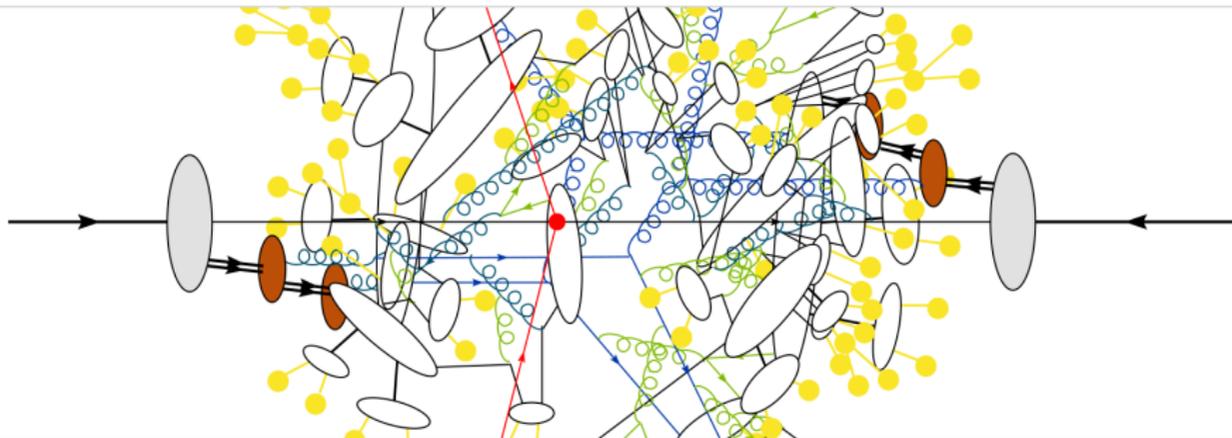


# Triple-Differential Z+Jet Production at 13 TeV

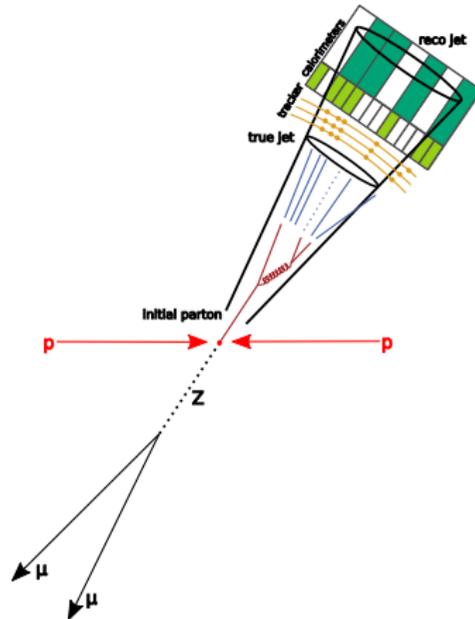
10th KSETA Plenary Workshop 2023

Robin Hofsaess, Maximilian Horzela, Günter Quast, Klaus Rabbertz, Cedric Verstege | 29. March 2023



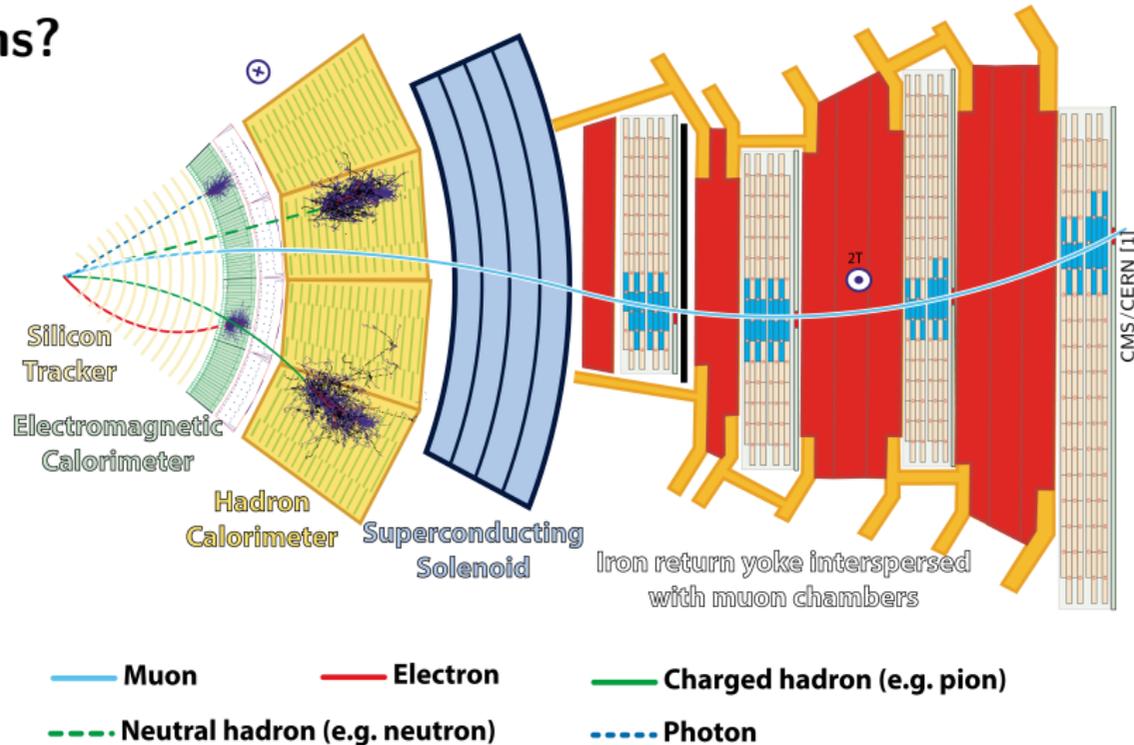
S. Gieseke

# Why Z+Jets?



- Goal
  - Constraints on gluon (and other) parton distribution functions (PDFs)
  - Input for  $\alpha_s$  fits
- $Z \rightarrow \mu^+ \mu^-$ 
  - Good number of signal events
  - Low number of background events
  - Precise muon reconstruction and identification with CMS

# Why Muons?



Analysis Strategy  
 ●●○○○

Selections  
 ○○○

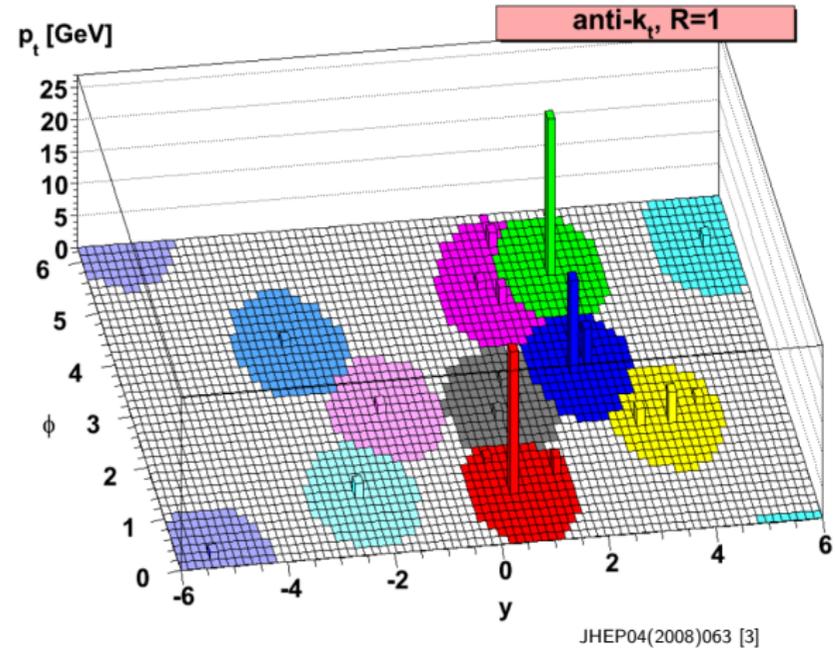
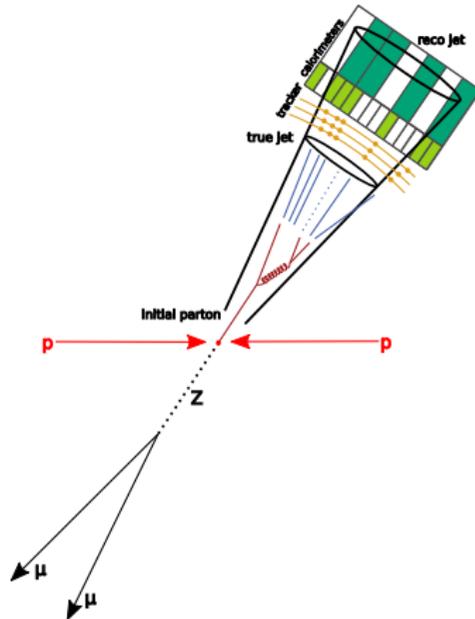
Unfolding  
 ○○○○○○

Uncertainties  
 ○

Results  
 ○○○

Conclusions  
 ○

# What is a Jet?



Analysis Strategy  
 ○●○○

Selections  
 ○○○

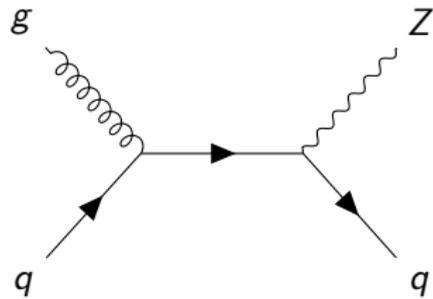
Unfolding  
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Uncertainties  
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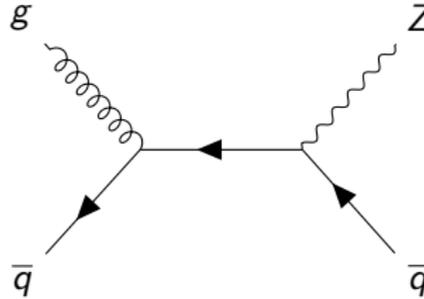
Results  
 ○○○

Conclusions  
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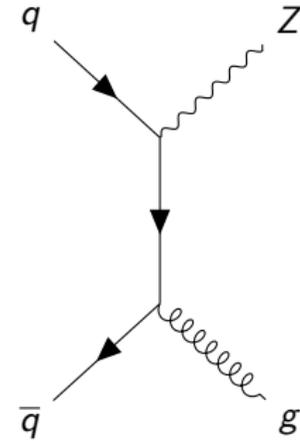
# Why plus Jet?



(a) quark-gluon

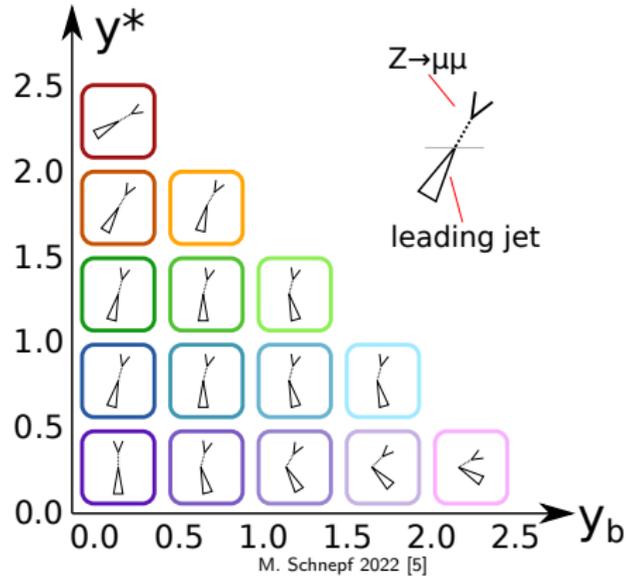


(b) antiquark-gluon



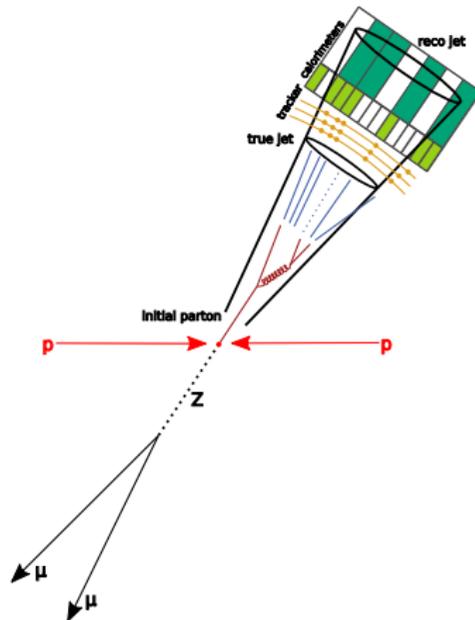
(c) quark-antiquark

# Why Triple-Differential?



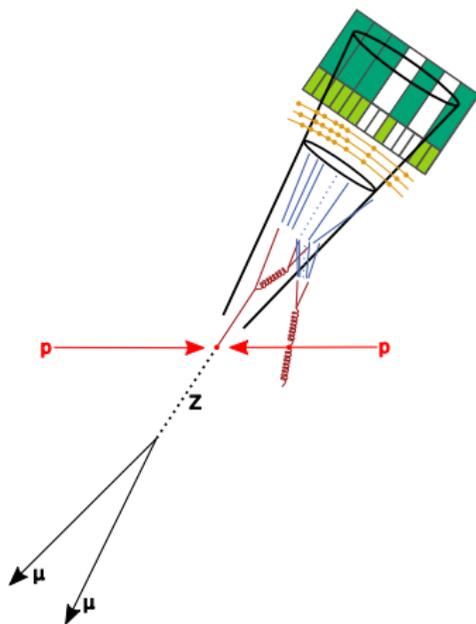
- Transverse momentum of di-muon system
  - $p_T^Z$
  - Scale of the hard interaction
- Boost of center-of-mass system
  - $y_b = \frac{1}{2}|y^Z + y^{\text{Jet}1}|$
  - Parton momentum fractions of the protons
- Rapidity separation
  - $y^* = \frac{1}{2}|y^Z - y^{\text{Jet}1}|$
  - Scattering angle in center-of-mass system

# Event Selections and Corrections (Muons)



- Events passing single muon trigger
  - $p_T^\mu$  above trigger threshold
  - Corrected for trigger efficiency
- Muon selection
  - Within muon system coverage  $|\eta| < 2.4$
  - Tight identification and isolation criteria
  - Cluster final state radiation (dressed muons)
- Z-boson reconstruction
  - $\mu^+\mu^-$  pair compatible with Z-boson mass

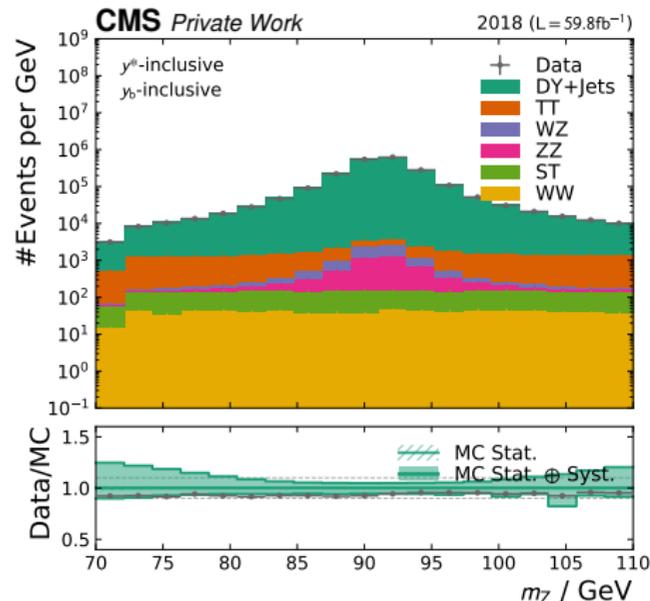
# Event Selections and Corrections (Jets)



- Jet selection
  - Within similar detector coverage  $|y| < 2.4$
  - Tight identification incl. lepton veto
  - Muon-jet overlap removal
  - Tight pile-up jet identification
  - $p_T$  cut to reduce pile-up contributions

# Datasets and MC

- Proton-proton collisions at  $\sqrt{s} = 13$  TeV recorded from 2016 to 2018
- Total integrated luminosity  $138 \text{ fb}^{-1}$
- Signal MC:
  - $Z(\rightarrow \ell^+ \ell^-) + 0, 1, 2 \text{ jets}$  MadGraph+Pythia8 aMC@NLO FFXF
- Background MC:
  - $t\bar{t} \rightarrow 2b2\ell2\nu$  Powheg+Pythia8 NLO
  - Single top quark t-channel and  $tW$   
Powheg+MadSpin+Pythia8 NLO
  - Di-Boson  $WW, WZ, ZZ$  Pythia8 LO



# Unfolding Basics

- Unfolding for detector effects of observation  $s$  to true spectrum  $t$ 
  - Detector Resolution → Migration between generator and reconstruction bins
  - Detector Efficiency → Less events on reconstruction level than generator level

We have:  $s(\vec{y}) = \int_X D(\vec{y}, \vec{x}) t(\vec{x}) d\vec{x}$

We want:  $t(\vec{x}) = \int_Y D'^{-1}(\vec{x}, \vec{y}) s(\vec{y}) d\vec{y}$

# Unfolding Basics

- Unfolding for detector effects of observation  $s$  to true spectrum  $t$ 
  - Detector Resolution → Migration between generator and reconstruction bins
  - Detector Efficiency → Less events on reconstruction level than generator level
- Variations below finite resolution ↔ Ill-posed problem
- Usually  $s$  and  $t$  discretized in histograms
  - “invert” Response Matrix  $\mathbf{R}$  (i.e. TUnfold [4])
    - Estimate Response Matrix from MC → Systematic and statistical uncertainties
    - If matrix ill-conditioned → Regularize “unphysical” oscillations

$$\text{We have: } s(\vec{y}) = \int_{\mathcal{X}} D(\vec{y}, \vec{x}) t(\vec{x}) d\vec{x}$$

$$\text{We want: } t(\vec{x}) = \int_{\mathcal{Y}} D'^{-1}(\vec{x}, \vec{y}) s(\vec{y}) d\vec{y}$$

$$s^j = \mathbf{R}_j^i t_j \rightarrow t_j = \mathbf{R}^{-1}{}^i_j s^i$$

$$\text{with } \mathbf{R}_j^i = \frac{\int_{\mathcal{Y}_i} \int_{\mathcal{X}_j} D(\vec{y}, \vec{x}) t(\vec{x}) d\vec{x} d\vec{y}}{\int_{\mathcal{X}_j} t(\vec{x}) d\vec{x}}$$

# TUnfold

- Algorithm for estimating truth  $\mathbf{t}$  from measured observables  $\mathbf{s}$
- Assumes Gaussian distribution of  $\mathbf{s}$  with average  $\tilde{\mathbf{s}} = \mathbf{R}\tilde{\mathbf{t}} \rightarrow$  least-square method
- Maximize likelihood

$$\mathcal{L} = (\mathbf{s} - \mathbf{R}\mathbf{t})^T \mathbf{V}_{ss} (\mathbf{s} - \mathbf{R}\mathbf{t}) + \mathcal{L}_{\text{reg}} + \mathcal{L}_{\text{norm}}$$

with covariance matrix  $\mathbf{V}_{ss}$

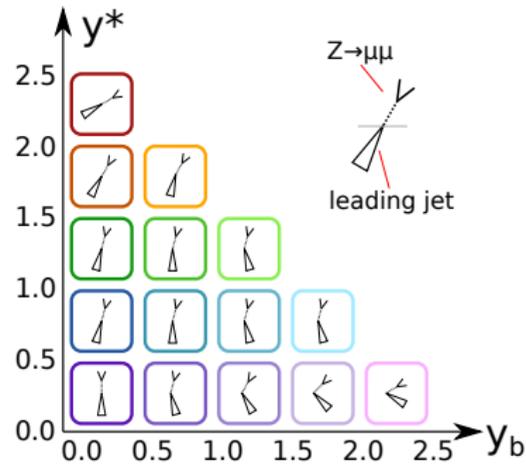
- General analytical solution  $\mathbf{t}_0(\mathbf{s}, \mathbf{R}, \mathbf{V}_{ss})$  and covariance  $\mathbf{V}_{tt}(\frac{\partial \mathbf{t}_0}{\partial \mathbf{s}}, \mathbf{R}, \mathbf{V}_{ss}) \rightarrow$  plug in and do the linear algebra
- Similar for contributions to  $\mathbf{V}_{tt}$  due to statistical uncertainties on  $\mathbf{R}$ 
  - Avoid regularization  $\mathcal{L}_{\text{reg}}$ , when  $\mathbf{R}$  well-conditioned ( $\delta\mathbf{s} \approx$  resolution)
  - Avoid normalization  $\mathcal{L}_{\text{norm}}$ , when Gaussian approximation holds  $\rightarrow$  true in this analysis

# Bin Unraveling

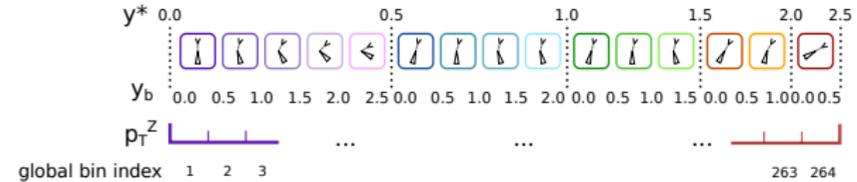
3D phase-space

→

1D visualization



→



M. Schnepf 2022 [5]

Analysis Strategy  
○○○○○

Selections  
○○○

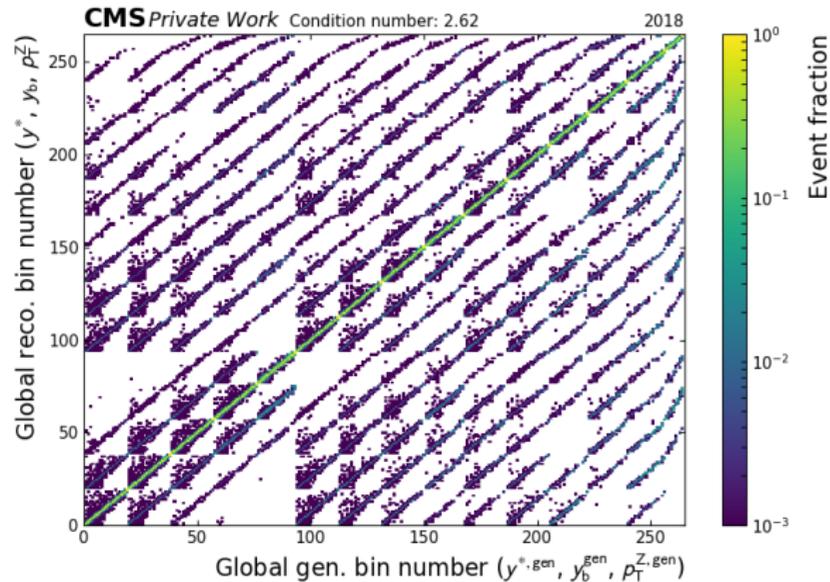
Unfolding  
○○●○○○

Uncertainties  
○

Results  
○○○

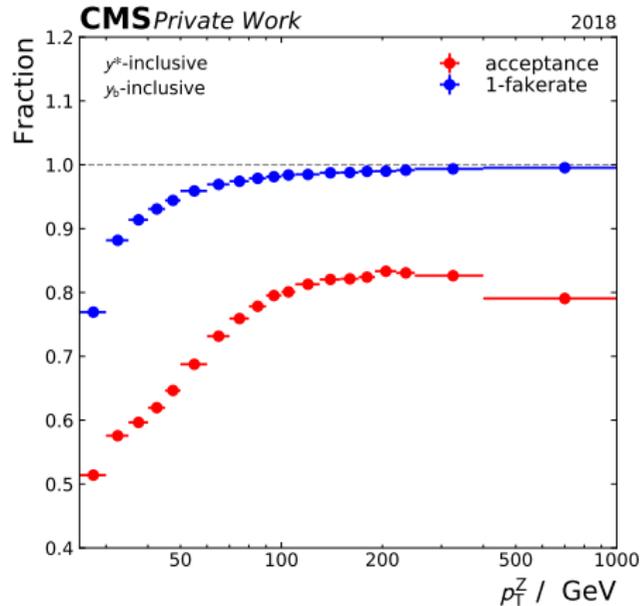
Conclusions  
○

# Response Matrix



- Migrations from truth level to observation level due to detector effects
  - $\mathcal{P}(\text{event in reco bin } i | \text{event in gen bin } j)$
- Fill MC events passing selections on reco- and gen-level for each analysis bin and normalize
- Small condition number, well-conditioned → Regularization not necessary
- Found to be similar for all data taking years

# Acceptance & Fake rate



- Some events reconstructed in underflow or overflow of Response Matrix
- Acceptance
  - Events passing cuts on generator level but not on reconstruction level
  - Including detector & reconstruction inefficiencies
  - Treat as inefficiencies
- Fake rate
  - Events passing cuts on reconstruction level but not on generator level
  - Subtract as background
- Accounted for during unfolding

Analysis Strategy  
○○○○○

Selections  
○○○

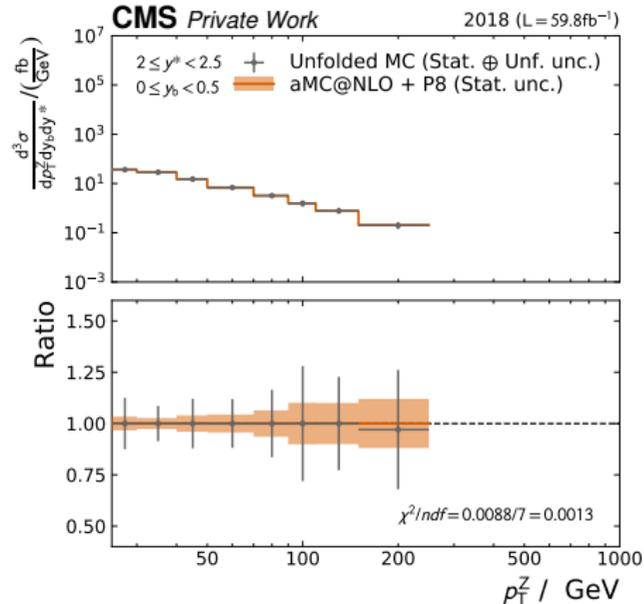
Unfolding  
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Uncertainties  
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Results  
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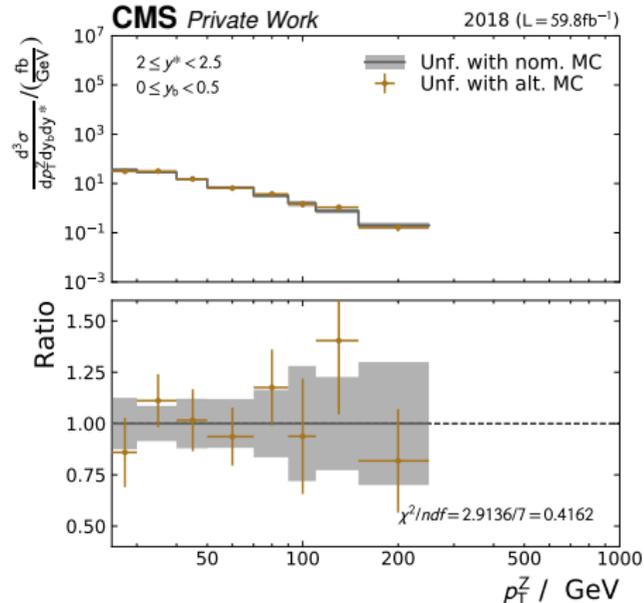
Conclusions  
○

# Unfolding Closure



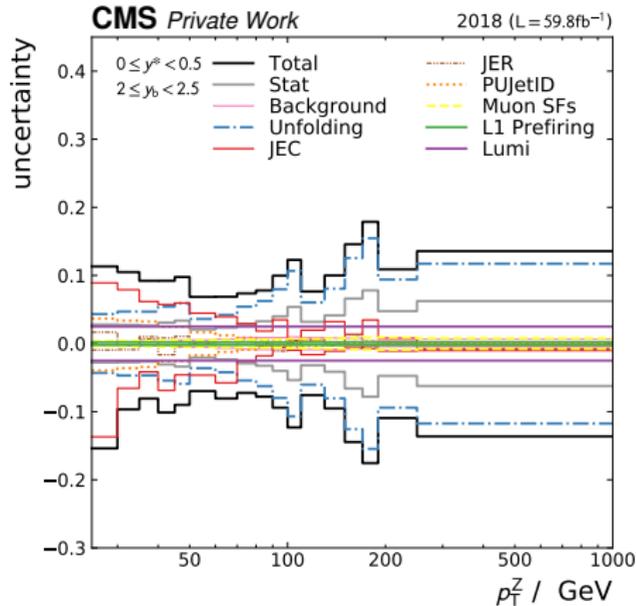
- Consistency check
  - Unfold simulated distribution with response using the same MC events
  - Perfect agreement between unfolded MC and generator level
- Unfolding works as expected

# Model Dependence of Unfolding



- Choice of MC to fill Response Matrix might bias the results
  - Estimate effect of alternative MC simulation
  - Compare unfolded distribution using nominal & alternative response matrices
  - Agreement within statistical uncertainties
- No significant model dependence

# Systematic Uncertainties



- Various systematic effects impacting unfolded event yields, e.g.
  - Jet energy calibration (**JEC**) and resolution correction on MC (**JER**)
  - Measured **Luminosity**
  - Limited number of events for creation of Response Matrix for **Unfolding**
  - Estimated **Background** contributions
  - ...
- Subject to systematical uncertainties
- Adapt response matrix, acceptance, and fake rate for each systematical variation
- New unfolding for each uncertainty

Analysis Strategy  
○○○○○

Selections  
○○○

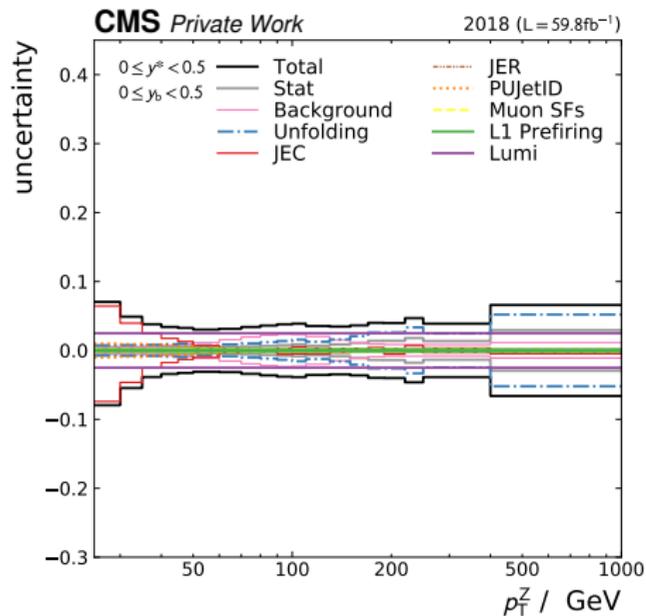
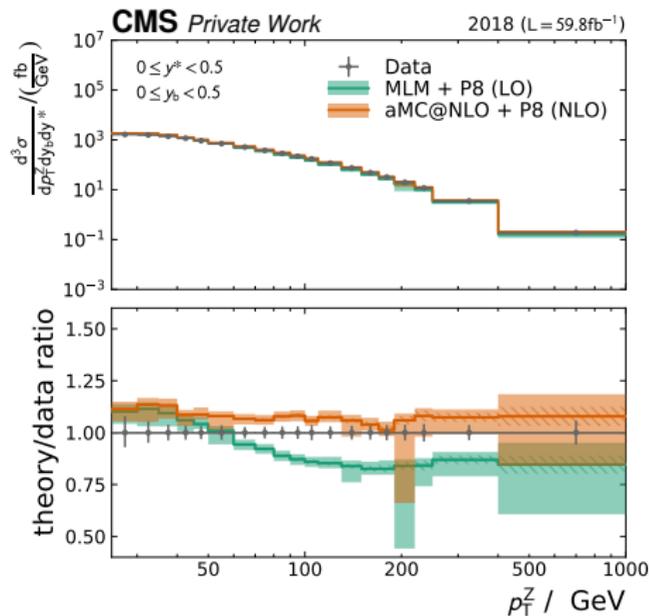
Unfolding  
○○○○○○○

Uncertainties  
●

Results  
○○○

Conclusions  
○

# Unfolded Cross-Sections 2018: Central Region



Analysis Strategy  
○○○○○

Selections  
○○○

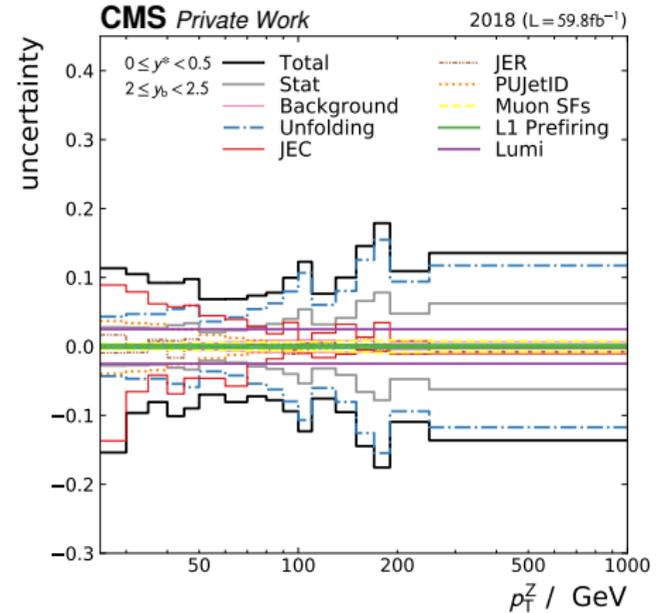
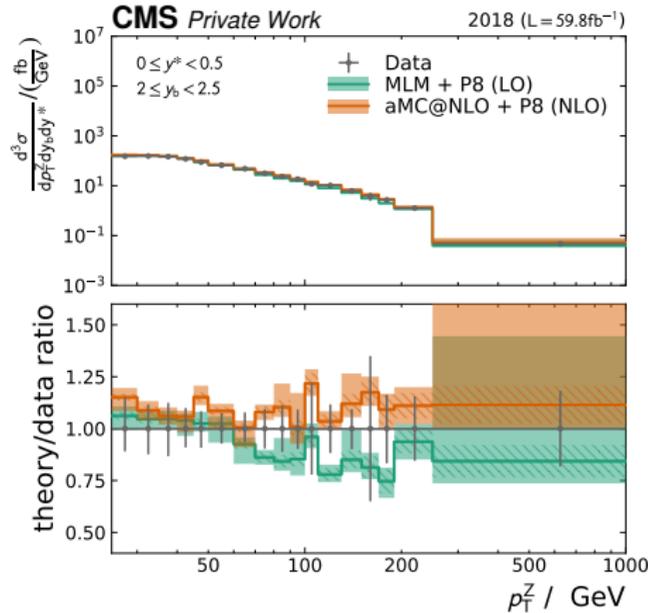
Unfolding  
○○○○○○○

Uncertainties  
○

Results  
●○○

Conclusions  
○

# Unfolded Cross-sections 2018: High Boost



Analysis Strategy  
○○○○○

Selections  
○○○

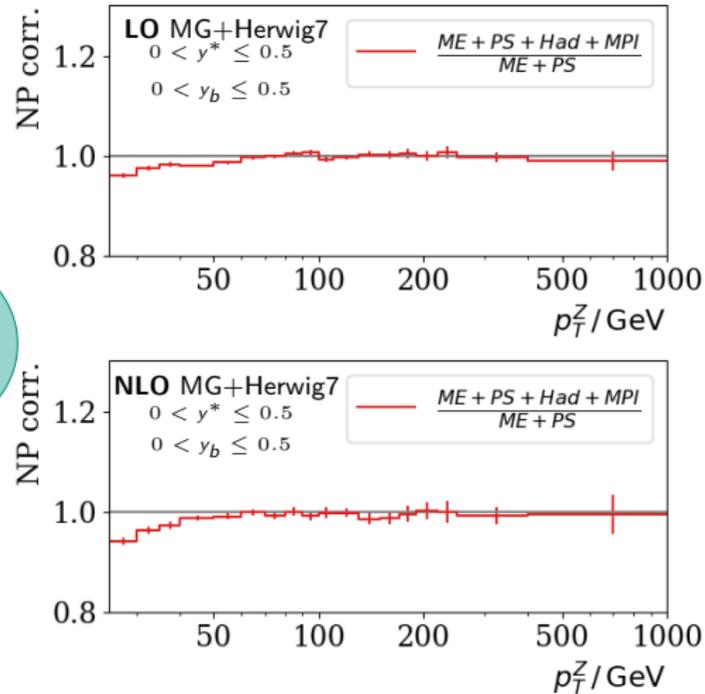
Unfolding  
○○○○○○○

Uncertainties  
○

Results  
●●○

Conclusions  
○

# Comparison to NNLO Predictions and QCD Analysis



anti- $k_T$ ,  
 $R = 0.4$

- TBD: Compare and fit measured cross-sections to state-of-the-art theory predictions for  $Z + \text{Jet} \rightarrow$  NNLO QCD  $\otimes$  NLO-EWK  $\otimes$  **non-perturbative (NP) corrections**
- NP corrections  $\frac{ME+PS+Had+MPI}{ME+PS}$ 
  - diminish towards higher  $p_T^Z$
  - change to slightly lower values from LO to NLO perturbative QCD

Analysis Strategy  
○○○○○

Selections  
○○○

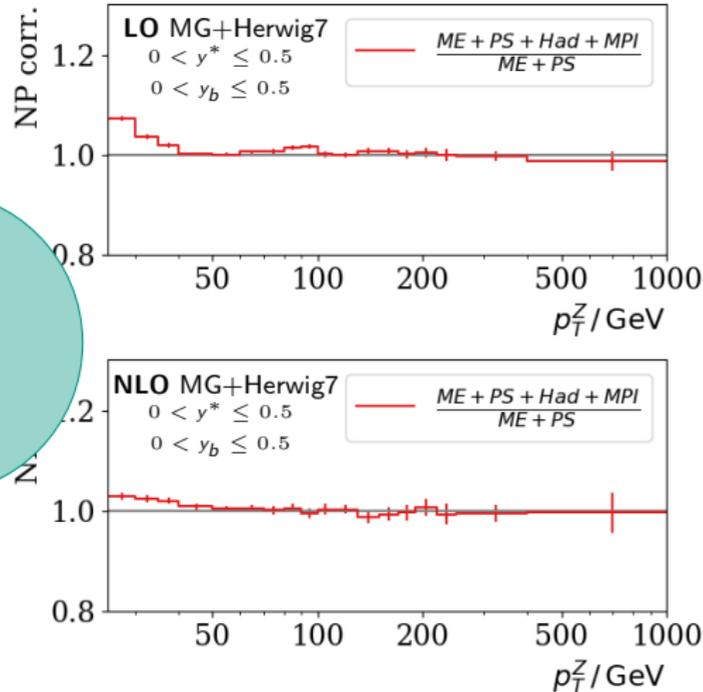
Unfolding  
○○○○○○○

Uncertainties  
○

Results  
○○●

Conclusions  
○

# Comparison to NNLO Predictions and QCD Analysis



anti- $k_T$ ,  
 $R = 0.8$

- TBD: Compare and fit measured cross-sections to state-of-the-art theory predictions for  $Z + \text{Jet} \rightarrow$  NNLO QCD  $\otimes$  NLO-EWK  $\otimes$  **non-perturbative (NP) corrections**
- NP corrections  $\frac{ME+PS+Had+MPI}{ME+PS}$ 
  - diminish towards higher  $p_T^Z$
  - change to slightly lower values from LO to NLO perturbative QCD
  - depend on the jet type

Analysis Strategy  
○○○○○

Selections  
○○○

Unfolding  
○○○○○○○

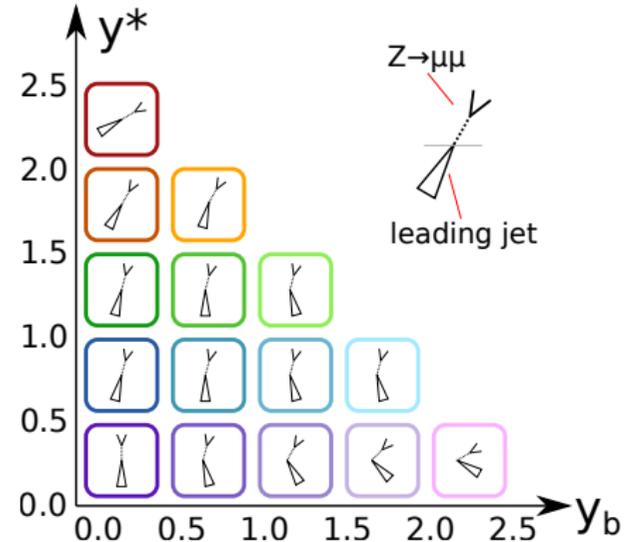
Uncertainties  
○

Results  
○○●

Conclusions  
○

# Outlook

- First Z+Jet triple-differential cross-section measurement at 13 TeV with full Run II CMS data in progress
    - Combination of all data-taking periods from 2016 to 2018 into single measurement
    - Comparison to NNLO fixed-order predictions including electroweak and non-perturbative corrections
    - PDF and  $\alpha_S$  fits
- Aiming for publication early 2024



# Backup

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●	Selections oo	IS-Partons o	Data/MC oooo	Response Matrices oooo	Closure oooo	Unfolding Model Dependence oooo	Results oooo	NP-Corrections o	References
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# Detailed Event Selection

One  $Z \rightarrow \mu\mu$  candidate with the following criteria

Selection	Value
Trigger	2016: HLT_IsoMu24 or HLT_TkMu24 2017: HLT_IsoMu27 2018: HLT_IsoMu24
Muon ID	Tight
Muon PF ISO	Tight
Muon $p_T$	$> 29 \text{ GeV}$
Muon $ \eta $	$< 2.4$
Z mass	$m_Z \pm 20 \text{ GeV}$
Z $p_T$	$> 25 \text{ GeV}$

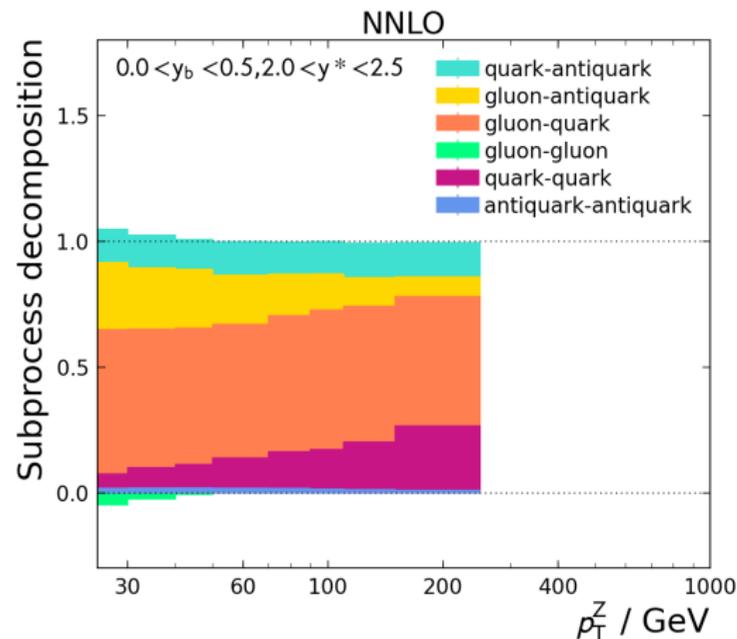
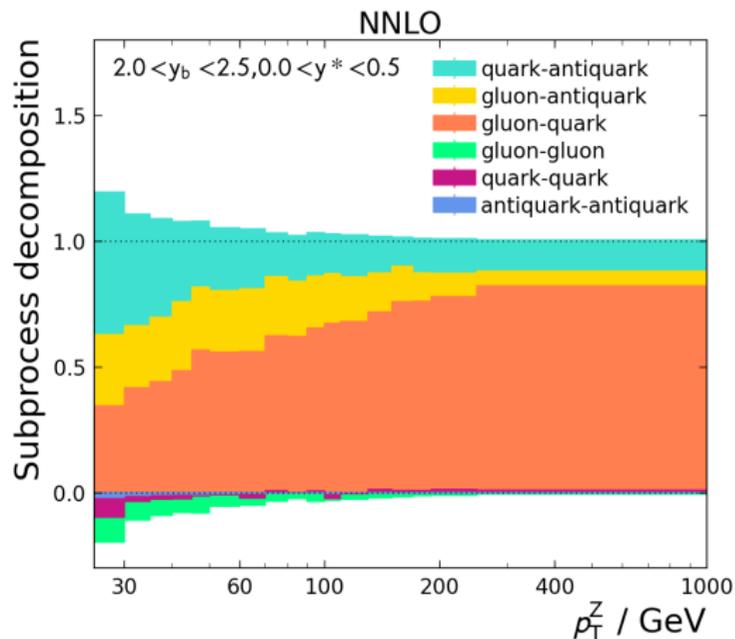
At least one Jet with the following criteria

Selection	Value
Jet ID	Tight + Lepveto
PUJetID	Tight
$\Delta R(\mu_Z, \text{Jet})$	$> 0.4$
Jet $p_T$	$> 20 \text{ GeV}$
Jet $ y $	$< 2.4$
Jet Veto Maps	✓

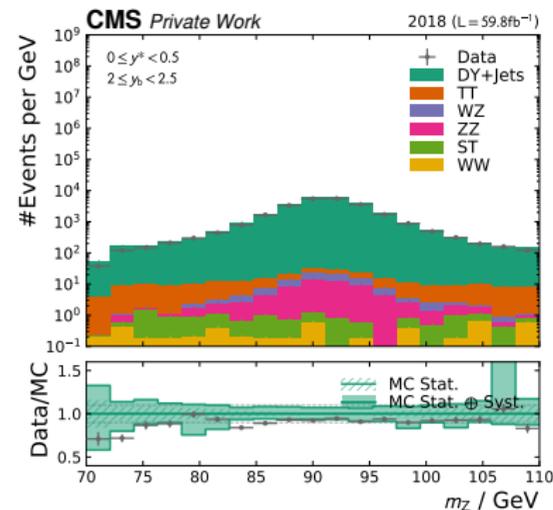
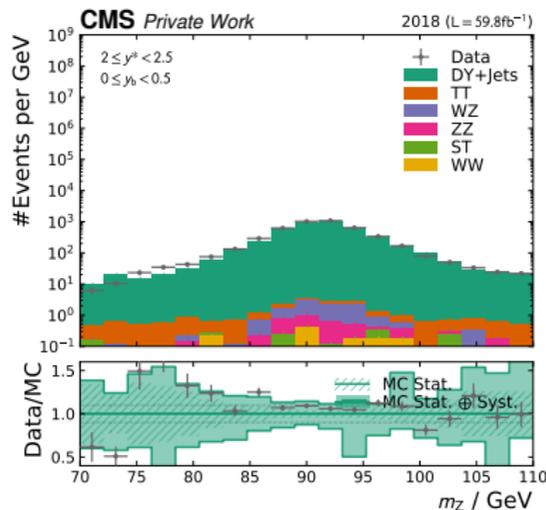
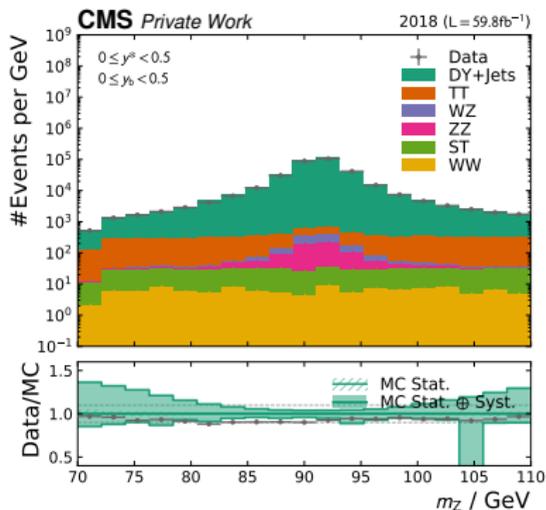
# Corrections

Correction/SF	2016preVFP	2016postVFP	2017	2018
Muon RECO SFs	✓	✓	✓	✓
Muon ISO SFs	✓	✓	✓	✓
Muon ID SFs	✓	✓	✓	✓
Muon Trigger SFs	✓	✓	✓	✓
Muon Rochester	Data (kScaleDT) + MC (kSpreadMC)			
Muon Dressing	Data + MC with $\Delta R(\mu, \gamma) < 0.1$			
Muon L1Prefiring	✓	✓	✓	✓
ECAL L1Prefiring	✓	✓	✓	not needed
METFilters	Data + MC (All recommended for each year)			
PuJetID SFs	✓	✓	✓	✓
JEC	V7	V7	V5	V5
JER (hybrid)	V3	V3	V2	V2

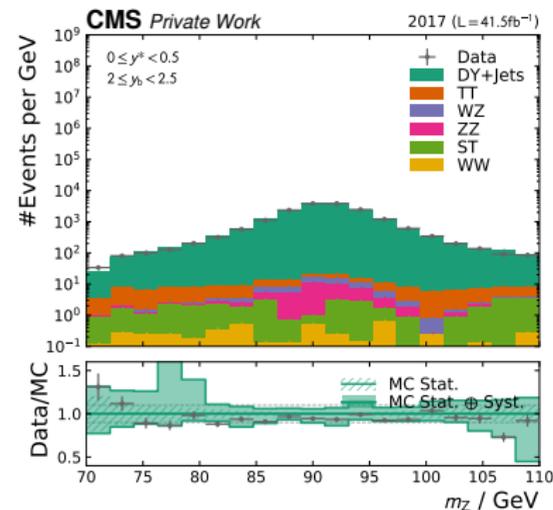
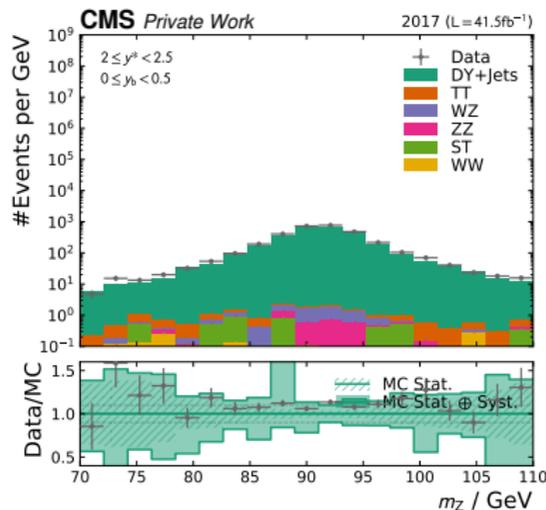
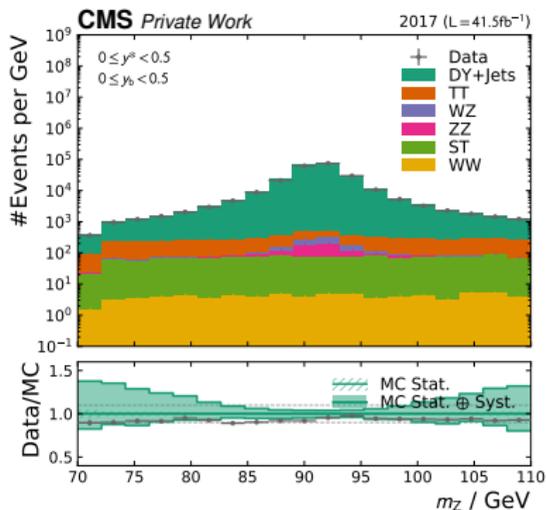
# Dependence of Parton Luminosities on Phase-Space



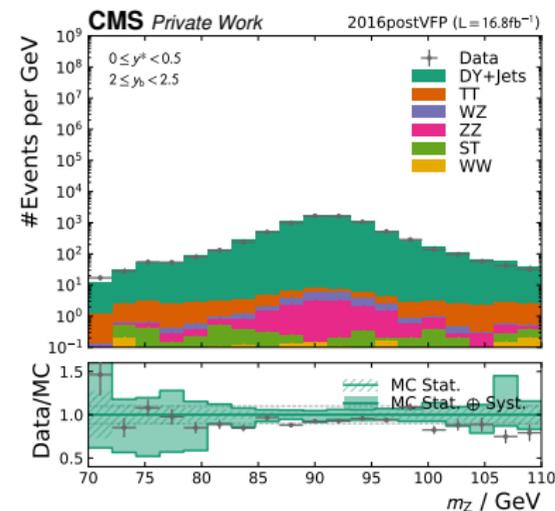
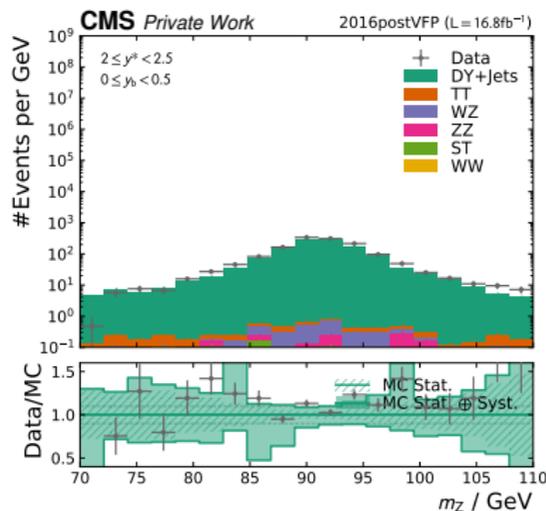
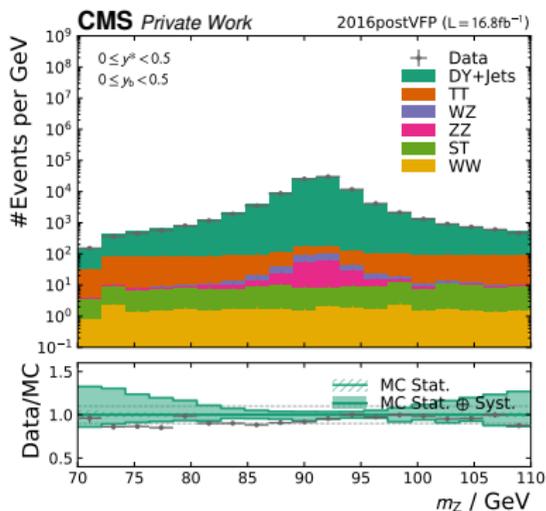
# Data/MC 2018



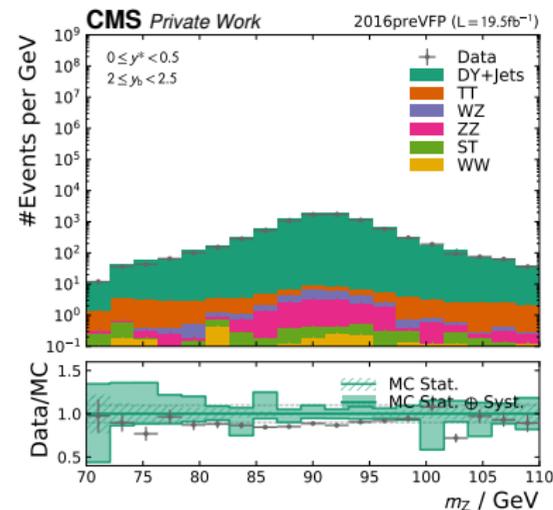
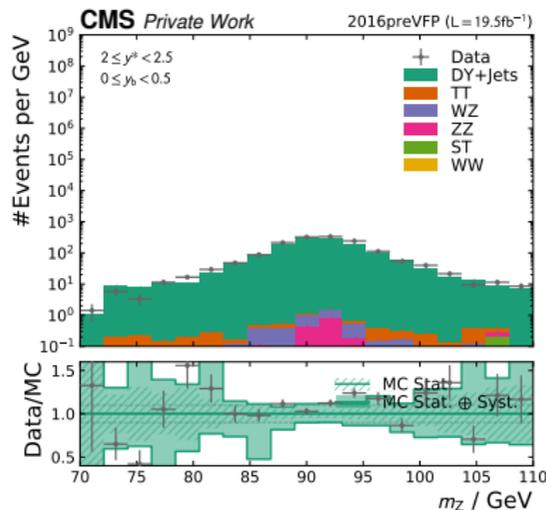
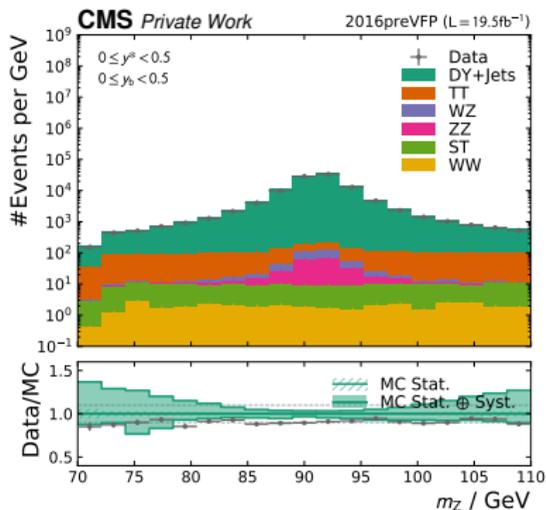
# Data/MC 2017



# Data/MC 2016postVFP

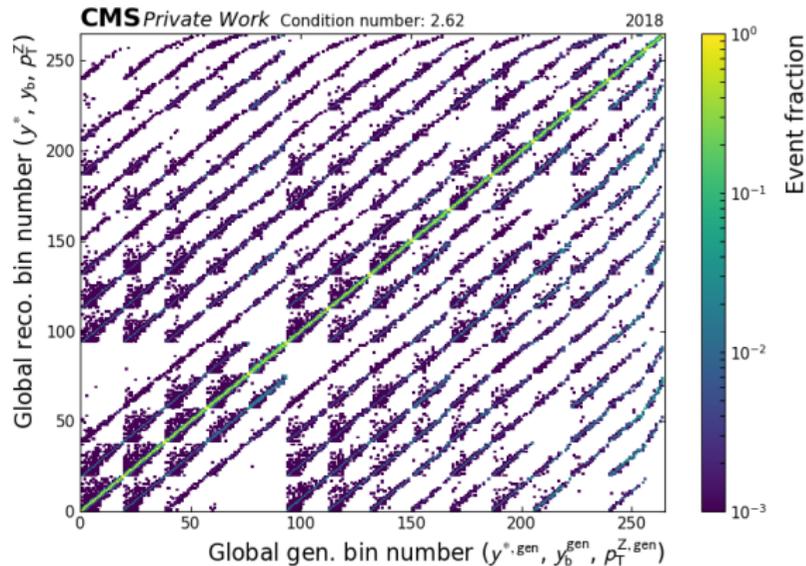


# Data/MC 2016preVFP

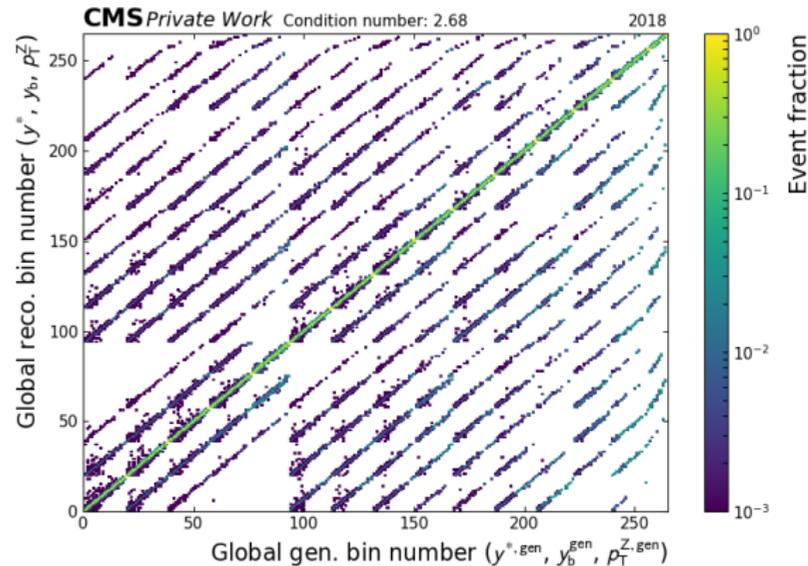


# Response Matrices 2018

## NLO

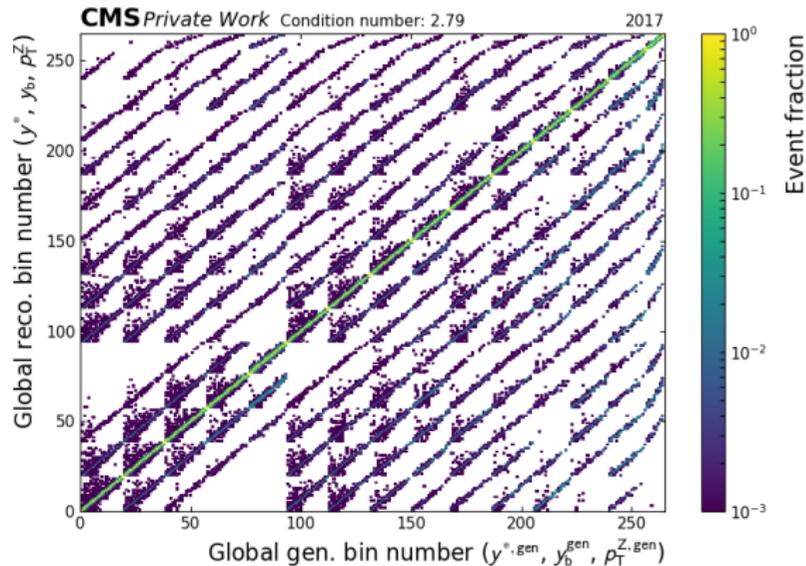


## LO

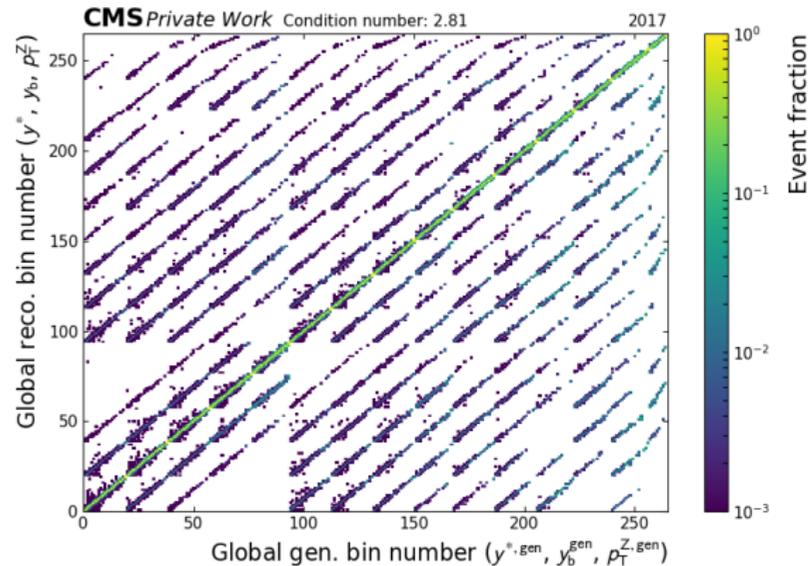


# Response Matrices 2017

## NLO

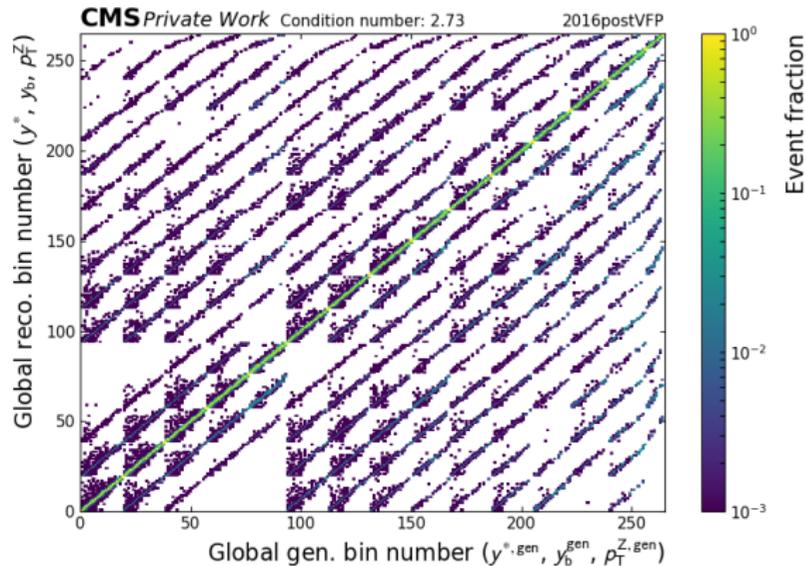


## LO

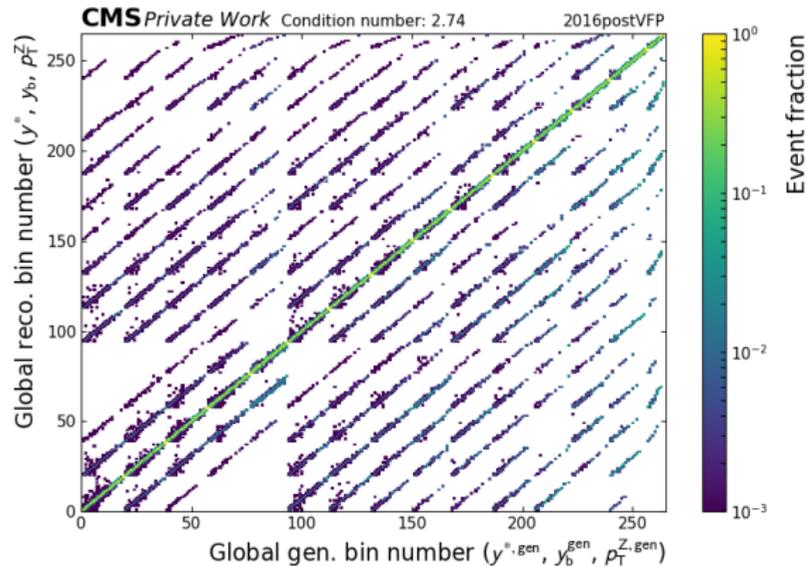


# Response Matrices 2016postVFP

## NLO

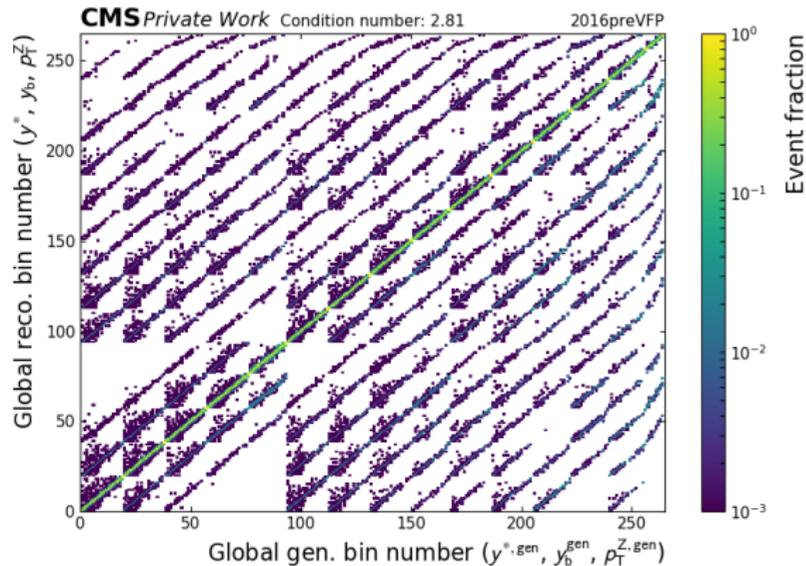


## LO

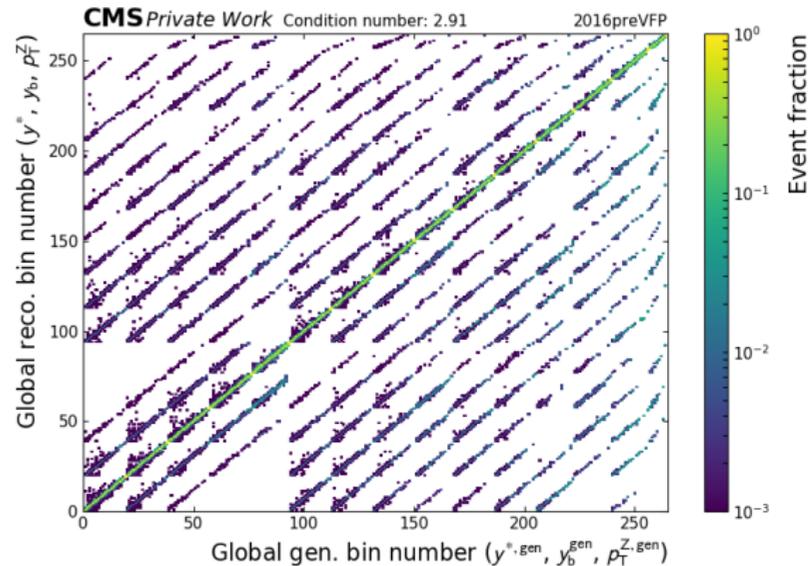


# Response Matrices 2016preVFP

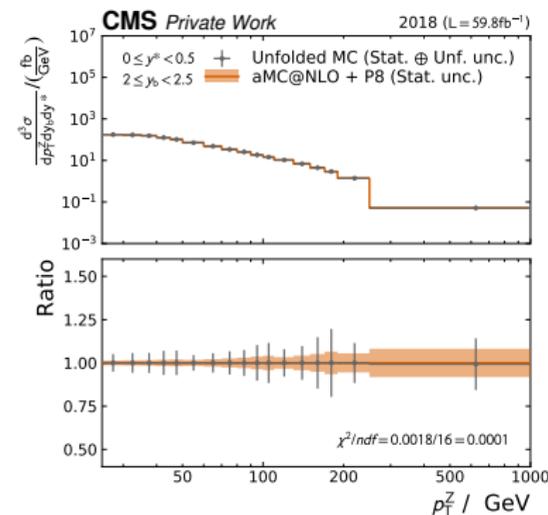
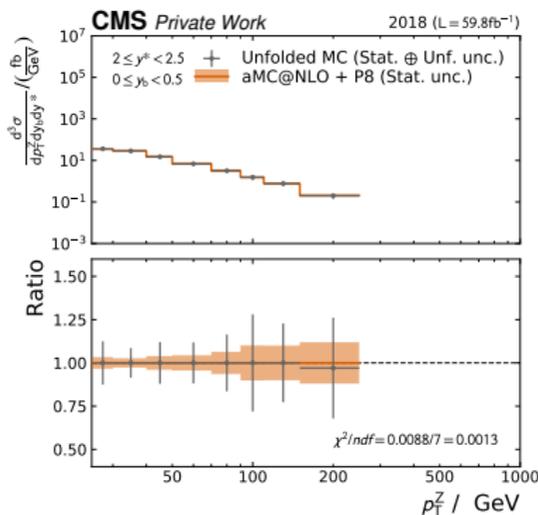
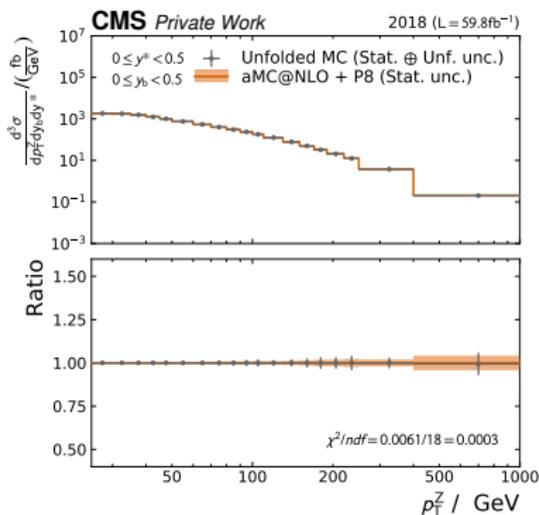
## NLO



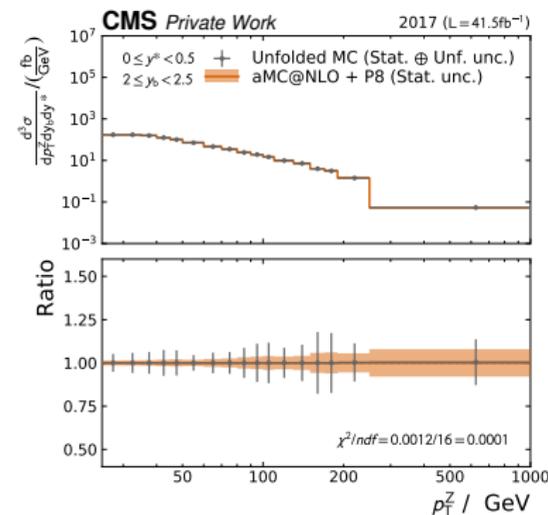
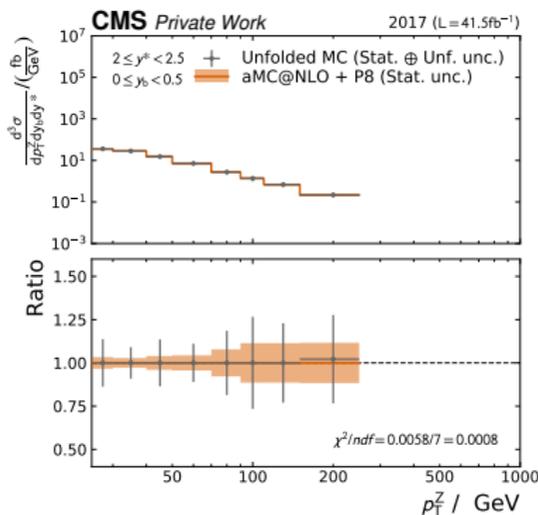
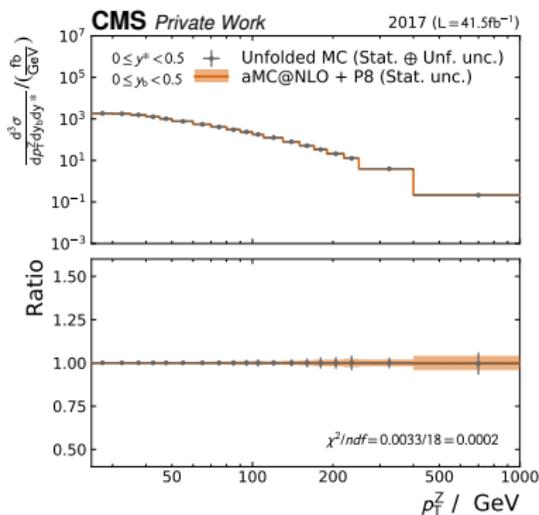
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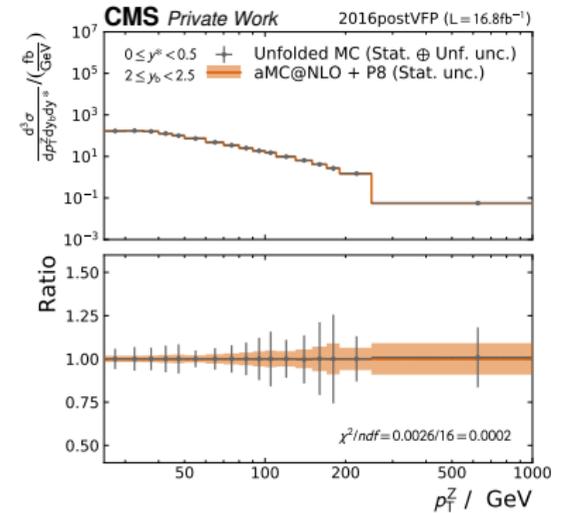
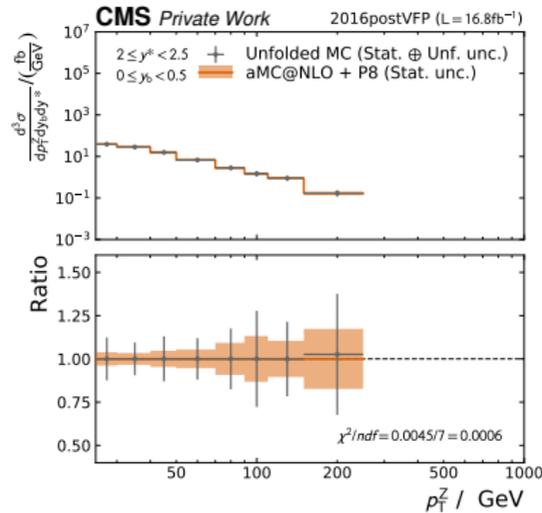
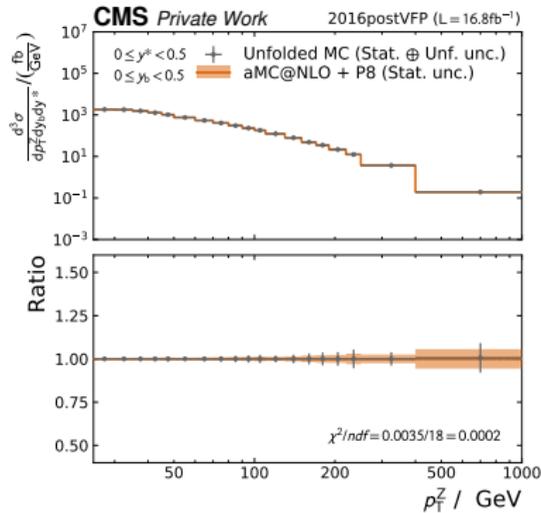
# Unfolding Closure 2018



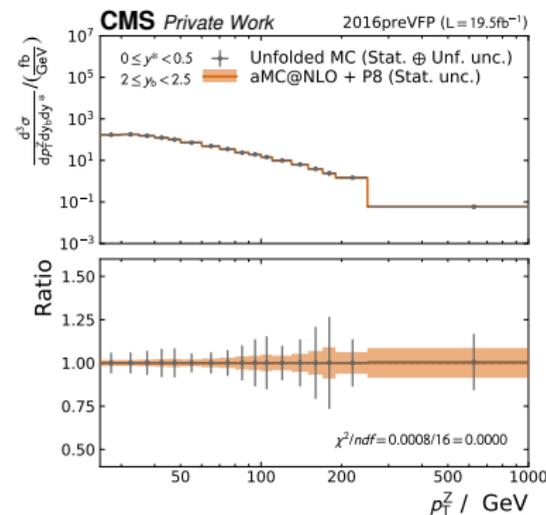
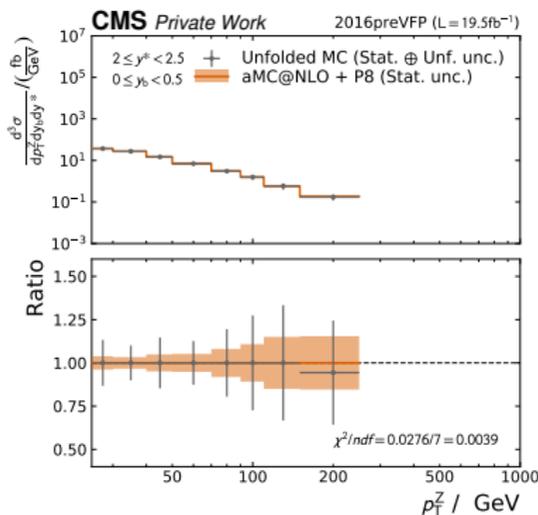
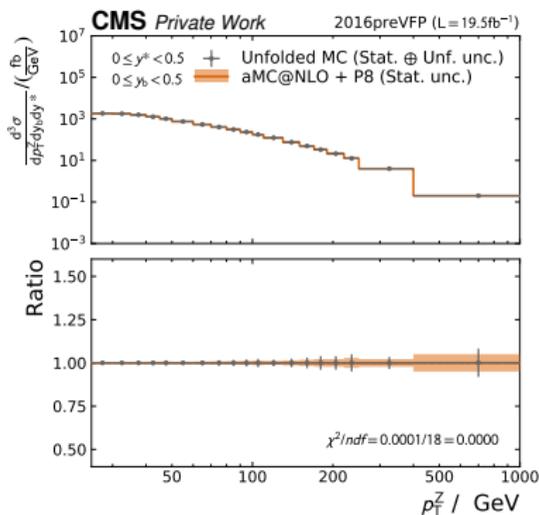
# Unfolding Closure 2017



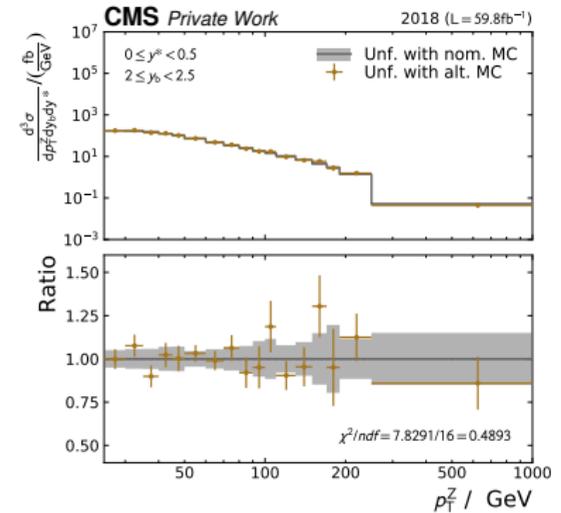
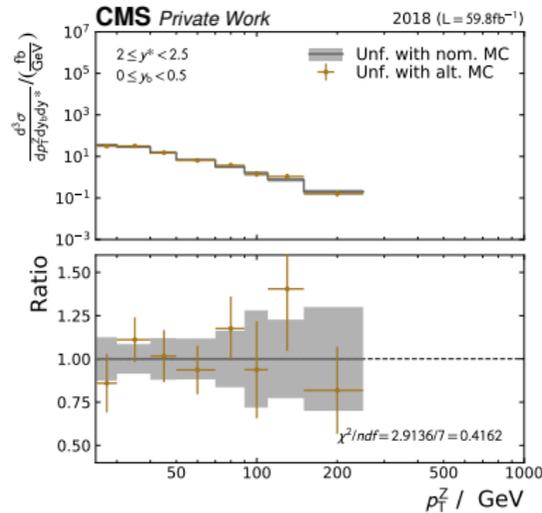
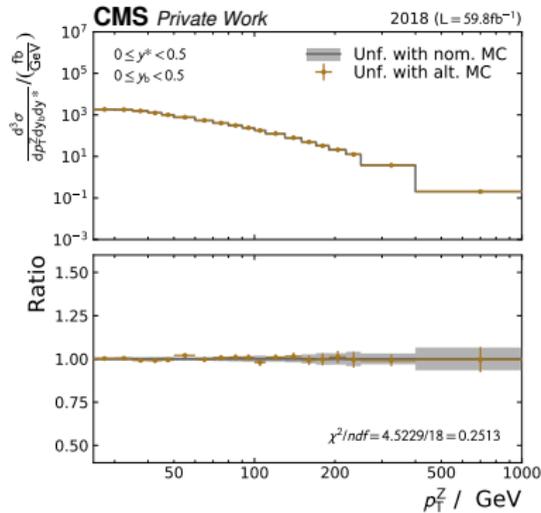
# Unfolding Closure 2016postVFP



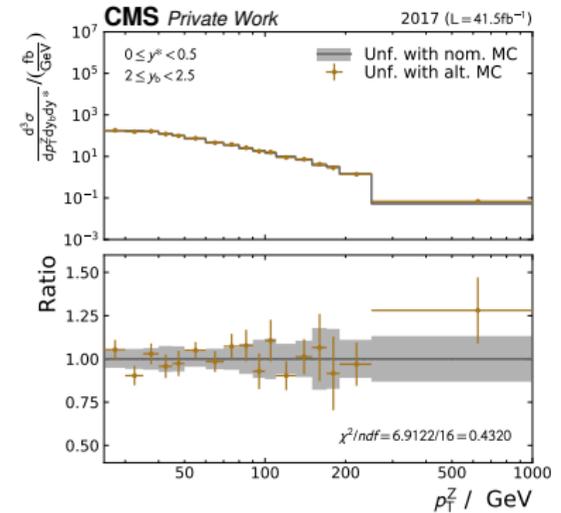
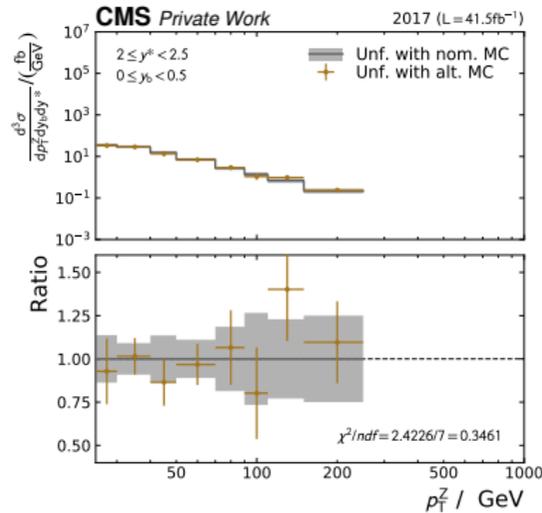
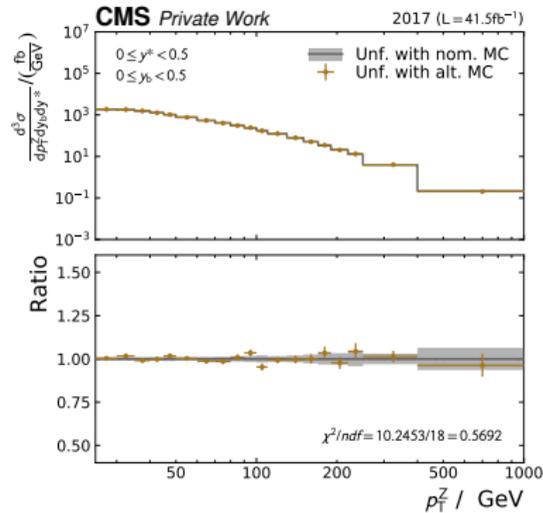
# Unfolding Closure 2016preVFP



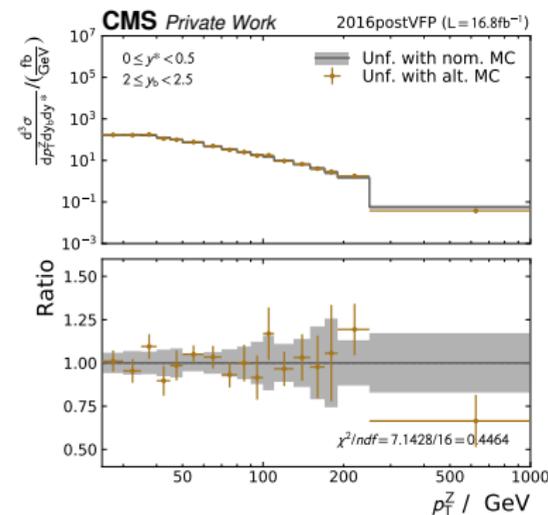
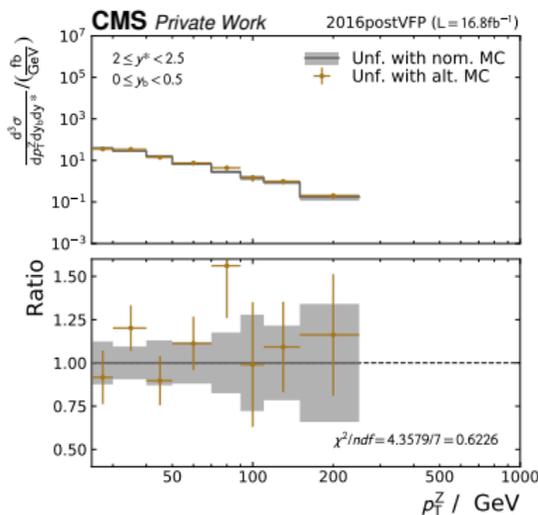
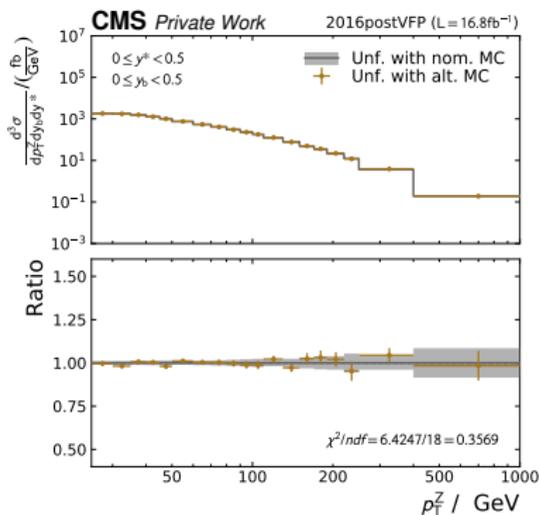
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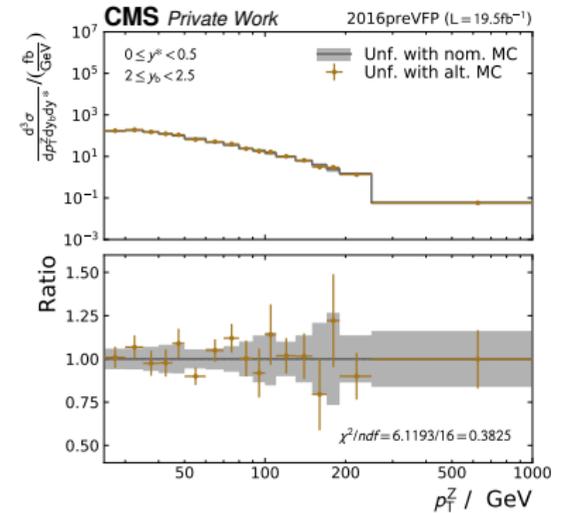
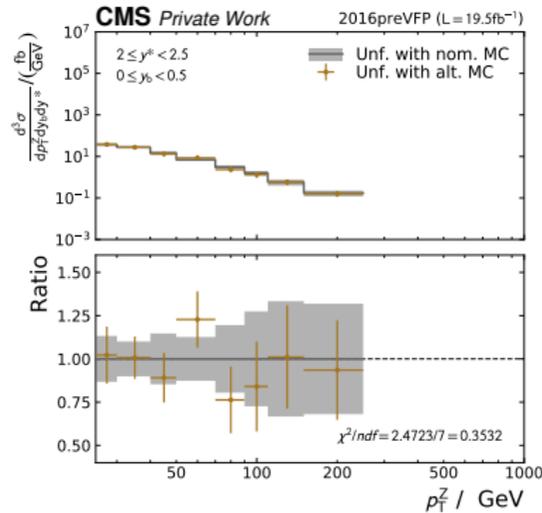
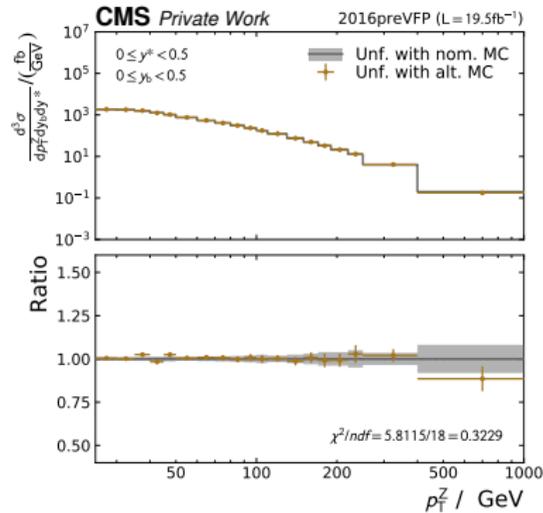
# Unfolding Model Dependence 2017



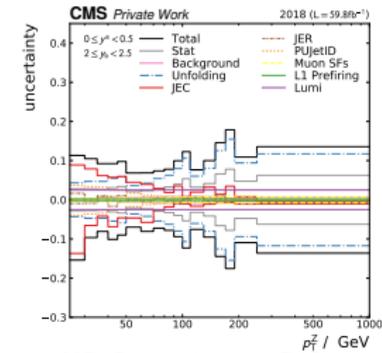
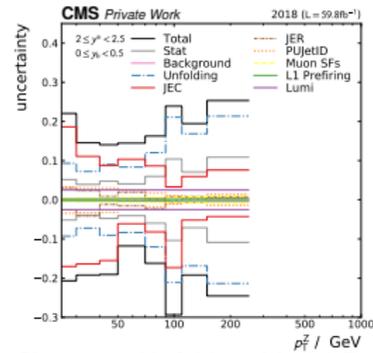
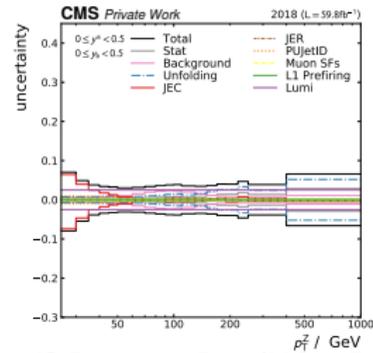
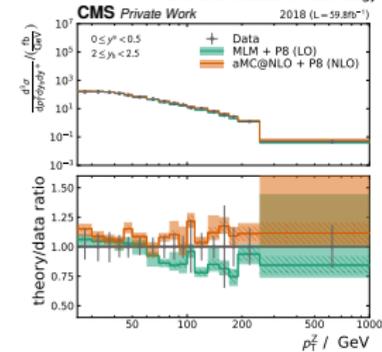
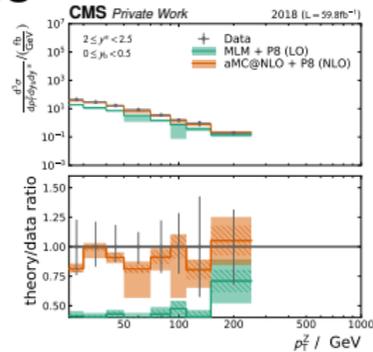
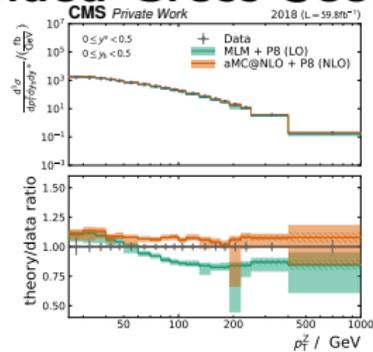
# Unfolding Model Dependence 2016postVFP



# Unfolding Model Dependence 2016preVFP

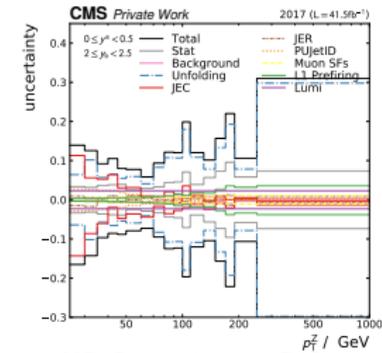
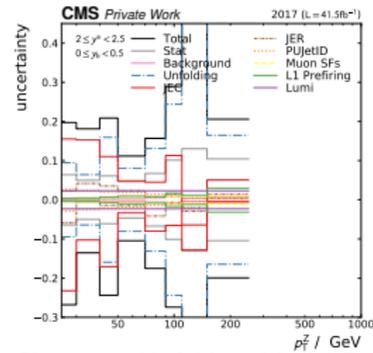
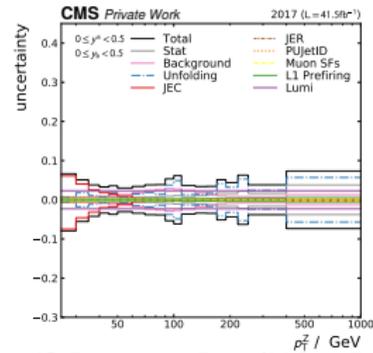
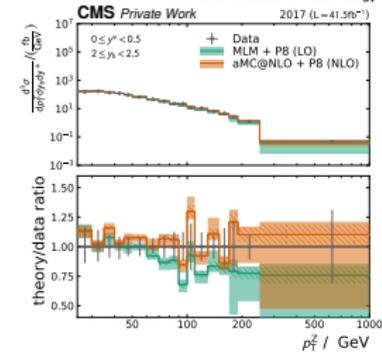
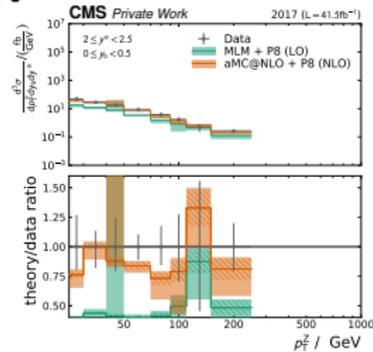
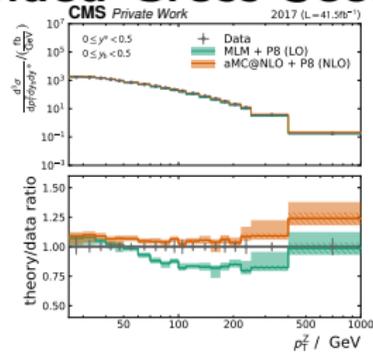


# Unfolded Cross-Sections 2018



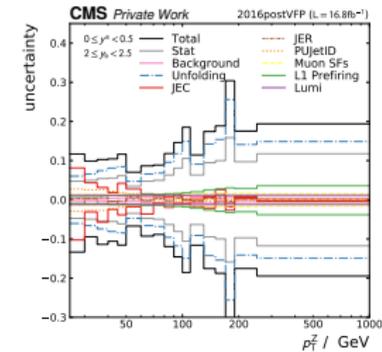
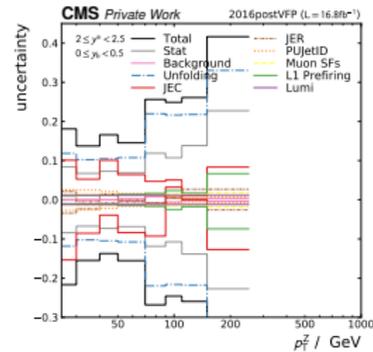
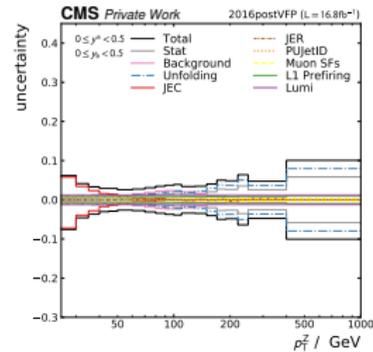
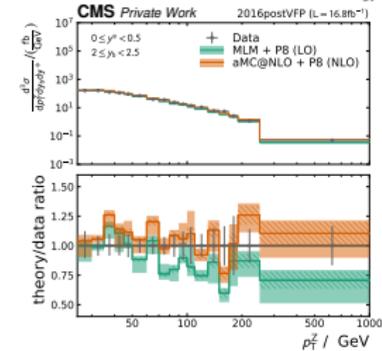
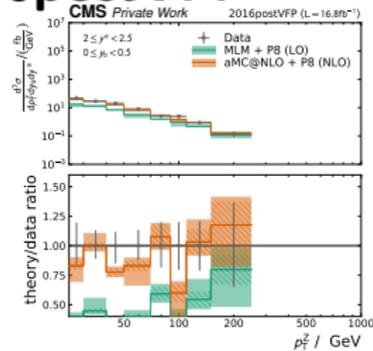
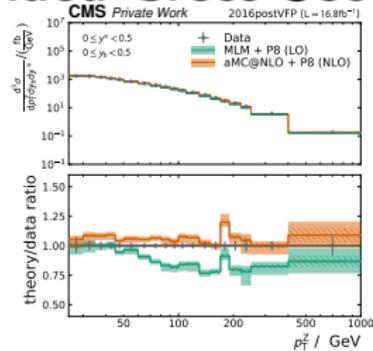
- Selections ○○
- IS-Partons ○
- Data/MC ○○○○
- Response Matrices ○○○○
- Closure ○○○○
- Unfolding Model Dependence ○○○○
- Results ●○○○
- NP-Corrections ○
- References ○

# Unfolded Cross-Sections 2017



- Selections ○○
- IS-Partons ○
- Data/MC ○○○○
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- Closure ○○○○
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- Results ●●○
- NP-Corrections ○
- References ○

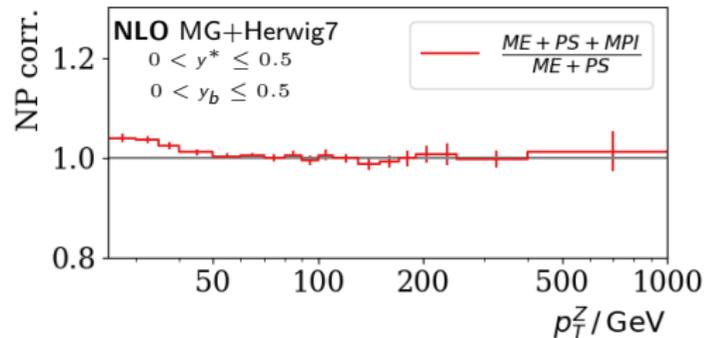
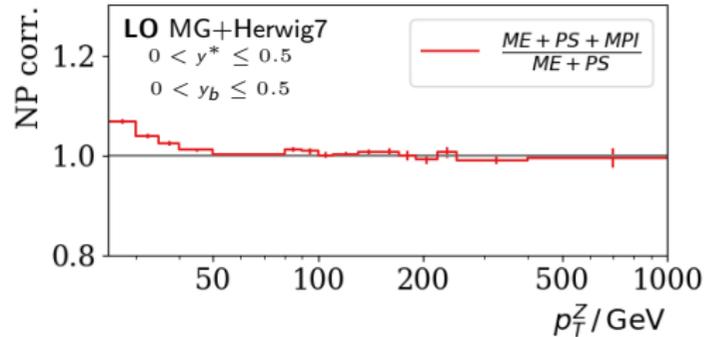
# Unfolded Cross-Sections 2016postVFP



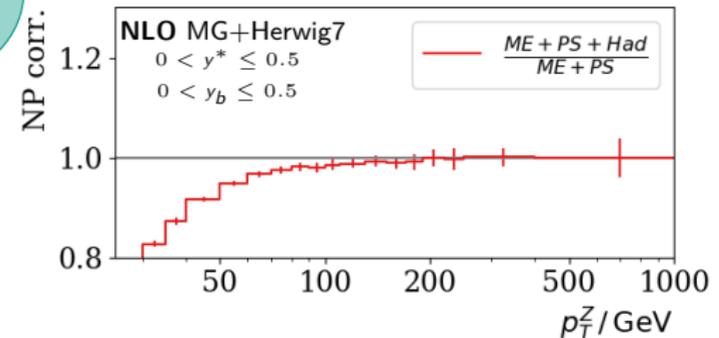
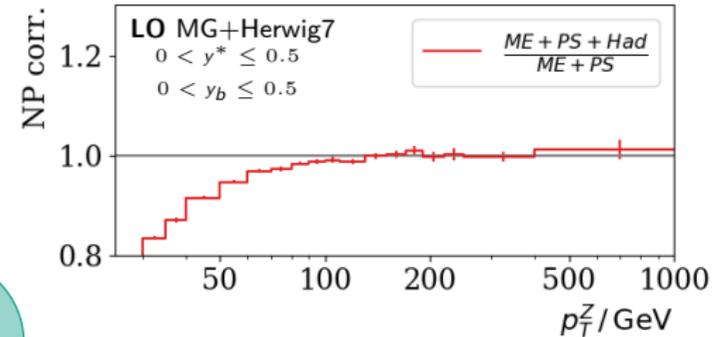
○ Selections    ○ IS-Partons    ○ Data/MC    ○ Response Matrices    ○ Closure    ○ Unfolding Model Dependence    ○ Results    ○ NP-Corrections    ○ References



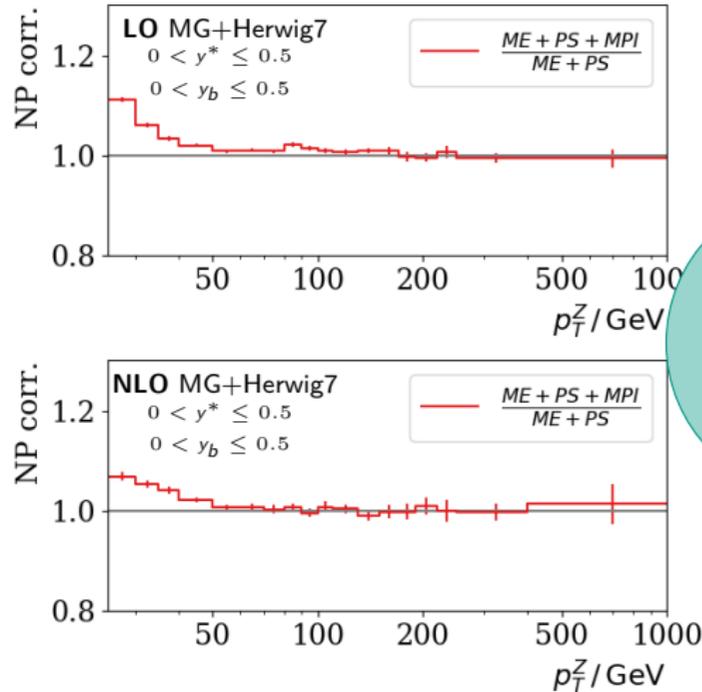
# MPI and Hadronization effects



anti- $k_T$ ,  
 $R = 0.4$



# MPI and Hadronization effects



anti- $k_T$ ,  
 $R = 0.8$

