

Studies of boosted topologies in the search for NMSSM inspired di-Higgs events in the $\tau\tau + bb$ final state with the CMS experiment

Martin Marz | September 12, 2022

Table of contents

- 1 Underlying model
- 2 Current status of the analysis
- 3 Boosted topologies
- 4 Goals of my thesis
- 5 Generator studies
- 6 Multiclassification with neural networks
- 7 Results
- 8 Summary and outlook

The Standard Model (SM)

- Lepton and boson masses generated via spontaneous electroweak symmetry breaking
- Prediction of a single Higgs boson
- SM has shortcomings (Gravitation, DM etc.)
- One possible extension is supersymmetry

Model: SM

Bosonic content
of Higgs sector:



Figure: Courtesy of Felix Heyen

Minimal Supersymmetric Standard Model (MSSM)

- Minimal extension with SU(2) Higgs doublet
- Predicts super partners for all particles with different spin quantum number
- No super partners observed till now

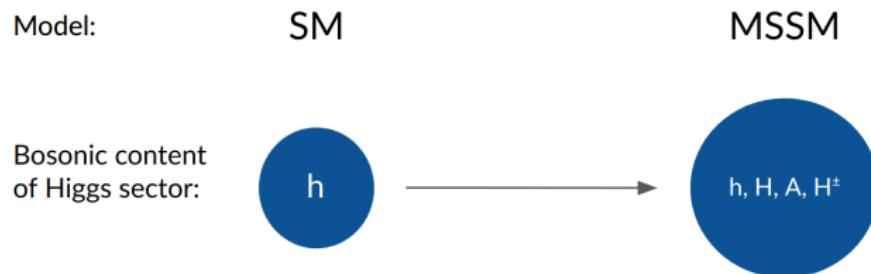


Figure: Courtesy of Felix Heyen

Introduction to the NMSSM

- MSSM symmetry **must** be broken
- Next-to-Minimal Supersymmetric Standard Model (**NMSSM**): symmetry breaking occurs **naturally**
- Introduce additional singlet scalar field
- Results in **even more** Higgs bosons (7 in total)
- For my thesis h and h_s of importance

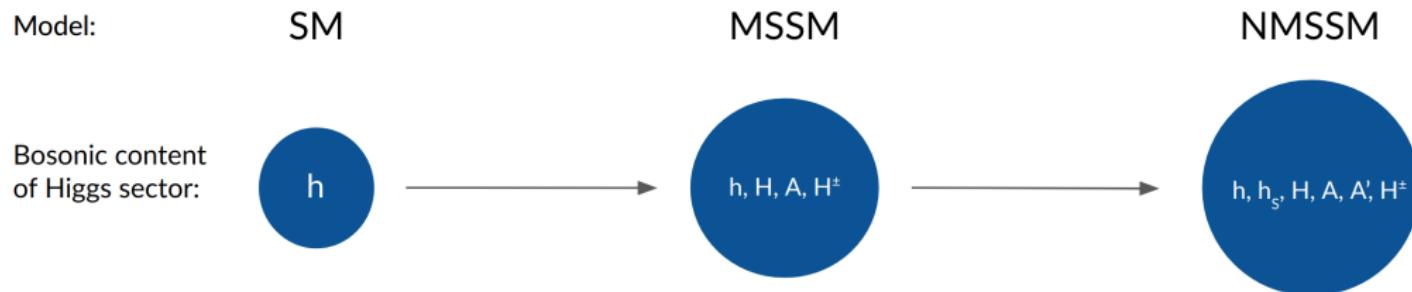


Figure: Courtesy of Felix Heyen

Overview

- Search for di-Higgs events in the $H \rightarrow h(\tau\tau)h_S(bb)$ final state
- $h \hat{=} \text{Higgs boson with standard model like properties } m_h = 125 \text{ GeV}$
- $h_S \hat{=} \text{new singlet Higgs boson}$
- $H \hat{=} \text{new heavy Higgs boson}$
- Analysis by Dr. Janek Bechtel at KIT ([ETP-KA/2021-04](#))
- Published analysis: [here](#)

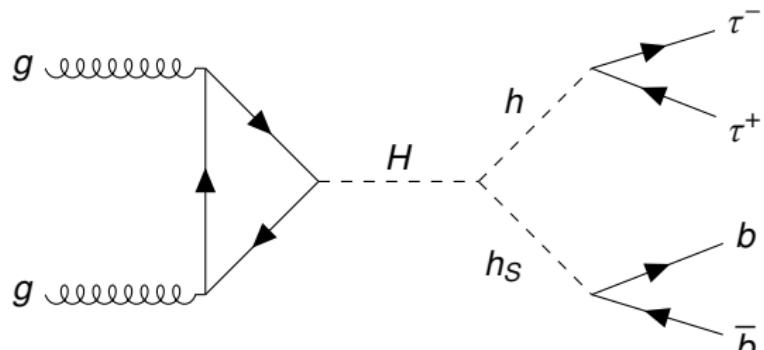


Figure: Feynman diagram for the $H \rightarrow h(\tau\tau)h_S(bb)$ final state.

Current upper limits

- $m_h = 125 \text{ GeV}$
- No theory prediction for m_H, m_{h_S}
 - ⇒ free parameters
 - ⇒ large possible mass range
- Only **on-shell** decays
 - ⇒ restriction on m_H, m_{h_S}
- Upper limits on
$$\sigma(gg \rightarrow H)B(H \rightarrow hh_S \rightarrow \tau\tau + bb)$$
- Limits in graph scaled for visualization purposes

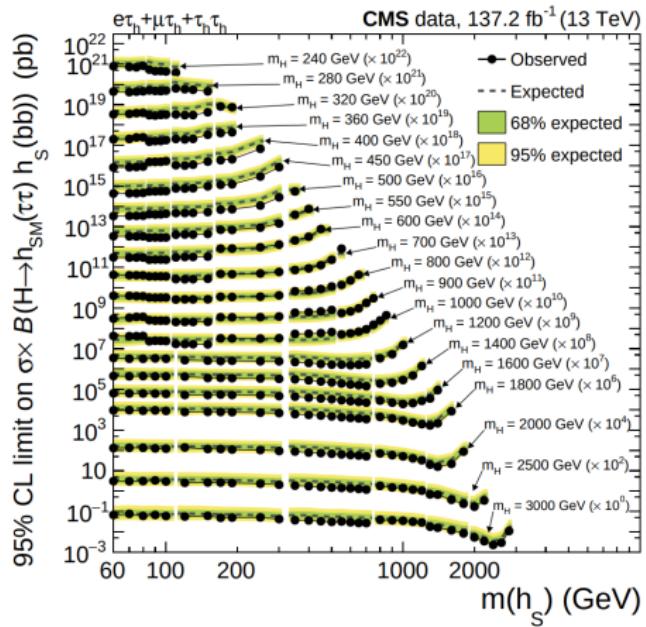


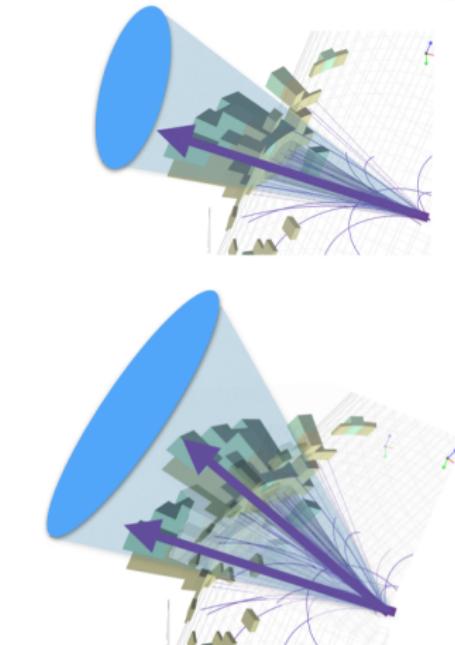
Figure: Taken from [published analysis](#)

Boosted topologies

- No dedicated studies regarding **high p_T** objects which could be useful for large heavy Higgs masses

$$\Delta R(\text{daughters}) \approx \frac{2M(\text{mother})}{p_T(\text{mother})}$$

- $\Delta R \hat{=} \text{relative distance in } \eta - \phi \text{ space between two objects}$
- **Light** objects decay with **high p_T**
 \implies **small ΔR** between decay products
- So for high m_H and/or small m_{h_S} small ΔR are expected
- Objects with **small ΔR** are called boosted



<https://indico.cern.ch/event/732102/contributions/3092580/attachments/1759641/2854473/>

Swapped final state

- Felix Heyen studied the inclusion of the swapped final state $H \rightarrow h(bb)h_S(\tau\tau)$ ([ETP-KA/2021-18](#))
- Only the $\tau_h\tau_h$ final state was used

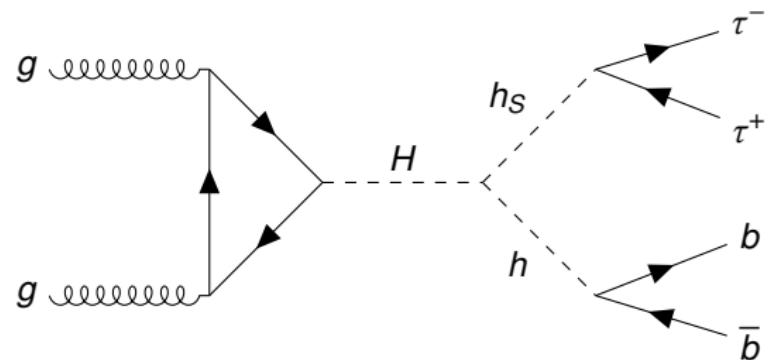


Figure: Feynman diagram for the $H \rightarrow h(\tau\tau)h_S(bb)$ final state.

Results of Felix's thesis

- An overall improvement is achieved
- Different exclusion sensitivity for the two final states
- Attributed to efficiency of boosted topologies
- Particularly relevant for boosted $h_s \rightarrow \tau\tau$ decays with $m_{hs} < 125$ GeV
- $h \rightarrow \tau\tau$ are boosted for heavy m_{hs}

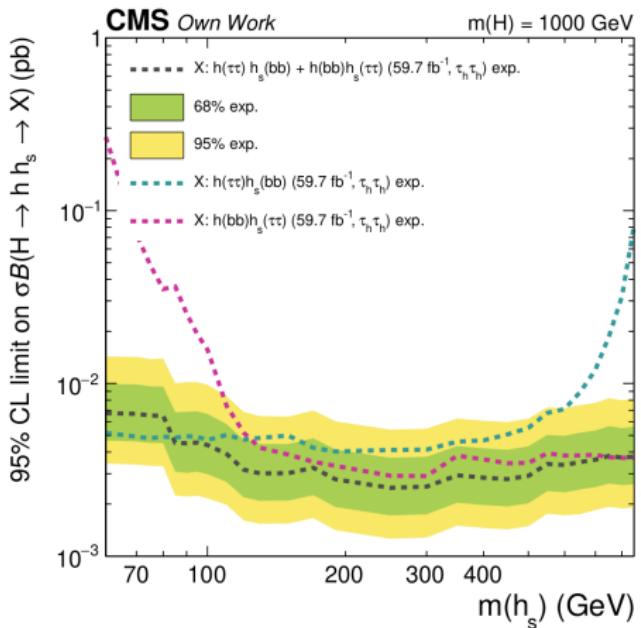


Figure: Taken from Felix Heyen's [master thesis](#)

Goals of my thesis

- ① Study the reconstruction efficiency of di-Higgs signal events
- ② Scan the mass phase space of m_H and m_{h_S} for boosted topologies
- ③ Study the impact of a dedicated treatment of events with boosted b-jet topologies
- Multiple differences w.r.t the published analysis due to switch to UL Run-2
- Final results **not** comparable with the published analysis
 \Rightarrow only relative improvement measured

Reconstruction efficiency

- Signal samples for $H \rightarrow h(bb)h_S(\tau\tau)$ and $H \rightarrow h(\tau\tau)h_S(bb)$
- $m_H = [600, 700, 800, 900, 1000, 1200]\text{GeV}$ and $m_{h_S} = 60\text{ GeV}$
- For the reconstruction efficiency calculation a reference set of events (N_{gen}) is needed
- Of interest are boosted topologies
- Reference set limited on fiducial volume (as shown in table below)
- In addition apply matching between generator and reconstruction level objects to determine identification purity

Table: Selection criteria on generator-level particles

Particle	Transverse momentum (GeV)	Pseudorapidity	Mother particle
μ	$p_T \geq 20$	$ \eta \leq 2.6$	h_S/h
τ_h	$p_T \geq 25$	$ \eta \leq 2.8$	h_S/h
b-quark	$p_T \geq 15$	$ \eta \leq 3.0$	h/h_S

Event selection criteria

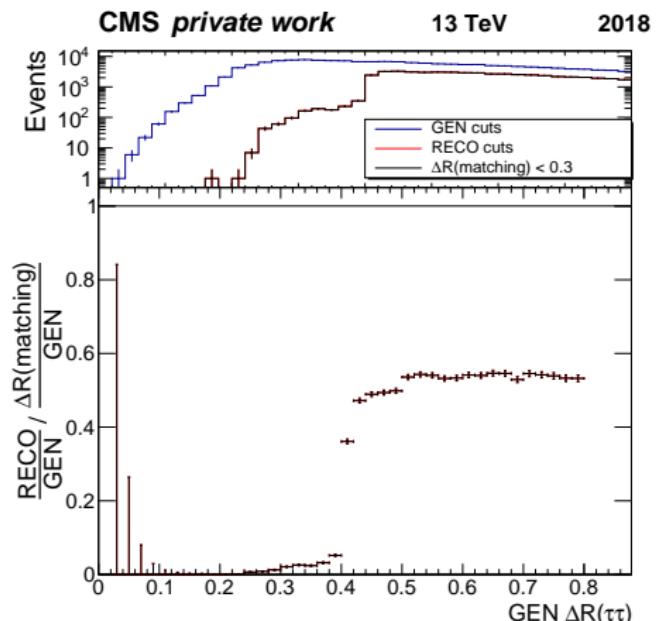
- Each event needs to pass multiple sets of selection criteria
- Most important RECO cuts: based on the published analysis
 - ① presence of a $\mu\tau_h$ -pair
 - ② $N_{\text{jets}} \geq 2$ with $p_T \geq 30 \text{ GeV}$
 - ③ $N_{\text{bjets}} \geq 1$ with $p_T \geq 20 \text{ GeV}$
- $\Delta R(\mu\tau_h) \geq 0.5$ cut left out since boosted topologies are of interest
- b-jet pair constructed from jets to reconstruct the respective Higgs boson

GEN $\Delta R(\tau\tau)$ dependency

- Only lepton selection applied to isolate reconstruction efficiency from the b-quark pair
- Only statistical uncertainties shown in plot on the right
- Reconstruction efficiency reveals a steep drop for

$$\text{GEN } \Delta R(\tau\tau) \leq 0.5$$

- Identification purity $\approx 100\%$
- Current event selection **not** suited for boosted τ -topologies
- This explains the lower event yield and subsequently the different exclusion sensitivity for boosted $\tau\tau$ events found by Felix Heyen

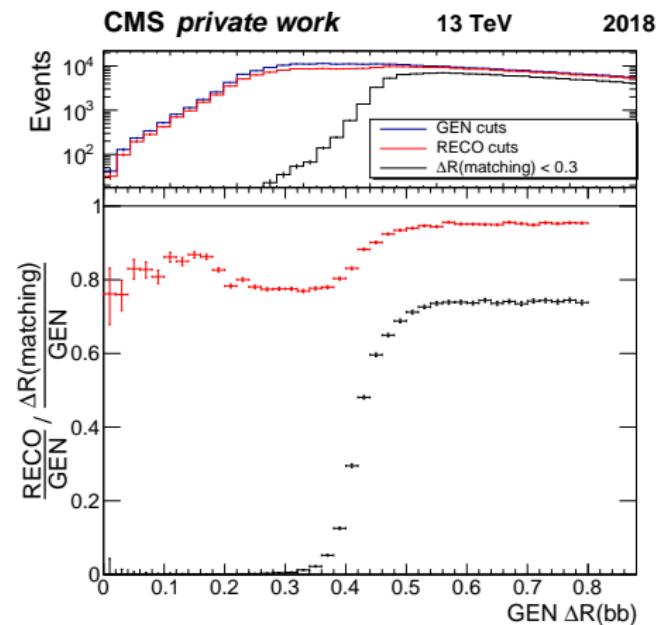


GEN $\Delta R(\text{bb})$ dependency

- Only b-quark and jet selection applied to isolate reconstruction efficiency from the $\mu\tau_h$ -pair
- Only statistical uncertainties shown in plot on the right
- Reconstruction efficiency reveals a small drop for

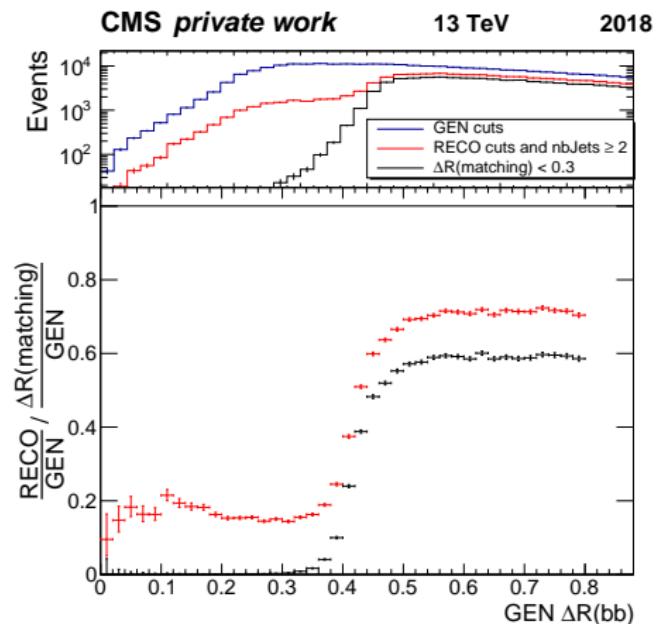
$$\text{GEN } \Delta R(\text{bb}) \leq 0.5$$

- Identification purity $\approx 0\%$ for this region
- Signal events with boosted b-jet pairs pass current event selection but are not reconstructed correctly



Interpretation

- $N_{\text{bjets}} \geq 1$ criteria allows most of the events with boosted b-jet topology
- A dedicated treatment of events with misidentified particles (boosted events) should improve the analysis in concerned kinematic regions



Goals

- 1 Study the generator event selection of signal events (selection as shown before)
- 2 Study the regions with boosted topologies
- 3 Categorization of each m_H ; m_{h_S} mass hypothesis

Categorization

- Each $m_H; m_{h_S}$ mass hypothesis falls into one of four categories

- ➊ A mass hypothesis is classified as **boosted $\tau\tau$** if

$$\text{median } \Delta R(\tau\tau) \leq 0.5$$

- ➋ Equally a hypothesis is classified as **boosted bb** if

$$\text{median } \Delta R(bb) \leq 0.5$$

- ➌ A hypothesis can be **boosted $\tau\tau$** and **boosted bb** at the same time

- ➍ A hypothesis can be neither **boosted $\tau\tau$** nor **boosted bb**

- The threshold 0.5 is chosen based on the previously observed efficiency drops

Results

- Hypotheses marked in:
 - Red have an event acceptance below 20 %
 - Green are the hypotheses categorized as **boosted bb**
 - Blue are the hypotheses categorized as **boosted $\tau\tau$**
 - Almost all hypotheses contain events with a boosted τ -pair and/or b-pair
- Similar study for the swapped final state $H \rightarrow h(bb)h_S(\tau\tau)$ (Manuel Freudig)
- Regions for **boosted $\tau\tau$** and **boosted bb** hypotheses are also swapped

CMS simulation
work in progress

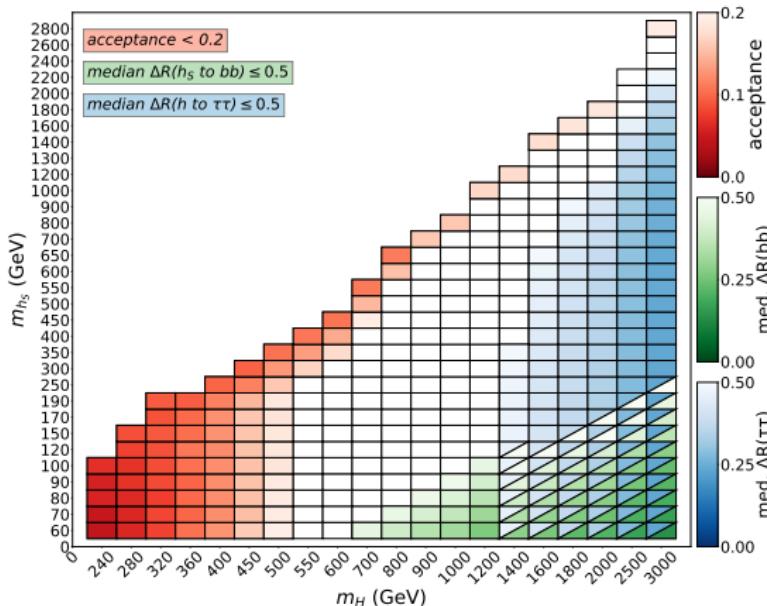


Figure: $H \rightarrow h(\tau\tau)h_S(bb)$

Summary of generator study

- Boosted $\mu\tau_h$ -pairs do **not** pass the event selection criteria
- $N_{bjets} \geq 1$ allows most of the boosted b-jet signatures to pass the event selection
- These events contain to a large fraction mis-identified b-jet pairs
- Boosted signatures are expected for a significant number of m_H - m_{h_S} hypotheses independent of the decay channel
- The kinematic acceptance is bad for small m_H and/or high m_{h_S}

Multiclassification

- Classify signal and background processes
- Event classification with neural network (NN)
- 16 input features
 - ① p_T of the μ
 - ② visible p_T of the τ_h
 - ③ ...
- 5 Output nodes
 - ① $H \rightarrow h(\tau\tau)h_S(bb)$
 - ② $H \rightarrow h(bb)h_S(\tau\tau)$
 - ③ Zll
 - ④ $W+jets$
 - ⑤ $t\bar{t}$

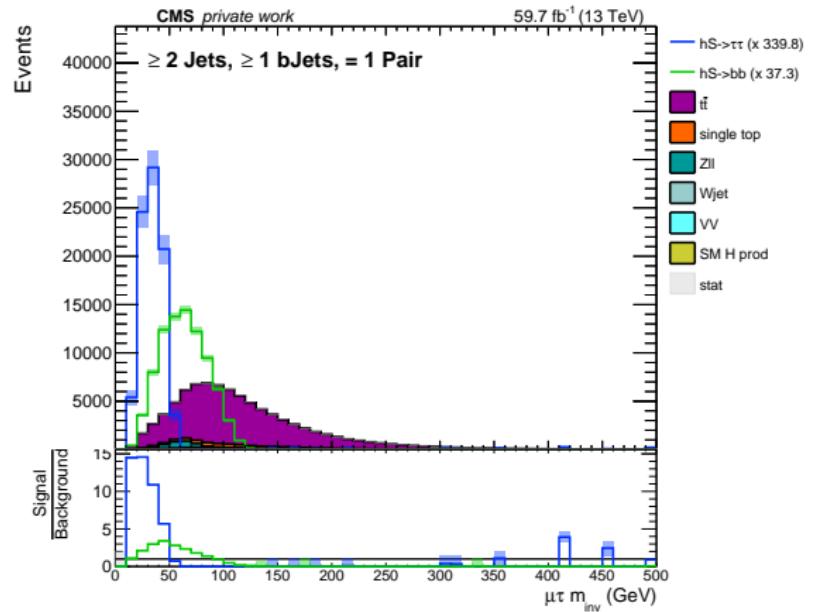


Figure: $m_H = 1200 \text{ GeV}$

Measures to improve multiclassification

- Architecture similar to the original analysis
- Baseline NN trained for relative comparison

Adding input features (Feat.)

- 13 new input features are introduced to the analysis
- Selected due to their high discriminating power between signal and background
- Mostly AK8 (i.e. $R = 0.8$) jet variables are chosen to make use of boosted b-jet topologies

Splitting $H \rightarrow h(\tau\tau)h_S(bb)$ into two orthogonal groups (Split.)

- 1 $H \rightarrow h(\tau\tau)h_S(bb)$ signal events with a spacial distance $\text{GEN}\Delta R(bb) \leq 0.5$ (boosted)
- 2 $H \rightarrow h(\tau\tau)h_S(bb)$ signal events with a spacial distance $\text{GEN}\Delta R(bb) > 0.5$ (resolved)

One additional selection criterion ($N_{\text{AK}8}$)

- $N_{\text{AK}8 \text{ jet}} \geq 1$
- Each aiming at optimizing the NN for boosted topologies without losing performance for resolved topologies

Comparison of confusion matrices and Taylor coefficients

- The discrimination between the two final states and signal versus background (ROC score range of 0.7-0.9) for each NN
- All NN's with changes performed better on confusion matrix level compared to the baseline
- The most important features for the baseline NN are:
 - ① m of the $\mu\tau_h$ -pair
 - ② m of $\tau\tau + bb$
 - ③ p_T of the p_T -leading b-jet
- The most important features for the NN with additional set of input features are:
 - ① m of the $\mu\tau_h$ -pair
 - ② **new:** ΔR between the $\mu\tau_h$ -pair and b-jet pair
 - ③ p_T of the p_T -leading b-jet
 - ④ **new:** p_T of the p_T -leading AK8-jet

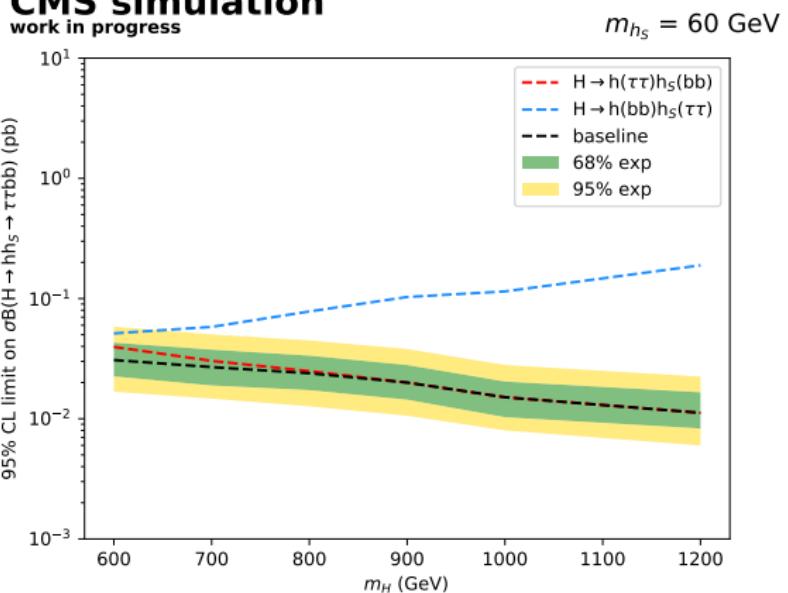
More realistic comparison method

- For each NN signal and background templates are produced
- Statistical model ($\mu \cdot s + b$) is only taking statistical uncertainties into account
- Expected asymptotic 95 % CL upper limit on $\sigma(gg \rightarrow H)B(H \rightarrow hh_S \rightarrow \tau\tau + bb)$ calculated for each approach using the CL_S method

Expected upper limit: baseline

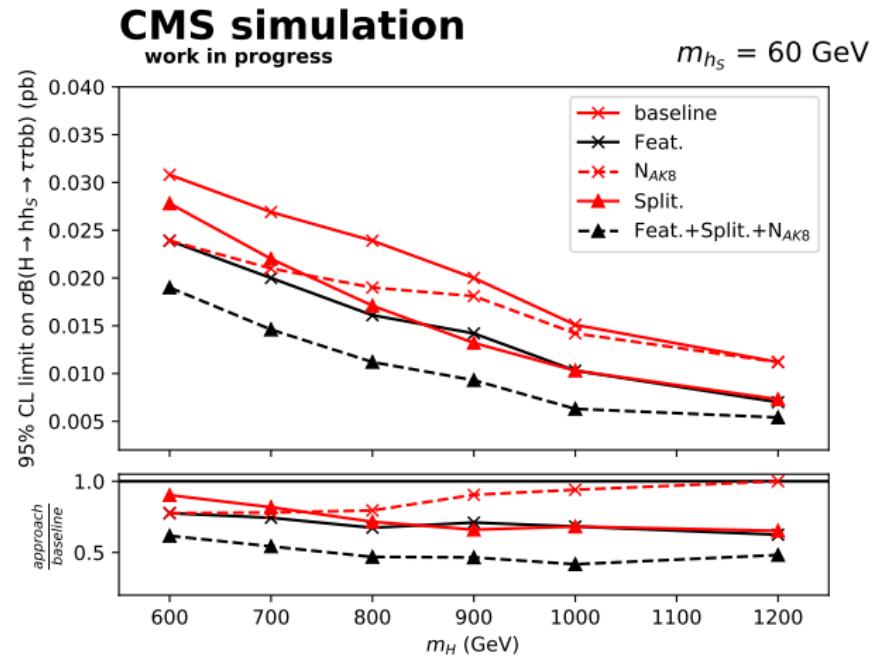
- Limit is decreasing for higher m_H
- Effect of increasing event acceptance
- Stronger effect than event loss due to reconstruction efficiency
- Weaker limit for $H \rightarrow h(bb)h_S(\tau\tau)$ correlates with high fraction of boosted events

CMS simulation work in progress



Interpretation of upper limits

- Isolated changes:
 - ① **Feat.**: Stronger for high m_H correlates with stronger discrimination power of variables
 - ② **Split.**: Bad discrimination between resolved and boosted signal topology for small m_H
 - ③ **N_{A_K8}**: Loss of events for high m_H
- Largest improvement when applying all three changes together
- Average improvement of 50 %



Conclusion

- On its own adding input features resulted in highest improvement between the three treatments
- Highest improvement when applying all three treatments at once
- Effect could be different for other m_H - m_{h_S} regions
- A dedicated treatment of boosted b-jet topologies is beneficial
- Only statistical uncertainties in this study

Summary and outlook

Summary

- Boosted $\mu\tau_h$ -pair topologies do **not** pass the event selection criteria
- Boosted b-jet topologies pass the current event selection criteria
- High number of events with boosted topologies are expected
- $\Delta R(hh_S)$ is a characterizing feature
- Dedicated treatment of boosted topologies is beneficial for the analysis

Outlook

- Extend study to bigger m_H - m_{h_S} parameter phase space
- Improve AK8 jet selection and description
 - ① spatial matching with b-jet
 - ② make better use of substructure
- Include $\tau_h\tau_h$ and $e\tau_h$ final states
- Adept event selection criteria for boosted $\mu\tau_h$ -pair topologies

Table: Selection criteria for μ in the $\mu\tau_h$ final state

Muon ID	Transverse momentum [GeV]	Pseudorapidity	Distance from PV [cm]	ParticleFlow isolation (ΔR)
medium	$p_T \geq 25$	$ \eta \leq 2.1$	$d_z \leq 0.2$ $d_{xy} \leq 0.045$	≤ 0.15 (0.4)

Table: Selection criteria for τ_h in the $\mu\tau_h$ final state

Transverse momentum [GeV]	Pseudorapidity	Distance from PV [cm]	DeepTau Identification WP
$p_T \geq 30$	$ \eta \leq 2.3$	$d_z \leq 0.2$ $d_{xy} \leq 0.045$	Tight vs μ VVLoose vs e Medium vs jets

Pair algorithm

Table: $\mu\tau_h$ pair algorithm

Importance	Criteria
4.	smallest μ ParticleFlow isolation
3.	highest μp_T
2.	highest DeepTau vs jets discriminator
1.	highest $\tau_h p_T$

Jet criteria

Table: Selection criteria for different jet types

Jet type	Transverse momentum [GeV]	Pseudorapidity	DeepFlavour Identification WP	Separation to leptons
b-jet	$p_T \geq 30$	$ \eta \leq 2.5$	medium	$\Delta R \geq 0.4$
non b-jet	$p_T \geq 20$	$ \eta \leq 2.5$	-	$\Delta R \geq 0.4$
AK8 jet	$p_T \geq 160$	$ \eta \leq 2.5$	-	$\Delta R \geq 0.8$

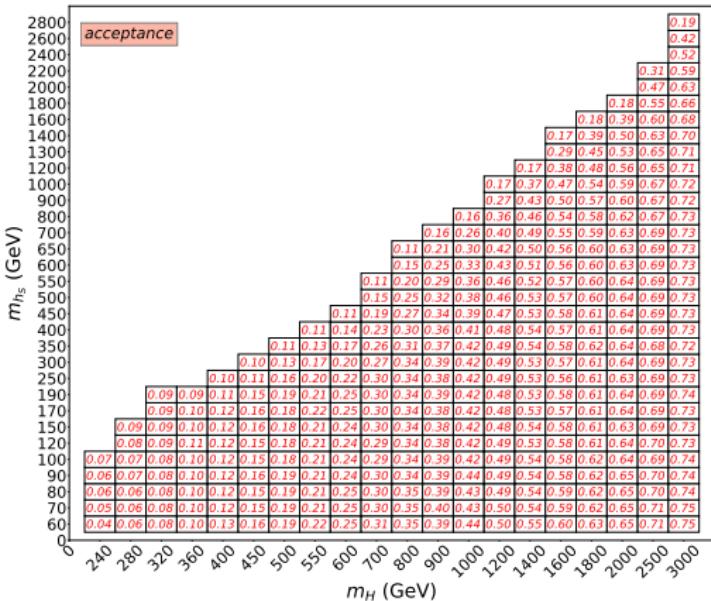
Veto leptons

Table: Selection criteria for veto leptons

Particle	Lepton ID	Transverse momentum [GeV]	Pseudorapidity	Distance from PV [cm]	ParticleFlow isolation (ΔR)
e	MVA noIso	$p_T \geq 10$	$ \eta \leq 2.1$	$d_z \leq 0.2$	≤ 0.3 (0.3)
	ID V2 WP90			$d_{xy} \leq 0.045$	
μ	medium	$p_T \geq 10$	$ \eta \leq 2.1$	$d_z \leq 0.2$ $d_{xy} \leq 0.045$	≤ 0.3 (0.4)

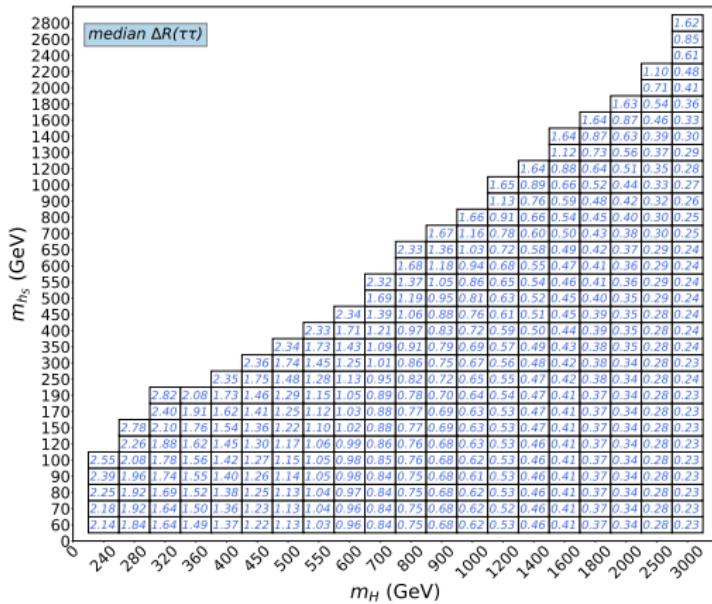
Acceptance

CMS simulation
work in progress

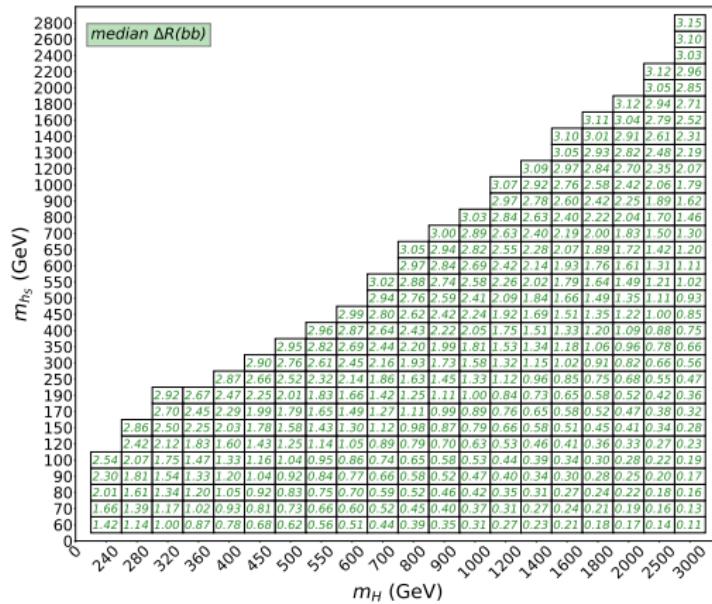


median ΔR

CMS simulation
work in progress



CMS simulation
work in progress



Baseline confusion

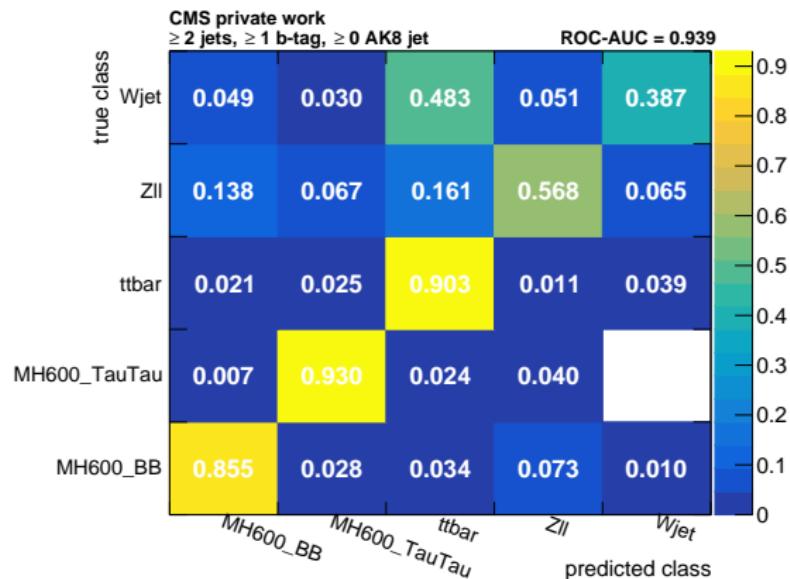


Figure: $m_H = 600$ GeV

Baseline Taylor

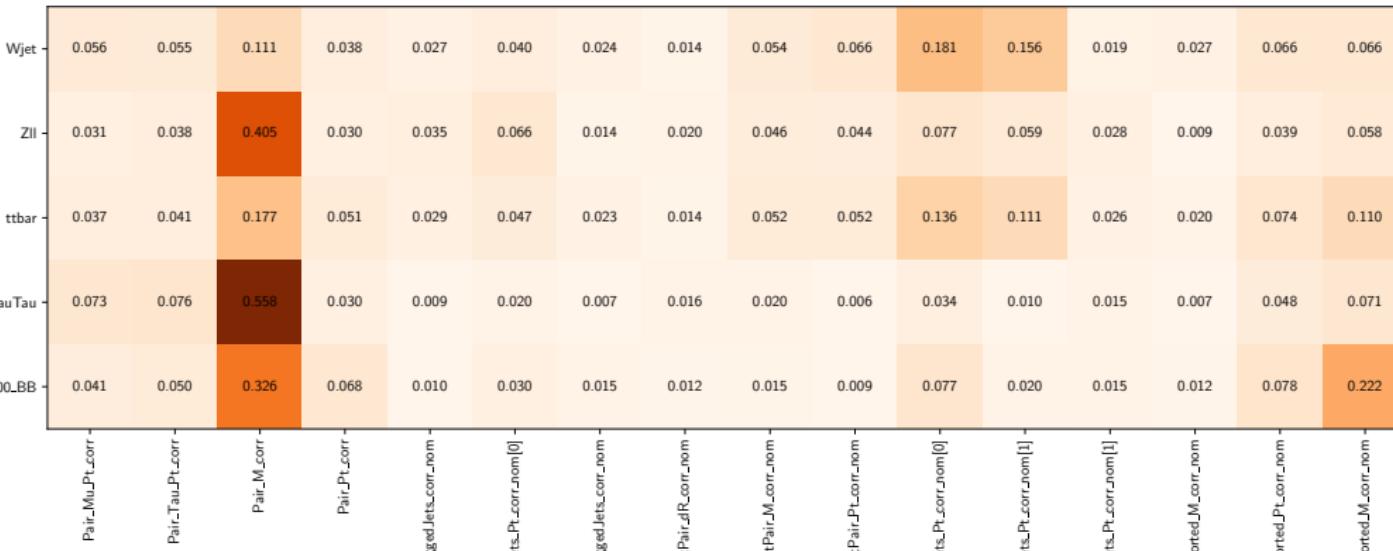


Figure: $m_H = 600 \text{ GeV}$

Add var confusion

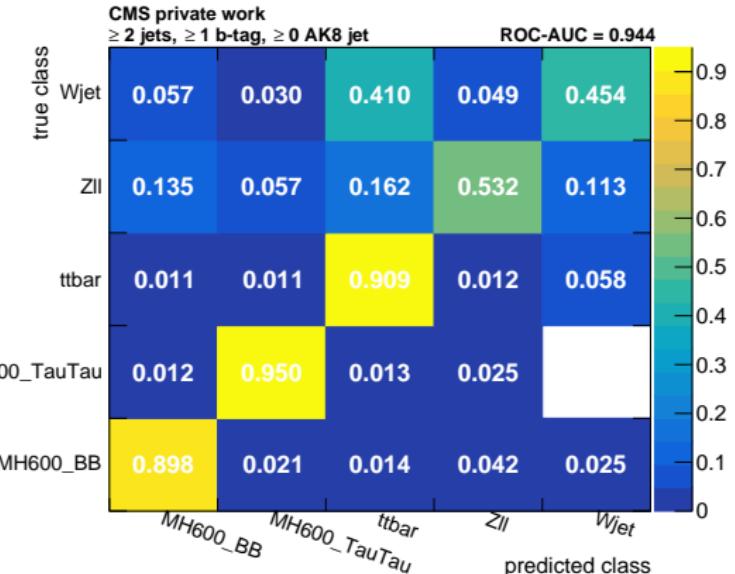


Figure: $m_H = 600$ GeV

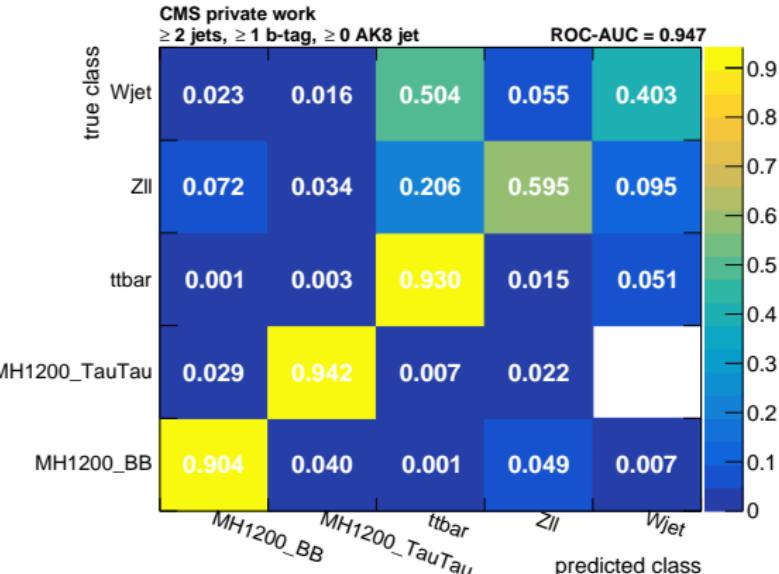


Figure: $m_H = 1200$ GeV

Add var Taylor

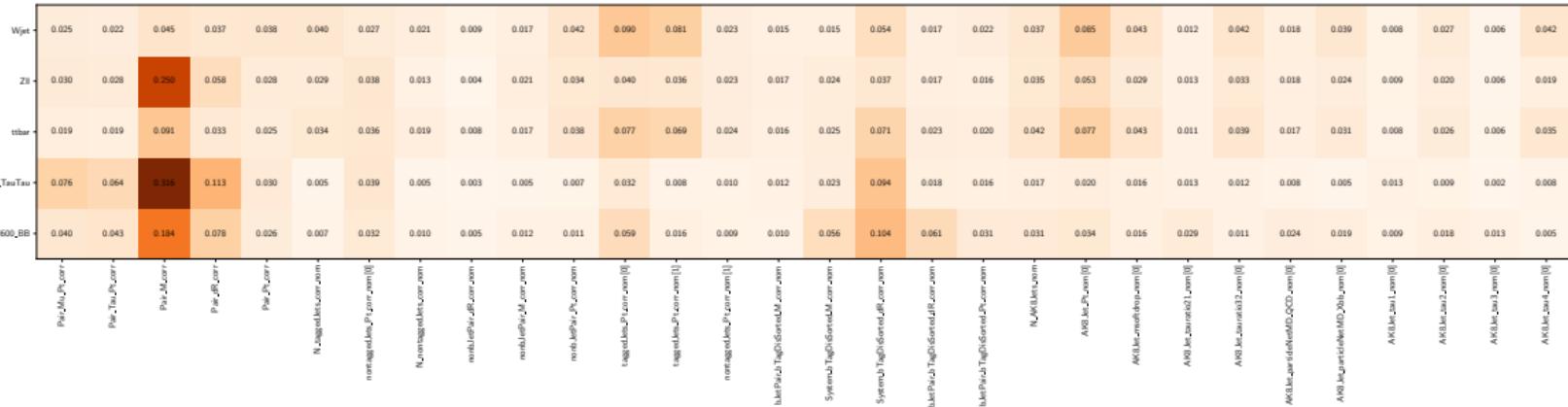


Figure: $m_H = 600 \text{ GeV}$

Split confusion

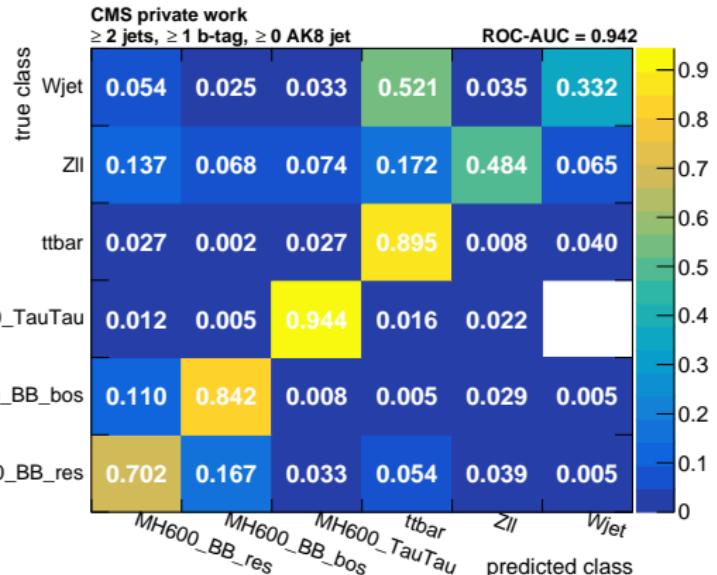


Figure: $m_H = 600$ GeV

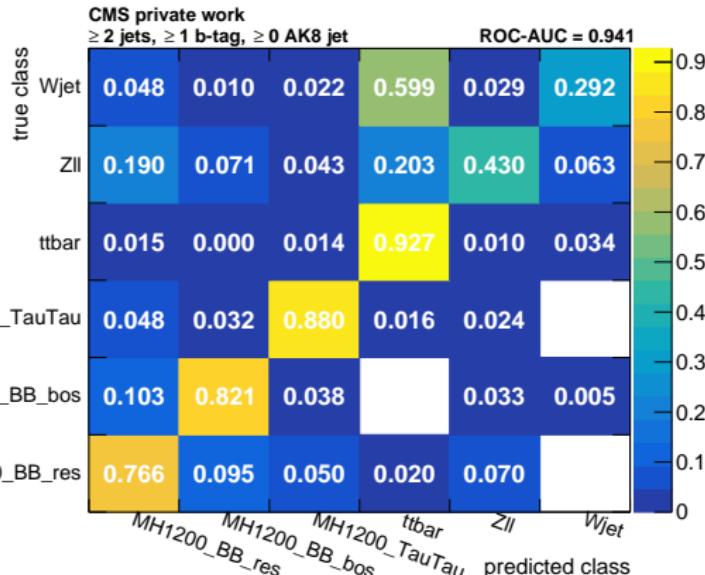


Figure: $m_H = 1200$ GeV

Cut confusion

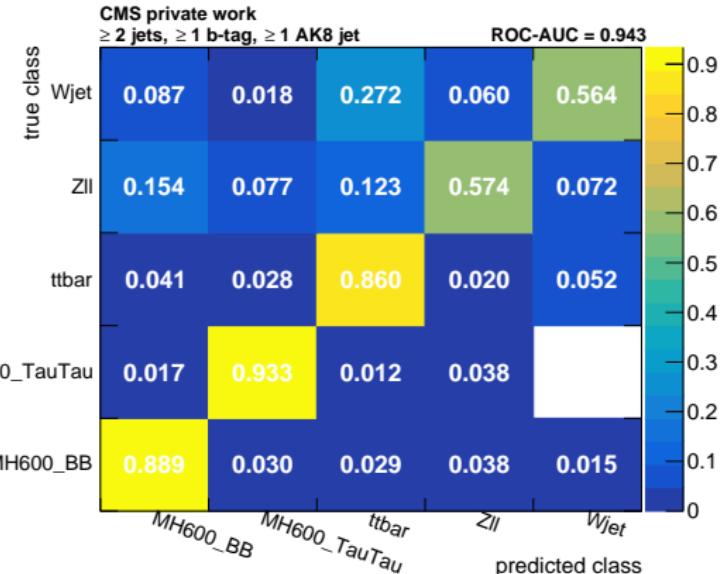


Figure: $m_H = 600$ GeV

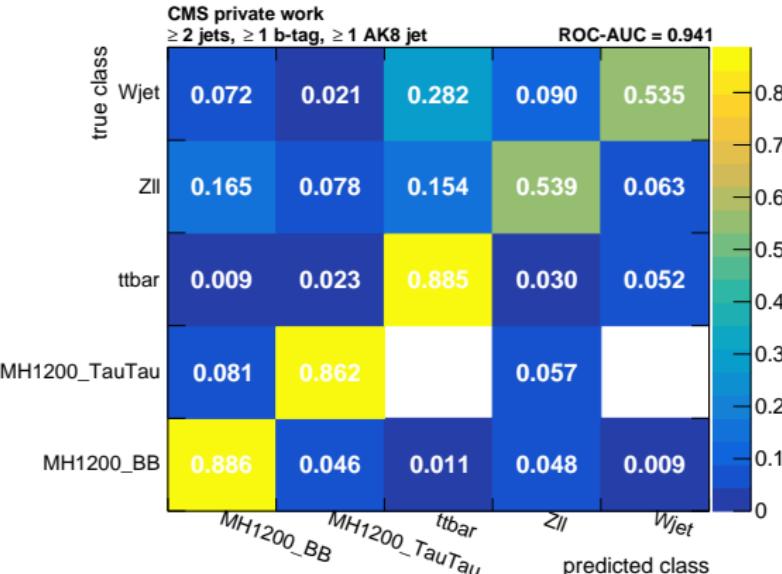


Figure: $m_H = 1200$ GeV

$\Delta R(\mu\tau_h; bb)$

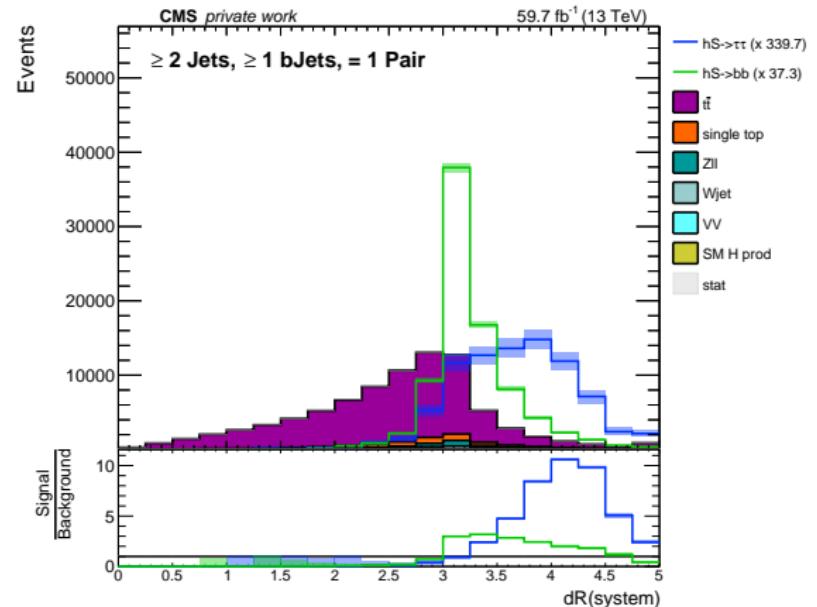
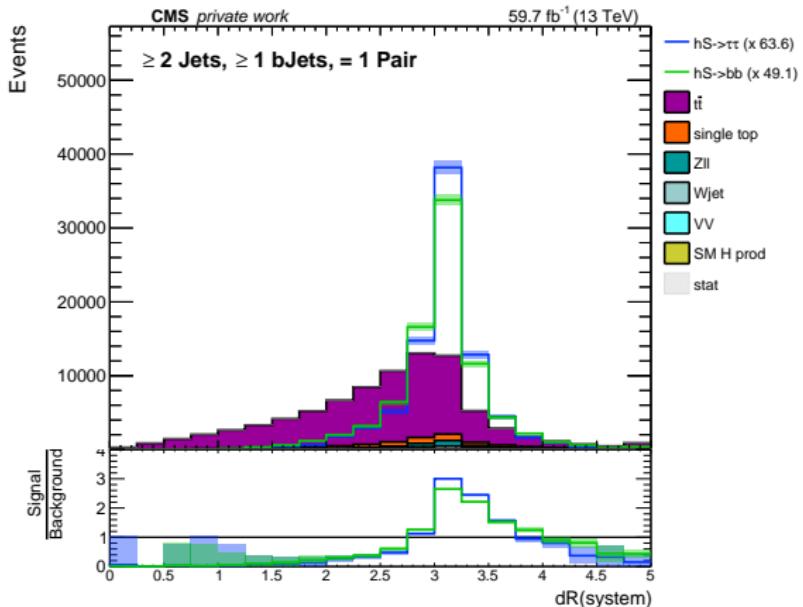


Figure: $m_H = 600 \text{ GeV}$

Figure: $m_H = 1200 \text{ GeV}$

Softdrop mass

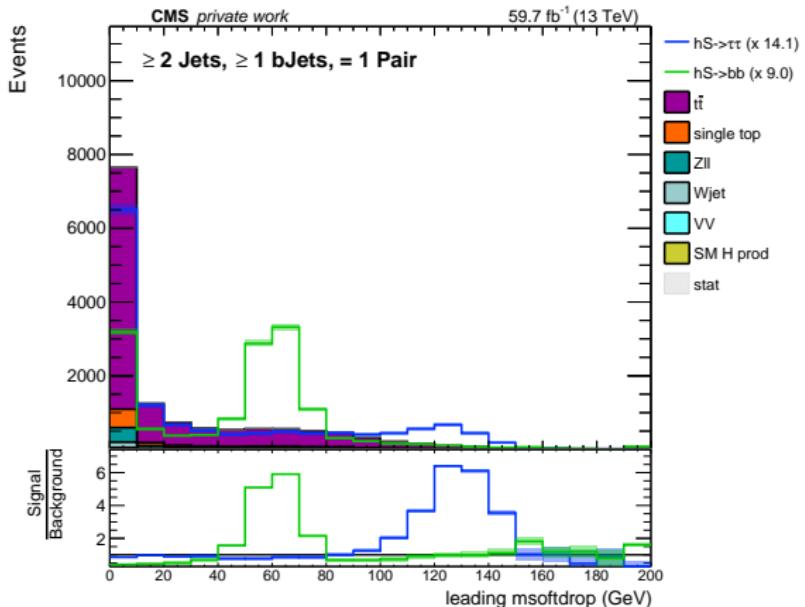


Figure: $m_H = 600 \text{ GeV}$

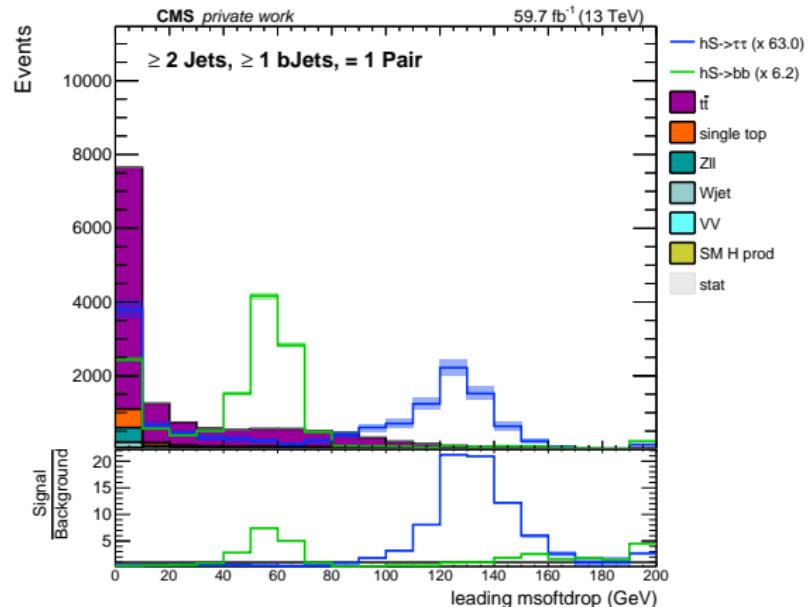


Figure: $m_H = 1200 \text{ GeV}$

QCD disc

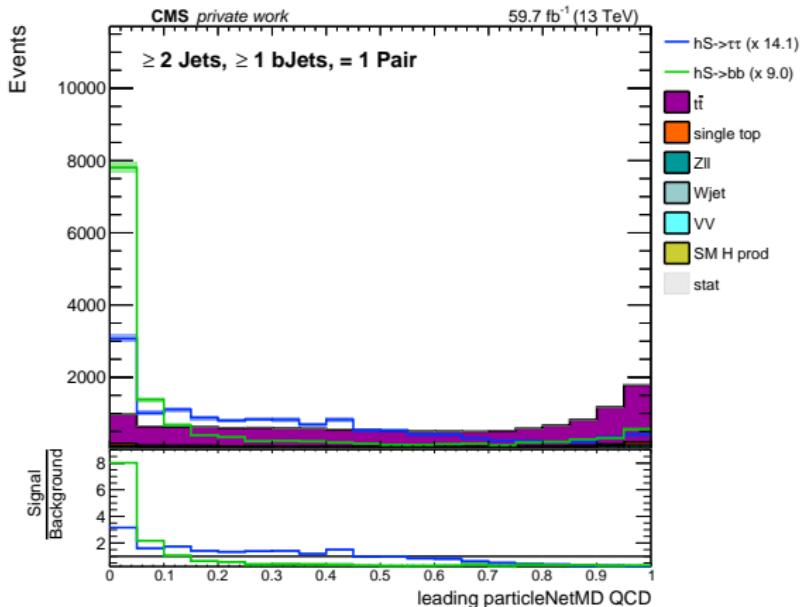


Figure: $m_H = 600 \text{ GeV}$

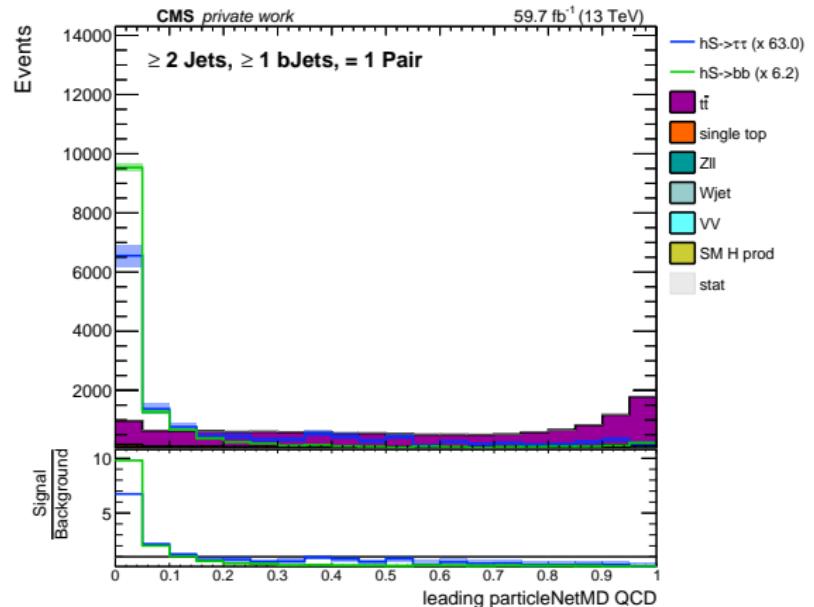


Figure: $m_H = 1200 \text{ GeV}$

X(bb) disc

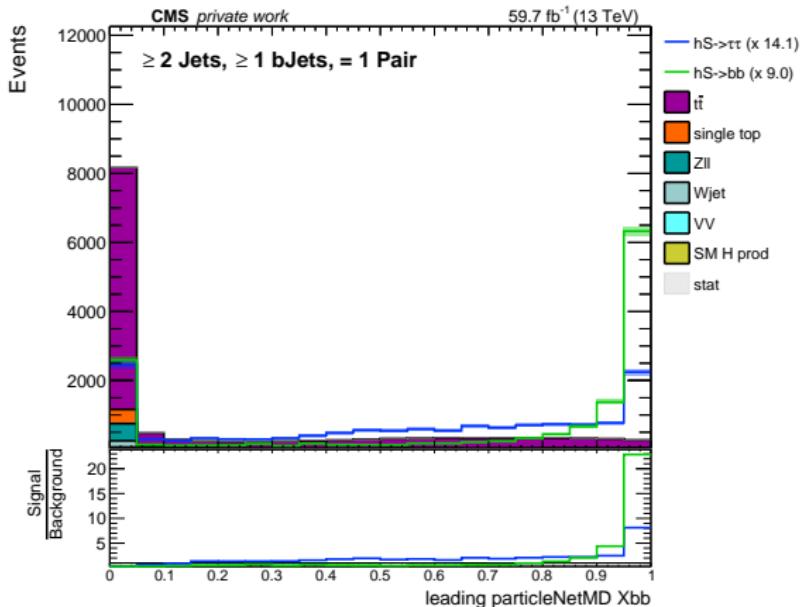


Figure: $m_H = 600 \text{ GeV}$

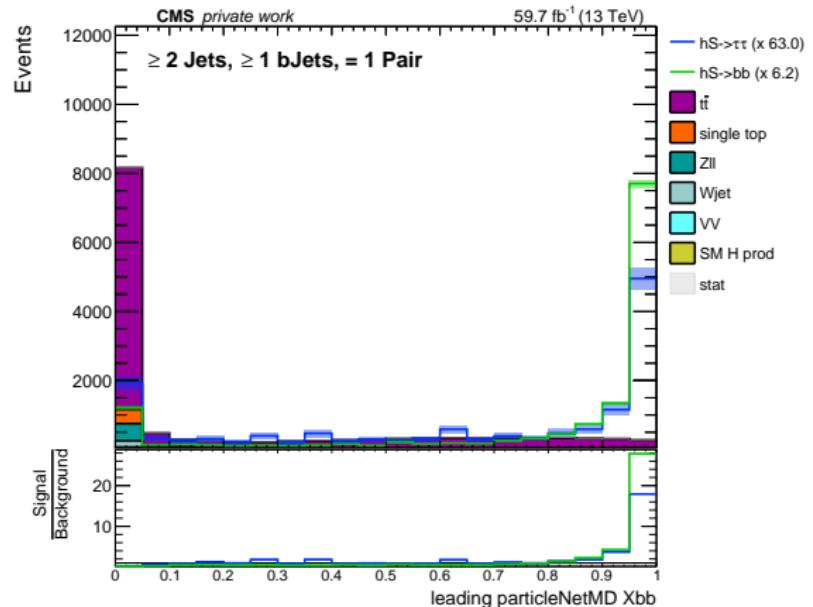
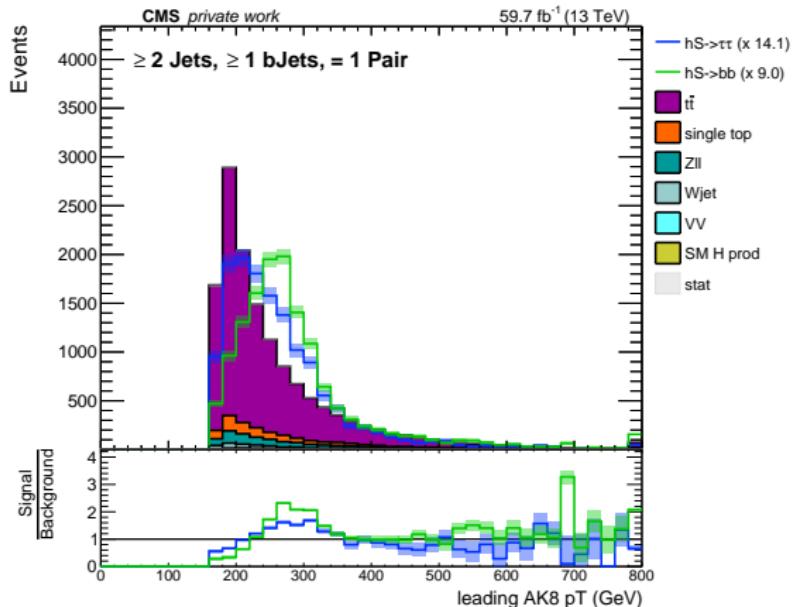
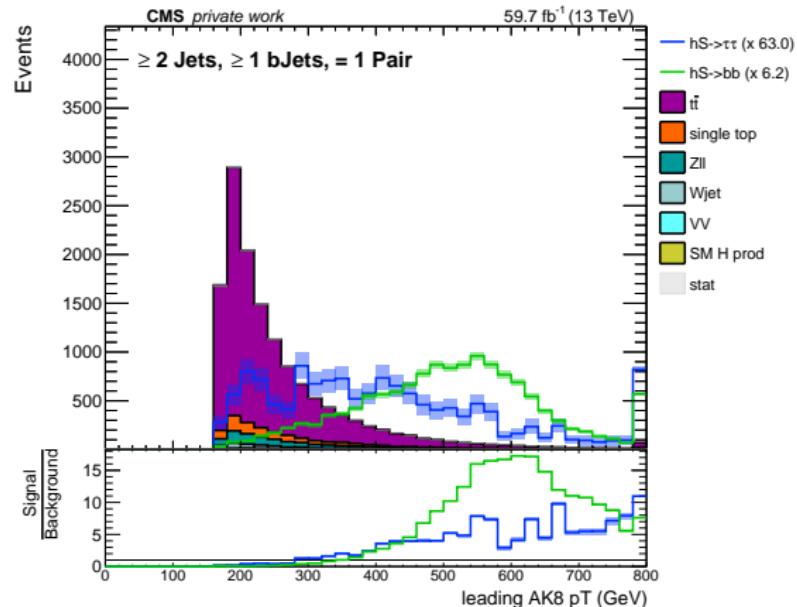
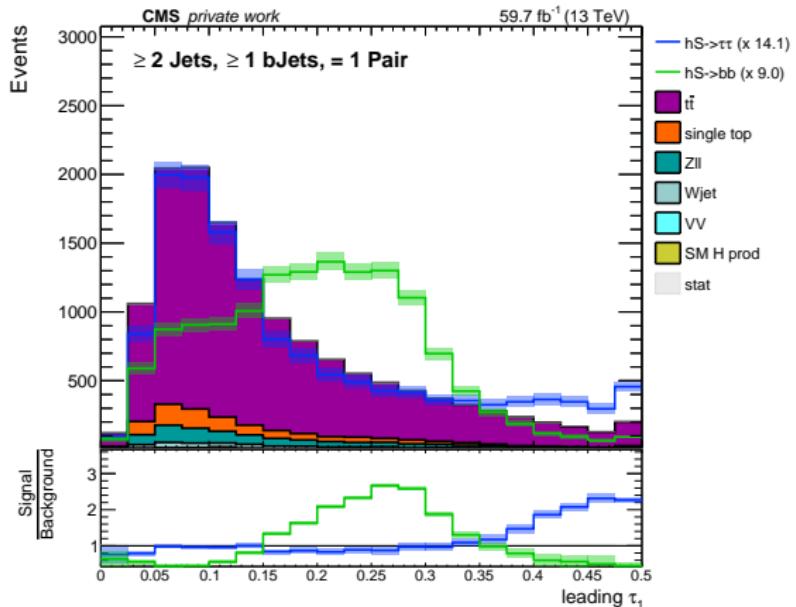
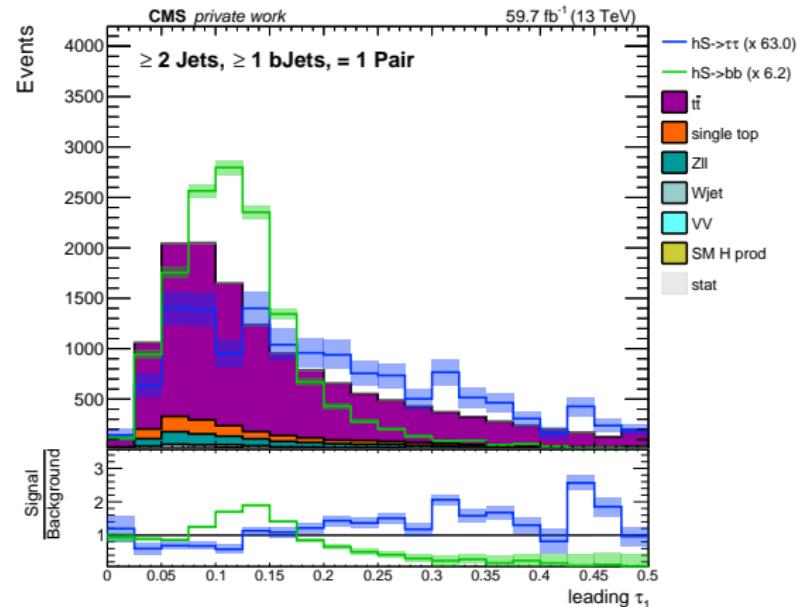
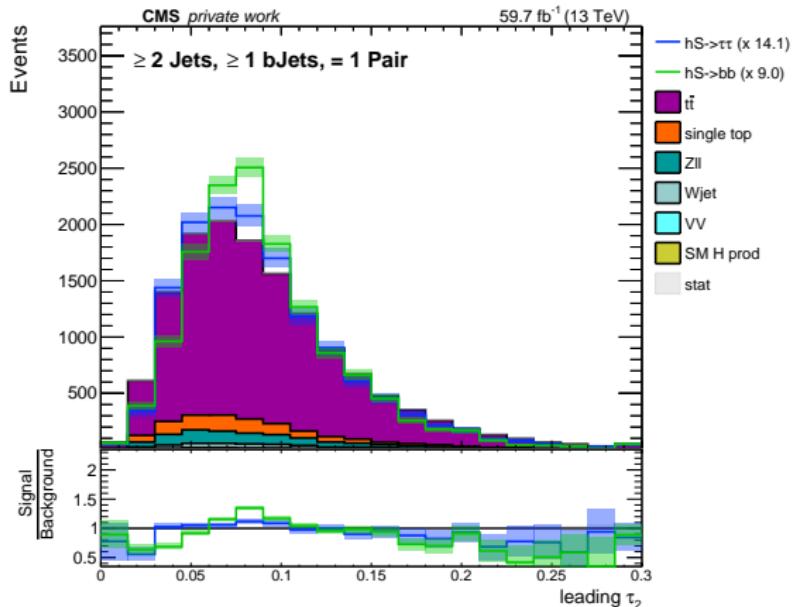
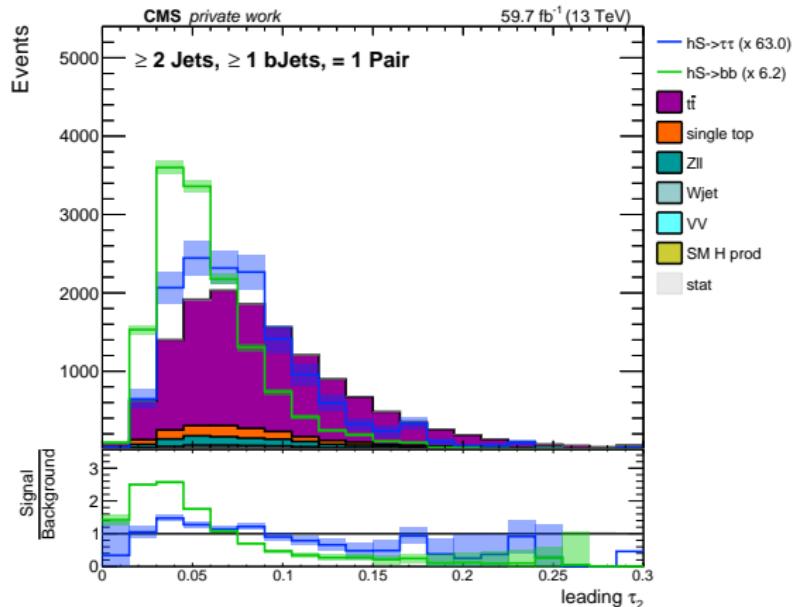
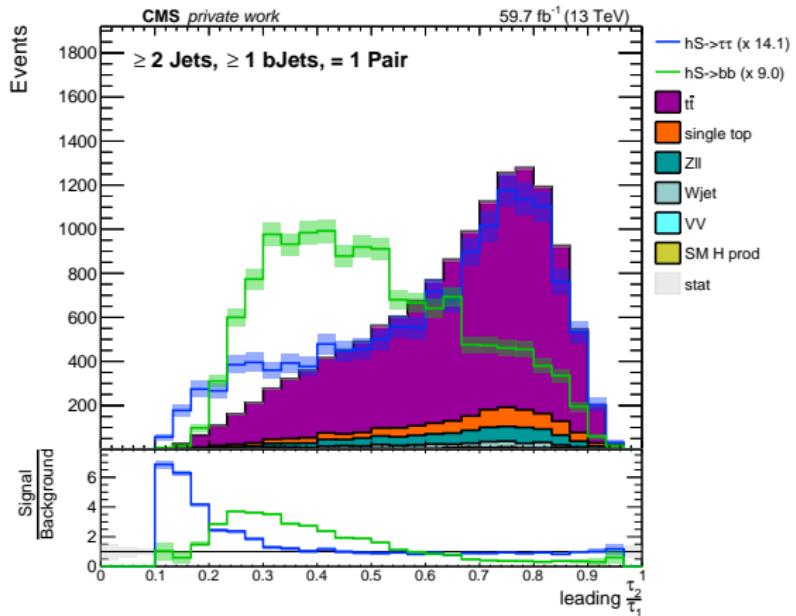
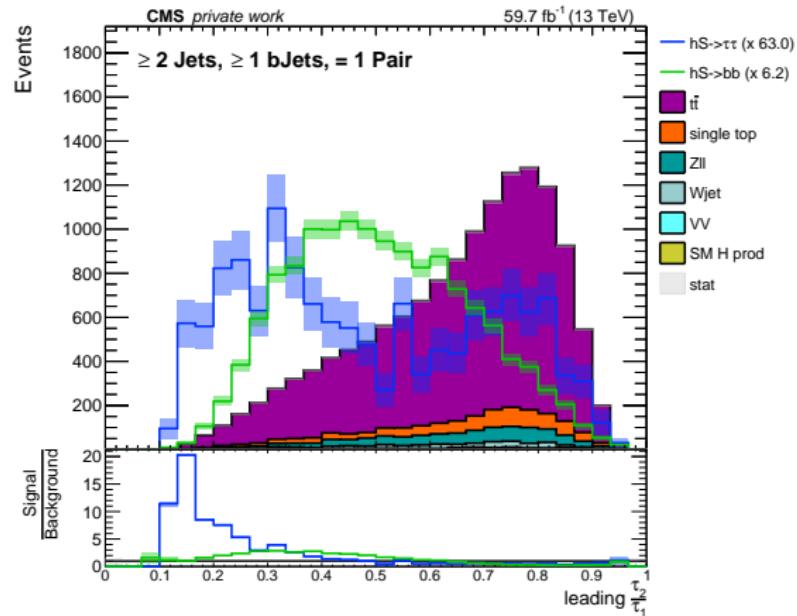


Figure: $m_H = 1200 \text{ GeV}$

Figure: $m_H = 600 \text{ GeV}$ Figure: $m_H = 1200 \text{ GeV}$

Figure: $m_H = 600 \text{ GeV}$ Figure: $m_H = 1200 \text{ GeV}$

τ_2 Figure: $m_H = 600 \text{ GeV}$ Figure: $m_H = 1200 \text{ GeV}$

τ_2/τ_1 Figure: $m_H = 600$ GeVFigure: $m_H = 1200$ GeV

Signal nodes baseline

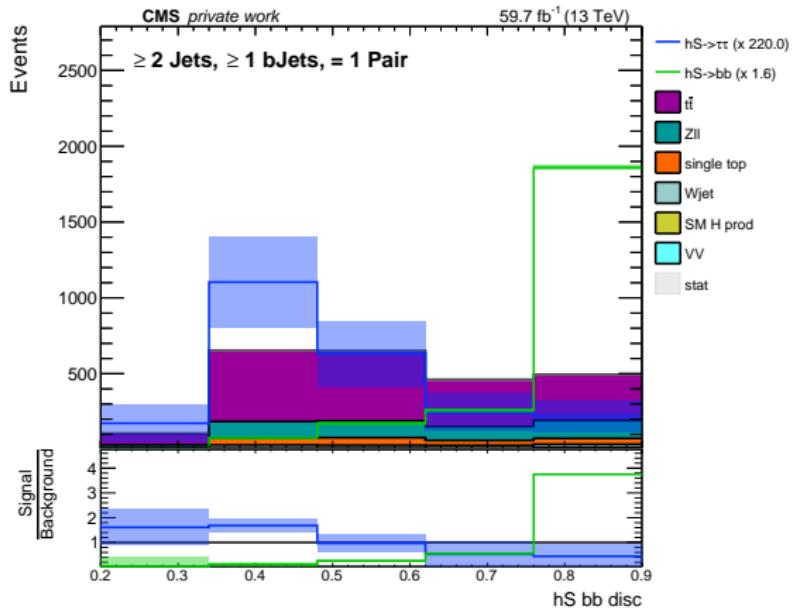


Figure: $m_H = 600 \text{ GeV}$

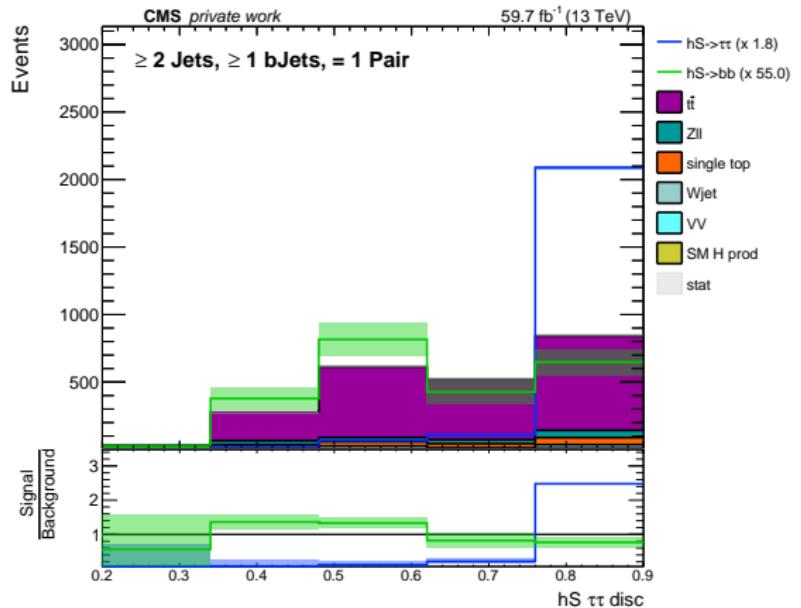


Figure: $m_H = 600 \text{ GeV}$

Background nodes baseline

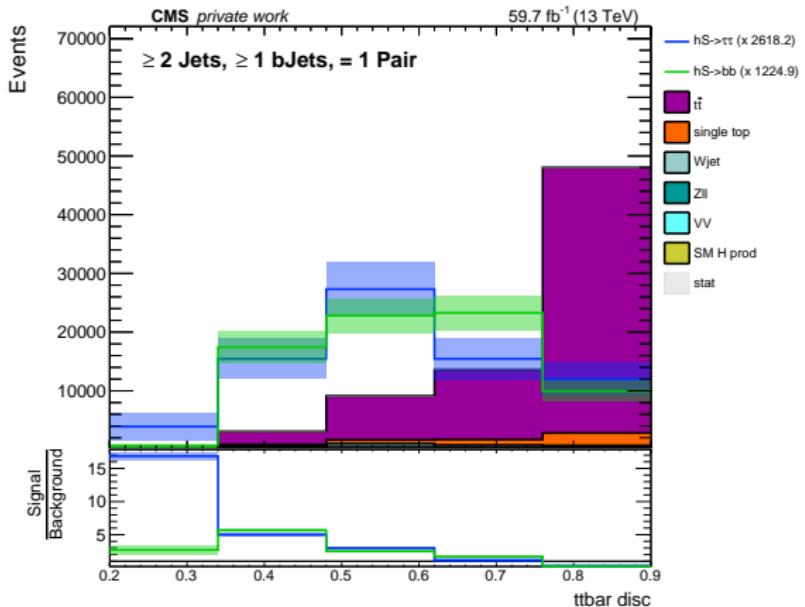


Figure: $m_H = 600 \text{ GeV}$

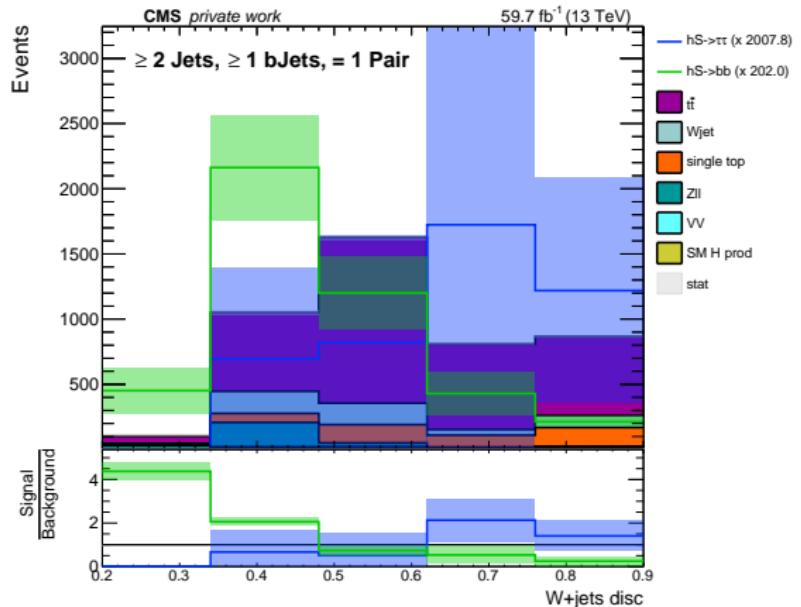


Figure: $m_H = 600 \text{ GeV}$

Background nodes baseline

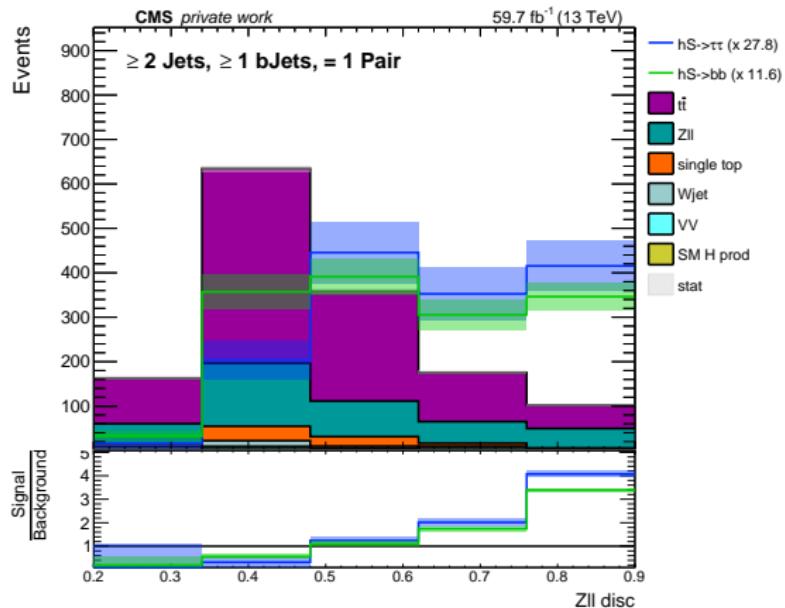


Figure: $m_H = 600 \text{ GeV}$

Signal nodes baseline

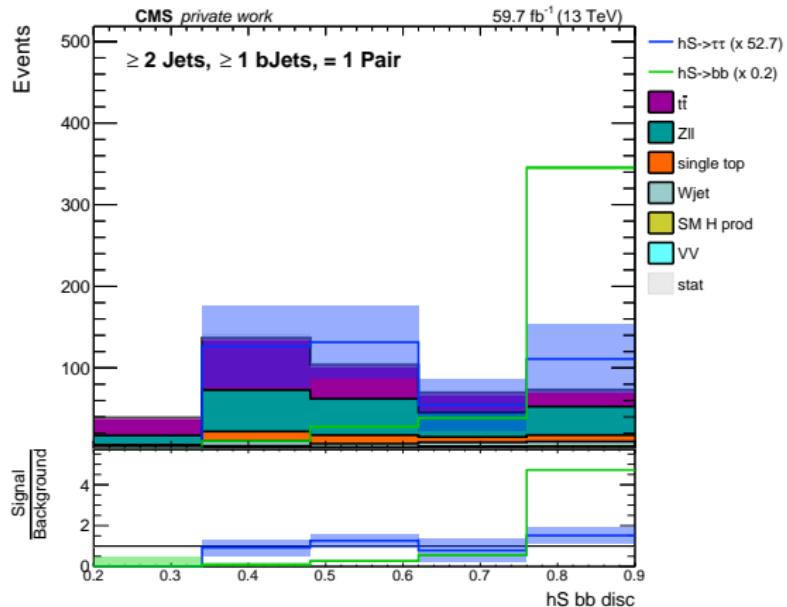


Figure: $m_H = 1200 \text{ GeV}$

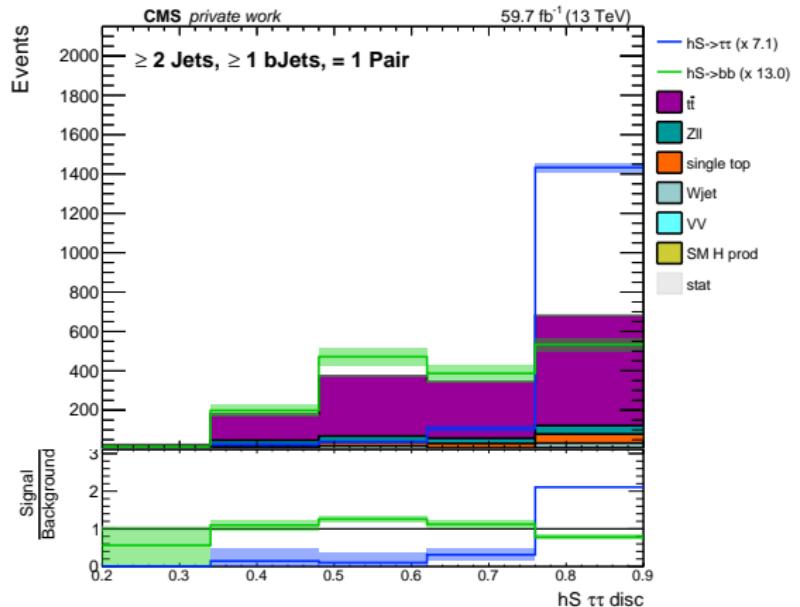


Figure: $m_H = 1200 \text{ GeV}$

Background nodes baseline

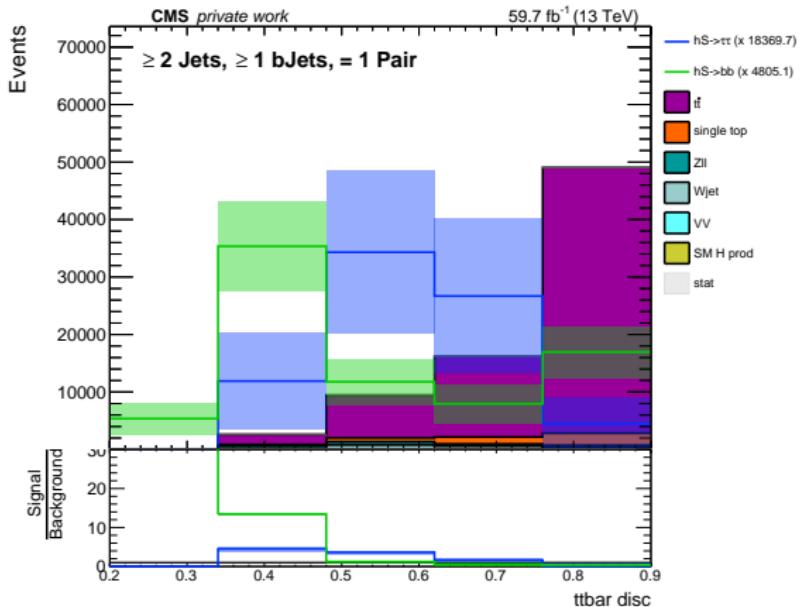


Figure: $m_H = 1200 \text{ GeV}$

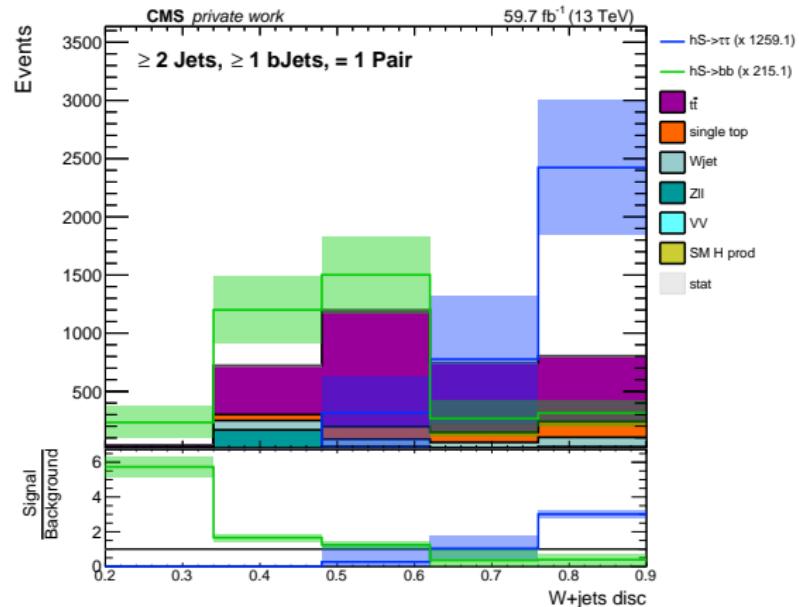


Figure: $m_H = 1200 \text{ GeV}$

Background nodes baseline

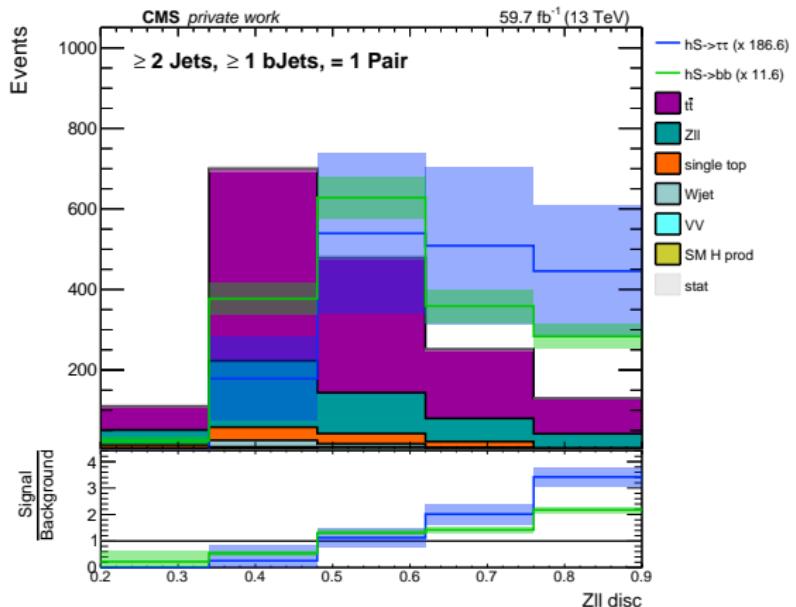


Figure: $m_H = 1200 \text{ GeV}$

Signal nodes add. vars

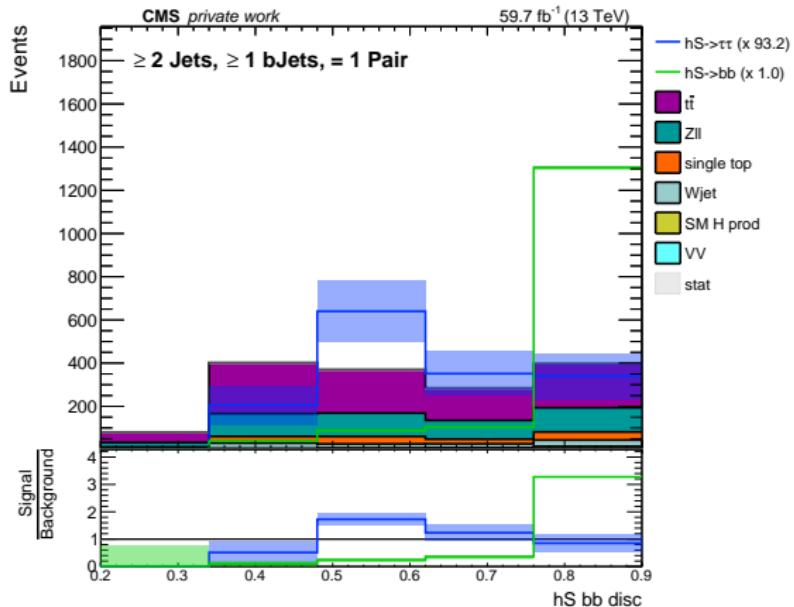


Figure: $m_H = 600 \text{ GeV}$

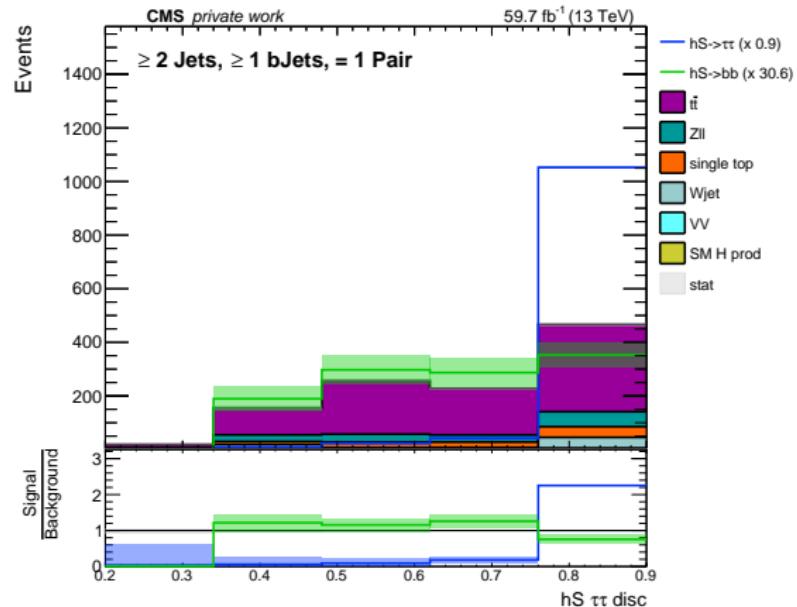


Figure: $m_H = 600 \text{ GeV}$

Background nodes add. vars

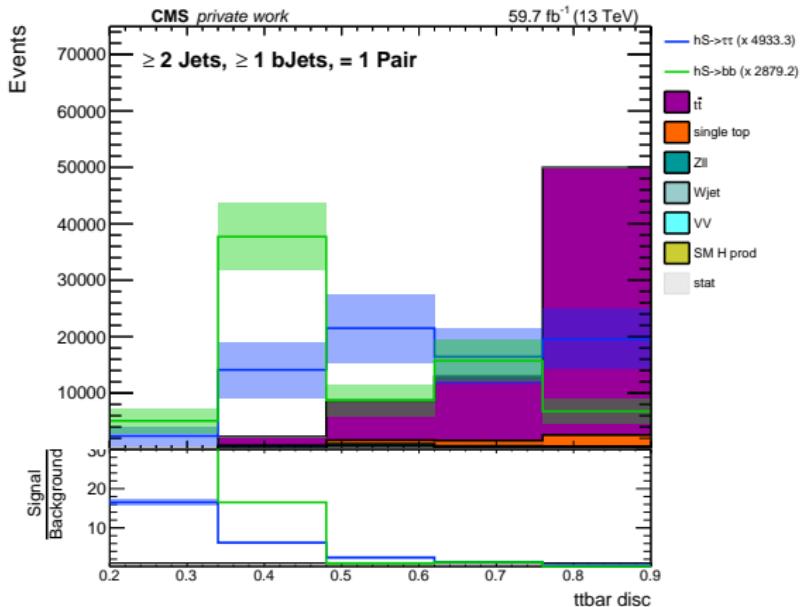


Figure: $m_H = 600 \text{ GeV}$

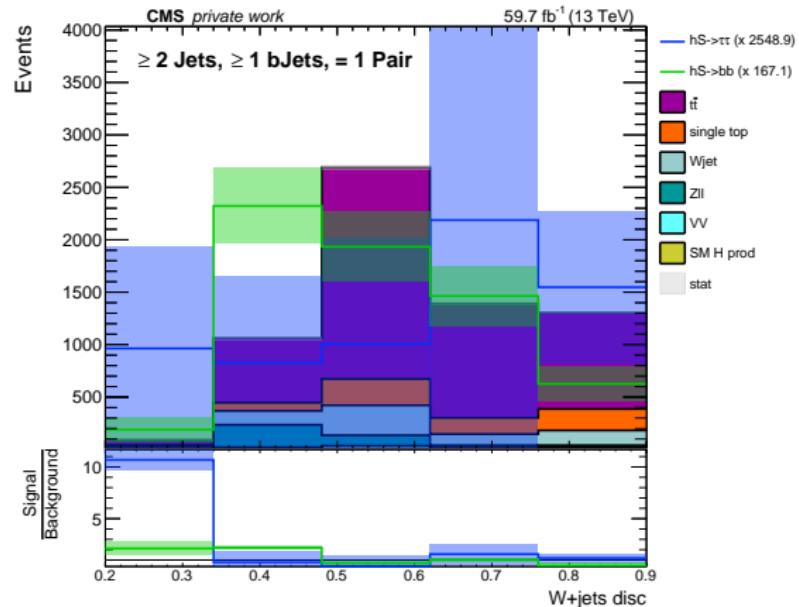


Figure: $m_H = 600 \text{ GeV}$

Background nodes add. vars

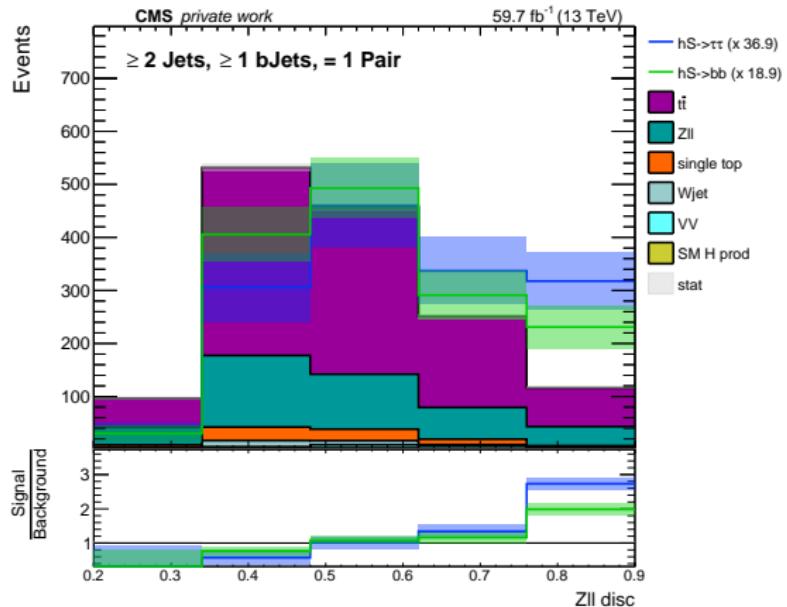


Figure: $m_H = 600 \text{ GeV}$

Signal nodes add. vars

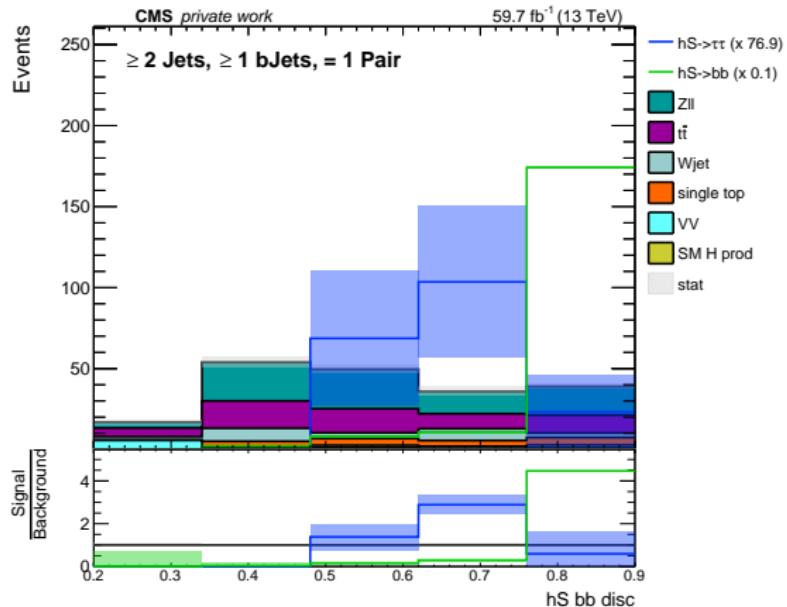


Figure: $m_H = 1200 \text{ GeV}$

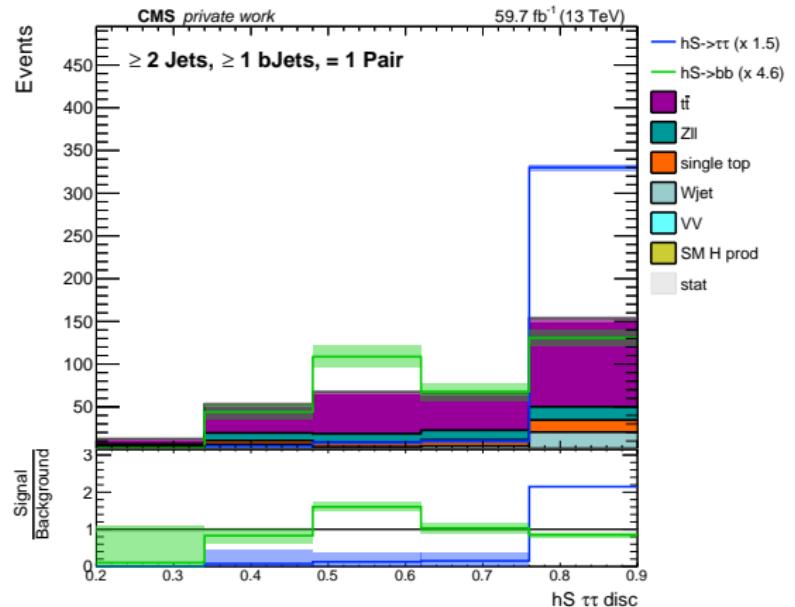


Figure: $m_H = 1200 \text{ GeV}$

Background nodes add. vars

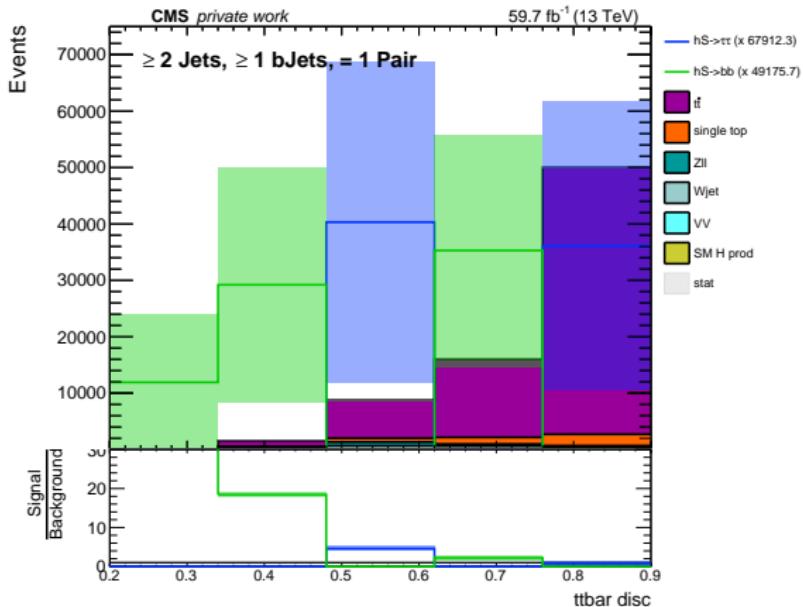


Figure: $m_H = 1200 \text{ GeV}$

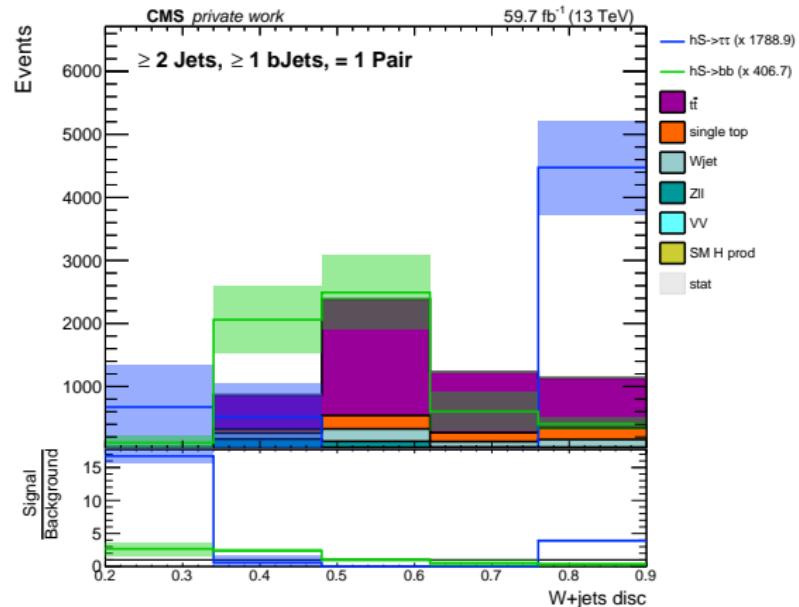


Figure: $m_H = 1200 \text{ GeV}$

Background nodes add. vars

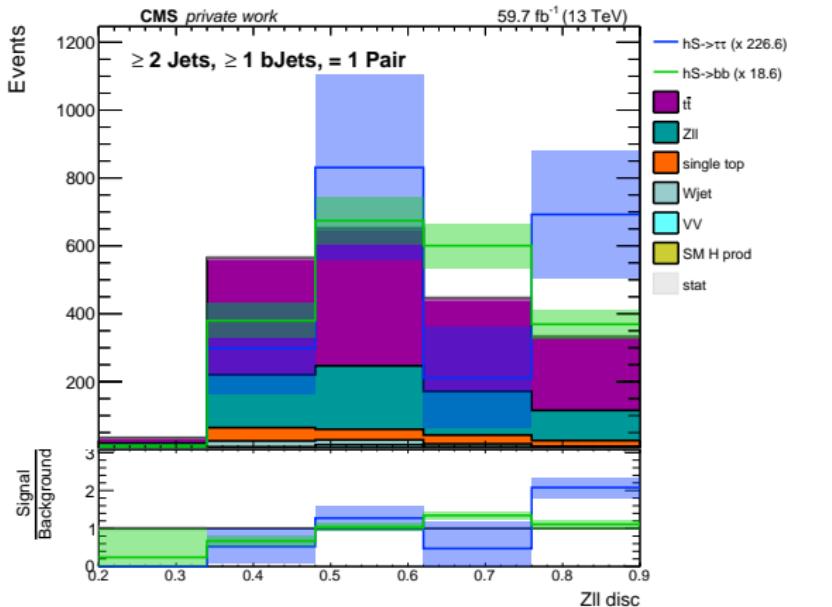


Figure: $m_H = 1200 \text{ GeV}$

Signal nodes split

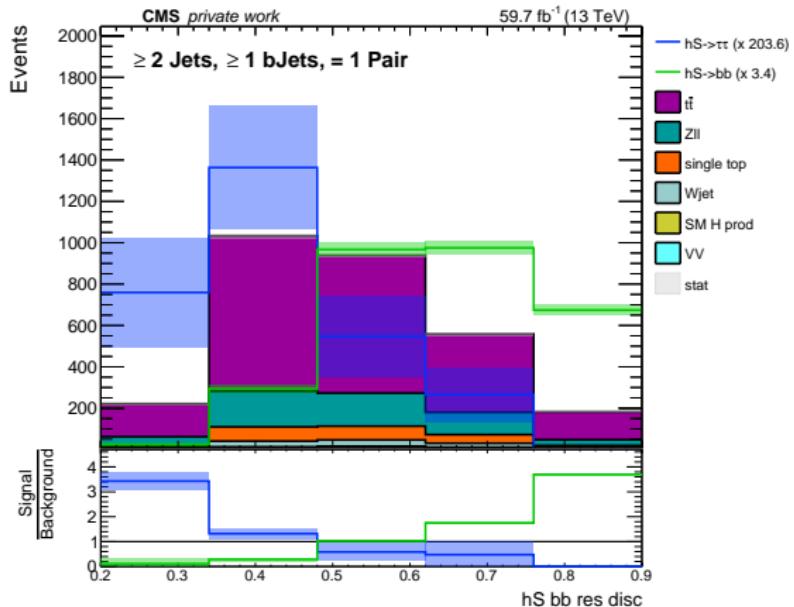


Figure: $m_H = 600 \text{ GeV}$

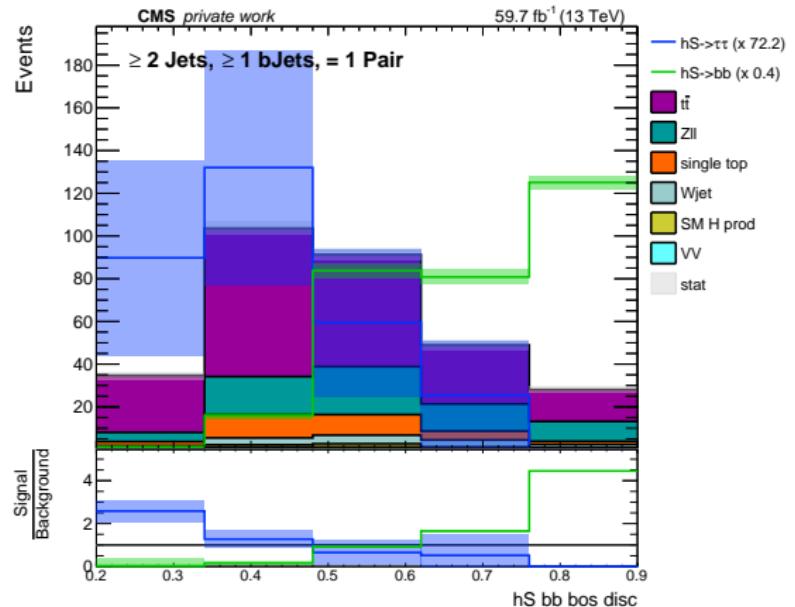


Figure: $m_H = 600 \text{ GeV}$

Signal nodes split

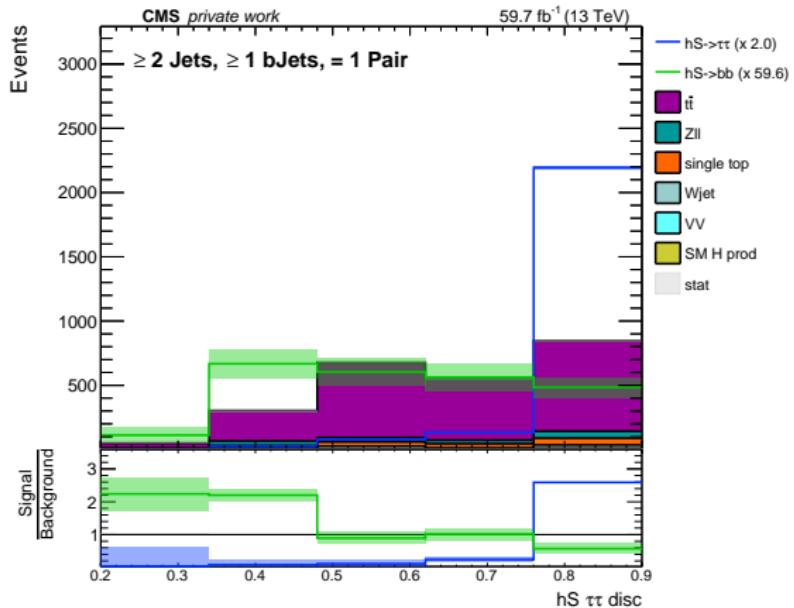


Figure: $m_H = 600 \text{ GeV}$

Background nodes split

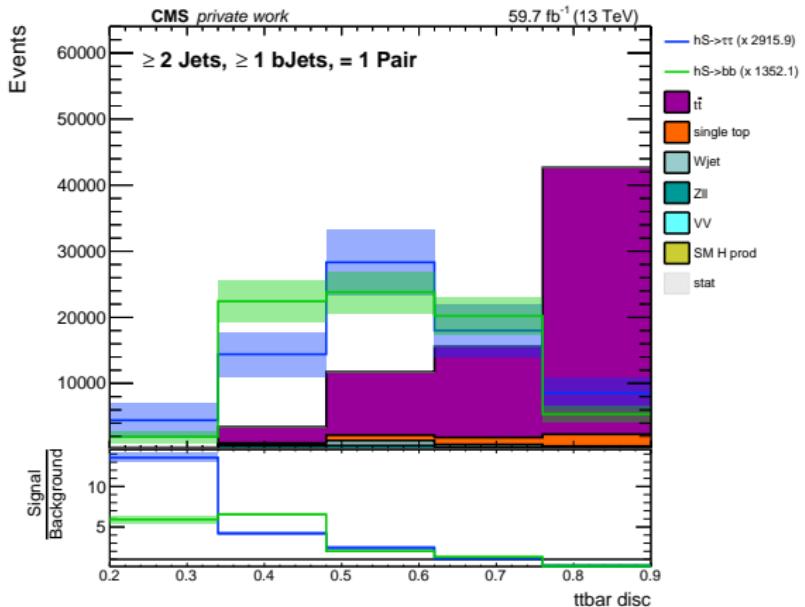


Figure: $m_H = 600 \text{ GeV}$

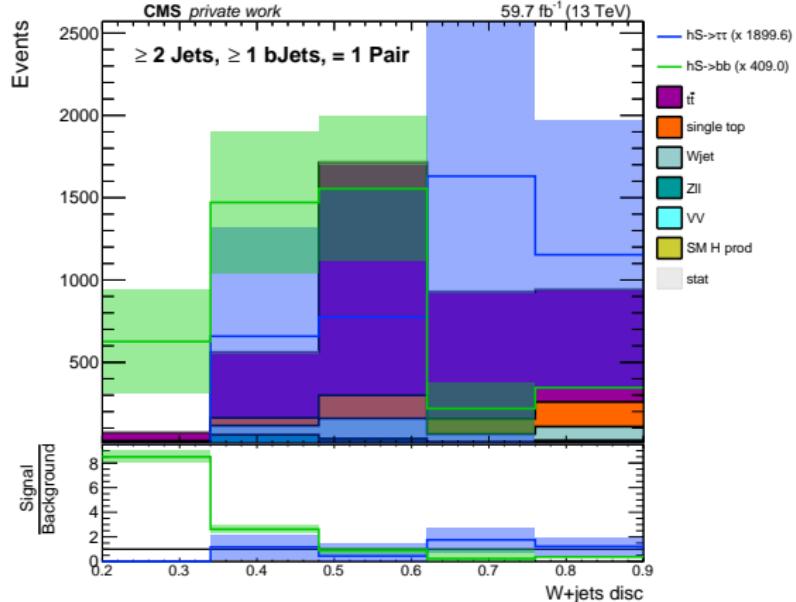


Figure: $m_H = 600 \text{ GeV}$

Background nodes split

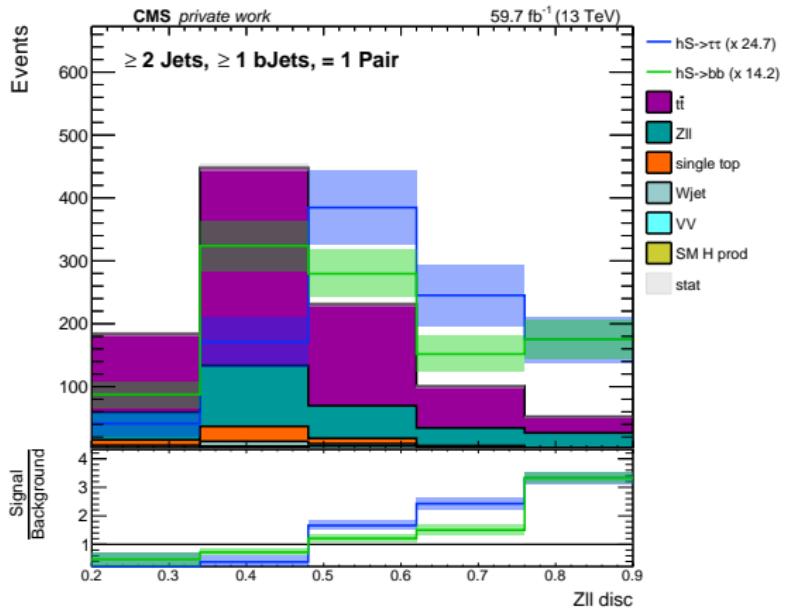


Figure: $m_H = 600 \text{ GeV}$

Signal nodes split

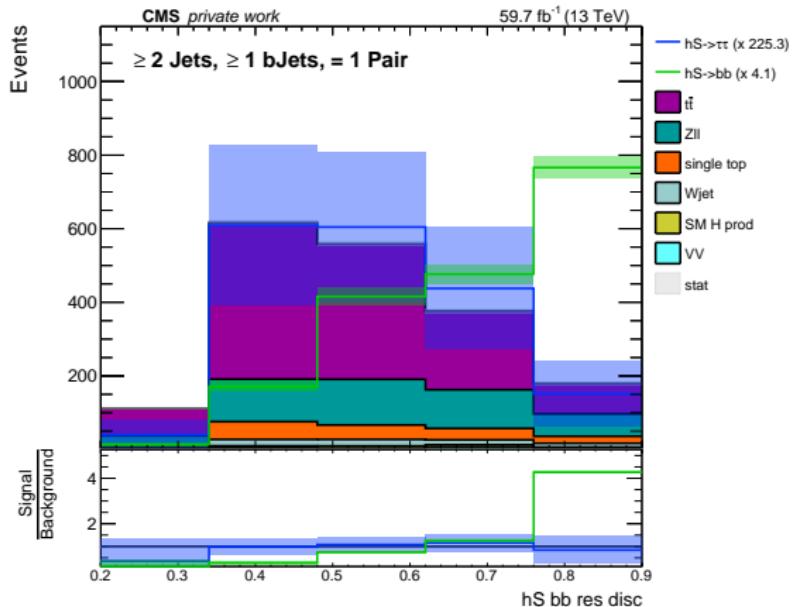


Figure: $m_H = 1200 \text{ GeV}$

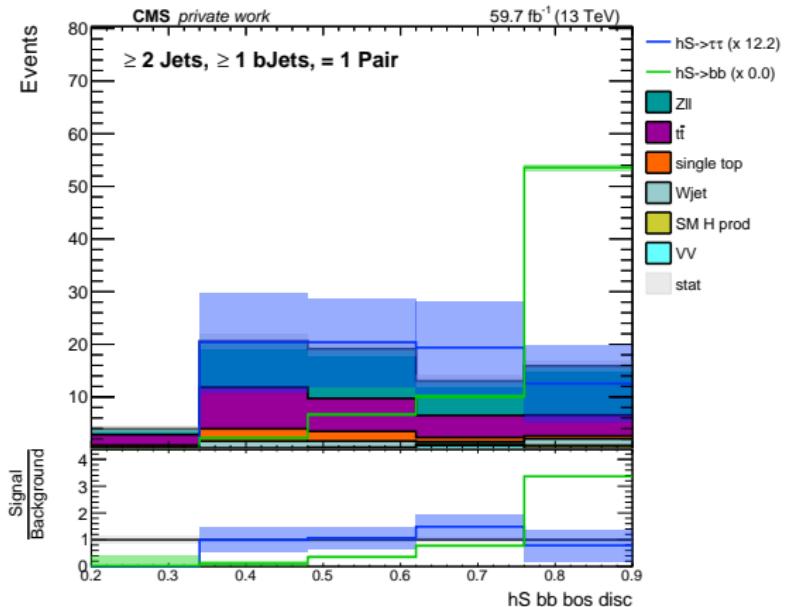


Figure: $m_H = 1200 \text{ GeV}$

Signal nodes split

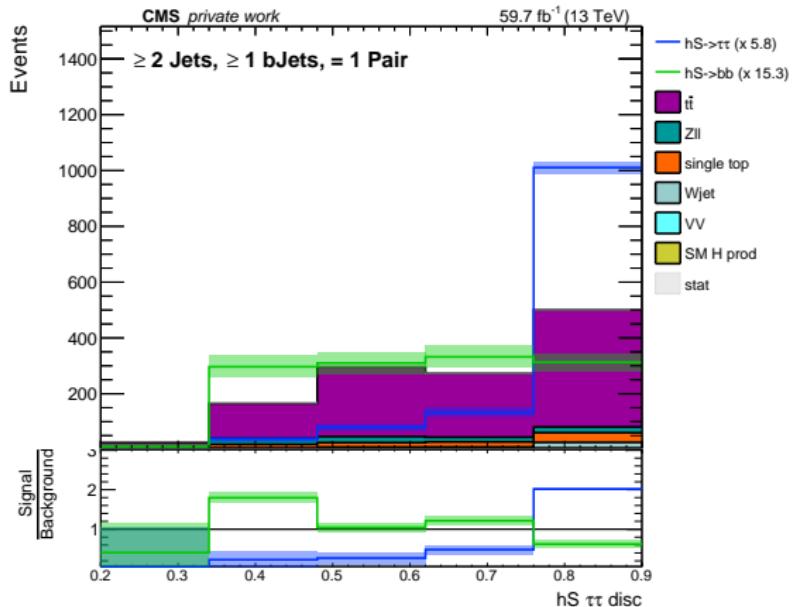


Figure: $m_H = 1200 \text{ GeV}$

Background nodes split

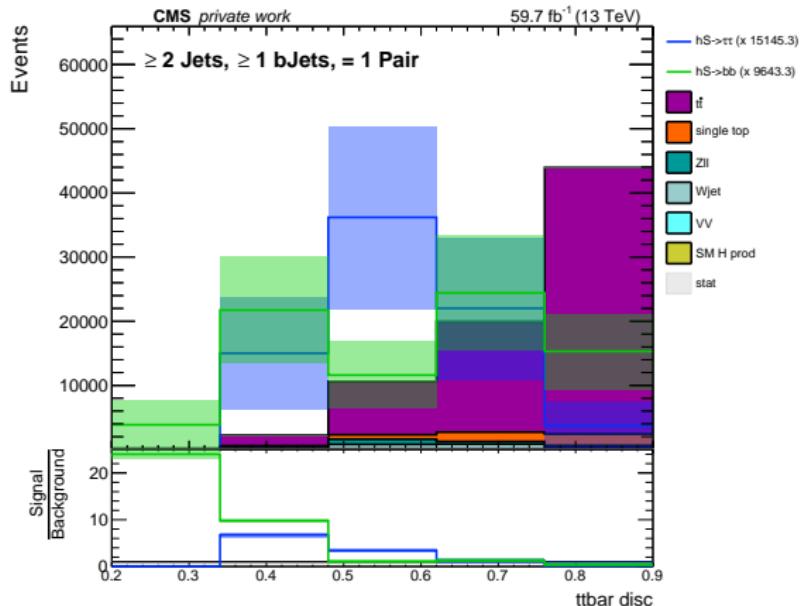


Figure: $m_H = 1200 \text{ GeV}$

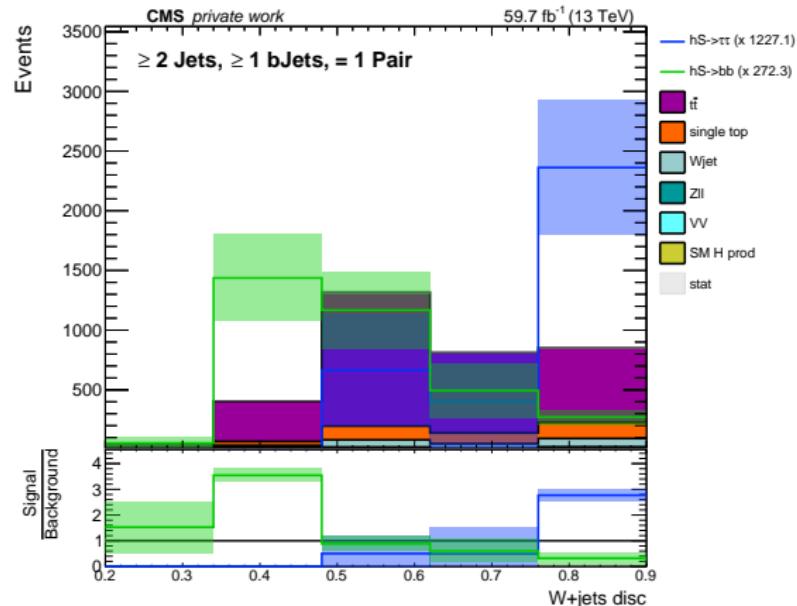


Figure: $m_H = 1200 \text{ GeV}$

Background nodes split

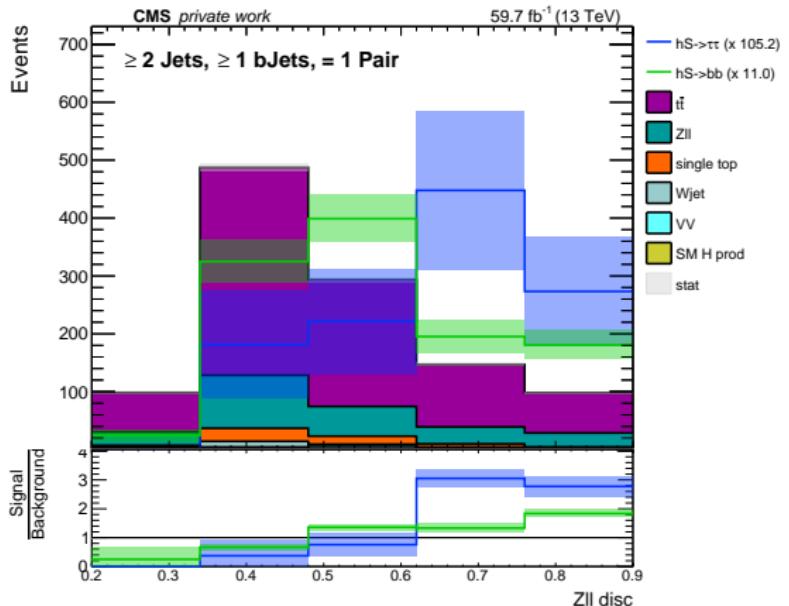


Figure: $m_H = 1200 \text{ GeV}$

Signal nodes cut

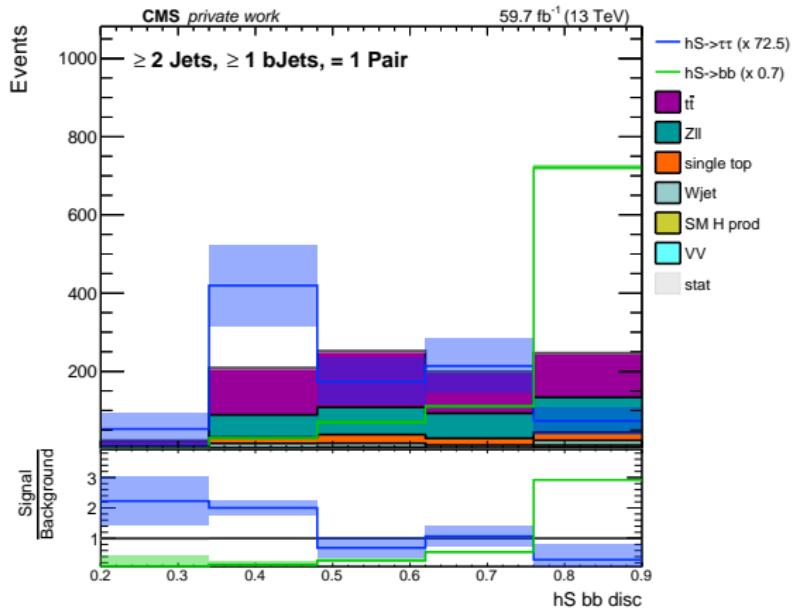


Figure: $m_H = 600 \text{ GeV}$

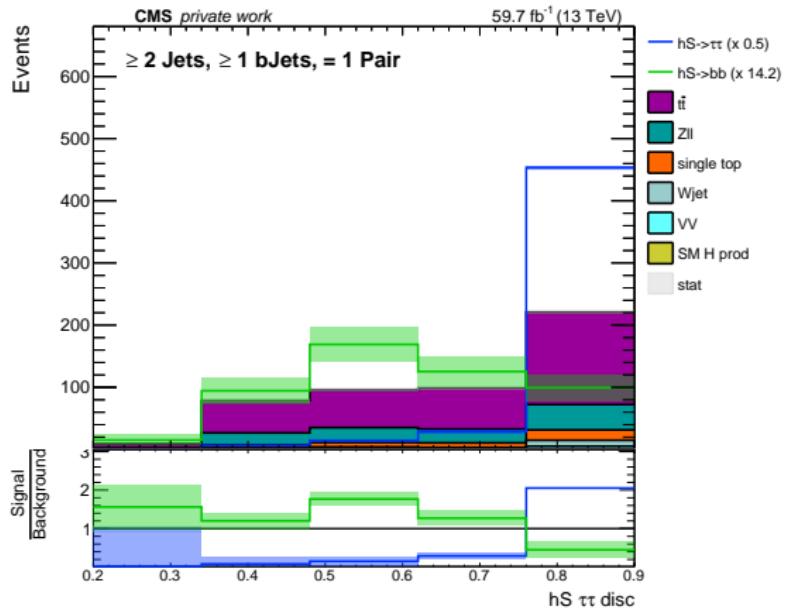


Figure: $m_H = 600 \text{ GeV}$

Background nodes cut

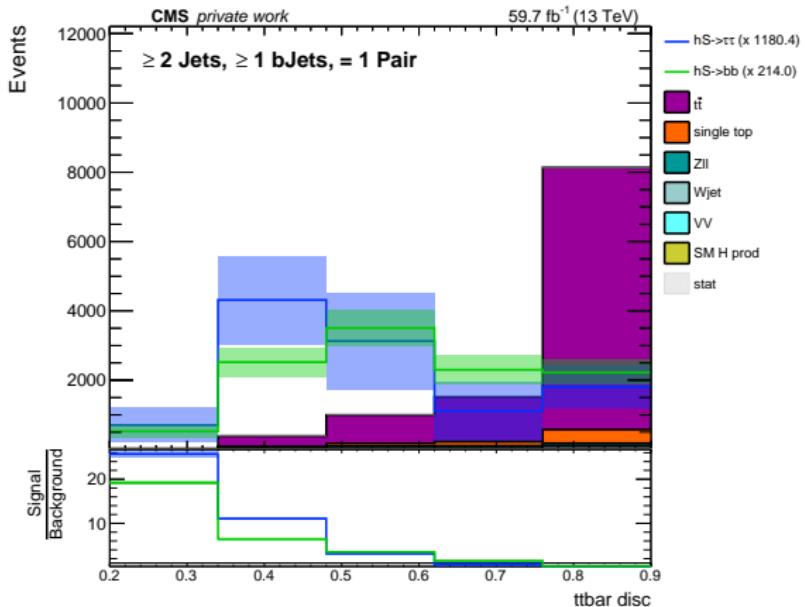


Figure: $m_H = 600 \text{ GeV}$

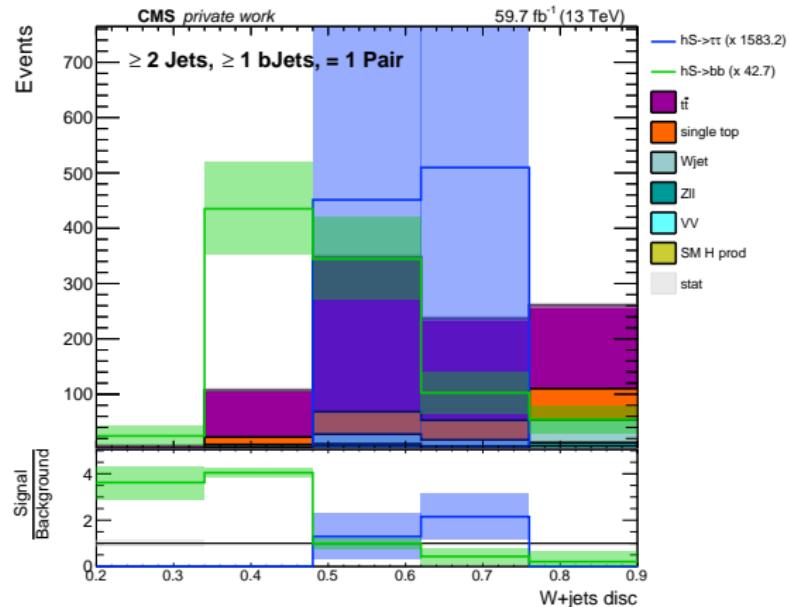


Figure: $m_H = 600 \text{ GeV}$

Background nodes cut

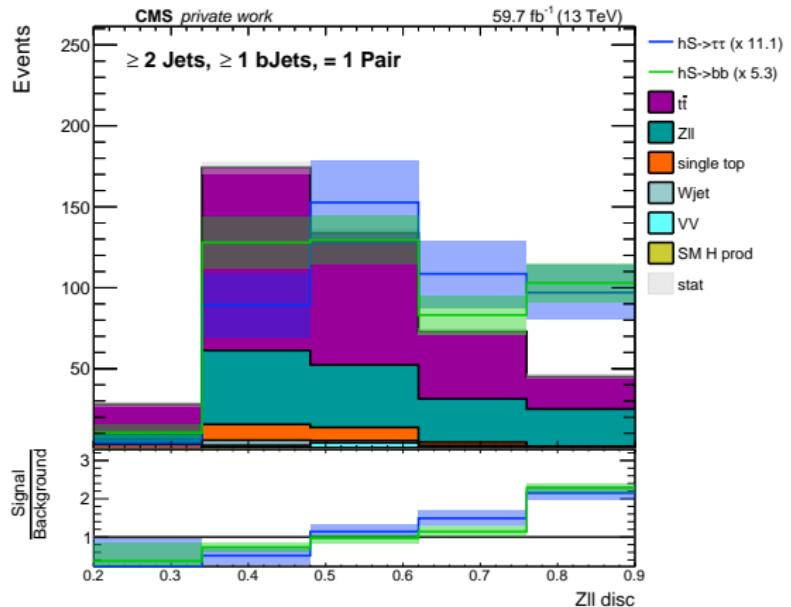


Figure: $m_H = 600 \text{ GeV}$

Signal nodes cut

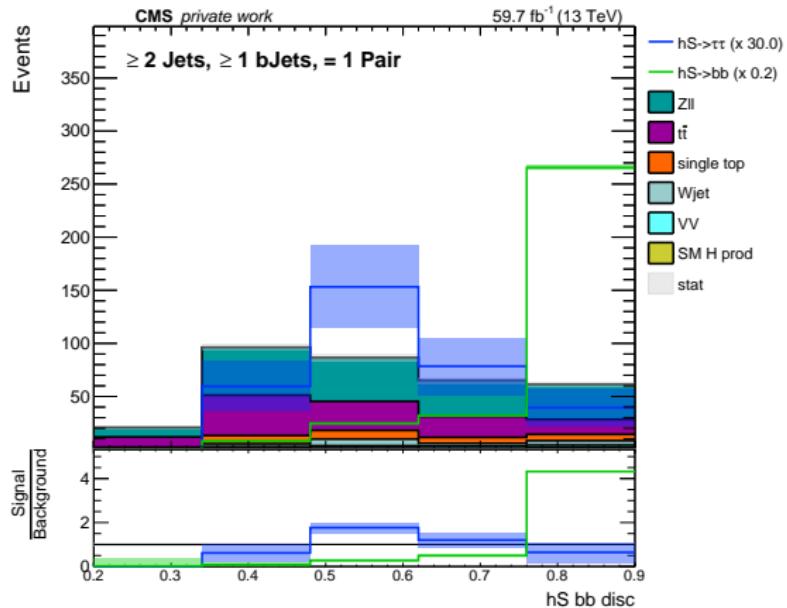


Figure: $m_H = 1200 \text{ GeV}$

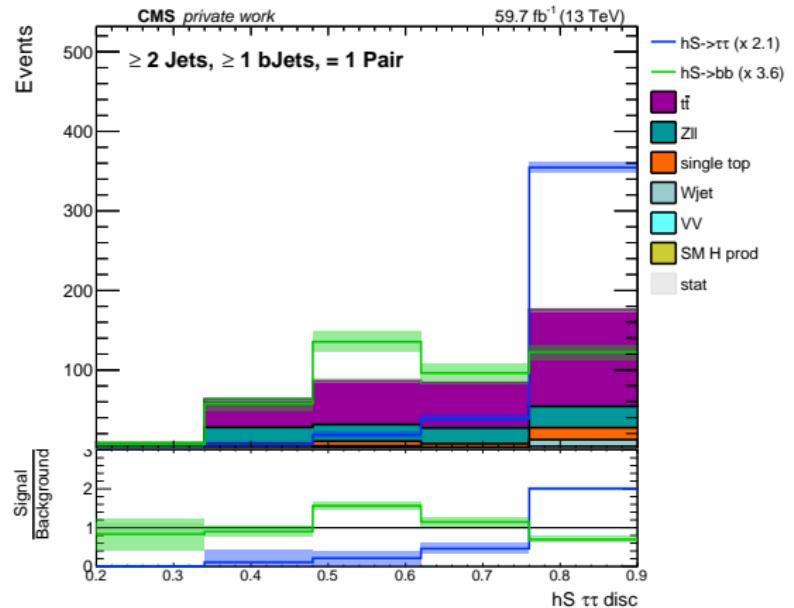


Figure: $m_H = 1200 \text{ GeV}$

Background nodes cut

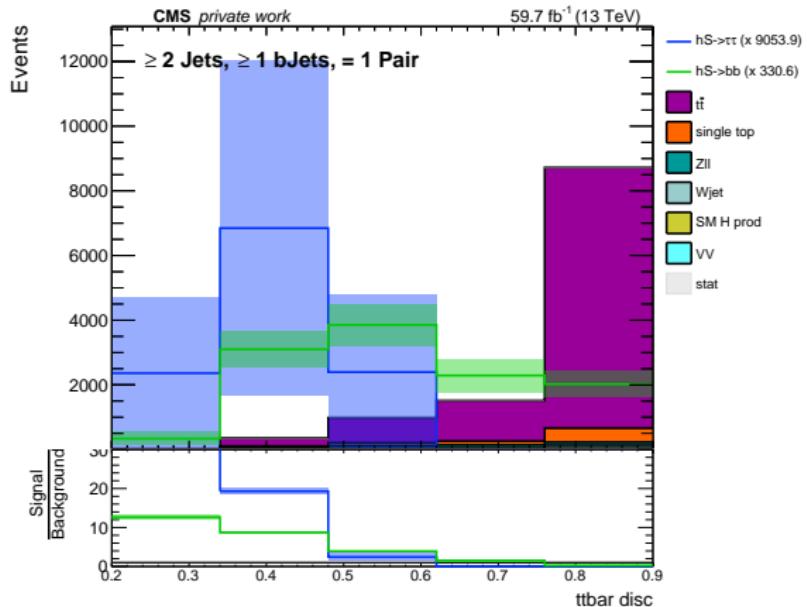


Figure: $m_H = 1200 \text{ GeV}$

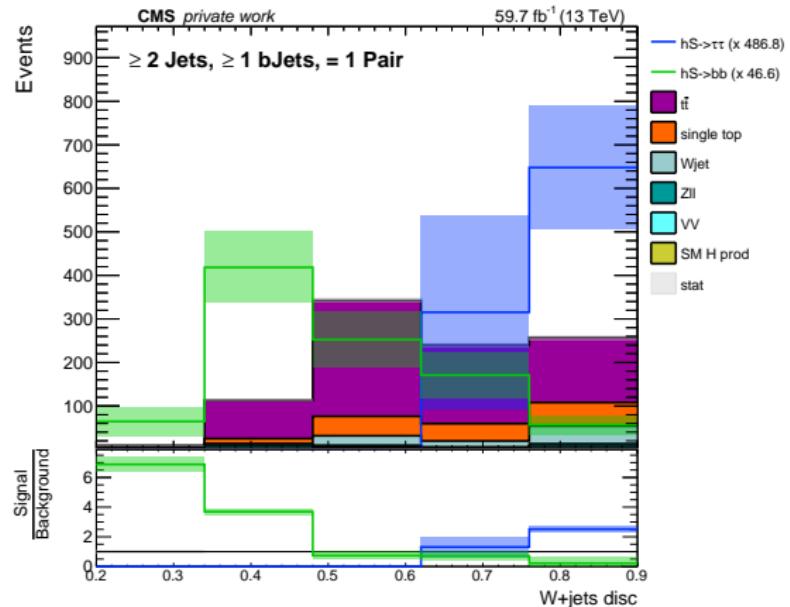


Figure: $m_H = 1200 \text{ GeV}$

Background nodes cut

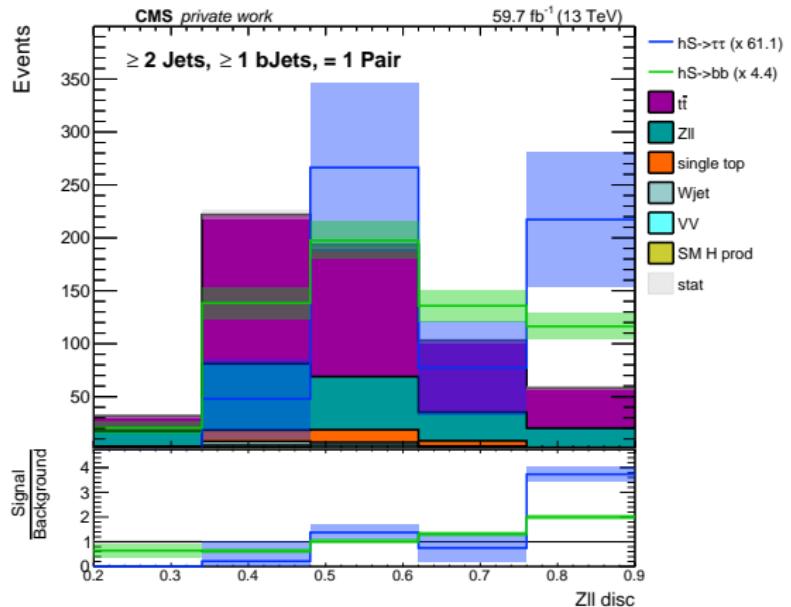


Figure: $m_H = 1200 \text{ GeV}$

Improvements

Table: Improvements on the upper limit on $\sigma B(H \rightarrow h h_S \rightarrow \tau\tau + bb)$ for each approach for a dedicated boosted topology description.

Changes	Average [%]	m_H [GeV]	Maximal [%]	m_H [GeV]	Minimal [%]
Feat.	29.83	1200	37.50	600	22.40
Split	26.17	1200	34.82	600	9.74
N_{AK8}	13.38	600	22.40	1200	0.00
Feat.+Split	47.49	1000	58.28	600	31.81
Feat.+ N_{AK8}	37.73	700	40.15	1200	34.82
Split+ N_{AK8}	34.50	900	39.00	600	28.57
Feat.+Split+ N_{AK8}	50.12	1000	58.28	600	38.31

Best fit

- s+b Asimov toy
- example best fit using only specific output nodes
- $m_H = 600 \text{ GeV}$; $m_{h_S} = 60 \text{ GeV}$
- background nodes have only a small impact
- ZII node also sensitive on signal due to signal migration

CMS simulation work in progress

baseline NN

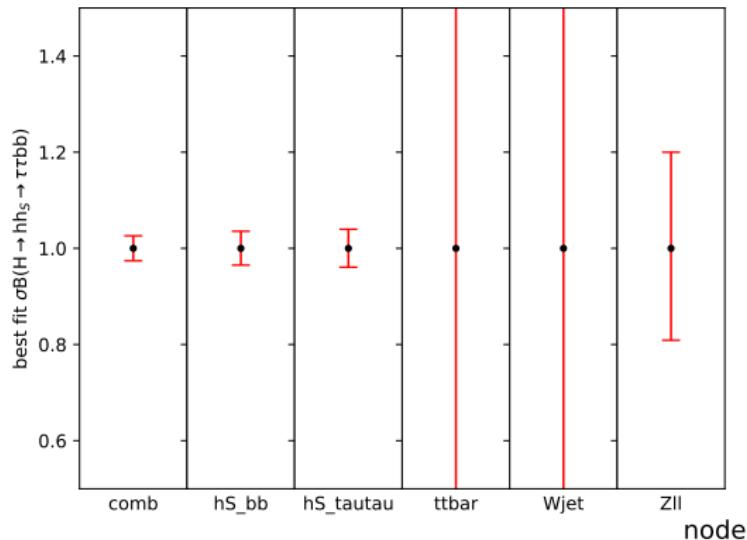
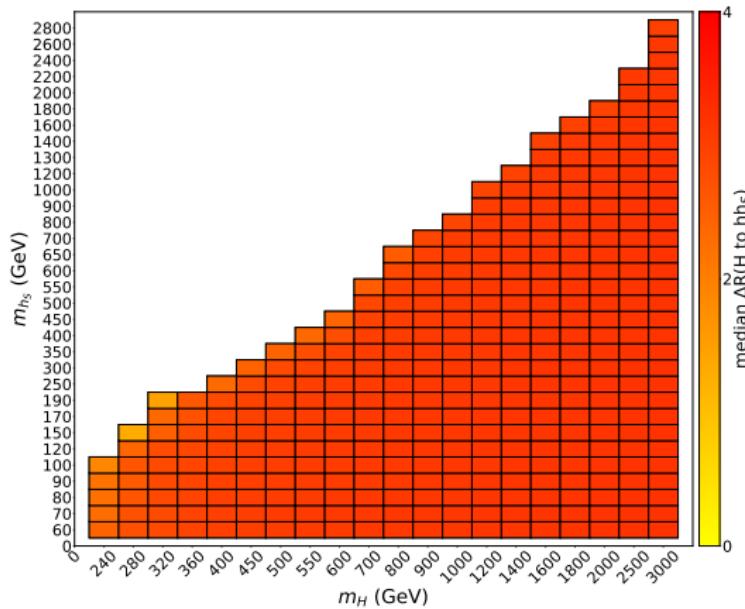


Figure: Statistical uncertainties only

Event signature

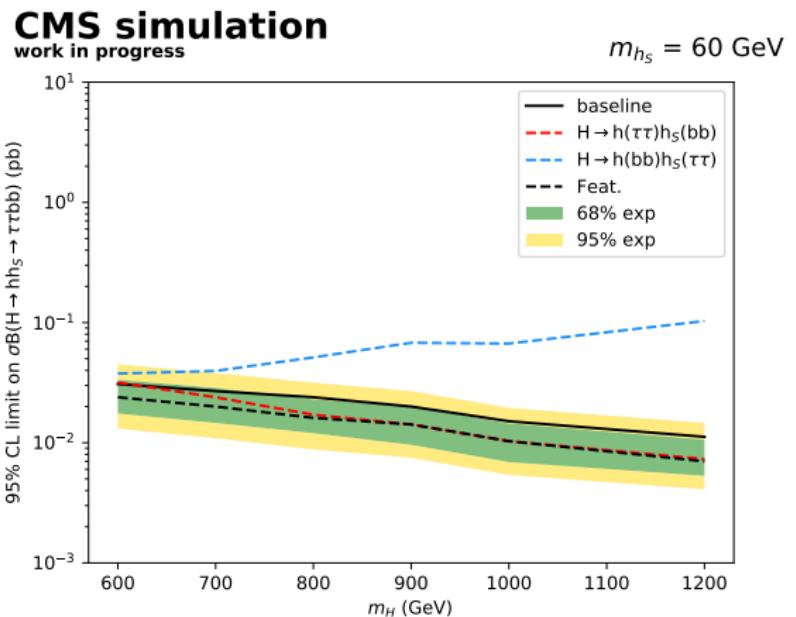
- Studied the event signature
- Spacial distance between the two lighter Higgs bosons
- Back-to-back decay regardless of hypothesis
- Characterizing feature for signal events

CMS simulation
work in progress



Expected upper limit: Additional input features

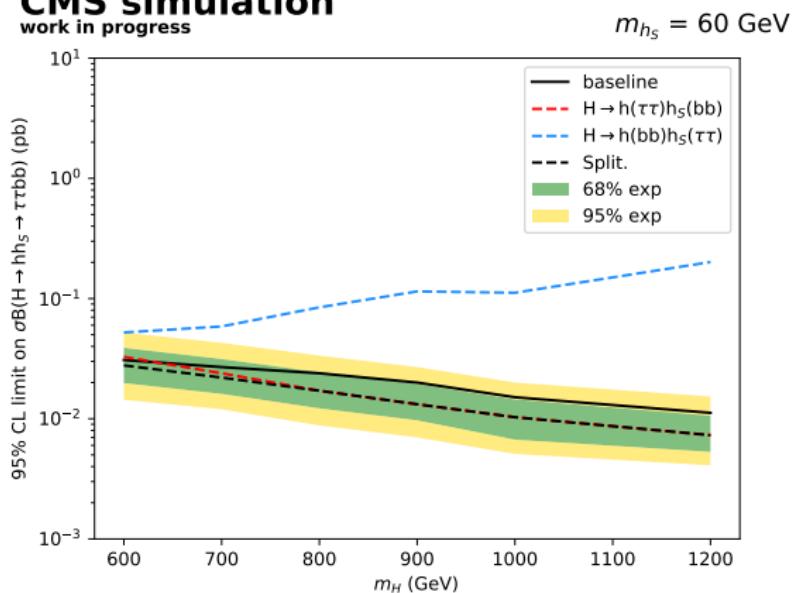
- Average improvement of around 30 %
- Stronger improvement for heavier m_H
- Correlates with discriminating power of added variables
- Higher signal over background ratio for heavier m_H



Expected upper limit: Splitting

- Average improvement of 26 %
- Stronger improvement for heavier m_H
- For lighter m_H the signal node discriminator for resolved topologies low
- Worse discrimination
- Phase space limited

CMS simulation work in progress

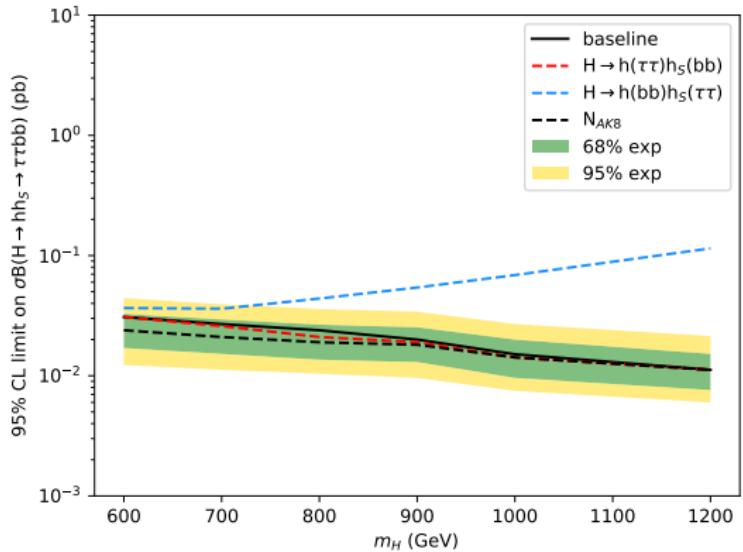


Expected upper limit: Cut

- Average improvement of 13 %
- Stronger improvement for lighter m_H
- For heavier m_H the imposed cut limits the statistic
- Studied phase space limited

CMS simulation work in progress

$m_{h_S} = 60 \text{ GeV}$



Input features

- p_T of the μ
- visible p_T of the τ_h
- visible m of the $\mu\tau_h$ -pair
- visible p_T of the $\mu\tau_h$ -pair
- number of b-tagged jets
- p_T of the p_T -leading b-tagged jet
- p_T of the p_T -sub-leading b-tagged jet
- visible m of the two p_T -leading b-tagged jets
- visible p_T of the two p_T -leading b-tagged jets
- number of non b-tagged jets
- p_T of the p_T -leading non b-tagged jet
- p_T of the p_T -sub-leading non b-tagged jet
- m between the two p_T -leading non b-tagged jets
- p_T between the two p_T -leading non b-tagged jets
- spatial distance ΔR between the two p_T -leading non b-tagged jets
- visible m of the entire $\tau\tau + bb$ system