

Forbidden Conformal DM

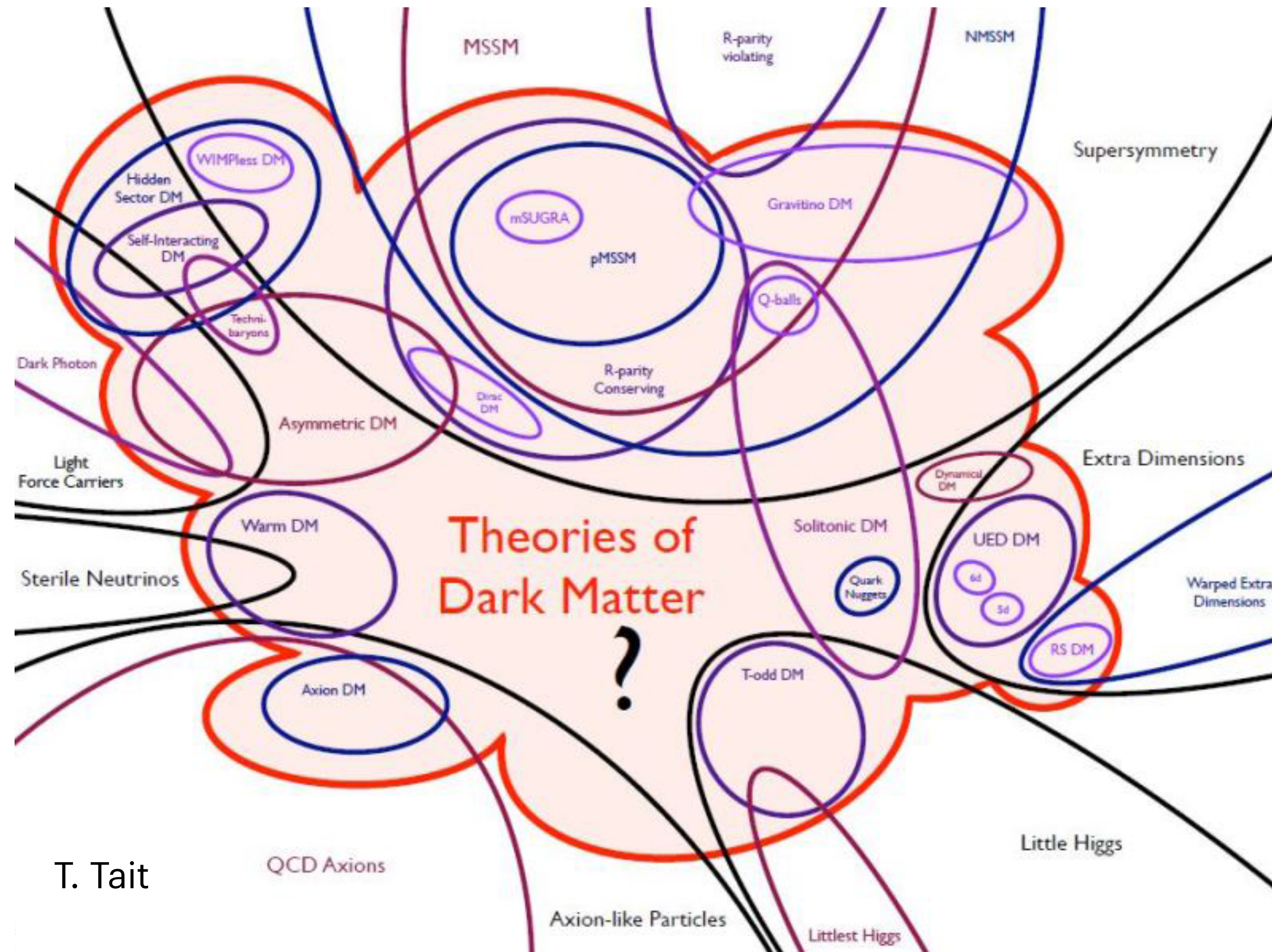


Seung J. Lee



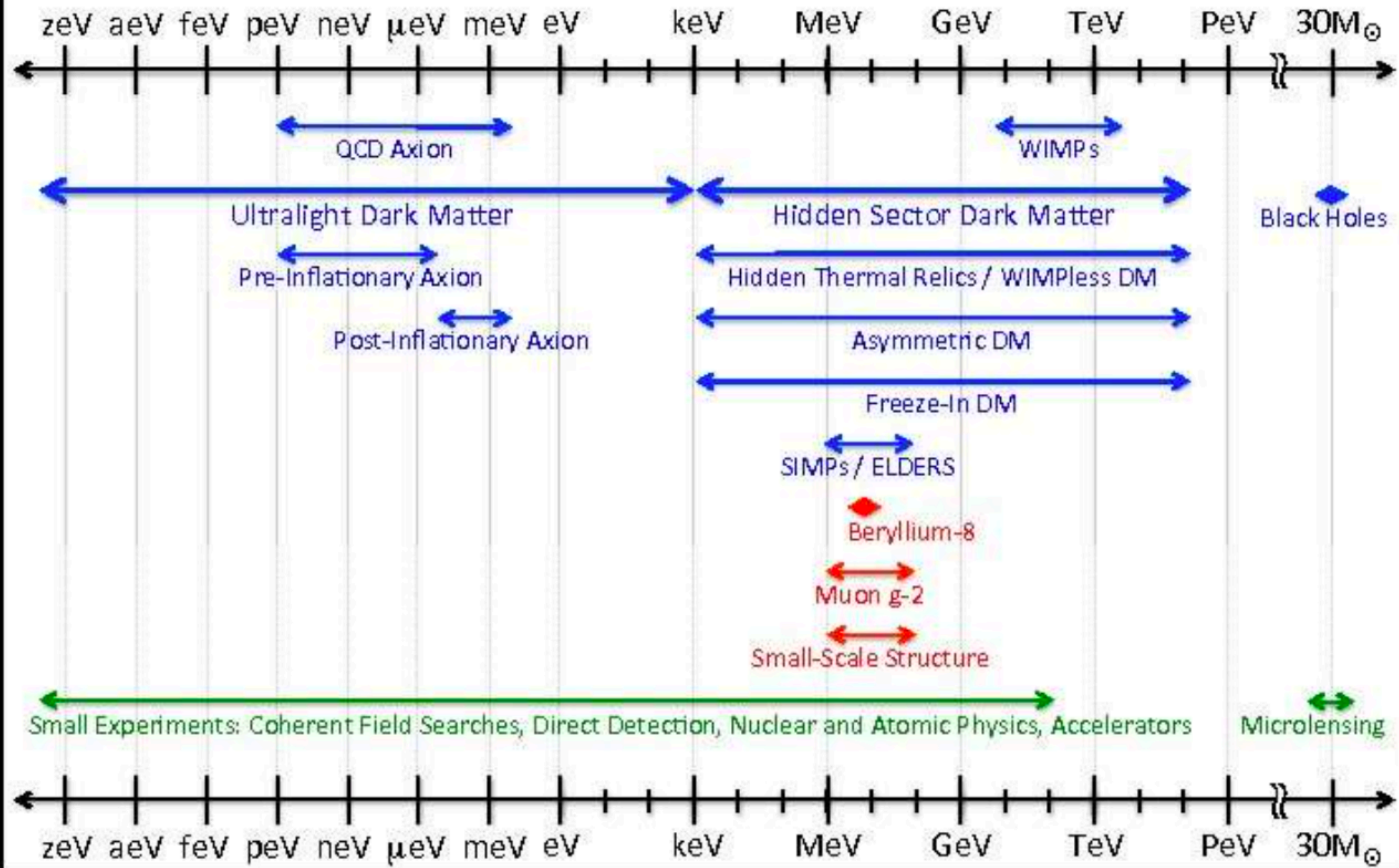
in collaboration with Steven Ferrante, Ameen Ismail and Yunha Lee

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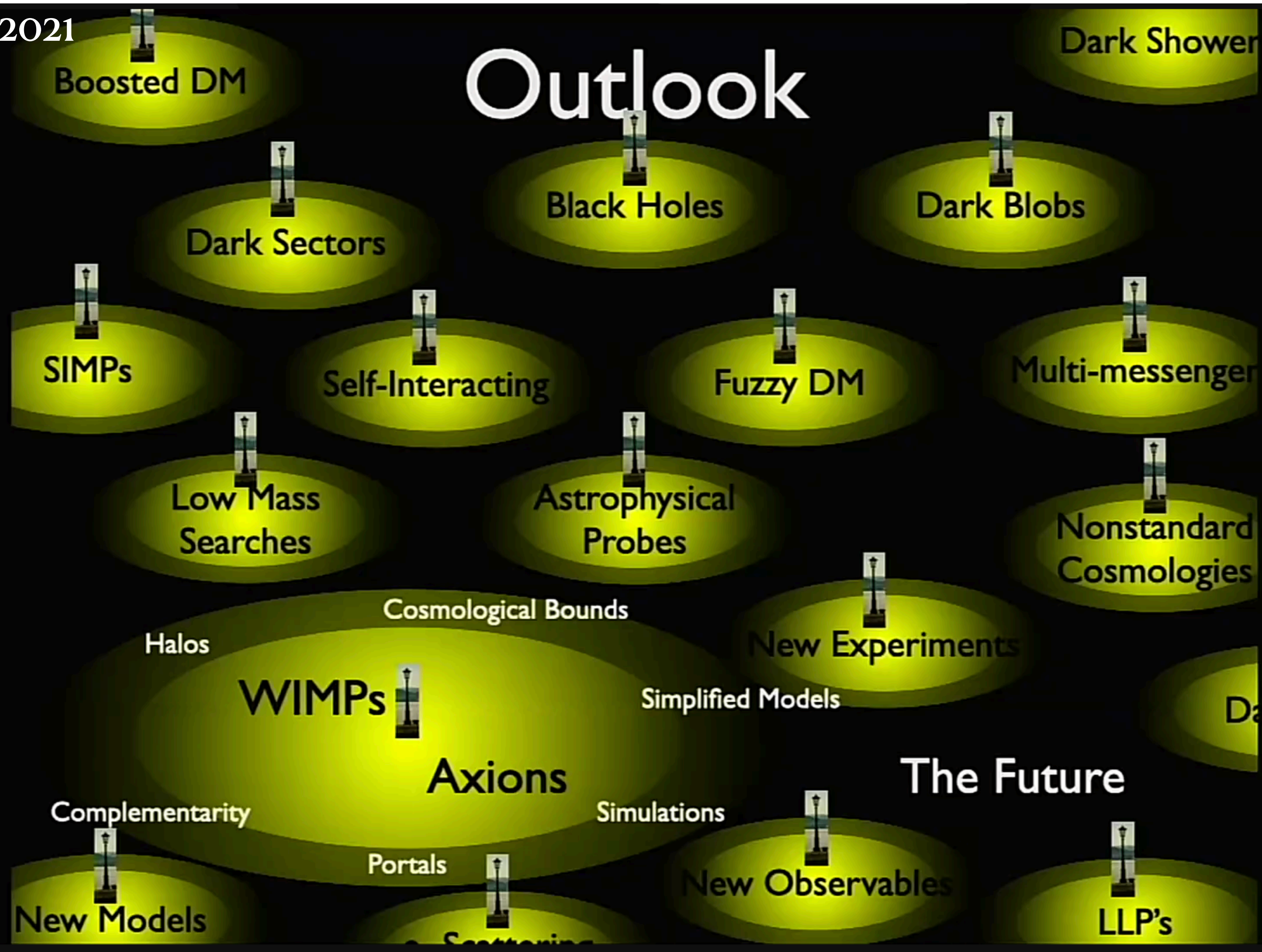
T. Tait

Dark Sector Candidates, Anomalies, and Search Techniques



Tim Tait 2021

Outlook

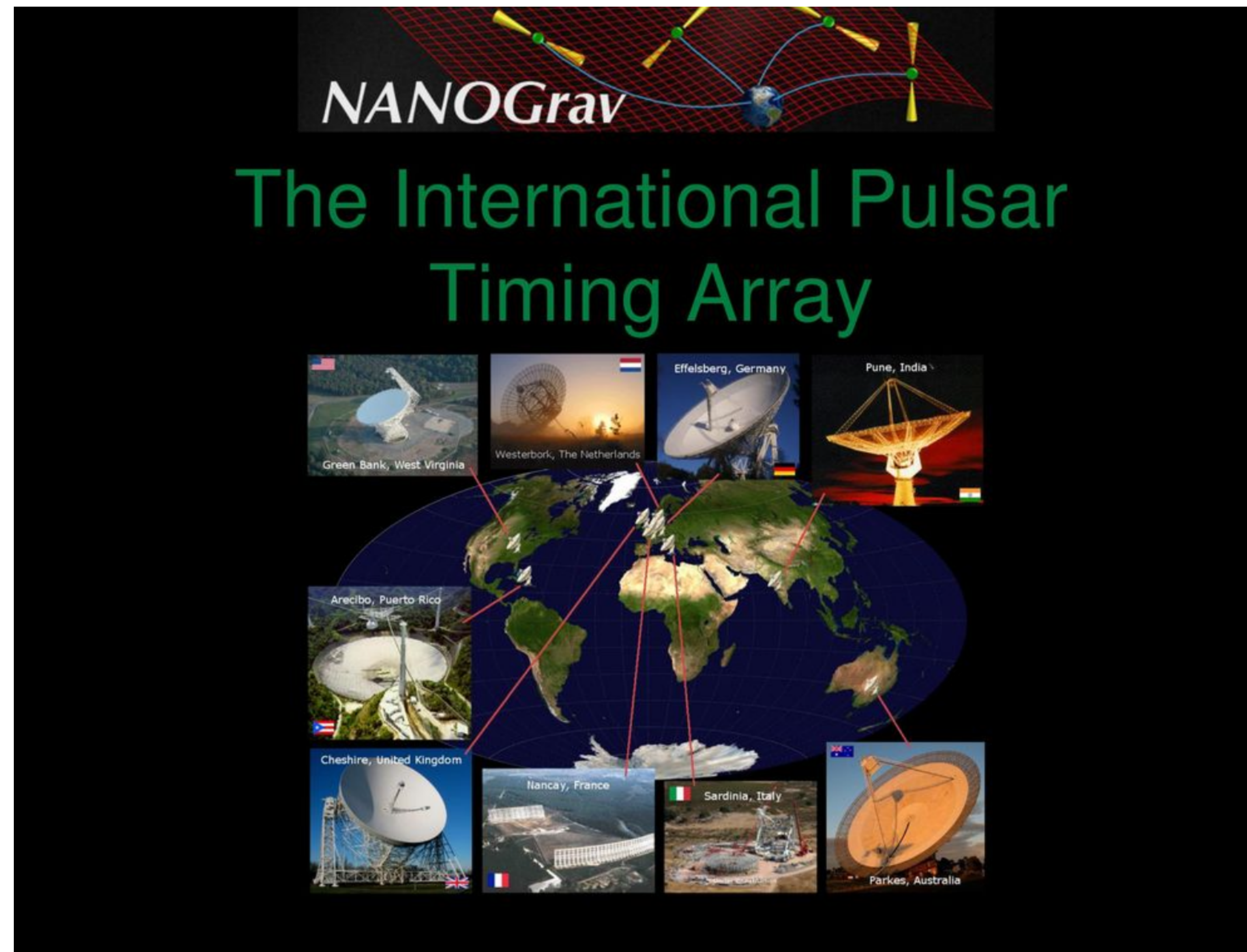


Beyond WIMP, so many new ways to probe possible DM, But mostly for (ultra)light DM

- ④ Table Top experiments (nuclear or electron scatteribg/absorption) for direct detection
- ④ Cavity experiments for axion like particles, Beam Dump Experiments, Quantum Sensing (atomic physics)
- ④ Cosmological Probes (indirect, CMB, star cooling, LSST,...)
- ④ At colliders (including facilities for LLP such as FASER II, SHiP,...) See Jamie Boyd's talk this afternoon
- ④ etc

Dark Matter: where are we?

- maybe another way to look at DM: Stochastic Gravitational Wave at a nanoHertz scale



See Kai Schmitz's talk this afternoon

Dark Matter: where are we?

- maybe another way to look at DM
Gravitational Wave at a nanoHertz

Apart from astrophysical
explanation:

- cosmic inflation
- first-order phase transitions
- topological defects



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Why Conformal DM?

Bai, Careba, Lykken 09'

Agashe, Blum, SL, Perez 09'

Blum, Cliche, Csaki, SL 14'

Efrati, Kuflik, Nussinov, Soreq , Volansky 14'

Fuks, Goodsel, Kang, Ko, SL, Utsch 20'

- Explicit scale for DM is add-hoc, unless well motivated:

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WIMP - solving Hierarchy Problem for EWSB or

QCD Axion- Peccei-Quinn scale for solving strong CP problem

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- Model-building: **AdS/CFT** allows explicit calculation for large N CFT

Dialton Portal Conformal DM

Bai, Careba, Lykken 09'

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- Embedding the SM partially or completely in a composite sector can solve the hierarchy problem, by making the Higgs boson composite. **DM is a composite of the conformal sector** and the SM fields are taken to be elementary

Dialton Portal **Conformal** DM

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- If the breaking of scale invariance is spontaneous, then it is accompanied by a **dilaton** (corresponding GB) that couples to the fields in the composite sector through

$$-\frac{\sigma}{f}\text{Tr}T$$

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- If the breaking of scale invariance is spontaneous, then it is accompanied by a **dilaton** (corresponding GB) that couples to the fields in the composite sector through
$$-\frac{\sigma}{f}\text{Tr}T$$
- Conformal phase transition can be 1st order phase transition- GW signals

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- For massive particles, coupling to dilaton is proportional to $\sim M/f$
 1. A very economic way to couple the SM to the dark sector (singlet under SM gauge symmetry)
 2. DM coupling to SM resembles Higgs portal, but with an extra suppression of order $(v/f)^2 (m_h/m_\sigma)^4$
- In the minimal set-up, basically three parameters determine the dynamics of thermal freeze-out in the early universe: f, m_{DM}, m_σ (all three around 1-10 TeV)

Forbidden Conformal DM at a GeV

0.1 - 10 GeV

- a model of thermal **GeV-scale DM** from a dark sector with spontaneously broken conformal symmetry
- DM is a composite of the conformal sector and the SM fields are taken to be elementary
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-
- ✓ A GeV scale DM that gives a **stochastic GW** consistent w/ NANOGrav,
 - ✓ A signal with future **Direct Detection** experiments
 - ✓ A signal with future searches for **Long Lived Particles** such as FASER II and SHiP

Why “Forbidden DM” at a GeV?

Ferrante, Ismail and SL, Lee. 23'

- The dark sector must contain a dilaton field σ , the Goldstone boson of broken scale invariance, so one might minimally consider a model where the dilaton is the DM $\boxed{-\frac{\sigma}{f}\text{Tr}T}$
 - Dilaton has couplings to the light SM fermions  dilaton to decay to e^+e^- pairs, ruling out the dilaton as the DM unless its lifetime is larger than about 10^{25} s


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- What if Λ_{CFT} sufficiently high? feeble interaction means one can still have conformal freeze-in scenario; but no GW signals 😞
 - An observable stochastic gravitational wave background is only generated if the dark sector temperature is comparable to or larger than the visible sector temperature.

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- So we need to do something slightly less minimal: adding composite DM field + dilaton

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- A minimal model with composite GeV DM (ϕ) + dilaton (σ):
 - What **mechanism** can set the relic abundance of ϕ ? The simplest option: ϕ to be a canonical WIMP that **freezes out** through $2 \rightarrow 2$, via dilaton-portal.
 - But, @ $T \simeq m_\phi$, $\langle \sigma v \rangle \sim m_\phi^2 / \Lambda^4 \rightarrow \langle \sigma v \rangle \sim (10^3 \text{ TeV})^{-2}$ with $m_\phi \sim \text{GeV}$ & $\Lambda \sim \text{TeV}$
c.f. what we need is $\langle \sigma v \rangle \sim (20 \text{ TeV})^{-2}$

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Why don't we just lower cutoff scale? i.e. setting $\Lambda \sim \mathcal{O}(100) \text{ GeV}$? \rightarrow **direct detection rules it out!**

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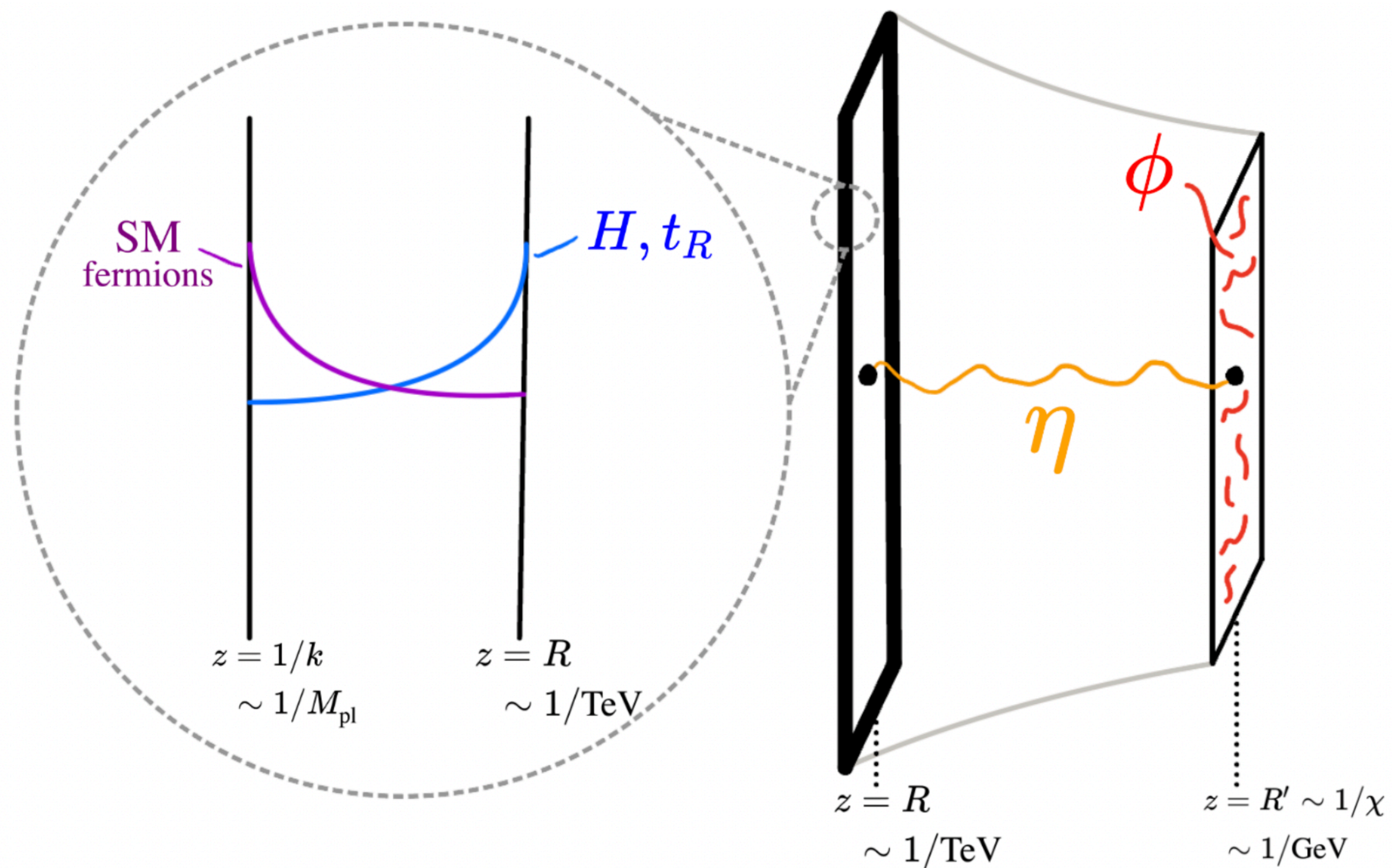
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Why don't we just lower cutoff scale? i.e. setting $\Lambda \sim \mathcal{O}(100)\text{GeV}$? \rightarrow **direct detection rules it out!**
 - **Way out**: SM interactions with the σ are suppressed by **f**, not by **Λ** , so the freeze-out of DM(ϕ) may be controlled by annihilations to dilaton(σ)
 - if $m_\phi < m_\sigma$, it is a **forbidden DM** scenario (D'Agnolo and Ruderman, 15'): the annihilation cross section is exponentially suppressed by Boltzmann factors
 $\phi\phi \rightarrow \sigma\sigma$ is the dominant process for the **freeze-out** process

Forbidden Conformal DM from 5D model

- ♦ modeling Conformal Forbidden DM at a GeV by Warped 5D model

$$ds^2 = \frac{1}{k^2 z^2} (\eta_{\mu\nu} dx^\mu dx^\nu - dz^2)$$



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- ♦ modeling Conformal Forbidden DM at a GeV by Warped 5D model

$$ds^2 = \frac{1}{k^2 z^2} (\eta_{\mu\nu} dx^\mu dx^\nu - dz^2) \quad R \gg 1/k$$

$$S_{\text{EH}} = \int d^5x \sqrt{g} (-2M_5^3 R - \Lambda_{\text{CC}}) - \sqrt{\tilde{g}} \Lambda_{\text{CC}} \frac{\delta(z-R)}{k} + \sqrt{\tilde{g}} \Lambda_{\text{CC}} \frac{\delta(z-R')}{k}$$

Z_2 symmetry

$$S_\phi = \int d^5x \sqrt{\tilde{g}} \delta(z-R') \left[\frac{1}{2} (\partial_\mu \phi)^2 - \frac{1}{2} m_\phi^2 \phi^2 - \frac{\lambda_\phi}{4!} \phi^4 \right]$$

$$S_{\text{GW}} = \int d^5x \sqrt{g} \left[\frac{1}{2} (\partial_M \eta)^2 - \frac{1}{2} m_\eta^2 k^2 \eta^2 \right] - \sqrt{\tilde{g}} \delta(z-R) V_{\text{UV}}(\eta) - \sqrt{\tilde{g}} \delta(z-R') V_{\text{IR}}(\eta)$$

$$V_{\text{UV}}(\eta) = \beta (\eta^2 - k^3 v_\eta^2)^2, \quad V_{\text{IR}} = \frac{1}{2} k m_{\text{IR}} \eta^2$$

- ♦ modeling can be easily UV completed by three brane set-up to incorporate into a composite Higgs model which address the hierarchy problem

Forbidden Conformal DM at a GeV

◆ 4D effective Lagrangian at $O(1/\Lambda)$

$$\begin{aligned}\mathcal{L} = & \mathcal{L}_{\text{SM}} + \frac{1}{2}(\partial_\mu \sigma)^2 - \frac{1}{2}m_\sigma^2 \sigma^2 - \frac{5}{6} \frac{m_\sigma^2}{f} \sigma^3 - \frac{11}{24} \frac{m_\sigma^2}{f^2} \sigma^4 \\ & + \frac{1}{2}(\partial_\mu \phi)^2 - \frac{1}{2}m_\phi^2 \phi^2 - \frac{1}{4!} \lambda_\phi^4 - \left(\frac{2\sigma}{f} + \frac{\sigma^2}{f^2} \right) \frac{1}{2} m_\phi^2 \phi^2 \\ & - \frac{\sigma}{\Lambda^2/f} \left[\sum_{\text{fermions}} m_\psi \bar{\psi} \psi + m_h^2 h^2 - 2m_W^2 W_\mu^+ W^{-\mu} - m_Z^2 Z_\mu Z^\mu \right] \\ & - \frac{\sigma}{\Lambda^2/f} \left[\frac{\beta_e(e)}{2e^3} F_{\mu\nu}^2 + \frac{\beta_3(g_3)}{2g_3^3} (G_{\mu\nu}^a)^2 + \sum_{\text{fermions}} \gamma_\psi \bar{\psi} \psi \right]\end{aligned}$$

Forbidden Conformal DM at a GeV

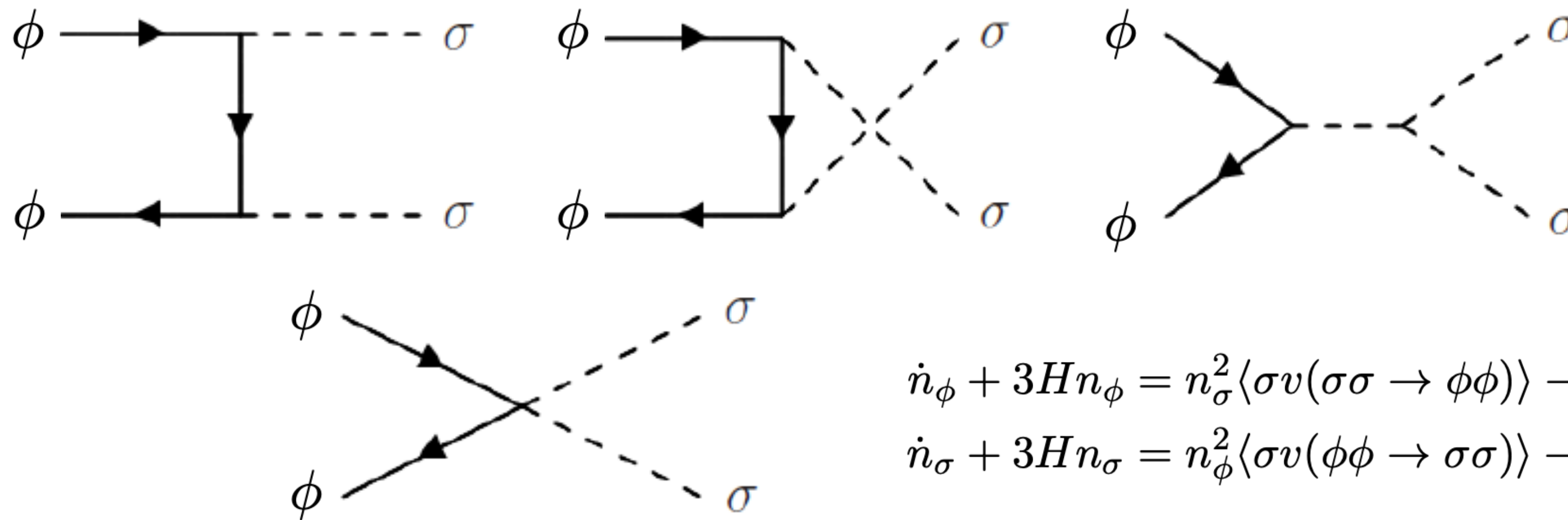
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dilaton-portal

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Relic Abundance

- Annihilations into SM states proceed via dilaton exchange.
- The dominant DM annihilation channels:



$$\begin{aligned}\dot{n}_\phi + 3Hn_\phi &= n_\sigma^2 \langle \sigma v(\sigma\sigma \rightarrow \phi\phi) \rangle - n_\phi^2 \langle \sigma v(\phi\phi \rightarrow \sigma\sigma) \rangle, \\ \dot{n}_\sigma + 3Hn_\sigma &= n_\phi^2 \langle \sigma v(\phi\phi \rightarrow \sigma\sigma) \rangle - n_\sigma^2 \langle \sigma v(\sigma\sigma \rightarrow \phi\phi) \rangle + \text{SM interactions}.\end{aligned}$$

Relic Abundance

$$\Delta = (m_\sigma - m_\phi)/m_\phi$$

$$\langle \sigma v(\sigma\sigma \rightarrow \phi\phi) \rangle = \frac{1}{9\pi m_\phi^2} \left(\frac{m_\phi}{f} \right)^4 \frac{\sqrt{\Delta(2+\Delta)}}{(1+\Delta)^7} (1 - 4\Delta - 2\Delta^2)^2$$

$$\begin{aligned} \langle \sigma v(\phi\phi \rightarrow \sigma\sigma) \rangle &= \left(\frac{n_\sigma^{\text{eq}}}{n_\phi^{\text{eq}}} \right)^2 \langle \sigma v(\sigma\sigma \rightarrow \phi\phi) \rangle \\ &= \frac{1}{9\pi m_\phi^2} \left(\frac{m_\phi}{f} \right)^4 \frac{\sqrt{\Delta(2+\Delta)}}{(1+\Delta)^4} (1 - 4\Delta - 2\Delta^2)^2 e^{-2\Delta x} \end{aligned}$$

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$$\Omega_\phi h^2 \sim 0.1 g_\Delta(x_f) \frac{9\pi (f/m_\phi)^4 m_\phi^2}{(20 \text{ TeV})^2} e^{2\Delta x_f},$$

$$x = m_\phi/T$$

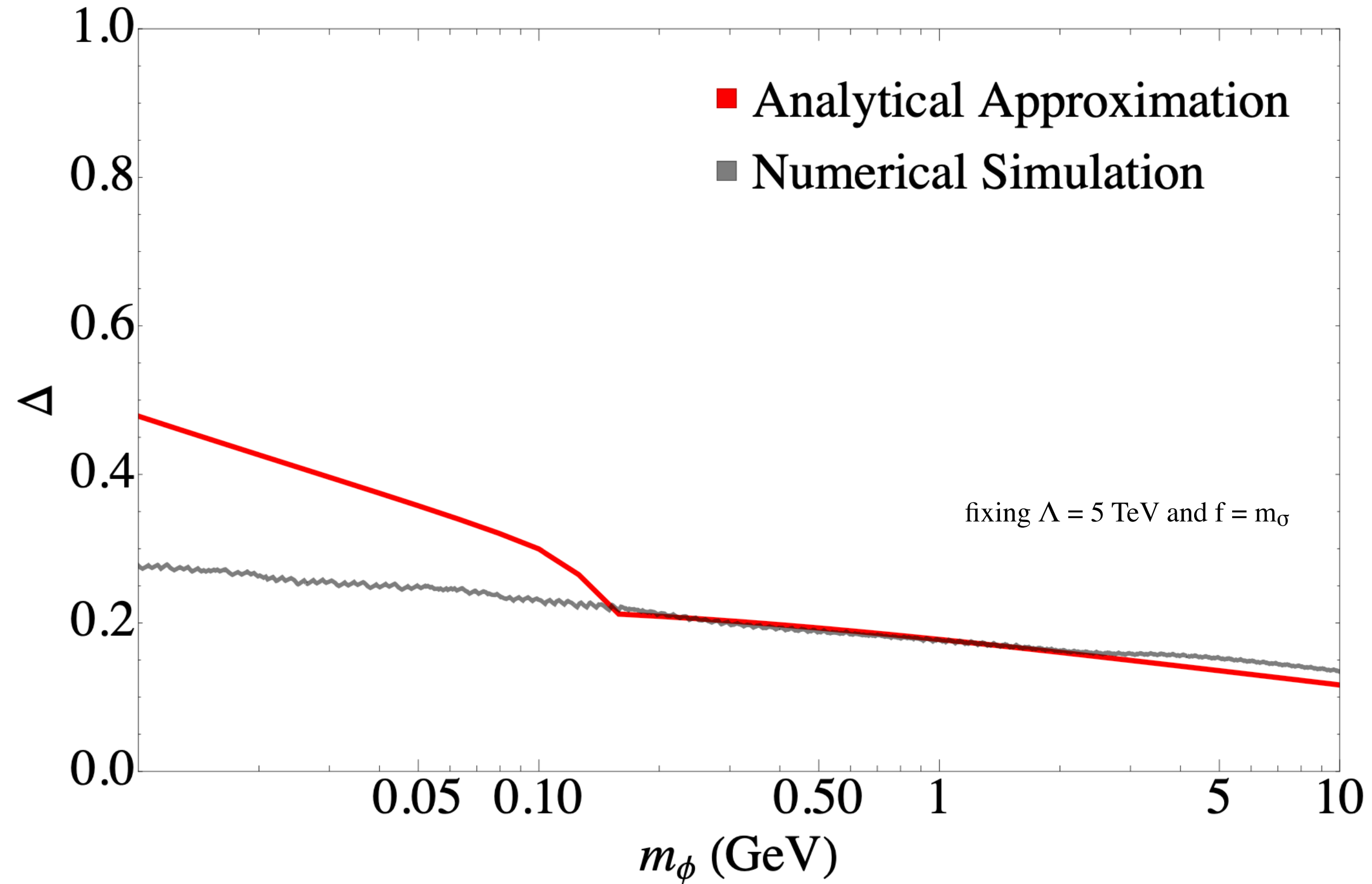
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$$\langle \sigma v(\phi\phi \rightarrow \sigma\sigma) \rangle = \left(\frac{n_c^\epsilon}{n_q^\epsilon} \right) = \frac{1}{9\pi n}$$



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Conformal Phase Transition

High T

T_c : nucleation of bubbles of the IR brane

Low T

Usual 5D picture here

◆ Important things to check:

Conformal Phase Transition

High T

conformal sector is in its hot,
deconfined phase with unbroken
conformal symmetry

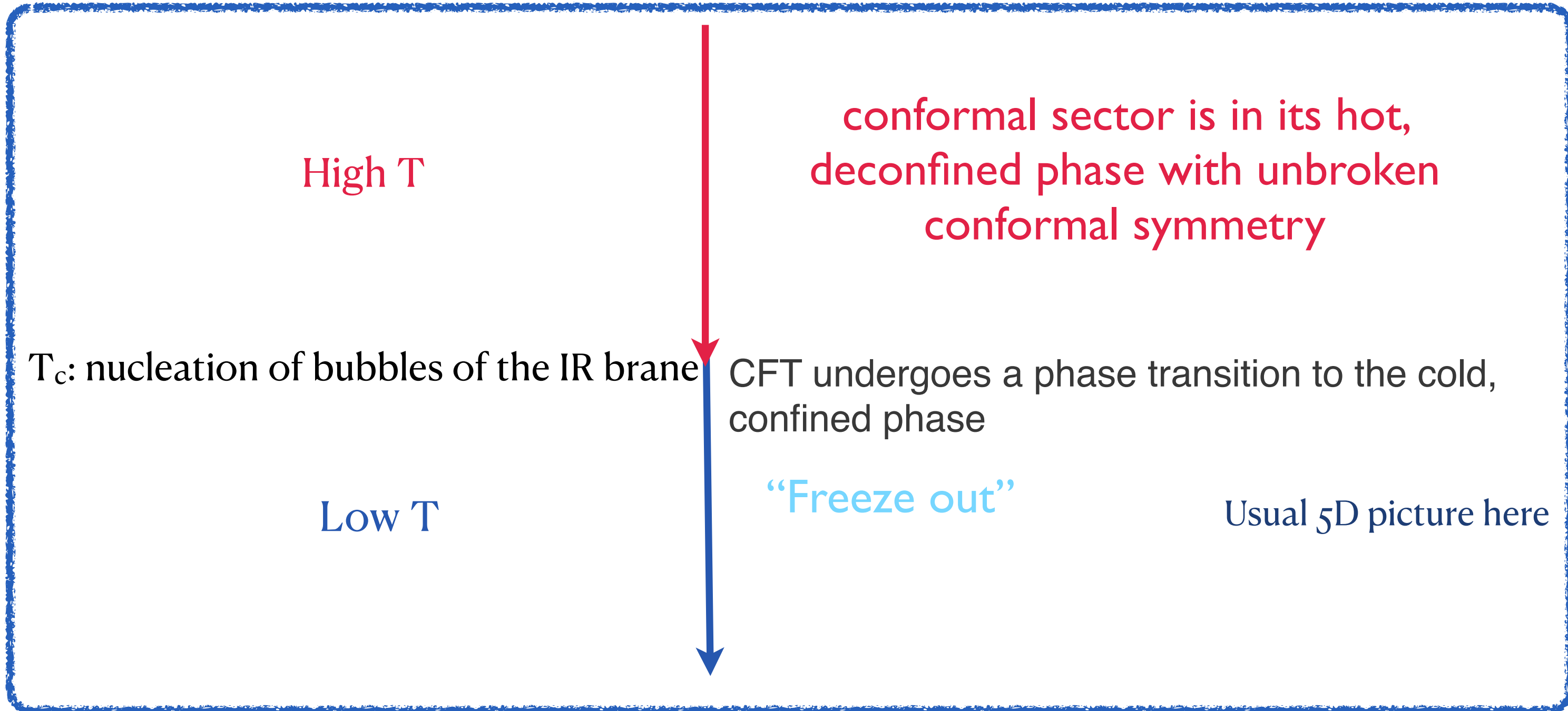
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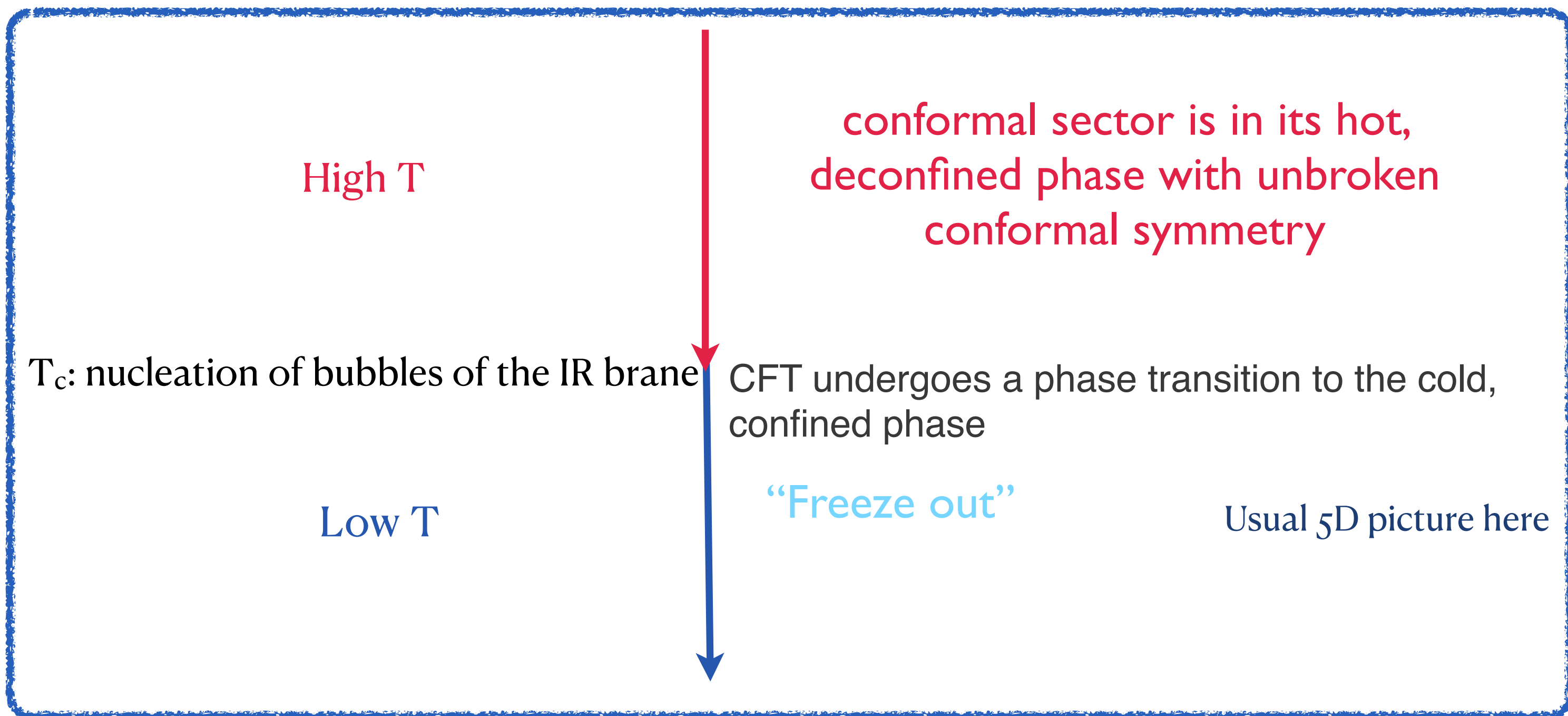
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Conformal Phase Transition



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◆ Important things to check:

- Does the phase transition complete? (otherwise the conformal sector remains in the hot phase and there is no DM candidate)
- Do the bubble collisions during the phase transition source stochastic gravitational waves consistent with NANOGrav?

Conformal Phase Transition

◆ Phase transition completion

$$F_{\text{confined}}(\langle\chi\rangle) = F_{\text{deconfined}}(T_c) \implies T_c = \sqrt{\frac{m_\sigma f}{\pi N}} \left(\frac{2}{4 + \alpha} \right)^{1/4}, \quad \alpha = 2(\sqrt{4 + m_\eta^2} - 2)$$

Check: the probability of bubble nucleation per unit volume per unit time Γ is greater than the Hubble parameter H^4

$$\Gamma \sim T_n^4 e^{-S_b} \quad H \sim \sqrt{\rho}/M_{\text{Pl}} \sim T_c^2/M_{\text{Pl}}$$

the vacuum energy of the CFT dominates over the energy of the radiation bath before the phase transition:

$$\rho \approx \pi^2 N^2 T_c^4 / 8.$$

$$\Gamma > H^4$$

$$S_b \lesssim 4 \left(\log \frac{M_{\text{Pl}}}{T_c} + \log \frac{T_n}{T_c} \right)$$

von Harling and Servant , 17'

Agashe, Du, Ekhterachian, Kumar and Sundrum, 19'

$$S_b = S_3/T_n$$

Thick wall limit:

$$S_3 \approx \frac{\sqrt{3}}{\pi^2} \frac{N^3 \chi_r^3}{\sqrt{V(\langle\chi\rangle)(T_n/T_c)^4 - V(\chi_r)}},$$

χ_r = “release point”

Conformal Phase Transition

◆ Gravitational wave signal

NANOGrav data favor:

$$T_R \in (0.017, 3.3) \text{ GeV and } \beta_{\text{GW}}/H < 27 \text{ at the 95\% CL}$$

Assuming the signal is dominated by bubble wall collisions: [Caprini et al, 15', 20'](#)

peak fractional abundance: $\Omega_{\text{GW}} h^2 \approx 1.3 \times 10^{-6} \left(\frac{H}{\beta_{\text{GW}}} \right)^2 \left(\frac{100}{g_*} \right)^{1/3}$

peak frequency of the GW: $f_{\text{GW}} \approx 0.04 \text{ mHz} \left(\frac{\beta_{\text{GW}}}{H} \right) \frac{T_R}{\text{TeV}} \left(\frac{g_*}{100} \right)^{1/6};$

phase transition duration:
(can be extracted from bounce action) $\frac{\beta_{\text{GW}}}{H} = T \frac{dS_b}{dT} \Big|_{T_n}$

$$T_R^4 = \frac{15}{4} \frac{N^2}{g_*(T_R)} T_c^4 = \frac{15}{2\pi^2(4 + \alpha)} \frac{f^2 m_\sigma^2}{g_*(T_R)}$$

$$T_R \approx 0.2 \sqrt{m_\sigma f}$$

ratio of energy released
energy released
to energy of radiation bath

$$\alpha_{\text{GW}} = \frac{15 N^2}{4 g_*(T_n)} \left(\frac{T_c^4}{T_n^4} - 1 \right)$$

Conformal Phase Transition

◆ Gravitational wave signal

NANOGrav data favor:

$$T_R \in (0.017, 3.3) \text{ GeV and } \beta_{\text{GW}}/H < 27 \text{ at the 95\% CL}$$

Assuming the signal is dominated by bubble wall collisions: [Caprini et al, 15', 20'](#)

peak fractional abundance: $\Omega_{\text{GW}} h^2 \approx 1.3 \times 10^{-6} \left(\frac{H}{\beta_{\text{GW}}} \right)^2 \left(\frac{100}{g_*} \right)^{1/3}$

peak frequency of the GW: $f_{\text{GW}} \approx 0.04 \text{ mHz} \left(\frac{\beta_{\text{GW}}}{H} \right) \frac{T_R}{\text{TeV}} \left(\frac{g_*}{100} \right)^{1/6};$

phase transition duration:
(can be extracted from bounce action) $\frac{\beta_{\text{GW}}}{H} = T \frac{dS_b}{dT} \Big|_{T_n}$

$$T_R^4 = \frac{15}{4} \frac{N^2}{g_*(T_R)} T_c^4 = \frac{15}{2\pi^2(4+\alpha)} \frac{f^2 m_\sigma^2}{g_*(T_R)}$$

$$T_R \approx 0.2 \sqrt{m_\sigma f}$$

ratio of energy released
energy released
to energy of radiation bath

$$\alpha_{\text{GW}} = \frac{15N^2}{4g_*(T_n)} \left(\frac{T_c^4}{T_n^4} - 1 \right)$$

for supercooled phase transition $T_c^4 \gg T_n^4$

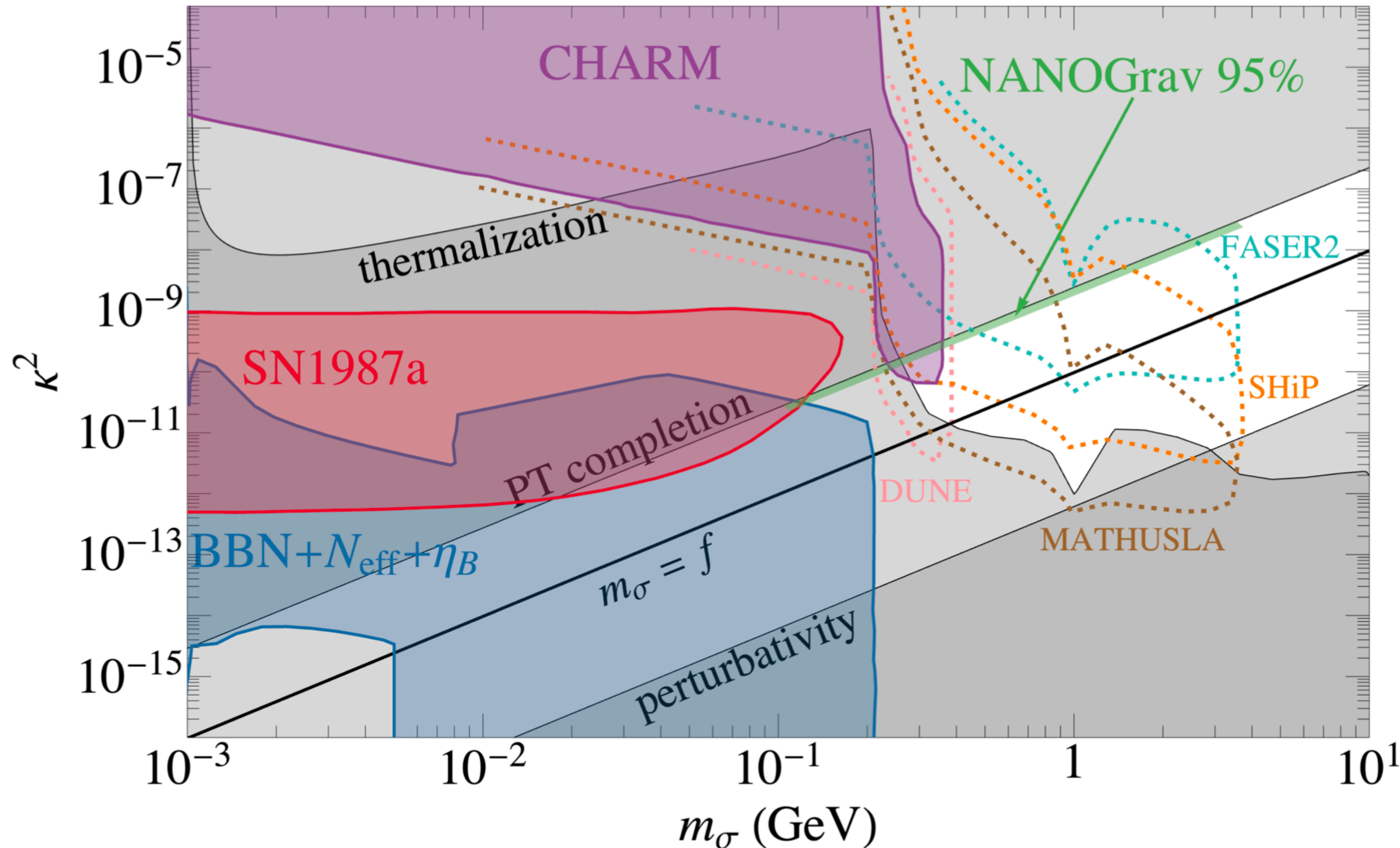
$$\alpha_{\text{GW}} \gg 1$$

Forbidden Conformal DM at a GeV

◆ Dilaton-porta Model

dilaton has the same couplings to the SM fermions and gauge bosons as the Higgs, but rescaled by a factor

$$\kappa = \frac{vf}{\Lambda^2}$$



$\Lambda=5\text{TeV}$

$\lambda=1$

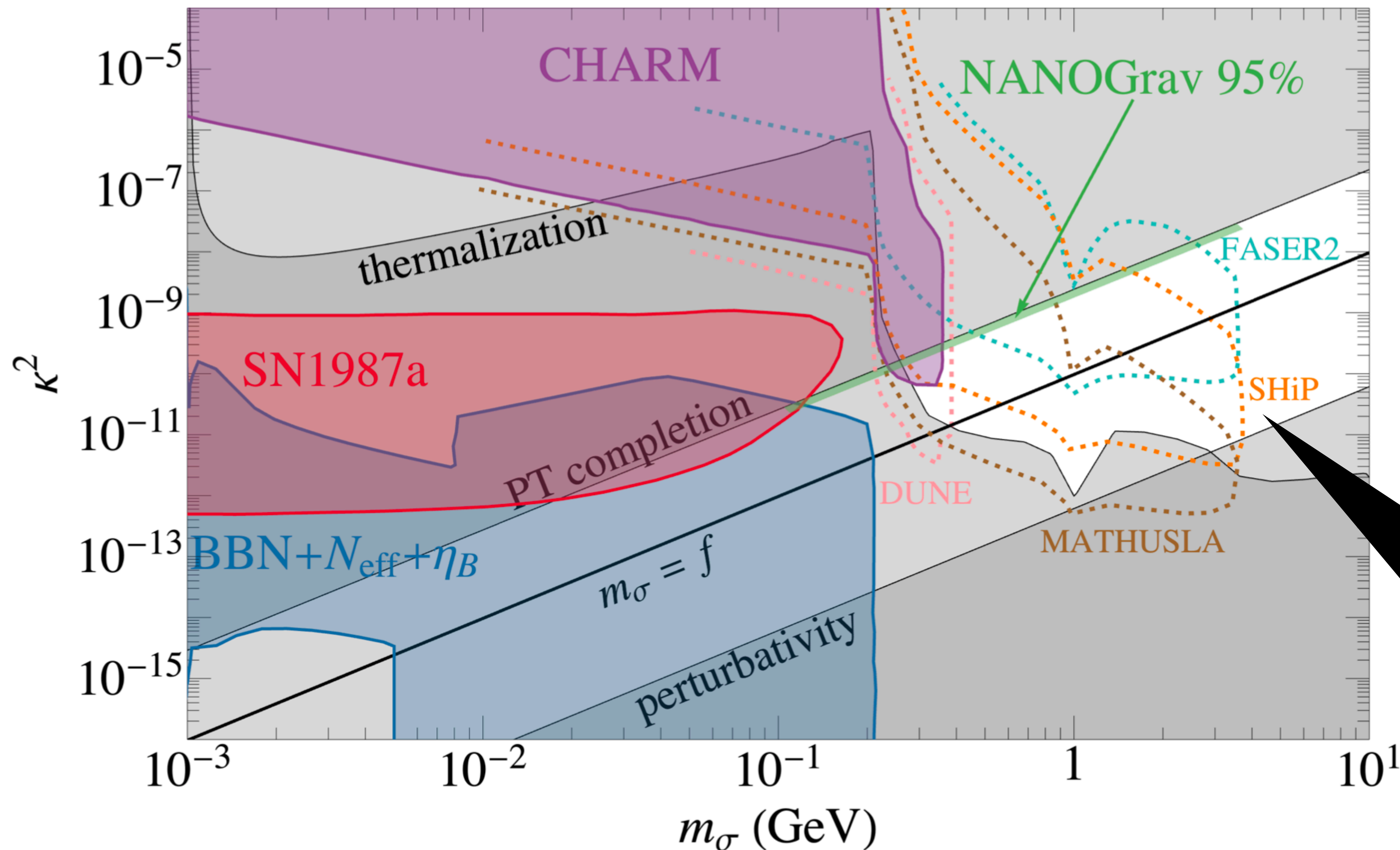
Thermalization bound:
 $\Gamma > H$ at $T = m_\sigma$

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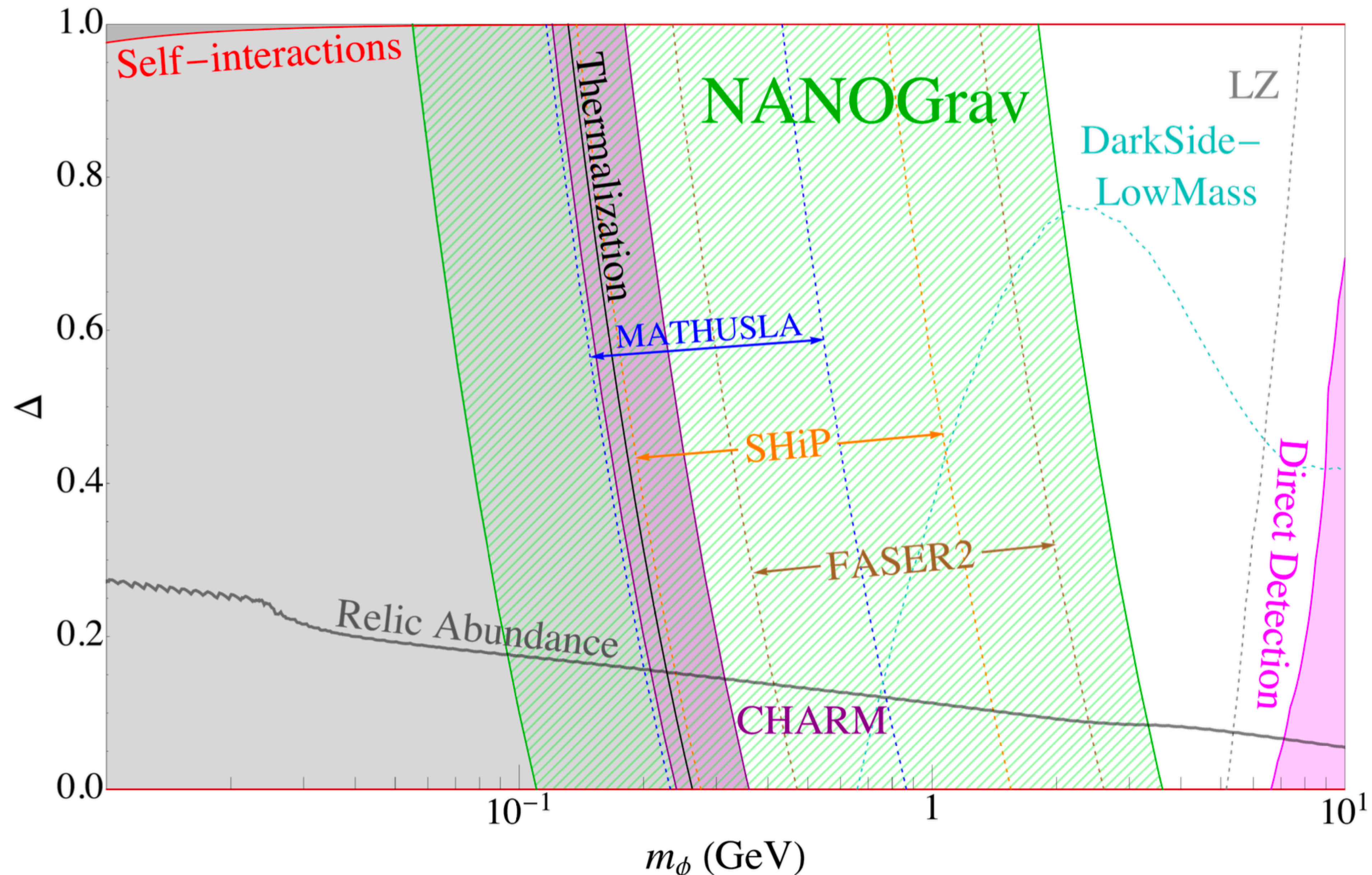
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$$\Delta = (m_\sigma - m_\phi)/m_\phi$$

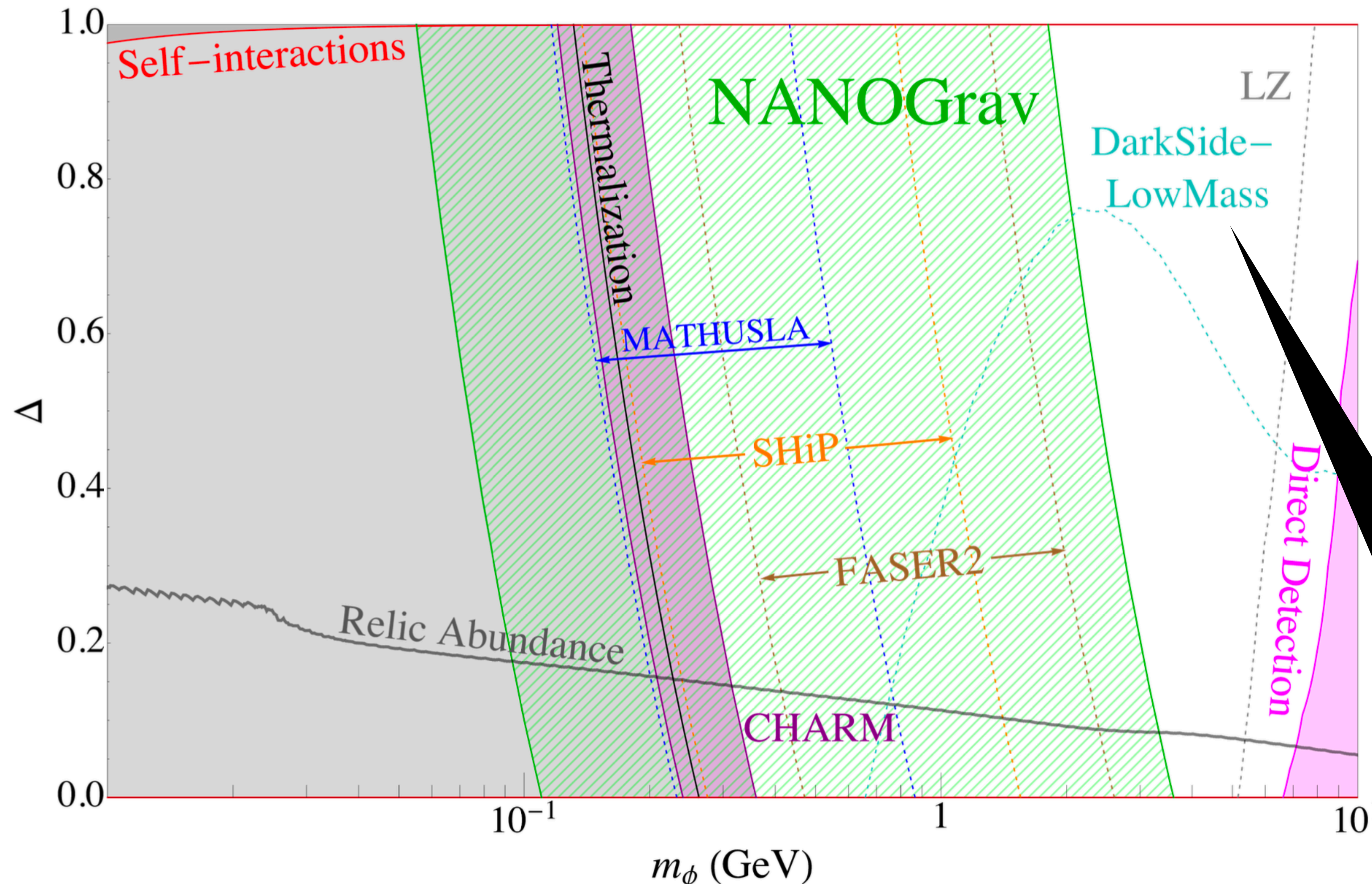
$$\sigma_{\phi N} = \frac{m_n^4}{\pi(1 + \Delta)^4 \Lambda^4 (m_\phi + m_n)^2}$$

$$f/m_\sigma = 4.5$$

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The salient feature: Not just NANOGrav signal: the model will be tested in the future facilities searching for LLP, and also by future direct detection

Other Constraints

◆ Higgs can decay to KK modes of the dilaton through a brane-localized interaction with the Goldberger–Wise scalar

$$\Gamma(h \rightarrow \text{KK} + \text{KK}) \sim \frac{\Lambda^2}{8\pi m_h} \left(\frac{f}{\Lambda} \right)^6$$

number of KK modes lighter than the Higgs is of order m_h/f

$$\Gamma(h \rightarrow \text{invisible}) \sim \frac{m_h}{8\pi} \left(\frac{f}{\Lambda} \right)^4 < \mathbf{0.11} \quad \text{ATLAS, 23'}$$

$$\Lambda/f \gtrsim 10.$$



$f \sim \text{GeV}$ and $\Lambda \sim \text{TeV}$.

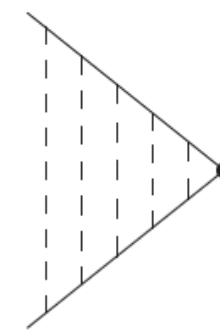
Other Constraints

◆ DM annihilation into SM fermions (via the dilaton portal)

Safe: Cross section is small

$$\langle \sigma v(\phi\phi \rightarrow f\bar{f}) \rangle \sim 10^{-36} \text{ cm}^3/\text{s} ((1 - \Delta)(3 + \Delta))^{-2} \left(\frac{m_f}{0.5 \text{ MeV}} \right)^2 \left(\frac{1 \text{ TeV}}{\Lambda} \right)^4$$

$$SE \approx \frac{\pi}{\epsilon_v} \frac{\sinh\left(\frac{12\epsilon_v}{\pi\epsilon_\phi}\right)}{\cosh\left(\frac{12\epsilon_v}{\pi\epsilon_\phi}\right) - \cos\left[2\pi\sqrt{\frac{6}{\pi^2\epsilon_\phi} - \left(\frac{12\epsilon_v}{\pi\epsilon_\phi}\right)^2}\right]},$$



$$\alpha_{\text{eff}} = m_\phi^2 / (4\pi f^2).$$

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$$\epsilon = \frac{m_\sigma}{\alpha_{\text{eff}} m_\phi} = 4\pi(1 + \Delta)^3 \frac{f^2}{m_\sigma^2}$$

Sommerfeld enhancement is only a large effect when $\epsilon \ll 1$



for $f = m_\sigma$ and a DM velocity of 0.5×10^{-3} , we find only a **small** enhancement of 2% to 17%

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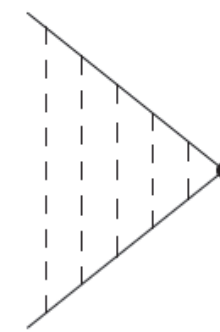
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- How about Sommerfeld Enhancement (via dilaton)?

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Summary

1. We present the first extensive study of light thermal relic DM which is a composite of a CFT. We have focused on forbidden DM
2. for a range of dilaton masses around 0.1–2 GeV, the conformal phase transition can source a nHz-scale stochastic GW background consistent with that observed at NANOGrav
3. Theoretical and experimental bounds pointed to dark sector masses in the range 0.1– 10 GeV. Imposing the requirements that the dark sector thermalizes with the SM, that the conformal phase transition completes, and that the dilaton effective theory is valid led to a lower bound on the dilaton mass of about 0.1 GeV; meanwhile, direct detection bounds constrained the DM mass to be less than 10 GeV.
4. The viable parameter space below a few GeV will be probed by experiments searching for light, weakly-coupled particles like FASER2, MATHUSLA, and SHiP. Future direct detection experiments specialized for low mass WIMPs, in particular DarkSide-LowMass, will be sensitive to the remaining parameter space up to 10 GeV.