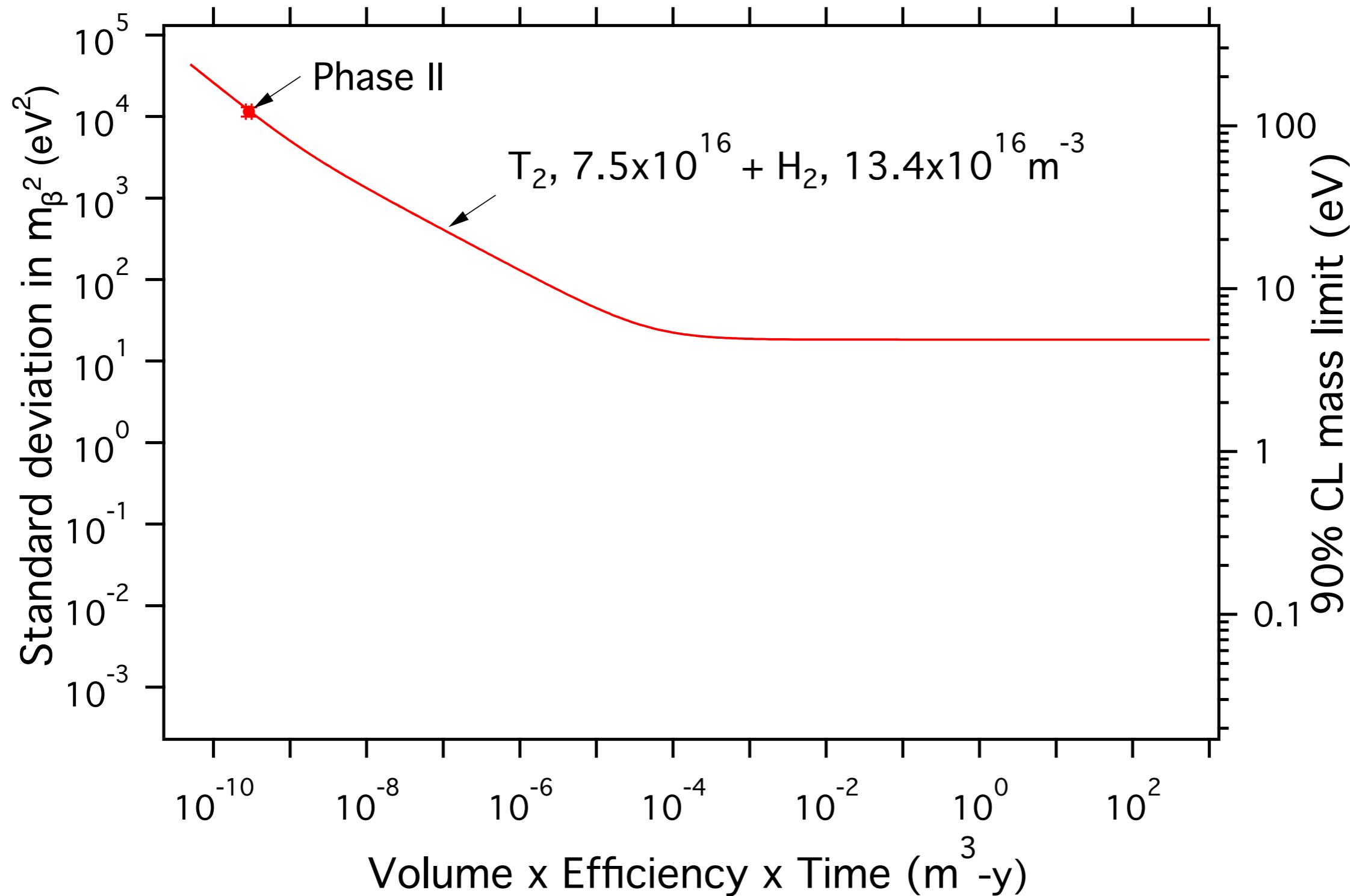


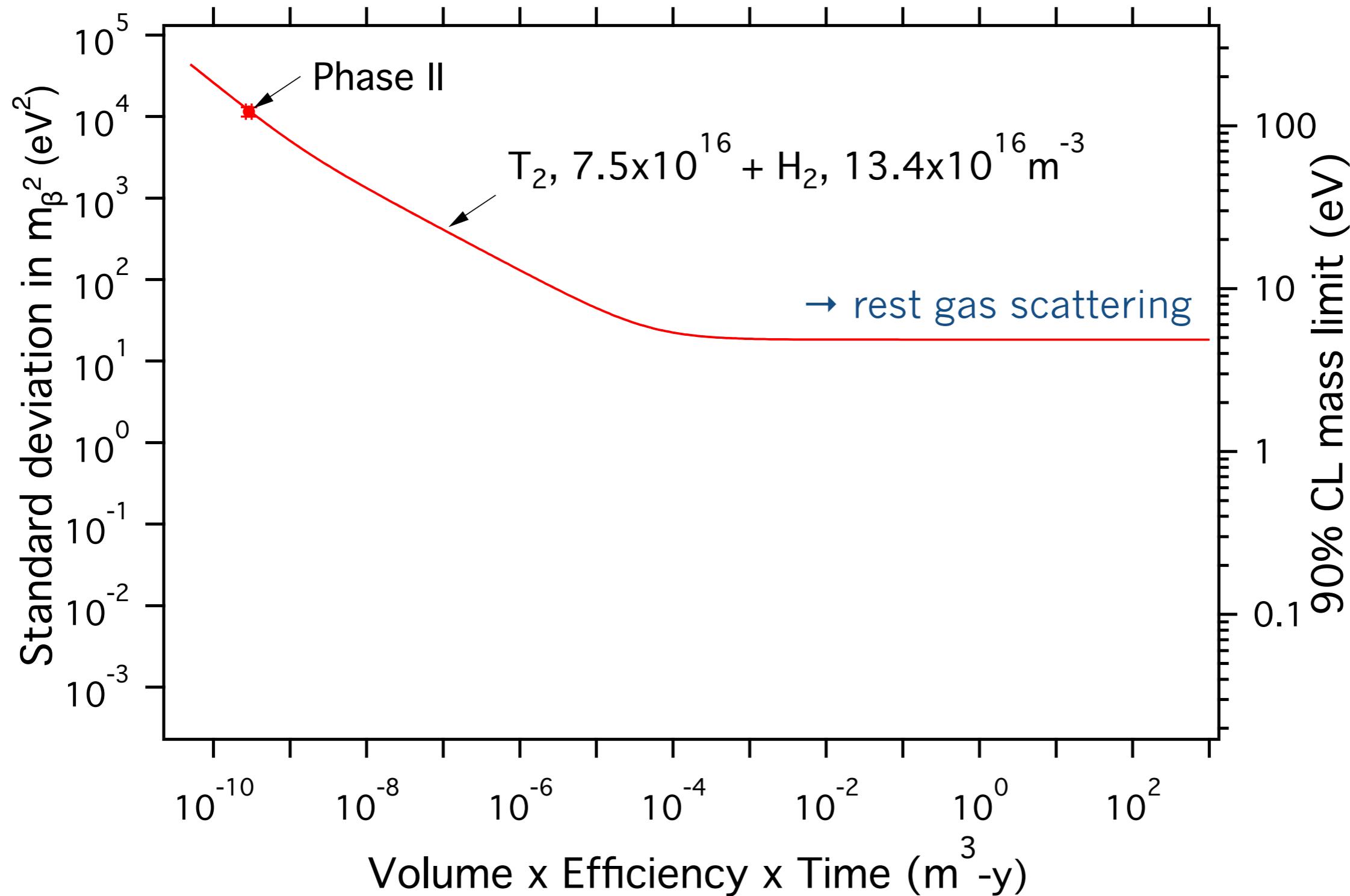
# Towards an atomic tritium source for Project 8

Sebastian Böser  
30 years TLK Symposium | Karlsruhe | May 24<sup>nd</sup> 2023

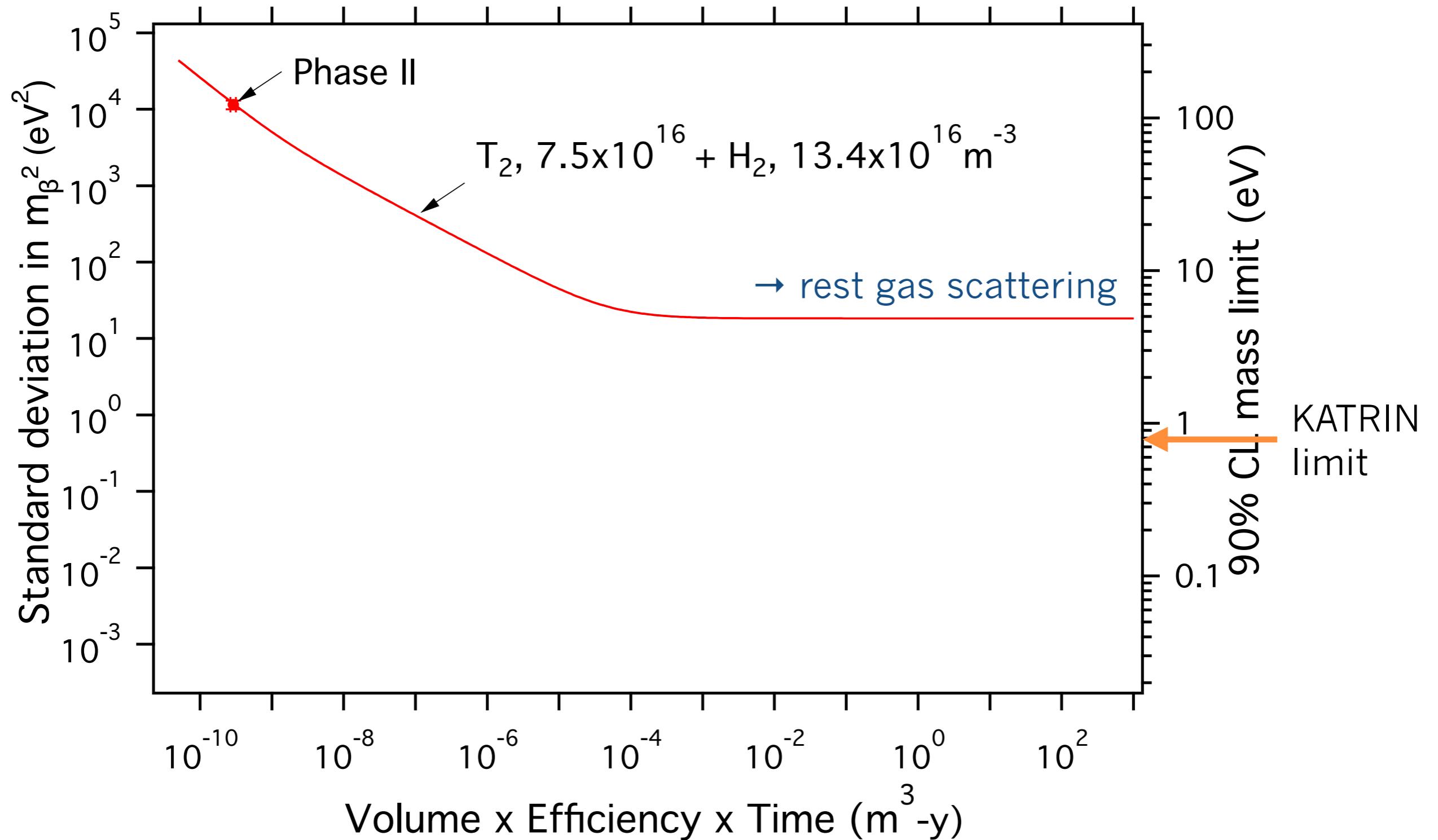
# Potential for neutrino mass?



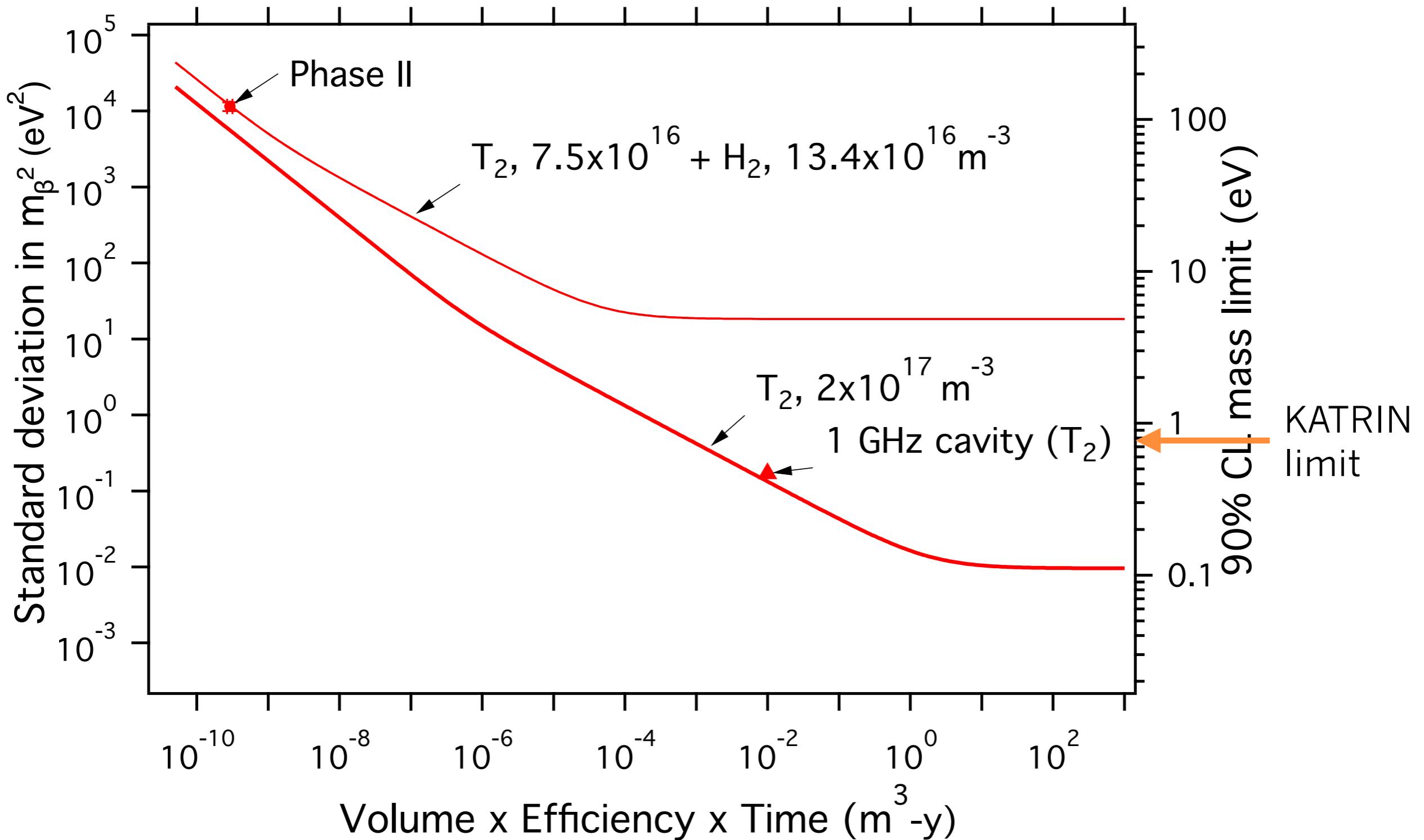
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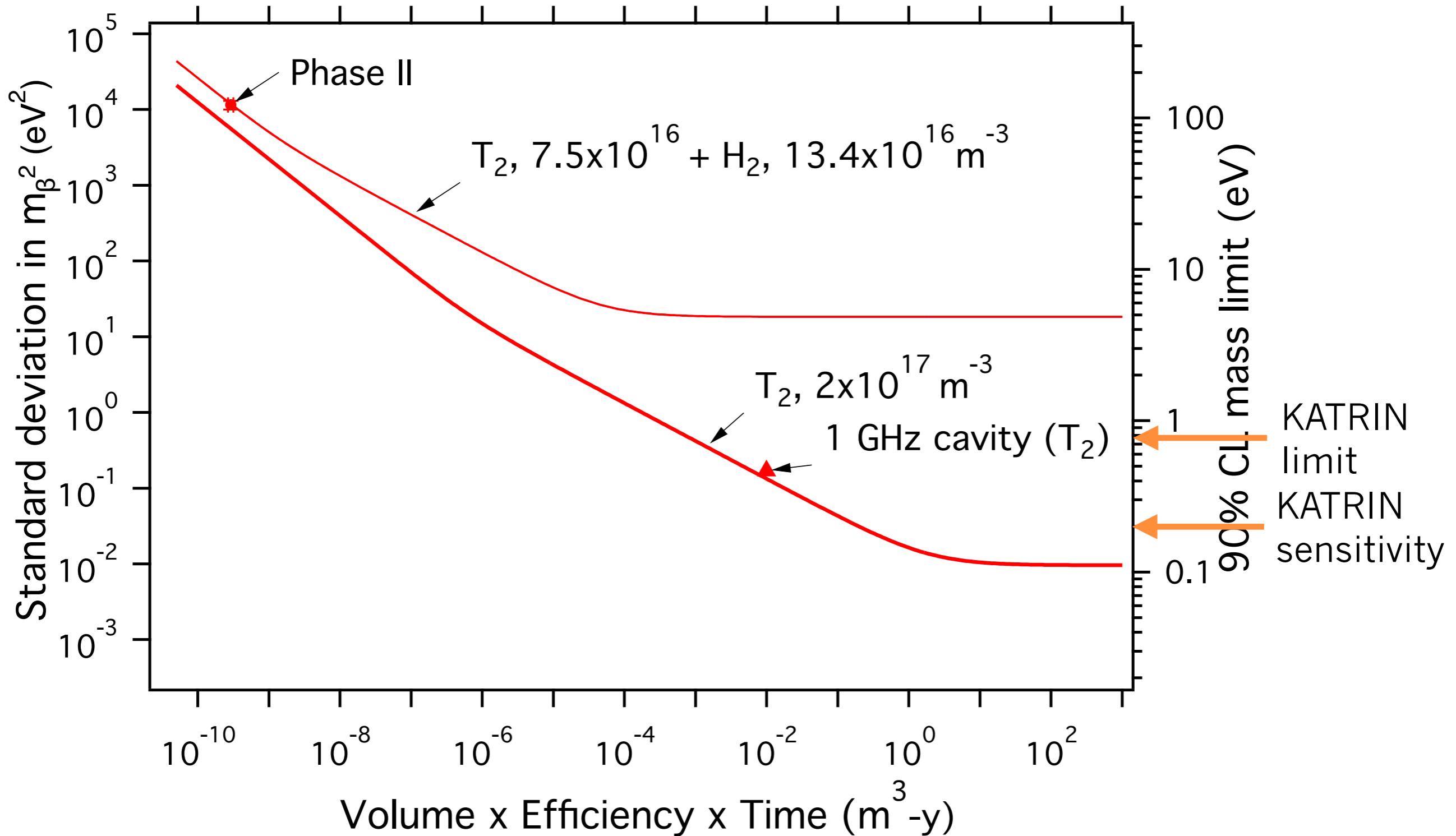
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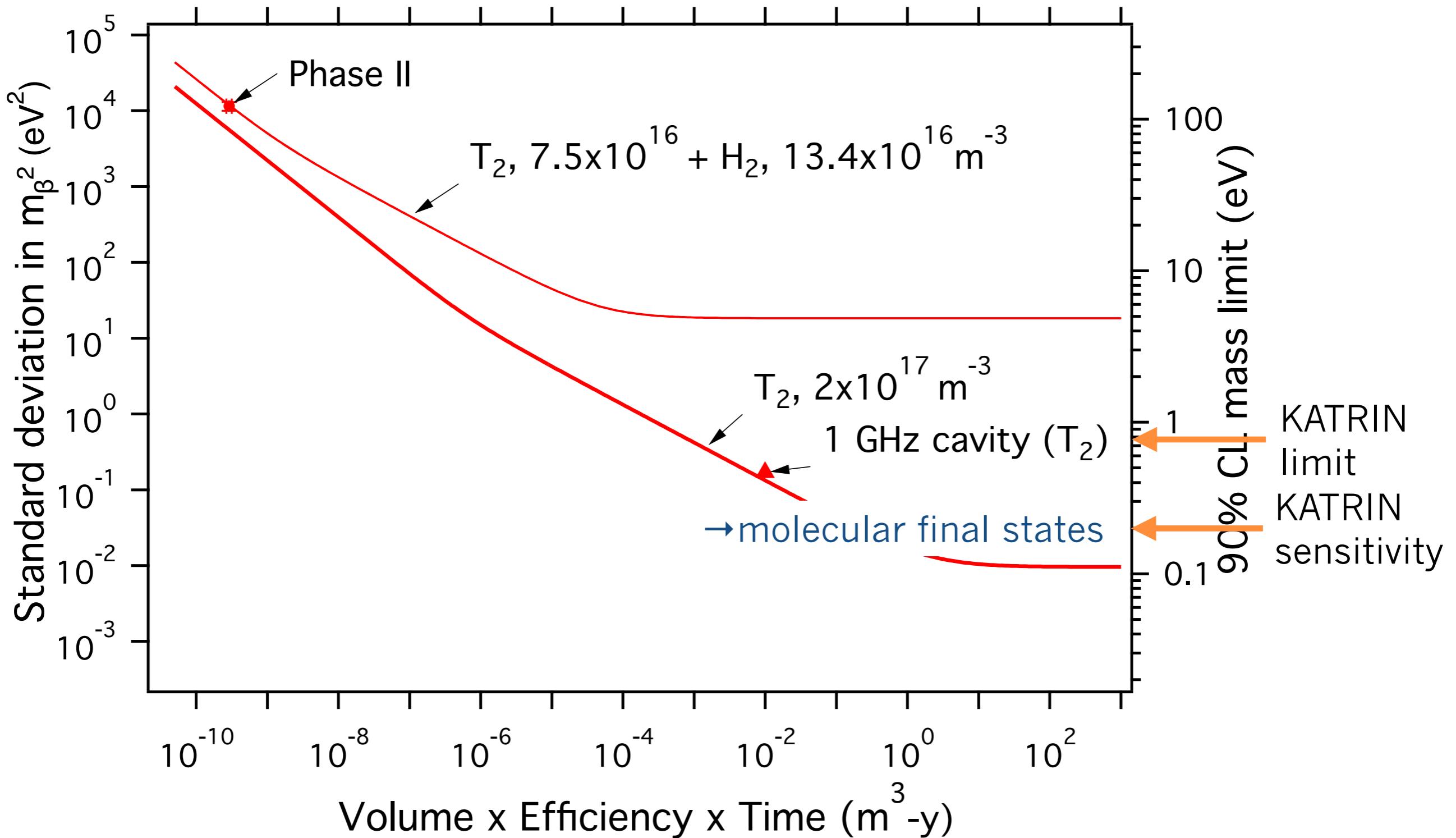
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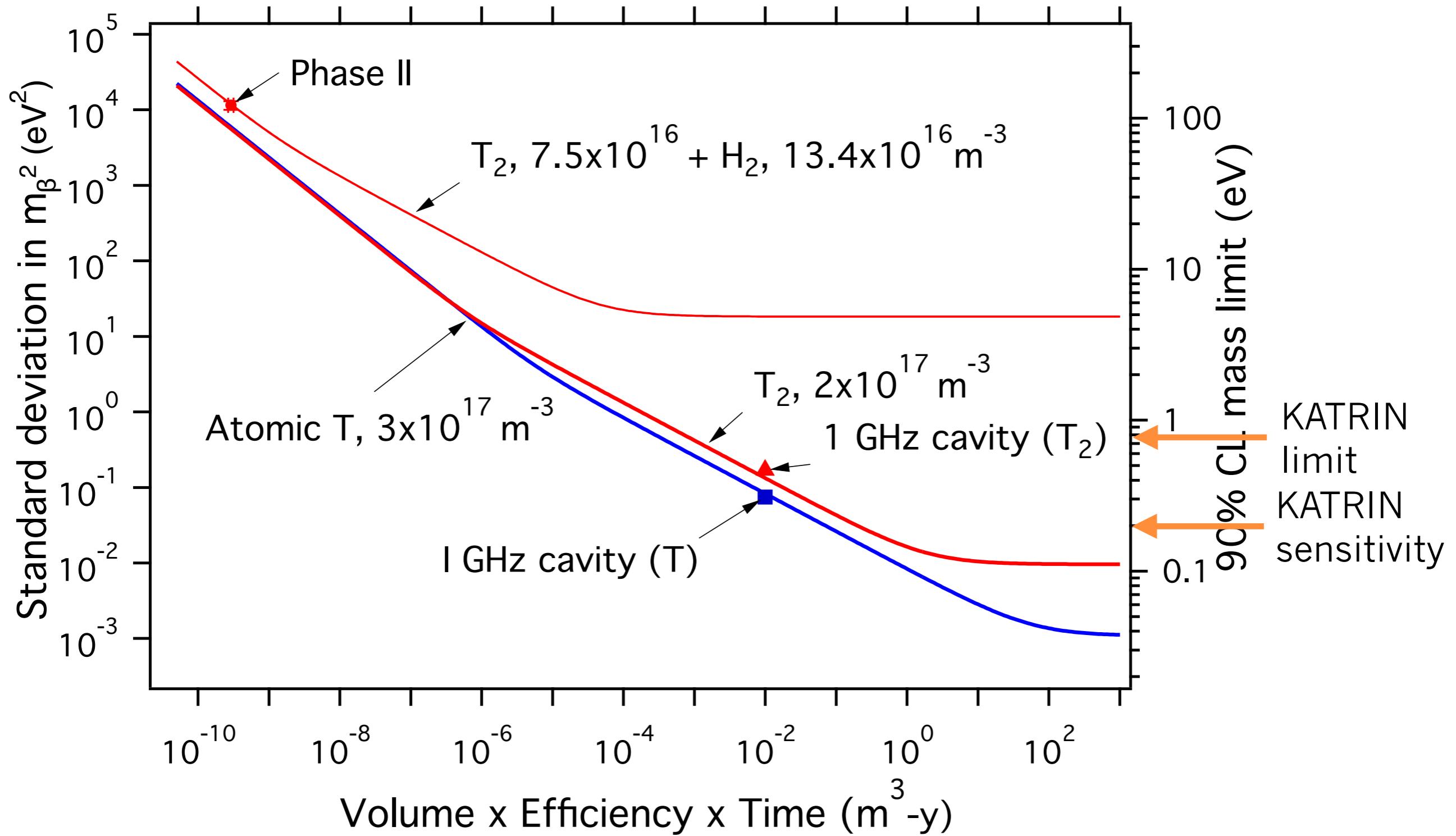
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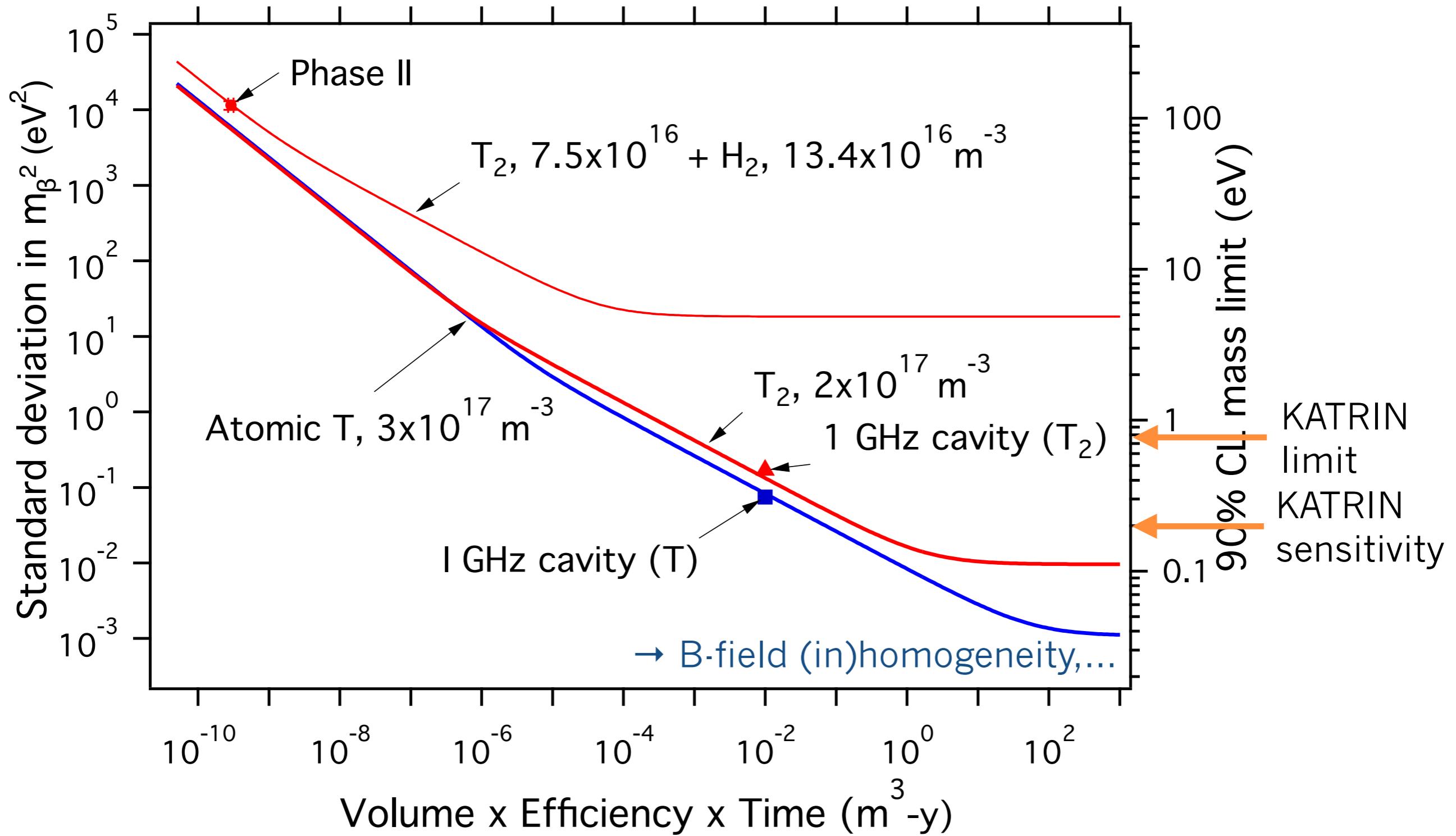
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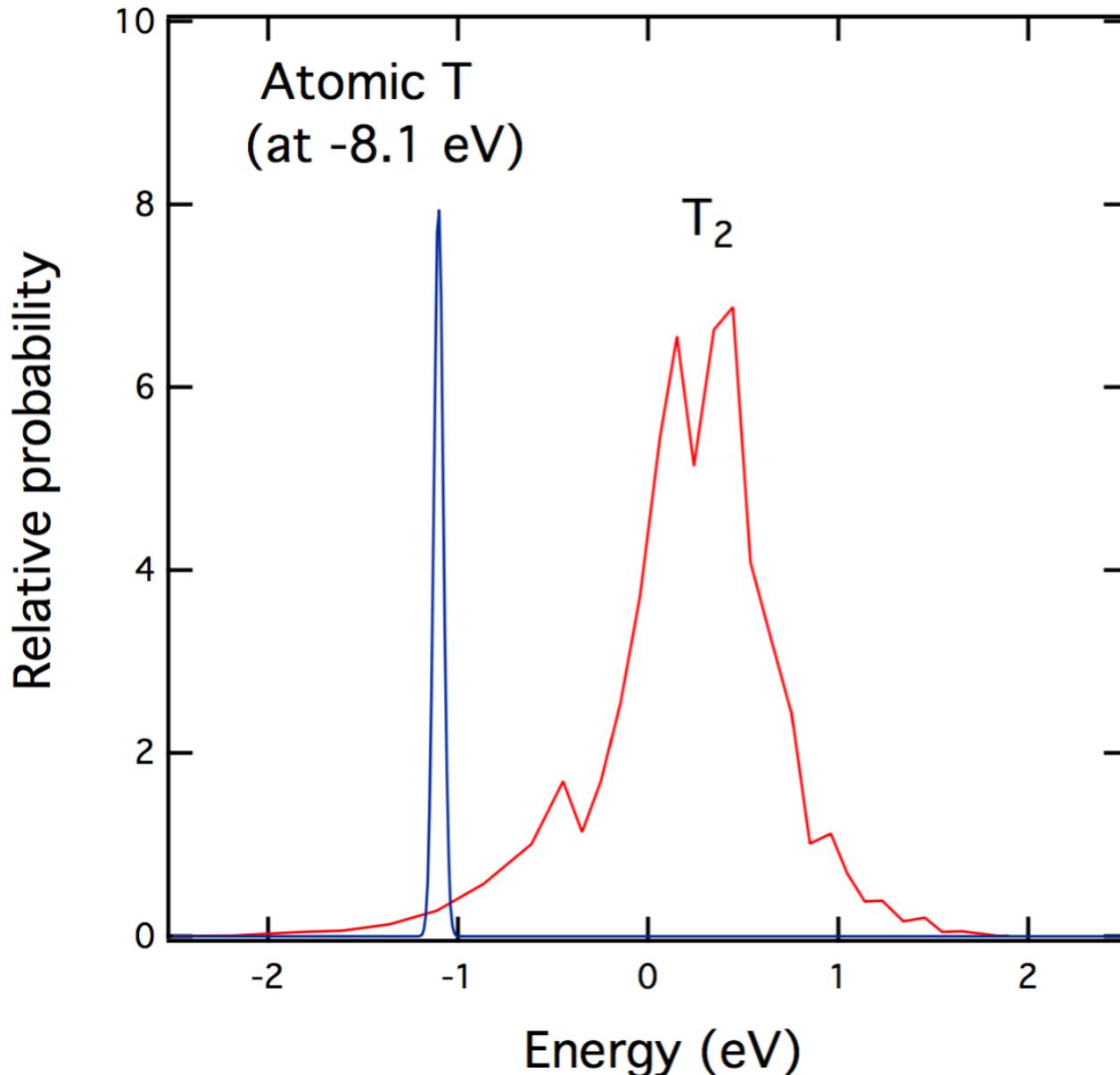
# Potential for neutrino mass?



# Potential for neutrino mass?



# Molecular tritium limitations



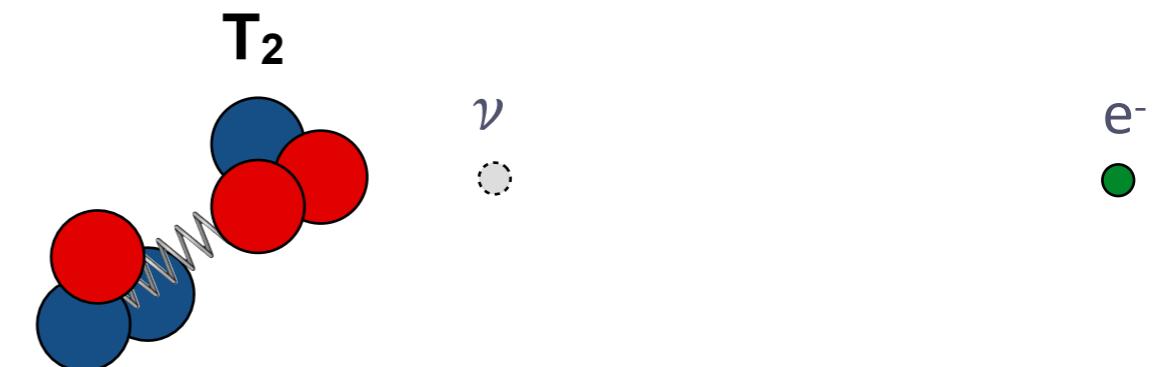
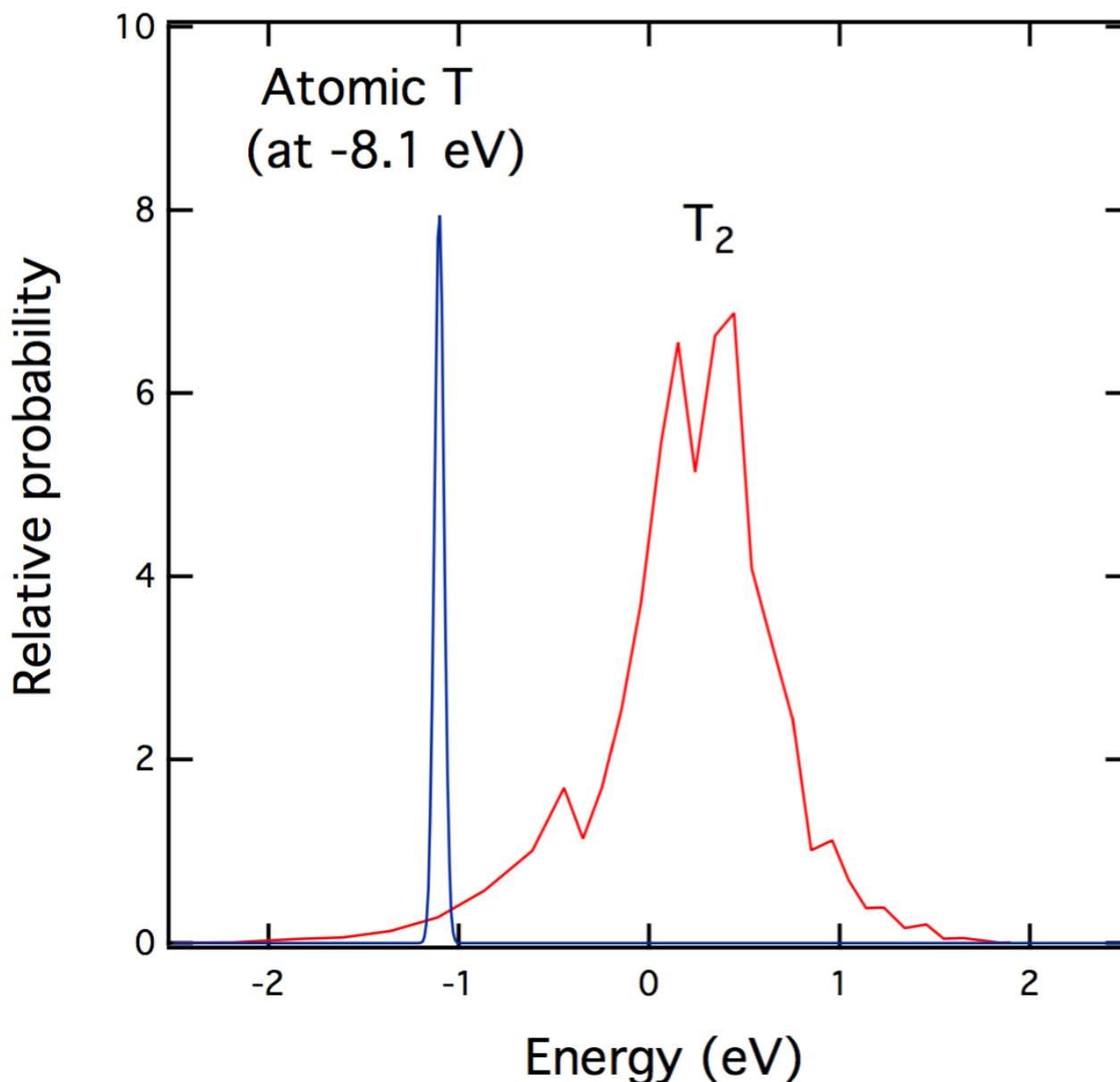
$T_2$

Molecular excitations  
in  ${}^3\text{HeT}$  daughter molecule

- blur tritium endpoint
- ▶ fundamental limit to measurement of  $\nu$ -mass

Need atomic tritium for **ultimate** experiment!

# Molecular tritium limitations

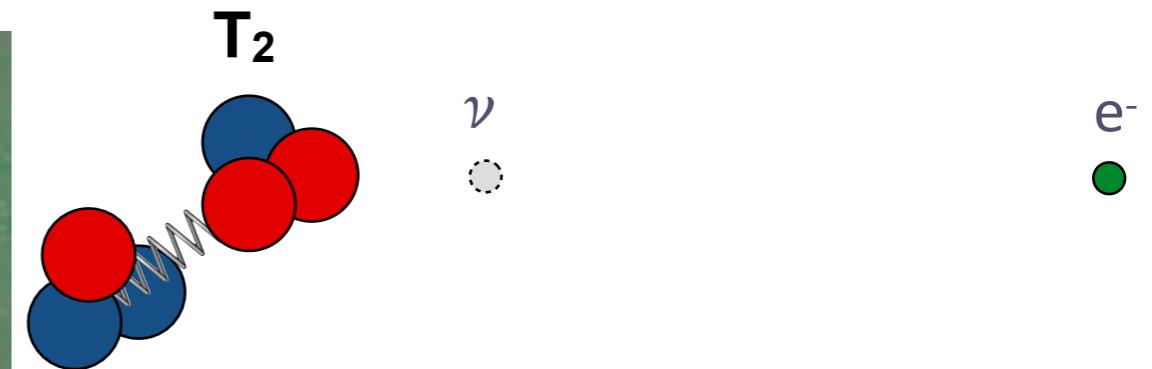
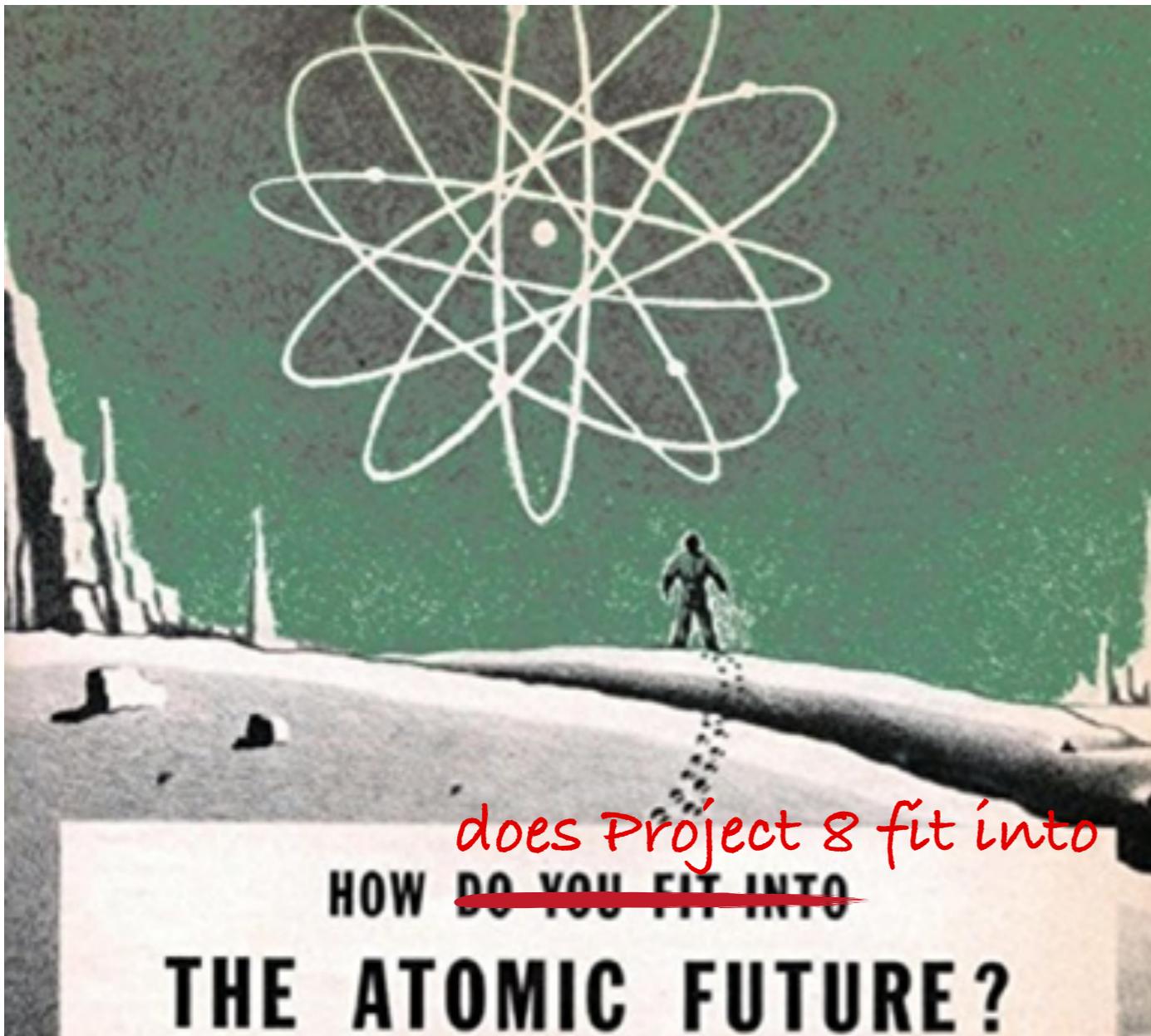


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# Magnetic storage of neutral atoms

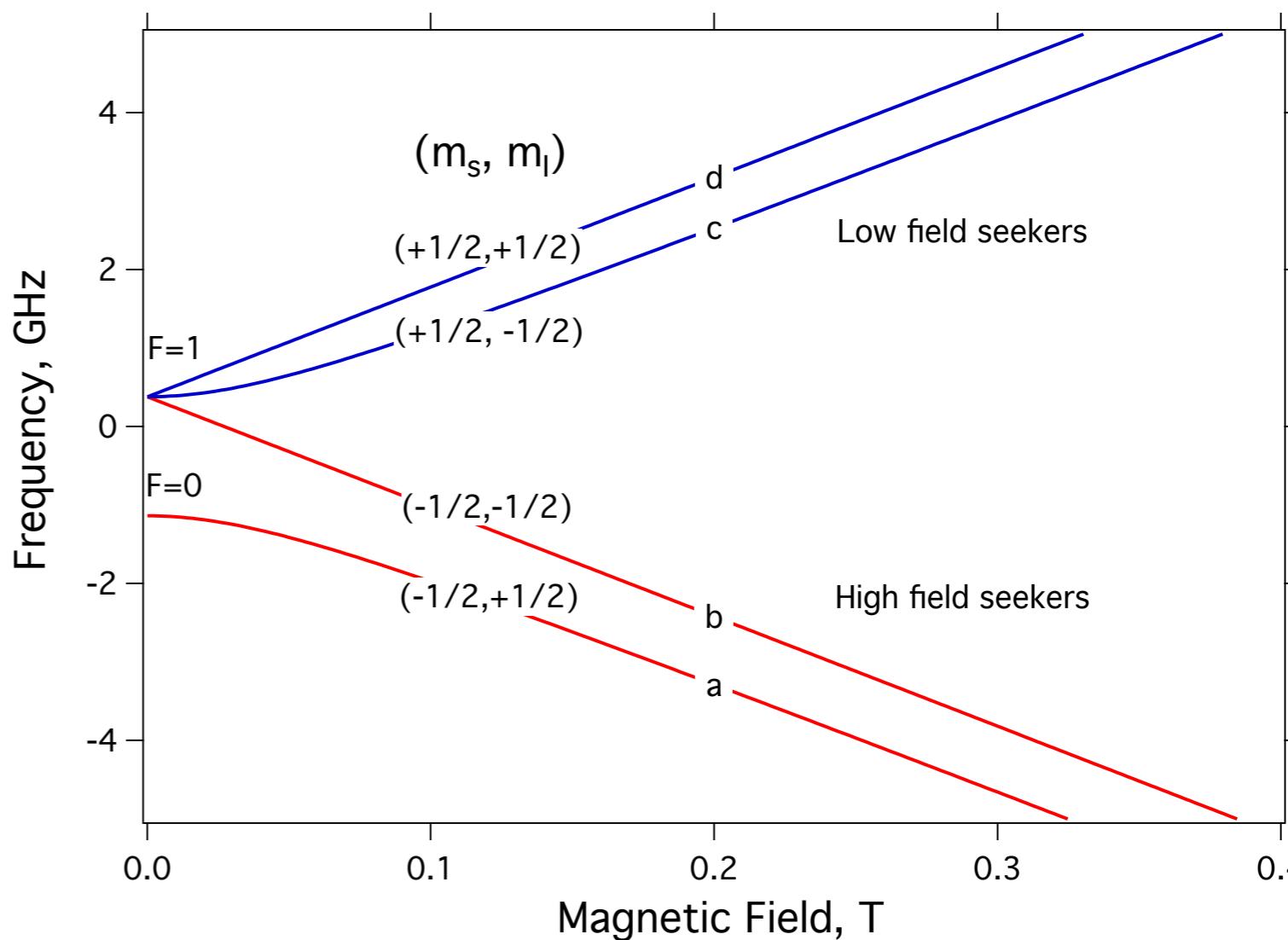
## Storage of atomic T

- recombination catalyzed by walls  
→ difficult!

- H,D and T have unpaired  $e^-$ 
  - ▶ non-zero magnetic moment  $\mu$
  - ▶ tend to (anti-)align with B-field if change is adiabatic

## Potential energy

- $\Delta E = -\vec{\mu} \cdot \vec{B}$   
→ half of spin states seek field minimum



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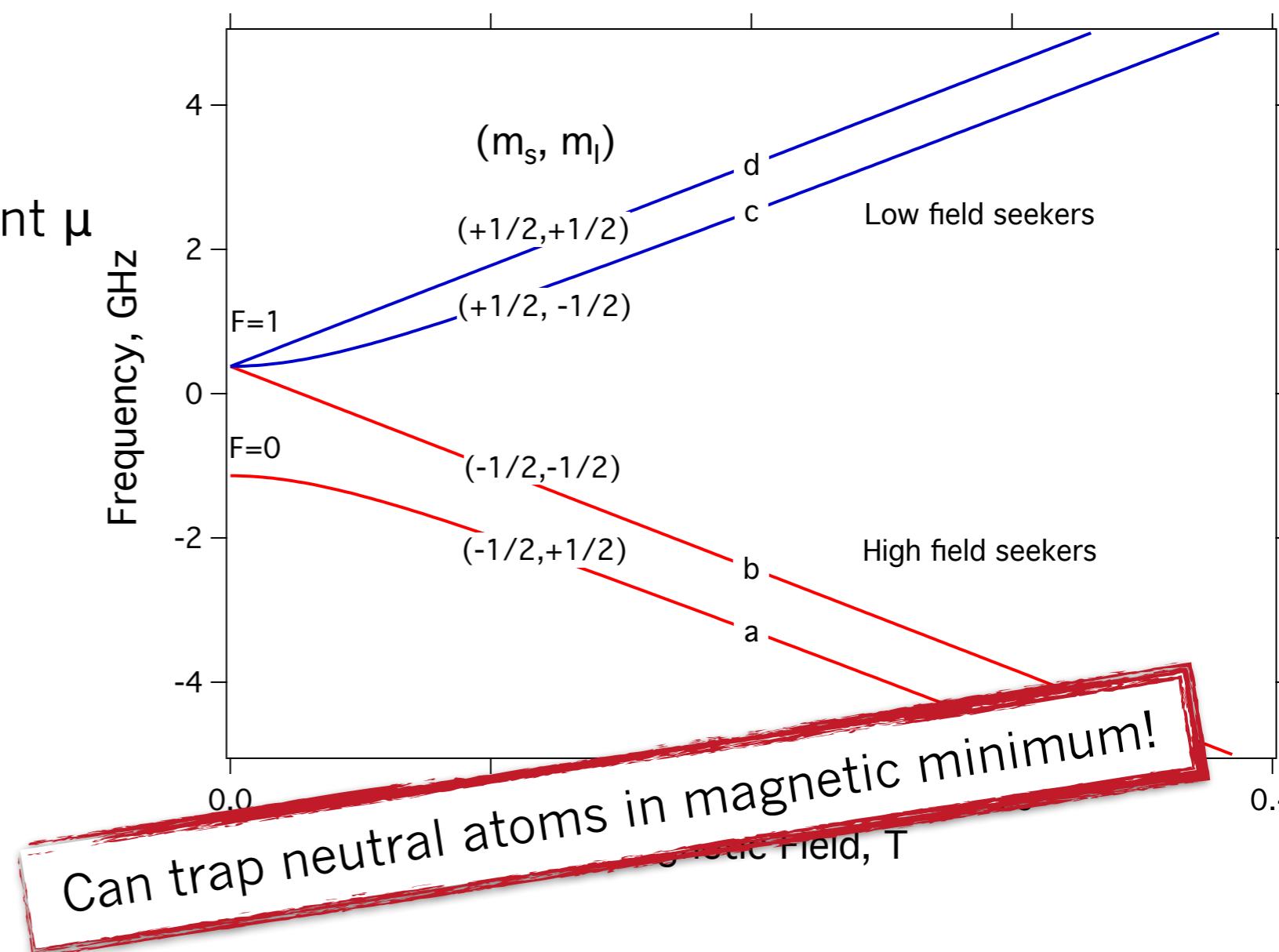
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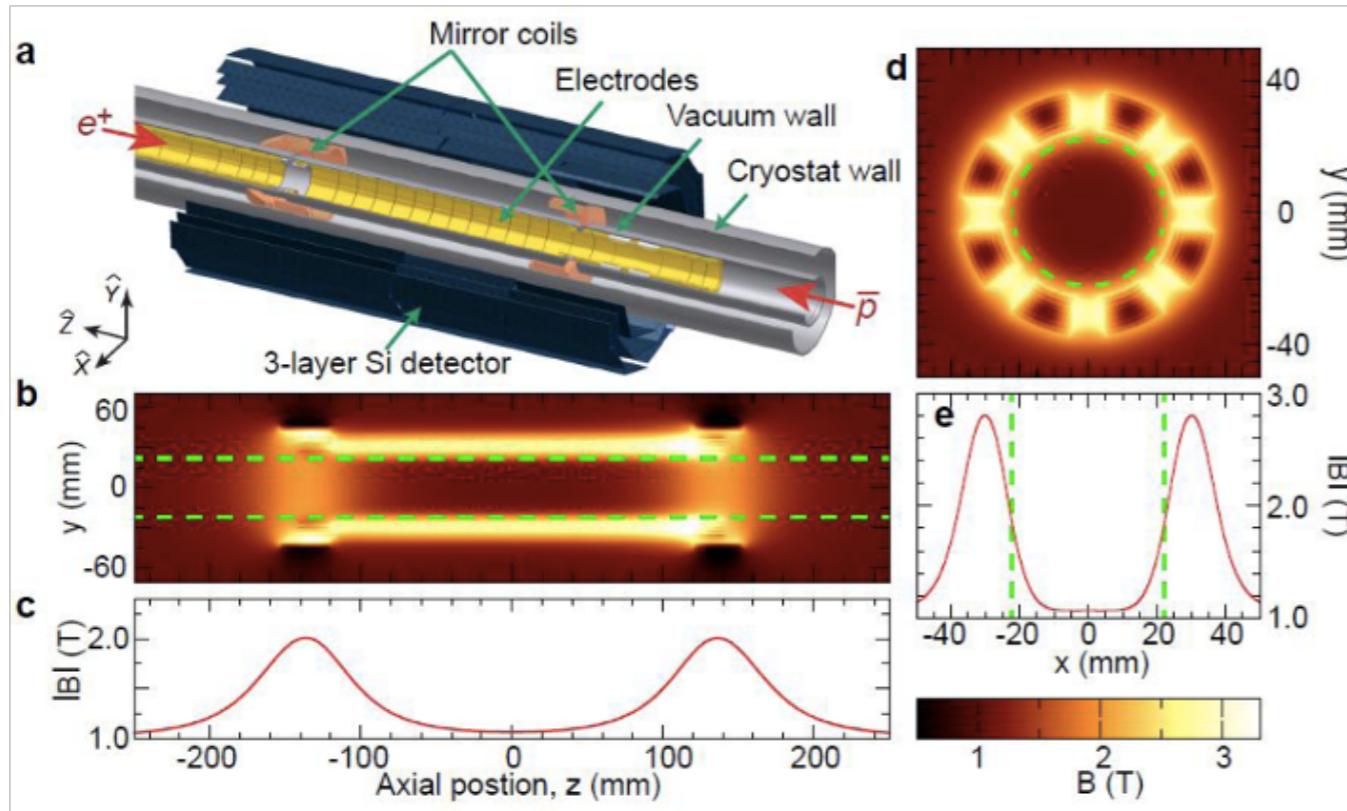
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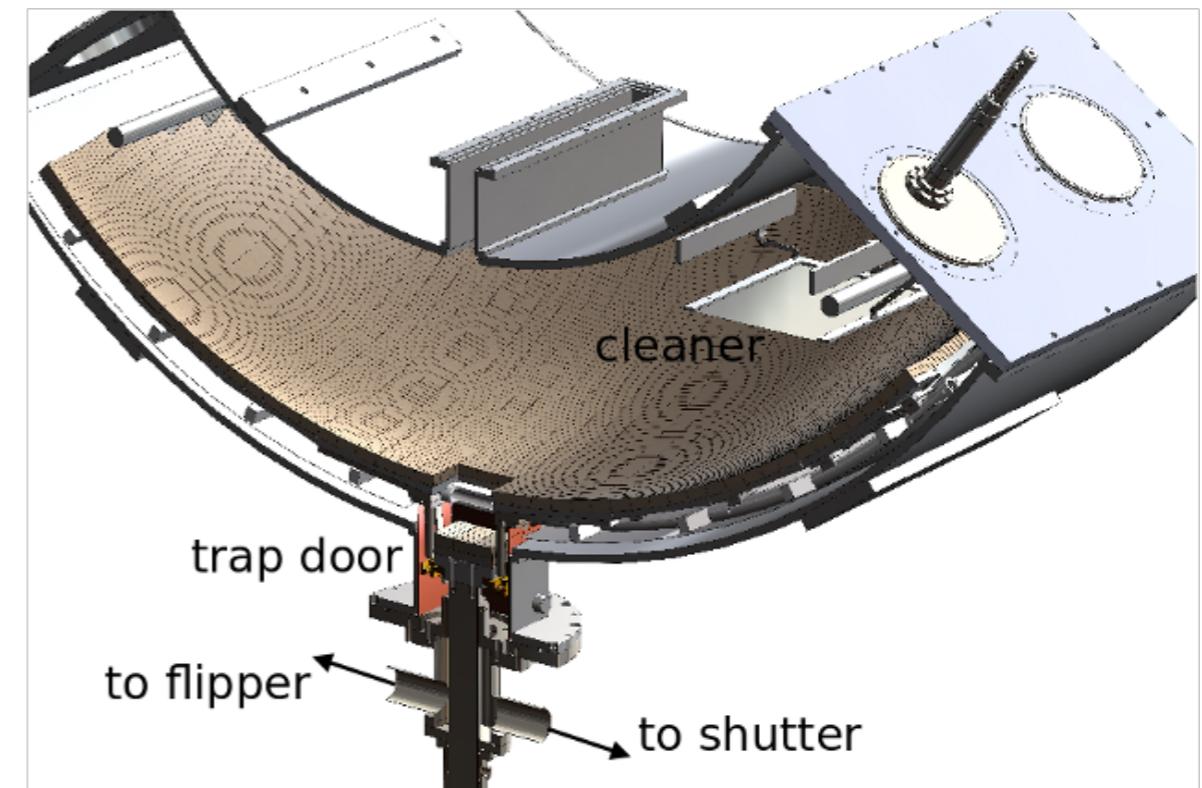
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# Neutral particle traps



ALPHA Collaboration: Nature Phys 7:558, 2011;  
arXiv 1104.4982

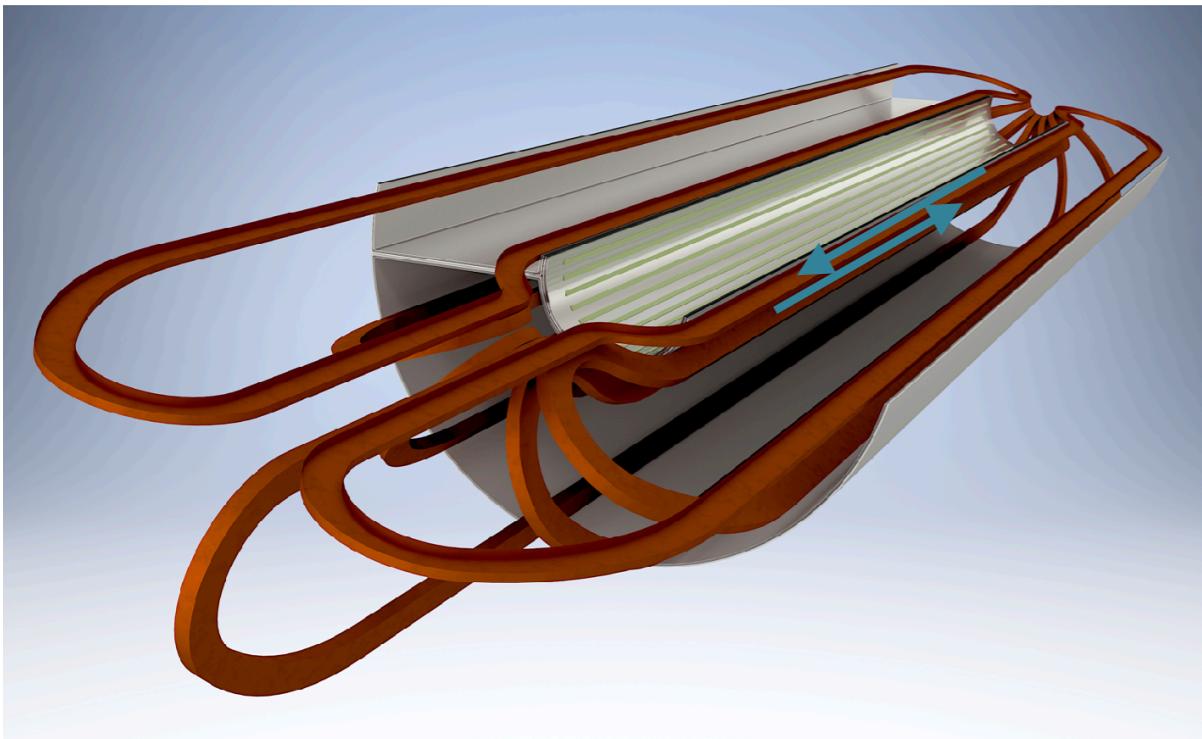


UCNtau Collaboration: Phys Rev C89, 052501, 2014;  
arXiv 1310.5759v3

## General design

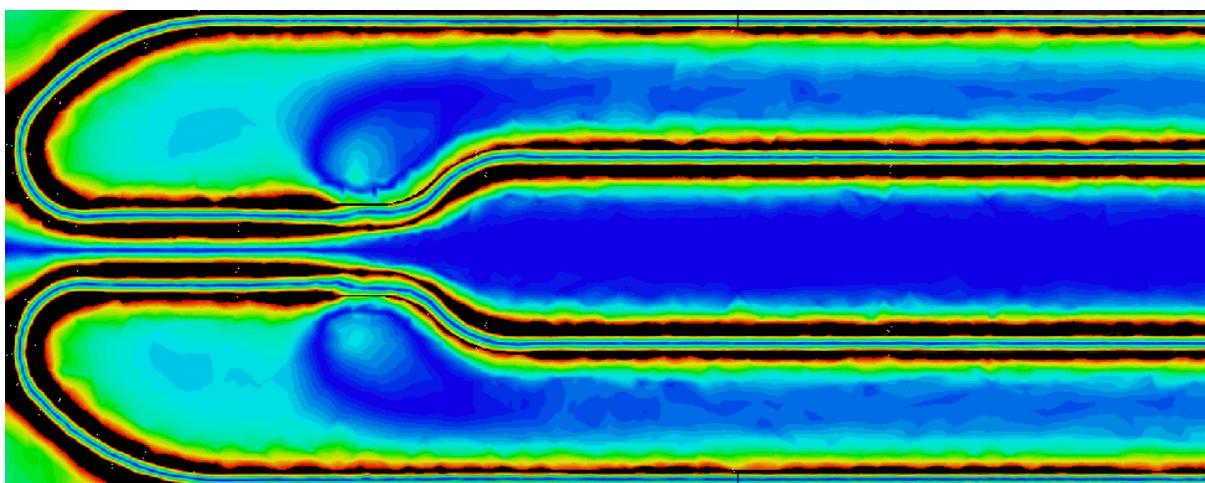
- high magnetic field at walls
- low magnetic fields in the center
  - ▶ near-field to far-field transition with opposing fields

# Atom trapping



## Studying Ioffe-Pritchard trap

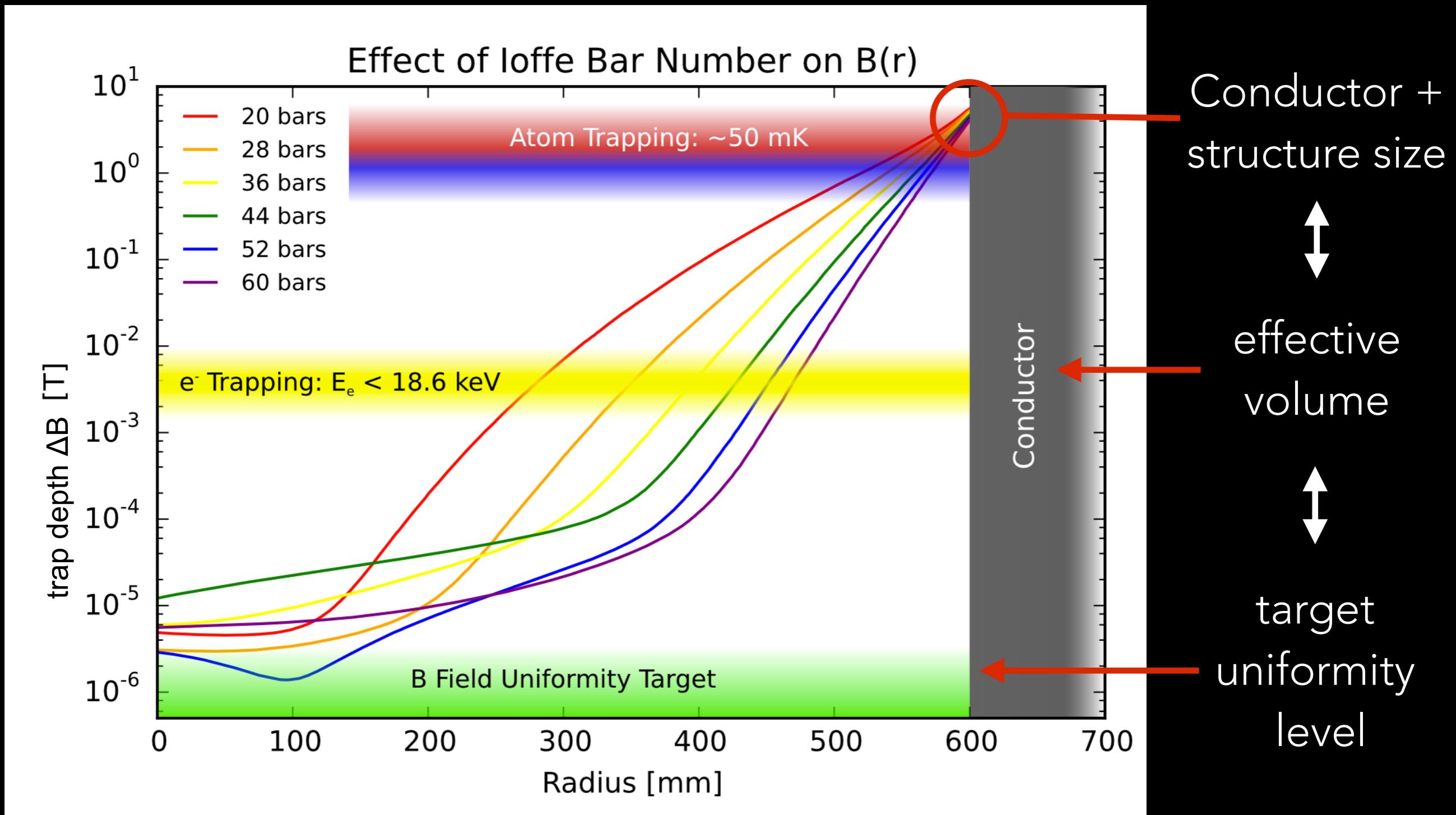
- plausible field step
  - ▶  $\Delta B = 2 \text{ T}$
- limit thermal loss fraction
  - ▶  $\epsilon_{\text{loss}} = 10^{-10}$
- maximum allowed temperature
  - ▶  $T_{\text{max}} = 30 \text{ mK}$



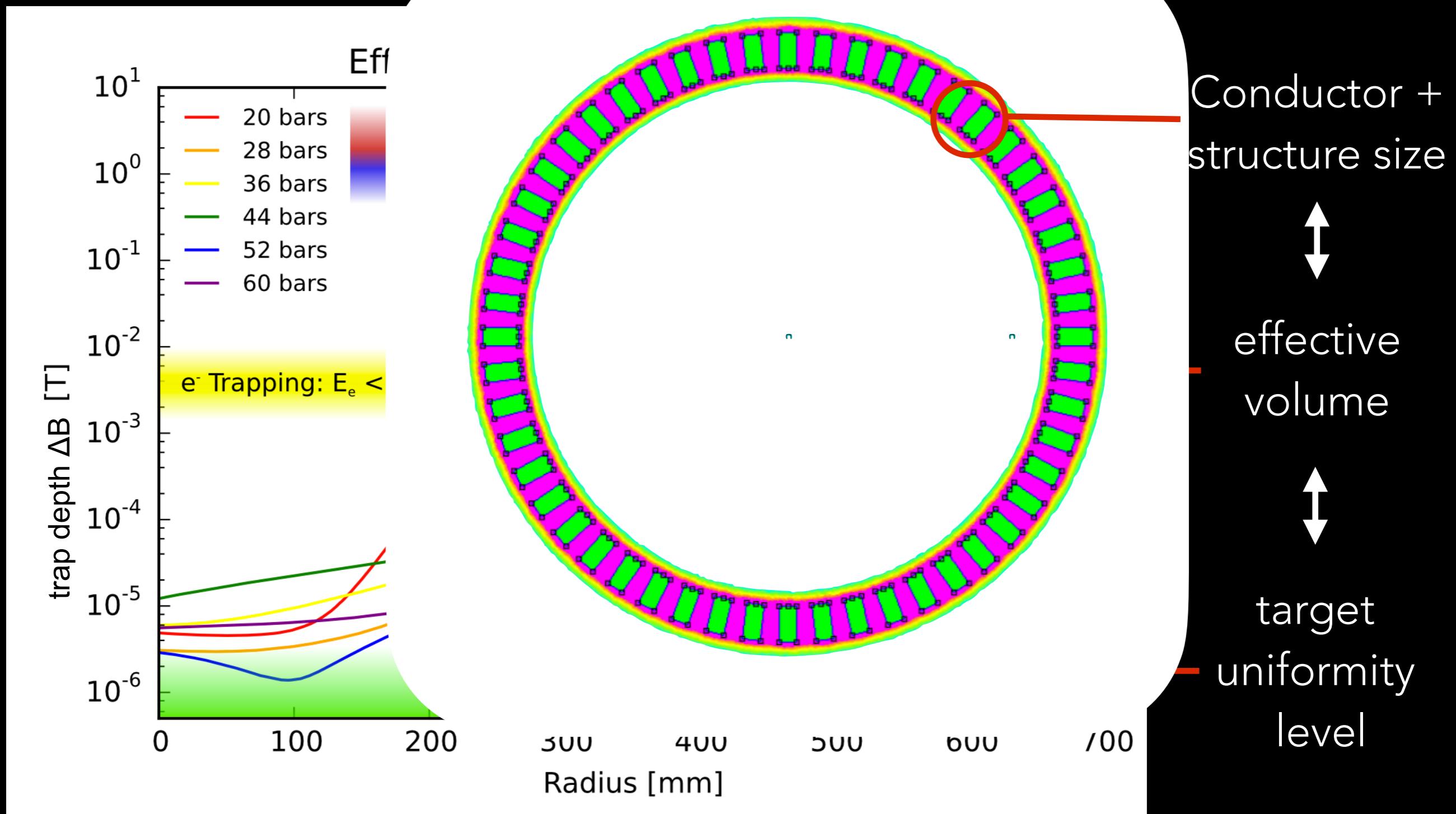
## Challenges

- cooling to sub-Kelvin level
- keep high  $T/T_2$  purity
  - ▶ molecular  $T_2$  not trapped!
- field uniformity in central region

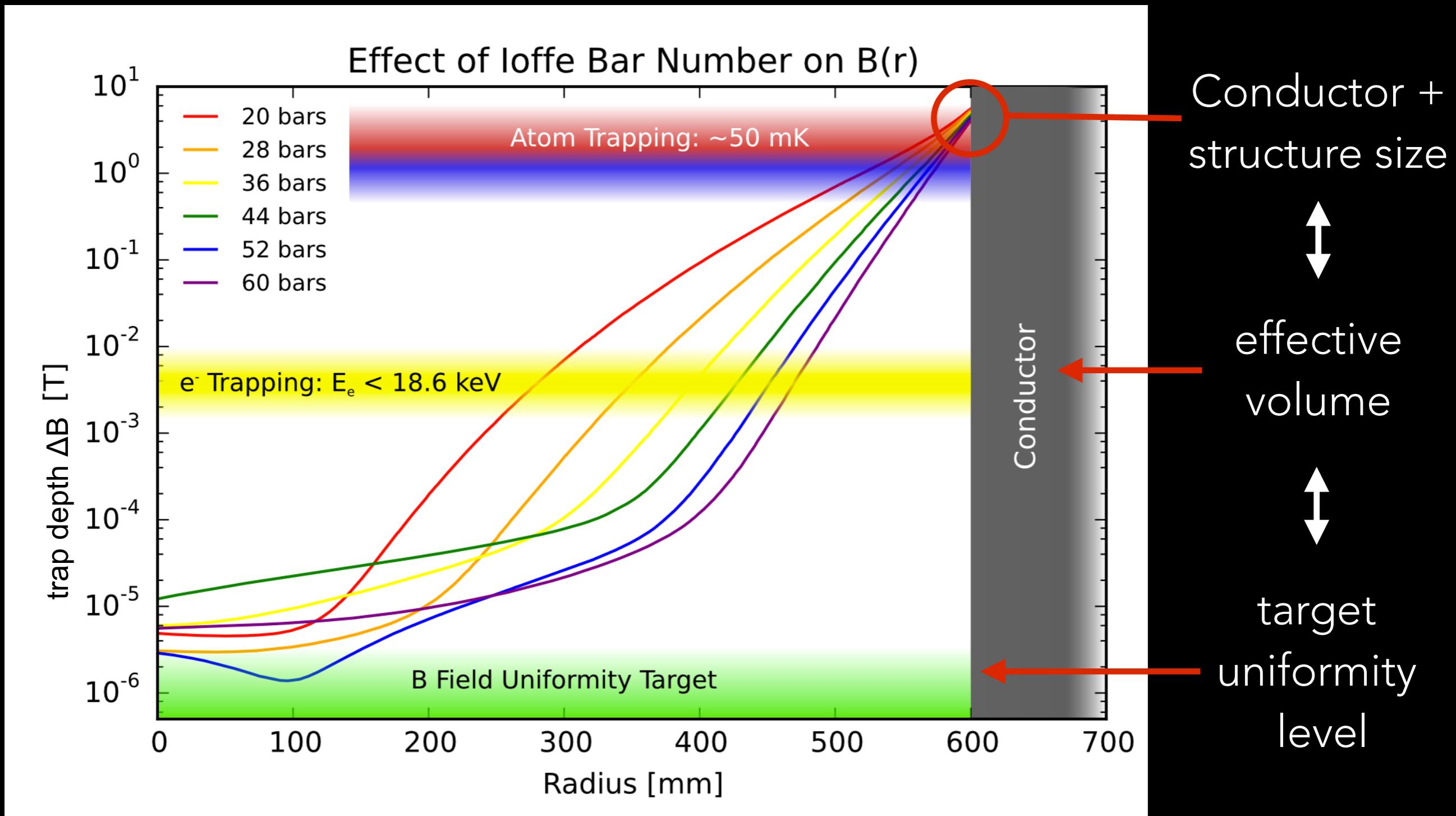
# Atomic trapping: trap challenges



# Atomic trapping: trap challenges



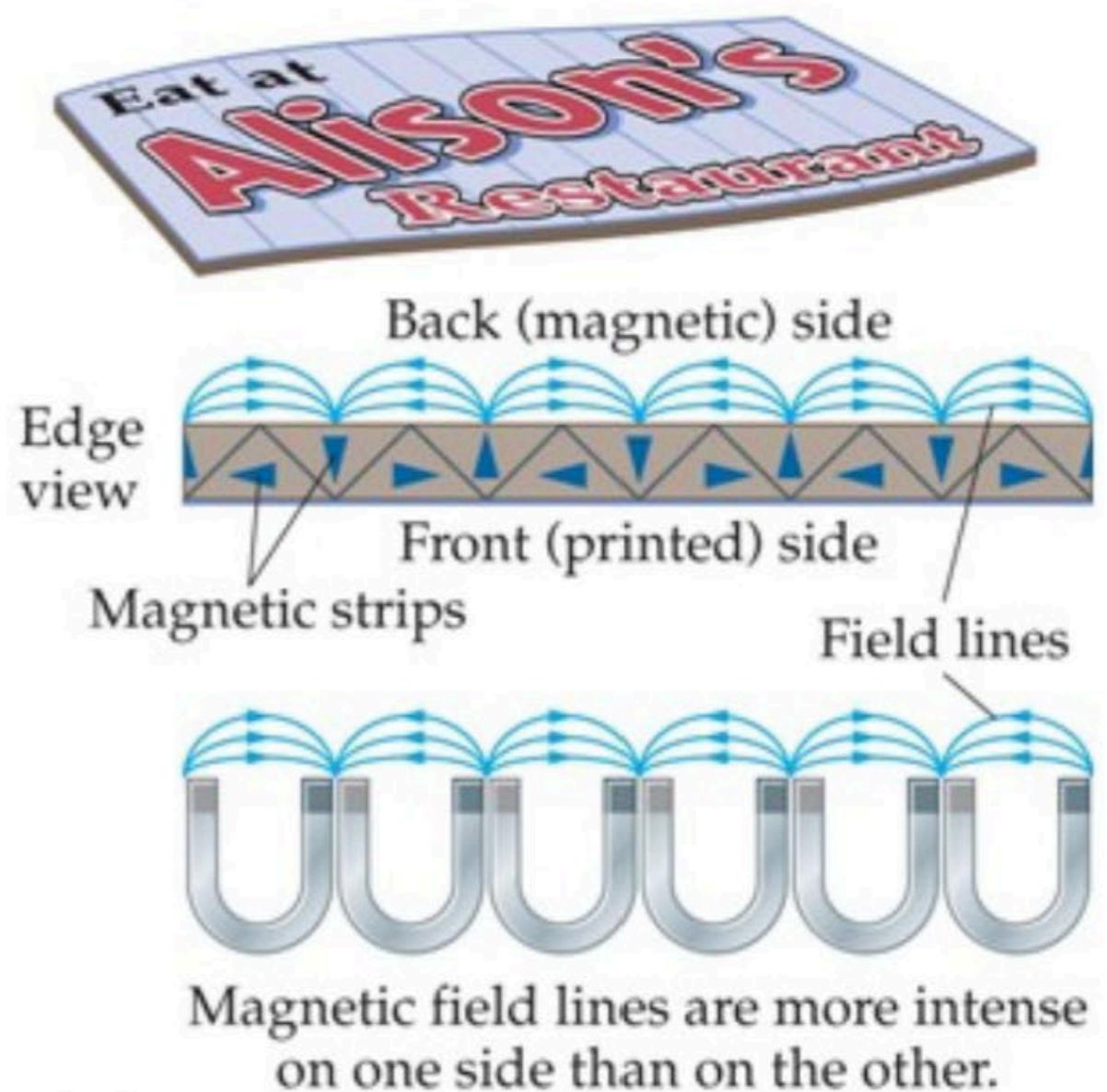
# Atomic trapping: trap challenges



# Halbach arrays

Permanent magnet configuration

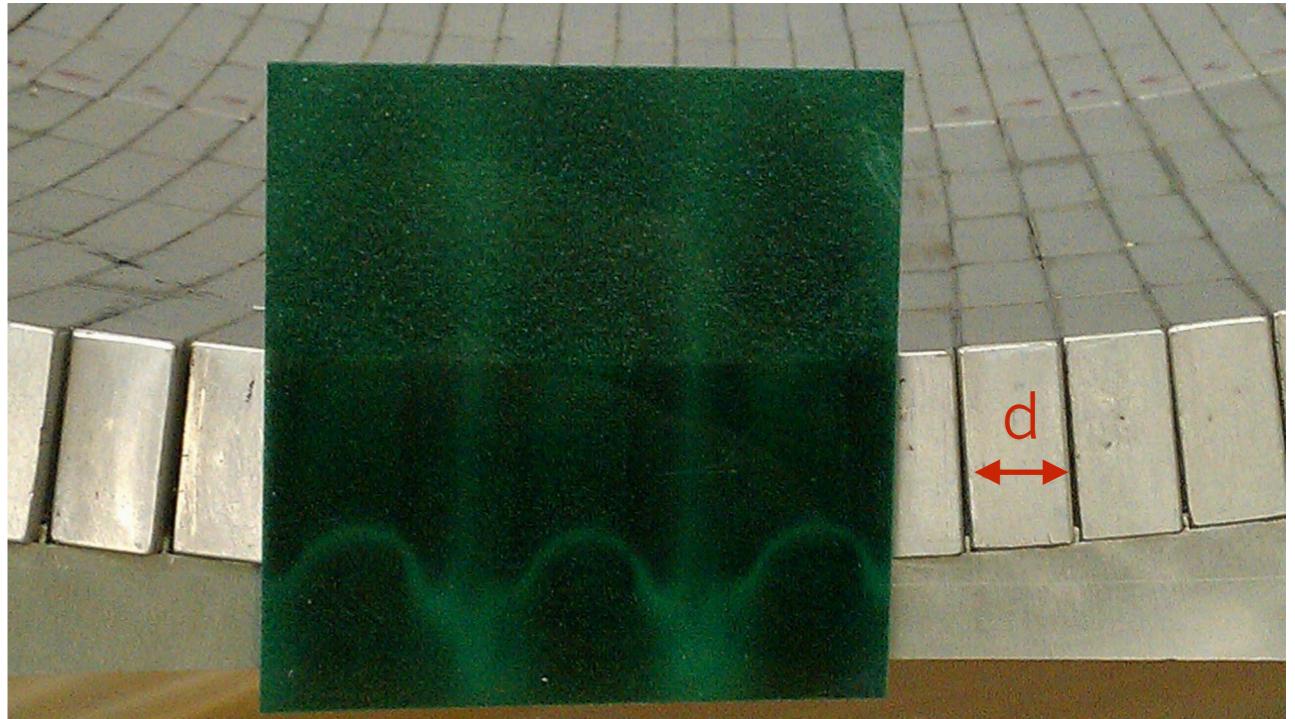
- alternate orientations
  - ▶ strong near field
  - ▶ weak far field
- circular flux configuration
  - ▶ one “magnetic” side
  - ▶ one “non-magnetic” side



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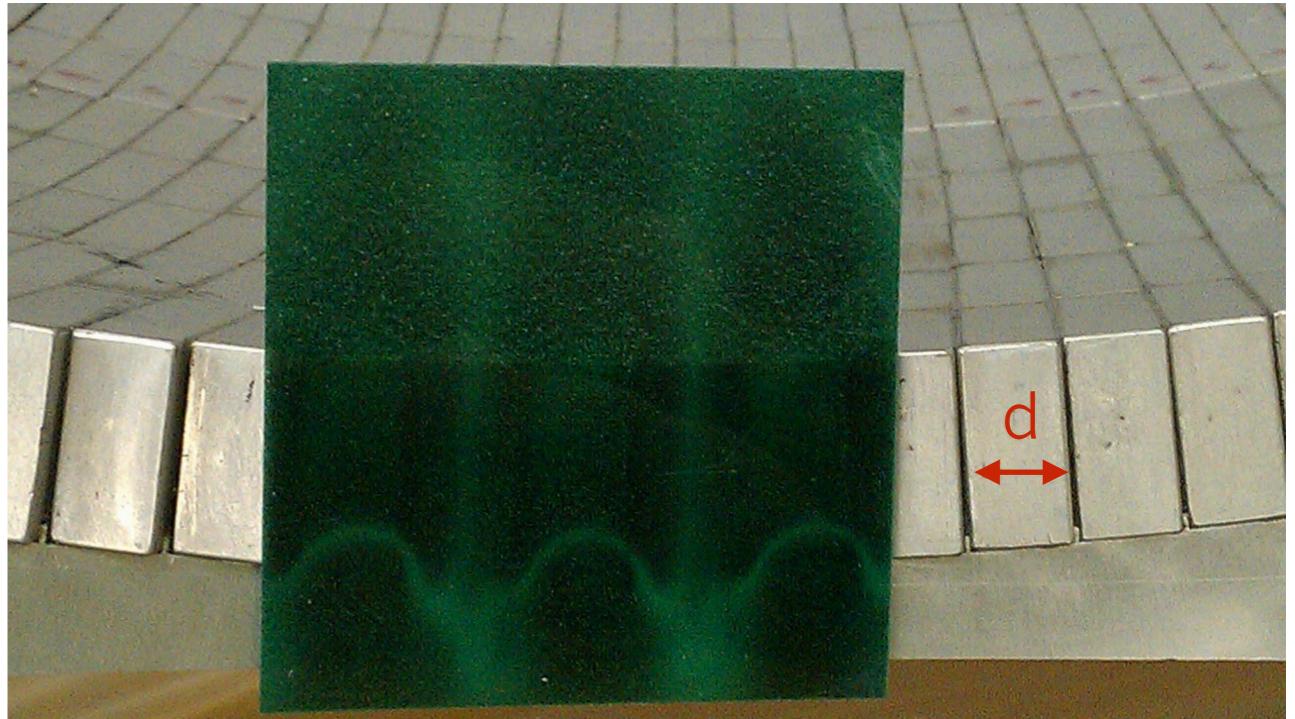
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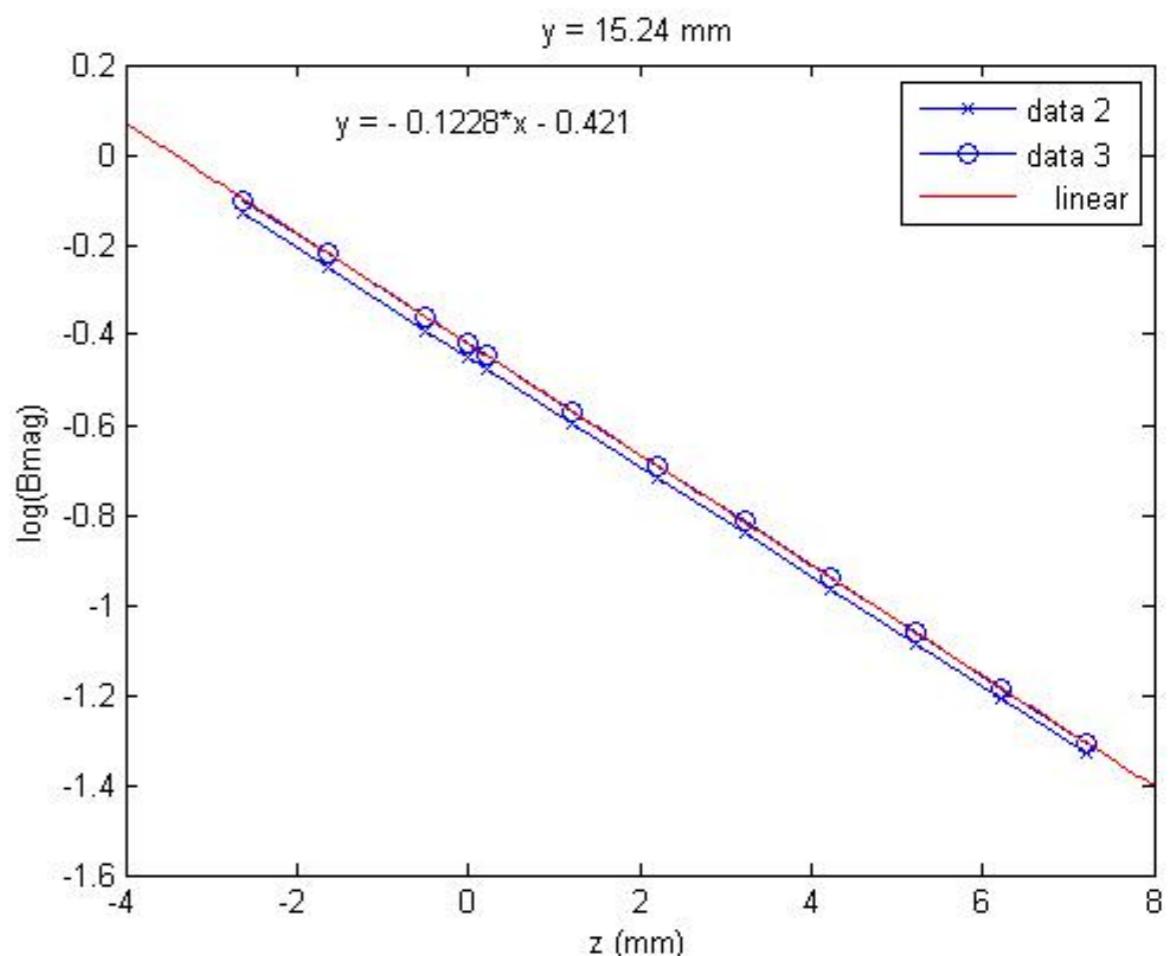
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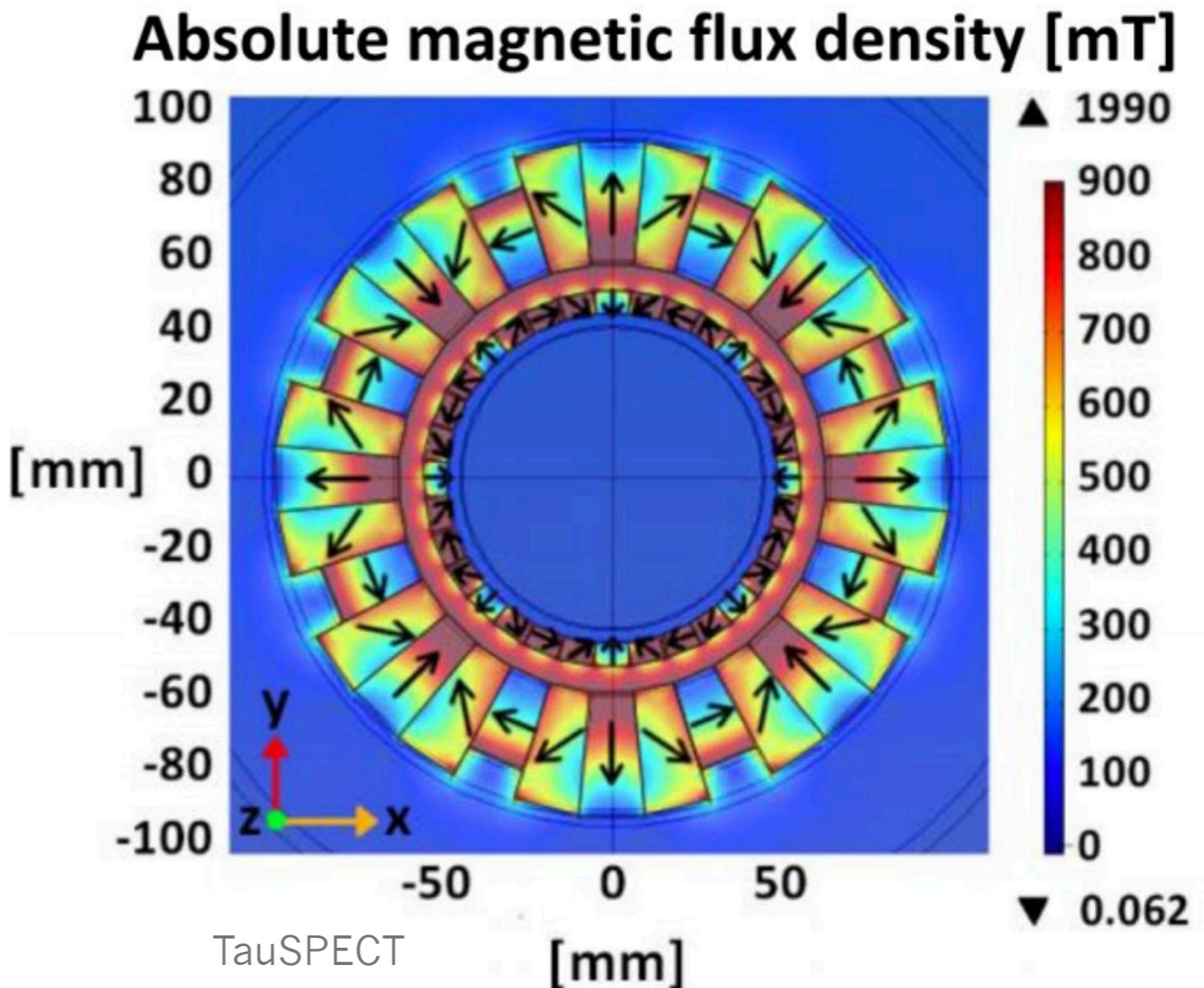


Flat Halbach array

- field falls exponentially with characteristic length  $l = \frac{2d}{\pi}$
- ▶ weak far field



# Halbach arrays for Project 8



# Halbach arrays for Project 8

TauSPECT

# Halbach arrays for Project 8

## Field configuration

- cylindrical configuration

$$\vec{B}_{\text{Halbach}} = \vec{B}_\rho + \vec{B}_\varphi$$

- ▶ no cancellation with solenoid electron field

$$\vec{B}_{\text{solenoid}} = \vec{B}_z$$

TauSPECT

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$$\vec{B}_{\text{solenoid}} = \vec{B}_z$$

## Choice of permanent magnets

- rare earth give highest field strength
- phase transition in NdFeB
  - ▶ not suitable below 140K
- SmCo, PrFeB,...

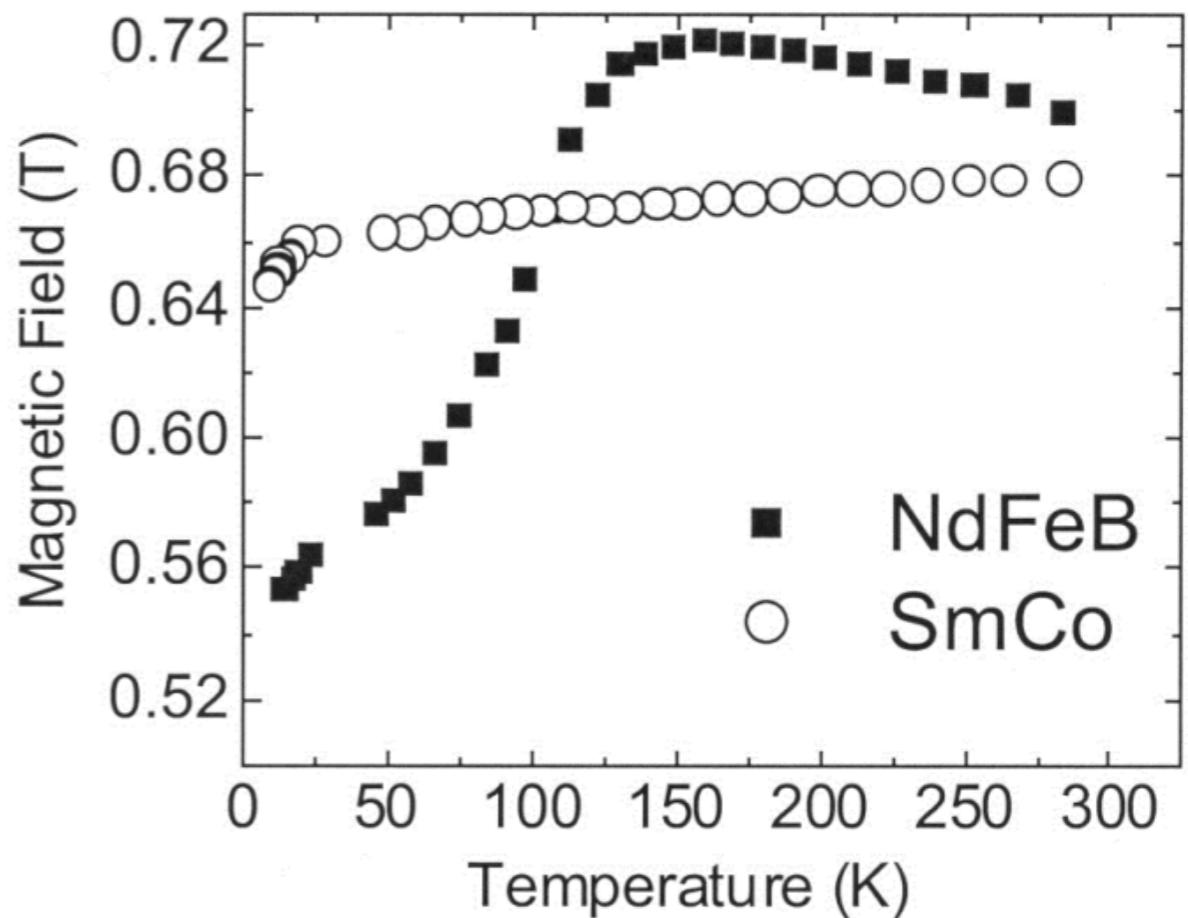


Figure 4. Magnetic Field as a Function of Temperature for NdFeB and SmCo. [6]

# Magneto-gravitational trap

Magnetic trapping

- $E_m = \mu_B B = 58 \mu\text{eV/T}$

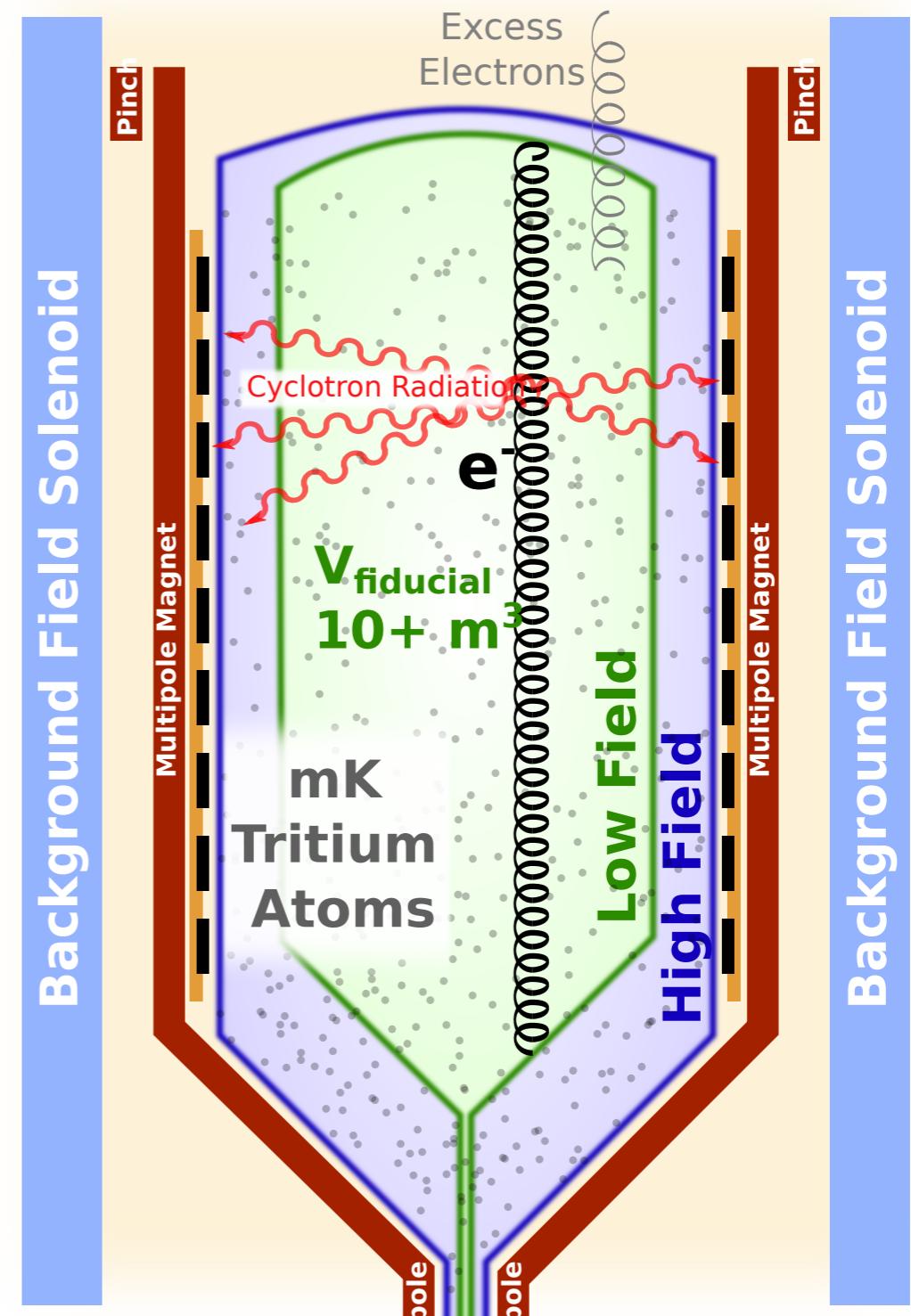
Gravitational trapping

- $E_g = mgh = 0.3 \mu\text{eV/m}$

Energy of cold atomic beam

- $E_k = k_B T = 64 \mu\text{eV/K}$

→ For 1mK cold beam, it takes 0.21 meters of gravity and 11 gauss of B-field to trap.

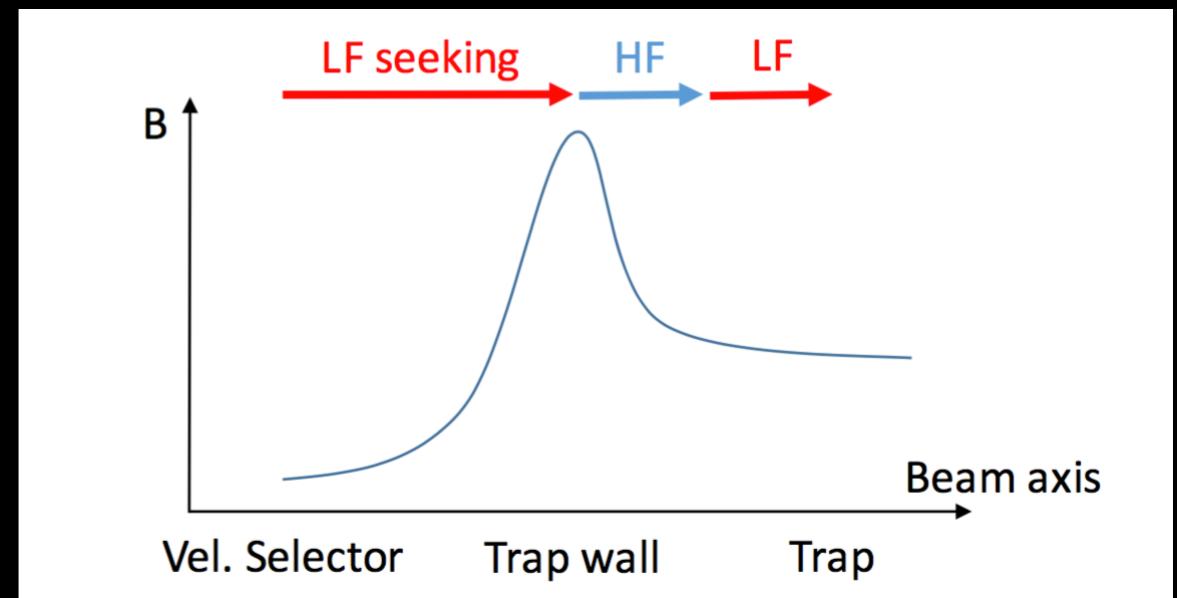


# How to fill the trap?

# How to fill the trap?

Spin-flip loading ?

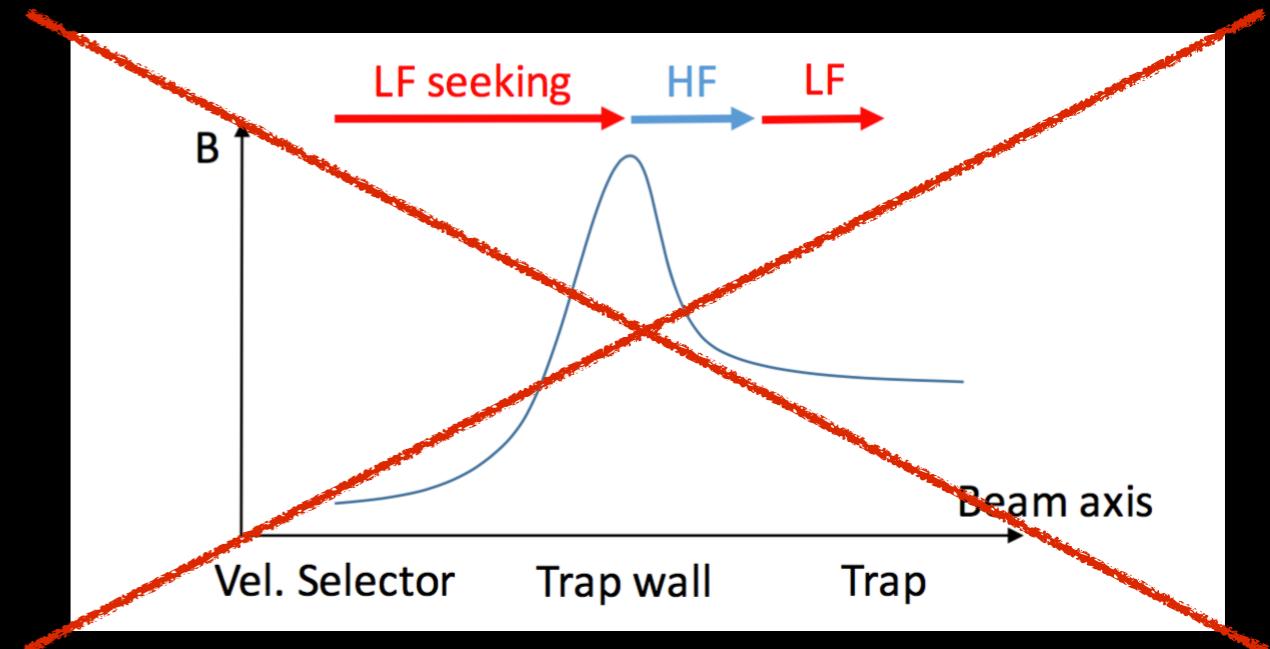
- Flip atom spin at trap edge
  - ▶ Carry atoms over potential wall (+ energy loss)
- But: stimulated emission
  - ▶ will lose trapped atoms



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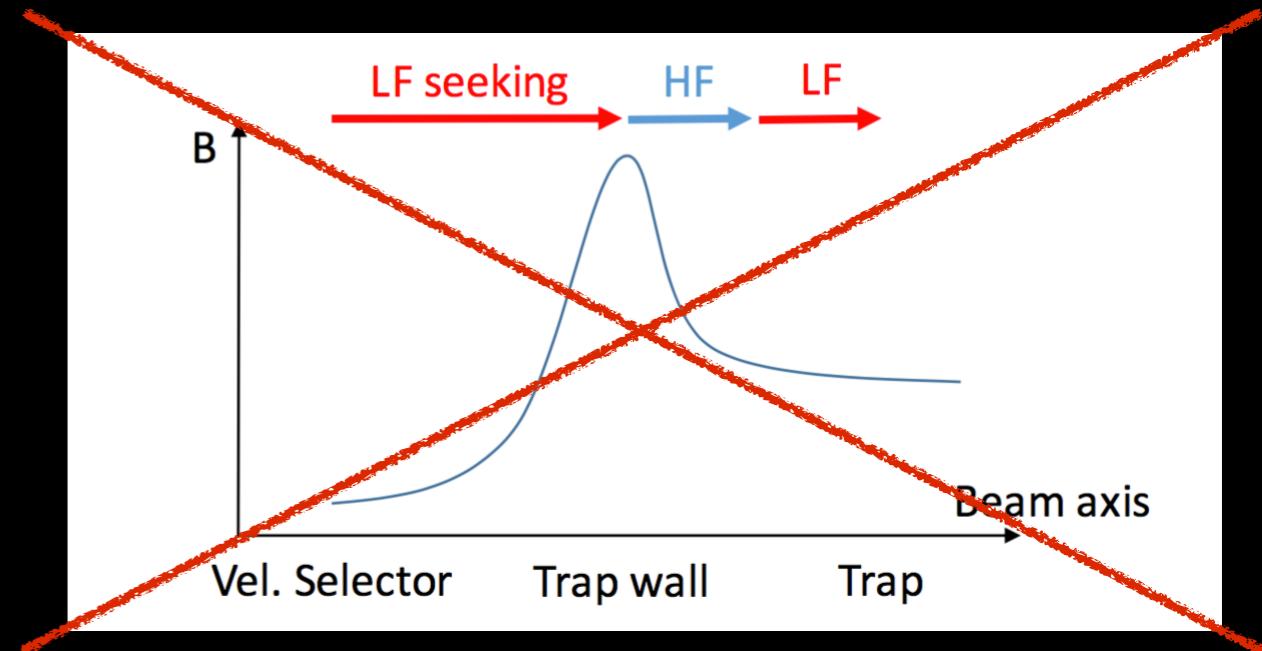
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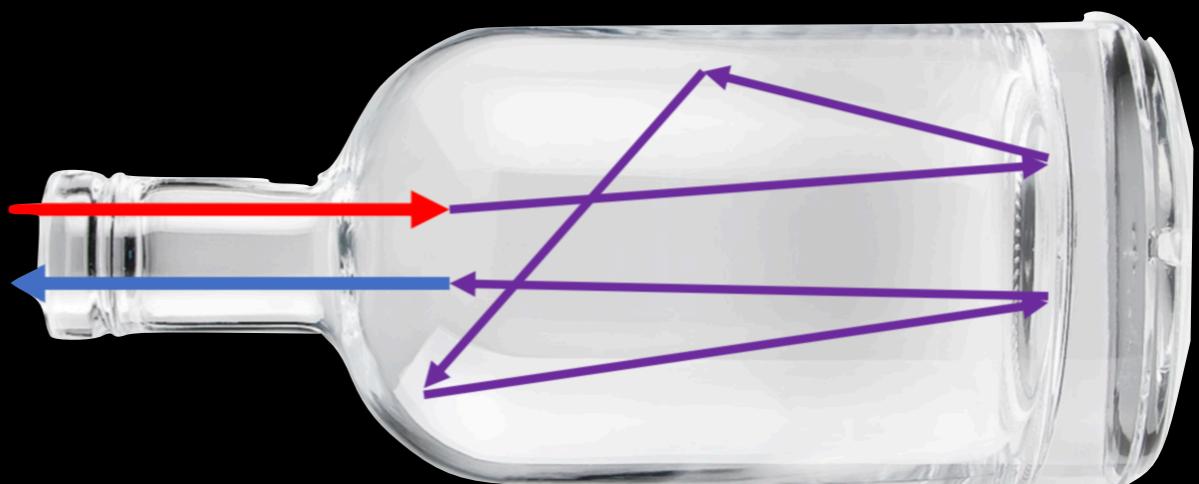
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Cornucopia\* loading

- Blow cold atoms into trap
  - accept loss through entrance hole
- required input flux for 1cm hole @ 50mK
  - ▶  $5 \cdot 10^{12}$  atoms/sec

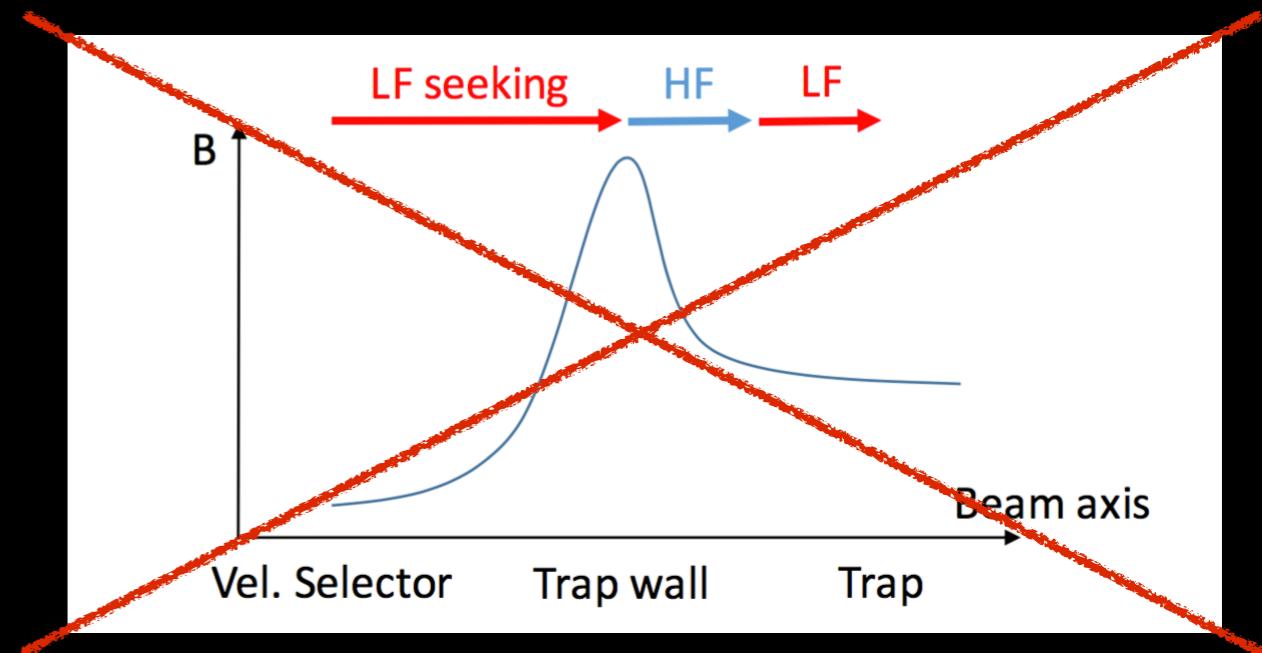


\* horn of plenty

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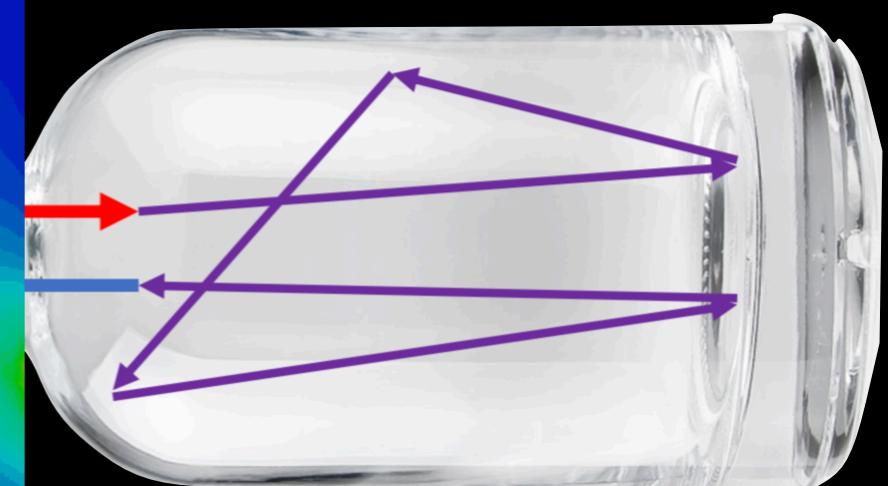
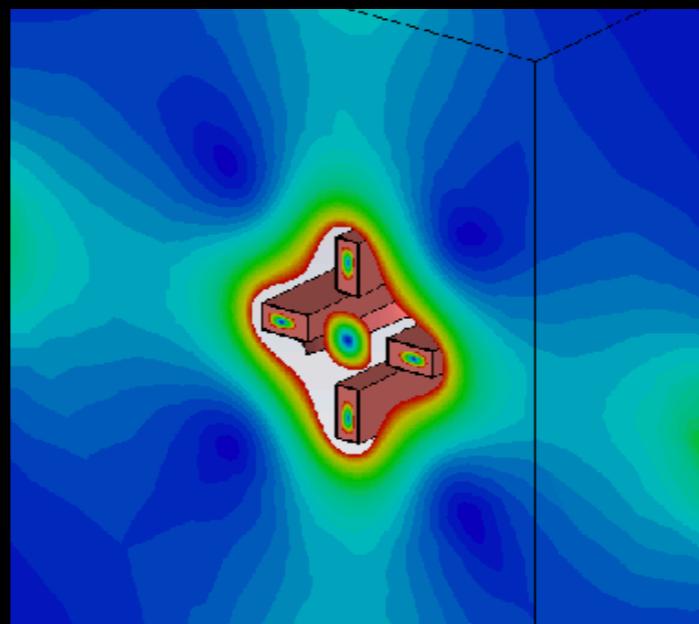
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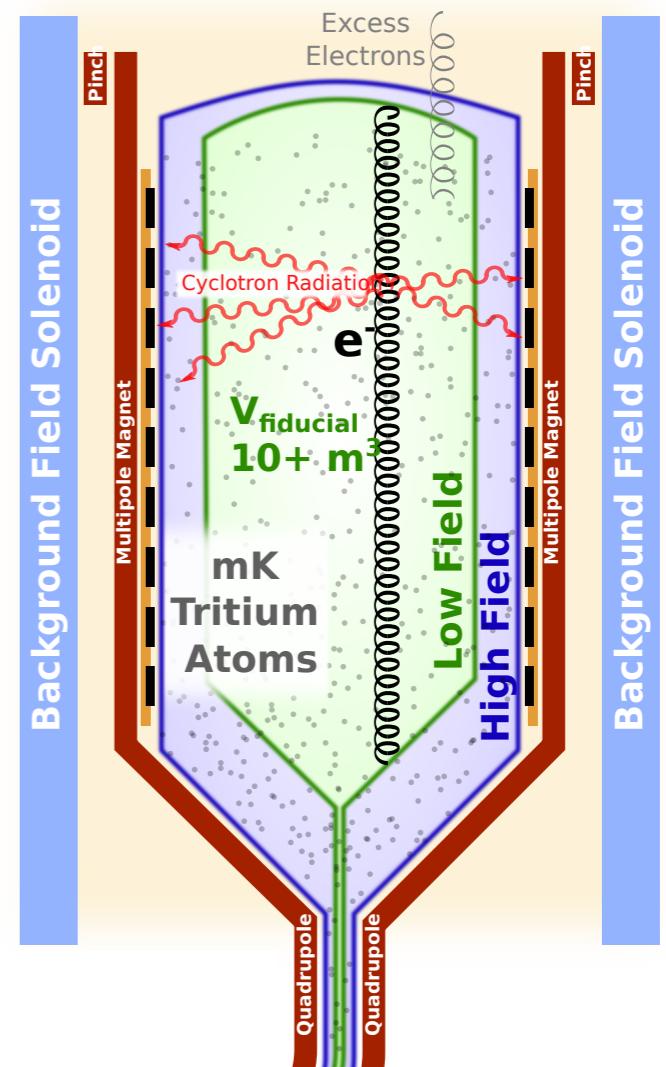
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# Project 8: Designs concepts

Atomic T source

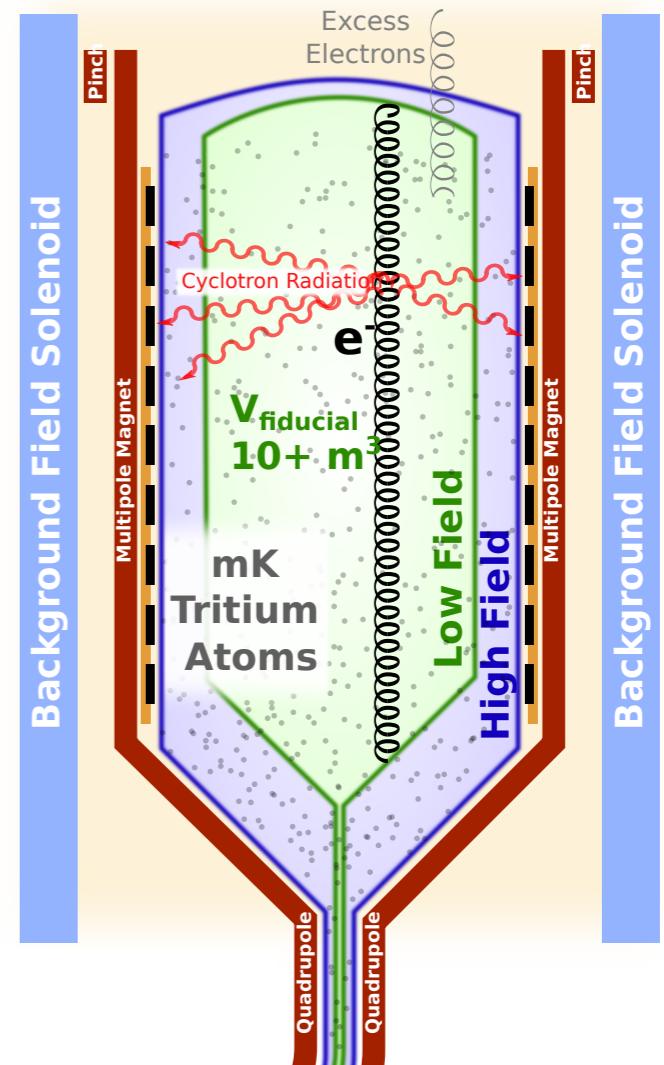
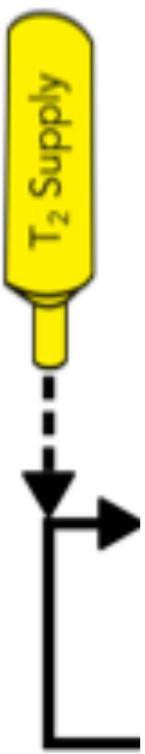
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Atomic T source



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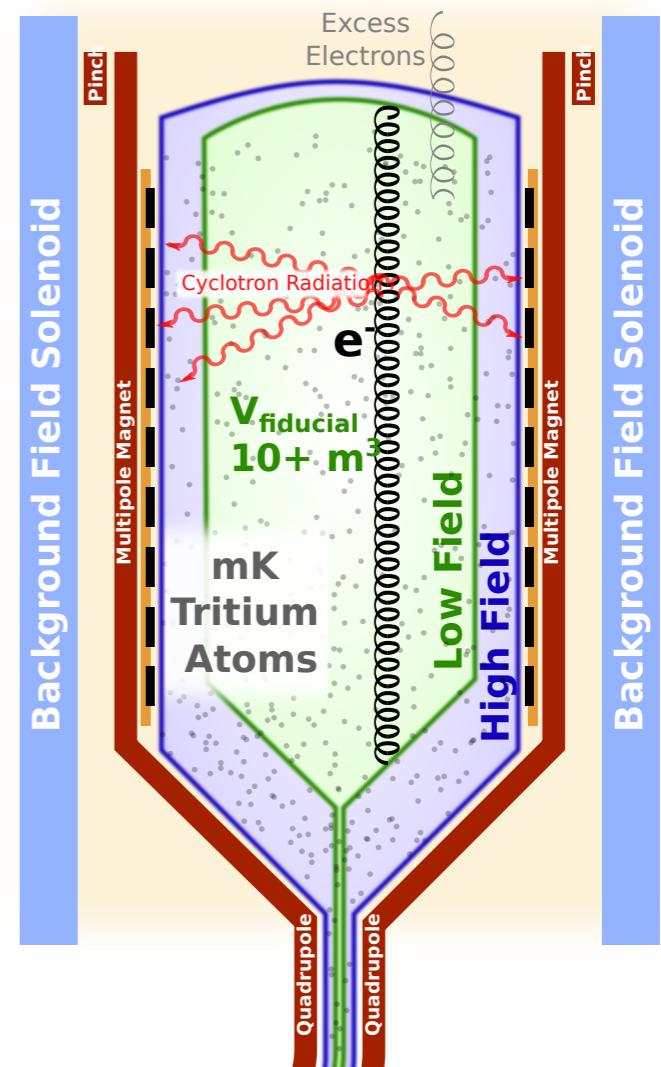
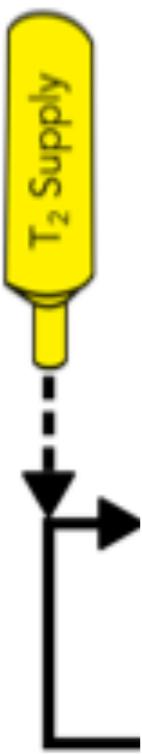
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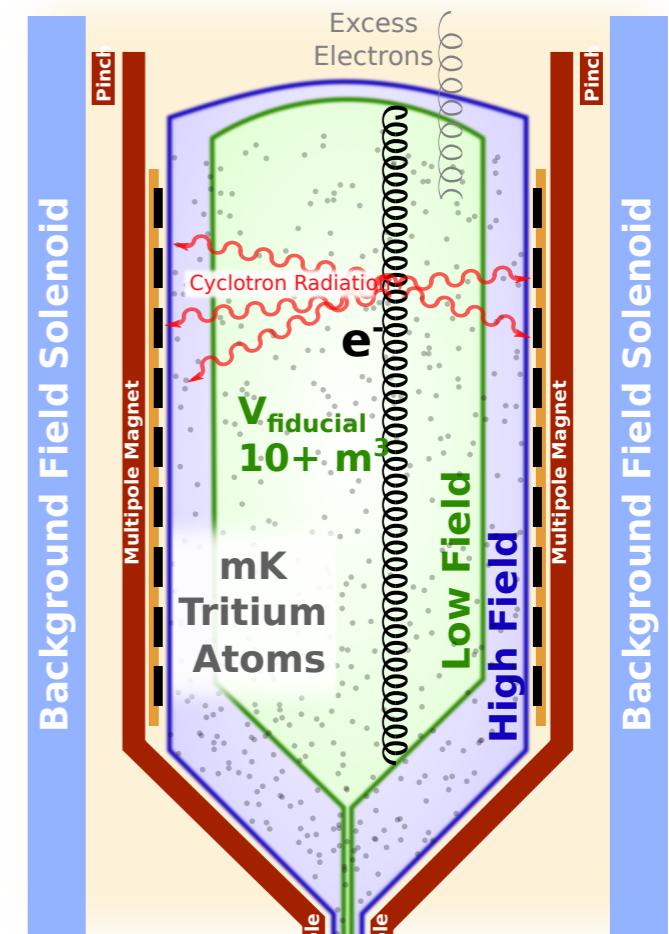
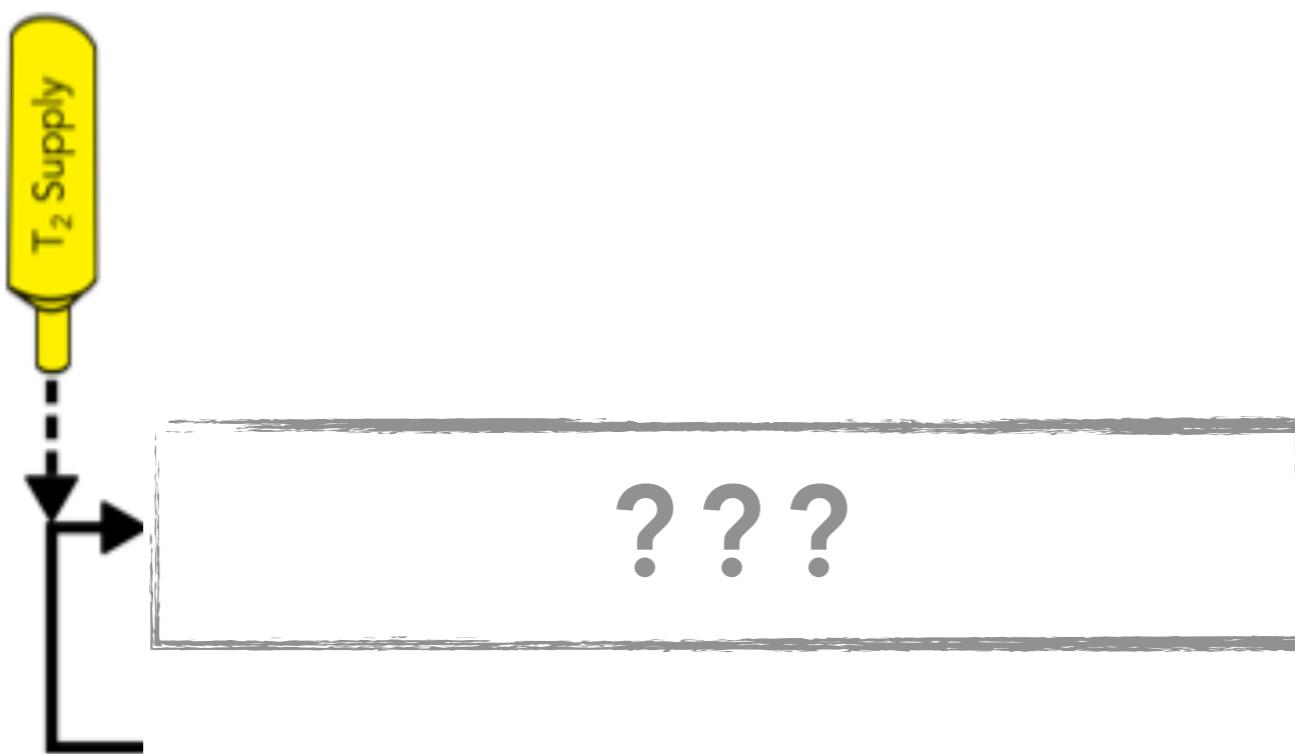
- Injection ✓
- Trapping ✓



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Atomic T source

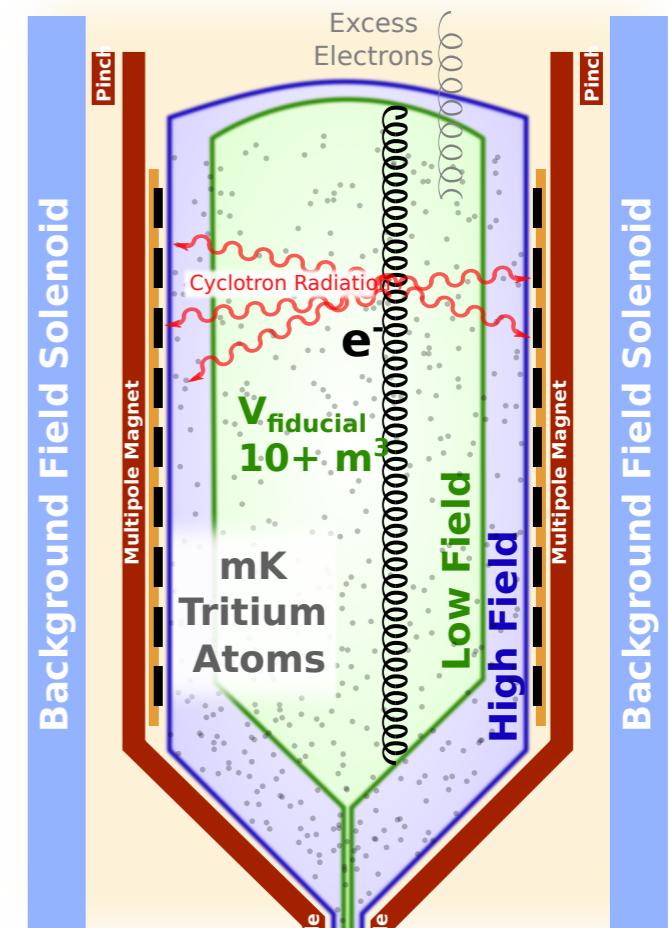
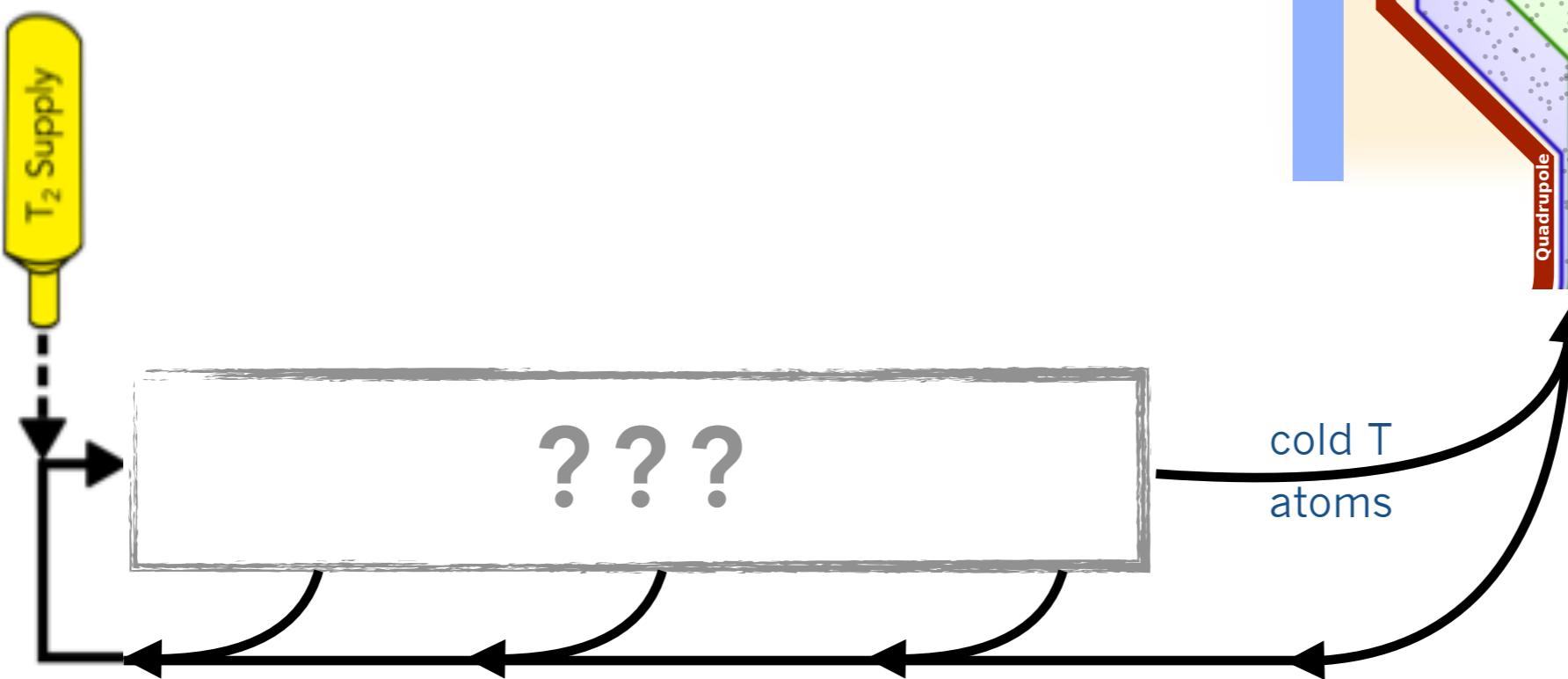
- Dissociation ???
- Cooling ???
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# Project 8: Designs concepts

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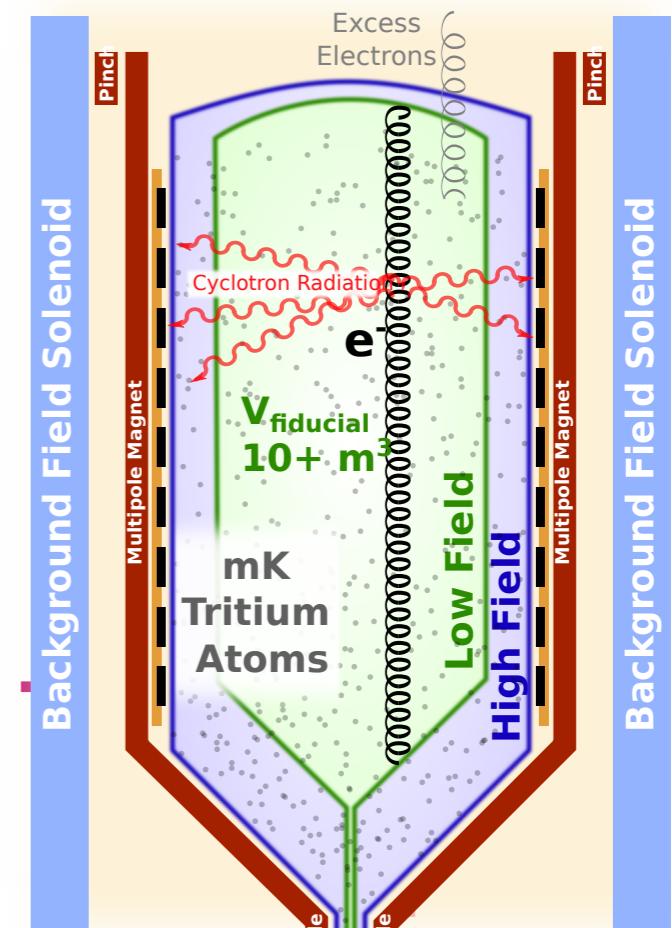
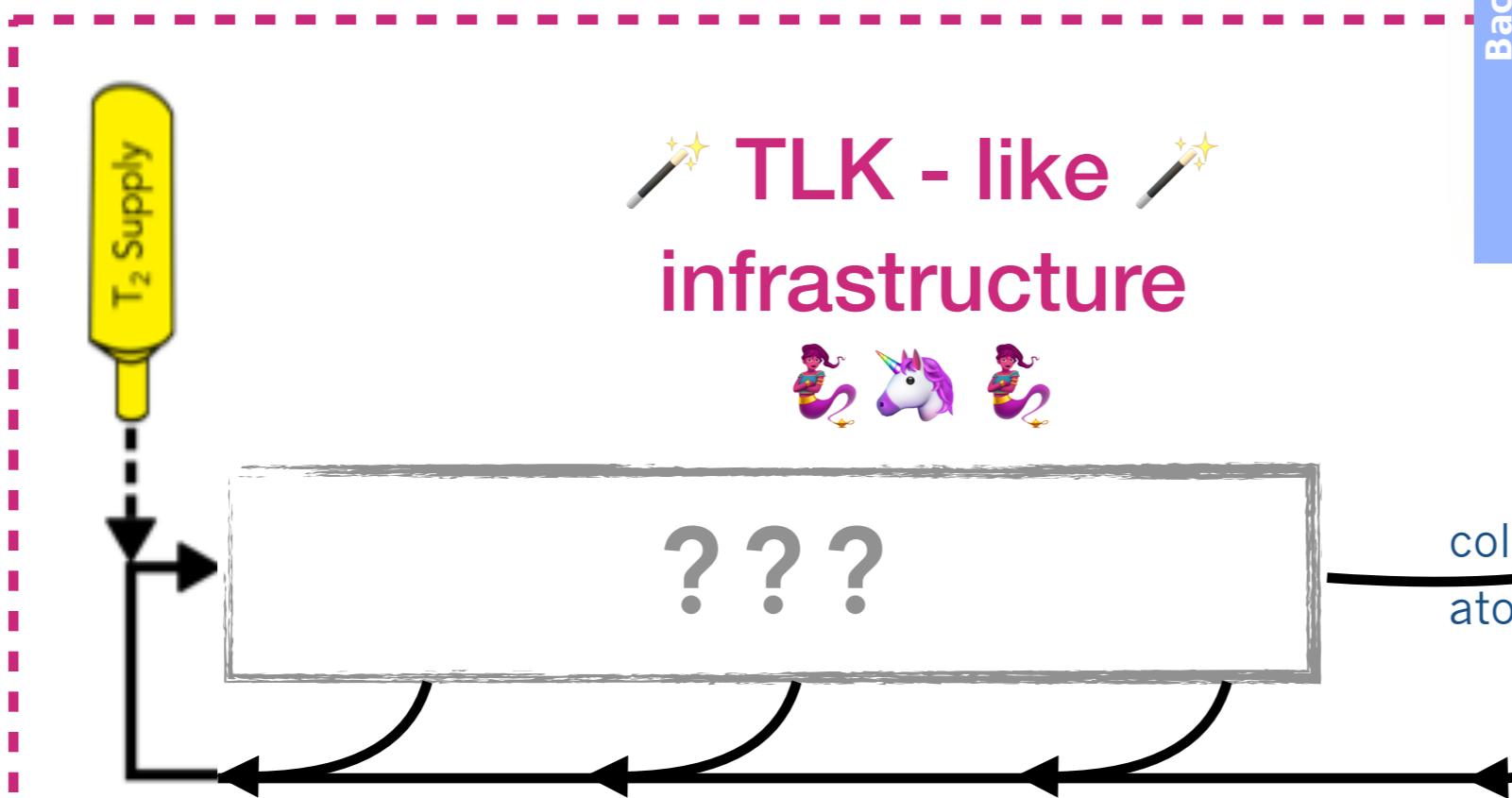
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# Project 8: Designs concepts

Atomic T source

- Dissociation ???
- Cooling ???
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# T<sub>2</sub> dissociation schemes

## Microwave dissociation @ 151MHz

- well tested for hydrogen
- chemical reaction with glass
  - ▶ not feasible with tritium!

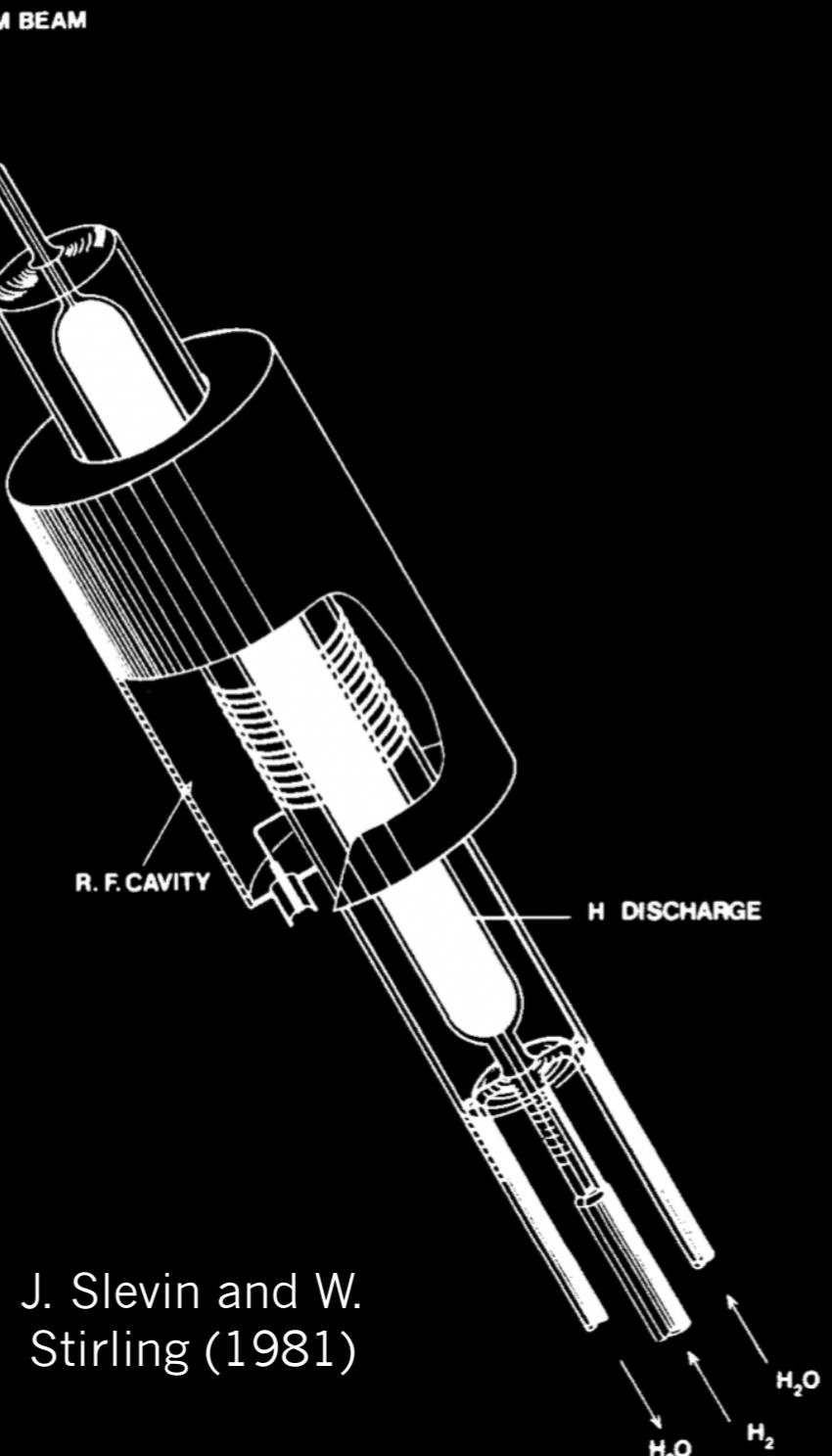
## Laser dissociation

- dissociation energy 4.52eV
  - ▶ wavelength < 274nm
- required laser power ~ kW!

## Coulomb explosion

- difficult to re-neutralize

...

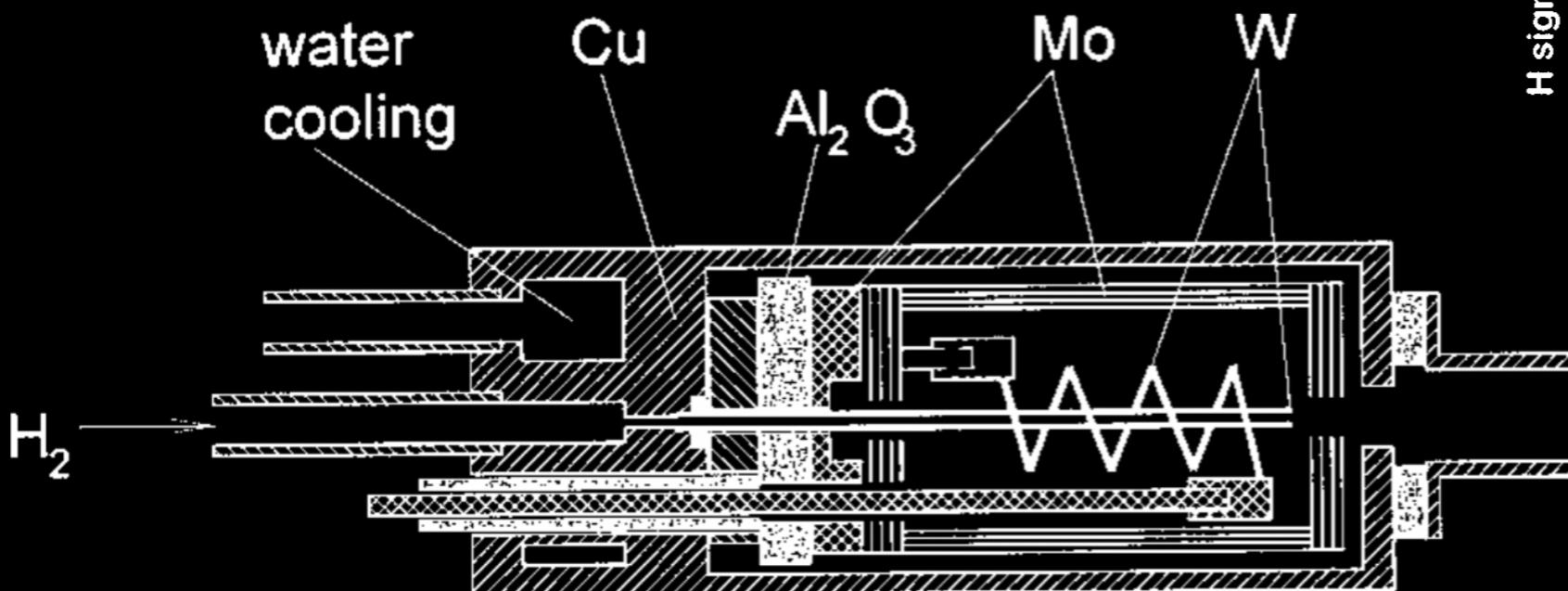


J. Slevin and W.  
Stirling (1981)

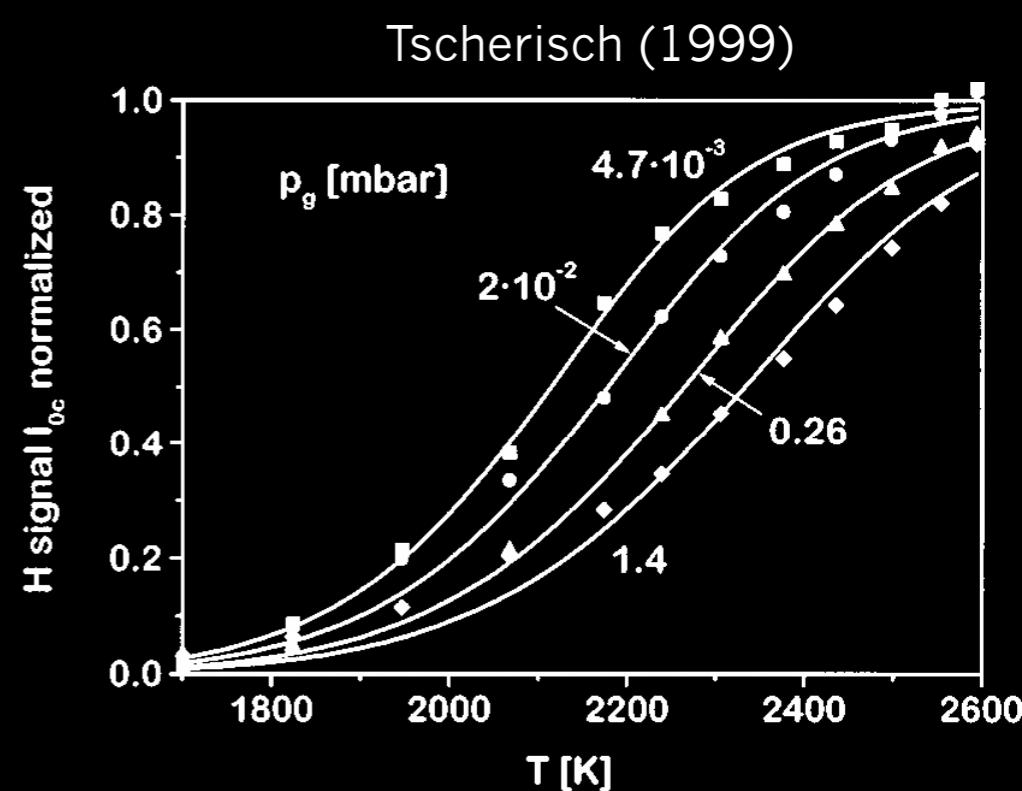
# Thermal Dissociator

Hot tungsten tube heated to 2500K

- radiatively or
- by electron bombardment
- ▶ commercial devices available



K.G. Tschersich and V. von Bonin (1998)



HABS hydrogen cracker

# Cooling atomic hydrogen

## Hydrogen recombination

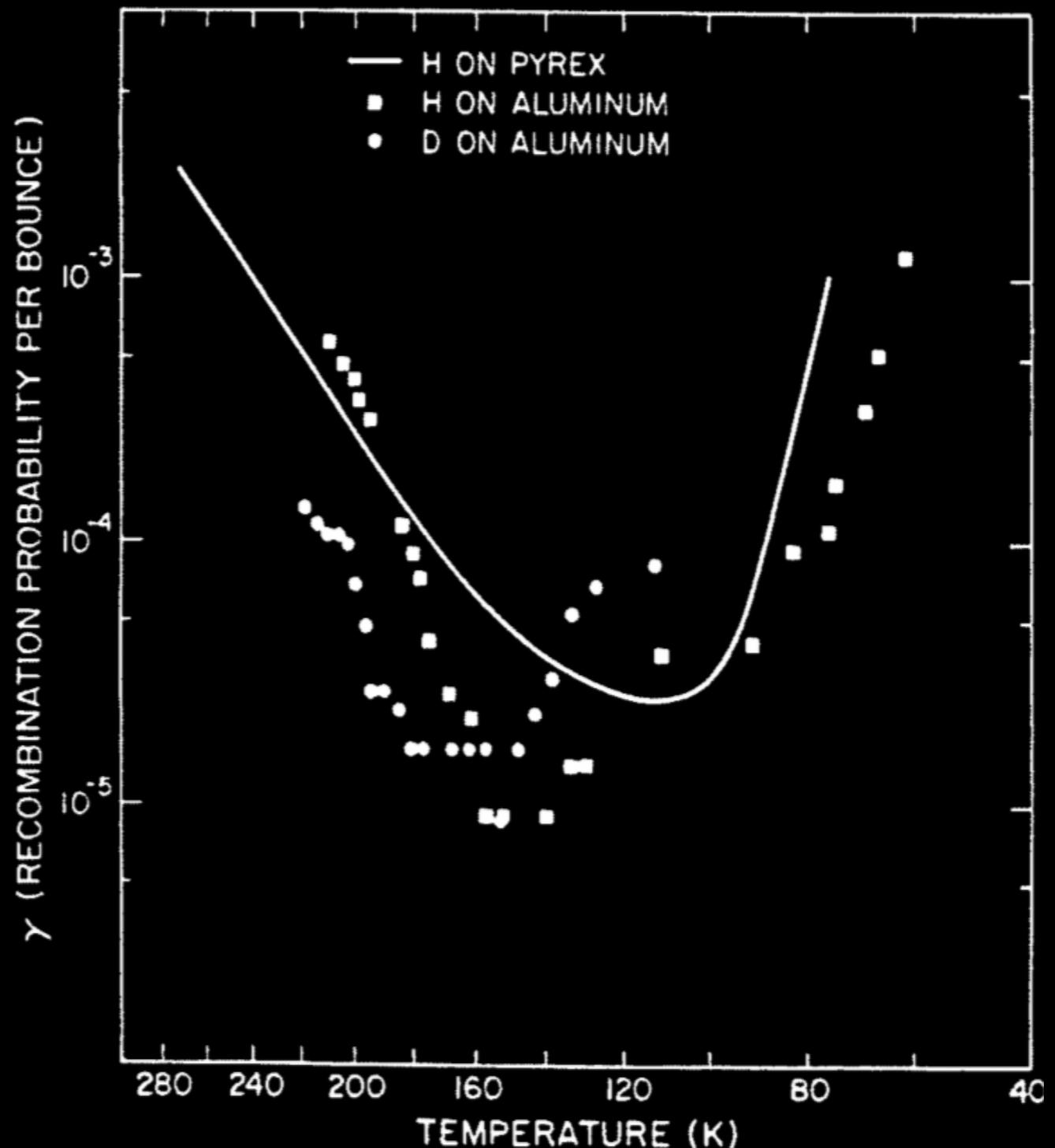
- three-body gas interactions
  - ▶ small rate
- wall interactions
  - long *sticking* time
  - ▶ dominates recombination

## Probability depends on

- temperature
- material
- hydrogen isotope

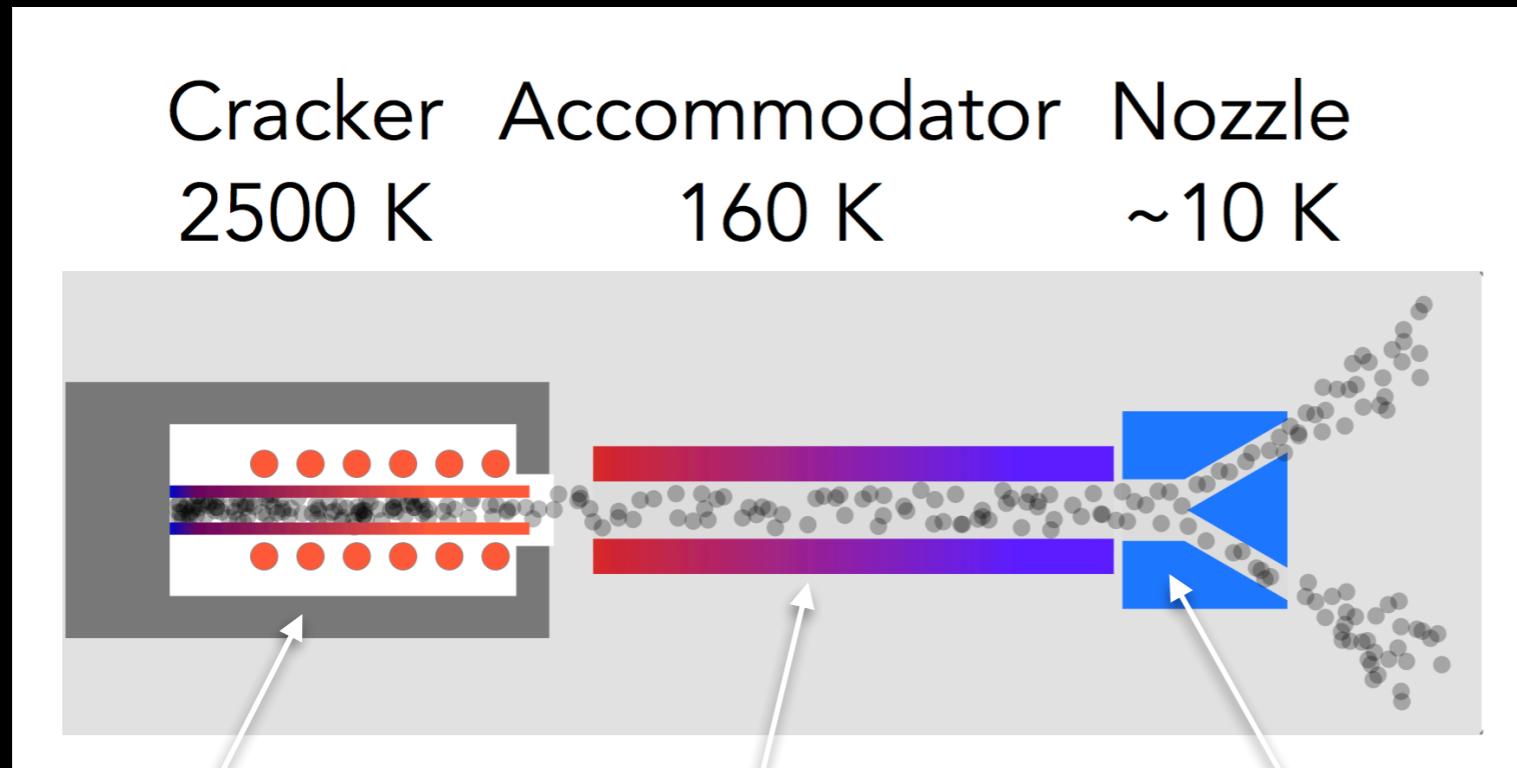
## Superfluid He containment

- ▶ does not work for tritium!



D. A. Knapp et al., AIP conference proceedings (1984)  
Wood and H. Wise, J. Chem. Phys. 66, 1049, (1962)

# Cooling tritium atoms



Cracker

→ purity vs. flow

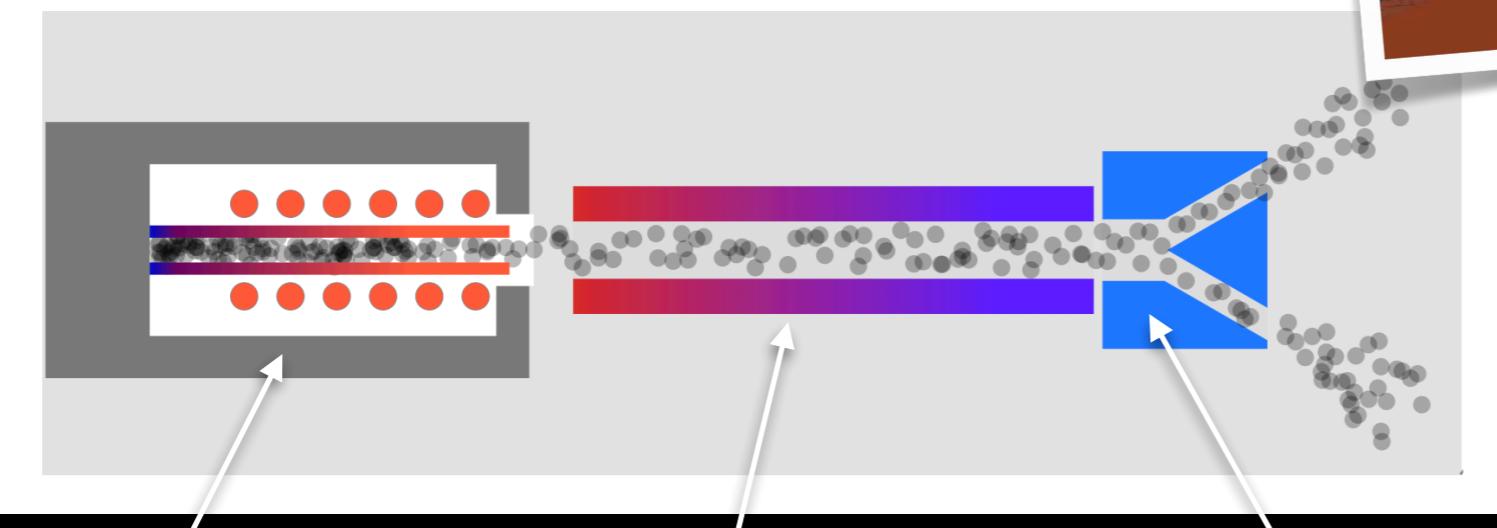
Accommodator  
(liquid nitrogen)

Final nozzle

- design for few bounces
  - freeze-out 30K
- periodic purging

# Cooling tritium atoms

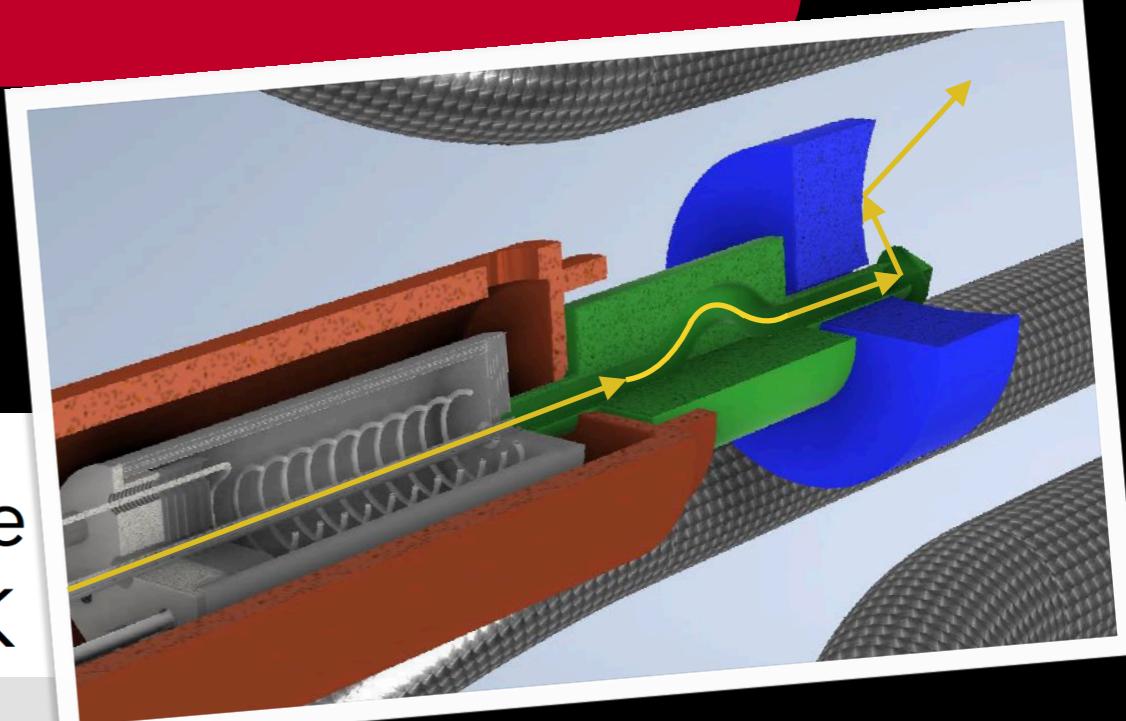
|         |              |        |
|---------|--------------|--------|
| Cracker | Accommodator | Nozzle |
| 2500 K  | 160 K        | ~10 K  |



Cracker  
→ purity vs. flow

Accommodator  
(liquid nitrogen)

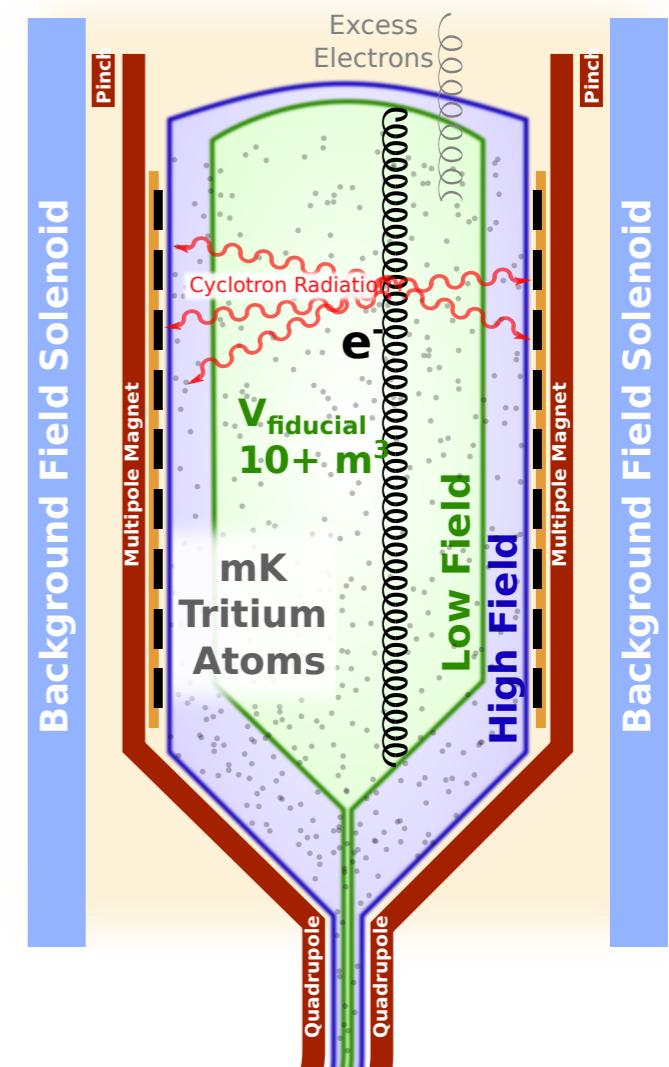
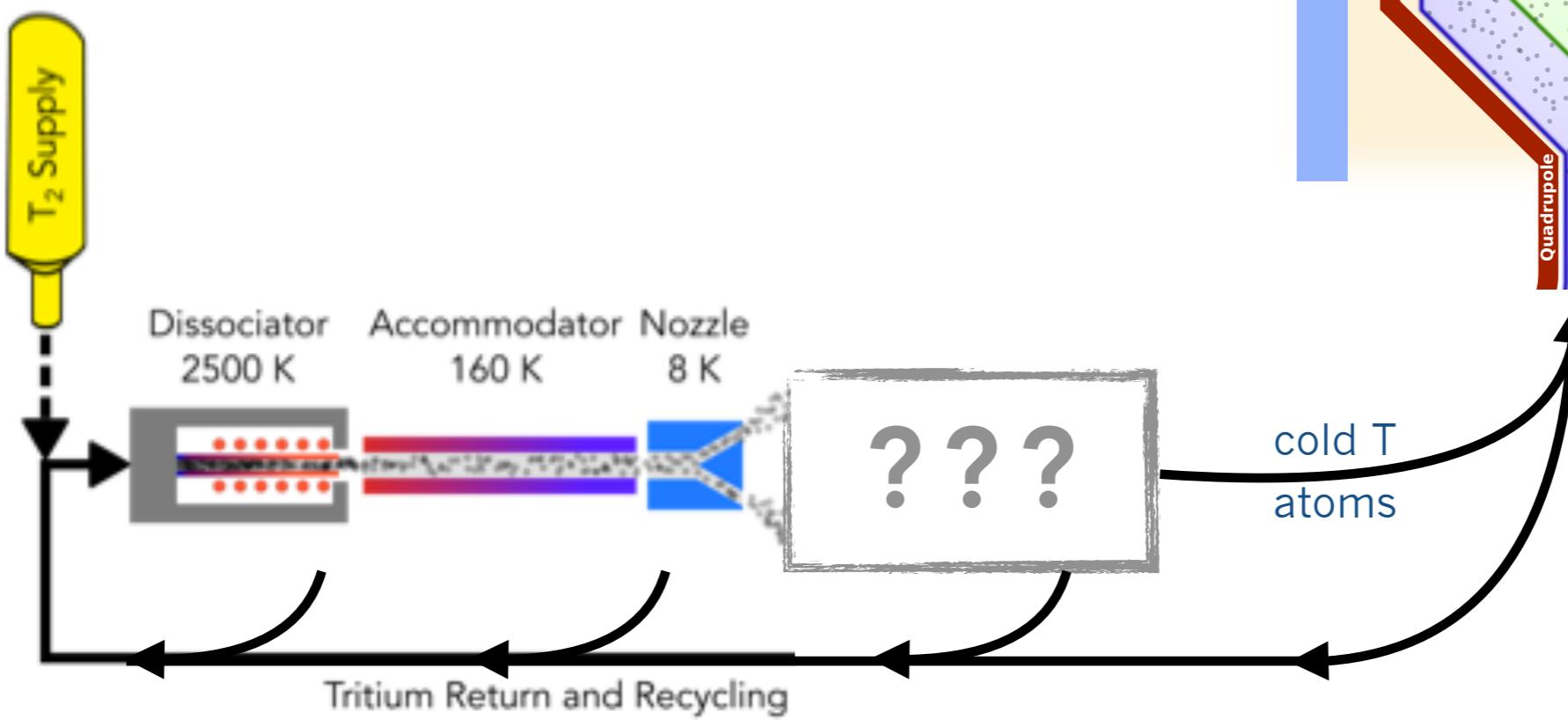
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# Project 8: Design concepts

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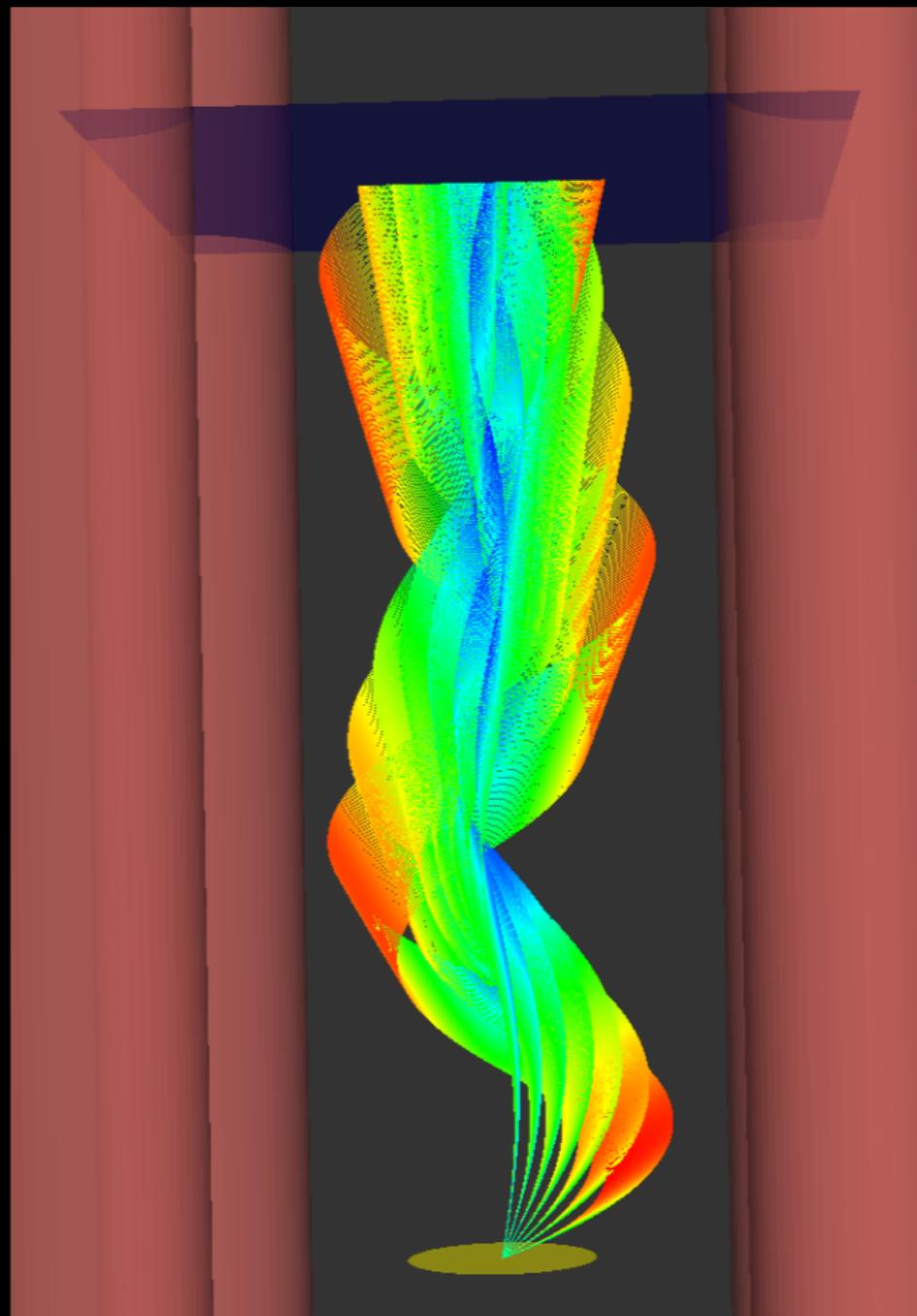
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# Velocity and State Selectors

Only atomic T guided magnetically

- (bend) quadrupole with skimmers



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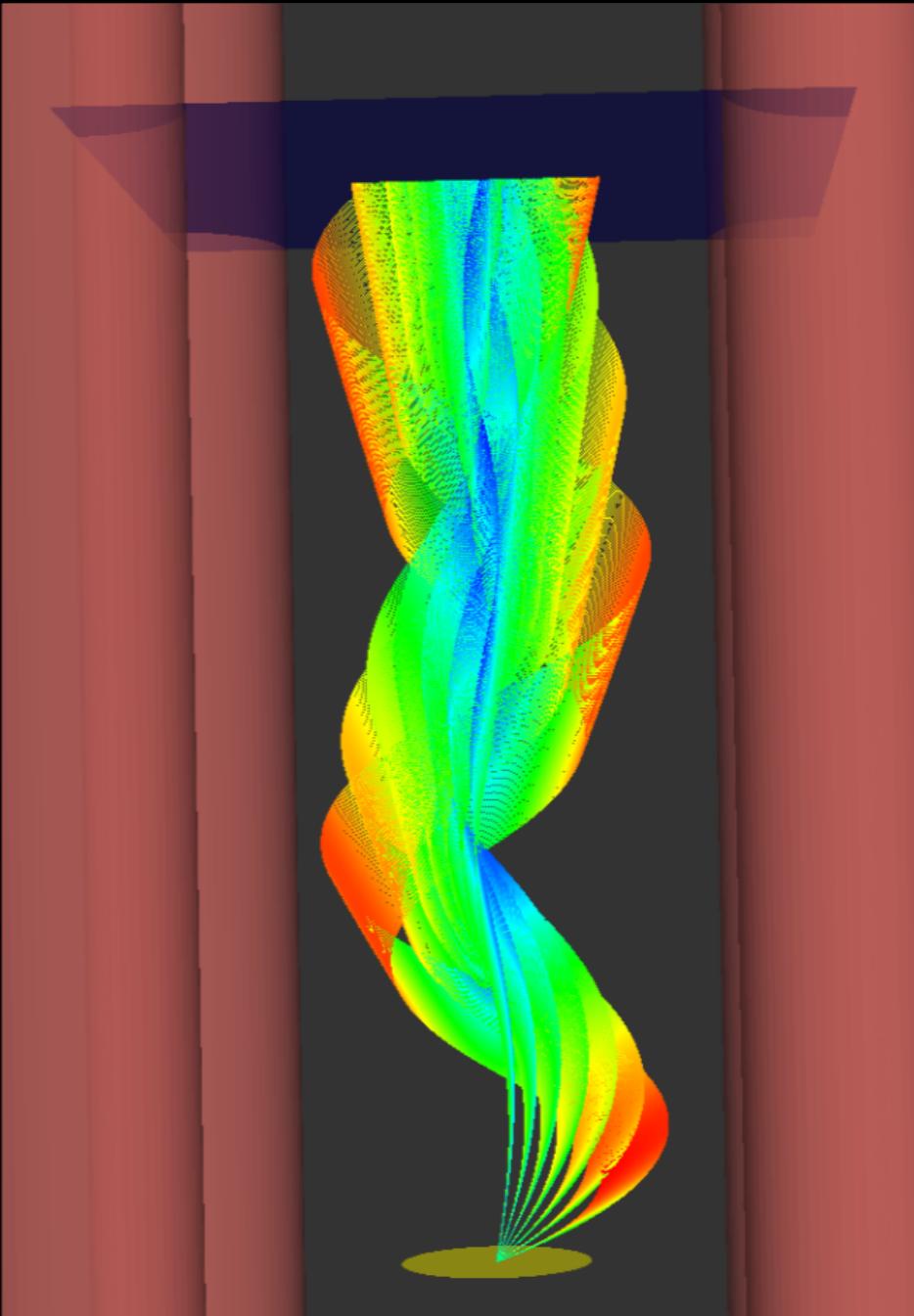
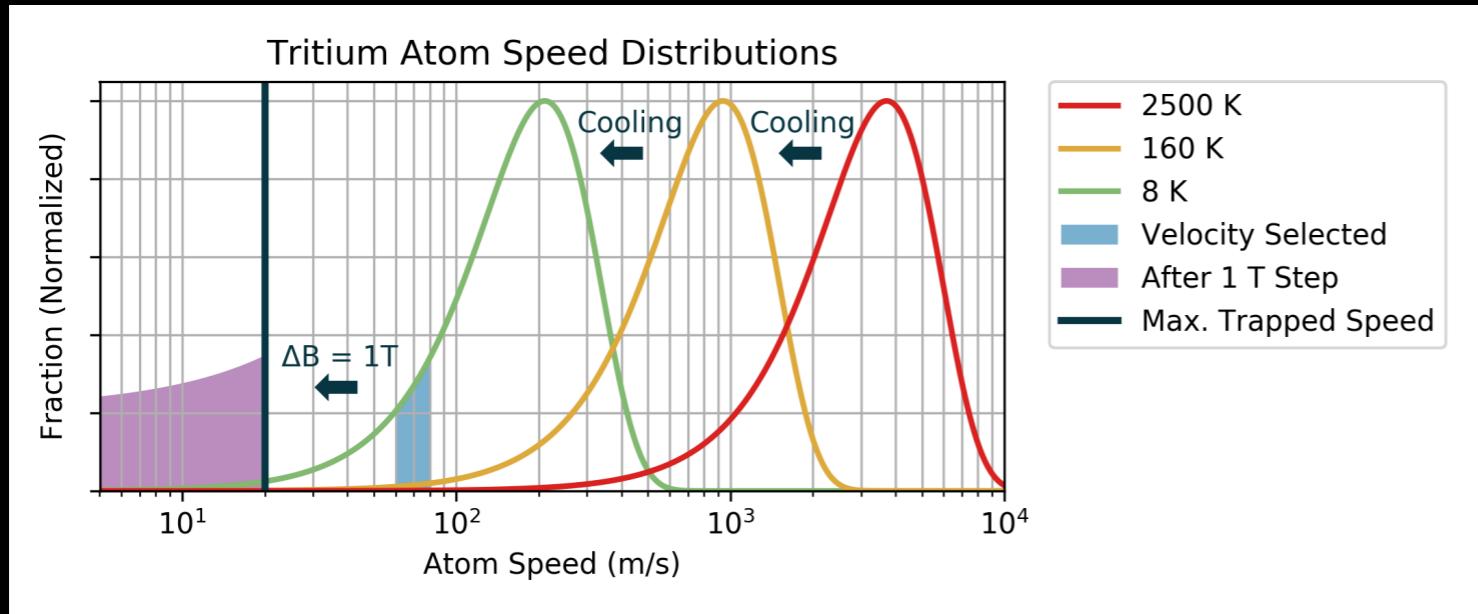
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Tune acceptance for

- $T_{\text{out}} = \mathcal{O}(50\text{mK})$
- $T_2$  contamination  $< 10^{-5}$ 
  - ▶ efficiency  $\epsilon_{\text{cold}} \sim 25\%-100\%$



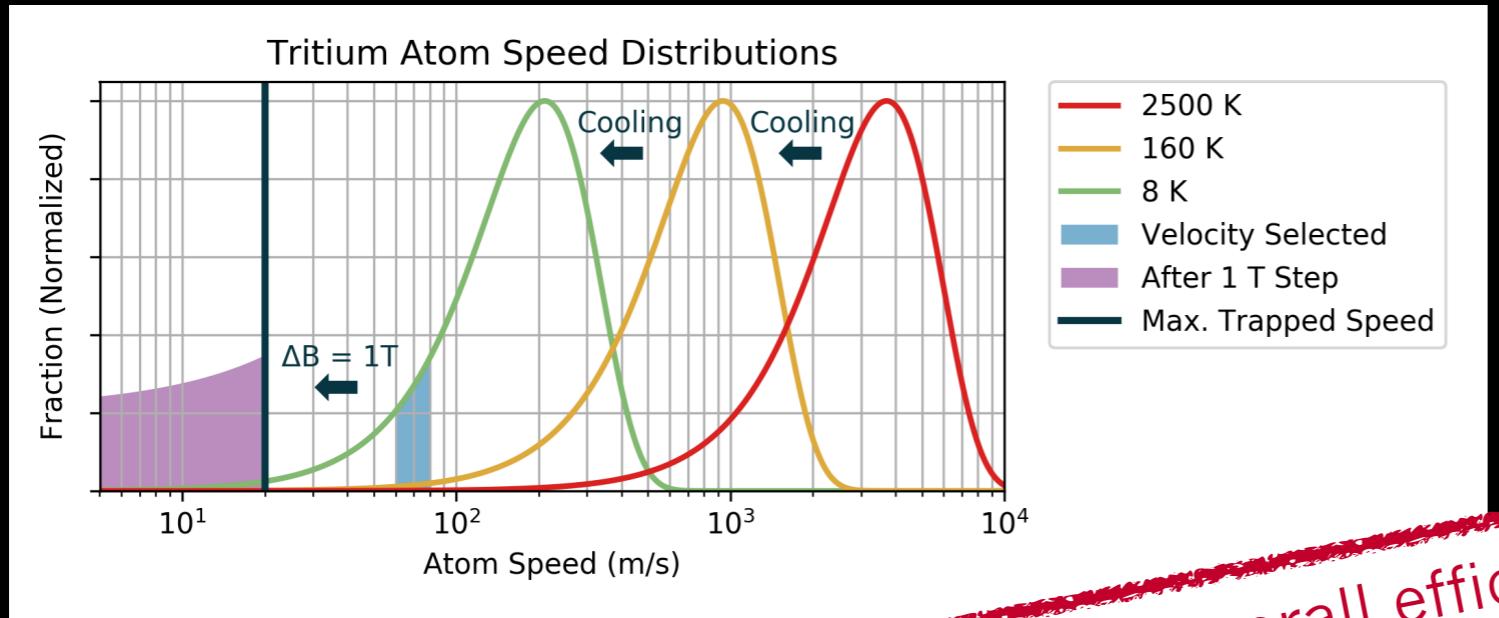
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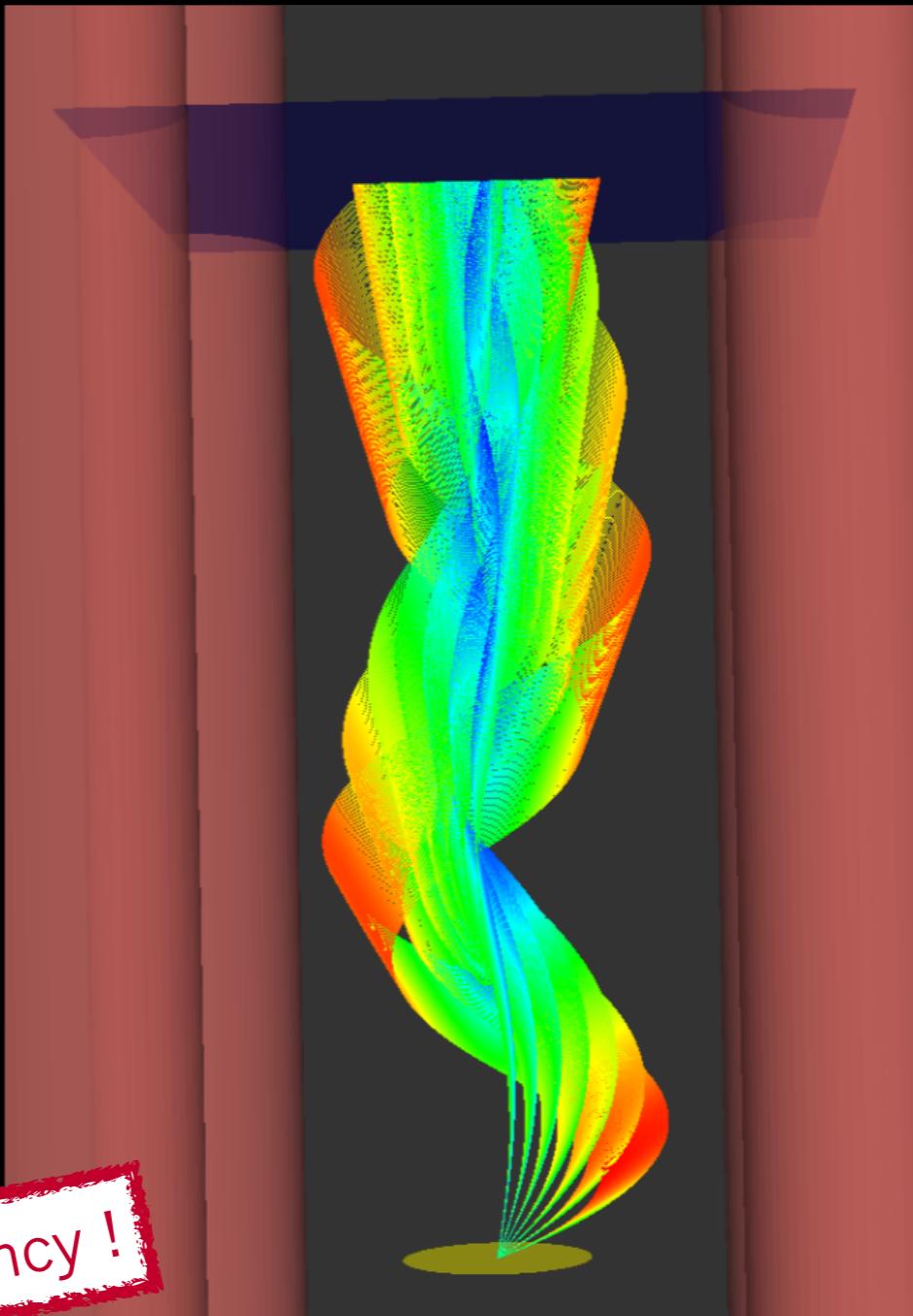
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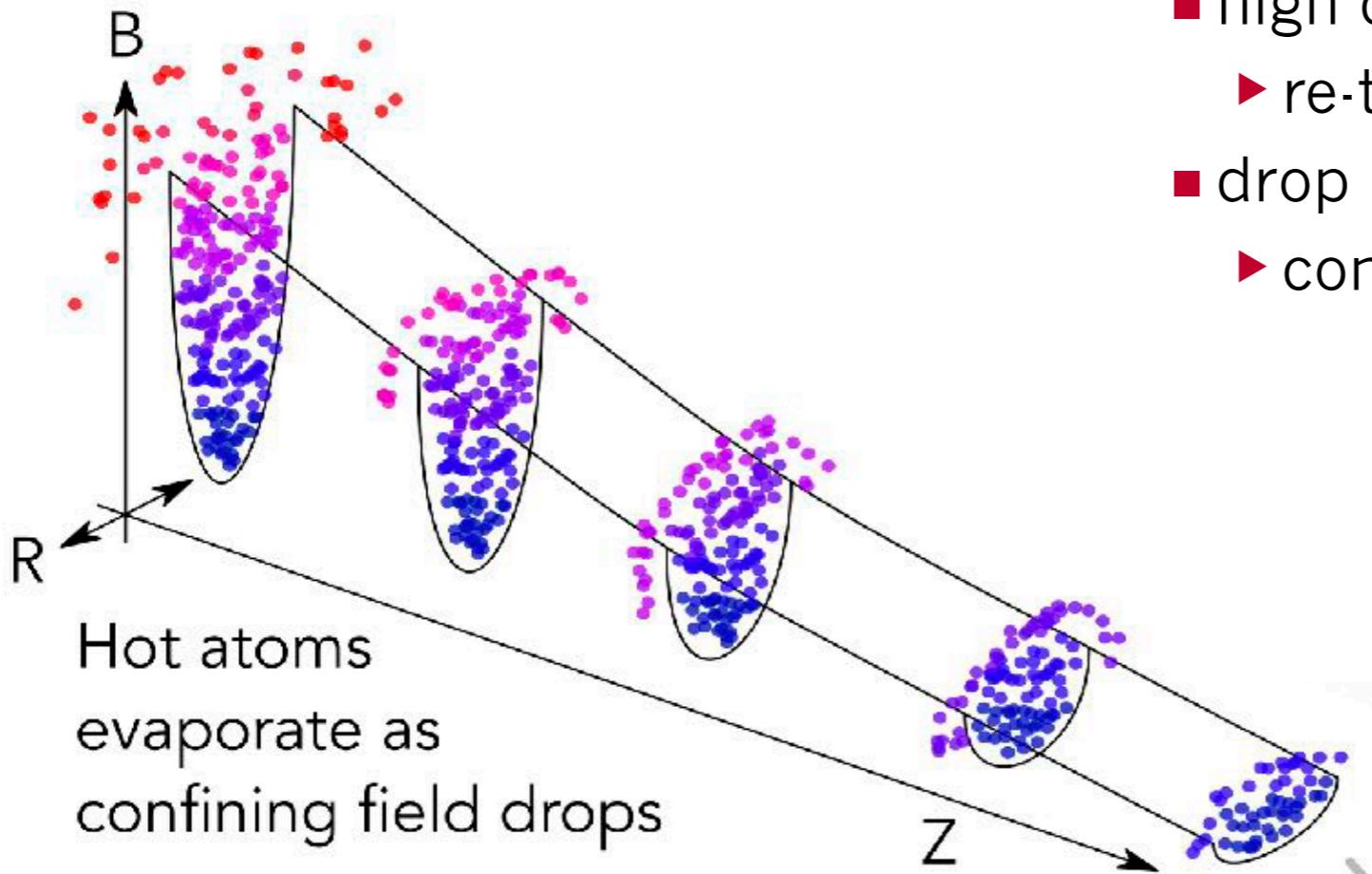
→ but poor overall efficiency !



# Evaporative cooling

## Evaporative cooling of an atomic beam

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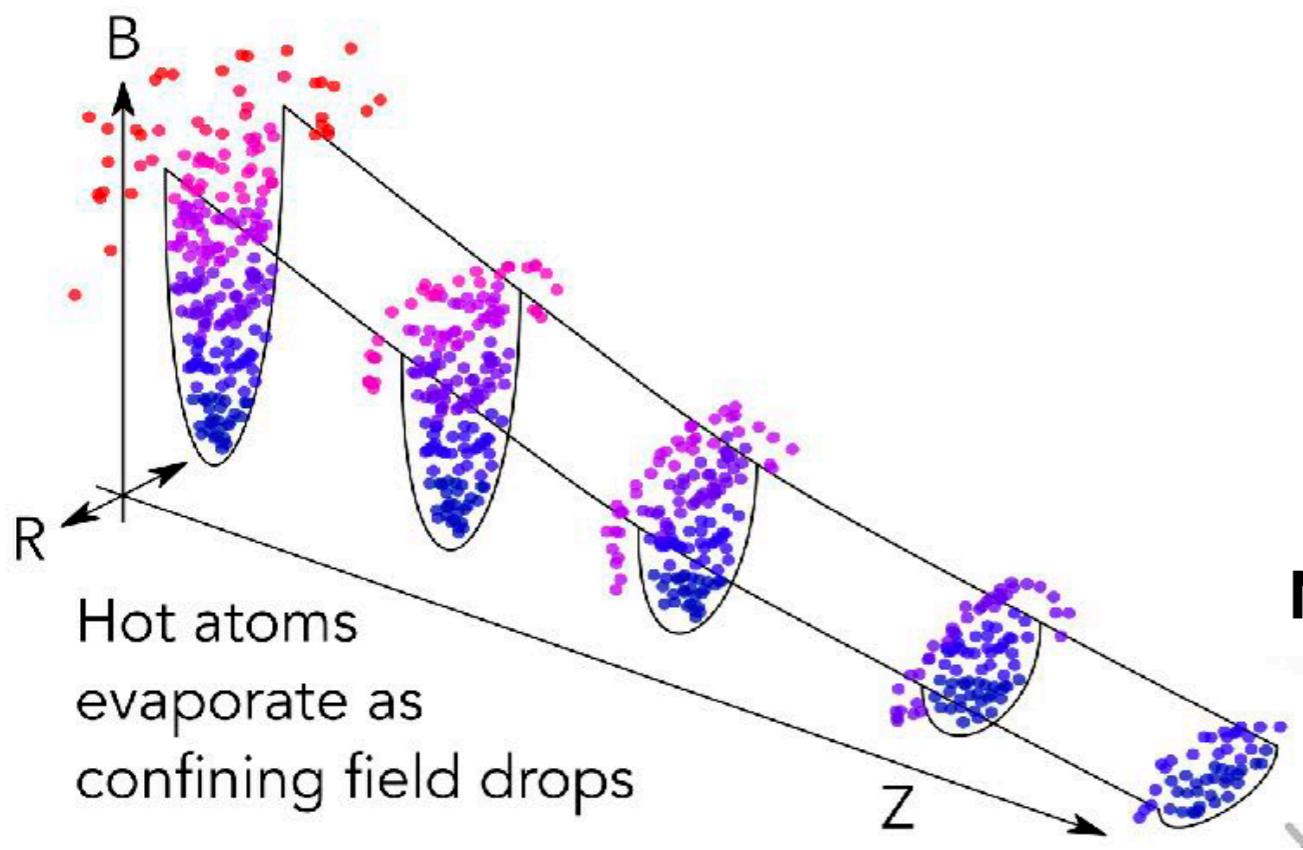
## Basic idea

- magnetic wall
  - ▶ loose *hot* atoms (high  $p_{\perp}$ )
- high density
  - ▶ re-thermalization
- drop magnetic field along beam
  - ▶ continuous cooling

# Evaporative cooling: the math

## Evaporation efficiency $\eta_{\text{ev}}$

$$\mu B(z) = \eta_{\text{ev}} k_B T(z)$$



- large  $\eta_{\text{ev}}$ 
  - ▶ slow cooling, high efficiency
- small  $\eta_{\text{ev}}$ 
  - ▶ fast cooling, low efficiency

## Number density

$$n \propto T^{1/\gamma} \quad \text{with} \quad \gamma = \frac{2}{3} \left( \eta_{\text{ev}} + \frac{1}{2} - C \right)$$

- optimal value ( $C = 2$ ,  $\eta_{\text{ev}} = 4.5$ )

$$\triangleright \gamma = 2 \quad \rightarrow \quad n \propto T^{\frac{1}{2}}$$

→ assumes equilibrium !

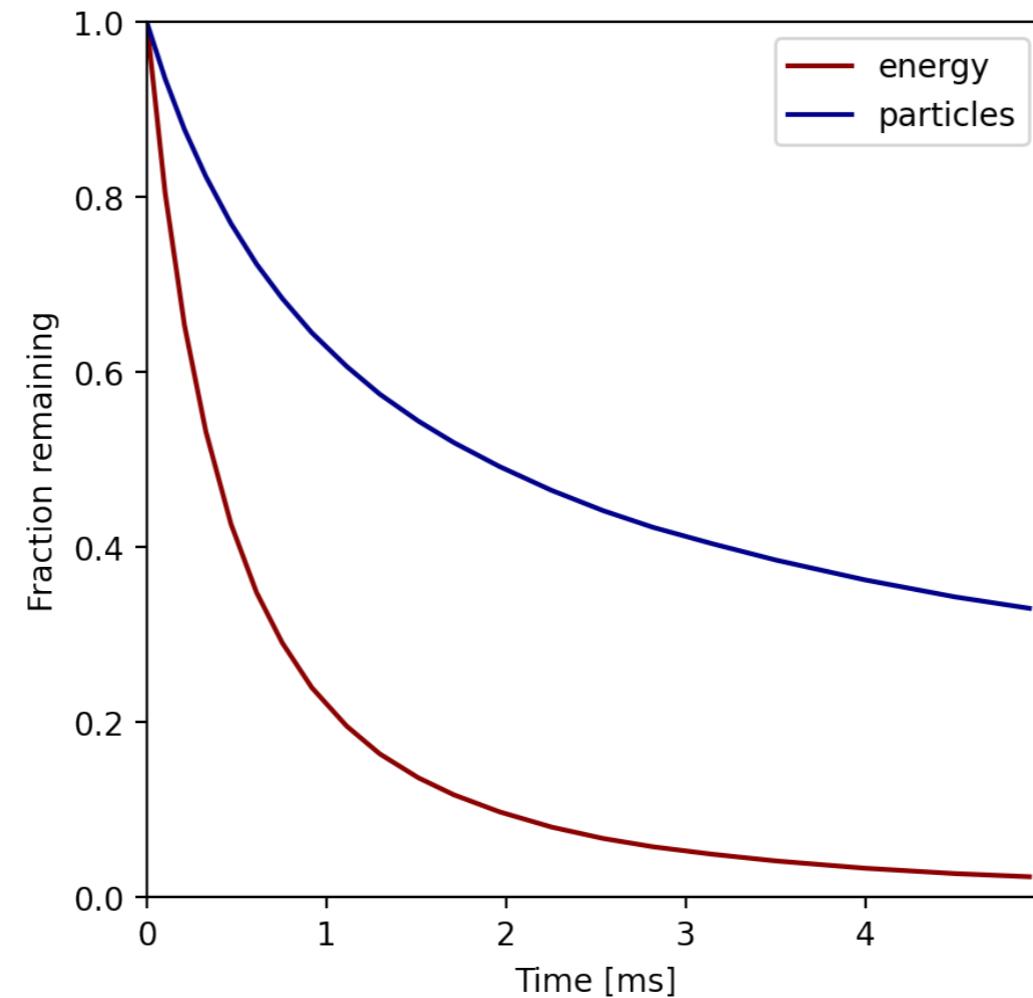
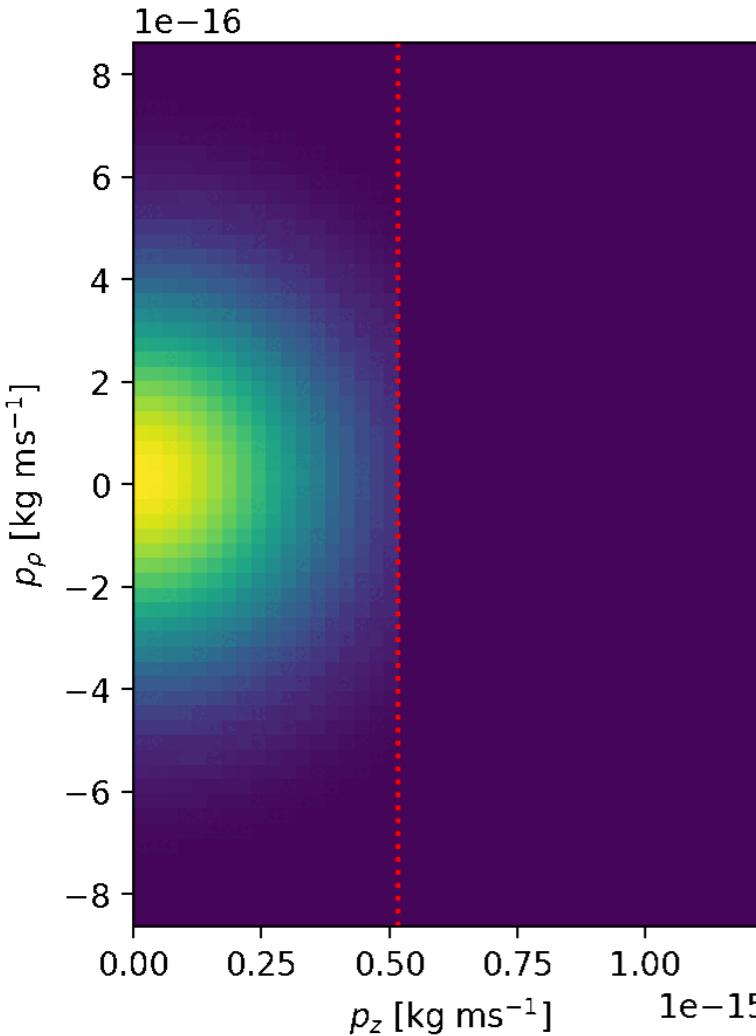
# Evaporative cooling: the hard math

Boltzmann transport equation

$$\left( \frac{p}{m} \nabla_r - \nabla_r U \cdot \nabla_p + \frac{\partial}{\partial t} \right) f(r, p) = \frac{1}{\pi m^2} \int d^3 p_2 \int d^3 p_3 \int d^3 p_4 \frac{d\sigma}{d\Omega}(p_1, p_2, p_3, p_4) (f(r, p_3) f(r, p_4) - f(r, p) f(r, p_2))$$

 **kinetic terms**       **collision integral**

► solve numerically

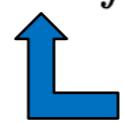


- Losing energy faster than particles means cooling
- Radial cooling also cools longitudinal motion since collisions redistribute momentum

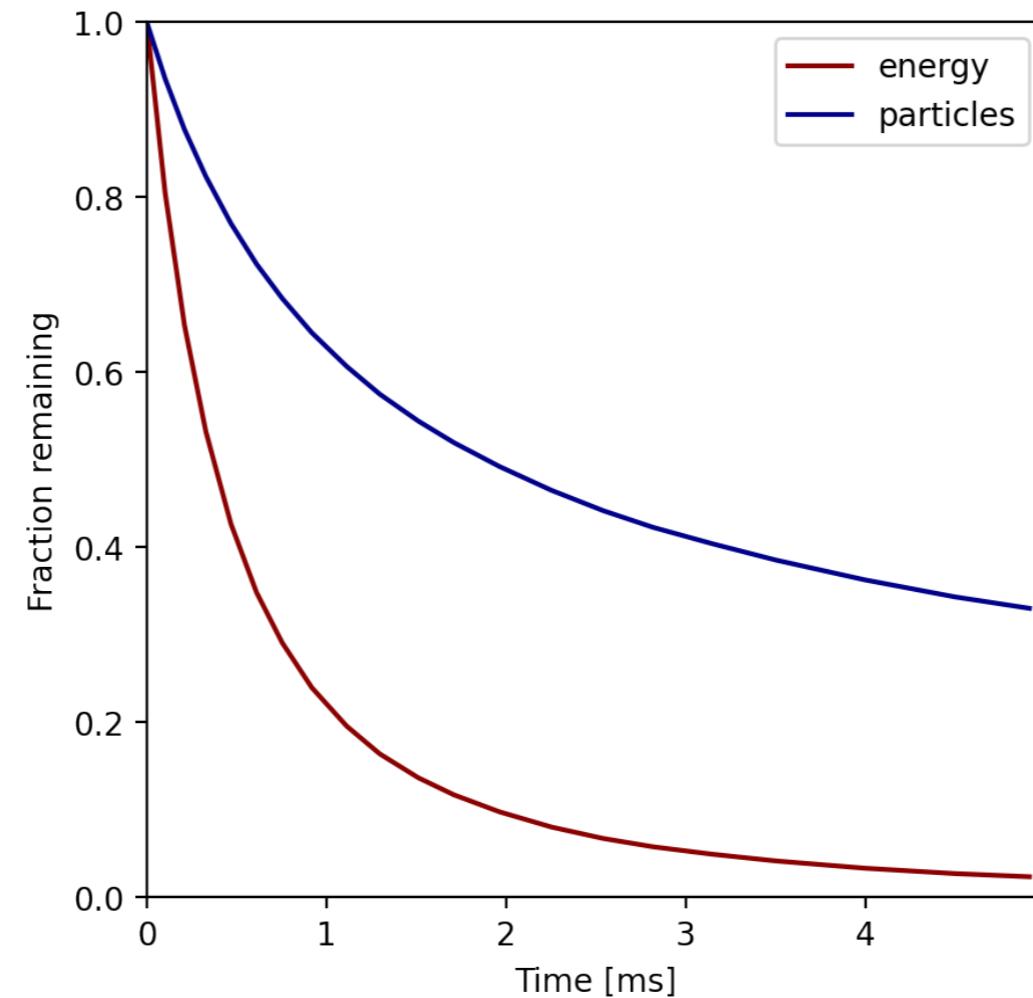
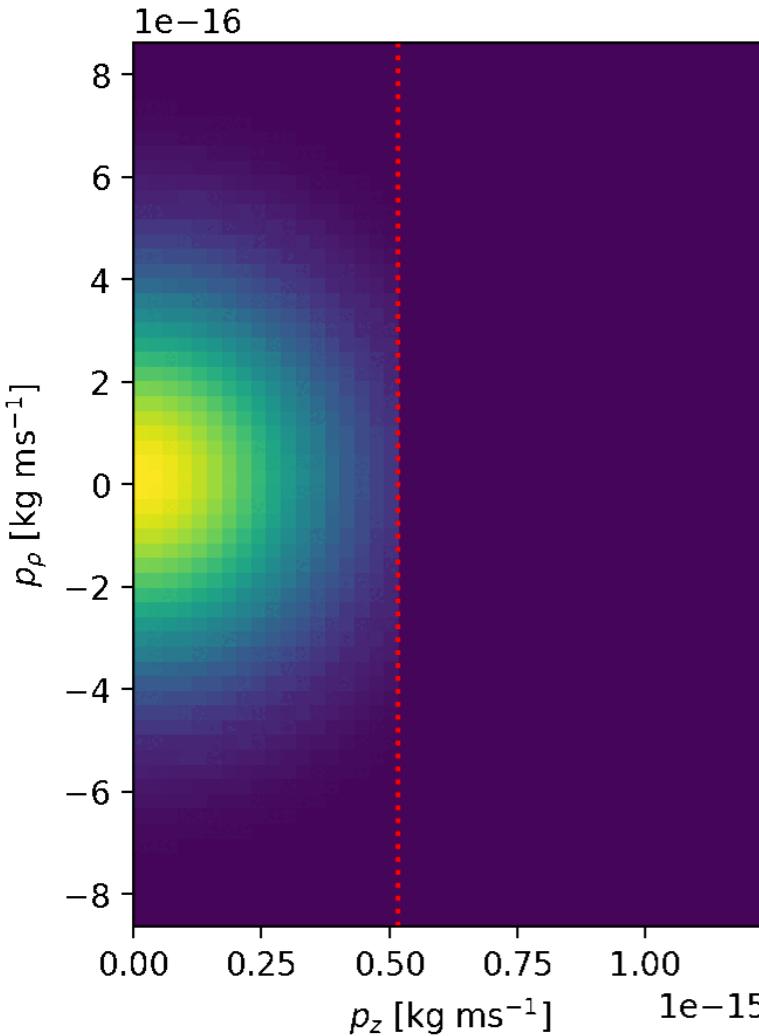
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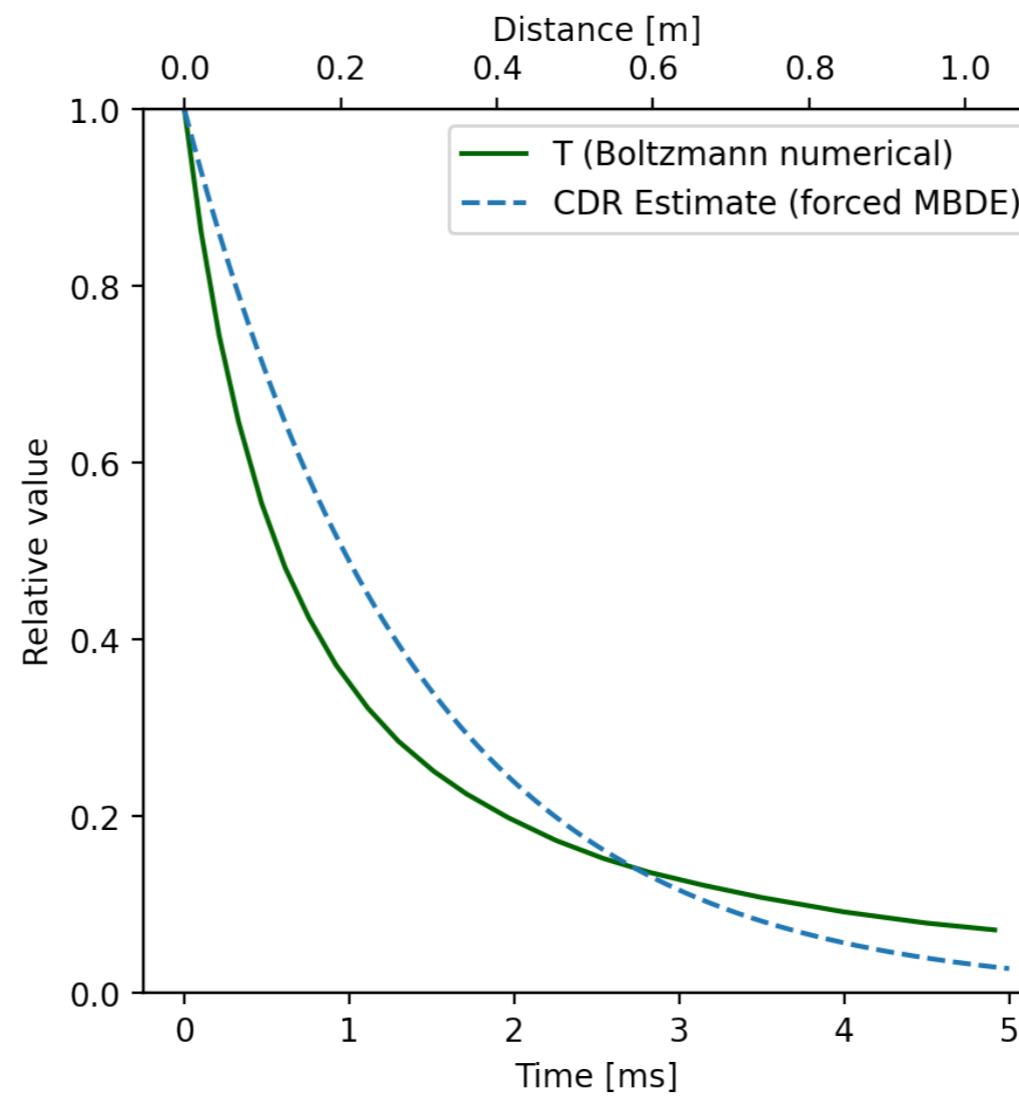
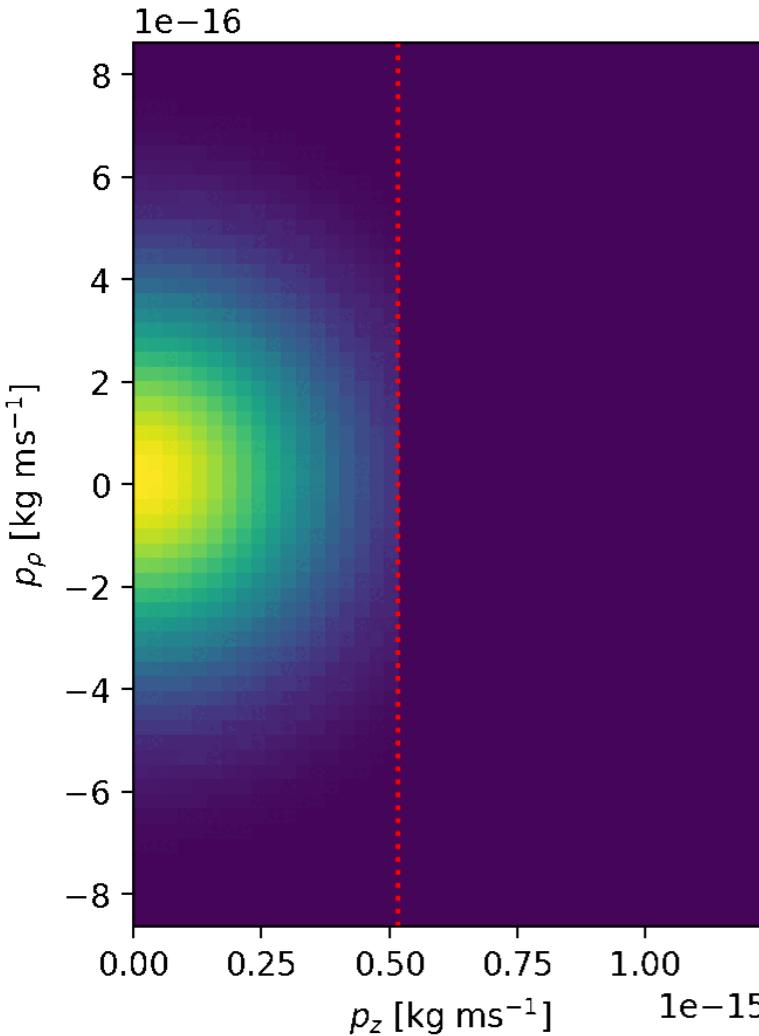
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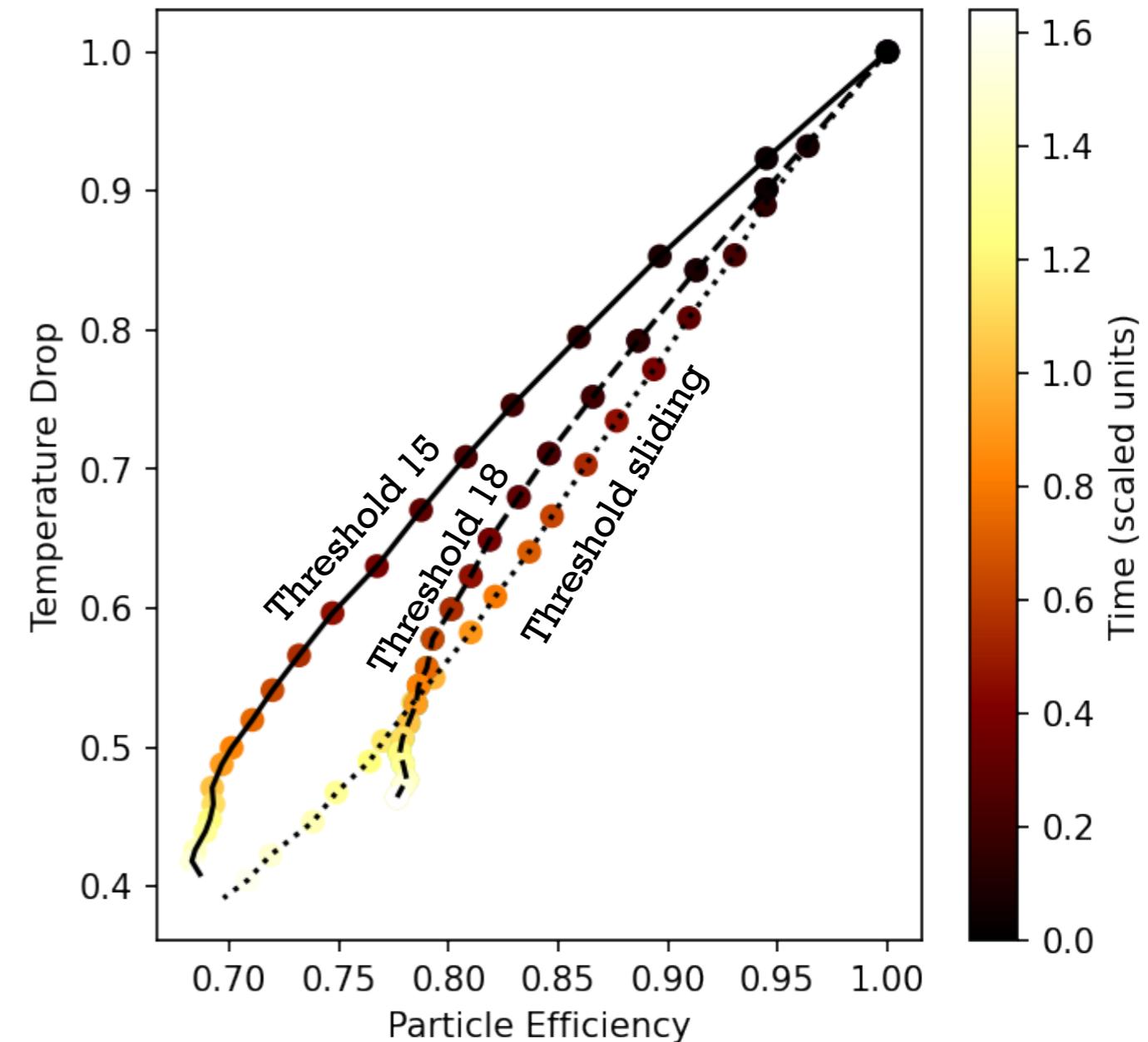
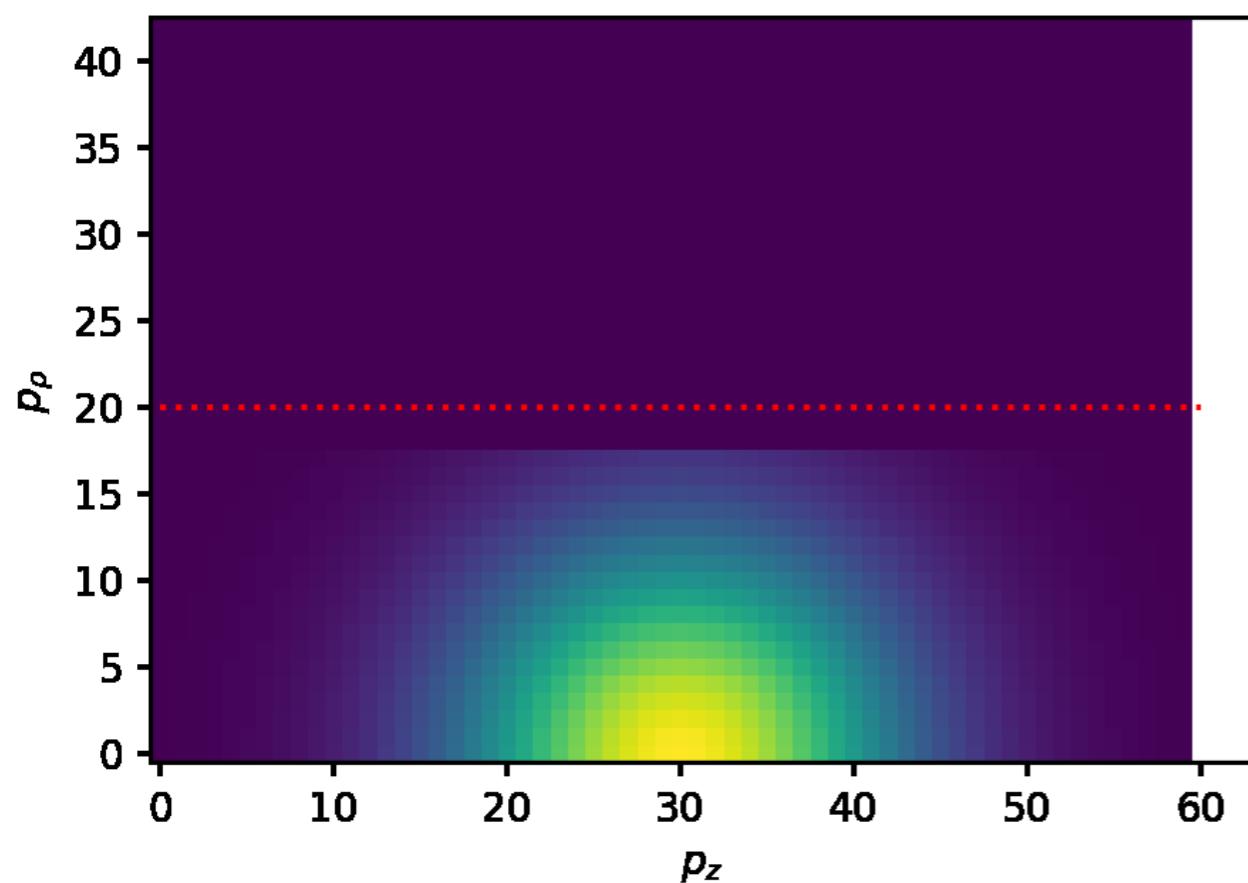
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# Evaporative cooling: sliding threshold

## Original idea

- decrease wall height with time
  - ▶ faster cooling (initially)

→ large phase space left to explore

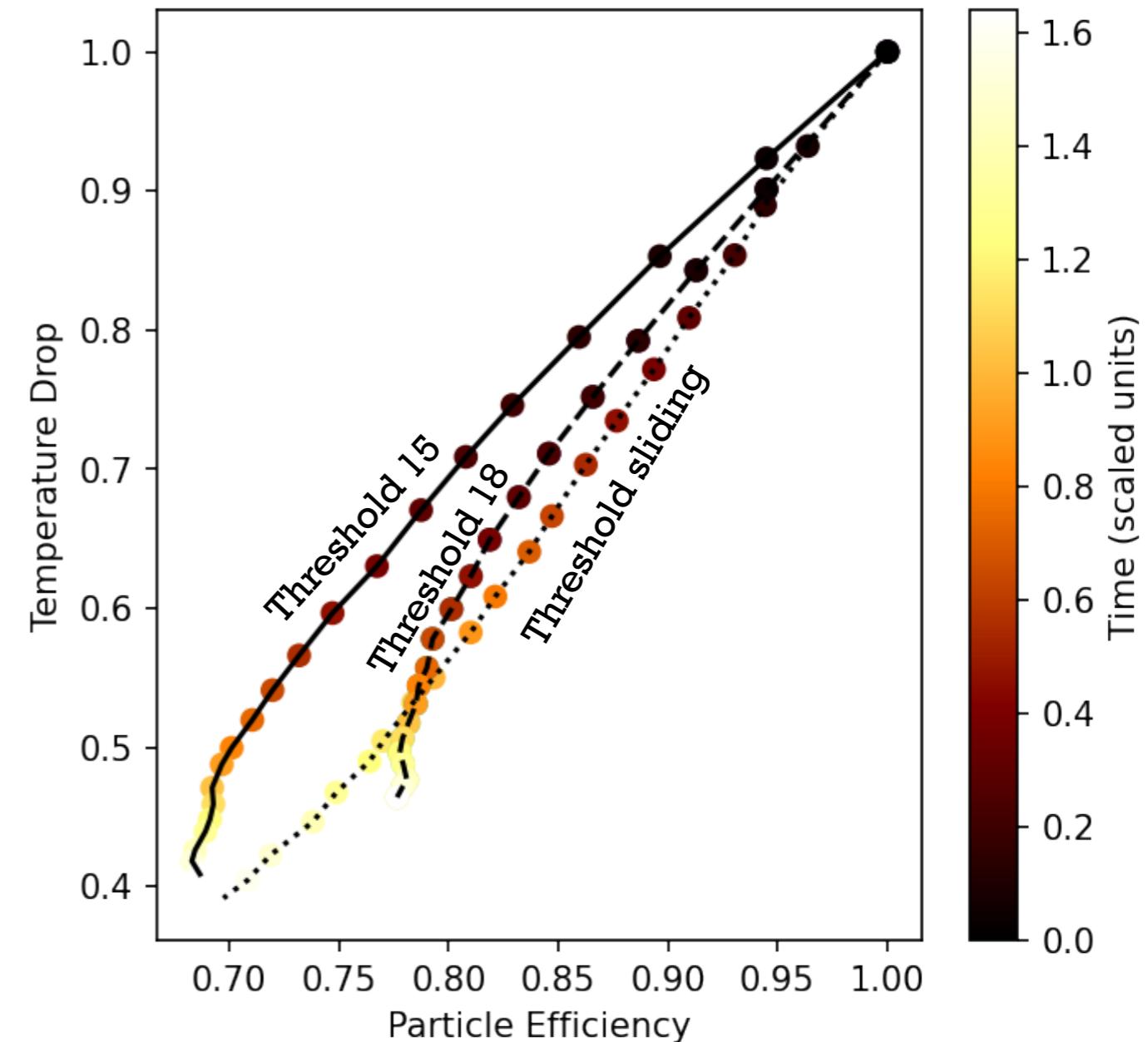
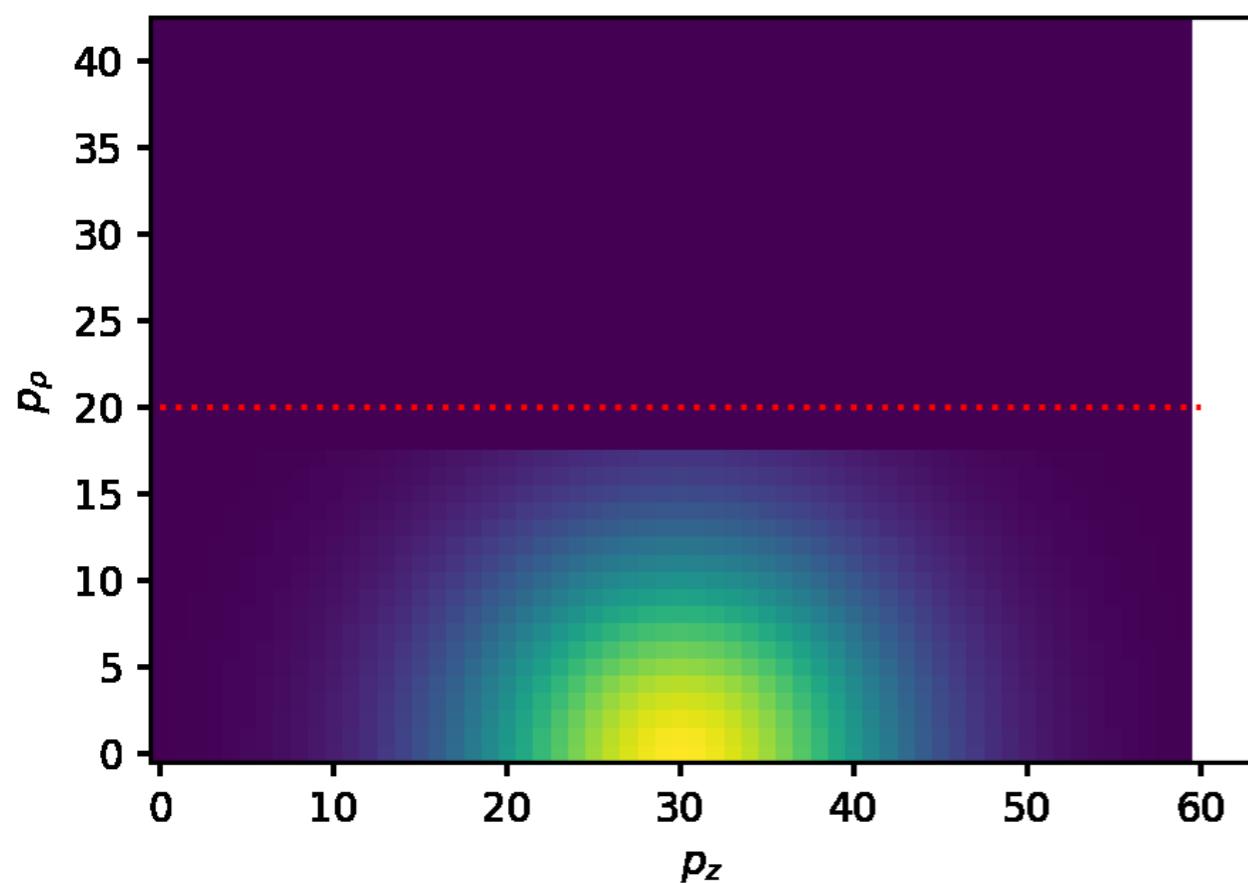


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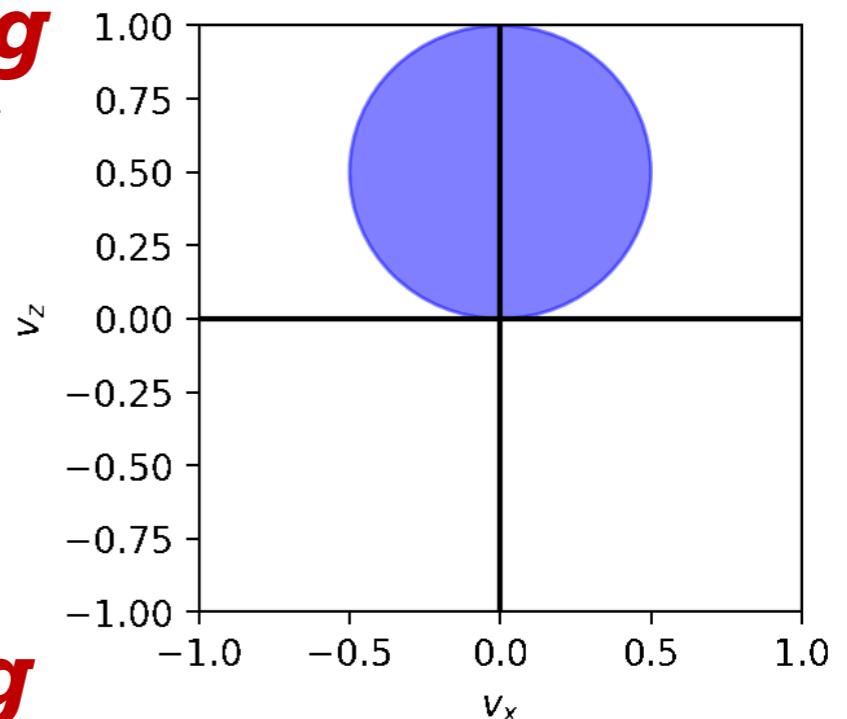
# Cooling vs slowing

Initial atomic beam

- net forward momentum
- ▶ need **cooling** and **slowing**

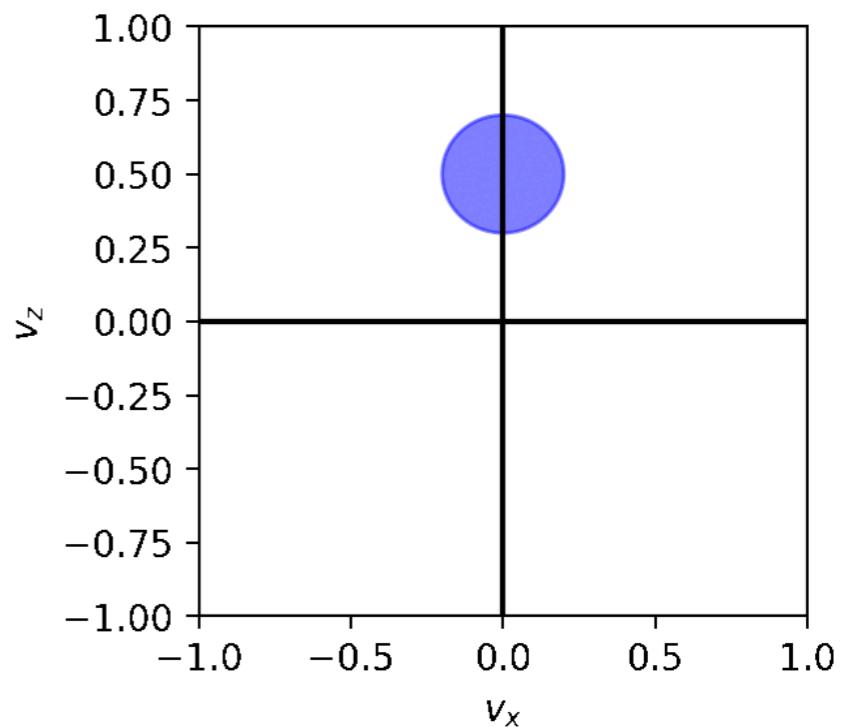
**Cooling**

Mean( $p$ ) conserved



**Slowing**

Mean( $p$ ) reduced



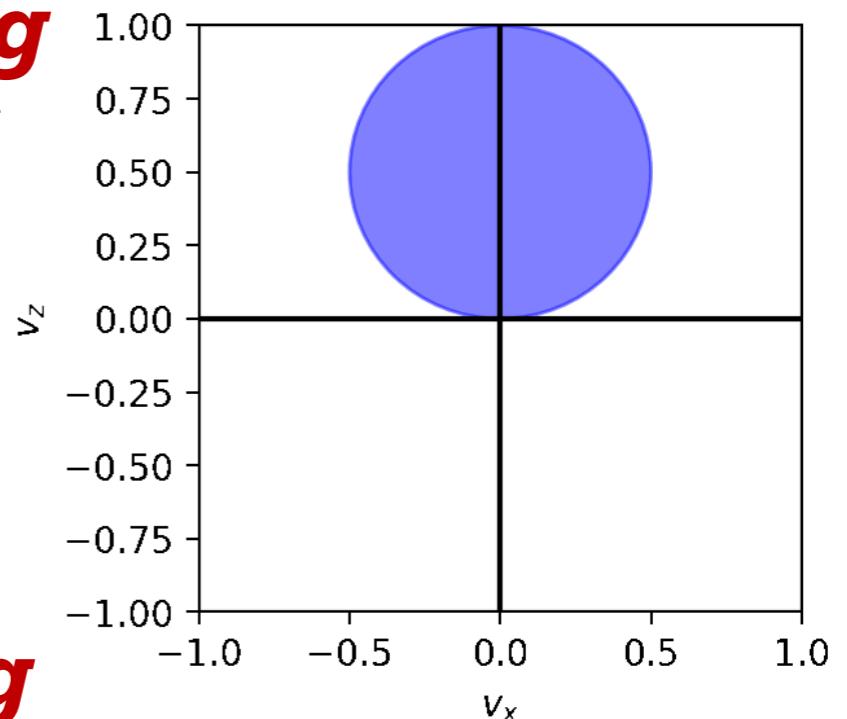
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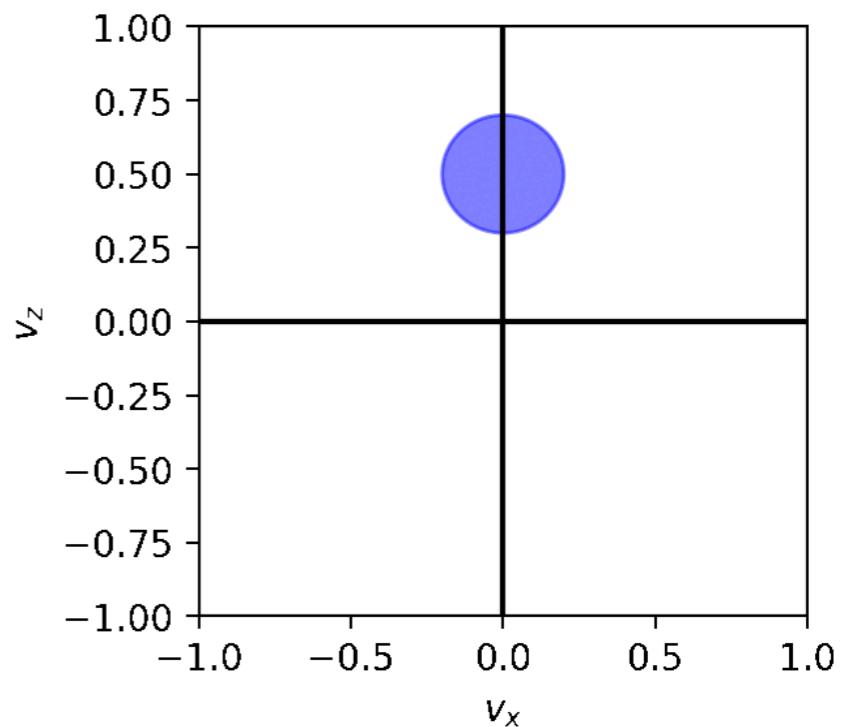
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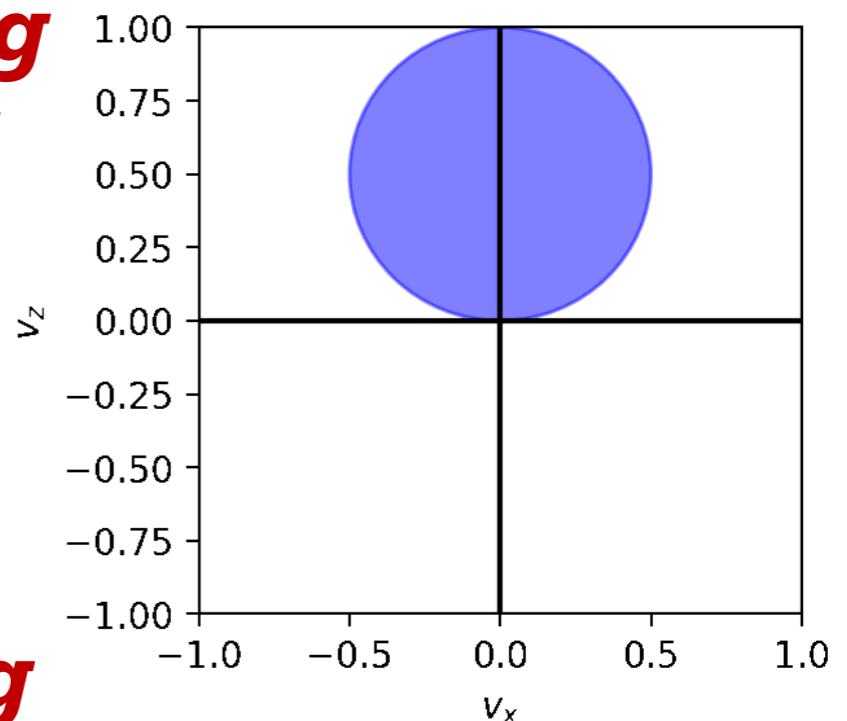
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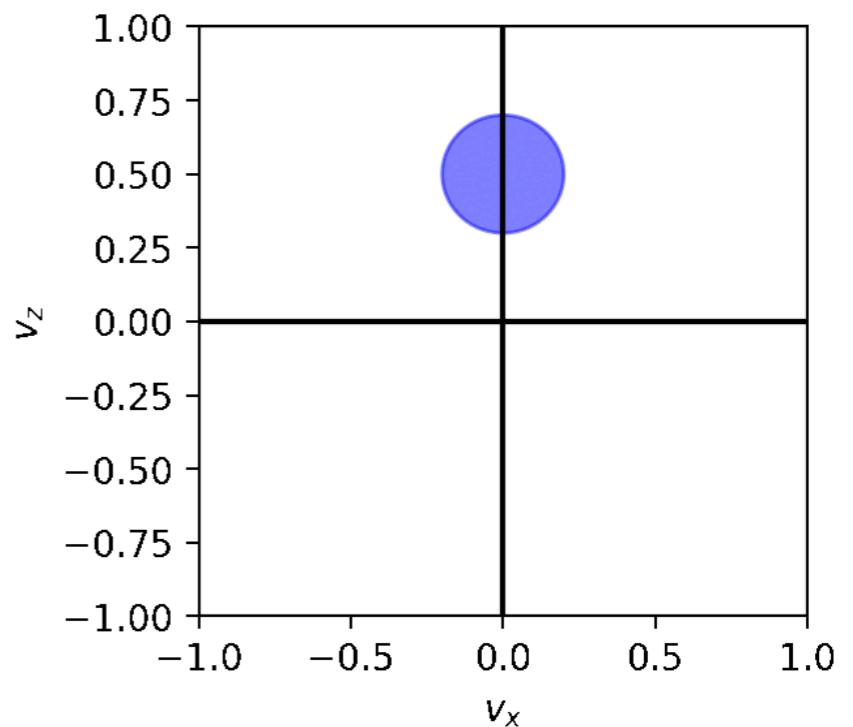
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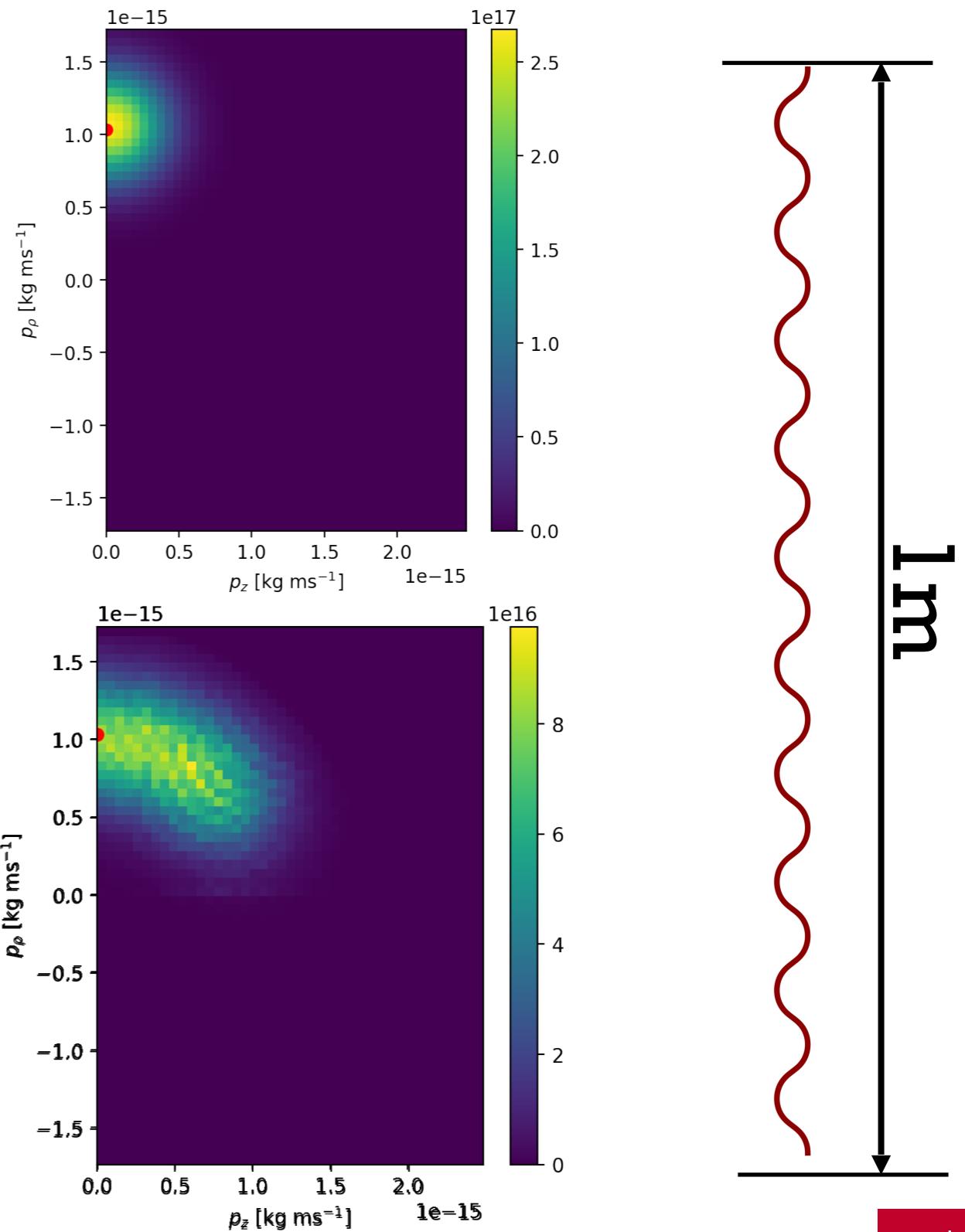
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The *wiggler*

- several wiggles within mean free path
  - ▶ transfer longitudinal to perpendicular momentum
- re-thermalization
  - ▶ slows down beam



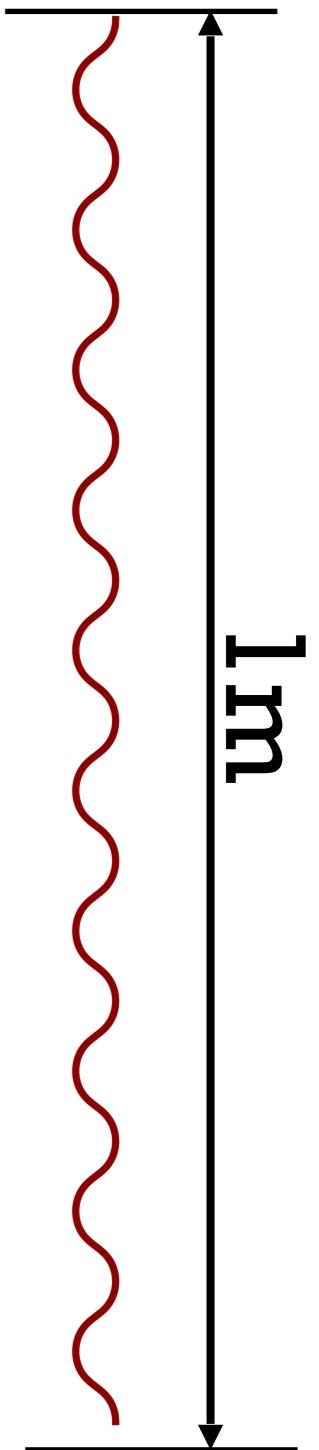
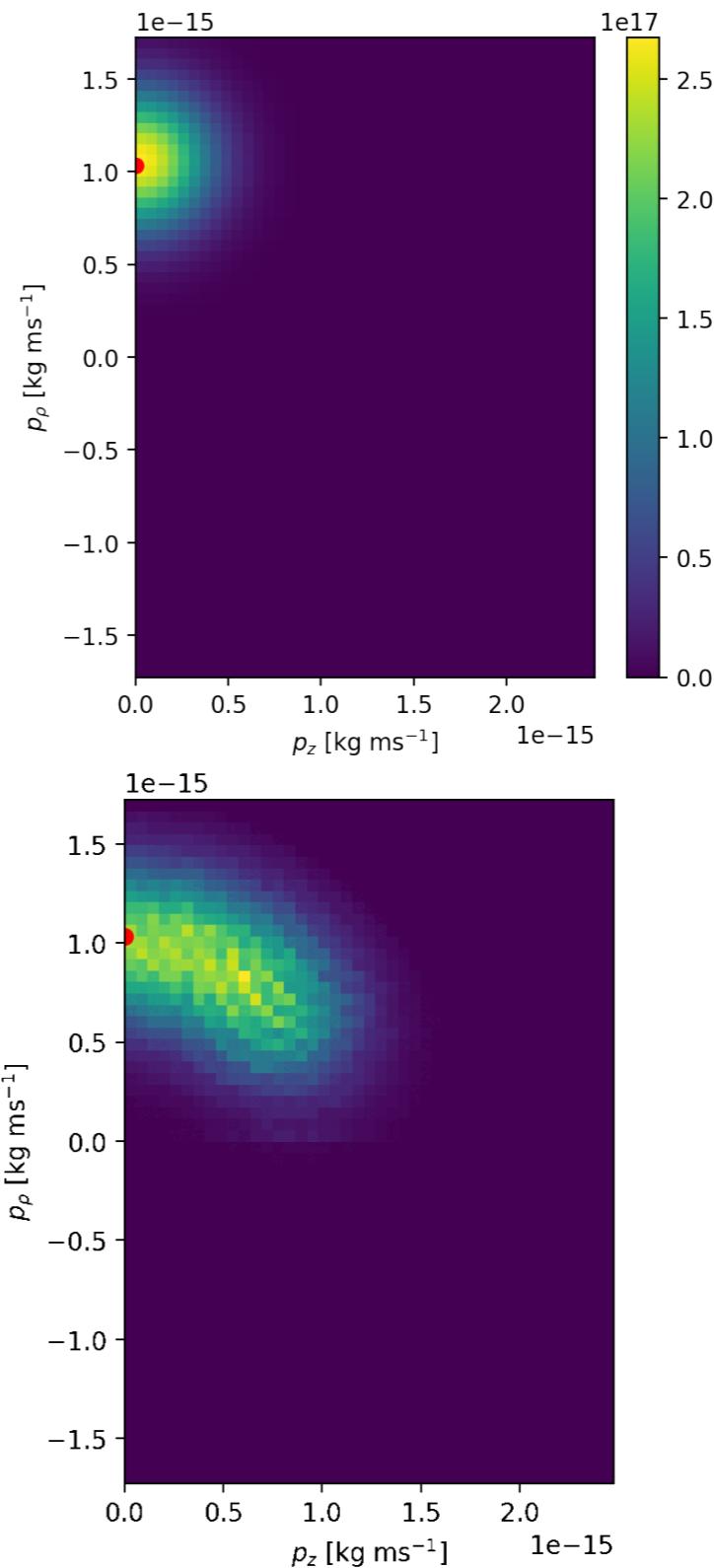
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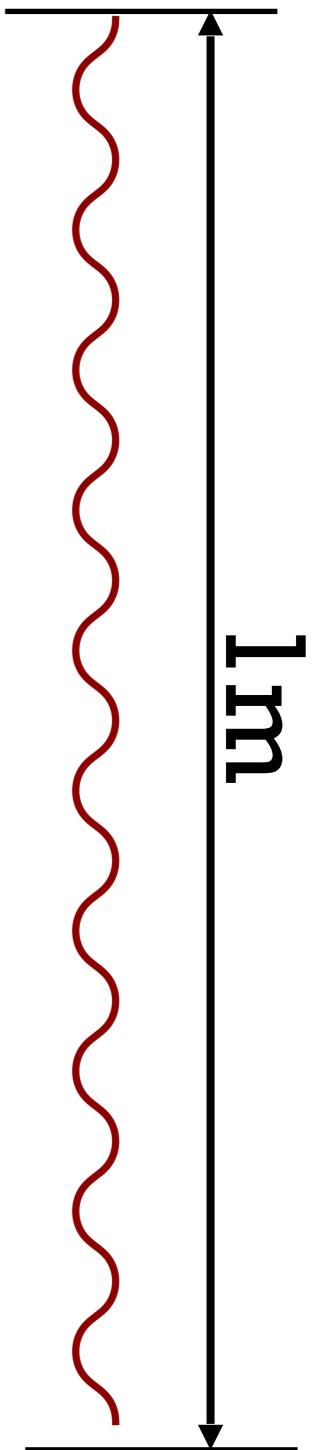
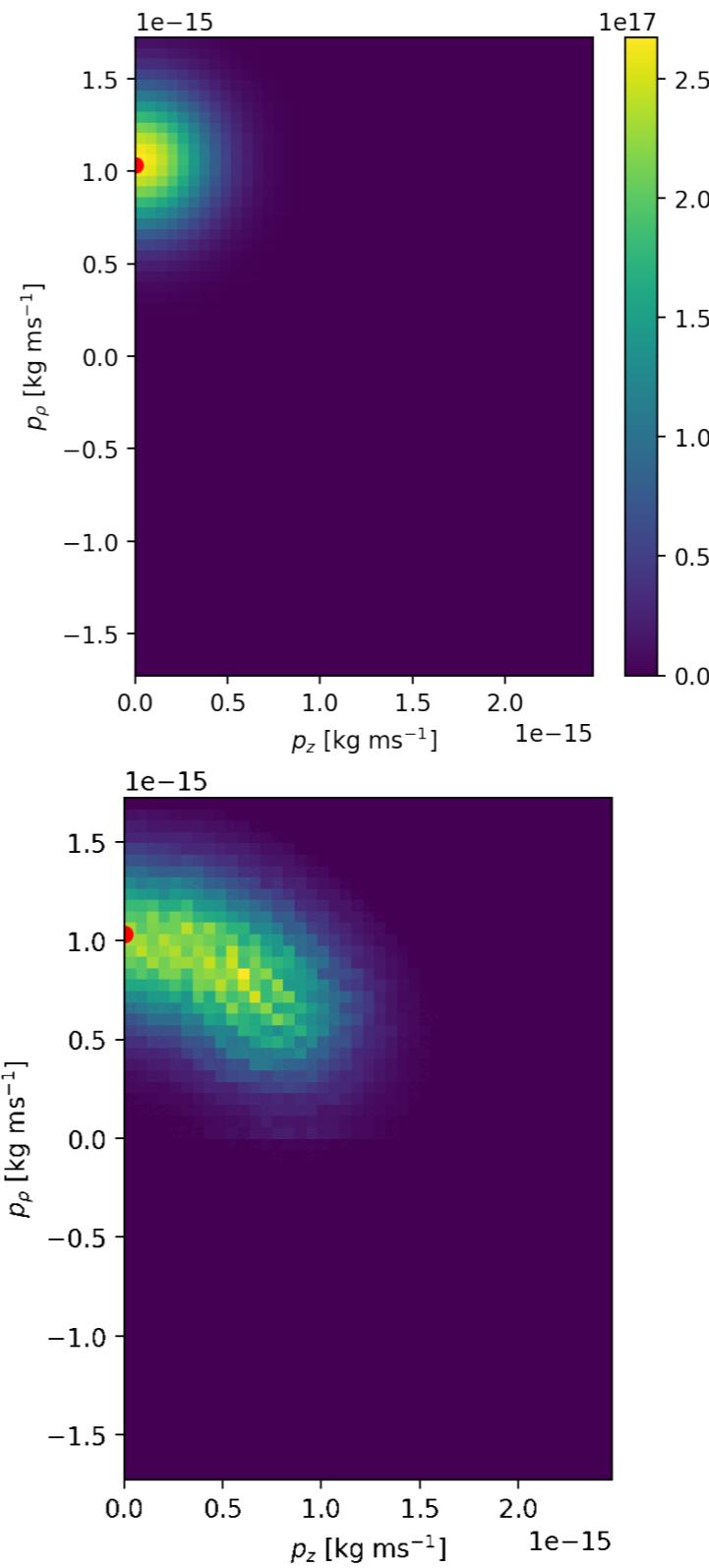
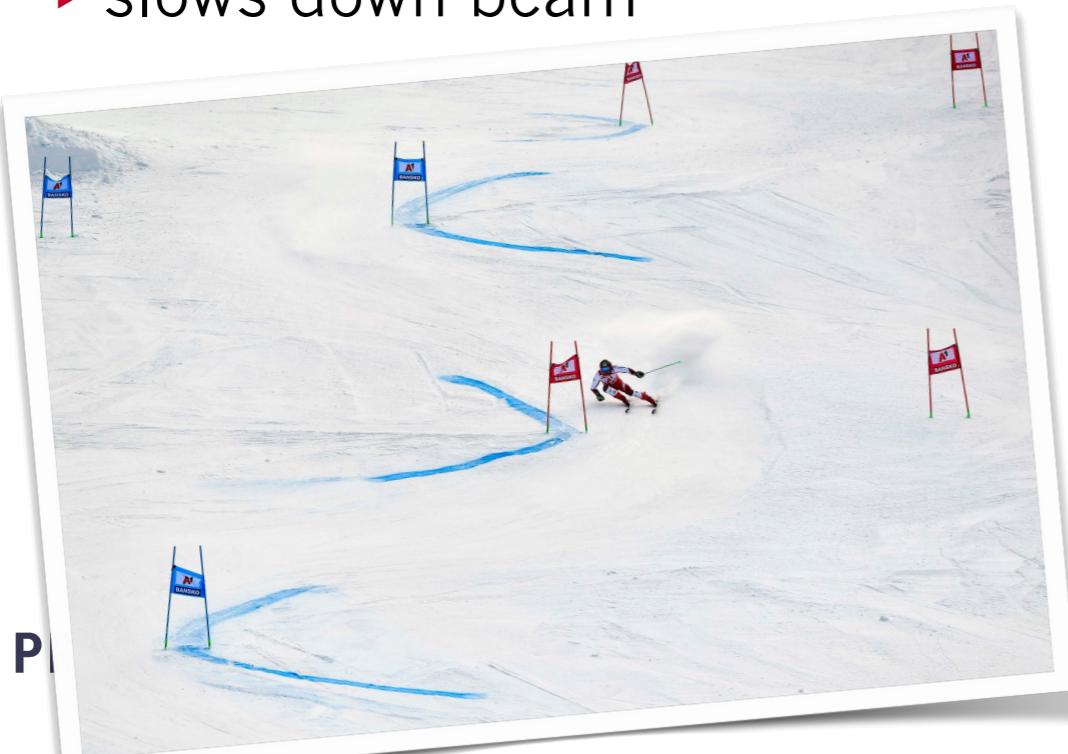
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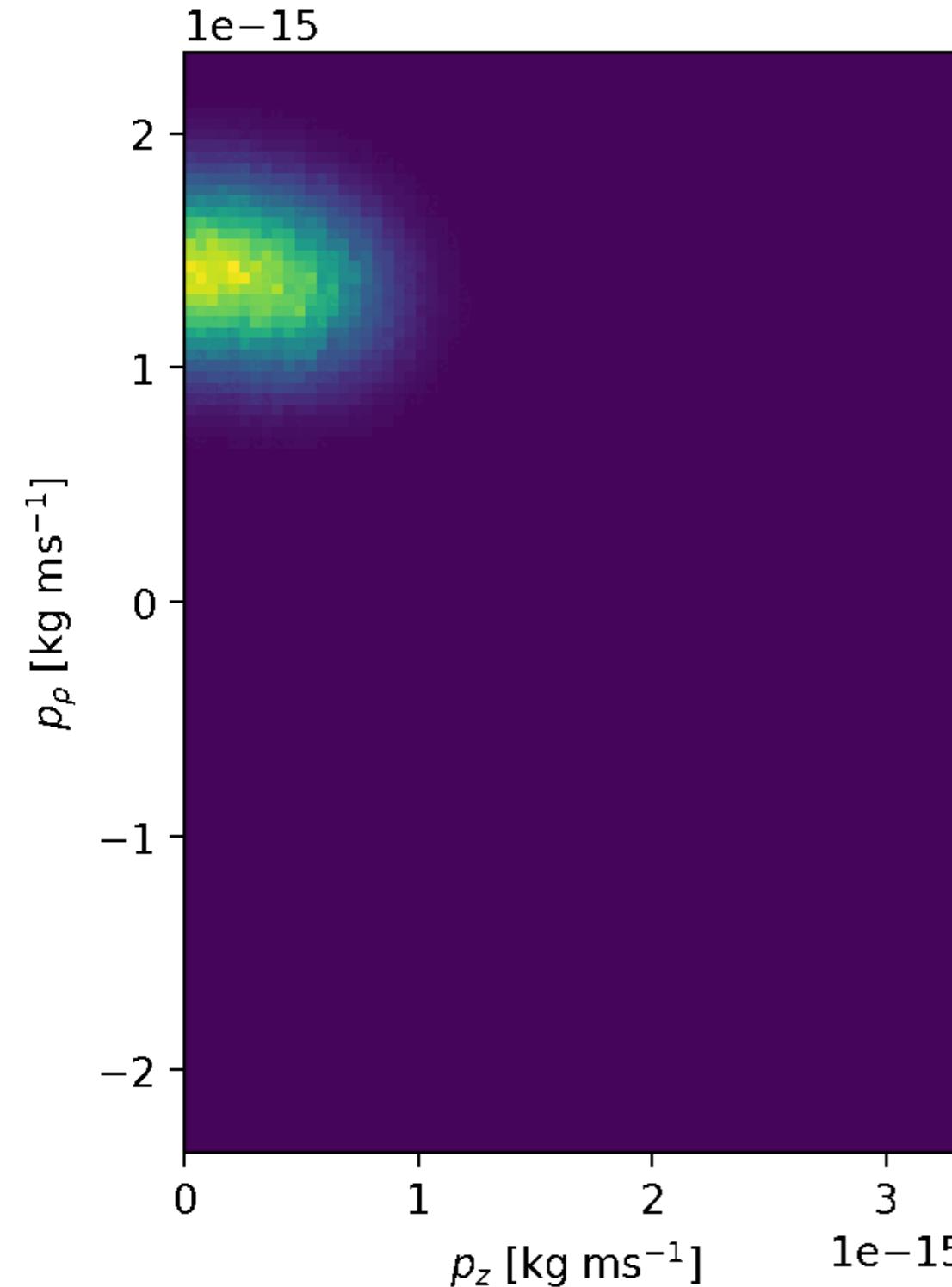
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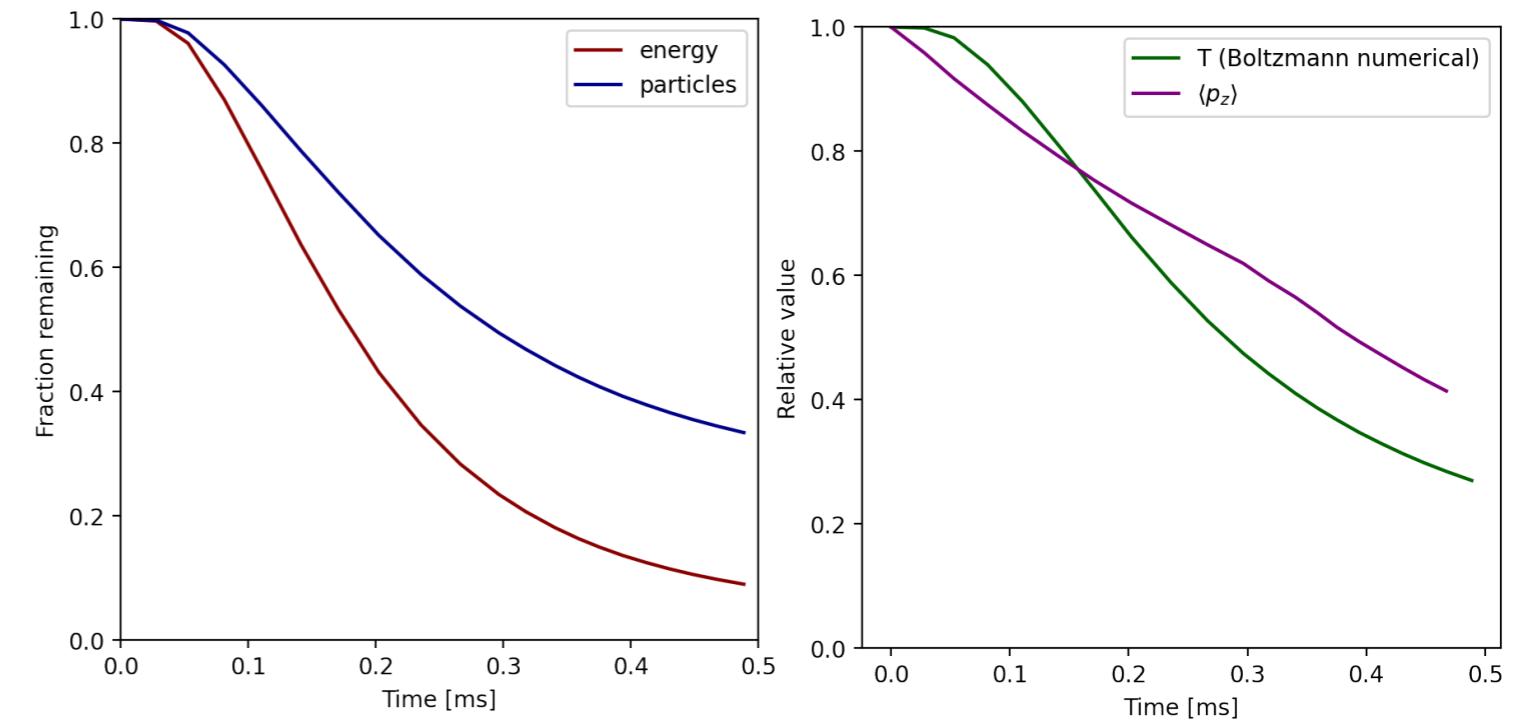


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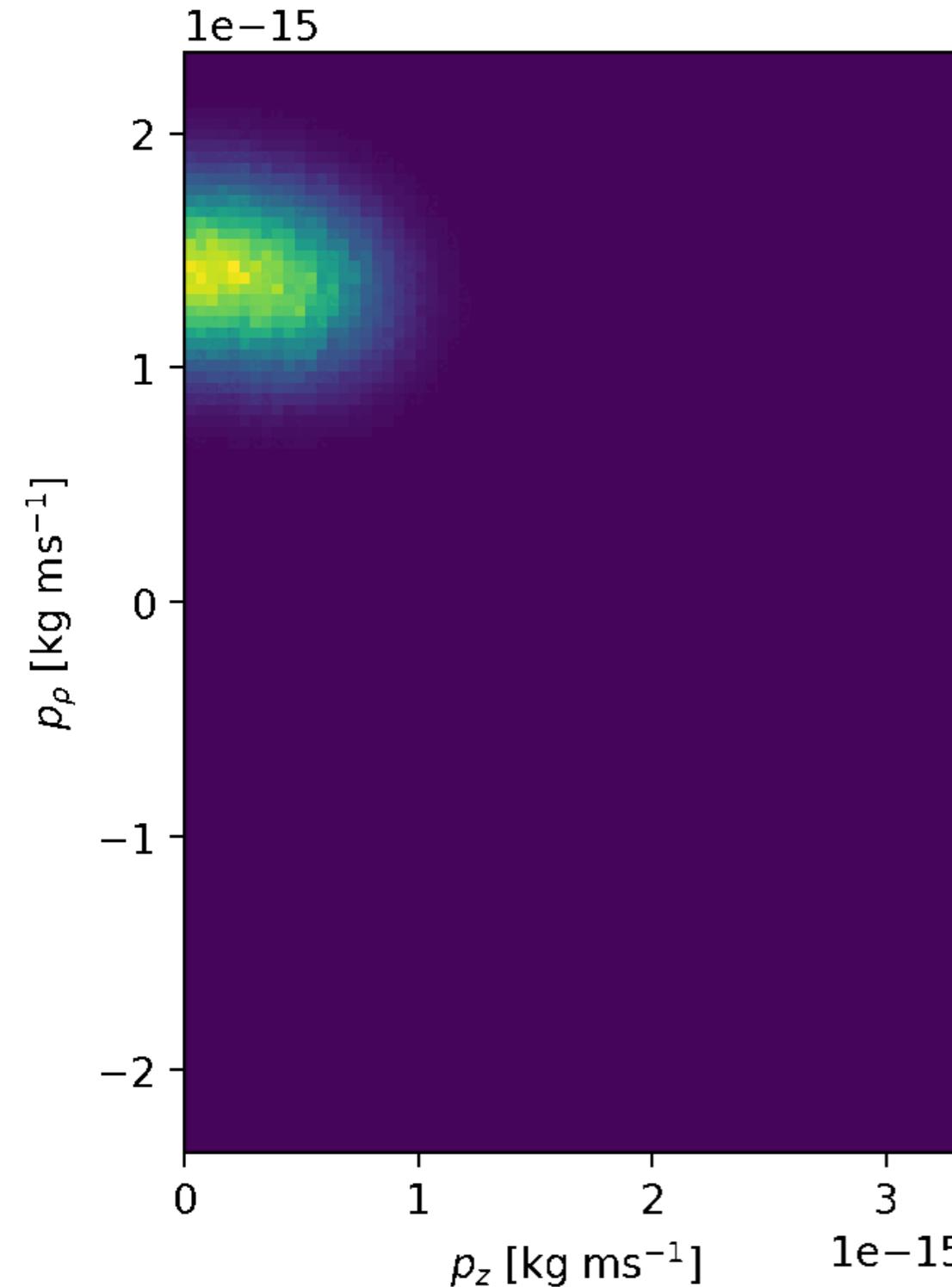


Simultaneous

- evaporative cooling
- wiggeling
- re-thermalization
- ▶ distribution gets **colder** and **slower**

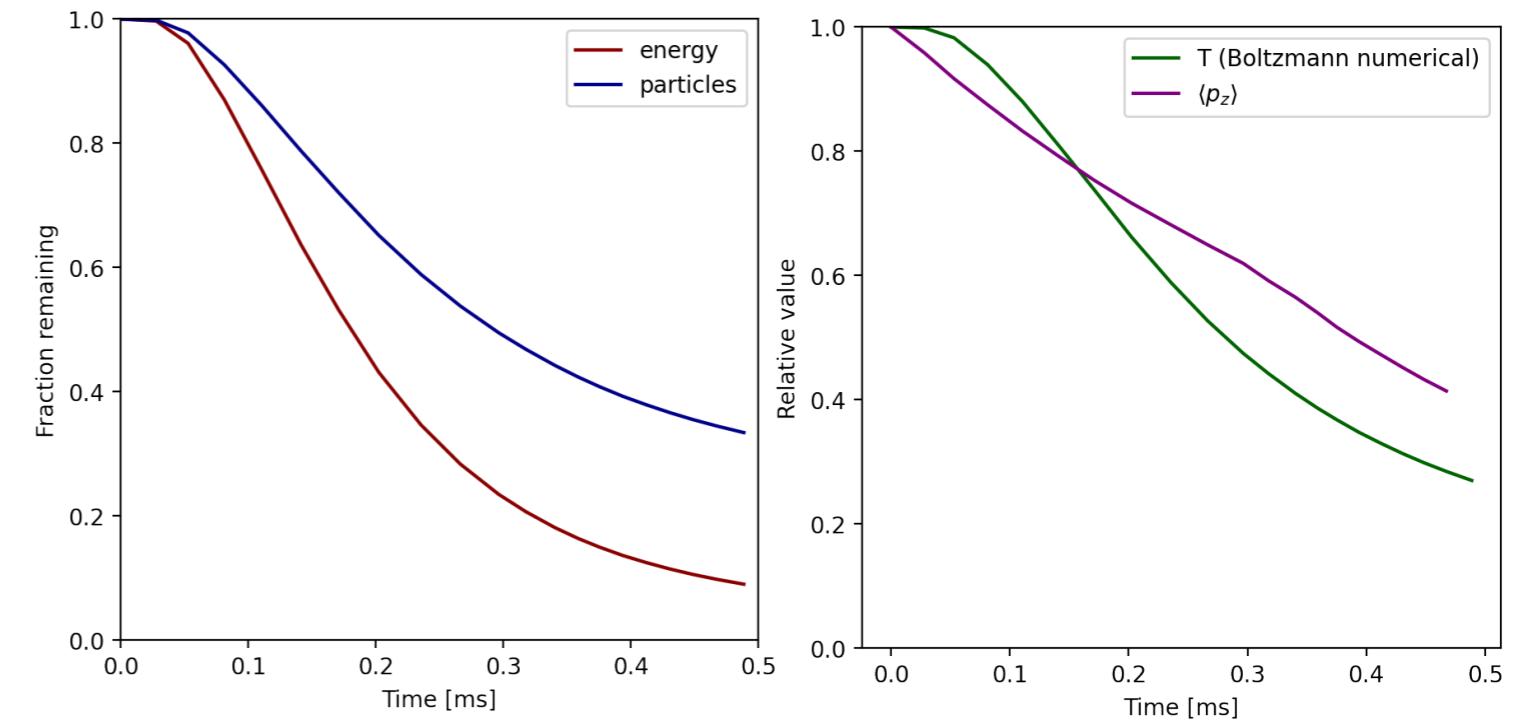


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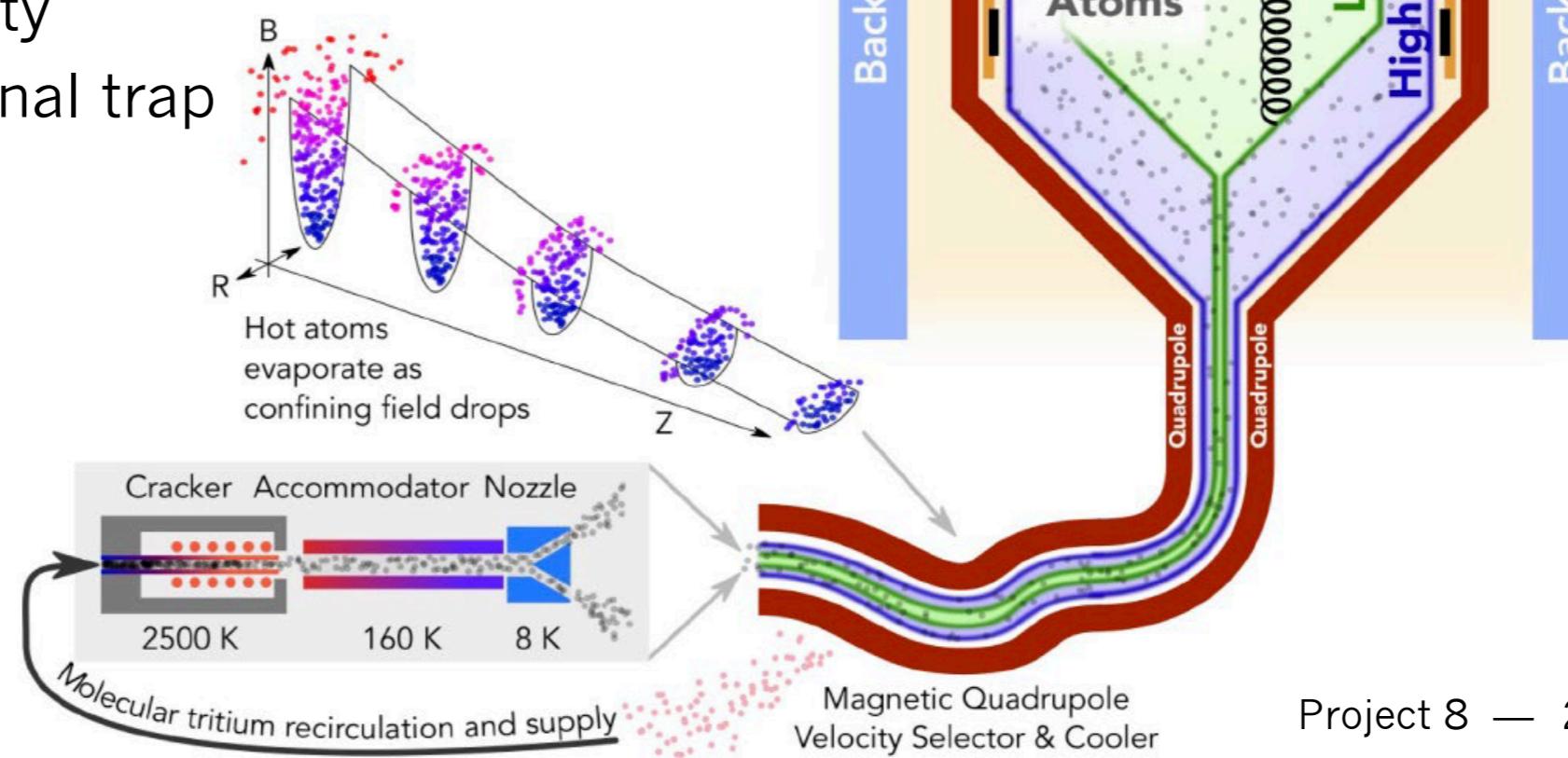
# Atomic tritium experiment

PROJECT 8

## Conceptual design

- thermal dissociation
  - ▶  $T_2 \rightarrow T$
- accomodation
  - ▶  $\phi(K)$  with acceptable recombination
- evaporative wiggle cooling
  - ▶  $\phi(mK)$  and slowing down
  - ▶ high atomic purity
- Magneto-gravitational trap
  - ▶ Halbach array

Atomic tritium experiment with anticipated sensitivity to  $m_\beta$  of 400 meV



# Atomic beam demonstration: next steps

Dissociation and accommodation

- surface physics critical
  - ▶ establish experimentally

Evaporative wiggle cooling

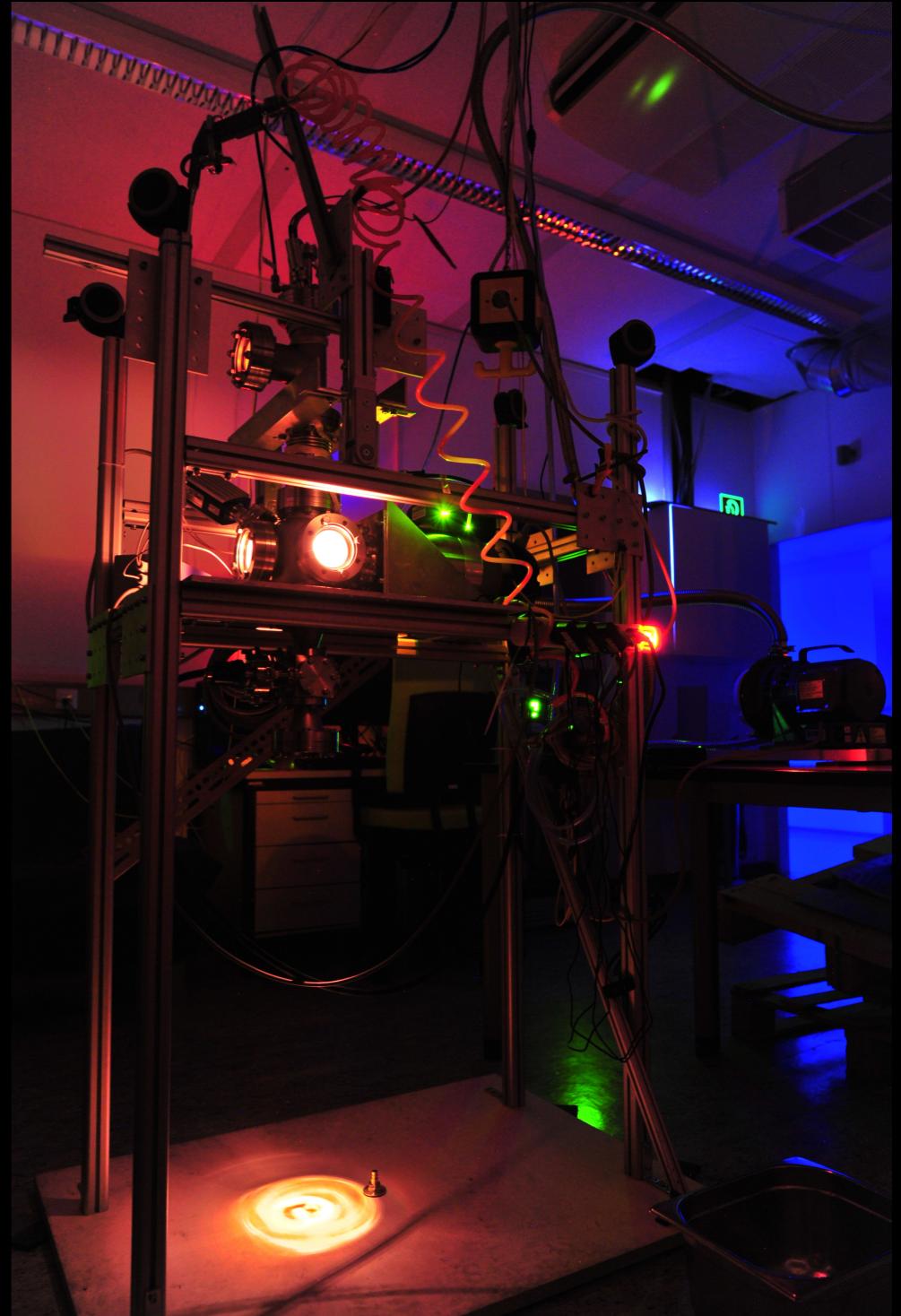
- magneto-thermodynamics
  - ▶ enter design phase

Trapping

- fix temperature and density
  - ▶ enter design phase

Overall approach

- start with H<sub>2</sub> and D<sub>2</sub>
  - ▶ see talk by A. Lindman
- vet with T<sub>2</sub>
  - ▶ see the future

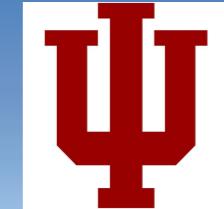


# Thank you!





UNIVERSITÄT  
HEIDELBERG  
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# Project 8 collaboration