

# Introduction to Cryogenics and Superconductivity

Carolin Heidt, Juliane Raasch  
**KSETA- Workshop Freudenstadt 2013**

INSTITUTE FOR TECHNICAL PHYSICS, INSTITUTE FOR TECHNICAL THERMODYNAMICS AND REFRIGERATION  
INSTITUTE OF MICRO- AND NANOELECTRONIC SYSTEMS



Source:  
Cern Website

# Outline – Cryogenics

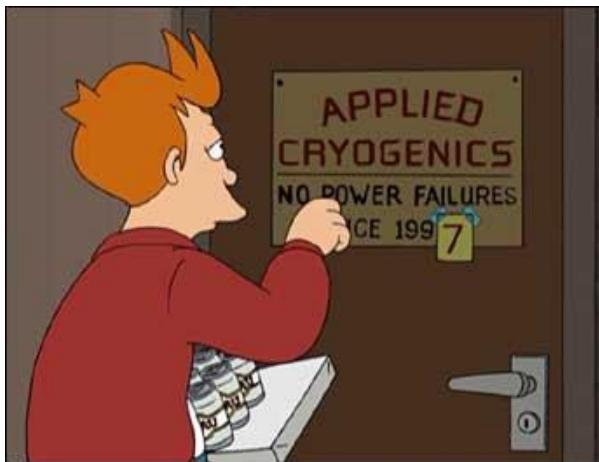
- Introduction
- Cold production
- Cryogenic Properties
  - Cryogenic fluids
  - Material Properties
- Cryostats
  - Dewar vessel
  - Thermal Insulation
  - Cern
  - Temperature measurement
  - Flow measurement
  - Safety



Source:  
Cern Website

# Introduction

- Cryogenics -> Greek: production of freezing cold
- Cryogenics -> Refrigeration at  $T < 120K$  (definition since 1971)
- Cryogenics <-> Cryonics= preservation of the human body in LN<sub>2</sub> after death



Source:  
[http://www.dailymotion.com/my\\_weblog/2007/10/experimental-tr.html](http://www.dailymotion.com/my_weblog/2007/10/experimental-tr.html)



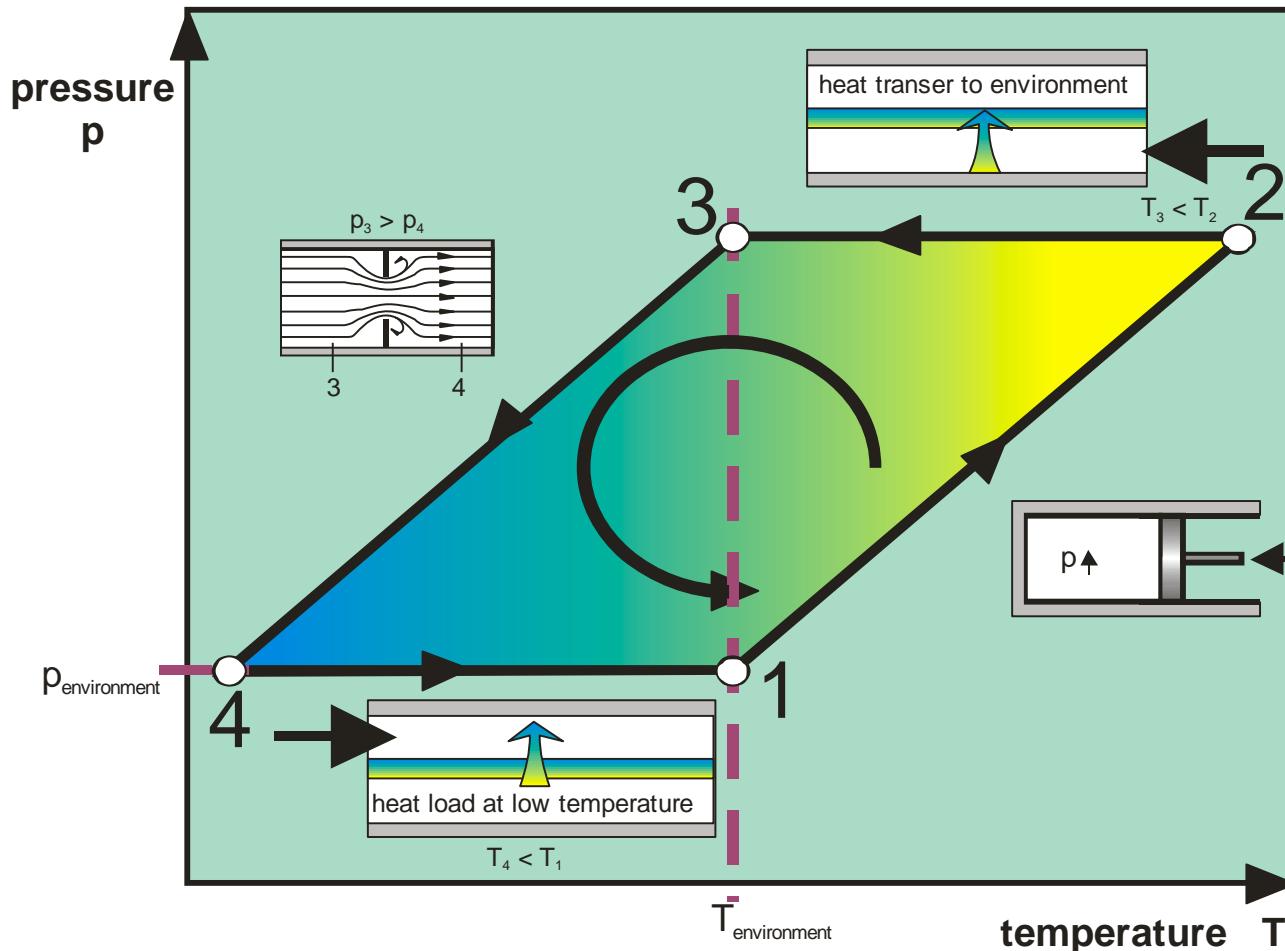
Source:  
[http://theinfosphere.org/images/cache/enwiki/fd/Cryogenic\\_Freezing\\_Chamber.html](http://theinfosphere.org/images/cache/enwiki/fd/Cryogenic_Freezing_Chamber.html)

# Introduction

## ■ Applications:

- Condensation & liquefaction of gases
  - Air separation
  - Transport
  - Storage
- Reduction of thermal noise and excitation
  - Particle accelerators
  - Particle detectors
- Others
  - Food Freezing
  - Space flight technology
  - LH<sub>2</sub> technology
  - Medical applications

# Cold production (Basic)



- Basic principle:
  - Compression
  - Heat transfer to ambient
  - Throttling/ expansion
  - Heat load at low temperature

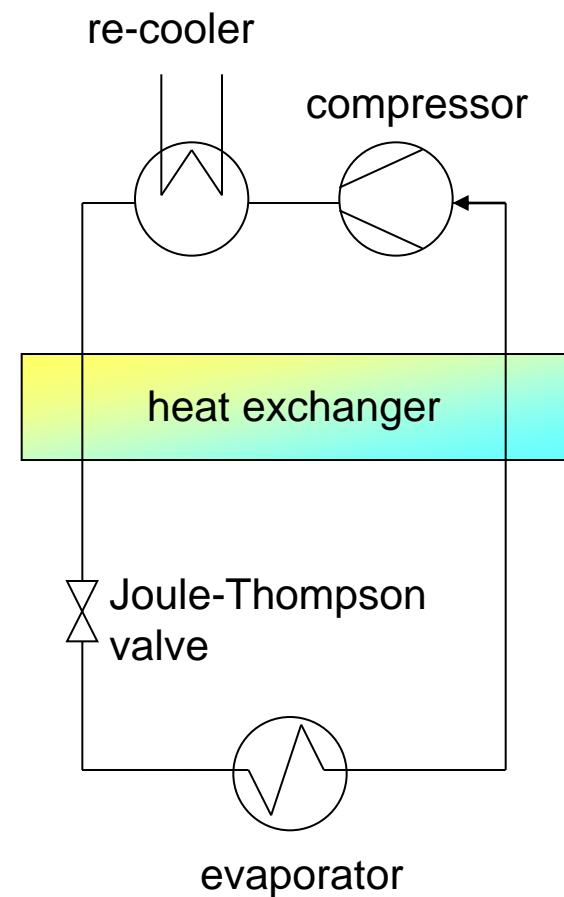
Source:  
 H. Neumann, IETP, KIT, 2013 ESAS Summer School

# Cold production (Refrigeration Cycles)

## ■ Joule-Thompson-Process

(Linde)

- Simple, reliable
- Low efficiency



Source:  
 H. Neumann, ITEP, KIT, 2013 ESAS  
 Summer School

# Cold production (Refrigeration Cycles)

## ■ Joule-Thompson-Process (Linde)

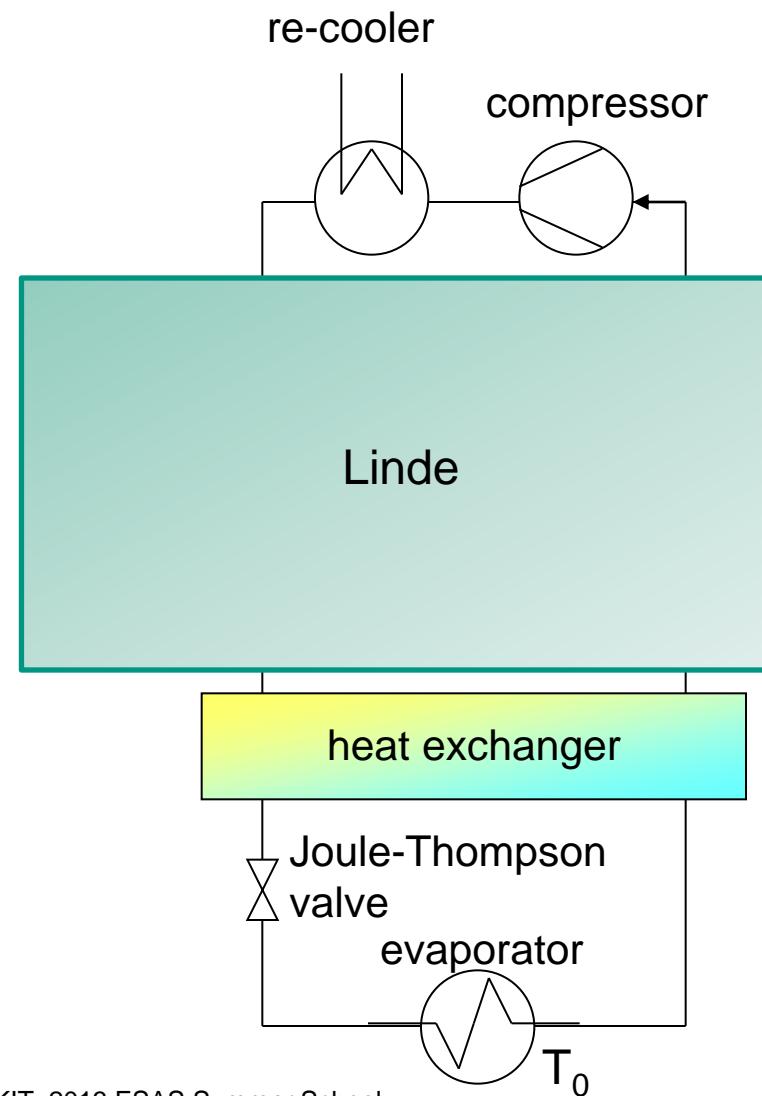
- Simple, reliable
- Low efficiency

## ■ Claude-Process

- Higher efficiency
  - Expansion of partial current for extra cooling
- Less reliable

## ■ Stirling Process

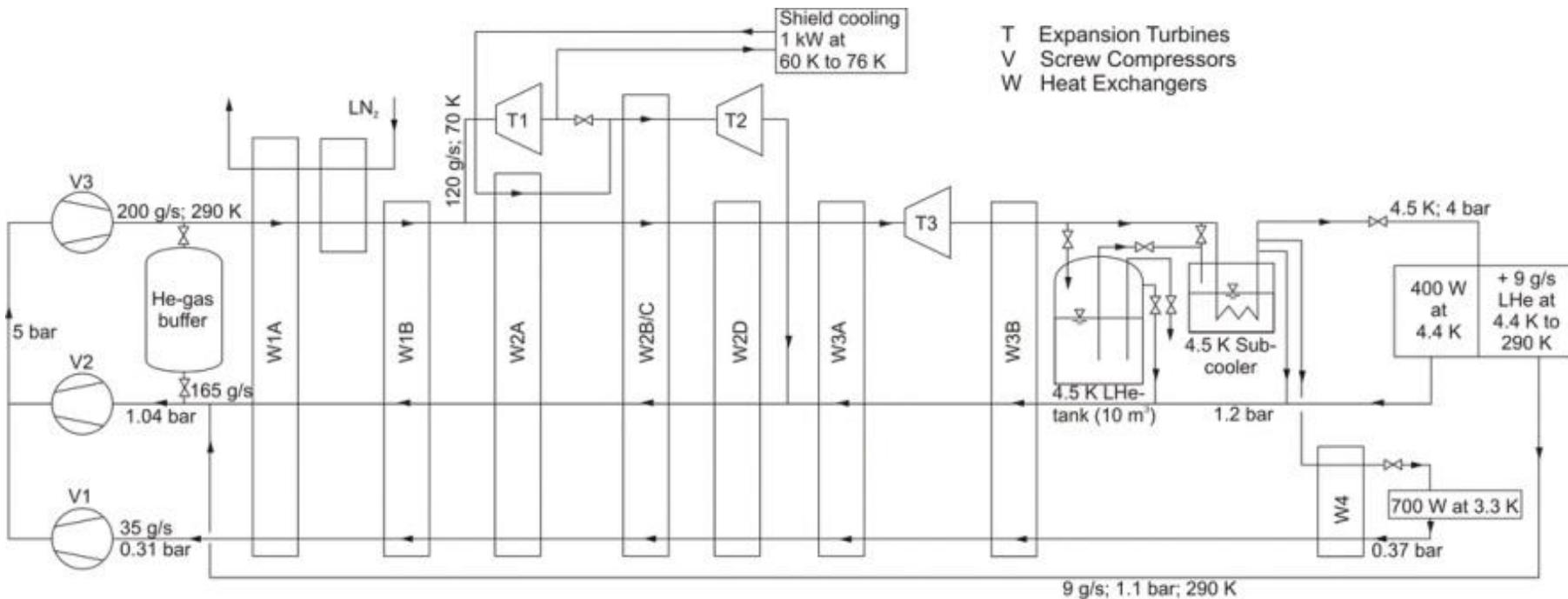
- Compact
- No liquefaction



Source:  
 H. Neumann, ITEP, KIT, 2013 ESAS Summer School

# Cold production (Refrigeration Cycles)

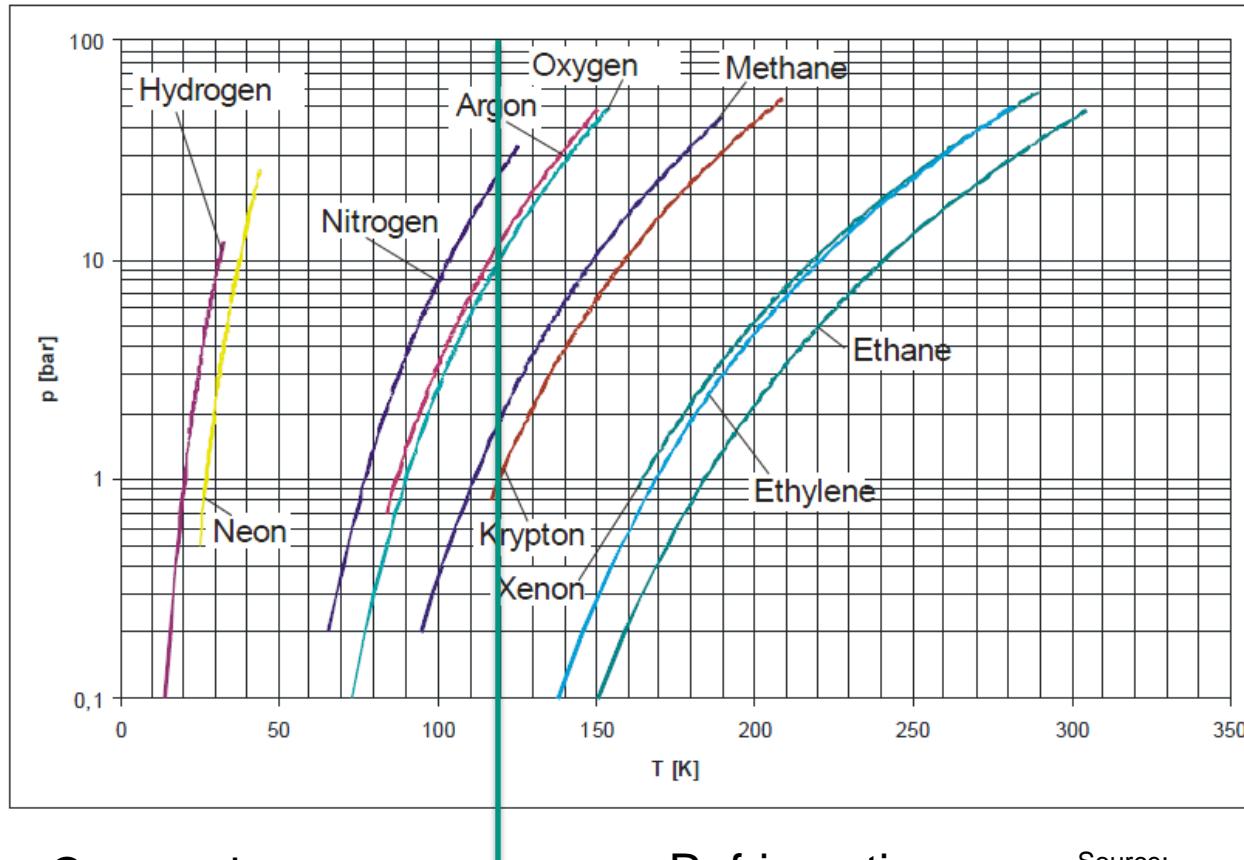
## ■ Example: 2kW helium liquefier at ITEP



Source:  
ITEP Homepage

# Cryogenic fluids

## Vapor-pressure curves



Cryogenics

120 K

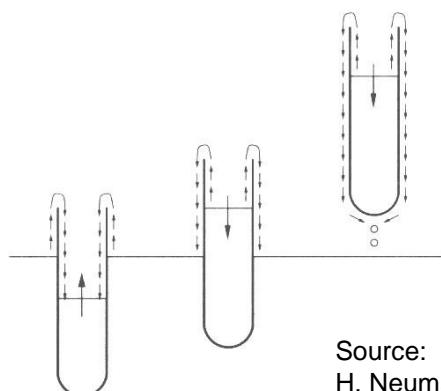
Refrigeration

Source:  
H. Neumann, ITEP, KIT, 2013 ESAS  
Summer School

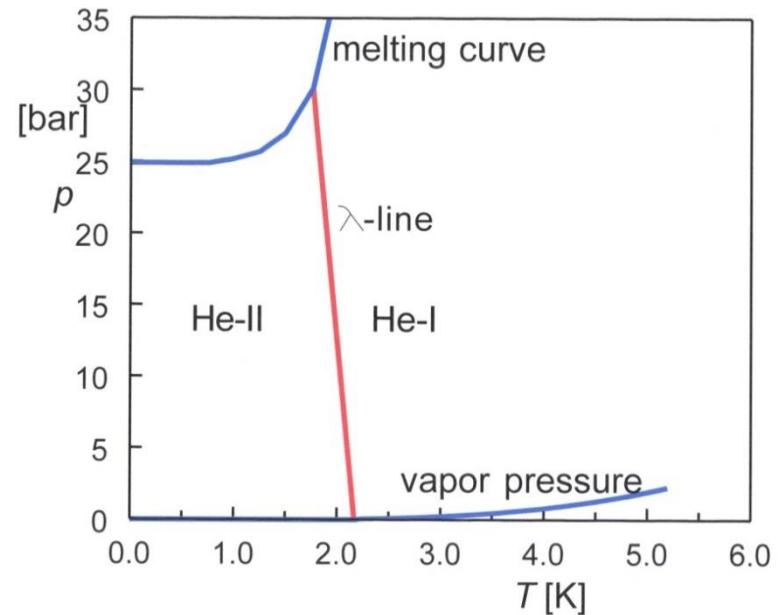
# Cryogenic fluids (Helium)

## ■ Specifics of helium

- $\lambda$  –line separates
  - LHe I
  - LHe II (superfluid)
    - Very high thermal conductivity
    - No boiling
    - Onnes-effect



Source:  
 H. Neumann, ITEP, KIT, 2013 ESAS  
 Summer School



Source:  
 Wikipedia „Helium“

# Material Properties

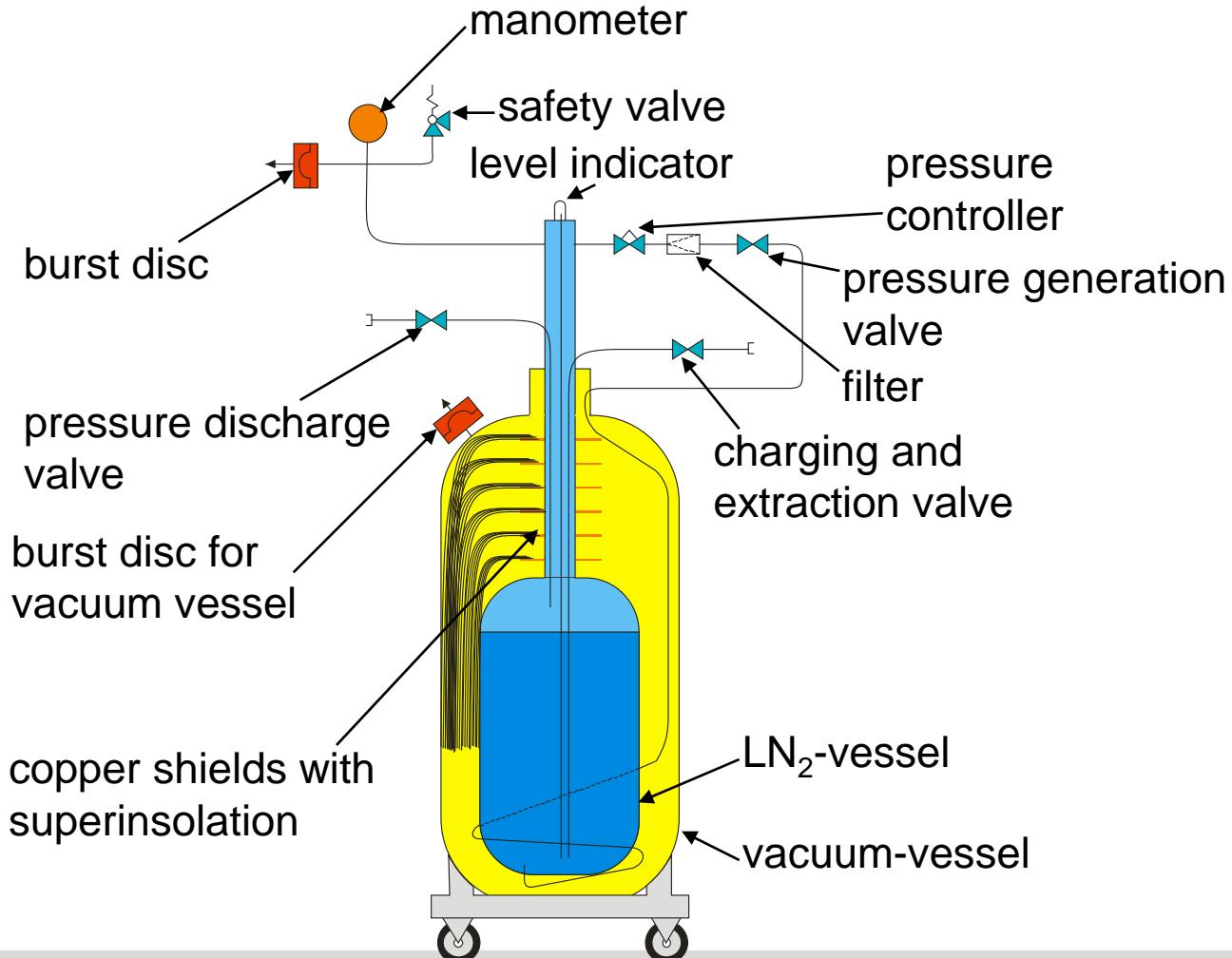
- To take into account:
  - Heat conductance
    - varies with decrease in T
  - Thermal contraction
    - different contractions of different materials
  - Mechanical characteristics
    - elastic limit and modulus increase ☺
    - ductility and plasticity decrease dramatically -> brittleness ☹
  - Consult AD 2000-W10 for materials at cryogenic temperatures



Source:  
K.Weiss, ITEP meeting 2012

# Cryostats (Layout)

- example: LN<sub>2</sub>-vessel with integrated pressure generation



# Cryostats (Insulation)

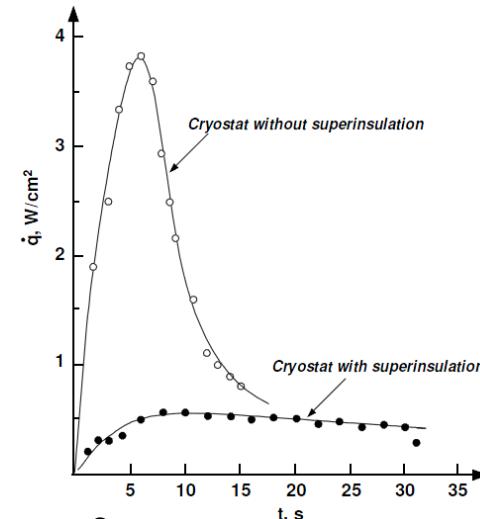
## ■ Types of thermal insulation

- Powders, foams, fibreglas,...
- Vacuum Insulation
- MLI (Multi-Layer-Insulation) or SI (Super-Insulation)
  - high vacuum (prevents convection)
  - reflecting layers, e.g. Al foil (reduce radiation)
  - spacer elements, e.g. glass fibre (have low heat conductivity)



Source: V. Chrz

<http://indico.cern.ch/getFile.py/access?sessionId=3&resId=0&materialId=0&confId=90787>



Source:  
Lehmann/Zahn, 1978, Proc. CEC

# Cryostats (CERN)

- Example: CERN, the largest cryogenic system in the world
  - 36,000 t of SC magnets (NbTi wires) operate at 1.9 K
  - Need of 136 t of helium (superfluid below 2.17K, very high thermal conductivity -> efficient heat conductor)
  - Closed LHe circuit, 27 km long
  - Entire cooling process takes weeks to complete



Source: Cern website  
<http://home.web.cern.ch/about/engineering/cryogenics-low-temperatures-high-performance>

# Cryostats (CERN)



Compressor unit of the 4.5 K refrigerator

- 8 units in the complete system
- Each cryoplant consists of 3 stages
  1. RT-> 80 K  
using 10,000 t LN<sub>2</sub> in HX (600 kW)
  2. 80 K -> 4.5 K  
using refrigerator with cooling capacity of 18 kW at 4.5 K
  3. 4.5 K ->1.9 K  
using refrigerator with cooling capacity of 2.4 kW at 1.8 K

Source: Cerncourier

<http://cerncourier.com/cws/article/cern/54382>

# Cryostats (Temperature Measurement)

## ■ temperature measurement

### ■ low temperature sensors (secondary temperature sensors)

#### ■ *resistive sensors*

##### ■ *negative temperature coefficient (NTC)*

- carbon - glas sensor (CG)
- Cernox (CX1050)
- carbon sensor (Allen Bradley C100 )
- germanium (Ge)
- carbon composite (TVO)

##### ■ *positive temperature coefficient (PTC)*

- platinum sensor (Pt100)
- rhodium - ferric - sensor (RhFe)

#### *diodes*

- Si - diodes
- GaAlAs - diodes

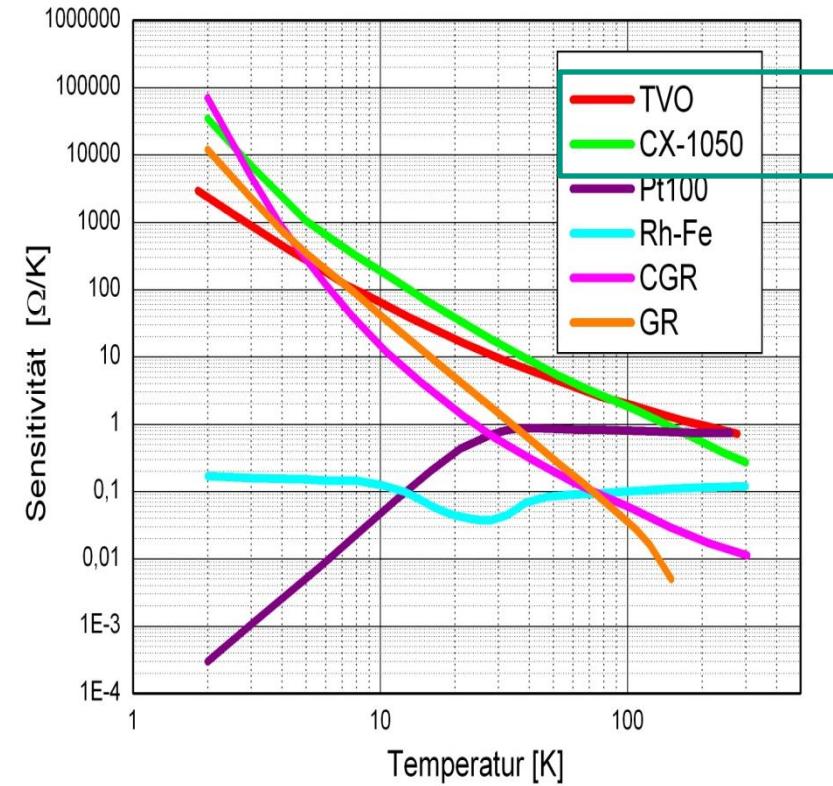
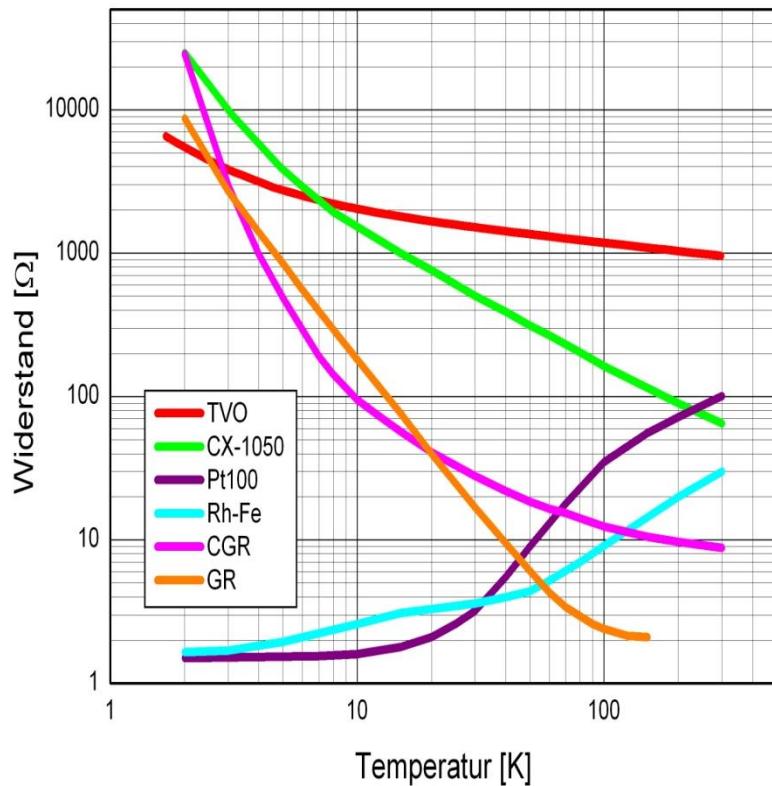
#### *others*

- thermocouple (CuKo)
- CLTS (Cryogenic Linear Temperature Sensor)
- capacity thermometers

(by M. Süßer)

# Cryostats (Temperature Measurement)

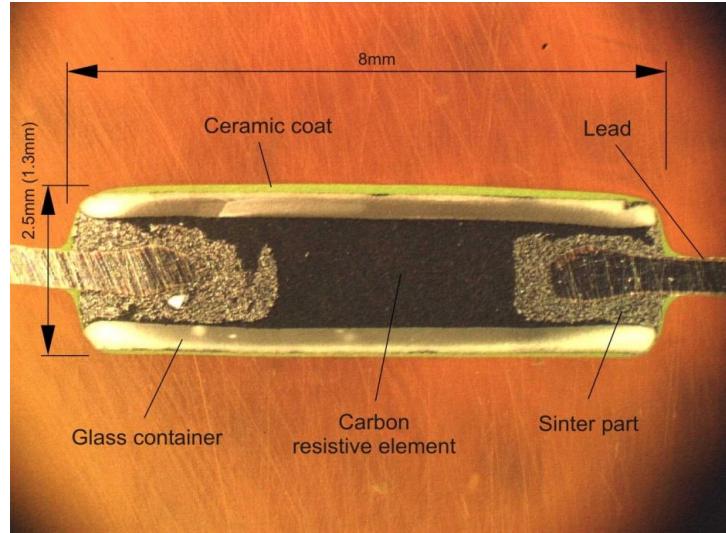
## Characteristic curves of resistive sensors



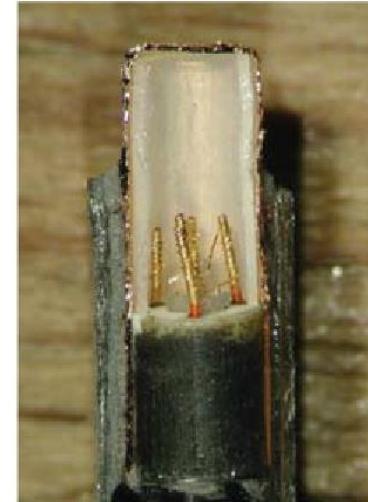
Source: M.Süßer, Einführung in die Tieftemperaturmesstechnik

# Cryostats (Temperature Measurement)

## TVO



## Cernox



- Carbon-  $\text{Al}_2\text{O}_3$  Compound
- Calibration at ITEP
- Costs ~ 400 €
- Able to work under high pressure and stress

- Zirconium-Nitrit-film on saphir body
- Lakeshore
- Costs ~650€

Source: M.Süßer, Einführung in die Tieftemperaturmesstechnik

# Cryostats (Mass flow measurement)

## ■ Mass flow measurement

System	Einsatzgebiet	Messgröße
	Thermischer Durchflussmesser	Prozesssteuerung $q \sim \Delta T$
	Laminarflow-element	Präzisionsmessung $q \sim \Delta P$
	Venturi-Rohr	Messung bei flüssig Helium Temperatur $q \sim \sqrt{\Delta p}$

Source: M.Schrank, DKV-Tagung 2012

# Cryostats (Safety)

## ■ Safety standards:

- DIN EN 13648
- EN ISO 4126
- AD 2000
- To come: DIN SPEC 4683 „Überdruck-Absicherung von Helium-Kryostaten“



# Sources

- Information on Cryogenics:
  - H. Neumann, ITEP, KIT, Talk at 2013 ESAS International Summer School oh Materials and Applications of Superconductivity, 1st August 2013
  - M.Schrank, Introduction to cryogenics, Vortrag beim Young Scientists Workshop 2013, Kristberg
- Information on Dewar vessels and MLI:
  - V. Chrz, Chart Ferox,  
<http://indico.cern.ch/getFile.py/access?sessionId=3&resId=0&materialId=0&confId=90787> Information on Cryogenic Measurement
- Information on CERN Cryogenics :
  - <http://cerncourier.com/cws/article/cern/54382>
  - <http://home.web.cern.ch/about/engineering/cryogenics-low-temperatures-high-performance>
- Information on Cryogenic Measurement
  - M. Süßer, Einführung in die Tieftemperaturmesstechnik, Interner Bericht FE.5130.0013.0012/N
  - M. Schrank, Gasdurchflussmessung in der Kryotechnik, Vortrag bei der DKV-Tagung 2012, Würzburg
- Information on Helium Cryogenics Safety
  - W. Lehmann/ G. Zahn, Safety aspects for Lhe cryostats and Lhe transport cpntainers, Proc. ICEC, London, 1978, Vol. VII, 569-579

# Introduction to Cryogenics and Superconductivity

Carolin Heidt, Juliane Raasch  
**KSETA- Workshop Freudenstadt 2013**

INSTITUTE FOR TECHNICAL PHYSICS, INSTITUTE FOR TECHNICAL THERMODYNAMICS AND REFRIGERATION  
INSTITUTE OF MICRO- AND NANOELECTRONIC SYSTEMS

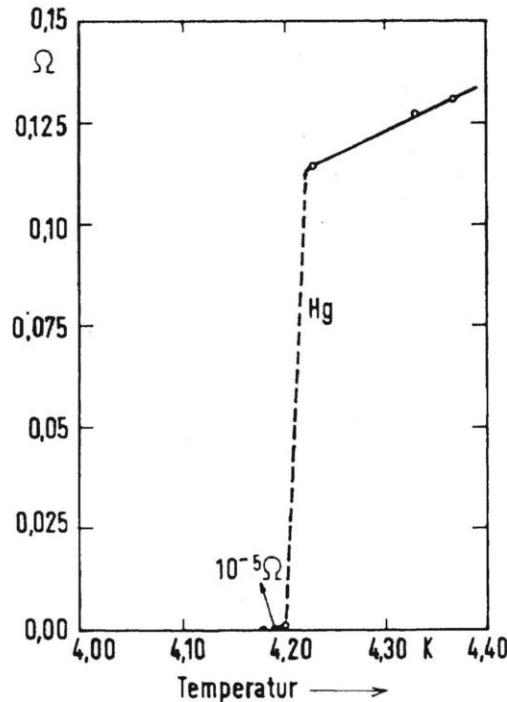
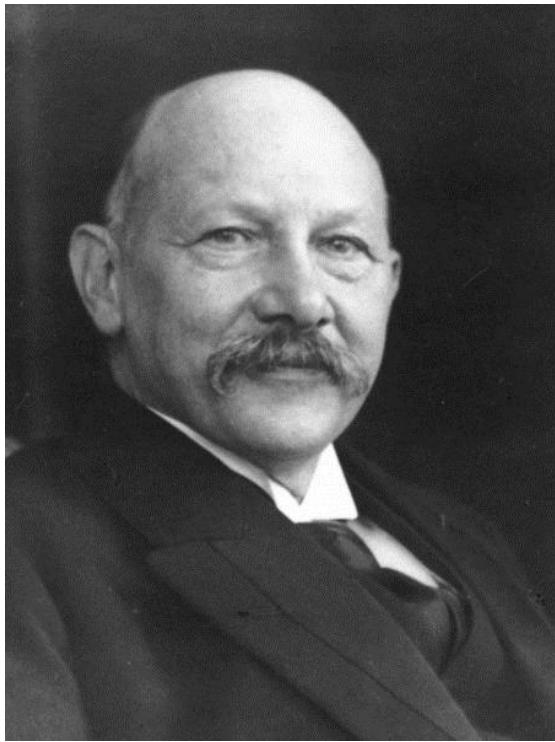


Source:  
Cern Website

# Outline – Superconductors

- Phenomenology and electromagnetic description
- Classification
- Theory of superconductivity
- Applications of superconductors

# Discovery of the superconductivity

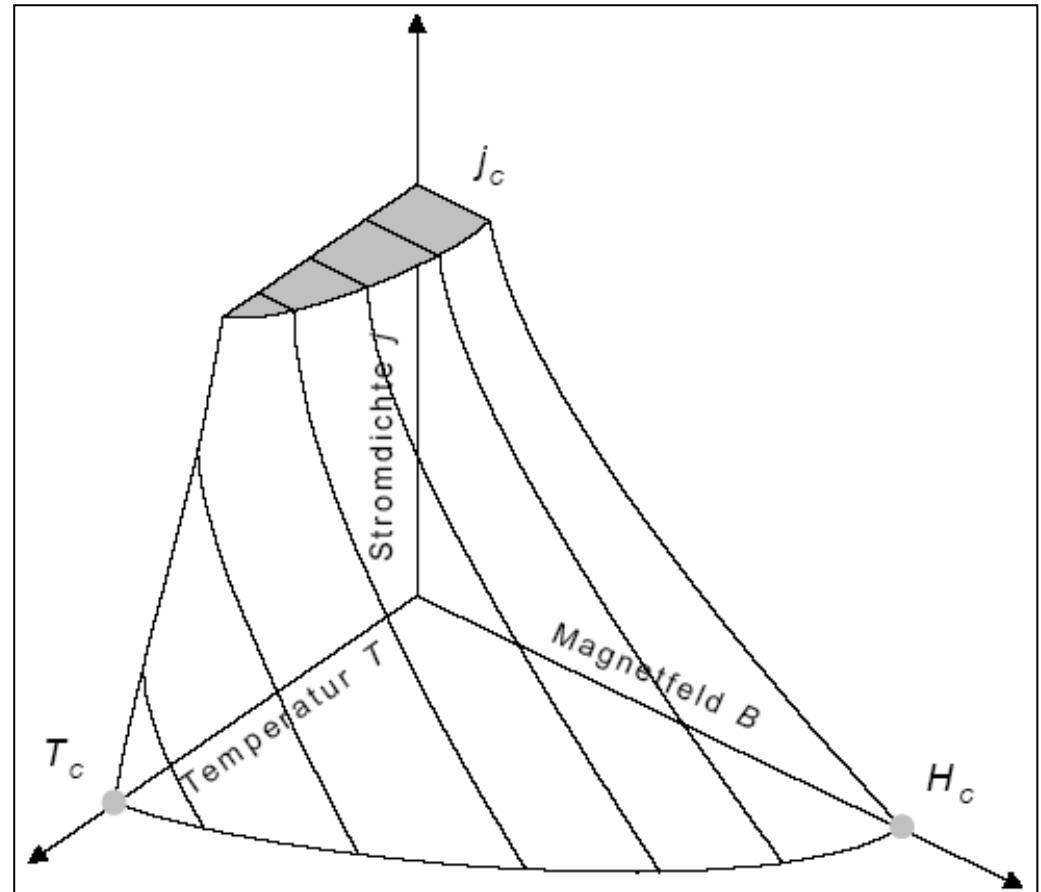
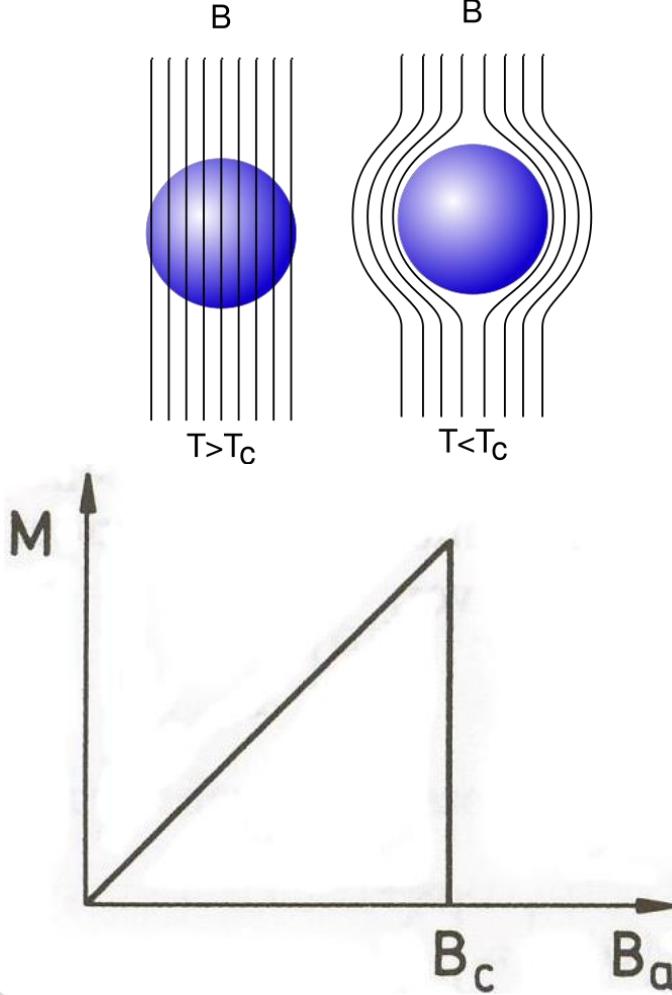


- 1908 Liquefaction of helium experiments at 1.5 K
- 1911 Discovery of superconductivity in mercury

<http://www.nobelprize.org>, <http://hoffman.physics.harvard.edu>

# Characteristics of Superconductivity

## ■ 1933 Meissner effect



<http://en.wikipedia.org>

# London equations

- Behaviour of electromagnetic fields in superconductor:

~~$$\vec{j} = \sigma \vec{E}$$~~

- 1st London equation:

$$\frac{d\vec{j}_s}{dt} = \frac{1}{\mu_0 \lambda^2} \vec{E}$$

- 2nd London equation:

$$\text{rot } \vec{j}_s = -\frac{1}{\mu_0 \lambda^2} \vec{B}$$

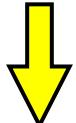
- London penetration depth:

$$\lambda^2 = \frac{m_s}{\mu_0 n_s e_s^2}$$

# Meissner effect

4th Maxwell equation

$$\vec{j}_s = \frac{1}{\mu_0} \text{rot } \vec{B}$$

rot 

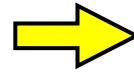
+

2nd London eqaution

$$\text{rot } \vec{j}_s = -\frac{1}{\mu_0 \lambda^2} \vec{B}$$



$$\text{rot } \vec{j}_s = \frac{1}{\mu_0} \text{rot rot } \vec{B}$$



$$-\frac{1}{\mu_0 \lambda^2} \vec{B} = \frac{1}{\mu_0} \text{rot rot } \vec{B}$$

$$\text{rot rot } \vec{B} = \text{grad div } \vec{B} - \Delta \vec{B} \quad ; \text{ 2nd Maxwell eq.: div } \vec{B} = 0$$

  $\Delta \vec{B} - \frac{1}{\lambda^2} \vec{B} = 0$

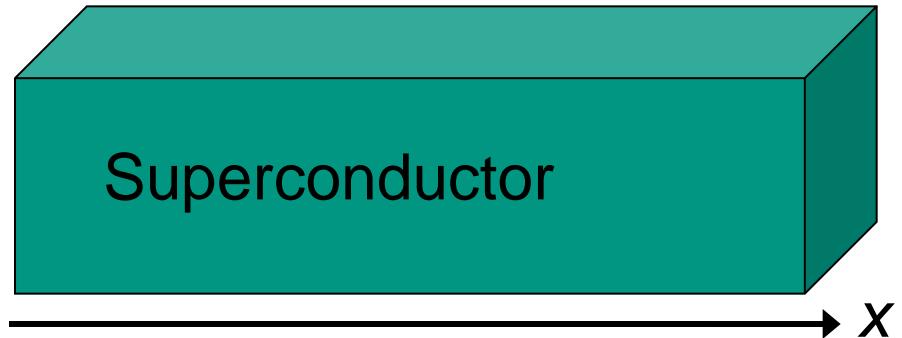
  $\vec{B} = B \cdot \vec{e}_z$

$B(x) = B_a e^{-x/\lambda}$

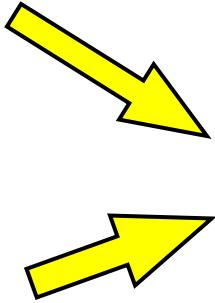
# Critical current density

$$\vec{j}_s = \frac{1}{\mu_0} \text{rot} \vec{B}$$

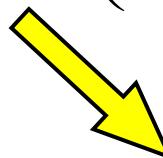
$\uparrow \vec{B} = B \cdot \vec{e}_z$



$$B(x) = B_a e^{-x/\lambda}$$



$$\vec{j}_s(x) = \frac{1}{\mu_0} \text{rot} \left( B_a e^{-x/\lambda} \cdot \vec{e}_z \right)$$

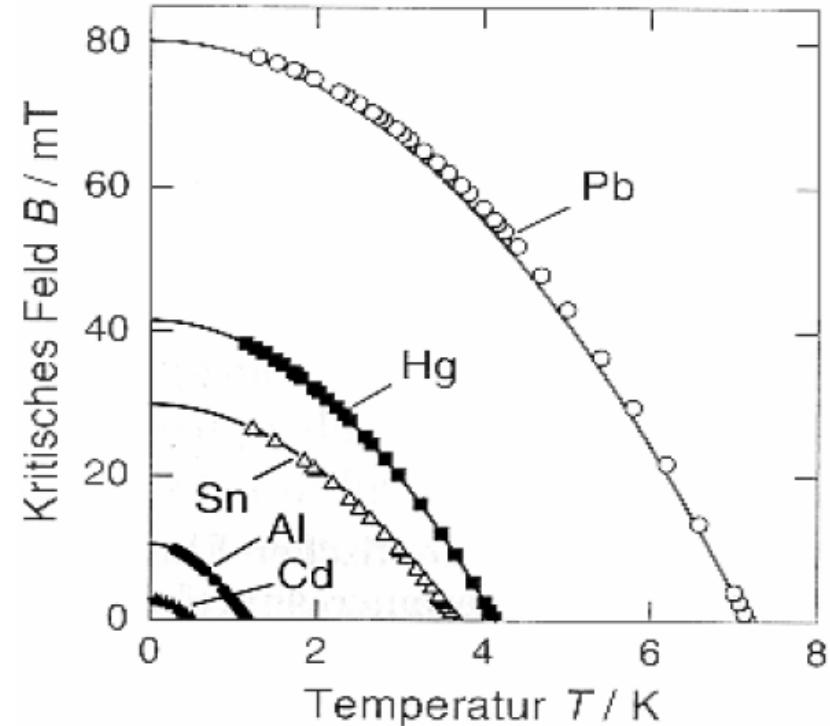
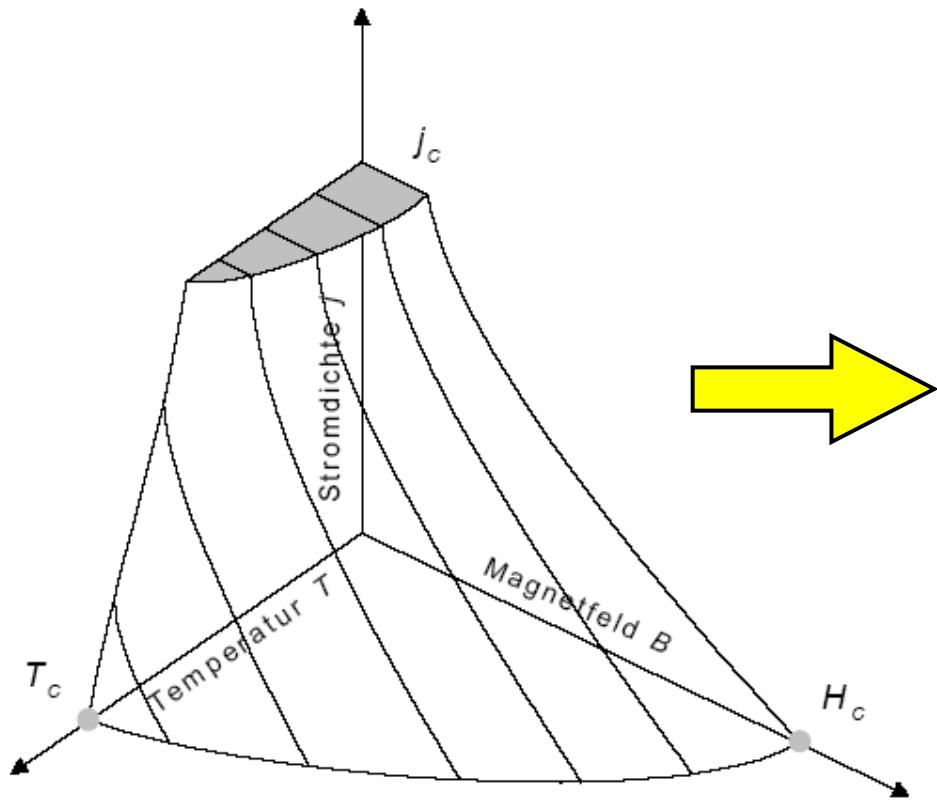


- $j_s$  → Screening current
- $j_s > j_c$  → break down of SC

$$\vec{j}_s(x) = \frac{1}{\mu_0 \lambda} B_a e^{-x/\lambda} \cdot \vec{e}_y$$

# Classification – Type-I superconductors

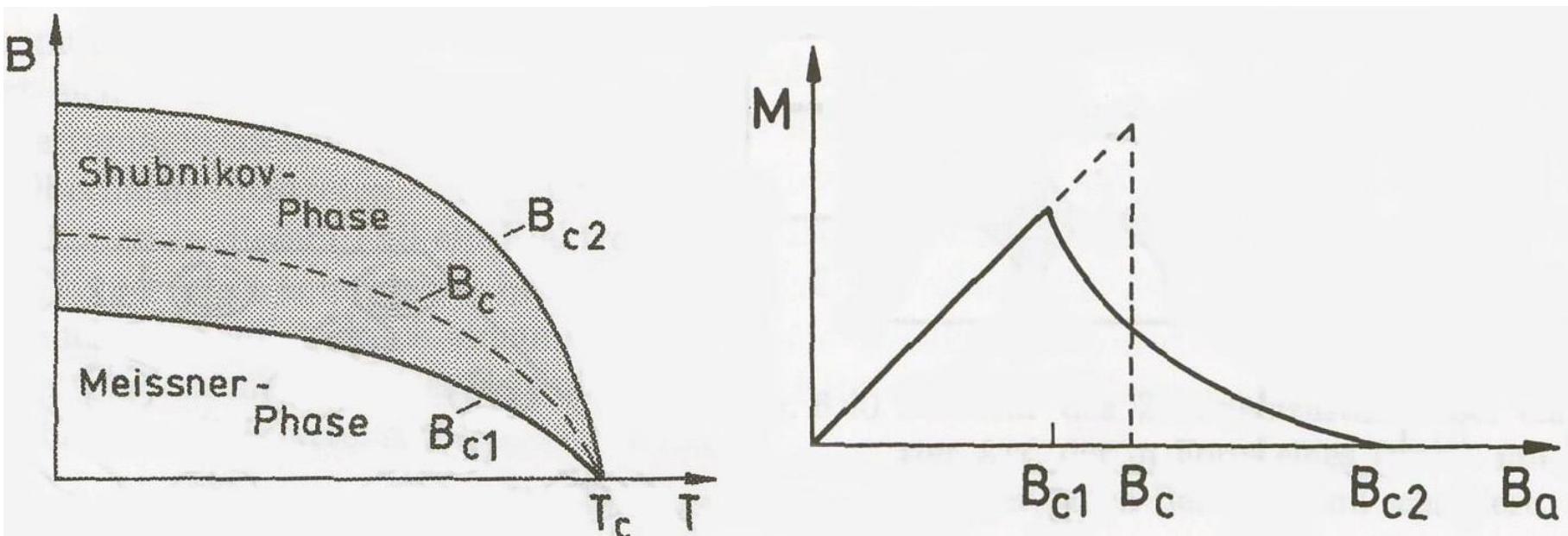
- Phase diagram in  $B, T$ -plane:



$$B_c(T) = B_c(0) \left[ 1 - \left( \frac{T}{T_c} \right)^2 \right]$$

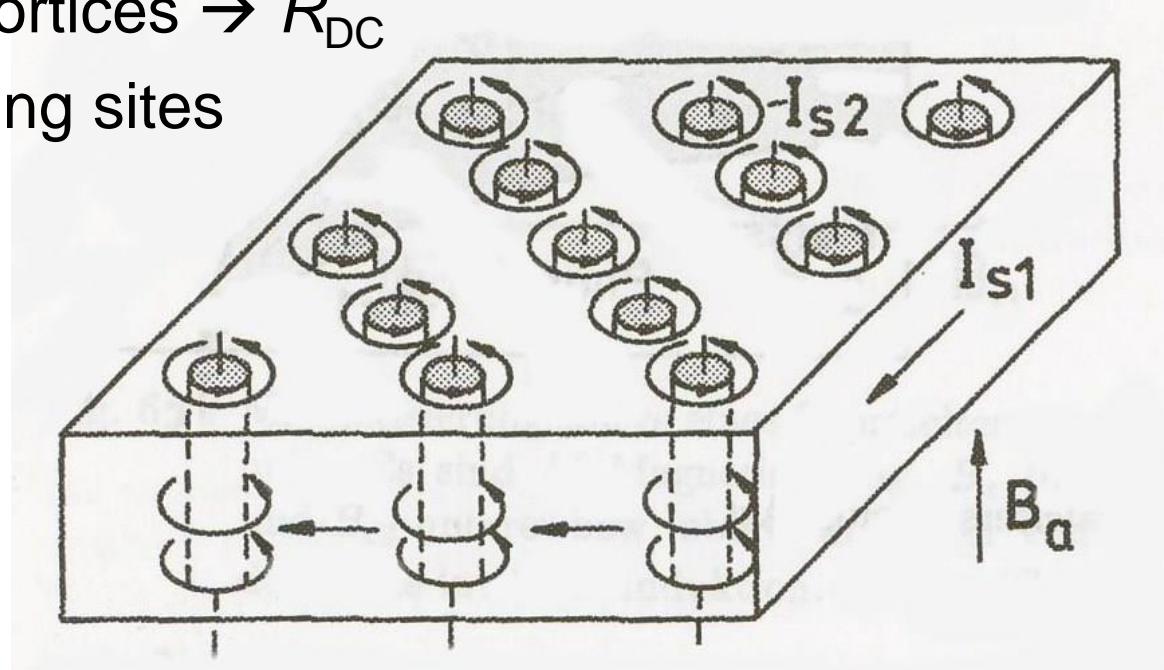
# Classification – Type-II superconductors

- $B < B_{c1}$ : Meissner phase
- $B_{c1} < B < B_{c2}$ : Shubnikov phase
- $B_{c2} < B$ : break down of SC



# Classification – Type-II superconductors

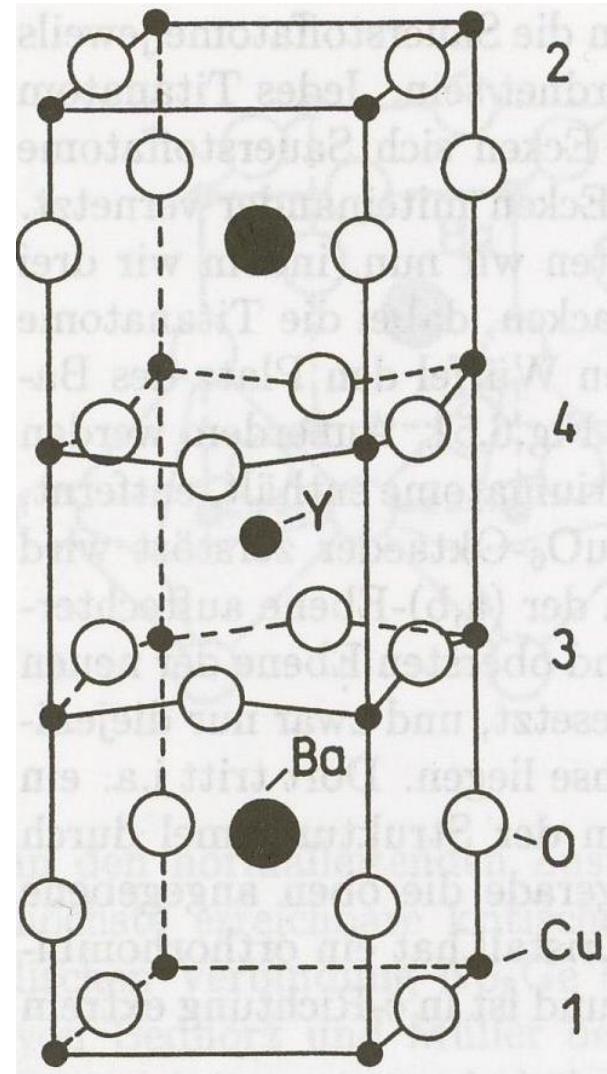
- $B_{c1} < B < B_{c2}$ : Shubnikov phase
  - Vortices carry magnetic flux
  - Magnetic flux quantum  $\Phi_0$
  - Movement of vortices  $\rightarrow R_{DC}$
  - Defects = Pinning sites



Abrikosov vortex lattice

# Classification – High temperature SC

- 1986 Bednorz & Müller
- Ceramics
- Cuprates:  $\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$
- $T_c > 77 \text{ K}$   
Liquid nitrogen or cryogen free cooling  
Maximum:  $T_c \sim 135 \text{ K}$
- Lack of theory



# Classification

Type-I SCs

Type-II SCs

HTSC

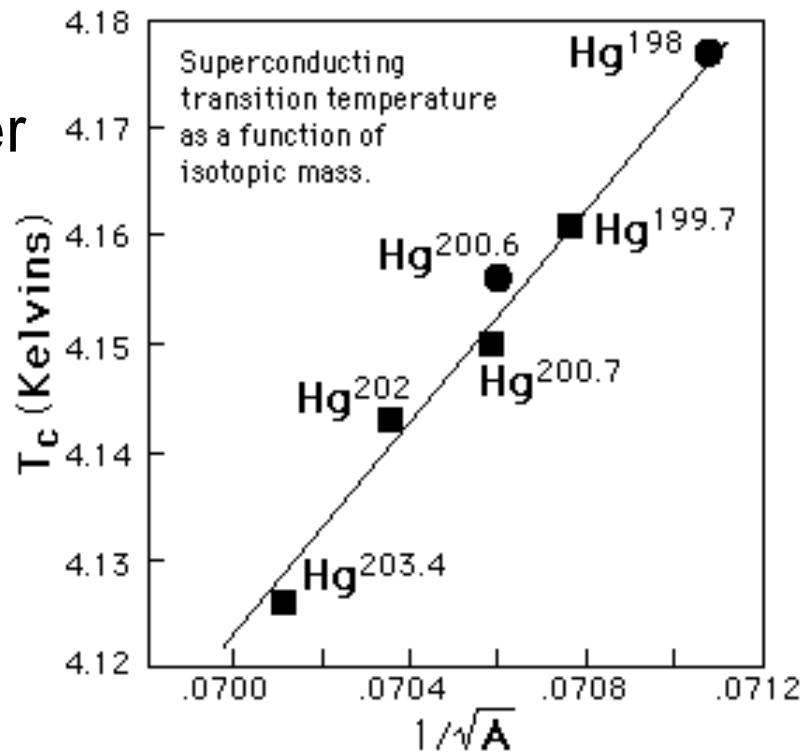
Material	$T_c$ (K)	$B_{c(2)}$ (T)
Al	1,19	0,0099
Hg	4,15	0,0412
Pb	7,2	0,0803
Nb	9,2	0,27
Ta	4,39	0,18
$\text{Nb}_3\text{Ge}$	23	30
$\text{PbMo}_6\text{S}_8$	15	45
$\text{YBa}_2\text{Cu}_3\text{O}_7$	93	30 bis 60
$\text{Te}_2\text{Ca}_2\text{Ba}_2\text{Cu}_3\text{O}_x$	135	100 bis 120

# BCS theory (1)

- London equations: electromagnetic, phenomenologic
- Ginzburg-Landau theory: thermodynamic, phenomenologic
- Quantum mechanics?
- 1957 Bardeen, Cooper, Schrieffer
- Postulation of Cooper pairs
  - Attractive force between 2 electrons

$$T_c \propto \frac{1}{\sqrt{M}}$$

*M – atomic mass*

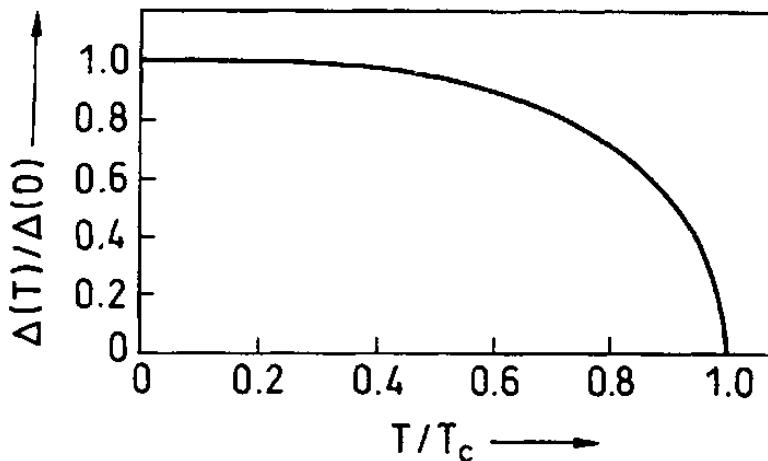


<http://hyperphysics.phy-astr.gsu.edu>

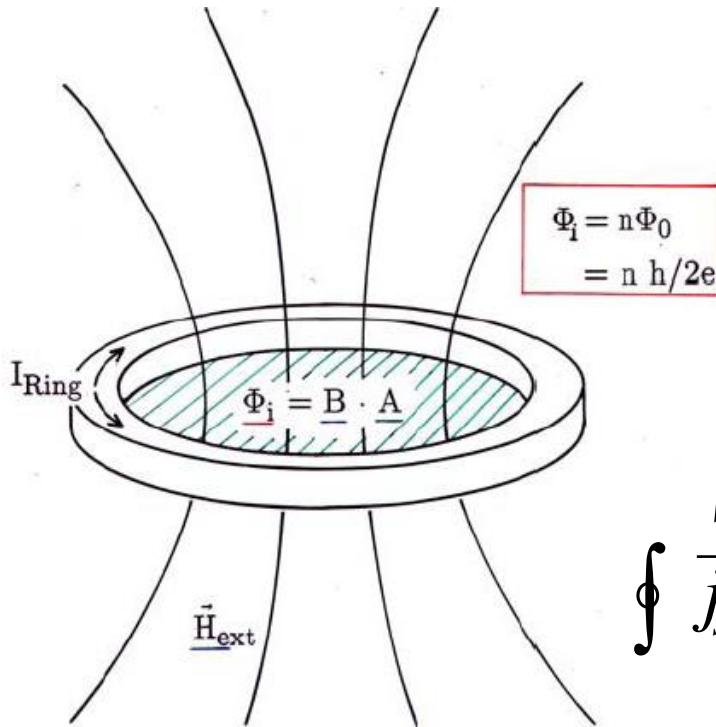
# BCS theory (2)

- Postulation of Cooper pairs
  - $(\mathbf{k}, \uparrow)$  and  $(-\mathbf{k}, \downarrow) \rightarrow$  spin and momentum zero
  - Bosonic macroscopic state
- Binding energy of Cooper pair:  $2\Delta$
- No DC resistance below excitations of  $2\Delta$

$$\psi = \sqrt{n_s} \cdot e^{i\varphi}$$



# Flux quantisation



$$\mu_0 \lambda^2 \vec{j}_s = -\frac{\hbar}{e_s} \text{grad } \varphi - \vec{A}$$

$\psi$  uniformly continuous

$\int \vec{j}_s d\vec{s} = 0$

Stokes

$$\int_A \vec{A} d\vec{s} = \int_A \vec{B} d\vec{A} = \Phi_A$$

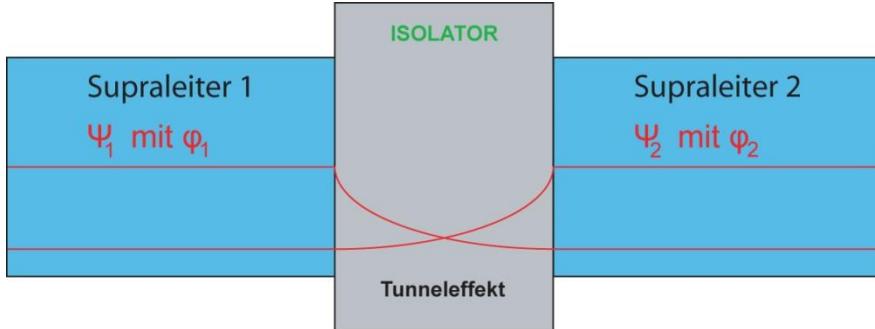
$$\int \text{grad } \varphi d\vec{s} = 2\pi n$$

→  $\Phi_A = \frac{h}{e_s} n = n \Phi_0$

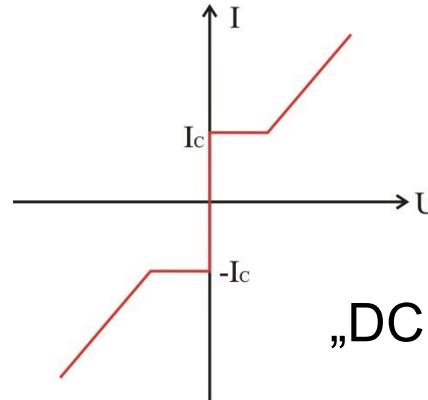
$$\Phi_0 = h/2e = 2,0678 \cdot 10^{-15} \text{ Tm}^2$$

# Josephson devices

## ■ 1st Josephson equation



$$I_S = I_C \cdot \sin(\varphi_2 - \varphi_1)$$



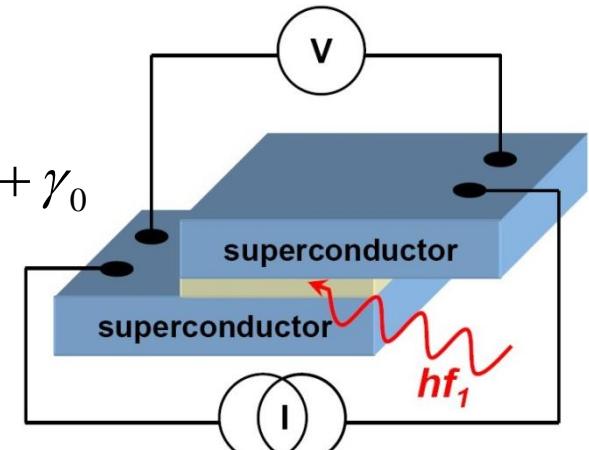
„DC Josephson effect“

## ■ 2nd Josephson equation

$$\frac{d}{dt}(\varphi_2 - \varphi_1) = \frac{2\pi}{\Phi_0} \cdot U \quad \Rightarrow \quad \varphi_2 - \varphi_1 = \left( \frac{2\pi}{\Phi_0} U \right) \cdot t + \gamma_0$$

$$I_S = I_C \cdot \sin\left(\frac{2\pi}{\Phi_0} U \cdot t + \gamma_0\right) \quad \Rightarrow \quad f = \frac{2e}{h} \cdot U$$

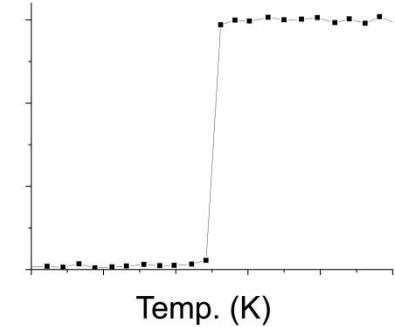
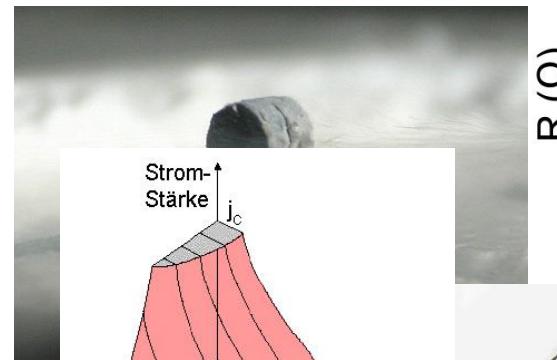
$$f = \frac{2e}{h} \cdot U$$



„AC Josephson effect“

# Summary of superconductor basics

- $R_{DC} = 0$  & Meissner effect



- Critical values:  $T_c$ ,  $j_c$ ,  $B_c$

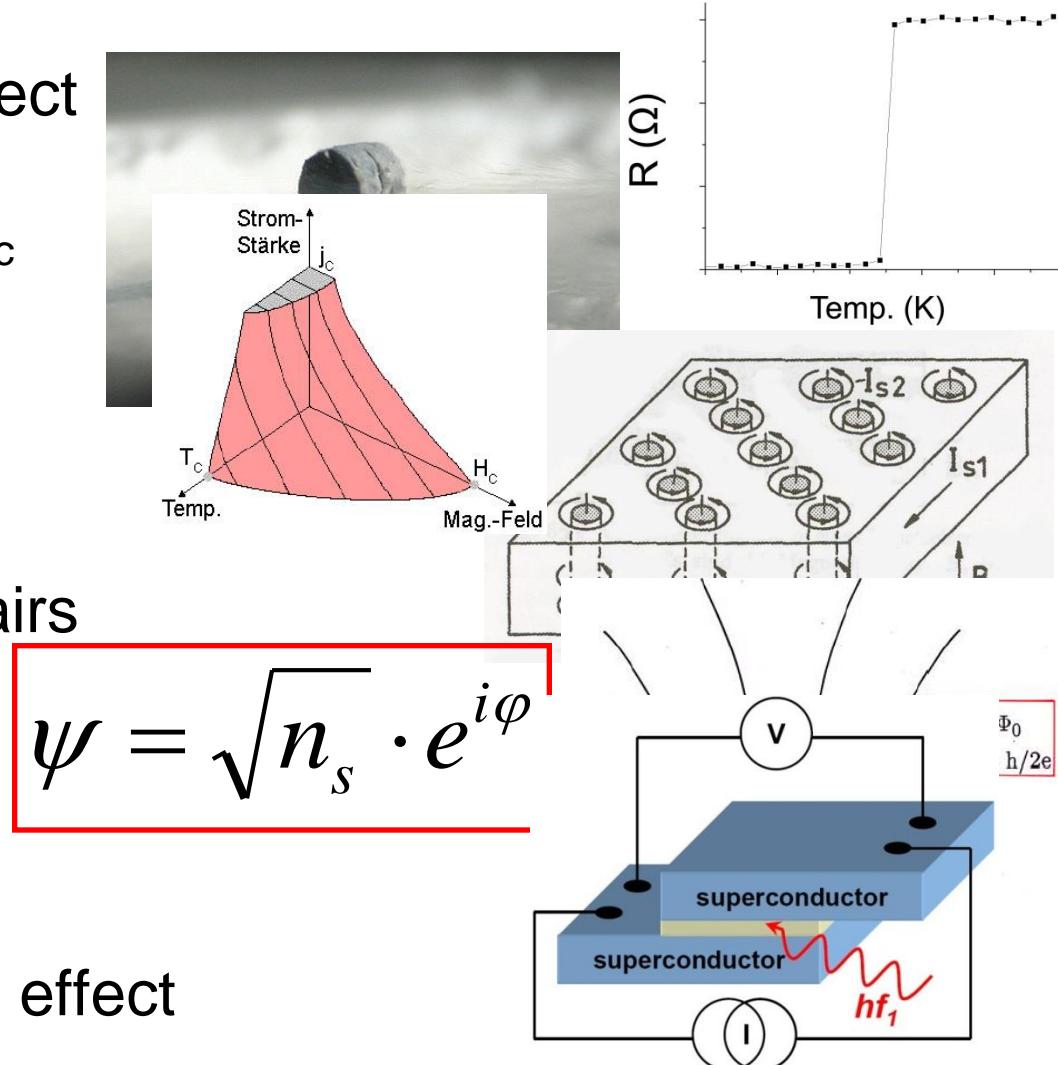
- Type-I & Type-II SCs

- BCS theory: Cooper pairs

$$\psi = \sqrt{n_s} \cdot e^{i\phi}$$

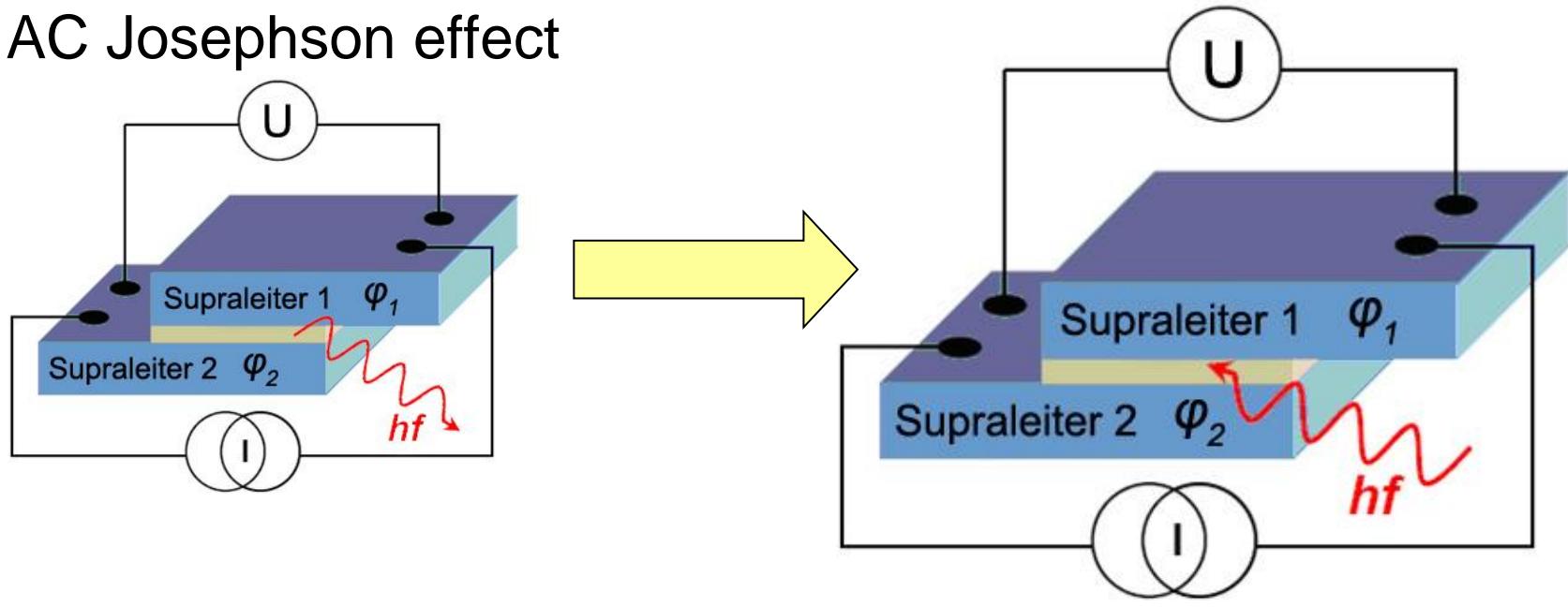
- Flux quantisation

- DC and AC Josephson effect



# Quantum electronics: Voltage standard

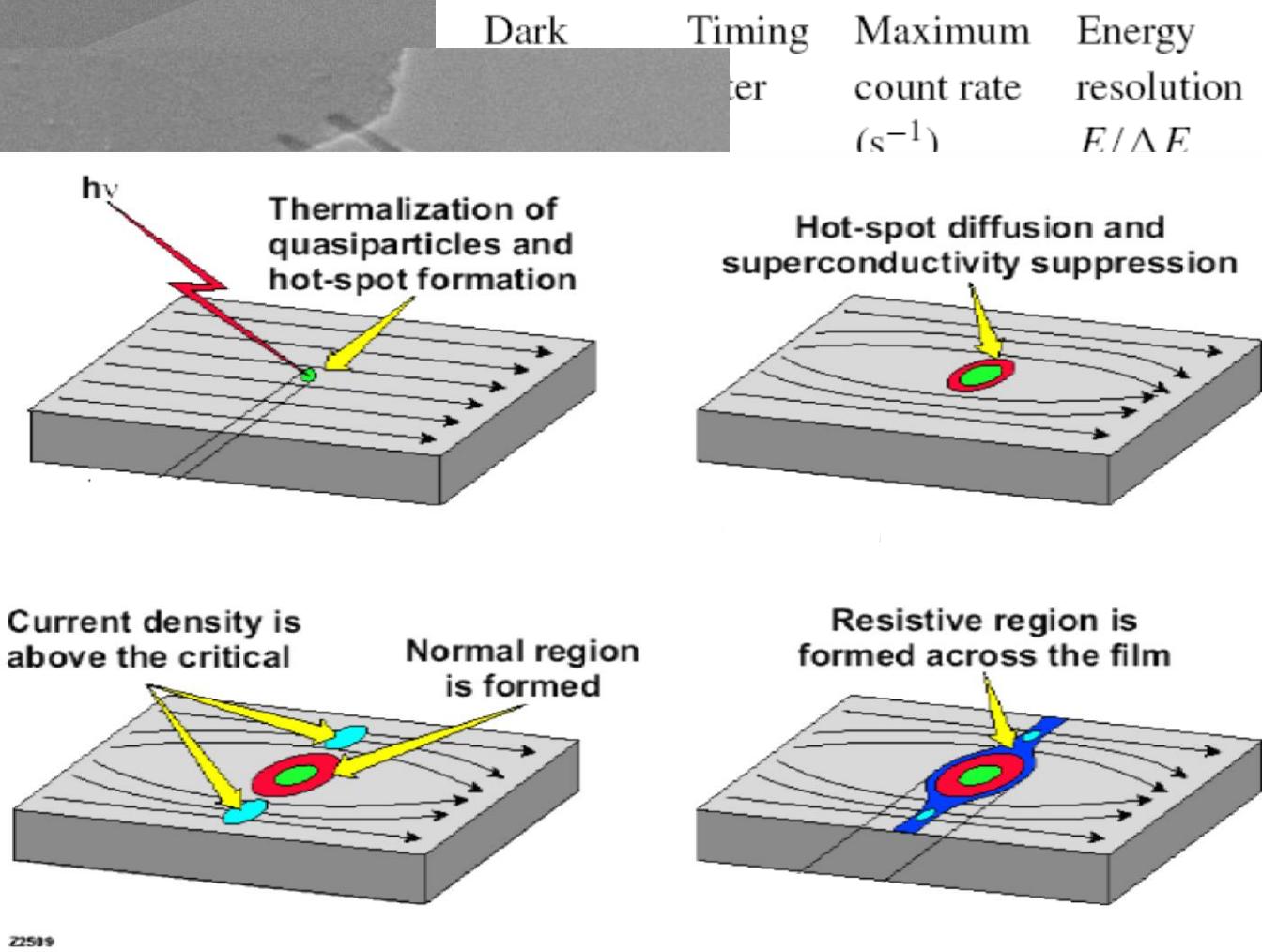
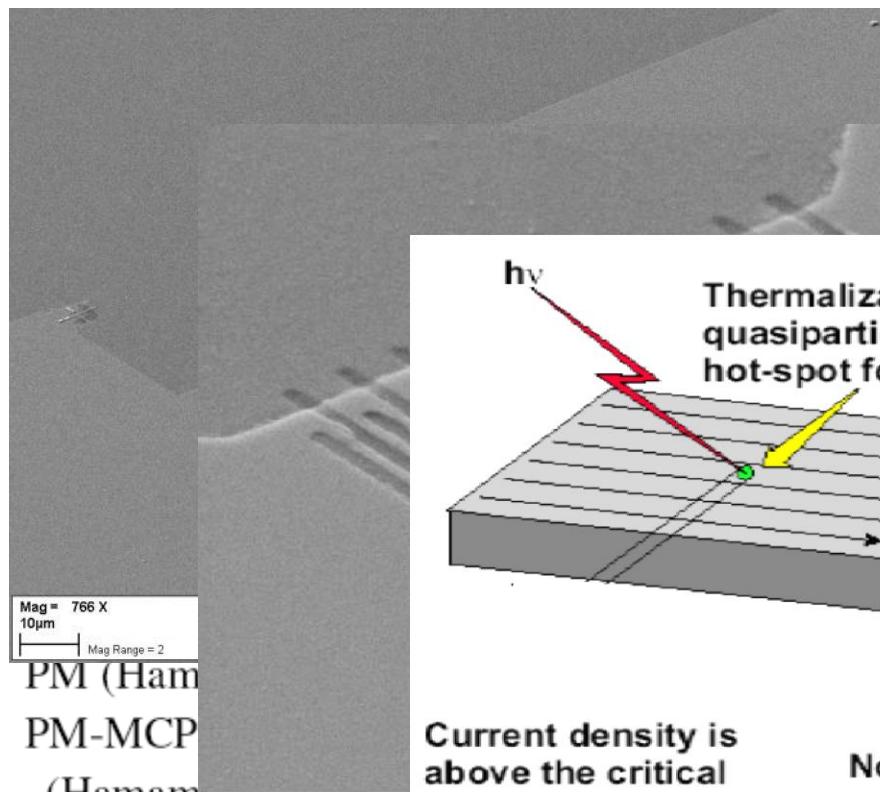
## ■ AC Josephson effect



„Inverse Josephson effect“

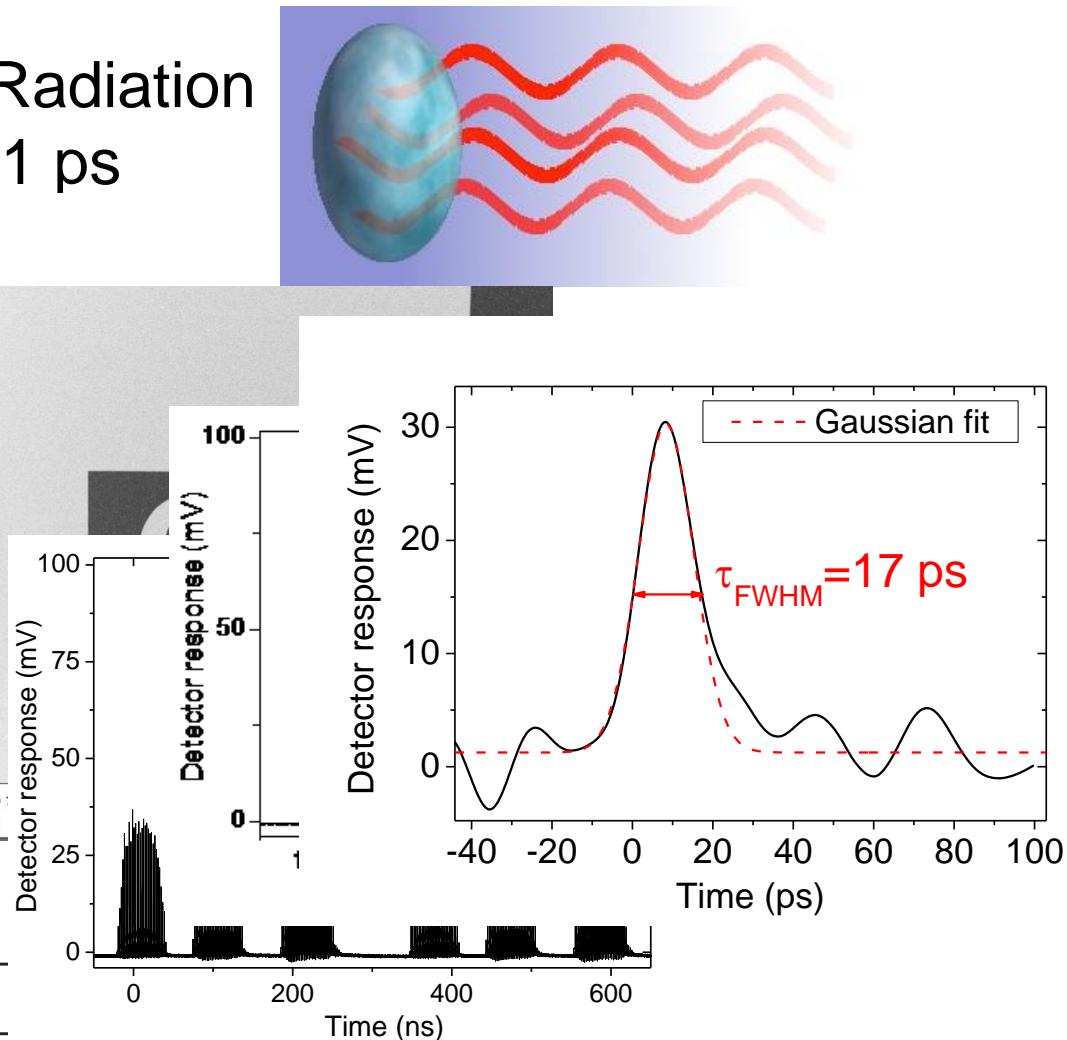
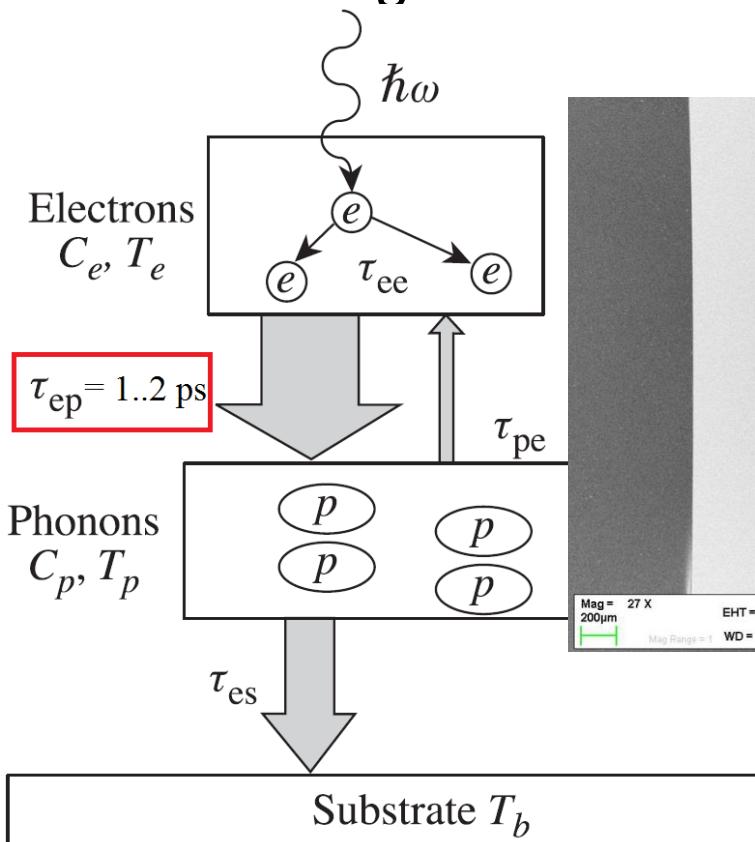
$$K_{J-90} = \frac{2e}{h} = 483,5979 \frac{\text{GHz}}{\text{mV}}$$

# Quantum electronics: Single Photon Detection



# Ultra-fast THz detection with $\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$

- Coherent Synchrotron Radiation bunch lengths down to 1 ps



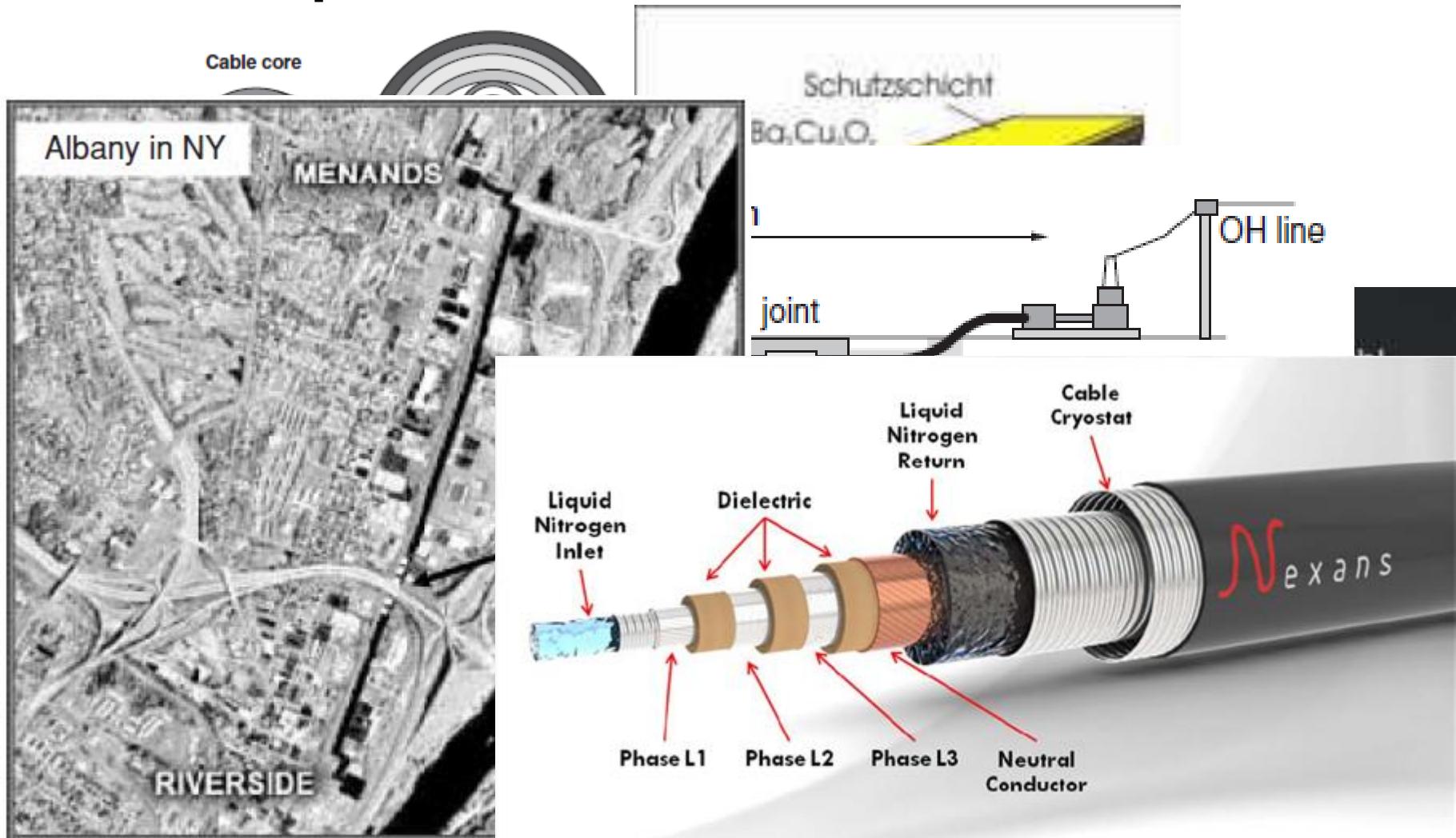
M. Klein, Studies of Bunch Distortion in the Generation of Coherent THz-Radiation at the ANKA Storage Ring, DPG 2009  
 A.D. Semenov, G.N. Gol'tsman, R. Sobolewski, Supercond. Sci. Technol. 15, R1 (2002)

# Magnetic Levitation Systems



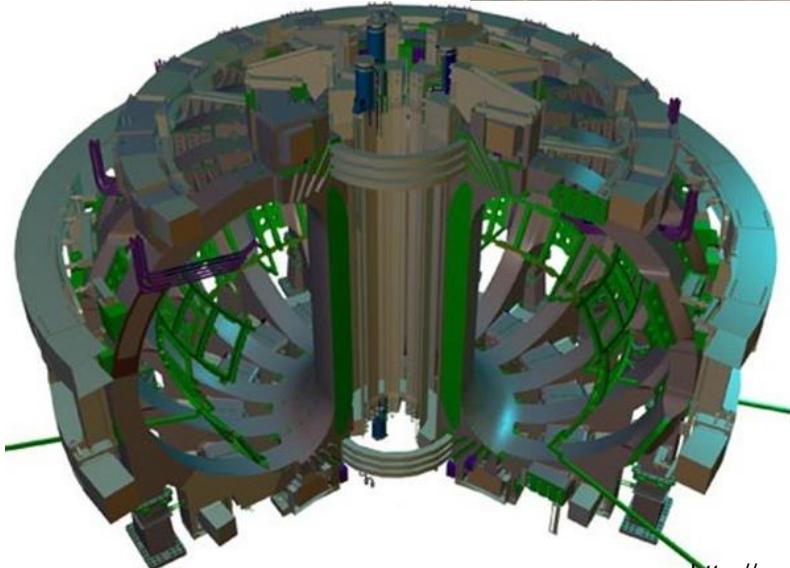
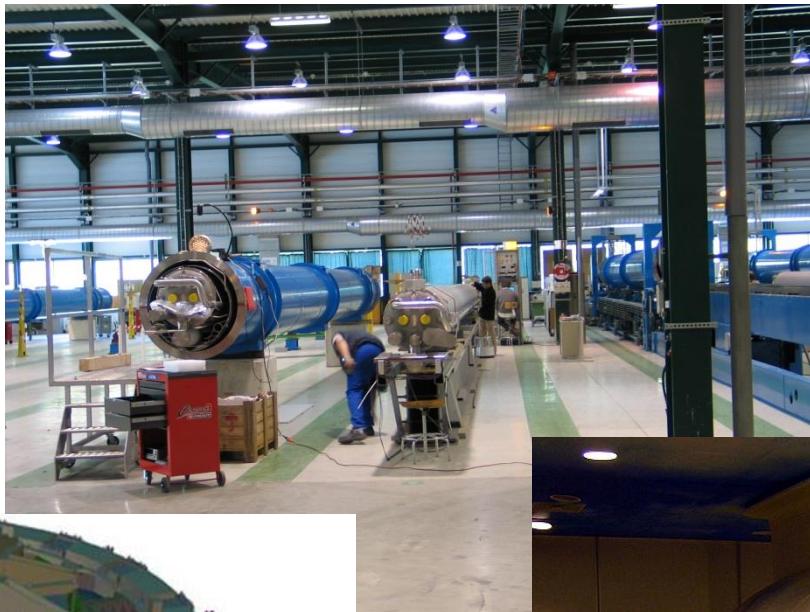
<http://en.wikipedia.org>

# Low-loss power cables



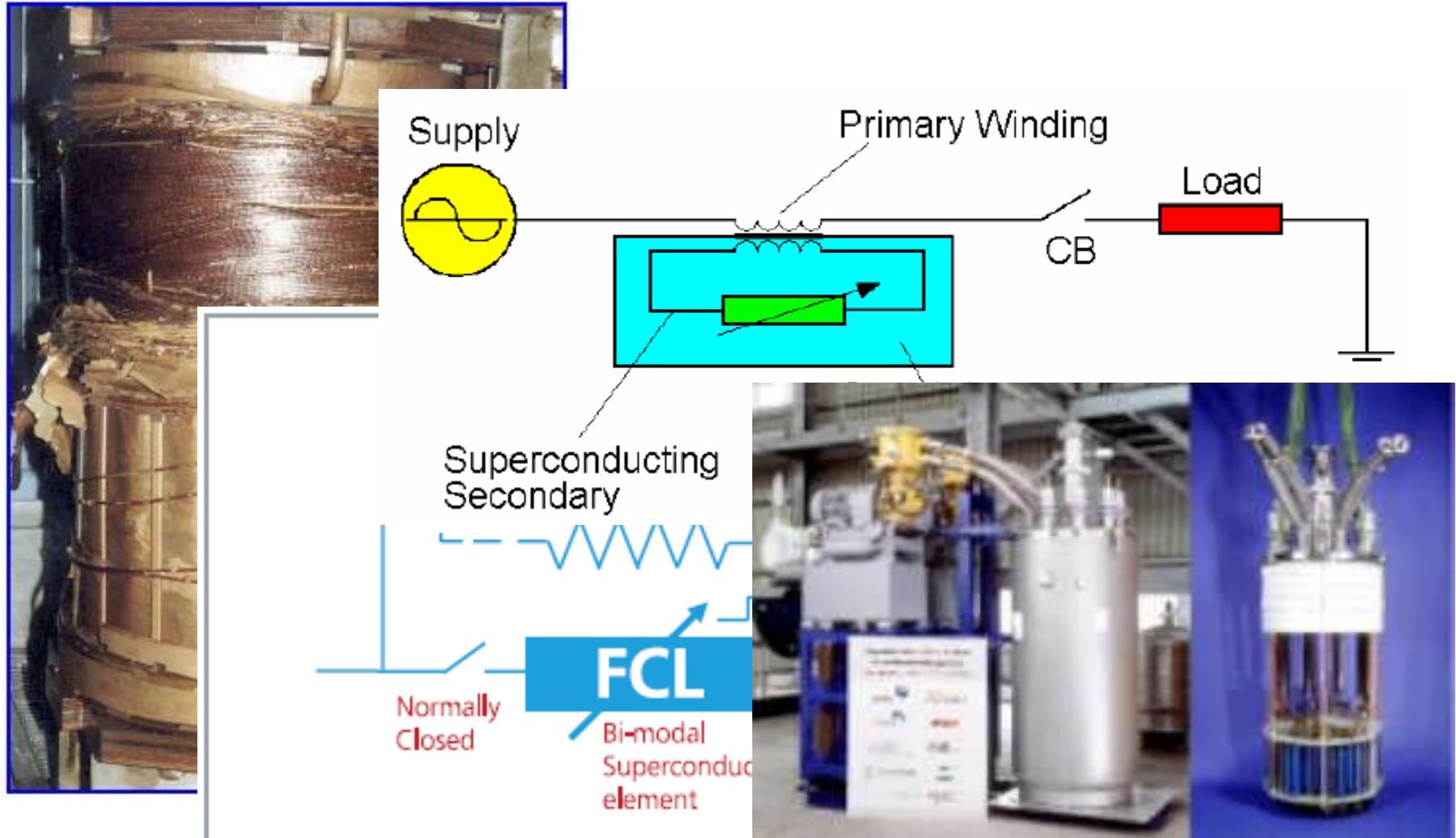
T. Masuda et al., High-temperature superconducting cable technology and development trends  
<http://www.nexans.de>, <http://www.itep.kit.edu/66.php>

# Superconducting Coils



<http://en.wikipedia.org>, <http://www.iter.org/mach/magnets>, <http://lhc-machine-outreach.web.cern.ch>

# HTS Fault Current Limiters



F. Mumford, Inductive and Resistive HTS Fault Current Limiters: Prototyping, Testing, Comparing  
<http://www.amsc.com>, <http://www.itep.kit.edu/21.php>

# Thank you for your Attention



Great thanks to H. Neumann, M. Süßer, M. Schrank  
and to C. Kaiser, M. Meckbach  
for their contribution to this talk



Zwei  $e^-$  stoßen sich eigentlich ab (Coulomb-Kraft)

Im Festkörper:

- Durch **Atomgitter** kann effektive Anziehung entstehen
- Erklärung 1: Austausch von virtuellem Phonon
- Erklärung 2: Polarisierung des Gitters
- Bindungsenergie im meV-Bereich

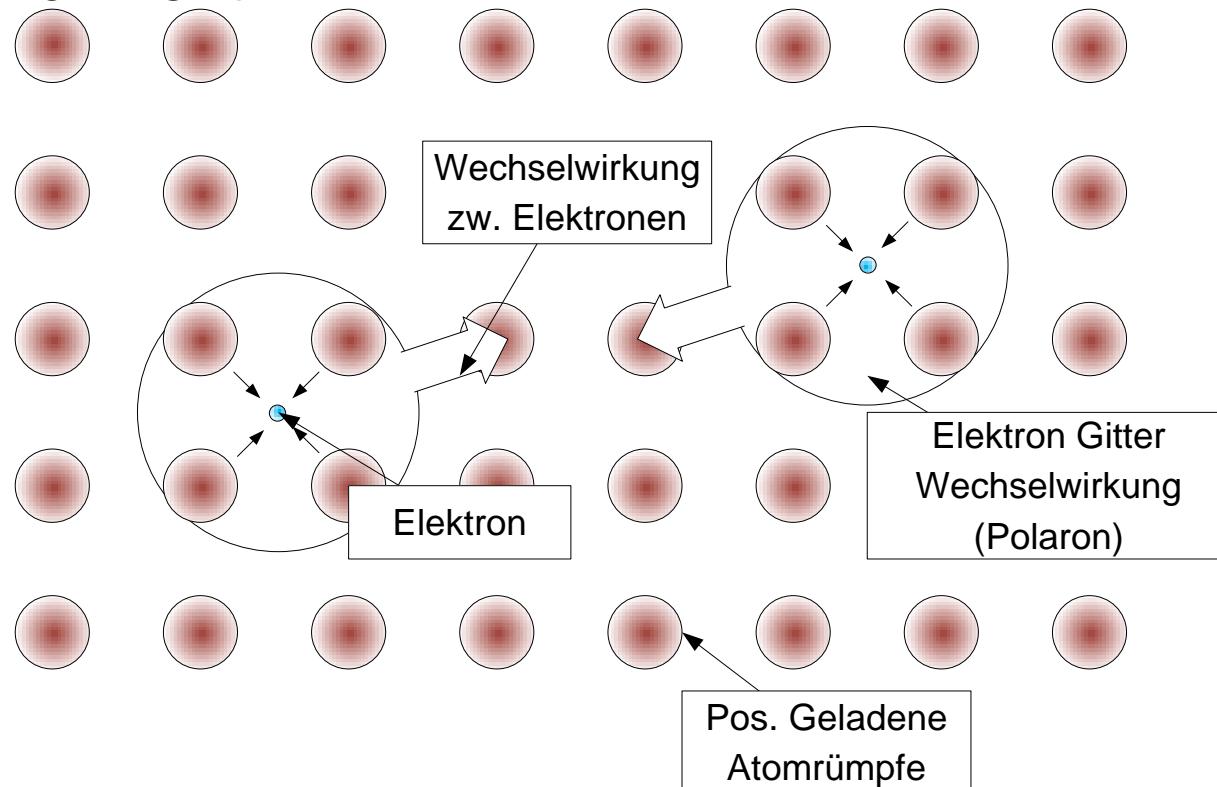
→ Cooper-Paare können nur in FK auftreten!

→ Beleg für Rolle des Atomgitters: Isotopieeffekt:

$$T_c \sim M^\alpha, M = \text{Atommasse}$$

# Bildung der Cooper Paare in einem Kristall

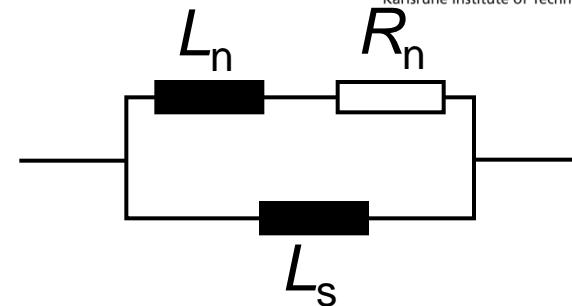
- Das 1. Elektron zieht die positiven Atomrumpfe zusammen. Das Elektron bewegt sich schneller als die Atomrumpfe, es bildet sich eine lokale Polarisation die das 2. Elektron anzieht



# HF-Eigenschaften

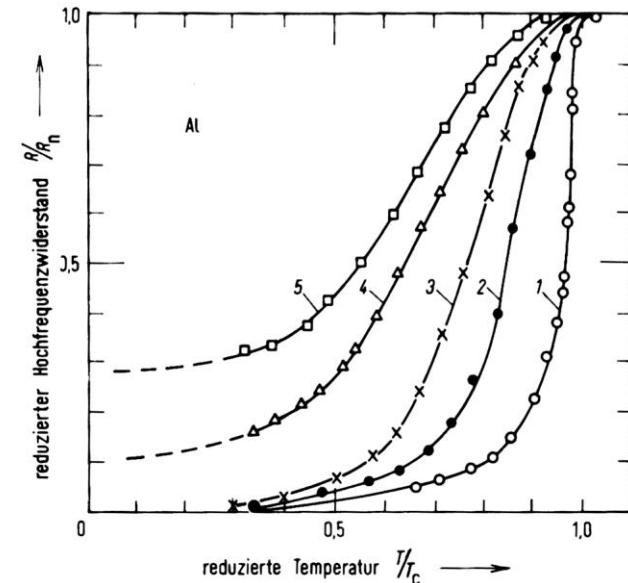
Hochfrequenzverhalten von SL:

- Zwei-Flüssigkeits-Modell



- a) CP: haben Masse, d.h. Trägheit  
→ Müssen beschleunigt werden →  $L_s \neq 0$
- b) Quasiteilchen (QT):  $R_n$ ,  $L_n$   
→ Je mehr QT, desto höher  $R_{HF}$
- Frequenzen  $hf > 2\Delta$ :  
(Fast) wie Normalleiter

→ Vortrag von Herrn Brengartner!



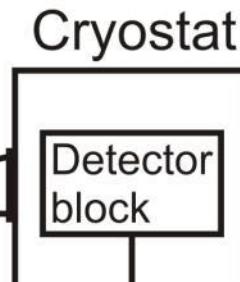
# YBCO THz measurements at ANKA, MLS and UVSOR-II



THz beam line



off-axis  
mirror



65 GHz

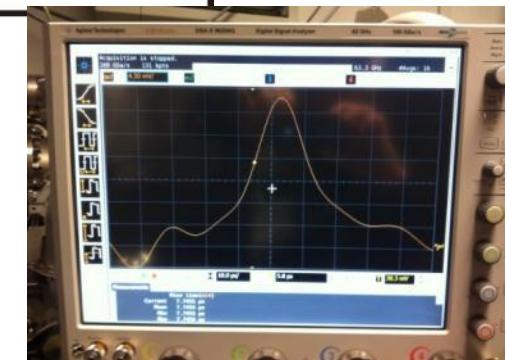


Bias  
Source

55 GHz

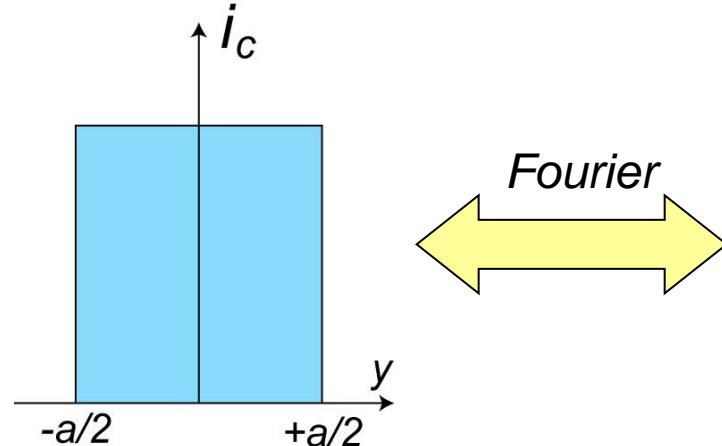
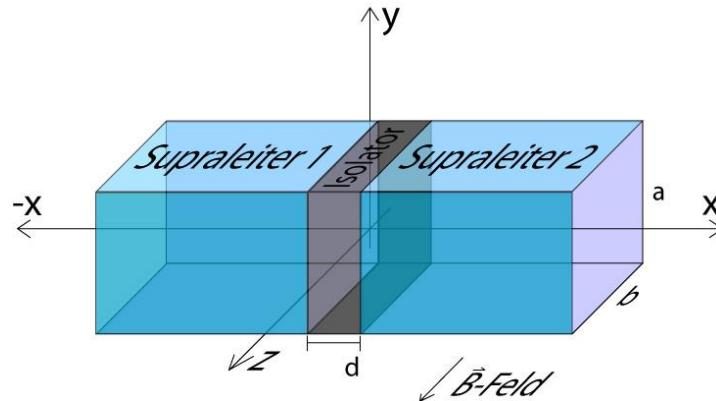


63 GHz  
Agilent  
Oscilloscope

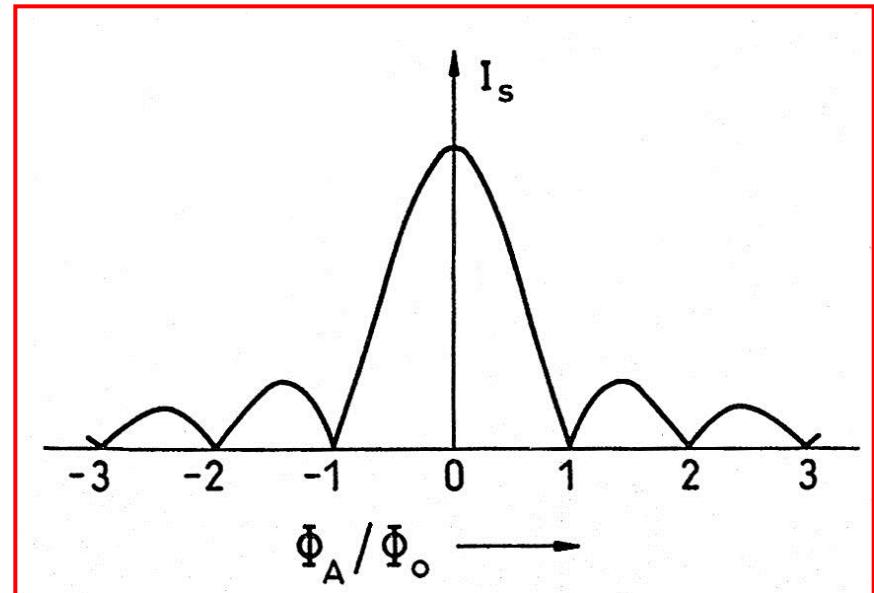


# Quantum electronics: SQUIDs

- Superconducting QUantum Interference Device
- Josephson junction in magnetic field



$$I_s = I_C \cdot \sin(\gamma_0) \cdot \sin\left(\pi \frac{\Phi_A}{\Phi_0}\right)$$



# Quantum electronics: SQUIDs

## ■ Superconducting QUantum Interference Device

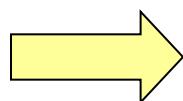
$$I_S = I_C \sin \gamma_1 + I_C \sin \gamma_2$$

$$I_S = 2I_C \cos\left(\frac{\gamma_1 - \gamma_2}{2}\right) \cdot \sin\left(\frac{\gamma_1 + \gamma_2}{2}\right)$$

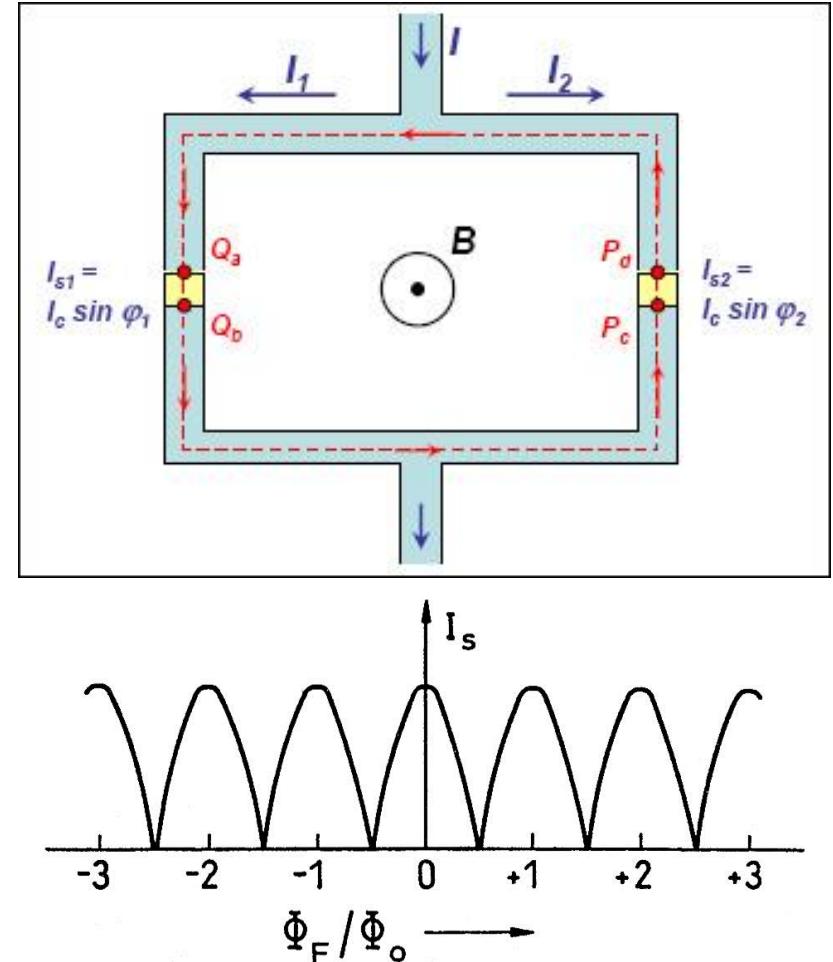
$\rightarrow \gamma_2 - \gamma_1 = 2\pi \cdot n + 2\pi \frac{\Phi_F}{\Phi_0}$

$$I_S = 2I_C \cos\left(\pi \frac{\Phi_F}{\Phi_0}\right) \cdot \sin\left(\gamma_1 + \pi \frac{\Phi_F}{\Phi_0}\right)$$

$\tilde{I}_C$                                      $\tilde{\gamma}$



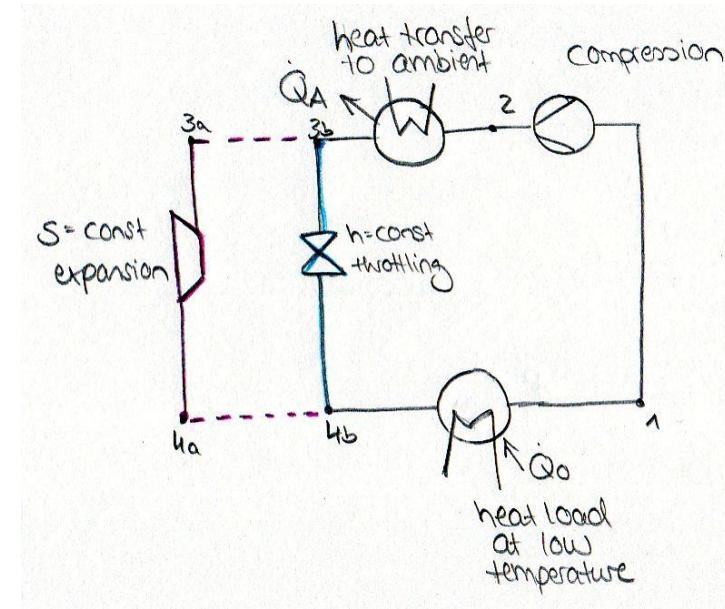
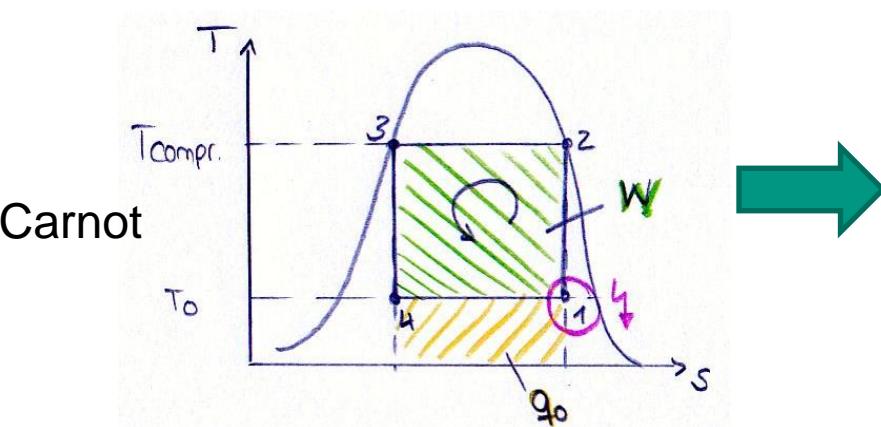
$I_S = \tilde{I}_C \cdot \sin \tilde{\gamma}$



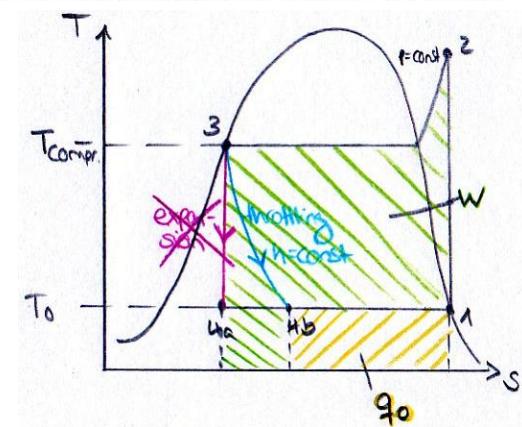
# Cold production (Basic)

- Basic principle:
  - Compression
  - Heat transfer to ambient
  - Throttling/ expansion
  - Heat load at low temperature

- Carnot:
  - Ideal process (best  $q_0/w$ )
  - Liquid yields problem for compressor & turbine

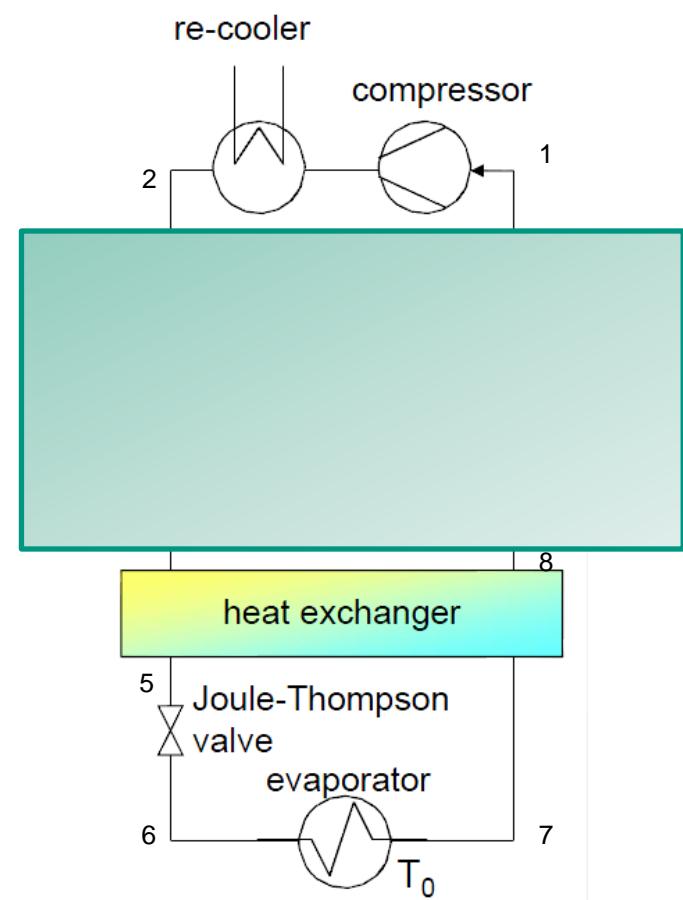
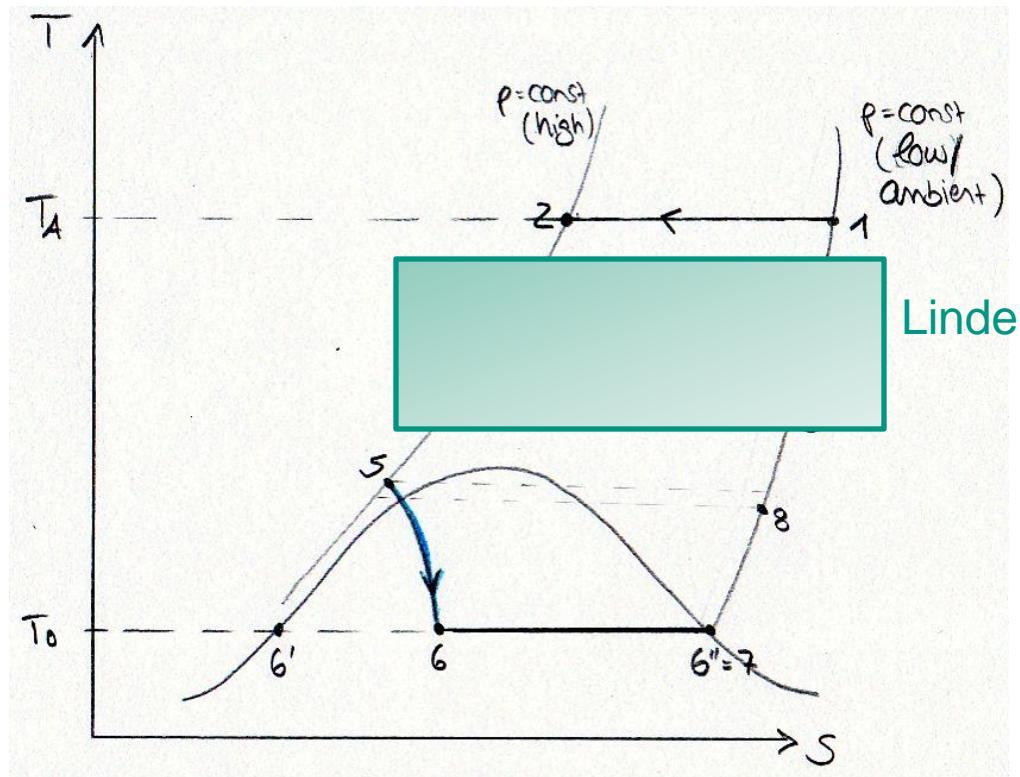


Clausius  
Rankine



# Cold production (Refrigeration Cycles)

## ■ Claude / Linde-Process



Source:  
 H. Neumann, IETP, KIT, 2013 ESAS  
 Summer School

# Cold production (refrigeration / liquefaction)

## ■ Refrigeration cycle

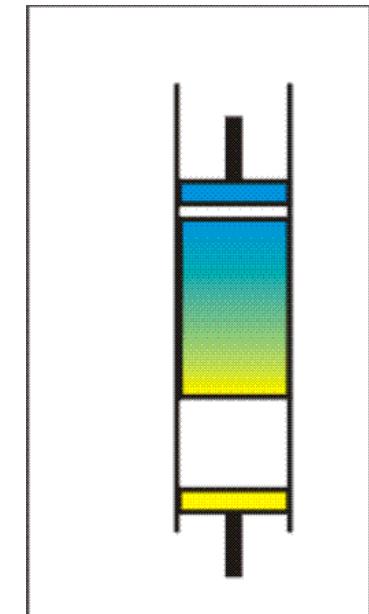
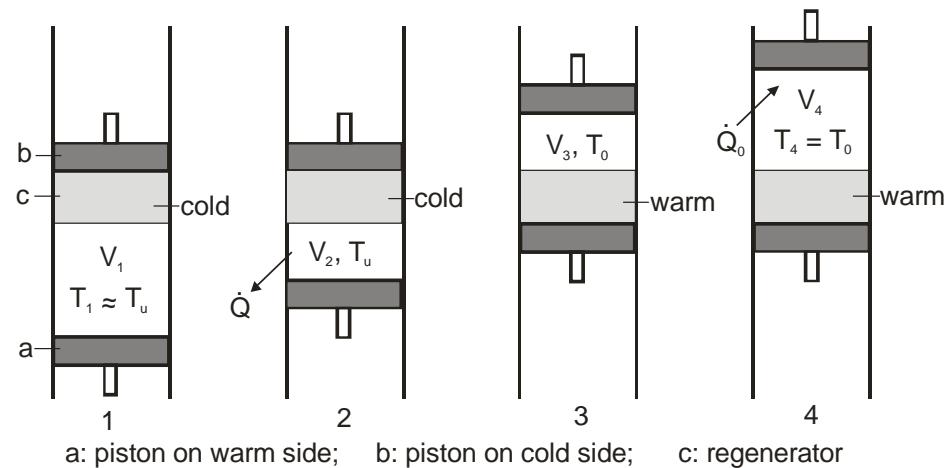
### ■ Stirling-process

#### ■ Advantages

- high efficiency
- compact

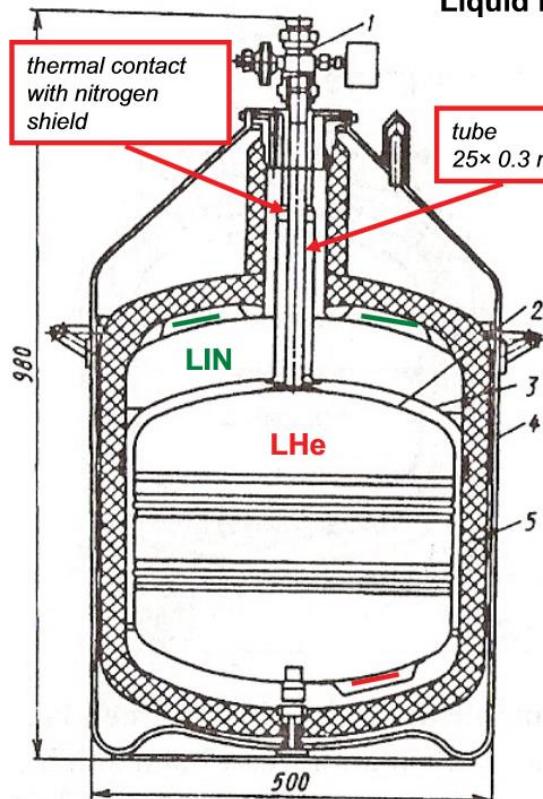
#### ■ Disadvantages

- no liquefaction
- mechanical movements in cold part
- additional cold cycles are needed to transport the refrigeration power to consumer far away



# Cryostats (Dewars)

## Dewar vessel



Liquid Helium Dewar vessel with LIN shielding

Capacity: 40 liters

Liquid helium volume: **28 Nm<sup>3</sup>**

**Remember:** 700 liters gas from 1 liter liquid

1 – valve head with thread connections for liquid fill and gas withdrawal, manometr and safety membrane.

2 – inner vessel (12Cr18Ni1.0T)

3 – nitrogen vessel (12Cr18Ni1.0T) with nitrogen shield (copper – high thermal conductivity for uniform temperature)

4 - outer jacket

5 – multilayer vacuum insulation

high vacuum between the inner vessel and the nitrogen shield

getter at nitrogen temperature

getter at helium temperature

[Arkharov et all., Cryogenic Systems]

Source: V. Chrz

<http://indico.cern.ch/getFile.py/access?sessionId=3&resId=0&materialId=0&confId=90787>