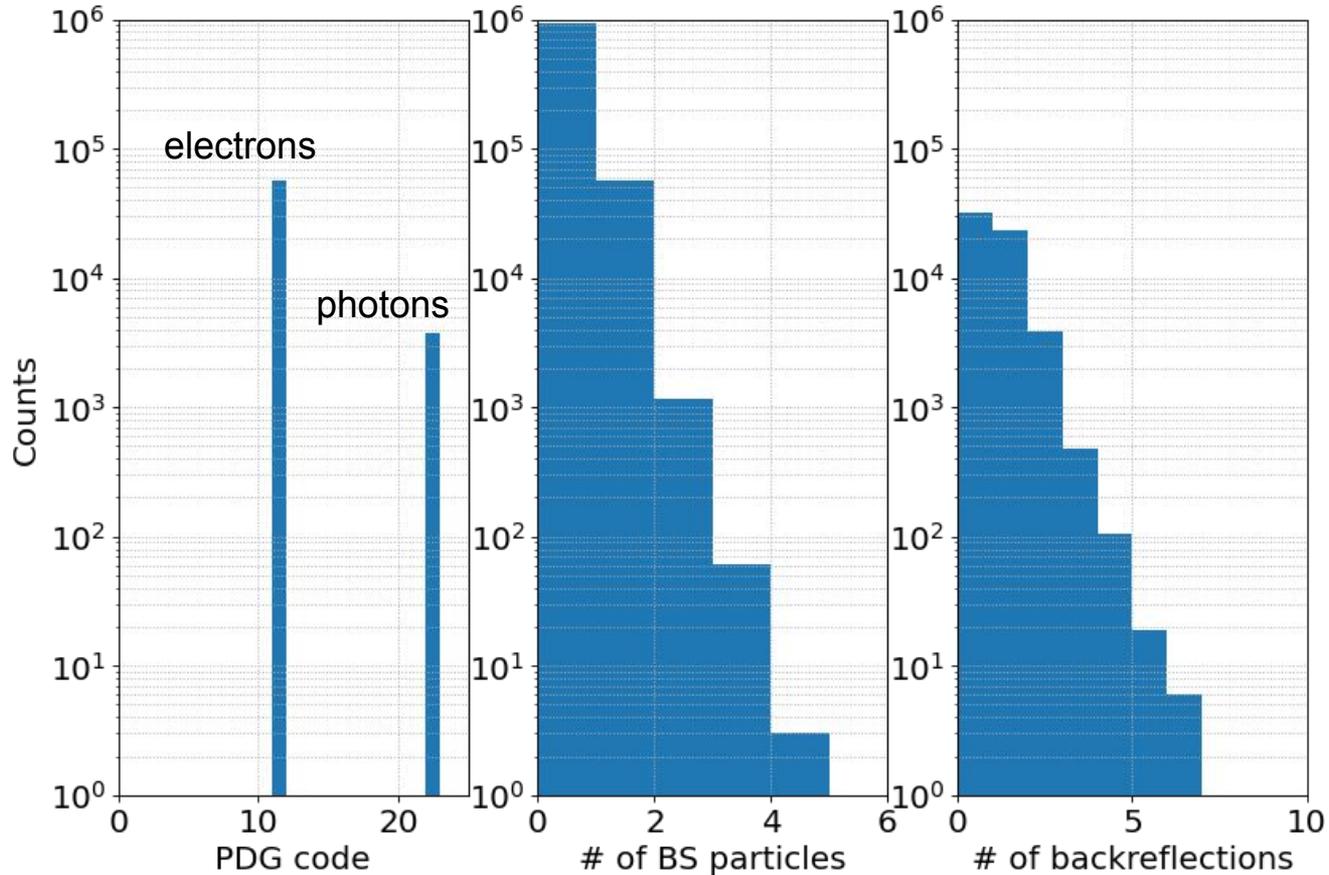
Shoulder in the response only present if a backscattered electron can overpass the PAE

- for Scenario1 more than 10 keV are needed
- for Scenario2 more than 20keV are needed

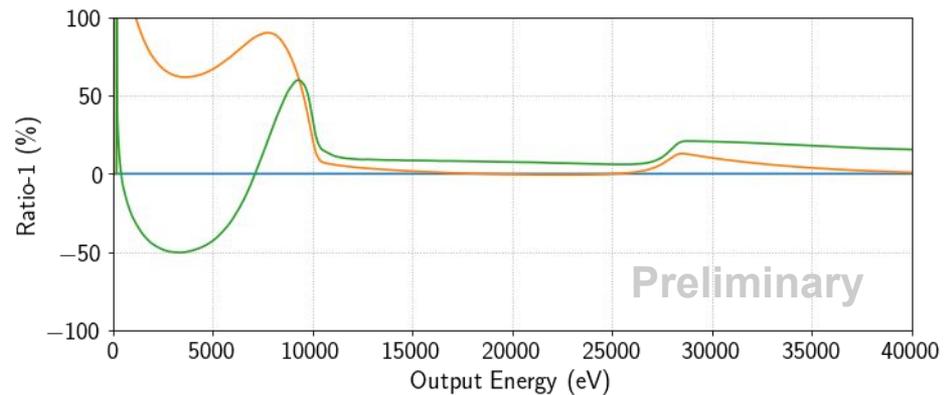
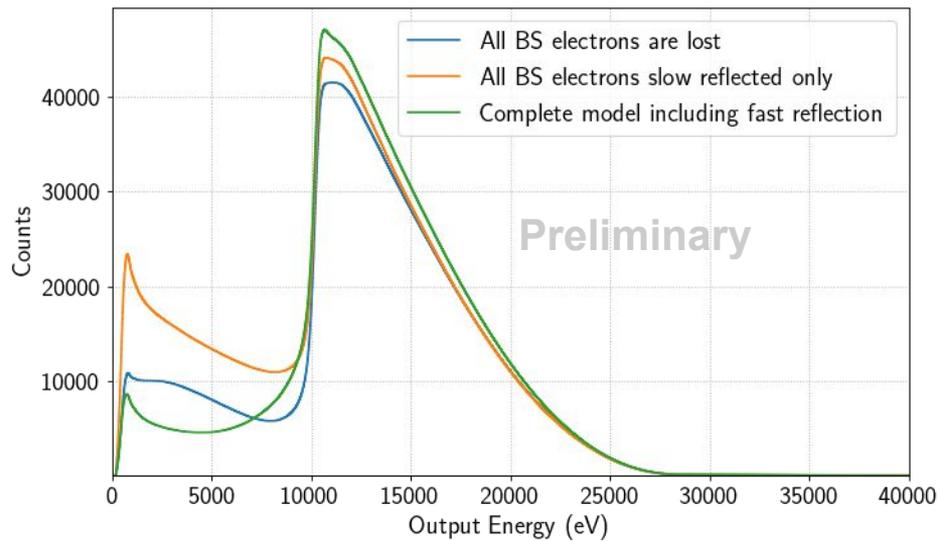
# Some backscattering informations (w/o BR)



# Some backscattering informations (with BR)



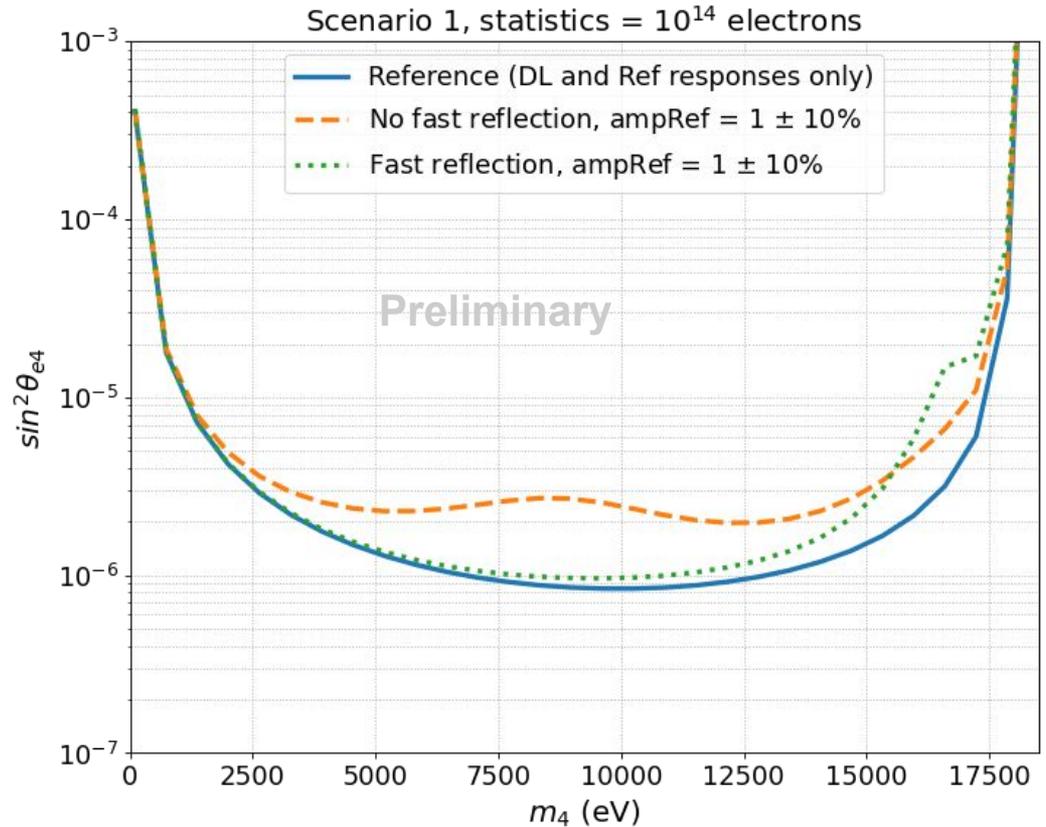
# Backreflection impact on Tritium spectrum



# Super preliminary sensitivity

## ampBR parameter:

- same implementation as ampRW
- 10% uncertainty considered
- reference spectrum with only DL and BS reflection responses



# Super preliminary sensitivity

## DL parameter:

- same implementation as always
- 5% uncertainty considered
- reference spectrum with only DL and BS reflection responses

