

SUB-GEV DARK MATTER IN THE LAB

NEW IDEAS AND NEW TOOLS

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Istituto Nazionale di Fisica Nucleare

Light Dark World 2023, September 2023

OUTLINE

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- Searching for keV-GeV dark matter

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- Down to the MeV: Migdal effect

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- Down to the MeV: Migdal effect
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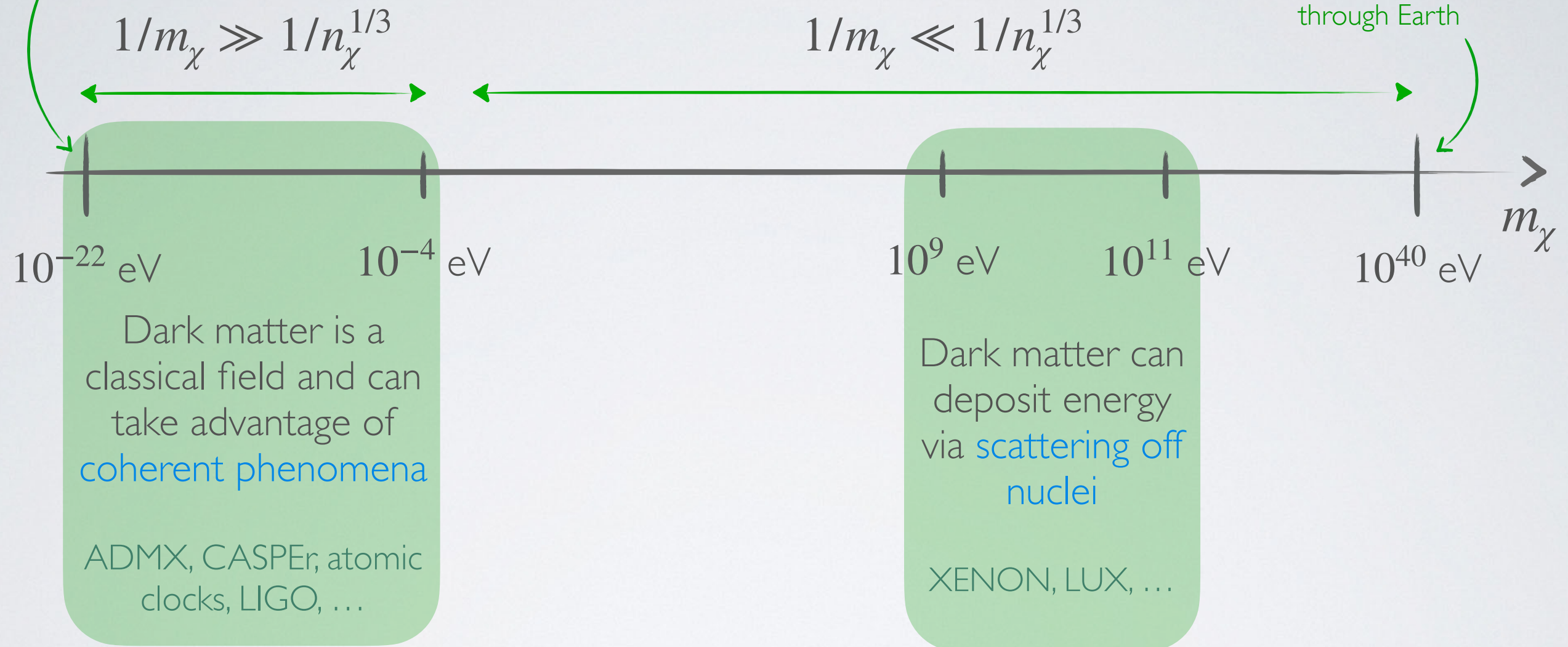
- Searching for keV-GeV dark matter
- Down to the MeV: Migdal effect
- Down to the keV: collective excitations
- Outlook

SUB-GEV DARK MATTER

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too light to explain halo structure

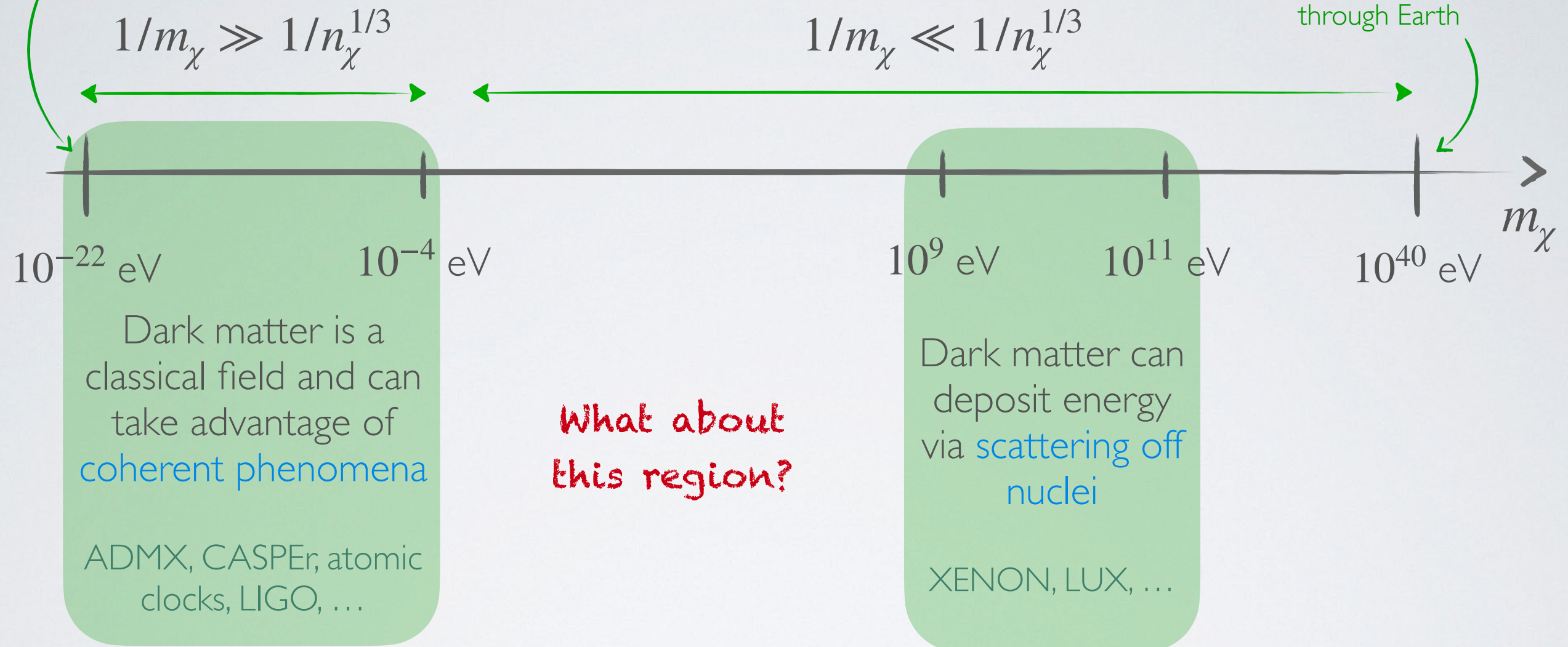
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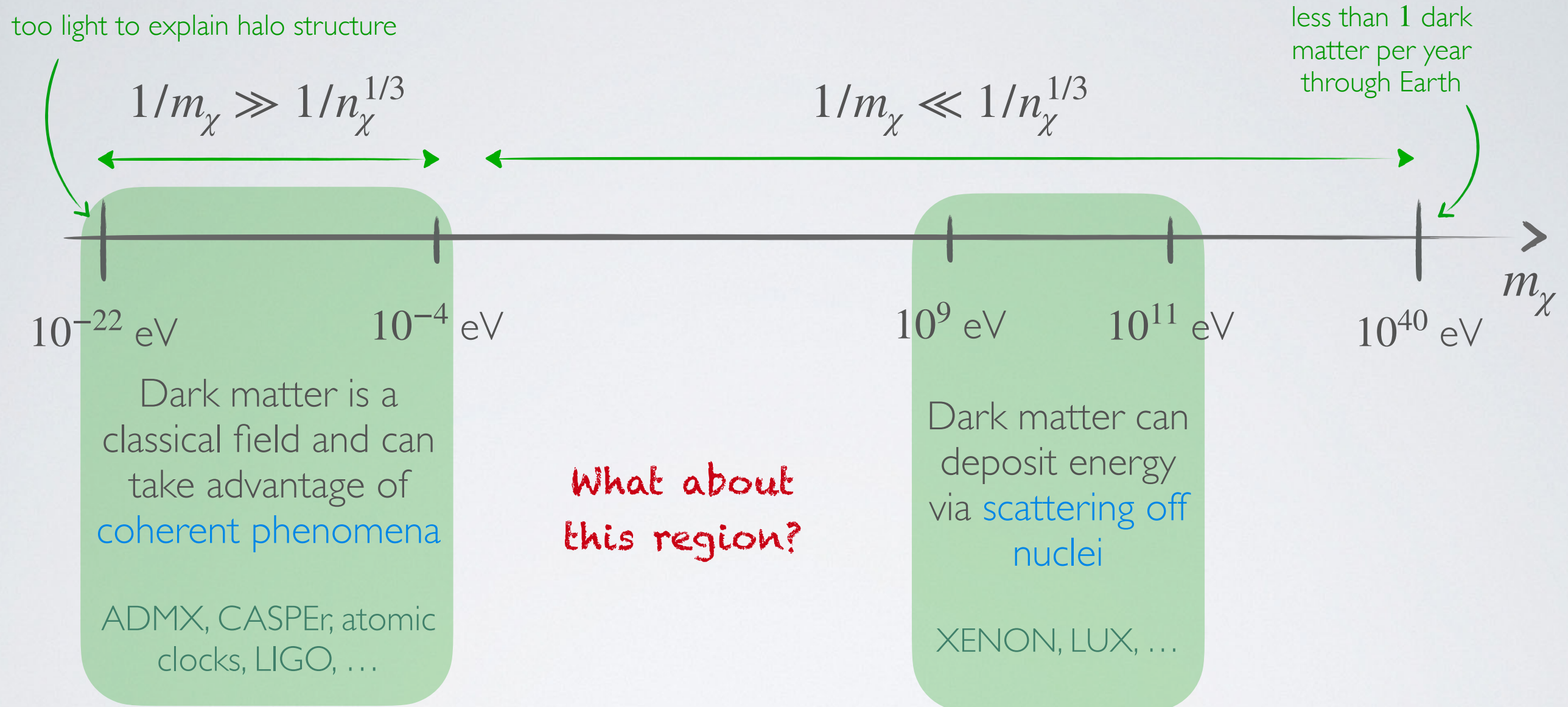
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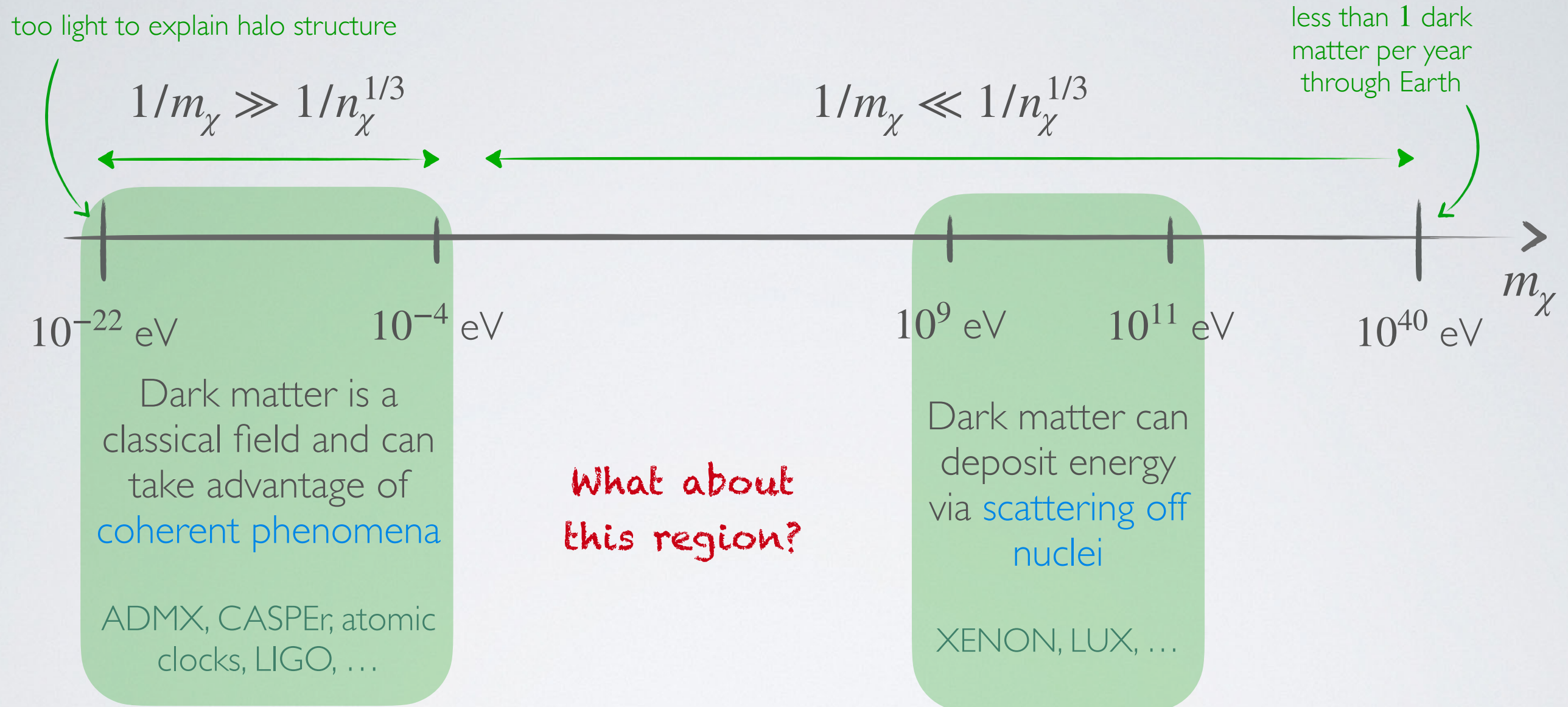


SUB-GEV DARK MATTER



- Dark matter is a particle but too light for elastic nuclear recoil

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- Need new materials and/or observables

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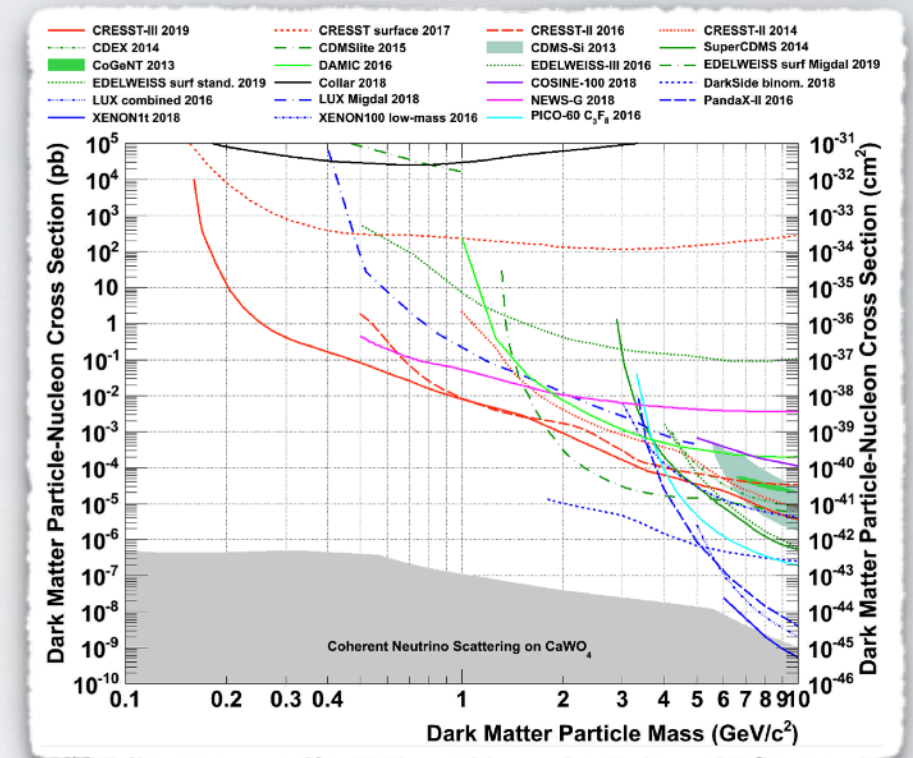
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[CRESST – PRD 2019, 1904.00498]

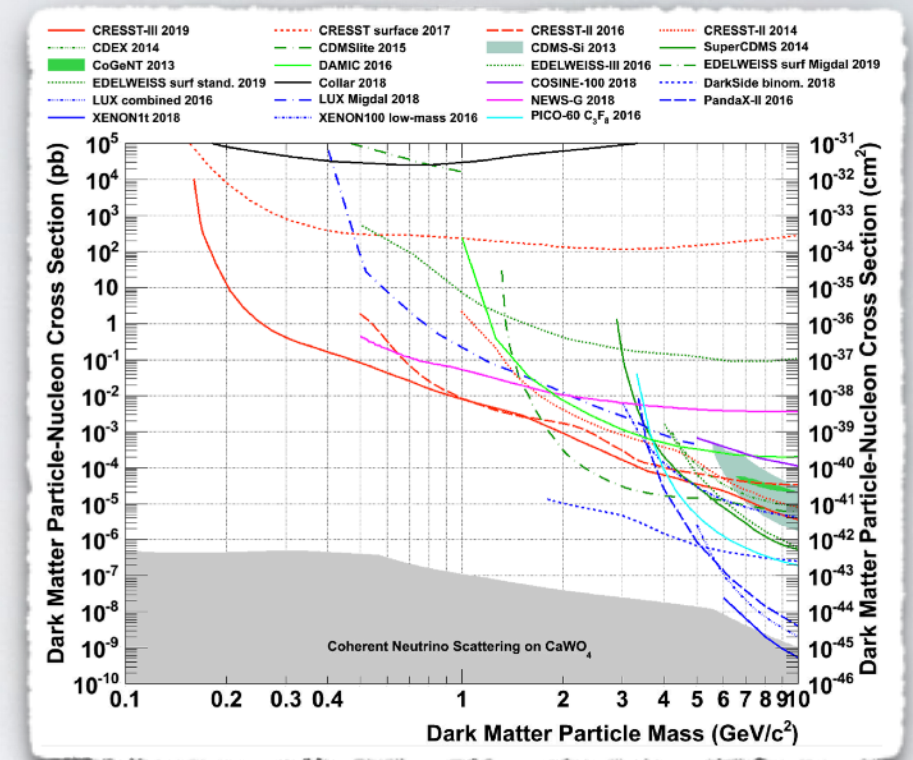
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- Two possibilities:
 - Look into lighter scattering targets
 - Look into inelastic processes

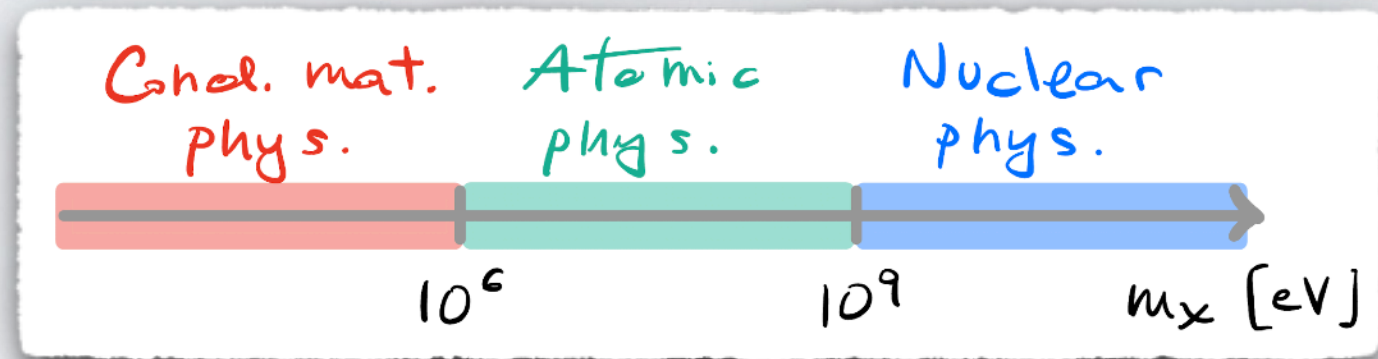


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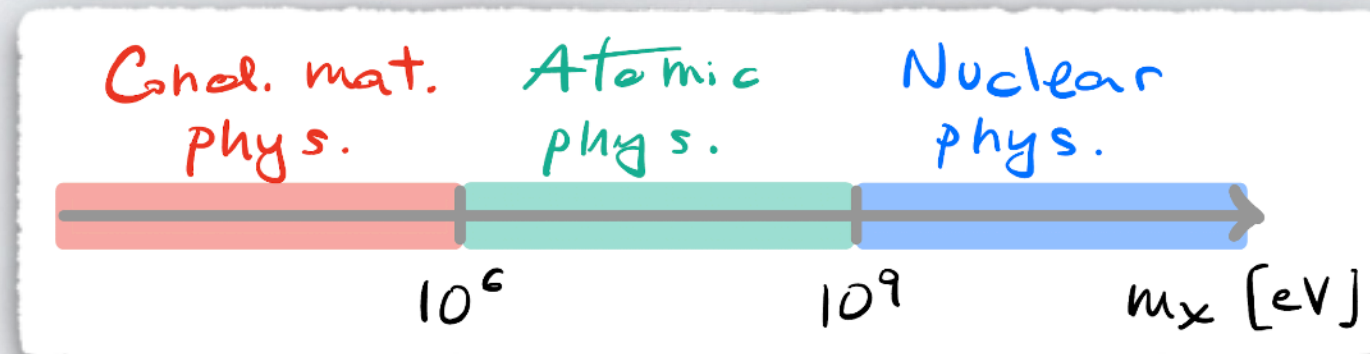
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- For sub-GeV dark matter one needs to delve into the condensed matter world

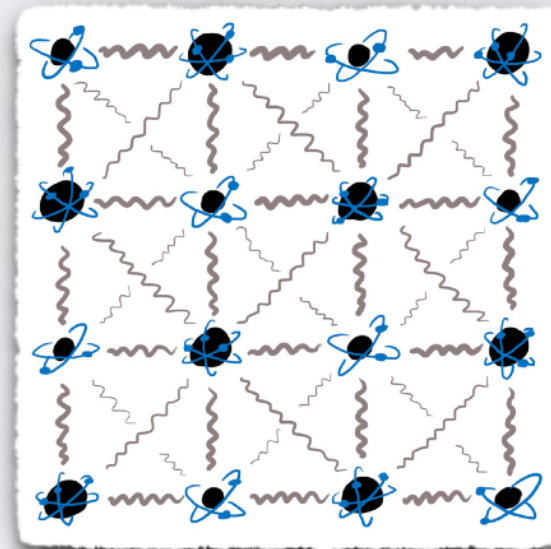


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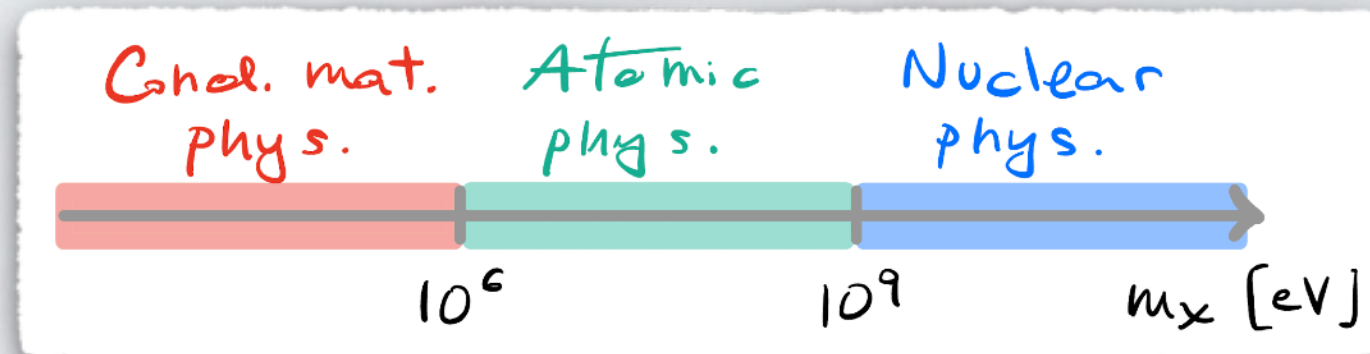


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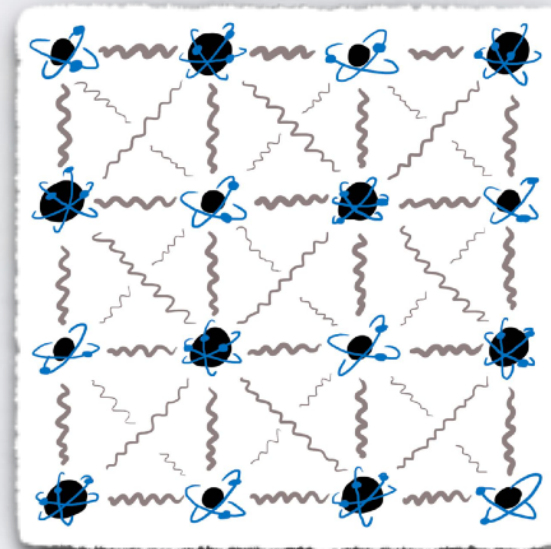


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- For sub-GeV dark matter one needs to delve into the **condensed matter world**



- Must **account for the complicated many-body physics** (correlations, strong coupling, ...)



- Need to find theoretical tools** that allow to solve or bypass these problems (measured correlation functions, EFTs, ...)

Down to the MeV

Migdal effect in semiconductors



MIGDAL EFFECT

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- For sub-GeV dark matter nuclear recoil signals become challenging
→ sensitivity can be lowered by [looking for inelastic processes](#)

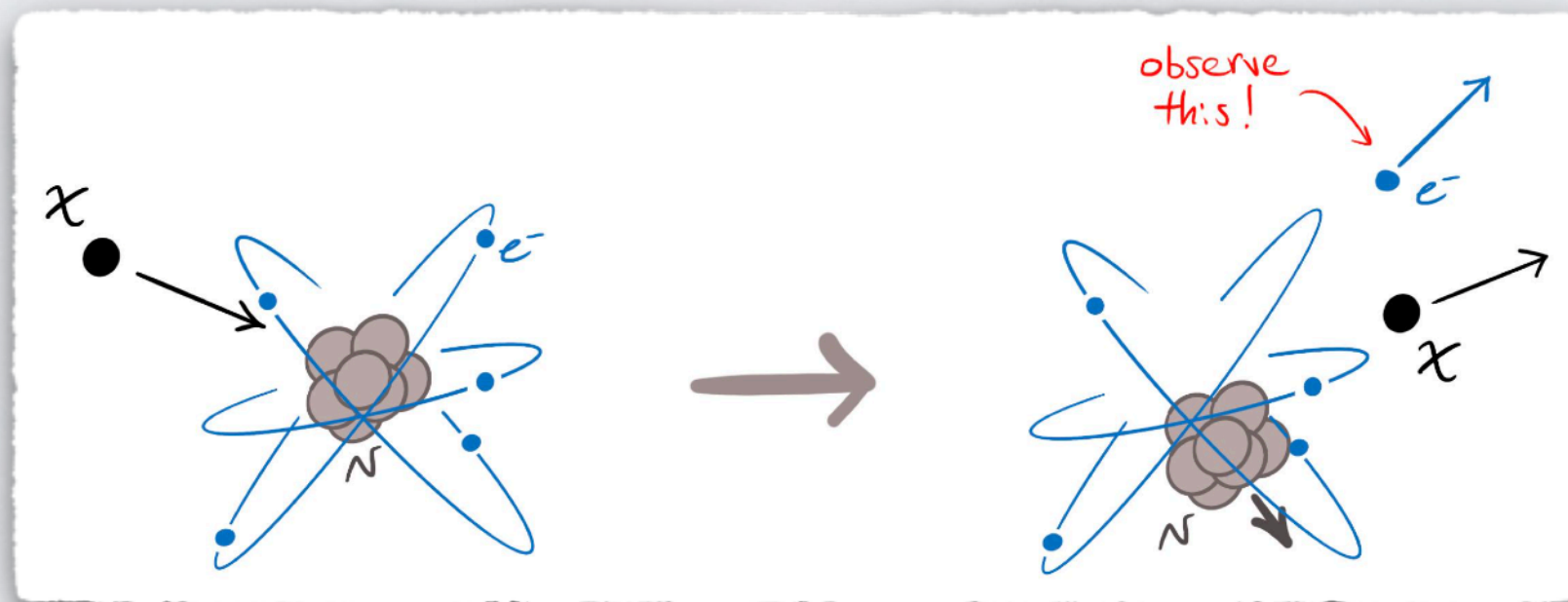
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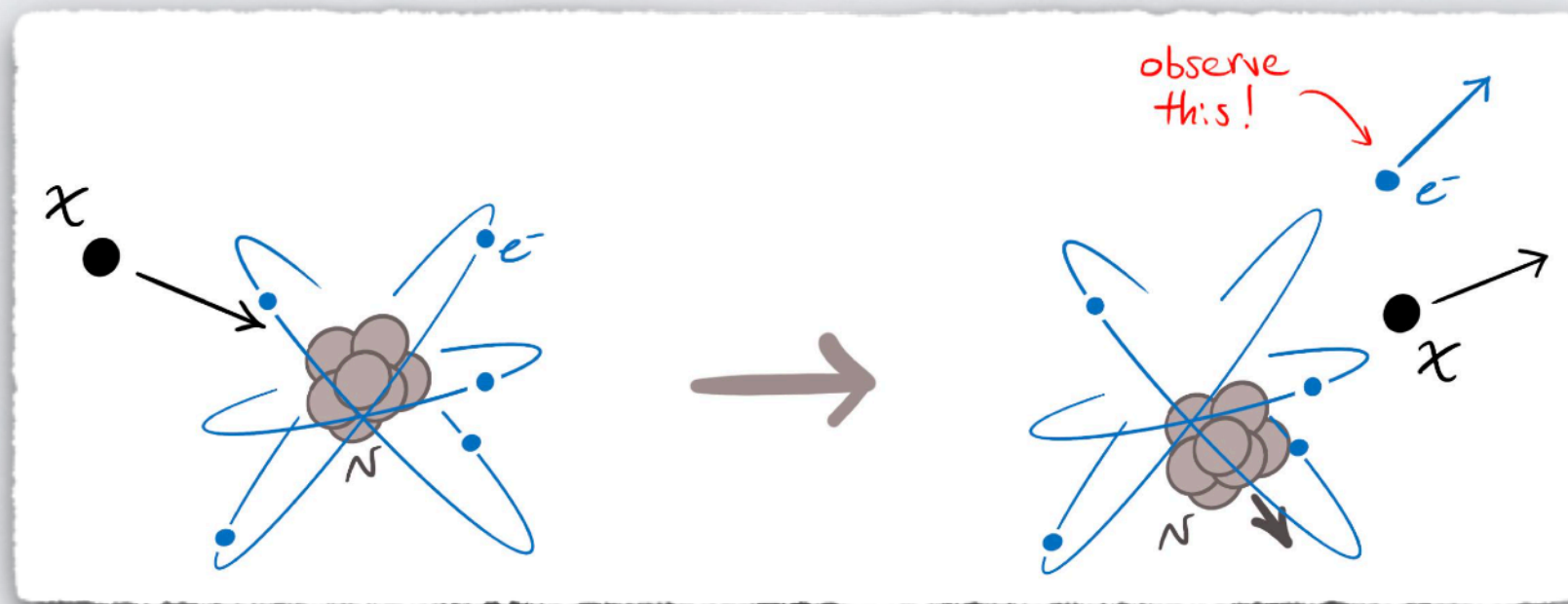


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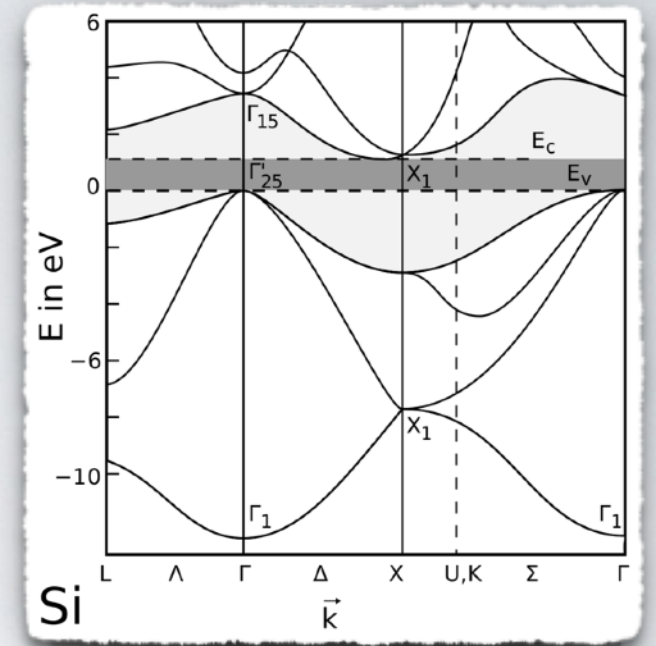
- Less likely... but lower threshold! → sensitivity down to $\mathcal{O}(100 \text{ MeV})$ masses

[e.g., Ibe, Nakano, Shoji, Suzuki – JHEP 2018, 1707.07258; DarkSide – 2207.11967]

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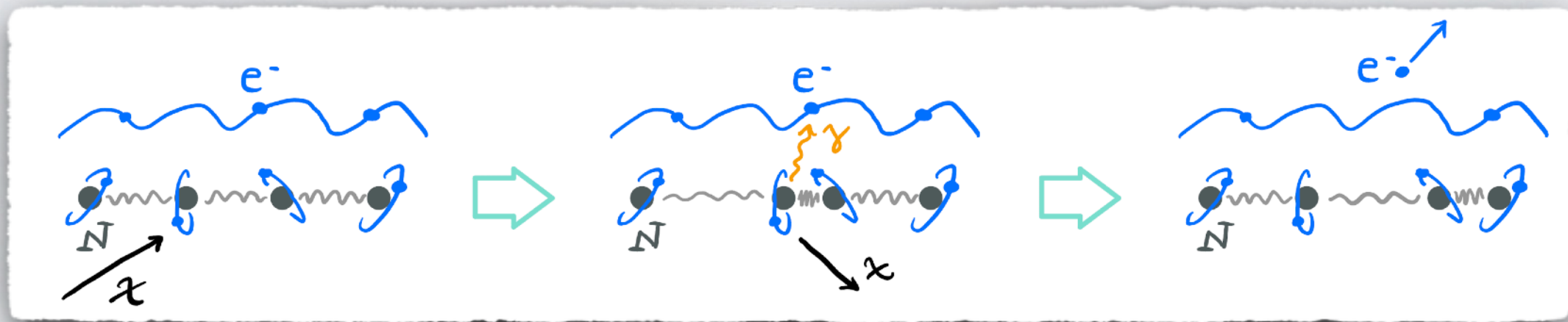
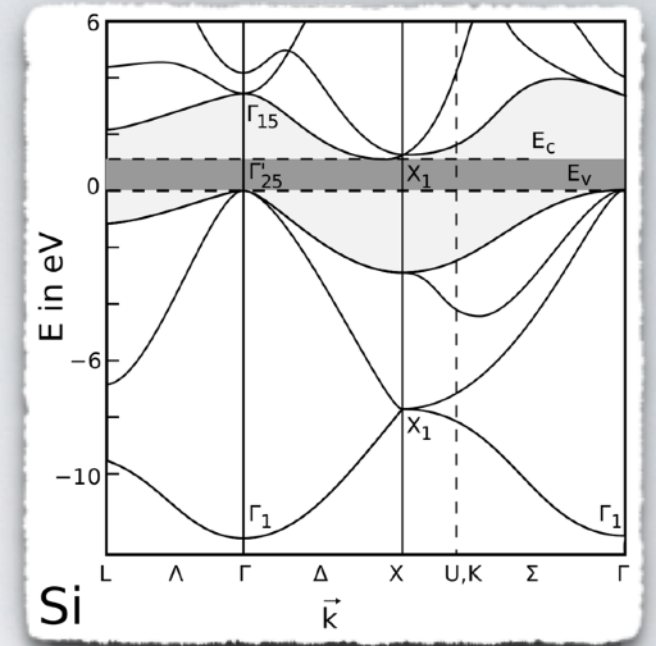
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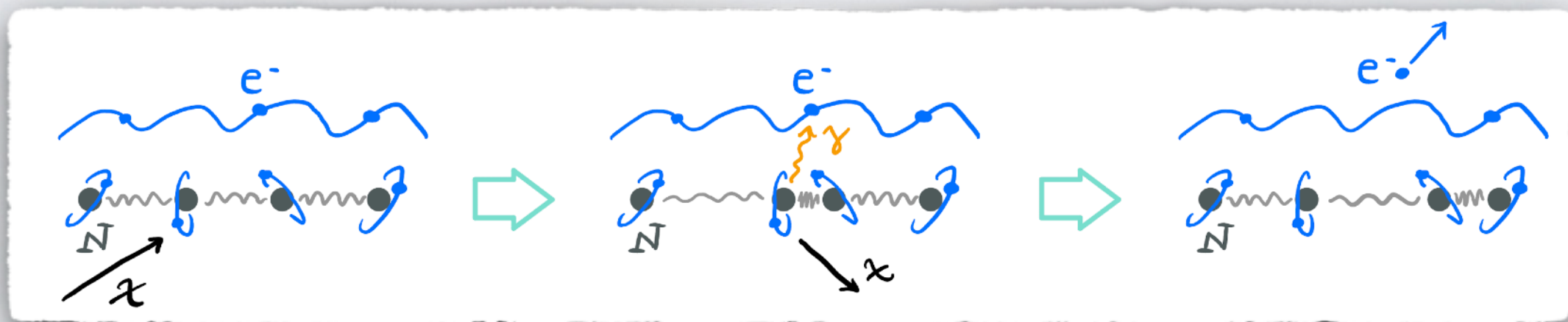
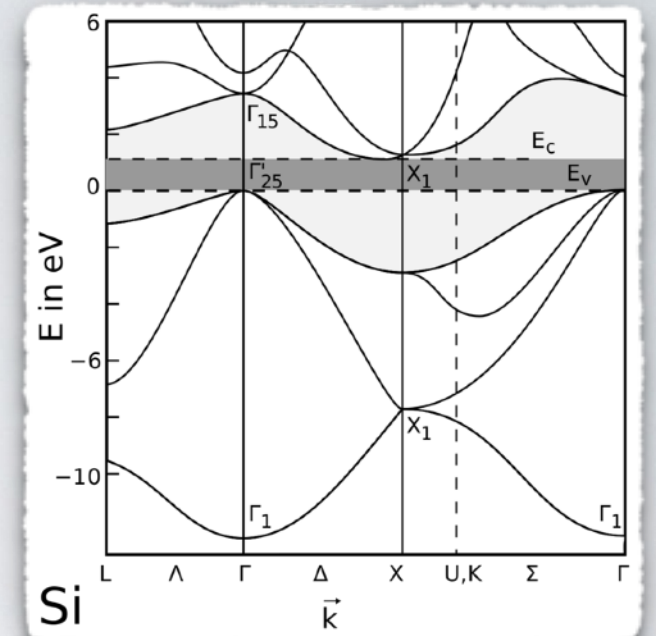
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- How to describe nucleus-nucleus and nucleus-electron interactions in a strongly correlated system?

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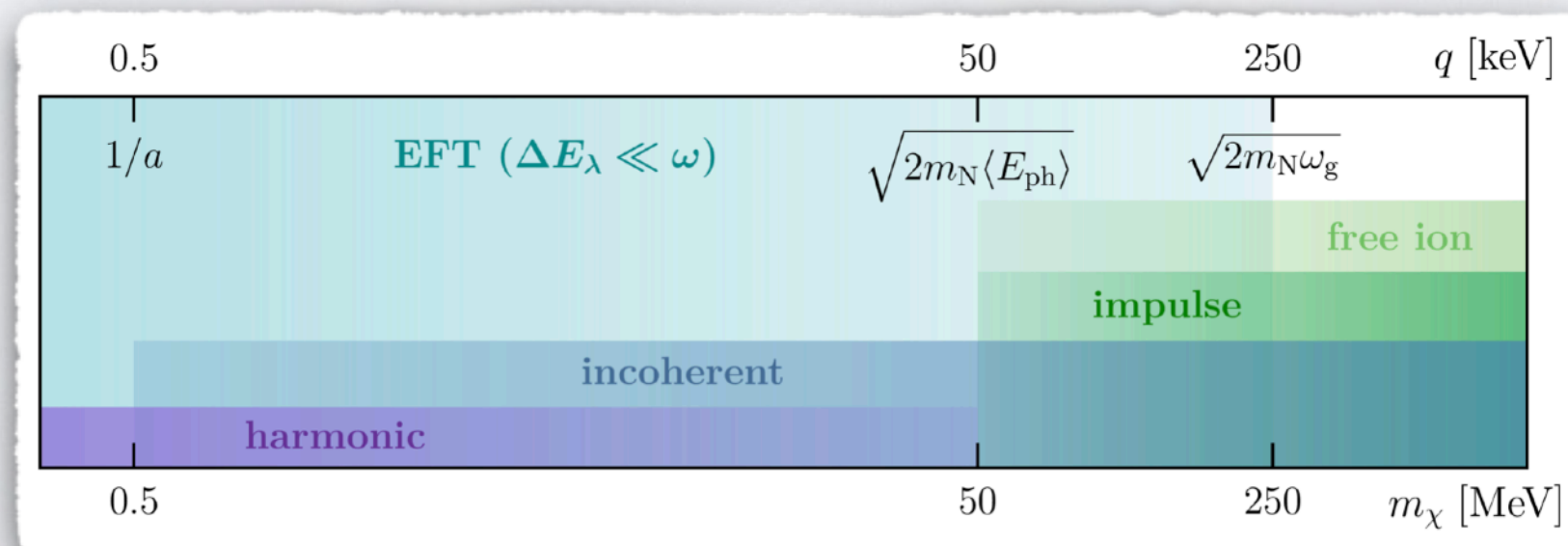
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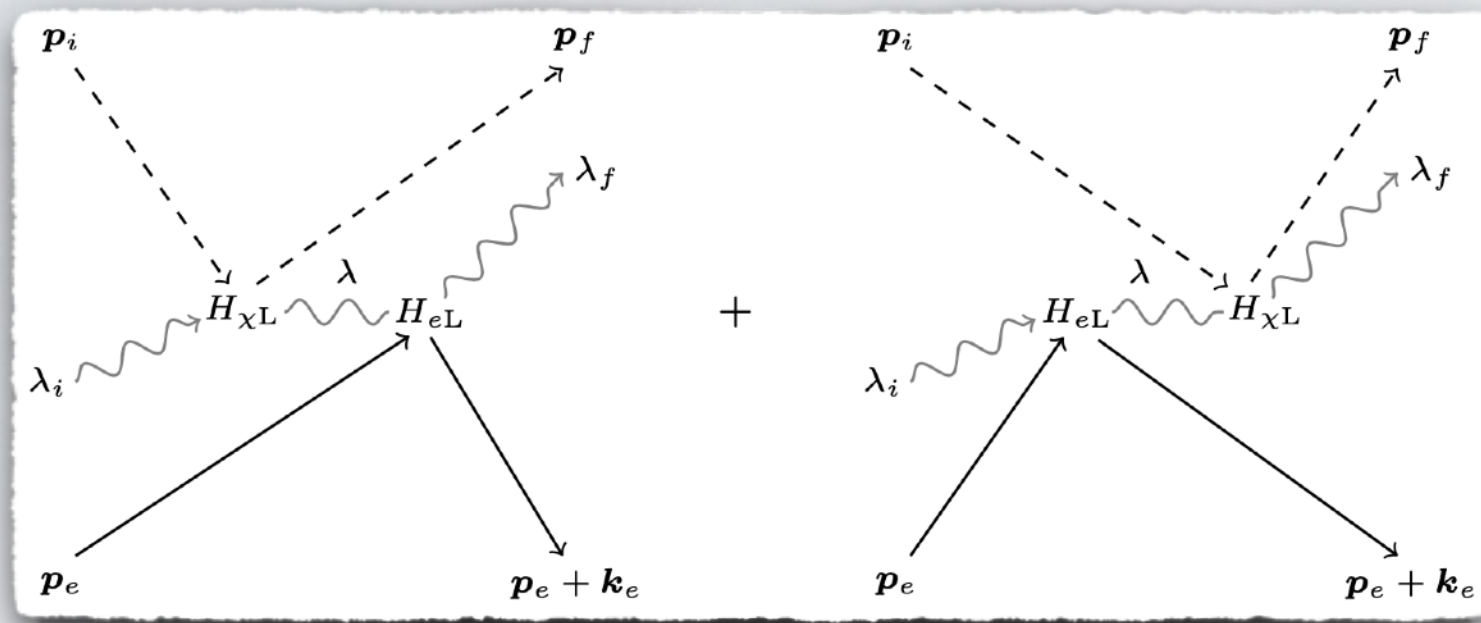
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EFT

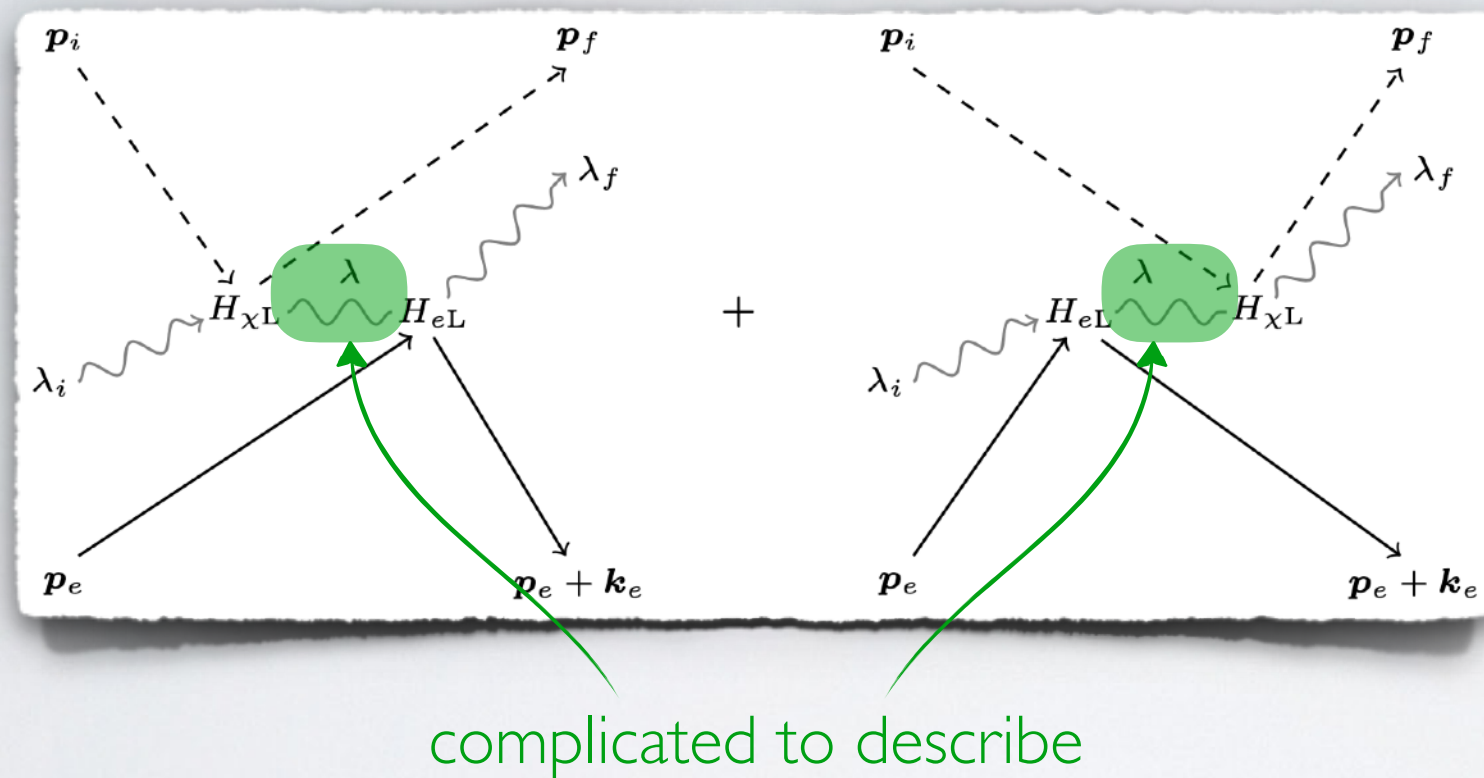
EFT

- Migdal effect in old-fashioned perturbation theory



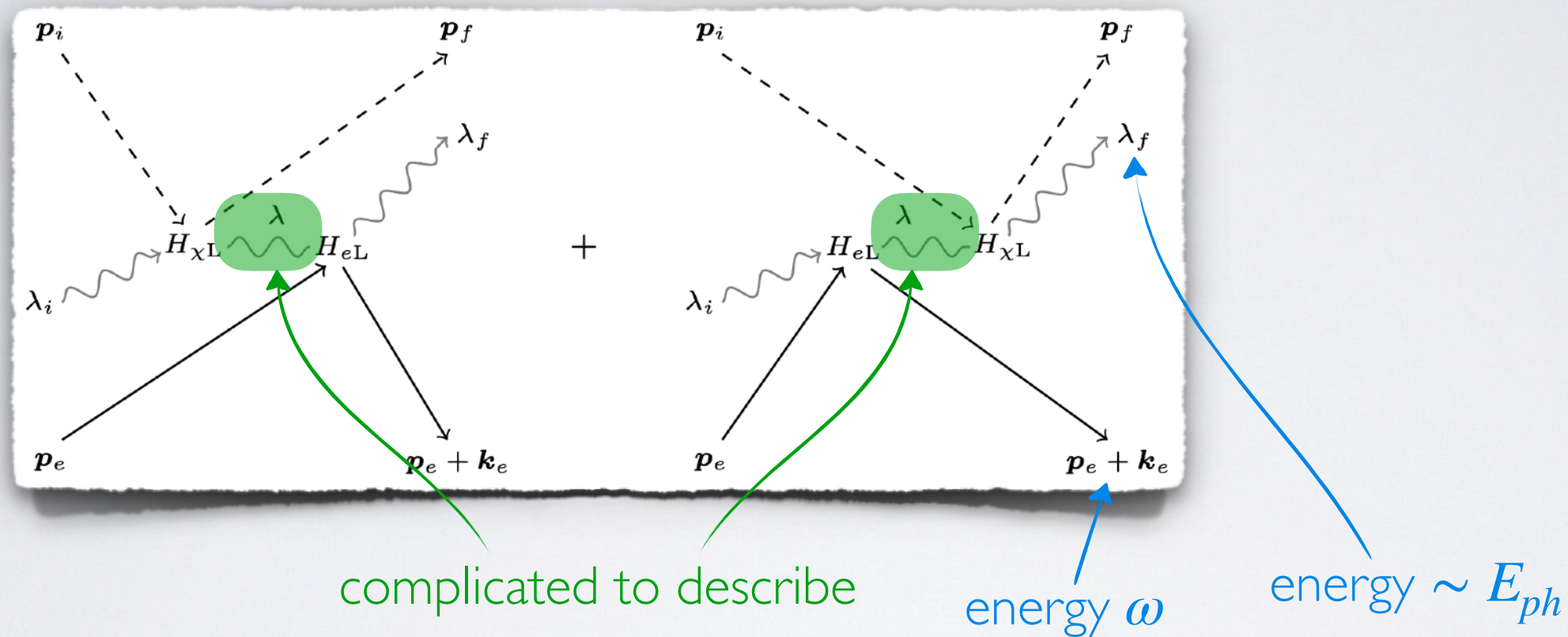
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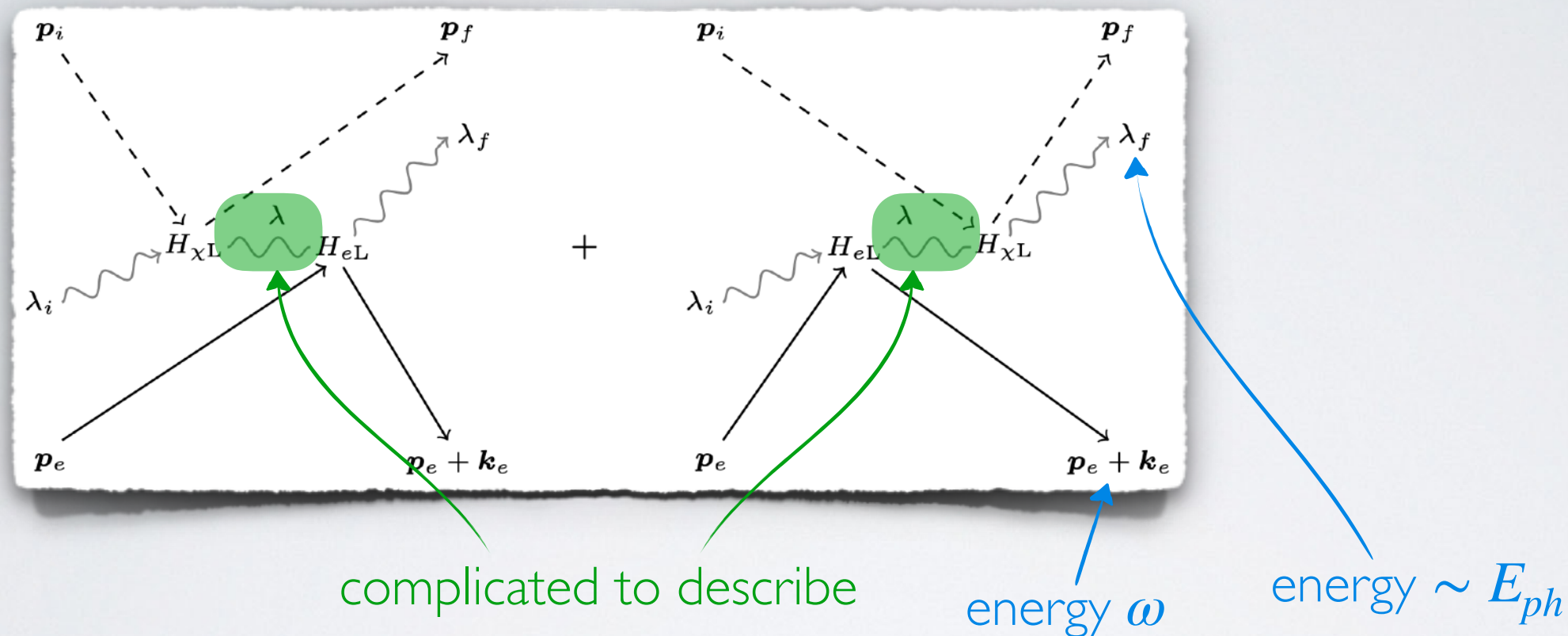
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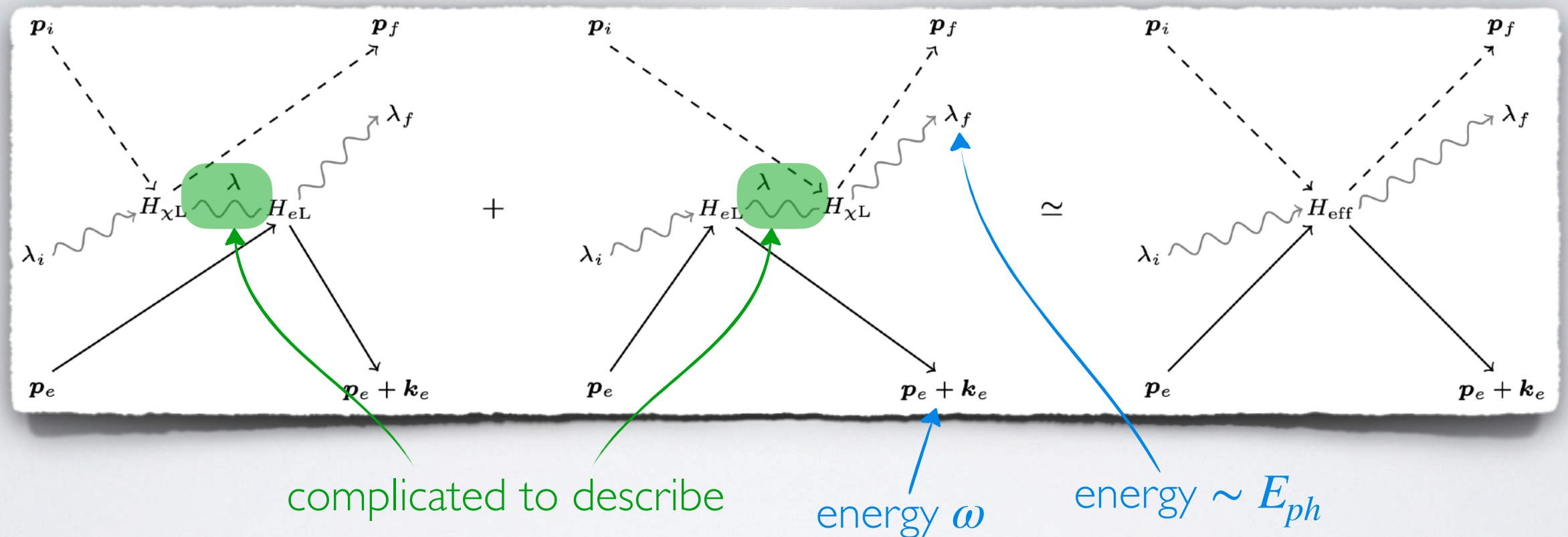
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$$H_{eff} = \frac{1}{m_N \omega^2} \vec{\nabla} H_{\chi L} \cdot \vec{\nabla} H_{eL} + \mathcal{O}\left(\frac{1}{\omega^3}\right)$$

[Berghaus, **AE**, Essig, Sholapurkar – JHEP 2020, 2210.06490]

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- Now simple to determine the [rate for Migdal emission](#)

$$\frac{d^2\Gamma}{d\omega dE_{ph}} \propto \sum_{\mathbf{k}} \sum_{\mathbf{K}, \mathbf{Q}} \frac{\mathbf{q} \cdot (\mathbf{k} + \mathbf{K}) \mathbf{q} \cdot (\mathbf{k} + \mathbf{K})}{|\mathbf{k} + \mathbf{K}| |\mathbf{k} + \mathbf{Q}|} \text{Im}(-\epsilon_{\mathbf{KQ}}^{-1}(\mathbf{k}, \omega)) S(\mathbf{q} - \mathbf{k} - \mathbf{K}, E_{ph})$$

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- Energy loss function** is already well studied

[e.g., Knapen, Kozaczuk, Lin — PRD 2021, 2101.08275; Hochberg et al. — PRL 2021, 2101.08263; Knapen, Kozaczuk, Lin — PRD 2022, 2104.12786]

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- No data yet** in the range of interest ($q \simeq 10 \text{ keV} - 100 \text{ keV}$)

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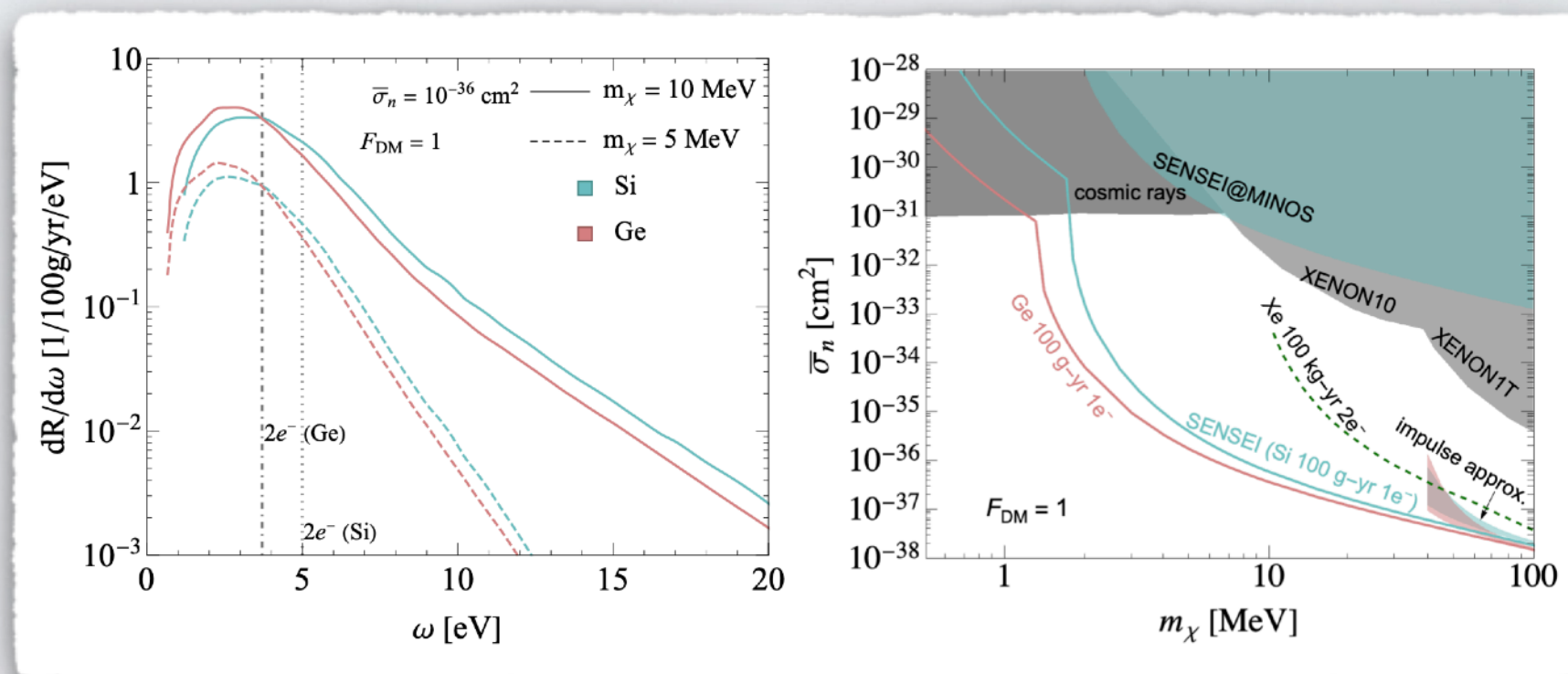
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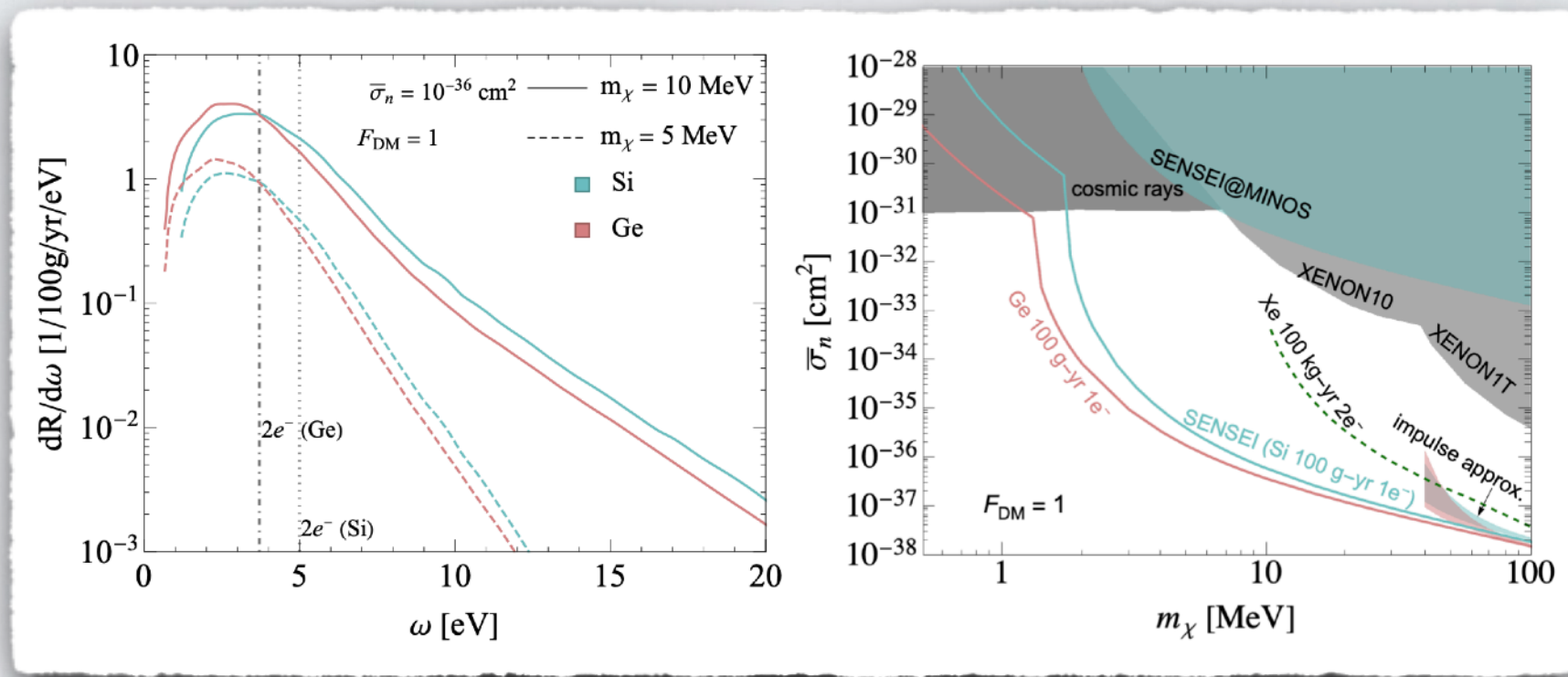


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- Description of Migdal effect in semiconductor extended to all masses

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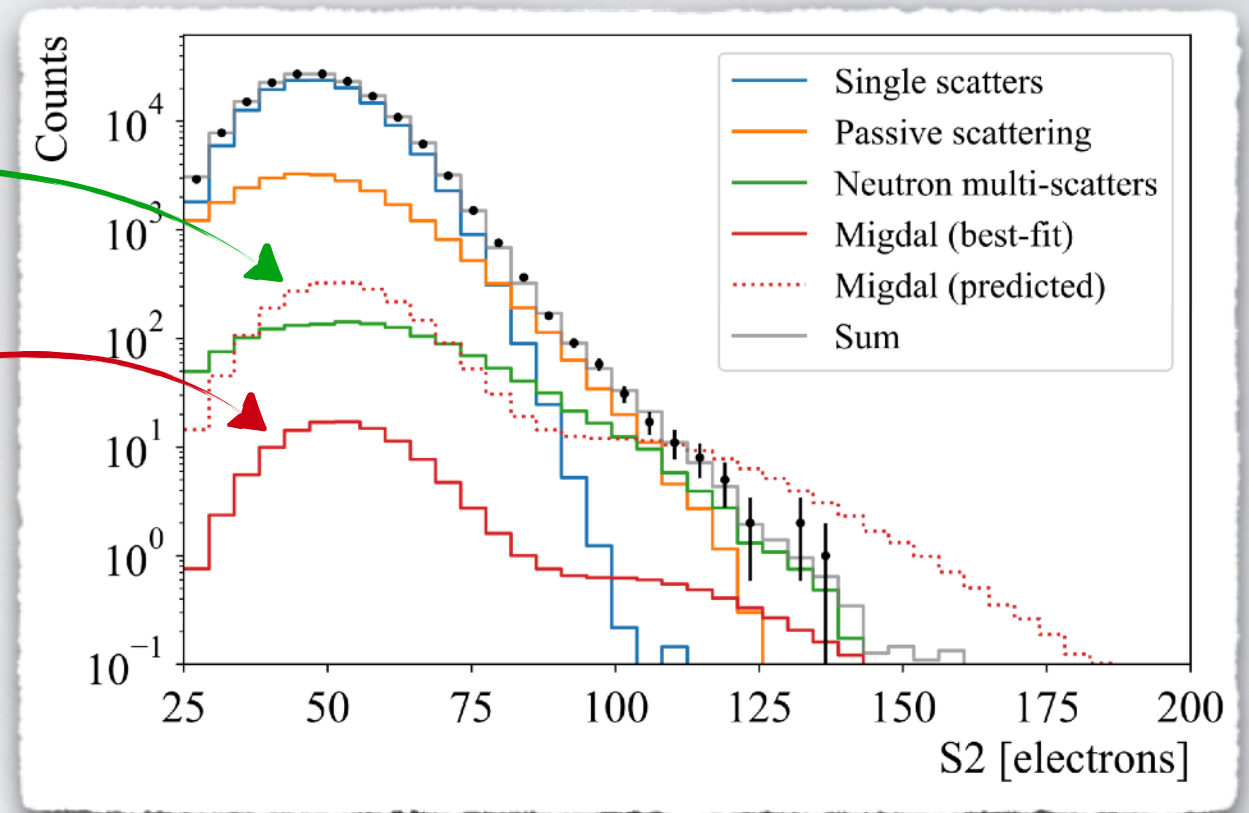
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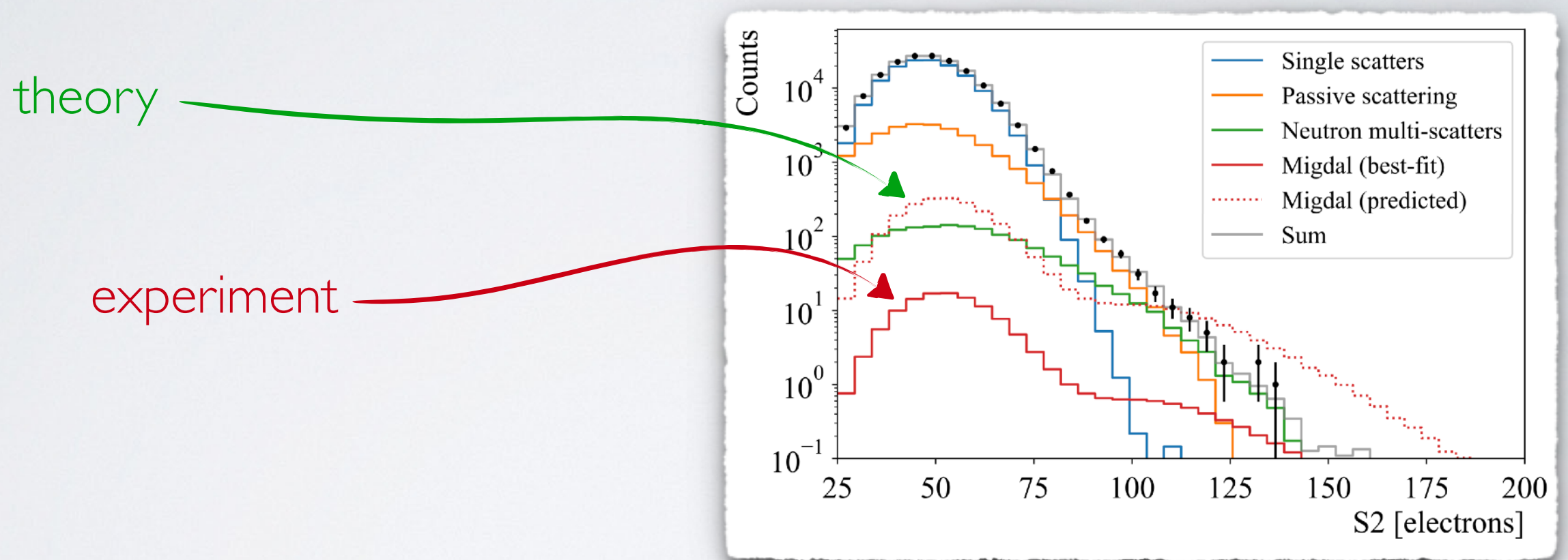
experiment



[Xu et al. - 2307.12952]

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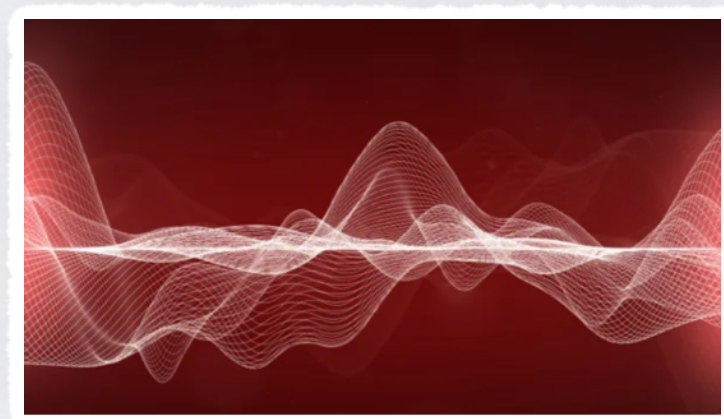


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- Theory assumes **free atoms** → could the difference be explained by **condensed matter effects?**

[work in progress w/ Grilli di Cortona]

Down to the keV collective excitations



COLLECTIVE EXCITATIONS

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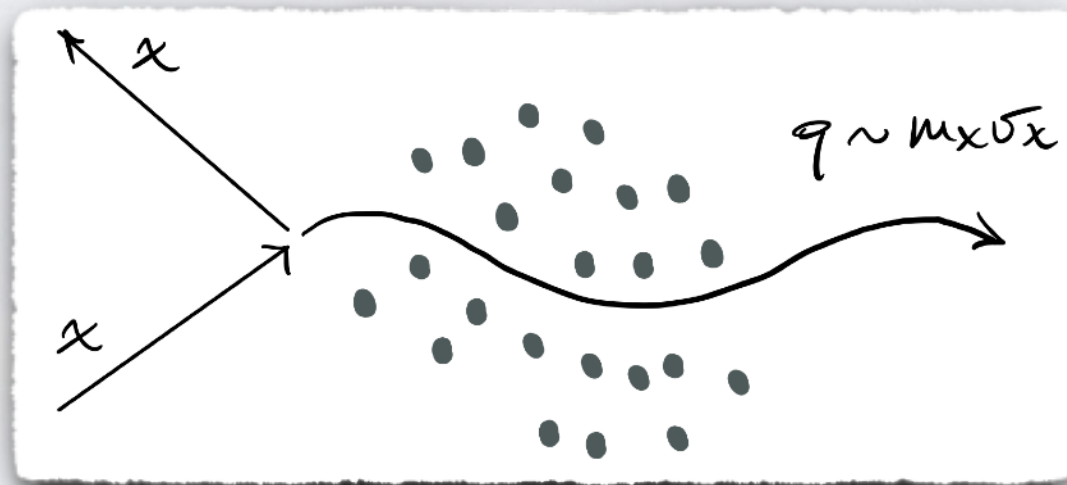
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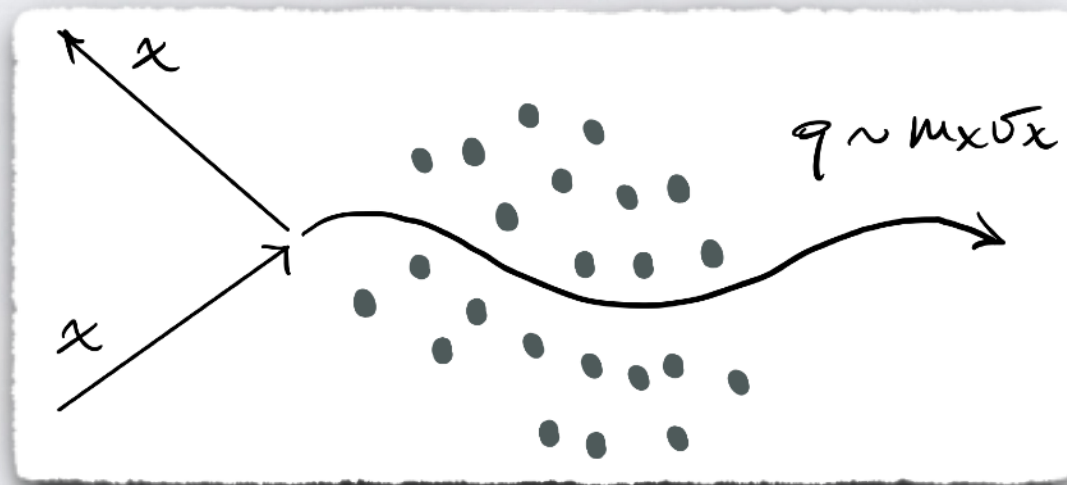


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- Typically, no more single particle final states $\rightarrow$ signatures involve collective excitation
- [see e.g., Trickle et al. – JHEP 2020, 1910.08092; Griffin et al. – PRD 2020, 1910.10716; Coskuner et al. – PRD 2022, 2102.09567]

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[e.g., Guo, McKinsey – PRD 2013, 1302.0534; Schutz, Zurek – PRL 2016, 1604.08206; Caputo, **AE**,
Polosa – PRD 2019, 1907.10635]

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3. Magnetic materials ($\text{Y}_3\text{Fe}_5\text{O}_{12}$, NiO, ...) → single- and multi-magnon

[e.g., Trickle, Zhang, Zurek – PRL 2020, 1905.13744; Trickle, Zhang, Zurek – PRD 2022, 2009.13534;
Mitridate, Trickle, Zhang, Zurek – PRD 2020, 2005.10256; **AE**, Pavaskar – PRD 2023, 2210.13516]

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[e.g., Guo, McKinsey – PRD 2013, 1302.0534; Schutz, Zurek – PRL 2016, 1604.08206; Caputo, **AE**,
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4. and more... [for a review, Kahn, Lin – Rept.Prog.Phys. 2022, 2108.03239]

COLLECTIVE EXCITATIONS

- A **growing field**, with many interesting ideas (a few on R&D):

1. Solid crystals (GaAs, SiO, ...) → multi-phonon

[e.g., Knapen et al. – PLB 2018, 1712.06598; Campbell-Deem et al. – PRD 2020, 1911.03482;
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(ANTI-)FERROMAGNETS

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(ANTI-)FERROMAGNETS

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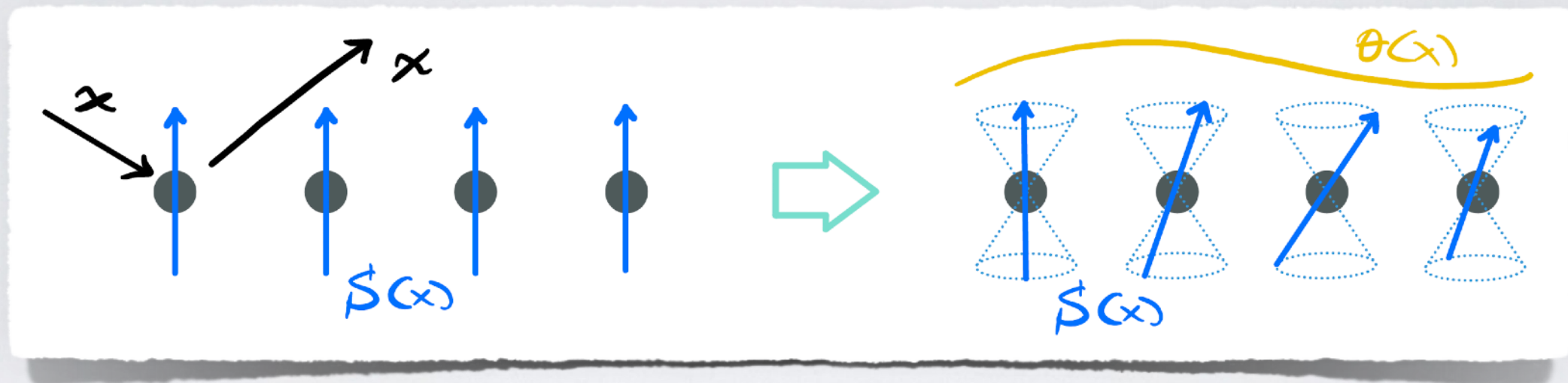
(anti-)ferromagnets

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- How can we probe spin-dependent interactions?

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- Interaction with spins excites a collective mode, called magnon

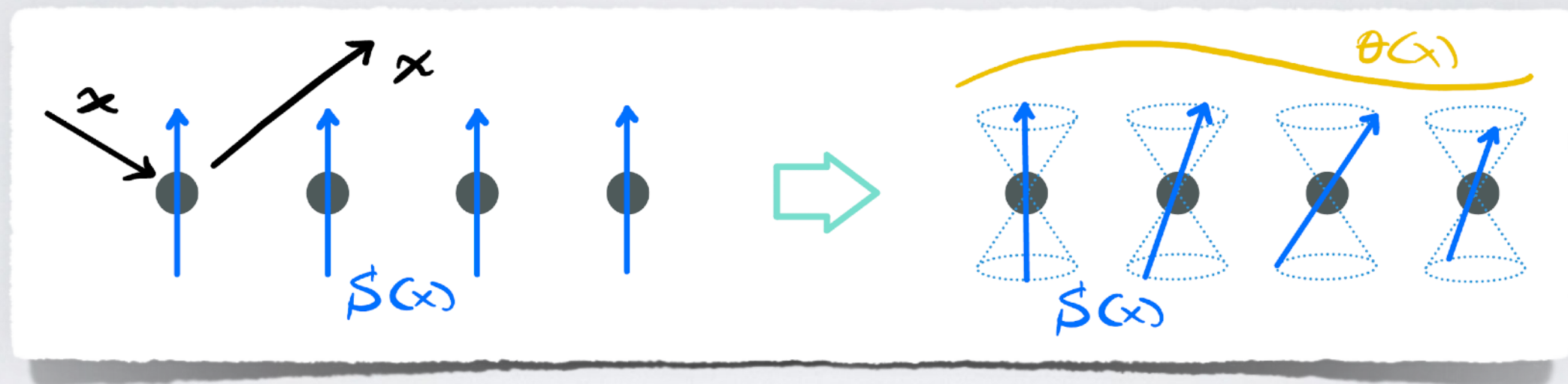


(ANTI-)FERROMAGNETS

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(anti-)ferromagnets

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- Ways to detect few magnons have been proposed and under work (TES, MKID, quantum sensors) [Trickle, Zhang, Zurek – PRL 2020, 1905.13744; Lachance-Quirion et al. – Science Advances 2017; Lachance-Quirion et al. – Science 2020]

FERROMAGNETS

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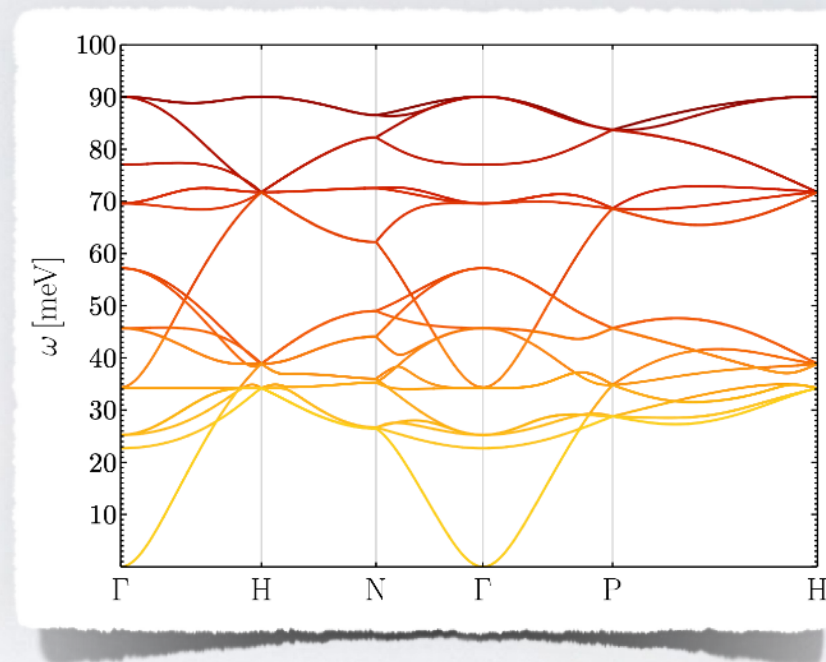
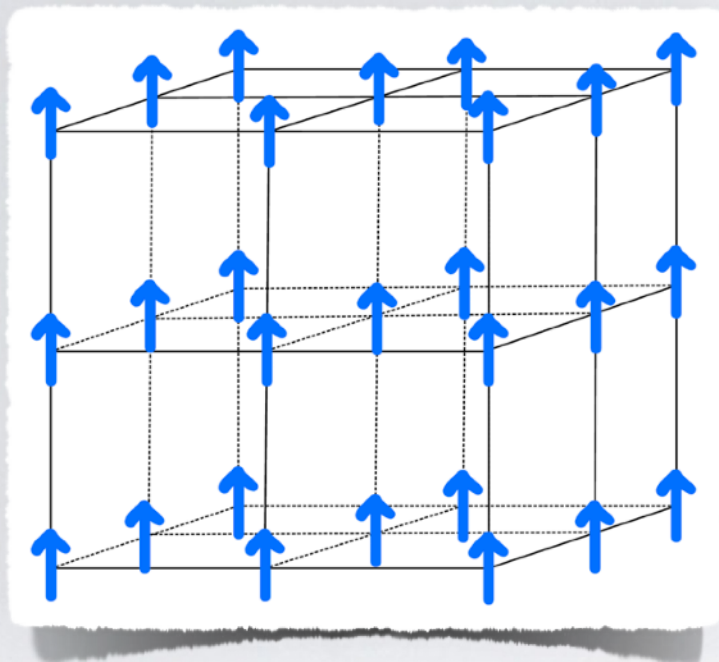
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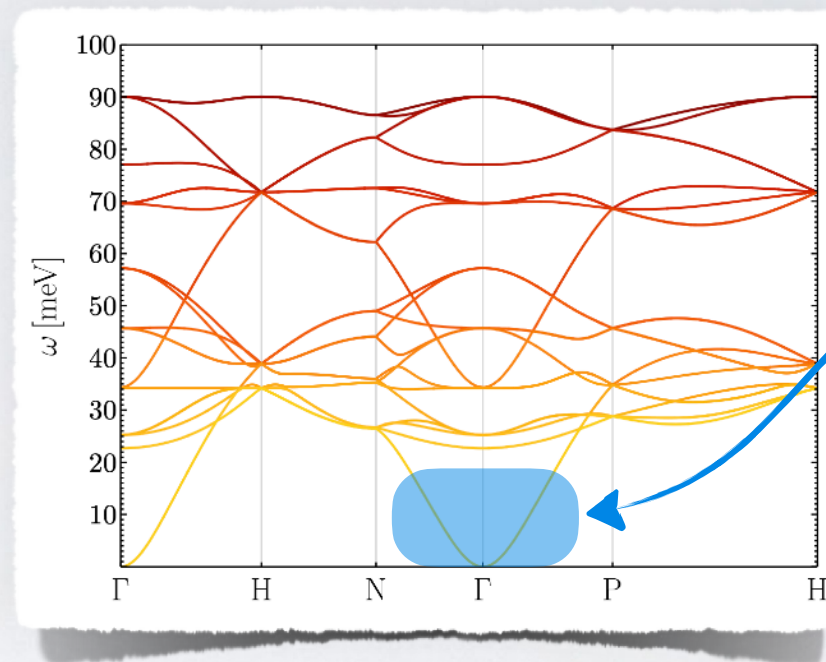
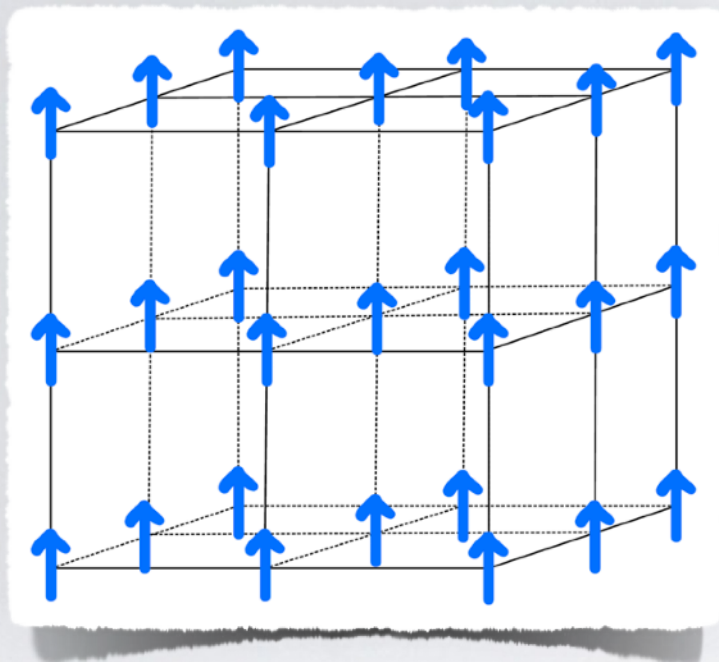
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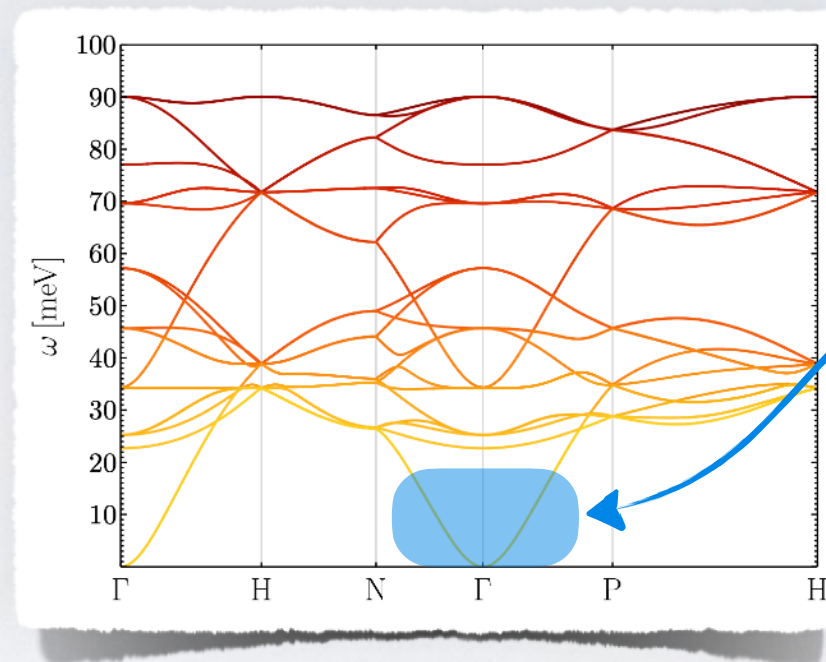
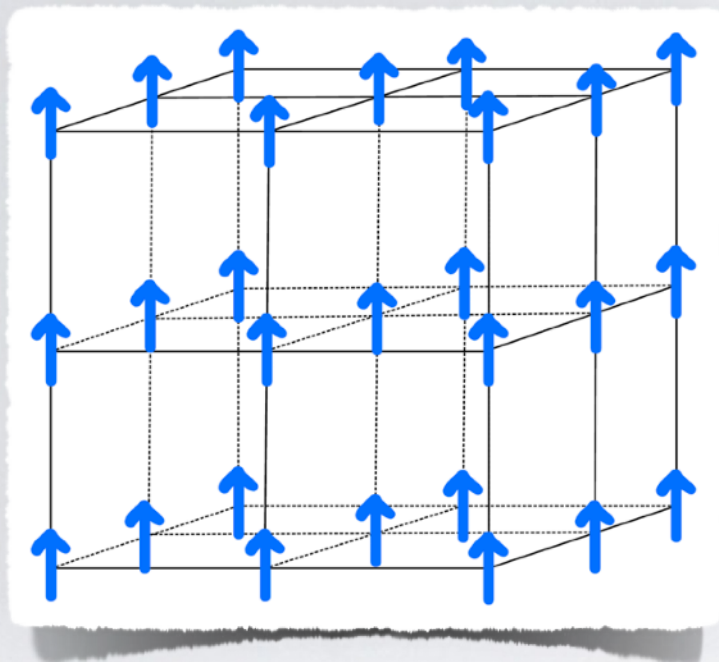


for $m_\chi \lesssim 10$ MeV only
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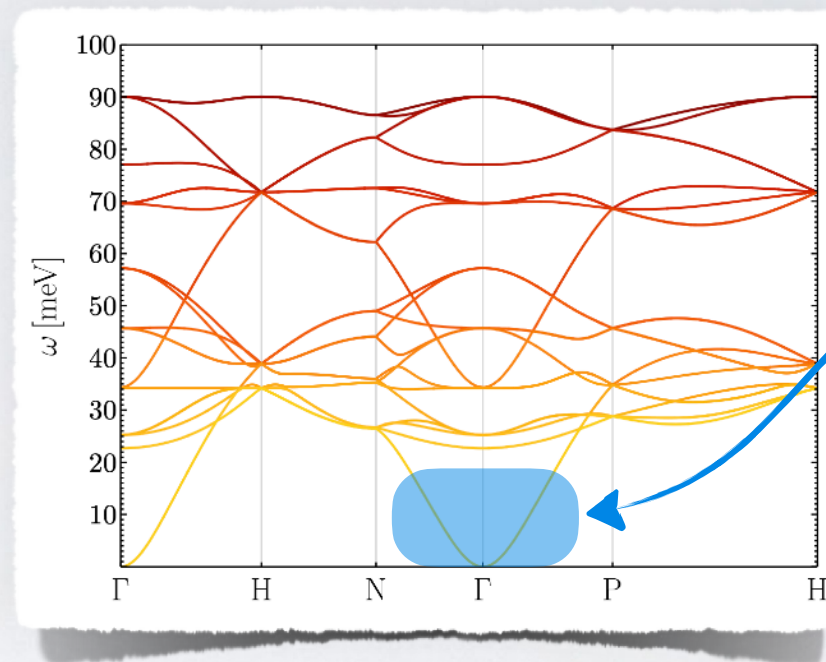
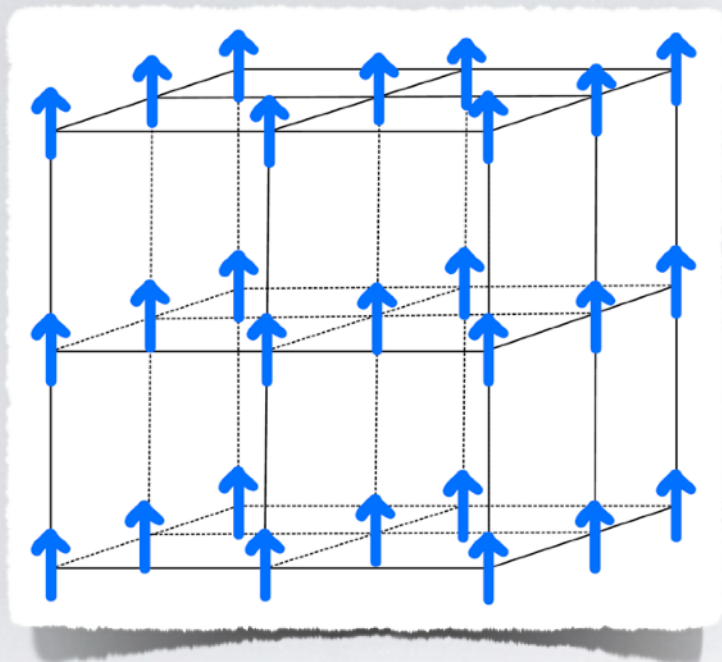


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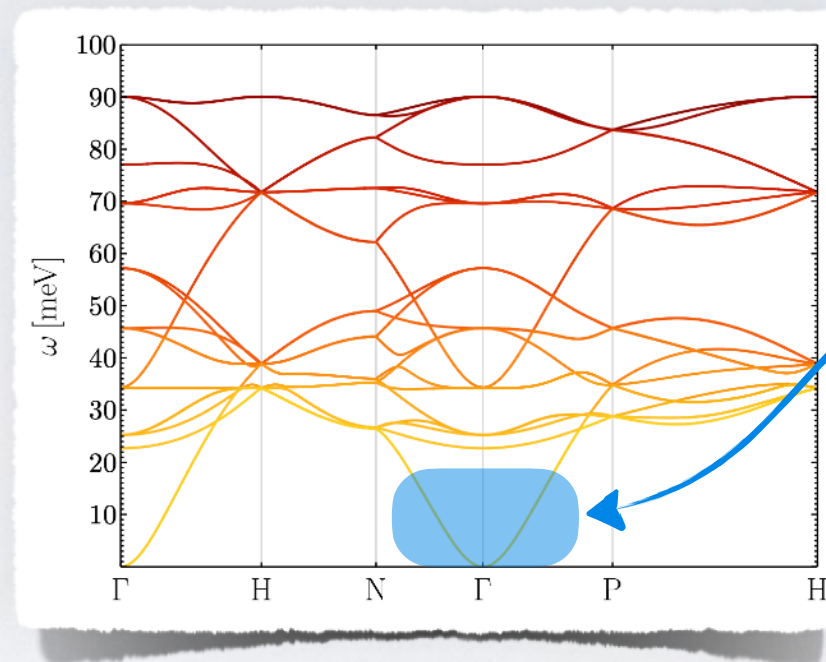
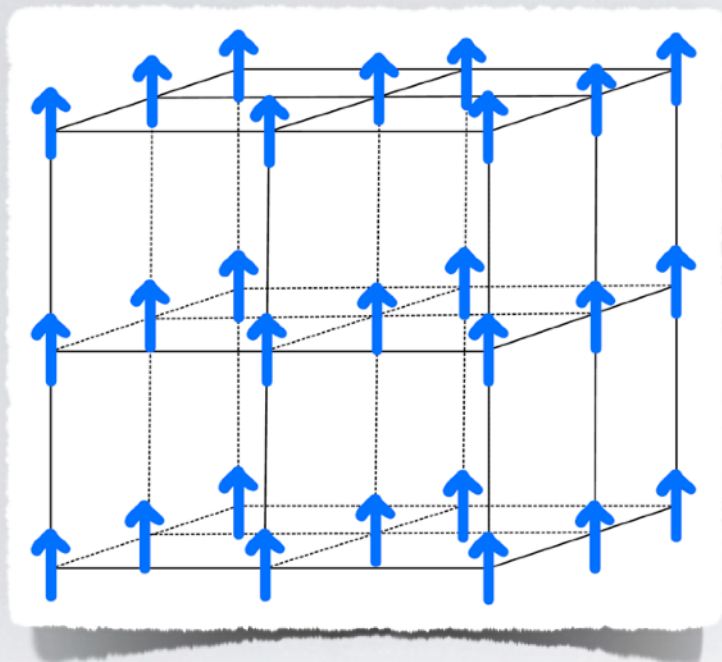
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FERROMAGNETS

FERROMAGNETS

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FERROMAGNETS

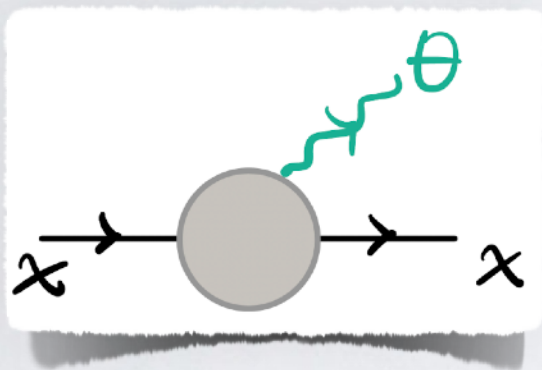
- Compute the magnon emission rate
- Traditional approach: quantize the Heisenberg model

$$H = \frac{1}{2} \sum_{\ell, \ell'}^N \sum_{j, j'}^n J_{\ell \ell' j j'} \mathbf{S}_{\ell j} \cdot \mathbf{S}_{\ell' j'} \rightarrow \sum_{\nu=1}^n \sum_{\mathbf{q} \in 1BZ} \omega_{\nu, \mathbf{q}} b_{\nu, \mathbf{q}}^{\dagger} b_{\nu, \mathbf{q}}$$

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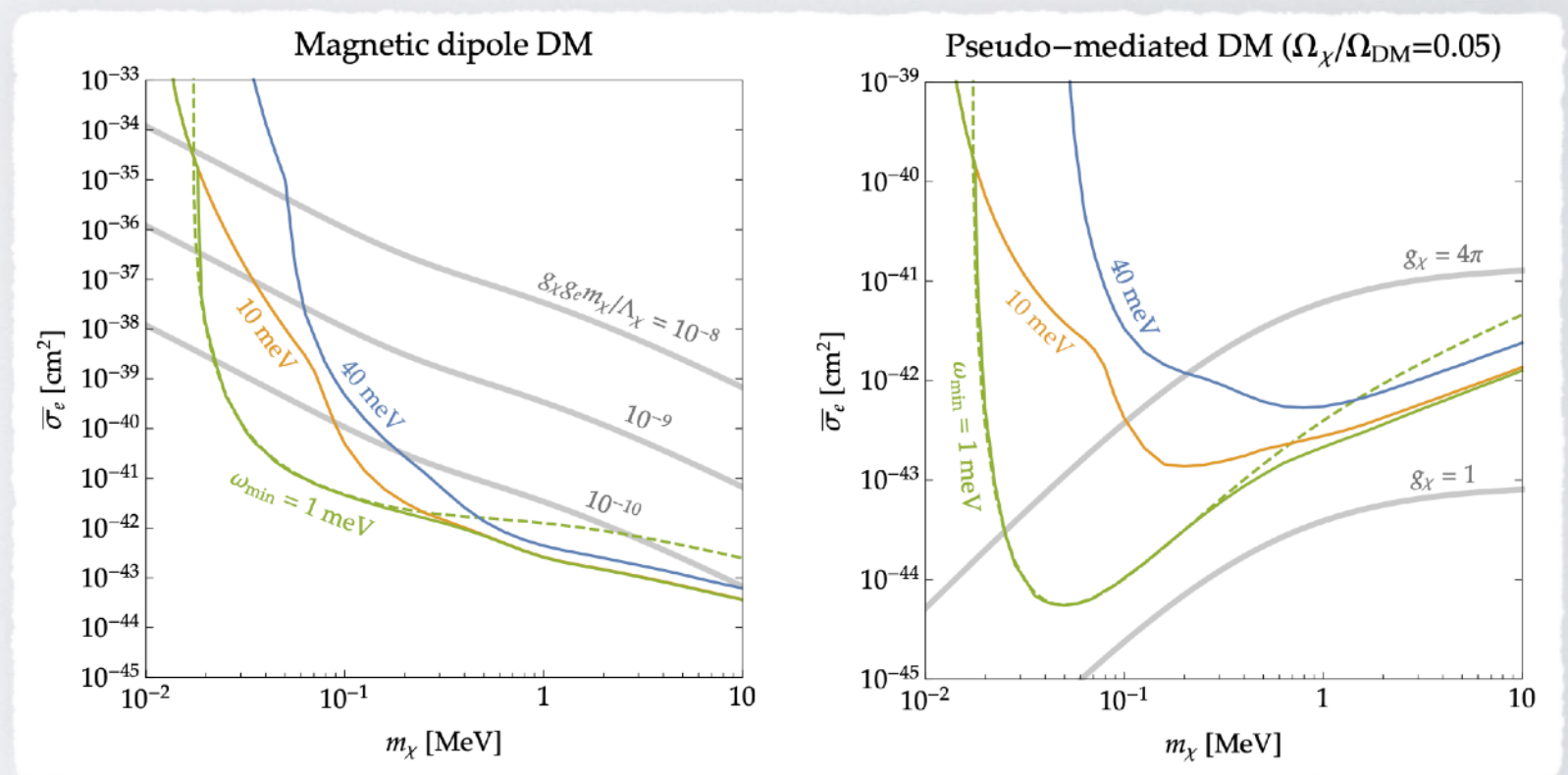
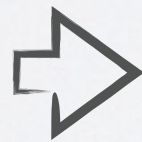
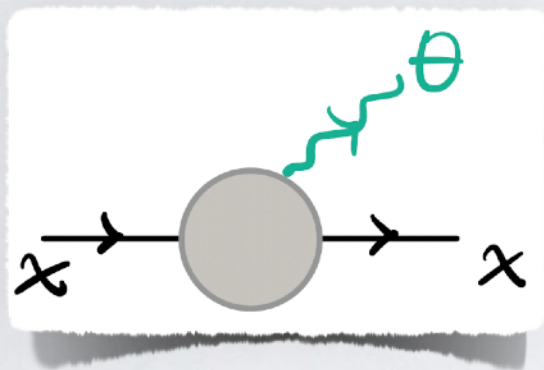
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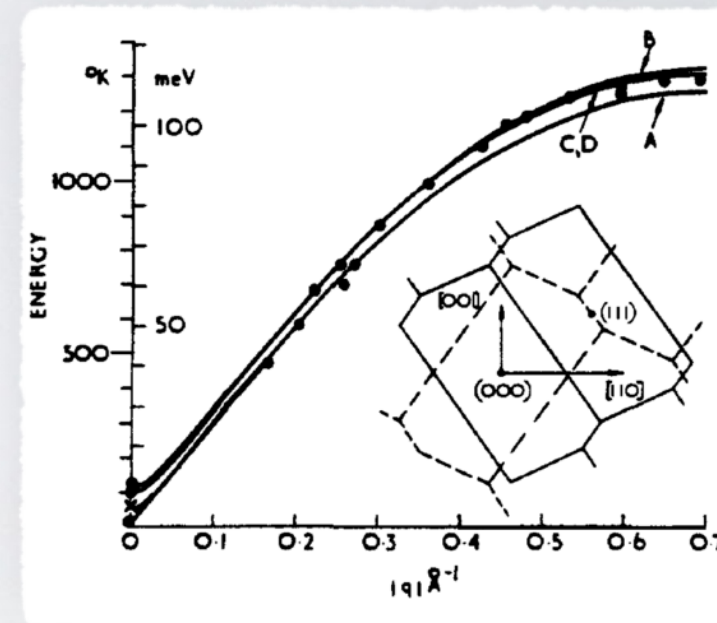
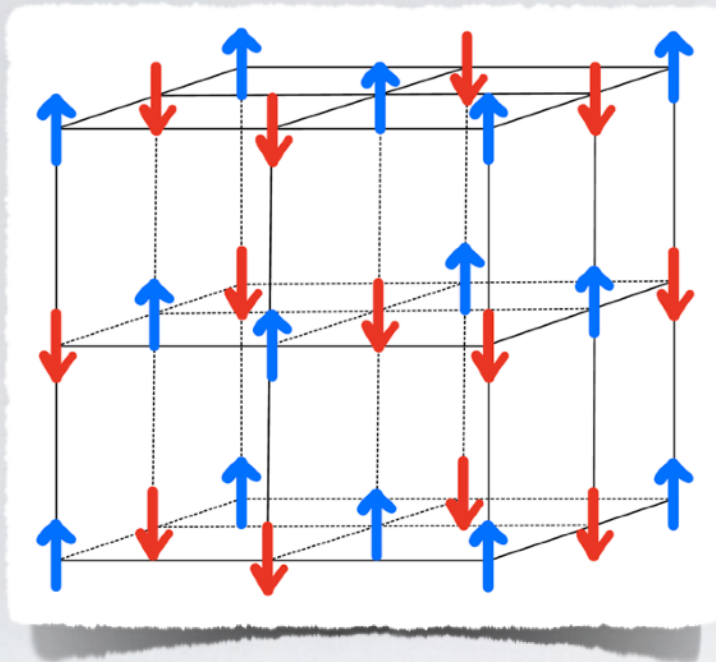
ANTI-FERROMAGNETS

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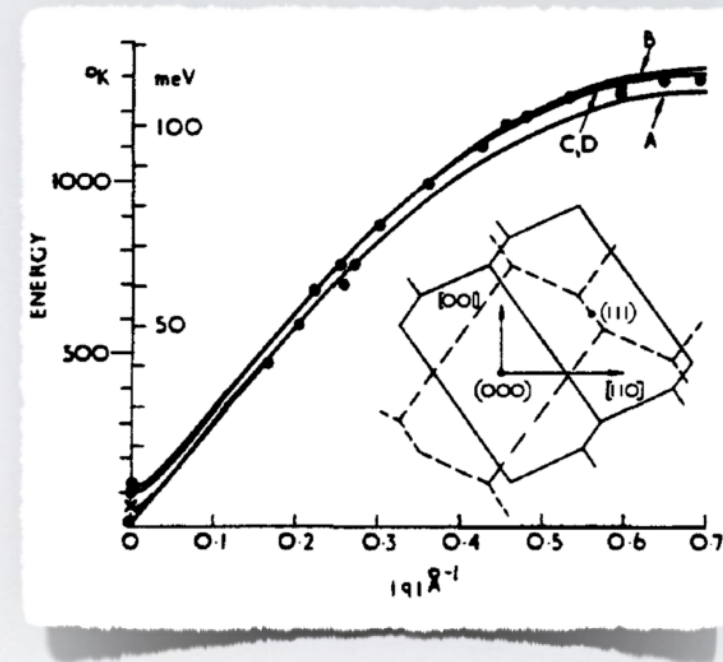
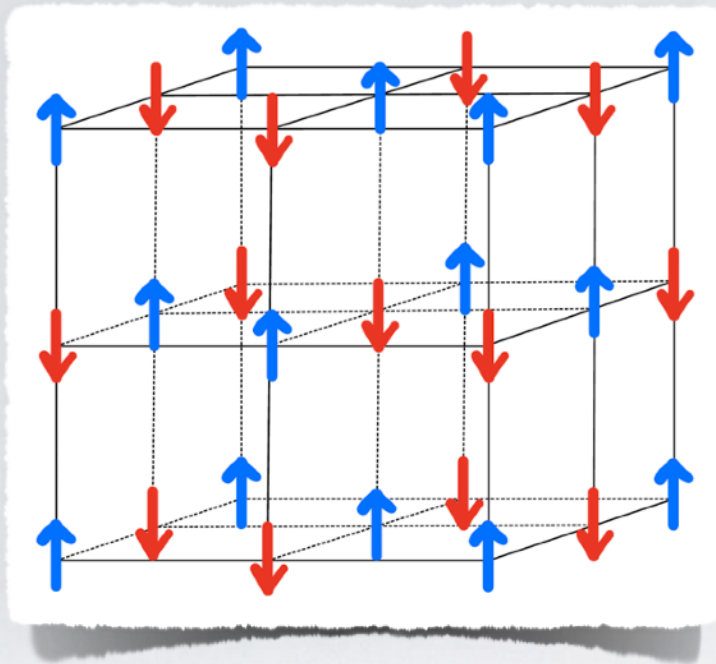
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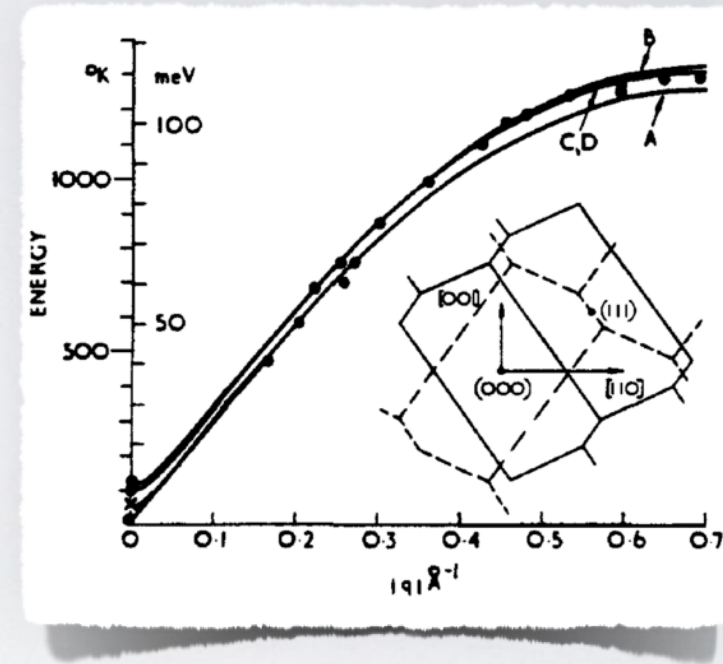
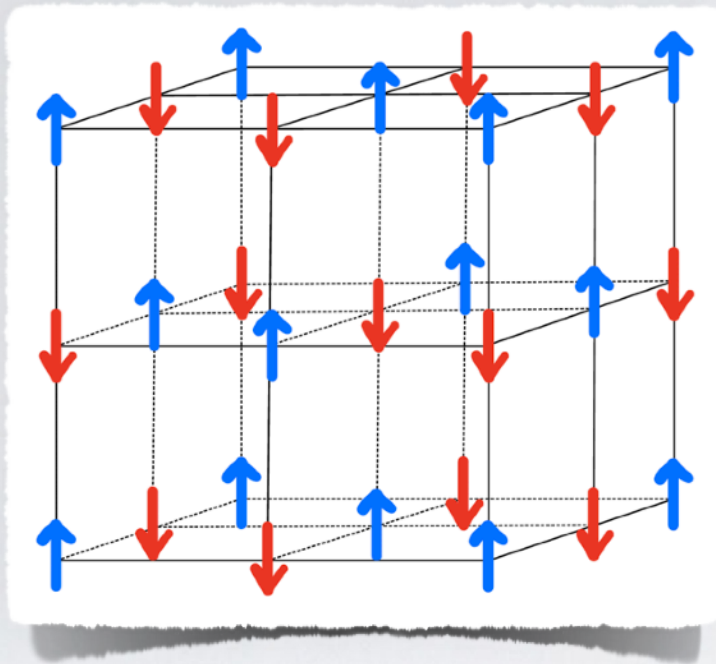
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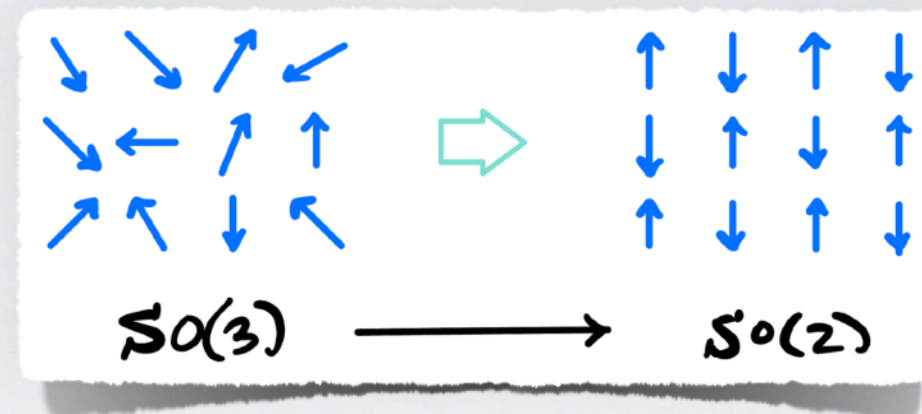


- Can always emit more than one magnon → multi-magnon emission allow to probe down to $m_\chi \sim 1$ keV
- Nickel-oxide has $\nu_\theta \simeq \nu_\chi$ → very efficient at absorbing dark matter energy [AE, Pavaskar – PRD (2023), 2210.13516]

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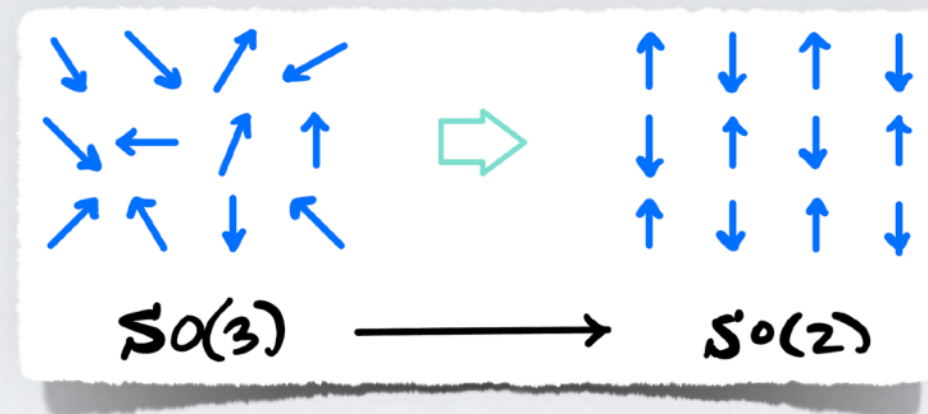
ANTI-FERROMAGNETS

- Anti-ferromagnet spontaneously break internal spin symmetry



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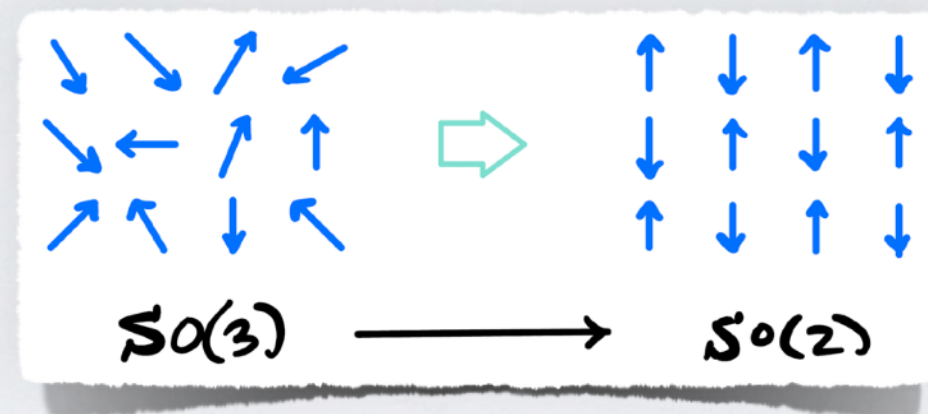
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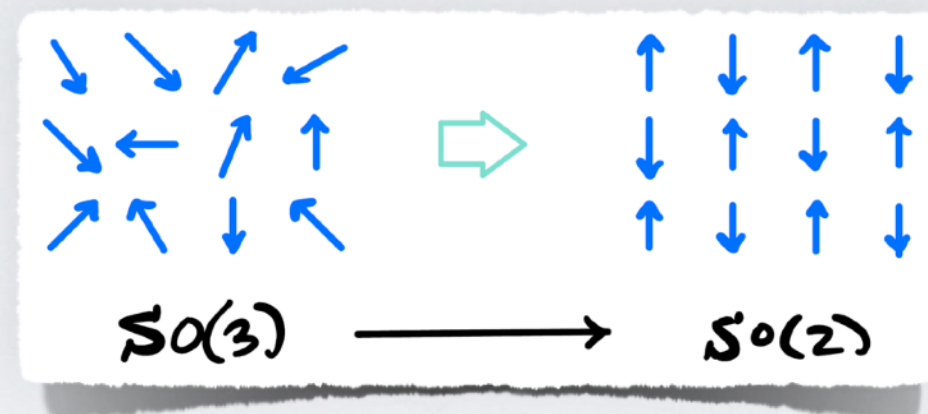


Write a low energy EFT: $\mathcal{L}_{EFT} = \frac{c_1}{2} \dot{\mathbf{n}}^2 - \frac{c_2}{2} (\partial_i \mathbf{n})^2$

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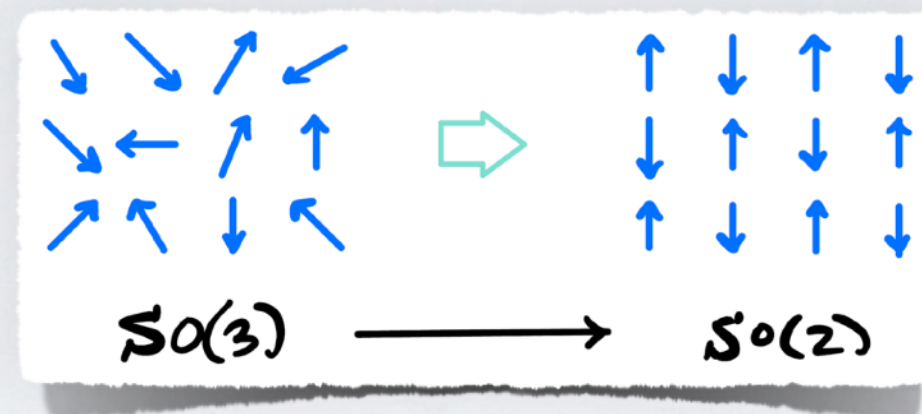
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Bypass standard difficulties in computing multi-magnon processes

[Dyson – Phys. Rev. 1956]

ANTI-FERROMAGNETS

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- With an EFT at hand → use standard QFT methods to compute event rates

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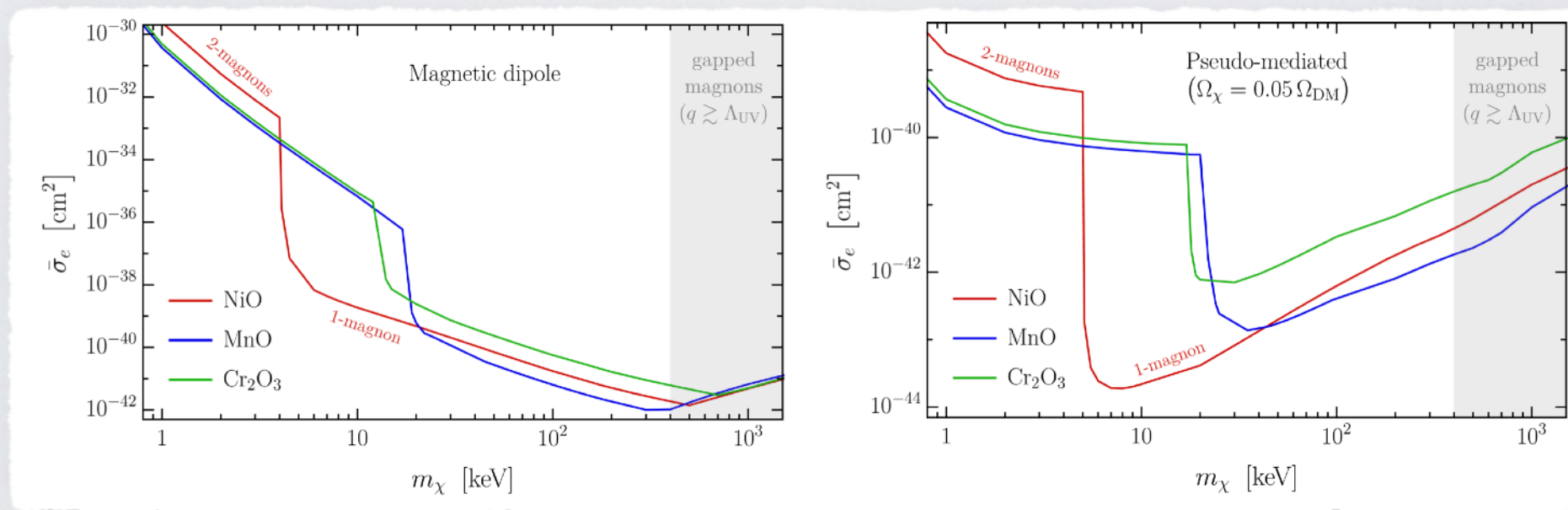
$$\begin{aligned}
 \text{Diagram 1: } & \begin{array}{c} a, \lambda_1 \\ \uparrow \\ s \rightarrow \bullet \rightarrow s' \end{array} = -\frac{g_\chi g_e \sqrt{c_1}}{m_e} \omega \times \begin{cases} \frac{4}{\Lambda_\chi} P_{ia}(\mathbf{q}) \sigma^i & \text{m.d.} \\ q^a/q^2 & \text{p.m.} \end{cases} \\
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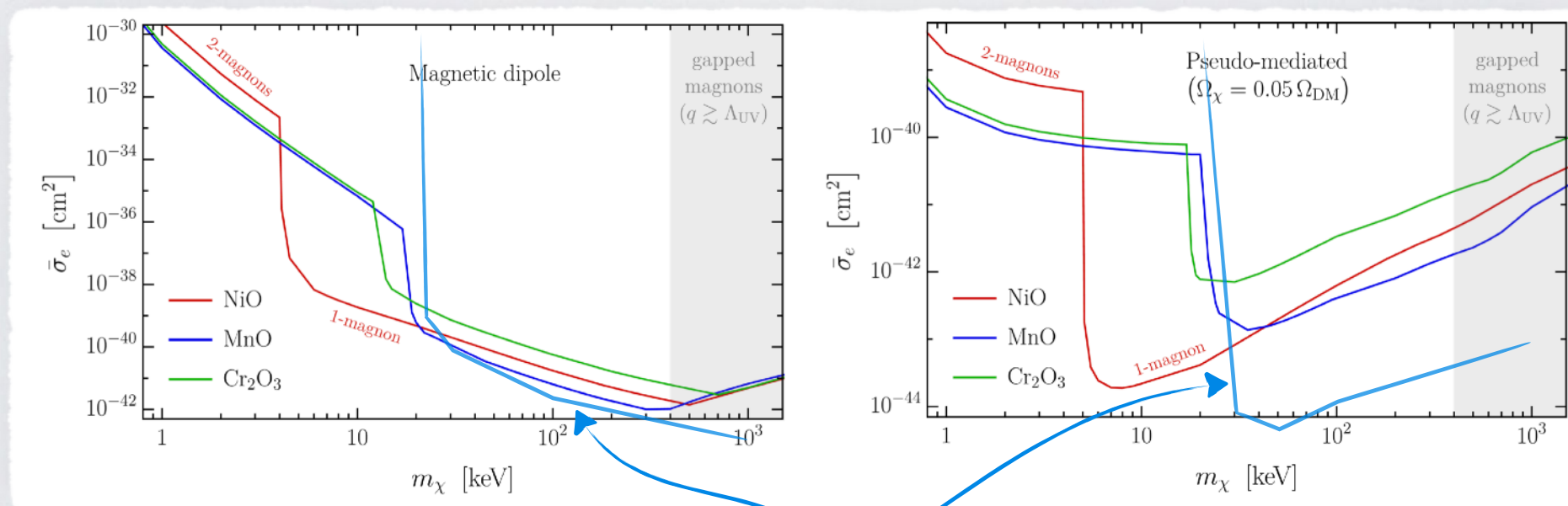


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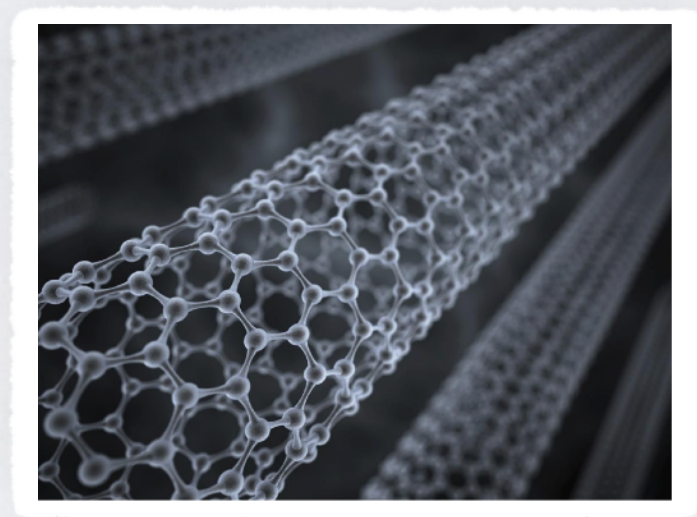
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ferromagnets

Honorable mention: carbon nanotubes



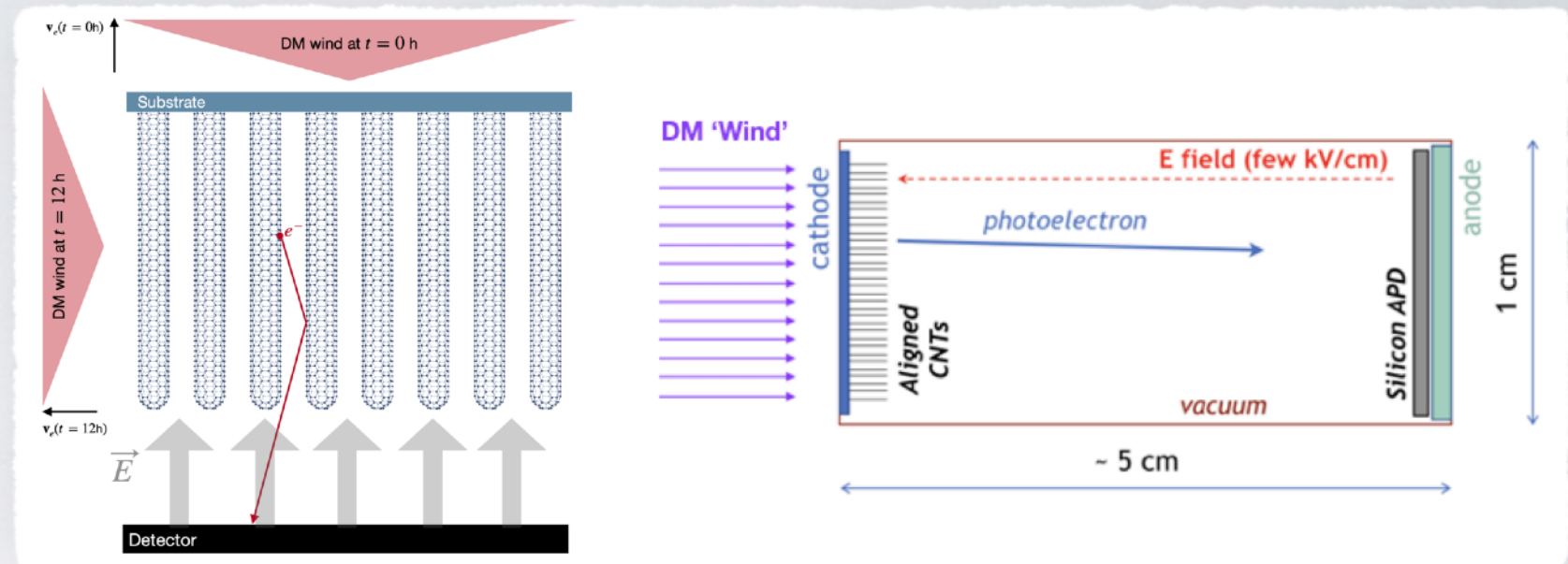
CARBON NANOTUBES

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- Another promising proposal for sub-GeV dark matter searches are

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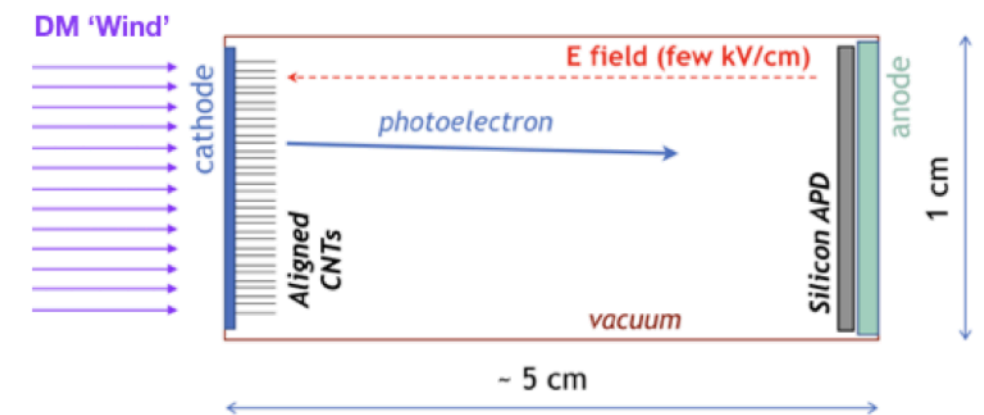
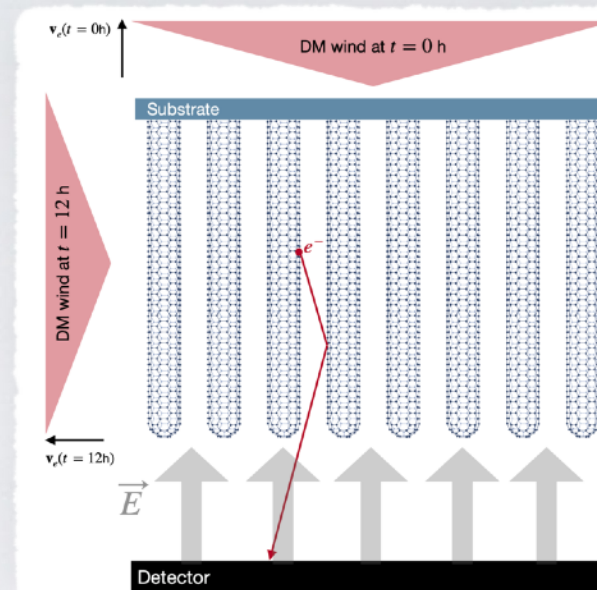


CARBON NANOTUBES

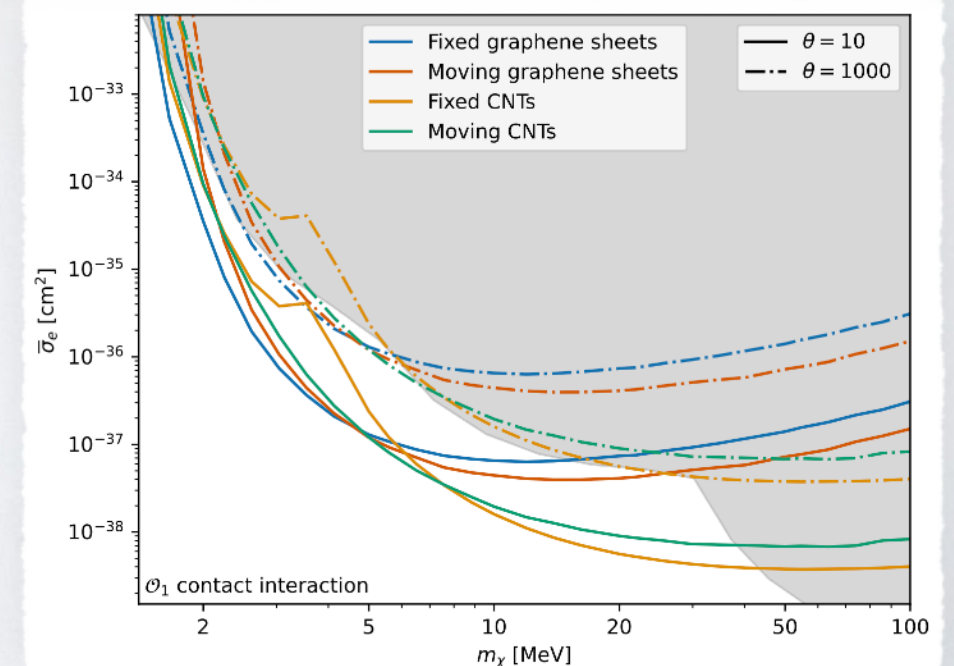
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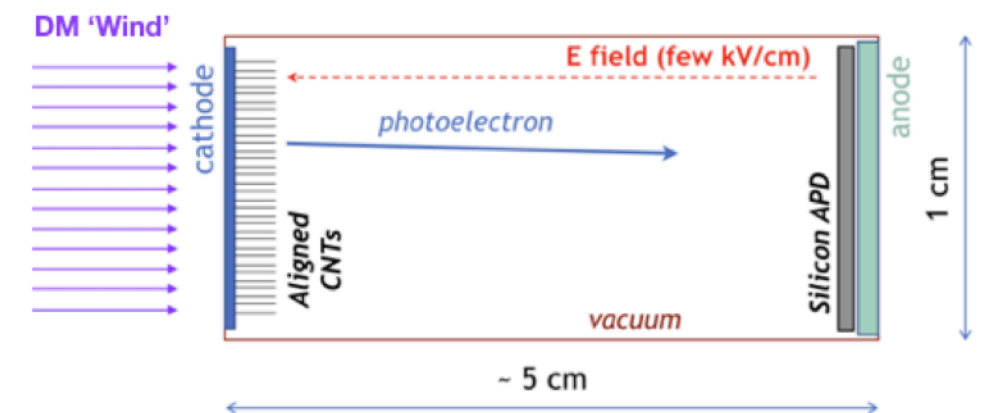
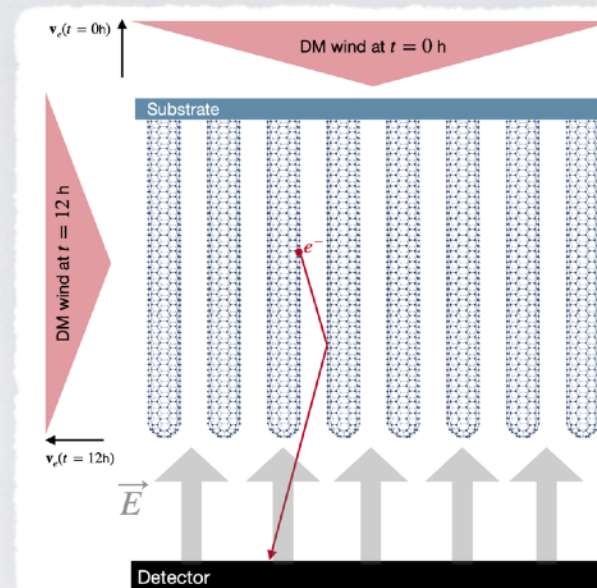


CARBON NANOTUBES

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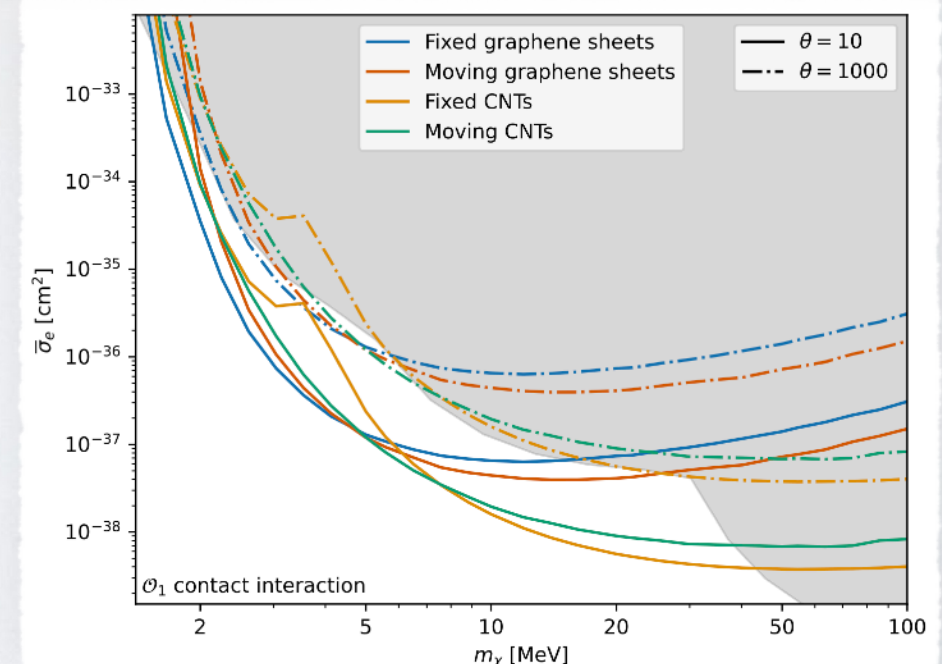
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- Promising probe of DM-electron interactions down to $m_\chi \sim \mathcal{O}(\text{MeV})$
- Might be a good probe for DM-nucleon interactions as well

[Cavoto, AE, Pandolfi, Papiri, Polosa, Tarquini – work in progress]



OUTLOOK

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Thank you for the attention!