

$B \rightarrow \rho \ell \nu_\ell$ with Hadronic Full Event Interpretation Tag at Belle II

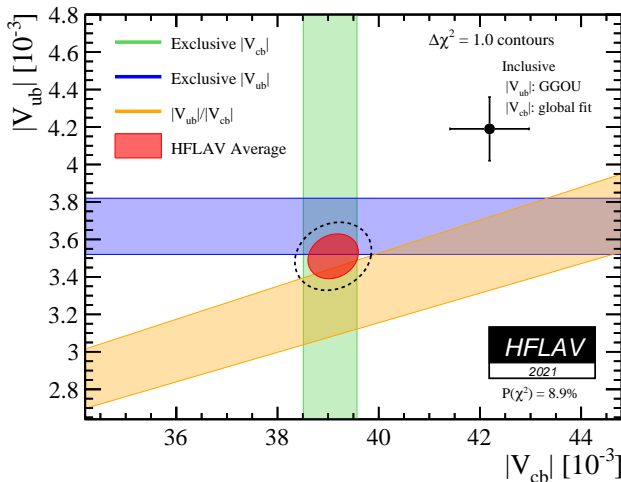
KSETA Plenary Workshop 2023

Moritz Bauer, Torben Ferber, Pablo Goldenzweig | 29. March 2023



B-Physics and Semileptonic Decays

- Many decay processes for B mesons \rightarrow Many opportunities for SM tests and searches
- CKM Matrix $|V_{ub}|$ and $|V_{cb}|$: Tension ($\approx 3.3\sigma$) between determination from
 - **inclusive** (all $B \rightarrow X\ell\bar{\nu}_\ell$) and
 - **exclusive** (one $b \rightarrow x$ process)
- Differences both in theory and experiment



$B \rightarrow \rho \ell \nu_\ell$ decays

- CKM matrix element $|V_{ub}|$ from $B \rightarrow \rho \ell \nu_\ell$ shows tension with

- $|V_{ub}|$ from $B \rightarrow \pi \ell \nu_\ell$
- $|V_{ub}|$ from $B \rightarrow X_u \ell \nu_\ell$ (inclusive)

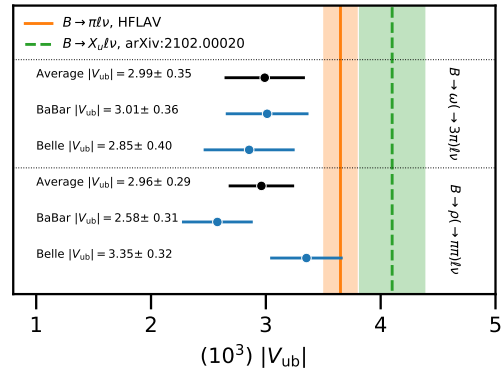
- Slight tension in last two published measurements of branching fraction of

... $B^+ \rightarrow \rho^0 \ell^+ \nu_\ell$:

- Belle (2013): $1.83 \pm 0.10 \pm 0.10$
- BaBar (2011): $0.94 \pm 0.08 \pm 0.14$

... $B^0 \rightarrow \rho^- \ell^+ \nu_\ell$:

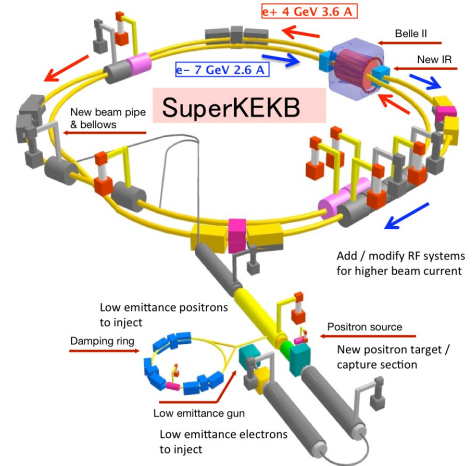
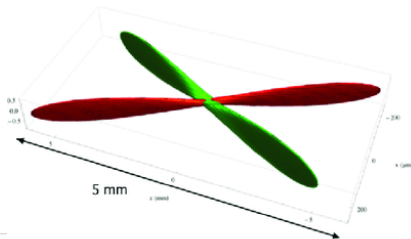
- Belle (2013): $3.22 \pm 0.27 \pm 0.24$
- BaBar (2011): $1.75 \pm 0.15 \pm 0.27$



Determination by Bernlochner, Prim, and Robinson

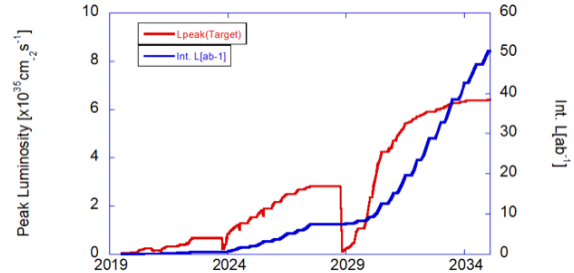
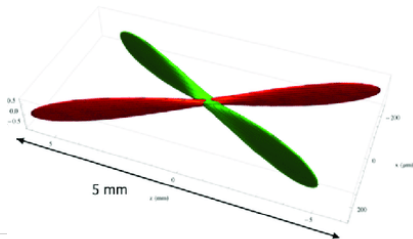
World record luminosity: SuperKEKB accelerator

- Asymmetric e^+e^- collider with $\sqrt{s} \approx 10.6$ GeV ($\Upsilon(4S)$ resonance)
- Peak luminosity (June 22): $3.1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ (+50% vs. KEKB)
 - In part thanks to nano-beam scheme.

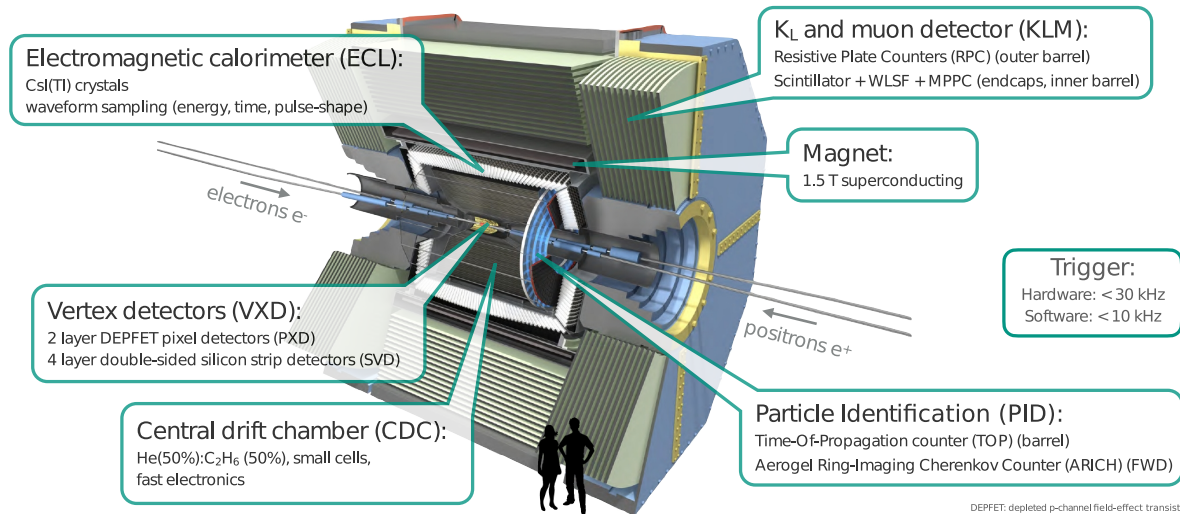


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- Current recorded dataset: $\approx 428 \text{ fb}^{-1}$
 - $\approx 1/2$ Belle, \approx BaBar
 - Aiming for 50x of Belle's dataset (50 ab^{-1})



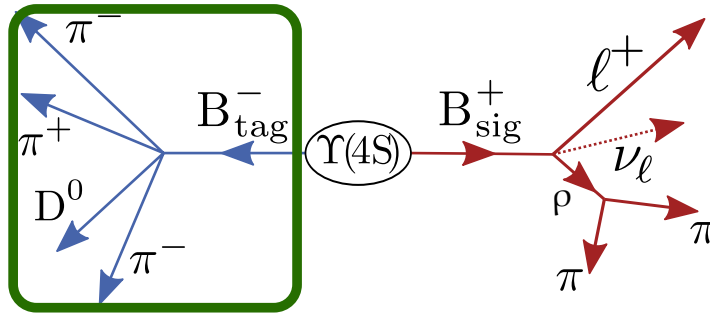
The Belle II detector



DEPFET: depleted p-channel field-effect transistor
WLSF: wavelength-shifting fiber
MPPC: multi-pixel photon counter

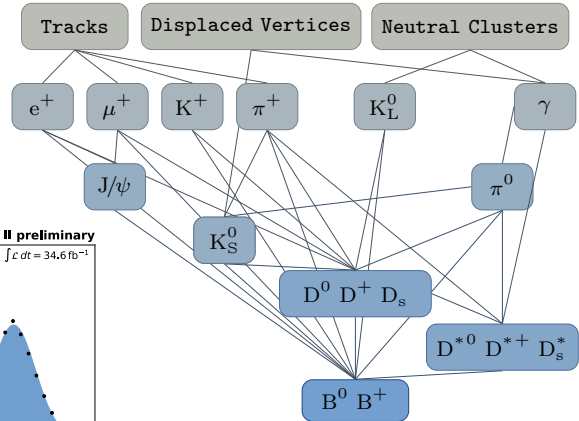
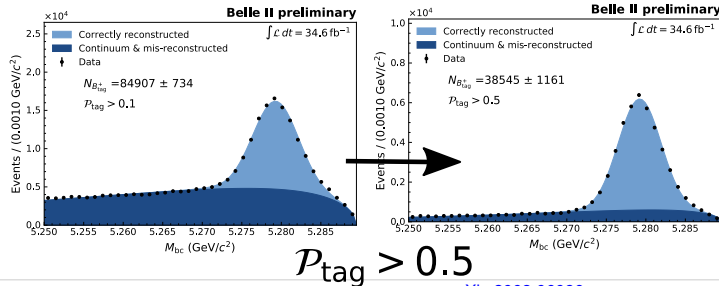
Experimental Techniques

- e^-e^+ collisions “clean” compared to pp and initial state well known.
→ knowing the second B gives you complete knowledge on kinematics
- Tagging: Reconstruct 2nd B (B_{tag}) e.g. with Full Event Interpretation (FEI). [Keck, T. et al. Comput Softw Big Sci 3, 6](#)



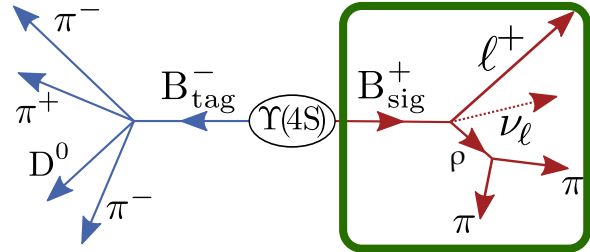
Experimental Techniques: FEI

- FEI: Use ≈ 200 BDT classifiers in 7 stages to reconstruct B mesons in $\mathcal{O}(10000)$ decay channels
- Cut on final classifier \mathcal{P}_{tag} used to set working point



Event Reconstruction and Selection

- Use track & particle ID selections to determine track quality & particle species
- Create a ρ candidate from two pion-like tracks/clusters
- Combine ρ candidate with lepton-like track to B_{sig}
- Combine B_{sig} with B_{tag} from FEI to $\Upsilon(4S)$ candidate
- Enhance purity using remaining tracks & clusters



MVA Event Selection

Suppress $e^-e^+ \rightarrow q\bar{q}$ with BDT:

- Sphericity & thrust variables
- Only use most-discriminating variables as determined by re-training without each variable
- Cut at 0.8 rejects 95% of $q\bar{q}$ background and retains 93% of signal

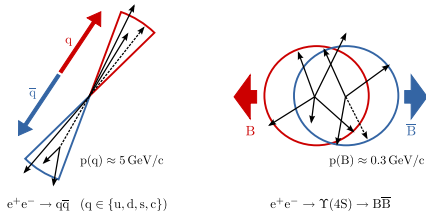
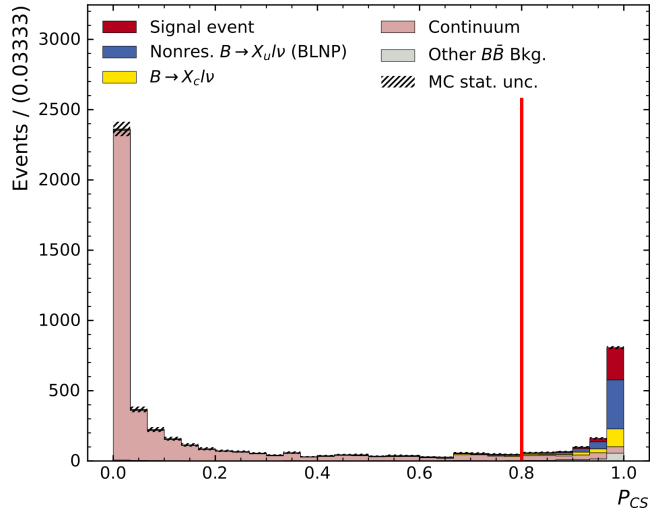


Illustration by M. Röhrken

Belle II Own Work

ρ^0 (Simulation)



ICHEP 2022: Preliminary Result (arXiv:2211.15270)

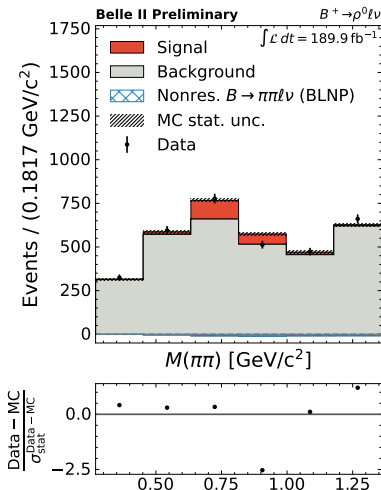
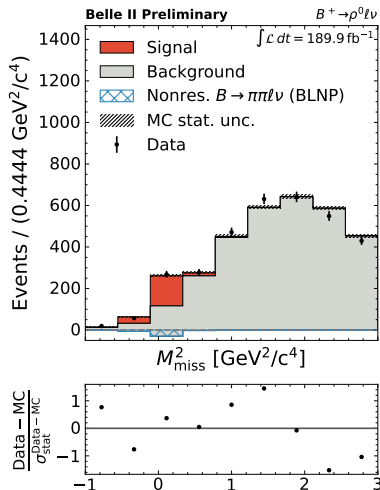
- Signal extraction in di-pion mass $M_{\pi\pi}$ and missing mass

$$M_{\text{miss}}^2 = (\mathbf{p}_{\text{CMS}} - \mathbf{p}_{\text{tag}} - \mathbf{p}_{\rho} - \mathbf{p}_{\ell})^2$$

- Two-dimensional binned template fit with three components:

- $B \rightarrow \rho \ell \nu_{\ell}$ signal
- Non-resonant $B \rightarrow \pi\pi \ell \nu_{\ell}$
- Other backgrounds (mostly $B \rightarrow X_c \ell \nu_{\ell}$)

- Large post-fit uncertainties from negative yield in non-resonant model



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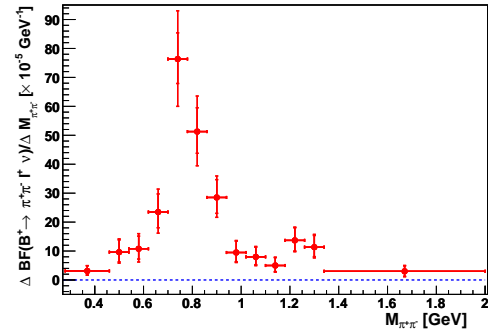
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Source	% of $\mathcal{B}(B^0 \rightarrow \rho^- \ell^+ \nu_{\ell})$	% of $\mathcal{B}(B^+ \rightarrow \rho^0 \ell^+ \nu_{\ell})$
-		
f_{+0}	1.2	1.2
FEI calibration	2.7	6.1
$N_{B\bar{B}}$	1.5	1.5
Reco. efficiency ϵ	0.5	0.3
Tracking	0.6	0.9
Lepton ID	0.7	0.5
Hadron ID	0.3	0.6
π^0 efficiency	4.4	—
$B \rightarrow f_2/f_0\ell\nu_{\ell}$ BF	—	12.1
$B \rightarrow X_u\ell\nu_{\ell}$ BFs	2.8	4.8
$B \rightarrow X_c\ell\nu_{\ell}$ BFs	0.5	0.5
$B \rightarrow \rho\ell^+\nu_{\ell}$ form factor	2.7	0.7
$B \rightarrow \pi\pi\ell\nu_{\ell}$ model	27.3	14.4
Total	28.2	20.5

Constraining the $B \rightarrow \pi\pi\ell\nu_\ell$ Background in $B^+ \rightarrow \rho^0\ell^+\nu_\ell$

- Complex backgrounds from other decays to two pions
 - $f_0(500)$, $f_0(980)$, $f_2(1270)$, $\rho^0(1450)$
 - Maybe non-resonant $B \rightarrow \pi\pi\ell\nu_\ell$
- These are not measured
 - extract in-situ using di-pion mass
- Constrain sum of all backgrounds and signal using input from Belle's 2021 inclusive measurement (Belle 2021) of $B \rightarrow \pi\pi\ell\nu_\ell$

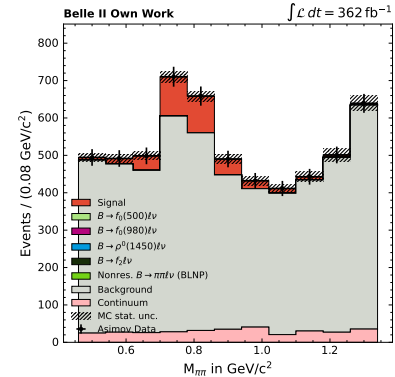
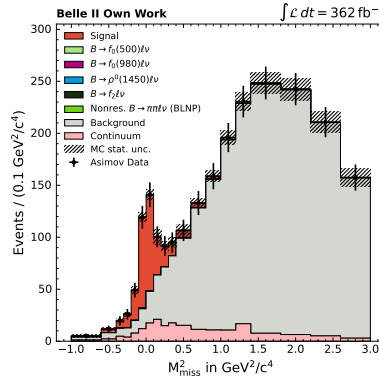
Phys. Rev. D 103, 112001 (2021)



Di-pion mass in Belle's inclusive $B \rightarrow \pi\pi\ell\nu_\ell$

Fit Setup (Asimov Data)

- Two-dimensional fit with 8 templates:
 - 6 for resonant and non-resonant $B \rightarrow X_u \ell \nu_\ell$
 - 1 for all $B\bar{B}$ backgrounds (dominated by $B \rightarrow X_c \ell \nu_\ell$)
 - 1 for $q\bar{q}$ backgrounds (constrained from non- $\Upsilon(4S)$ data)
- Larger bins at edges of M_{miss}^2
- $M_{\pi\pi}$ bins matching Belle 2021



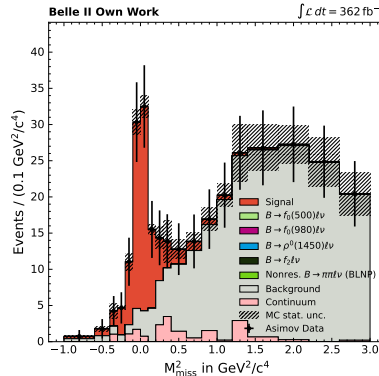
Fit Setup with Constraint (Asimov Data)

- Contributions from resonant, di-pion X_u backgrounds expected to be tiny but are unmeasured

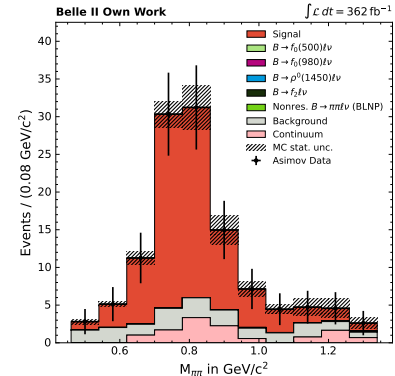
⇒ Float individual yields Y_i and constrain with Belle 2021 by adding term to $-\ln\mathcal{L}$:

$$\left(\frac{\mathcal{B}_{\text{Belle 2021}} - \sum_i^6 \epsilon_i \times Y_i}{\sigma_{\mathcal{B}_{\text{Belle 2021}}}} \right)^2$$

- ϵ_i from simulation but allowed to vary within Gaussian prior



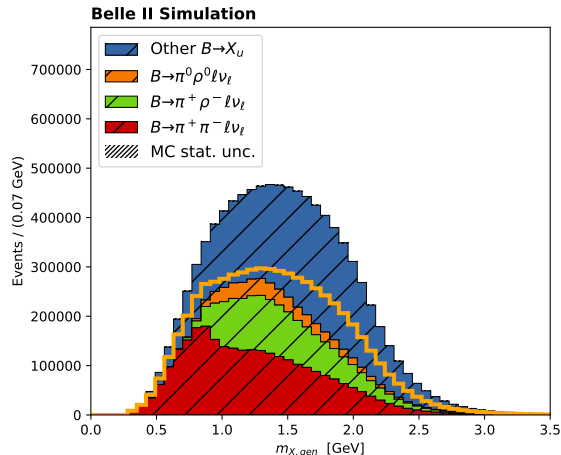
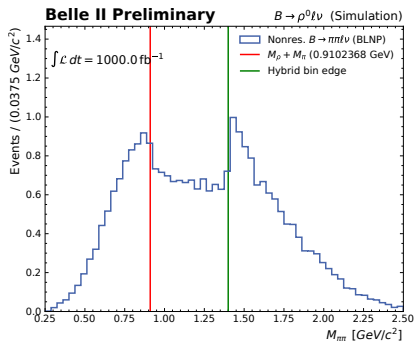
Bin 4: $0.7 < M_{\pi\pi} < 0.78 \text{ GeV}$



Bin 6: $-0.1 < M_{\text{miss}}^2 < 0.0 \text{ GeV}^2$

Systematic Uncertainties: Non-resonant shape

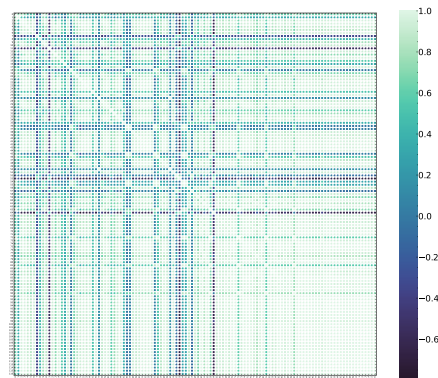
- ICHEP2022: Uncertainty from fit with two model variants
- Now: Reweight distribution to halve the effect and allow fit to modify the shape



Non-resonant $B \rightarrow \pi\pi\ell\nu_\ell$ shape from PYTHIA

Systematic Uncertainties in the Fit

- Main sources:
 - MC sample statistics
 - Analysis methods: Particle ID and FEI
 - $B \rightarrow X\ell\nu_\ell$ branching fractions and form factors
 - Non-resonant $B \rightarrow \pi\pi\ell\nu_\ell$ decay model
 - Procedure:
 - For each source, determine covariance matrix in bins of fit
 - In each template, sum covariance matrices assuming no correlation between sources
- $N_{bins} \times N_{template}$ nuisance parameters



Example: Correlation matrix for the background template

Up Next

$|V_{ub}|$ from $B \rightarrow \rho \ell \nu_\ell$

- BF in bins of momentum transfer + theory input gives access to $|V_{ub}|$
- At least three bins needed \rightarrow challenging with Belle II's statistics

Average and fit by
Bernlochner, Prim,
Robinson \rightarrow

