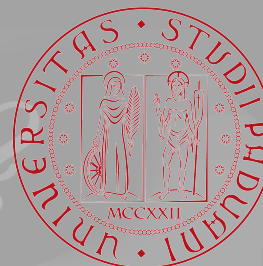


Composite ALPs through the Z portal



Ennio Salvioni

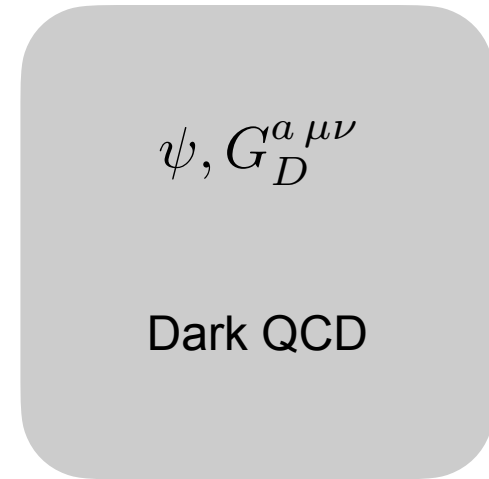
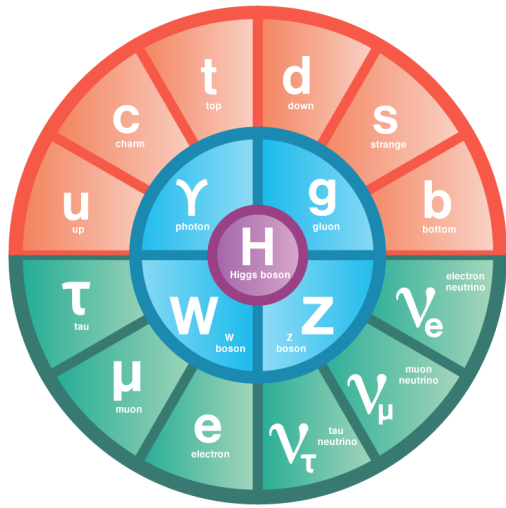


University & INFN, Padua

Light Dark World 2023
Karlsruhe, September 19

2310.xxxxx [hep-ph]
with Hsin-Chia Cheng (Davis), Xu-Hui Jiang (HKUST)
and Lingfeng Li (Brown)

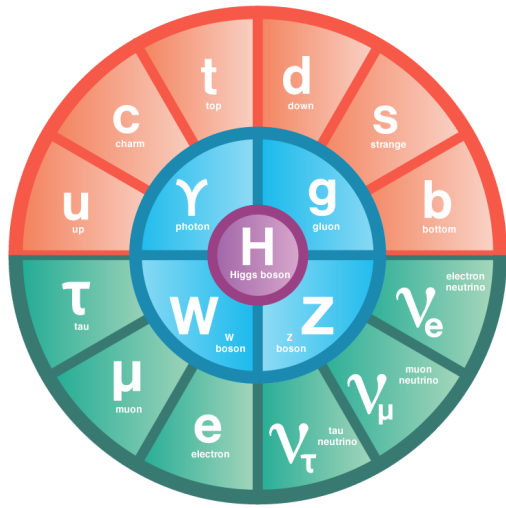
Introduction



(neutral under the Standard Model)

- Motivated by big questions: dark matter (e.g. SIMPs), naturalness (neutral naturalness, relaxion models), ...
[Hochberg et al. 2014]
[Chacko, Goh, Harnik 2005]
[Graham, Kaplan, Rajendran 2015]
- “Dark shower” - type signatures at the LHC: challenging, but major progress recently, with room for further improvement
[Born et al. 2023]
[Cohen et al. 2023]
[Bernreuther et al. 2022]
[Knapen, Shelton, Xu 2021]
...

Introduction



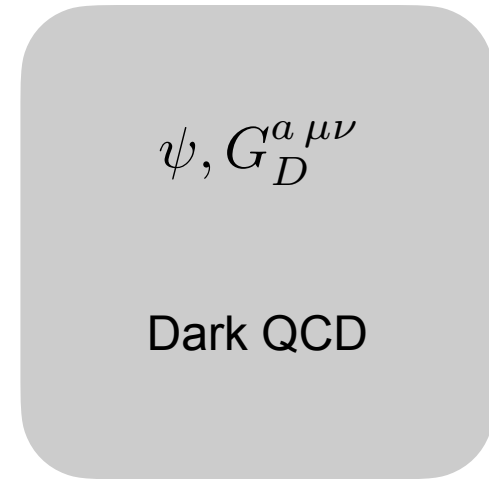
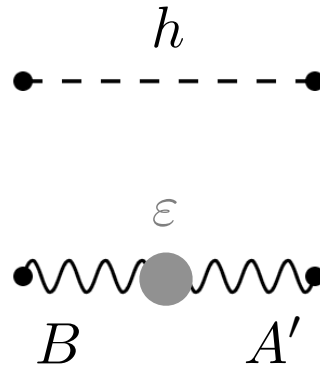
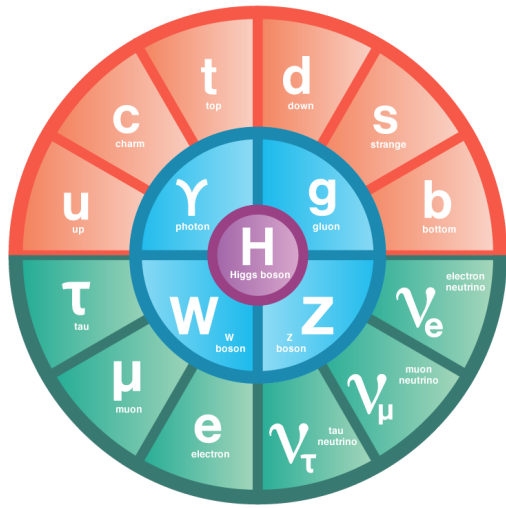
$$\psi, G_D^{a\mu\nu}$$

Dark QCD

(neutral under the Standard Model)

Which portal?

Introduction

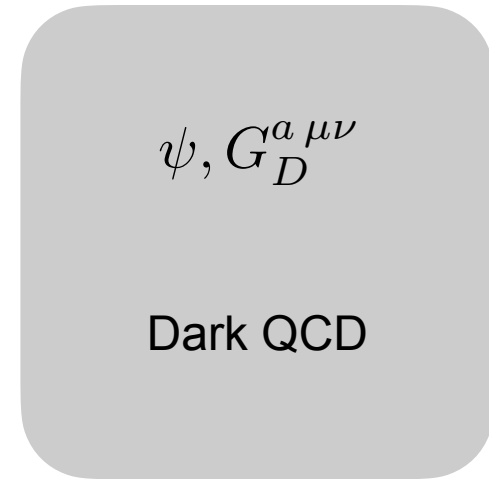
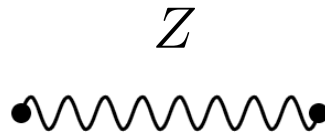
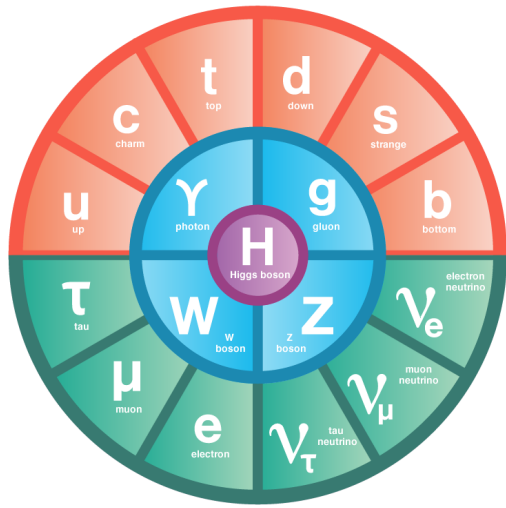


(neutral under the Standard Model)

Which portal?

Some interactions are very well studied: Higgs, dark photon

Introduction

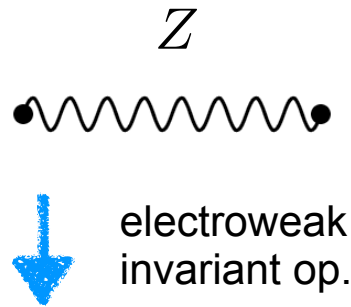
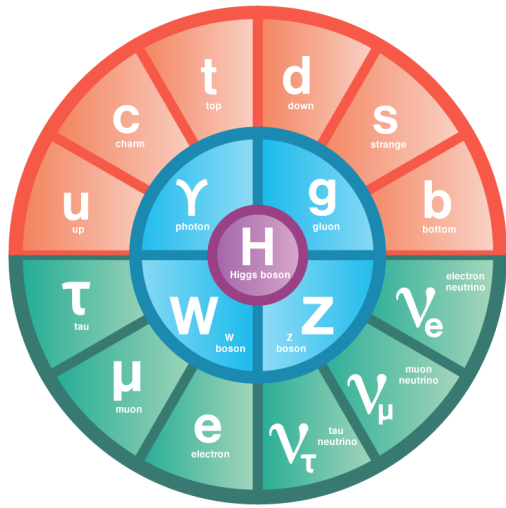


(neutral under the Standard Model)

Z portal is far less explored, yet the LHC is collecting a huge sample:
 $> 10^{11}$ Z bosons @ High-Luminosity phase

(one thousand times more than for Higgs)

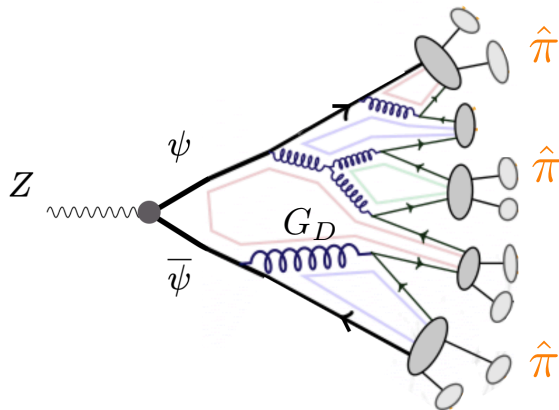
Introduction



$$\psi, G_D^{a\mu\nu}$$

Dark QCD

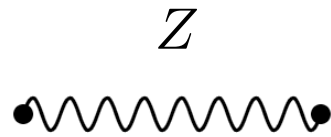
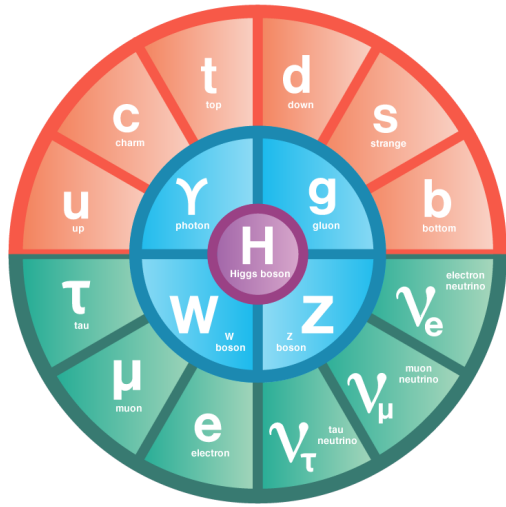
$$\frac{c}{M^2} (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{\psi} \gamma^\mu \psi)$$



“Dark shower” events generated by Z decays at LHC

Mostly produce lightest dark hadrons, the **dark pions**

Introduction



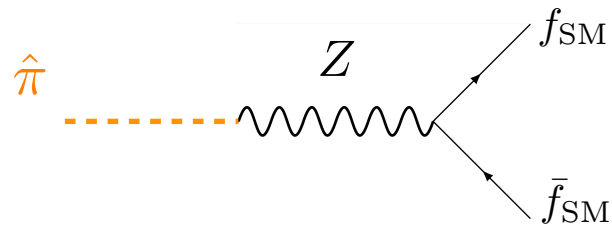
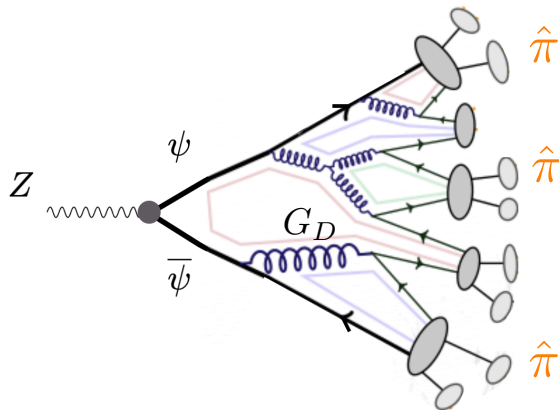
electroweak
invariant op.

$$\psi, G_D^{a\mu\nu}$$

Dark QCD

$$\frac{c}{M^2} (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{\psi} \gamma^\mu \psi)$$

$$\frac{1}{f_a} (iH^\dagger \overleftrightarrow{D}_\mu H) (\partial^\mu \hat{\pi})$$



dark pions behave as **composite ALPs**

ALP through the Z portal

Distinctive feature of Z portal is coupling of ALPs (dark pions) to Higgs current,

$$\frac{1}{f_a} (i H^\dagger \overleftrightarrow{D}_\mu H) (\partial^\mu a) \xrightarrow{\text{EOM}} -\frac{\partial_\mu a}{f_a} \sum_f c_f \bar{f} \gamma^\mu \gamma_5 f, \quad c_f = T_L^3(f)$$

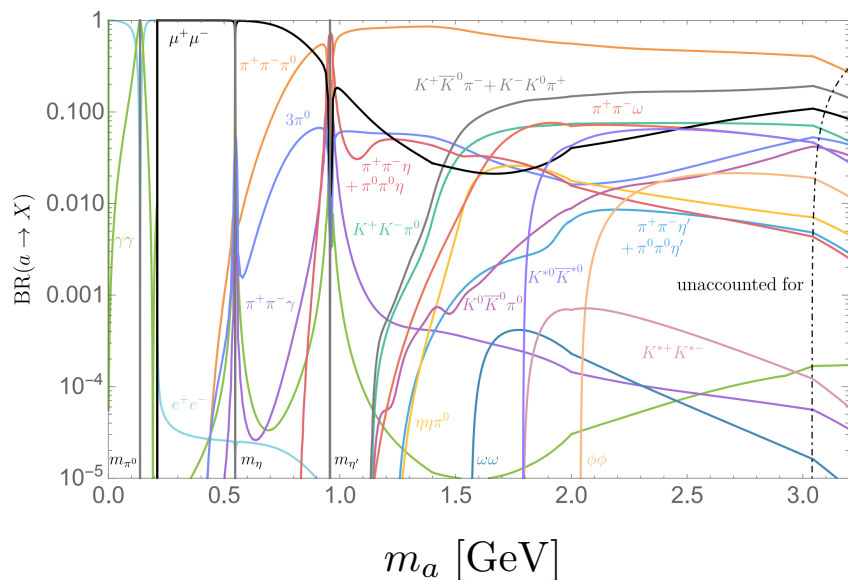
For $m_a \sim \text{GeV}$, must consider decays to exclusive final states containing SM hadrons

Apply data-driven methods, following [\[Aloni, Soreq, Williams 2018\]](#)

- For $m_a < m_{\eta'} \approx 1 \text{ GeV}$, match ALP effective field theory to Chiral Perturbation Theory (leading order + corrections)
- For $m_{\eta'} < m_a \lesssim 3 \text{ GeV}$: include exchange of scalar, vector, tensor resonances, using as much input from data as feasible

Isospin-violating couplings lead to important differences with universal scenarios

Big differences with gluon-coupled ALP

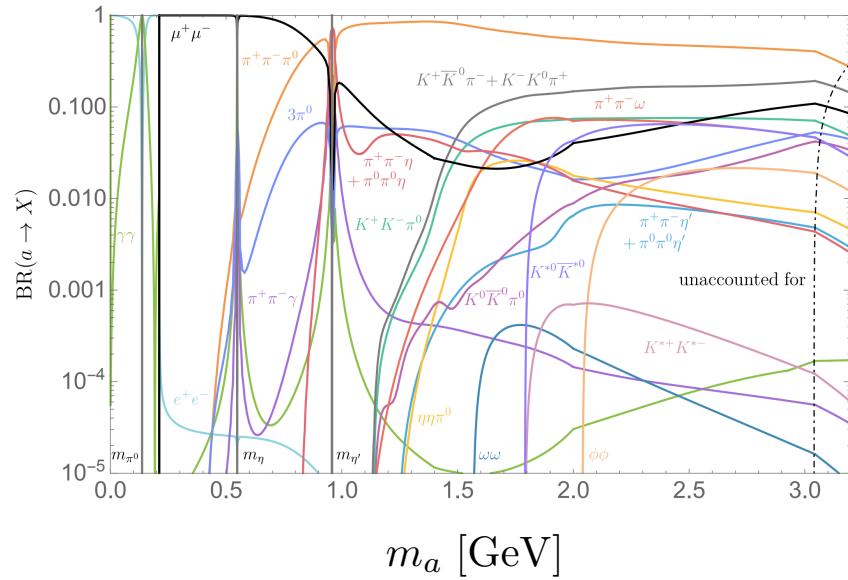


$$\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu a}{f_a} \sum_f c_f \bar{f} \gamma^\mu \gamma_5 f$$

$$c_f = T_L^3(f)$$

isospin-breaking coupling to fermions

Big differences with gluon-coupled ALP

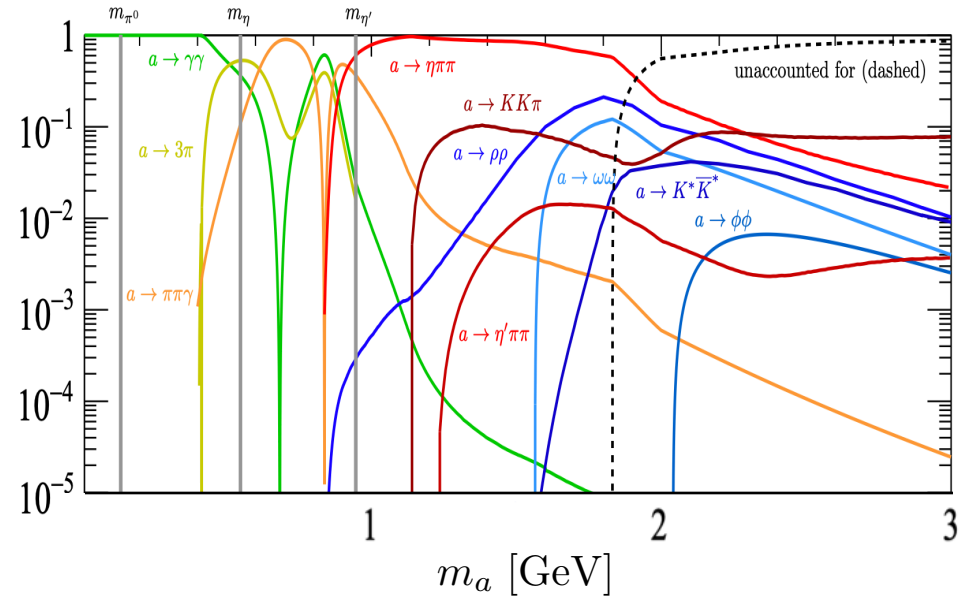


$$\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu a}{f_a} \sum_f c_f \bar{f} \gamma^\mu \gamma_5 f$$

$$c_f = T_L^3(f)$$

isospin-breaking coupling to fermions

[Cheng, Li, Salvioni, 2021]

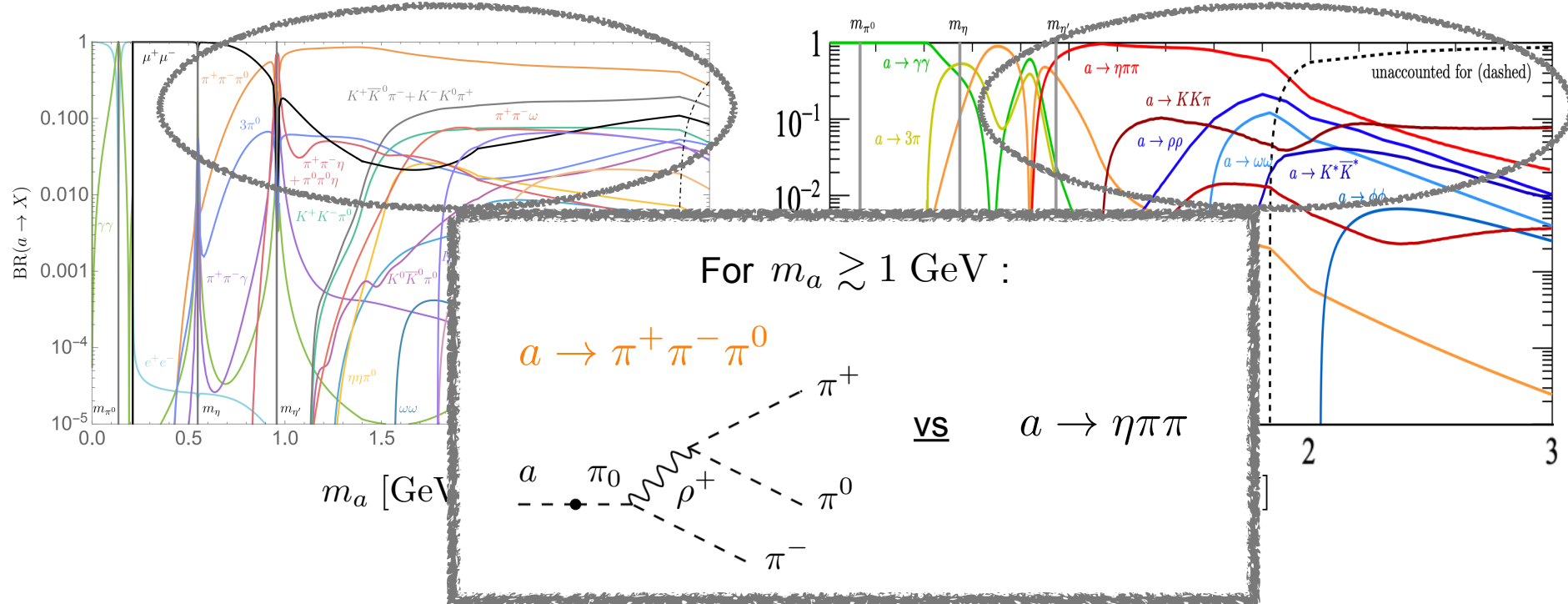


$$\mathcal{L}_{\text{eff}} \supset c_g \frac{\alpha_s}{4\pi} \frac{a}{f_a} G_{\mu\nu}^a \tilde{G}^{\mu\nu a}$$

coupling to gluons

[Aloni, Soreq, Williams 2018]

Big differences with gluon-coupled ALP



$$\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu a}{f_a} \sum_f c_f \bar{f} \gamma^\mu \gamma_5 f$$

$$c_f = T_L^3(f)$$

isospin-breaking coupling to fermions

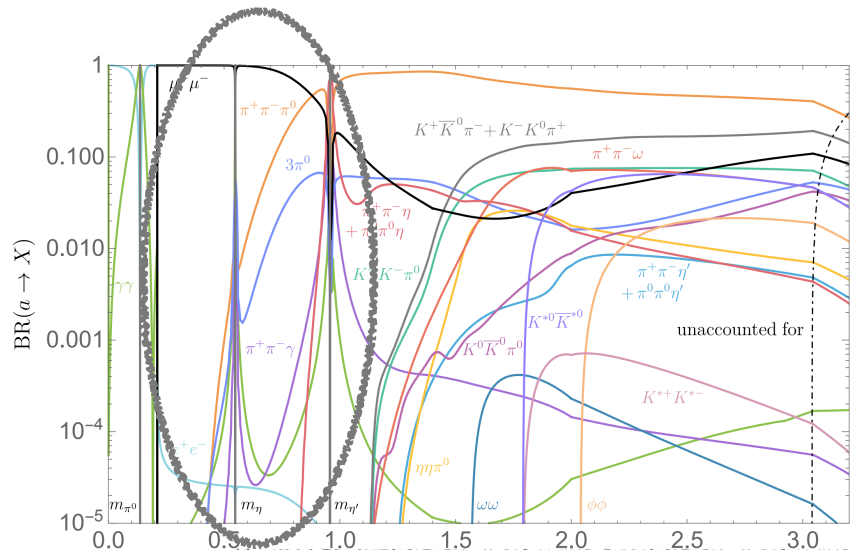
[Cheng, Li, Salvioni, 2021]

$$\mathcal{L}_{\text{eff}} \supset c_g \frac{\alpha_s}{4\pi} \frac{a}{f_a} G_{\mu\nu}^a \tilde{G}^{\mu\nu a}$$

coupling to gluons

[Aloni, Soreq, Williams 2018]

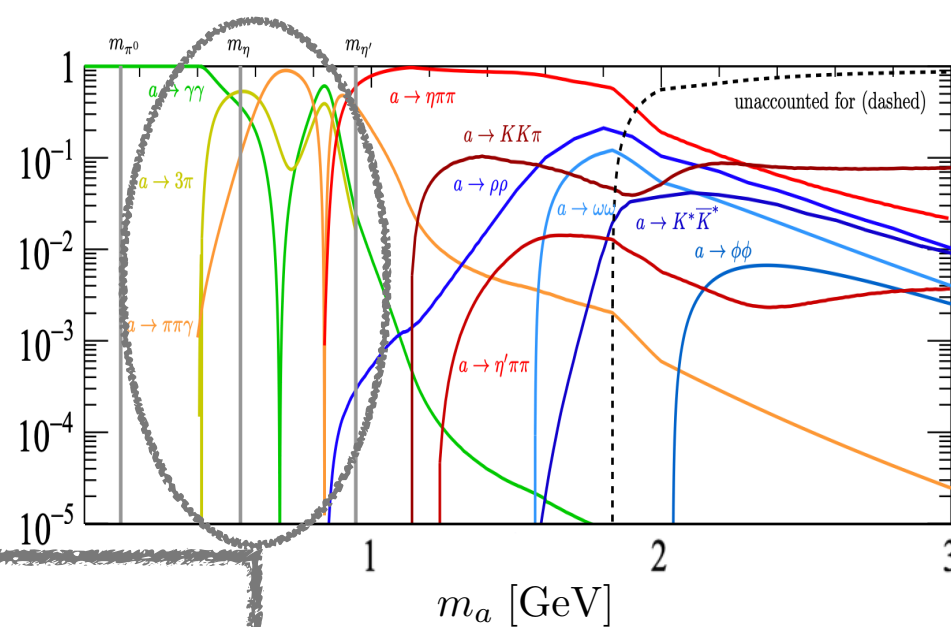
Big differences with gluon-coupled ALP


$$a \rightarrow \pi^+ \pi^- \gamma : \text{negligible \underline{vs} dominant}$$

$$\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu a}{f_a} \sum_f c_f \bar{f} \gamma^\mu \gamma_5 f$$

$$c_f = T_L^3(f)$$

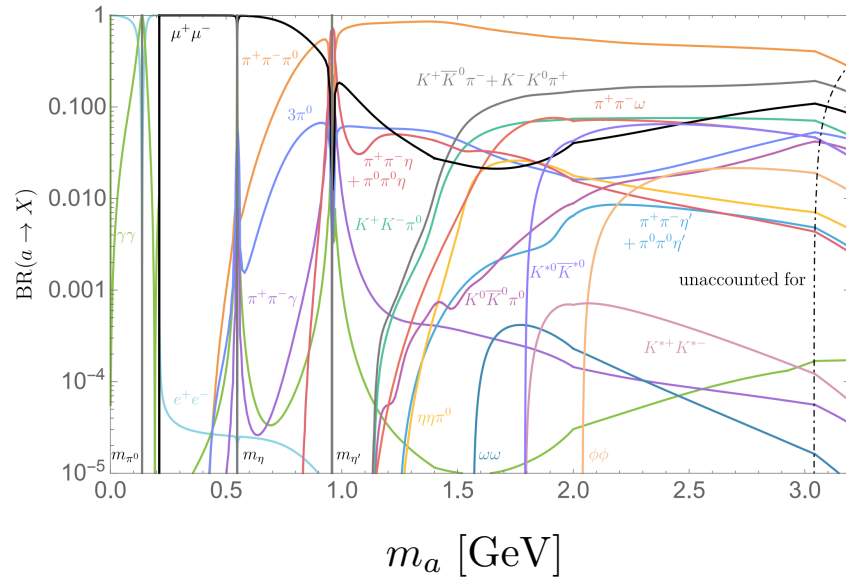
isospin-breaking coupling to fermions



$$\mathcal{L}_{\text{eff}} \supset c_g \frac{\alpha_s}{4\pi} \frac{a}{f_a} G_{\mu\nu}^a \tilde{G}^{\mu\nu a}$$

coupling to gluons

ALP couplings to SM hadrons



$$\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu a}{f_a} \sum_f c_f \bar{f} \gamma^\mu \gamma_5 f$$

Our calculations apply to **arbitrary**
(flavour-diagonal) couplings to fermions

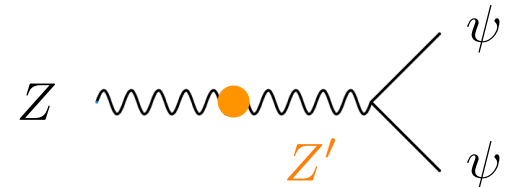
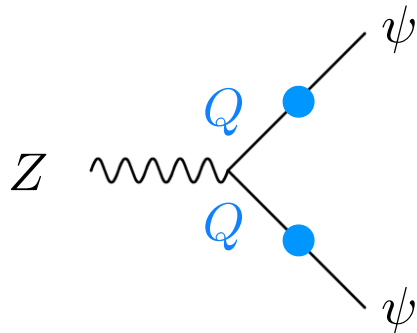


[Cheng, Li, Salvioni, 2021]

Use it for your next ALP model!

Models

$$\frac{c}{M^2} (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{\psi} \gamma^\mu \psi)$$



$$\mathcal{L}_{\text{UV}} \supset \bar{Q} Y \psi H \quad \rightarrow \quad \frac{c}{M^2} \sim \frac{Y^2}{M_Q^2}$$

$$\mathcal{L}_{\text{UV}} \supset \delta \hat{M}^2 Z^\mu Z'_\mu \quad \rightarrow \quad \frac{c}{M^2} \sim \frac{g_D^2}{M_{Z'}^2}$$

Dark quarks Q with SM electroweak charges

Need to be heavier than ~ 1 TeV

Dark gauge boson Z'

Can even be lighter than the Z

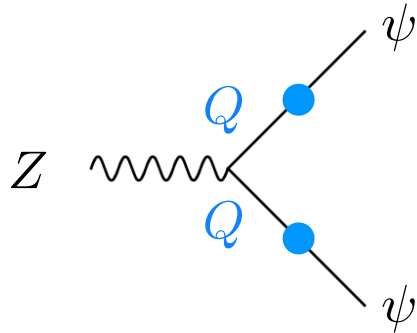
[Cheng, Li, Salvioni, 2021]

[Cheng, Jiang, Li, Salvioni, 2310.xxxxxx]

In both models, there are corrections to electroweak precision observables
What dark pion signatures can we expect, after taking the bounds into account?

Models

$$\frac{c}{M^2} (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{\psi} \gamma^\mu \psi)$$

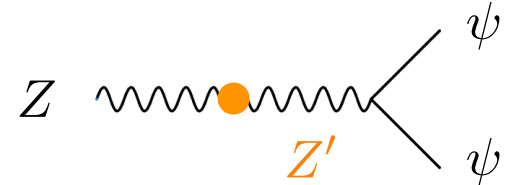


$$\mathcal{L}_{UV} \supset \bar{Q} Y \psi H \quad \rightarrow \quad \frac{c}{M^2} \sim \frac{Y^2}{M_Q^2}$$

Dark quarks Q with SM electroweak charges
Need to be heavier than ~ 1 TeV

[Cheng, Li, Salvioni, 2021]

today



$$\mathcal{L}_{UV} \supset \delta \hat{M}^2 Z^\mu Z'_\mu \quad \rightarrow \quad \frac{c}{M^2} \sim \frac{g_D^2}{M_{Z'}^2}$$

Dark gauge boson Z'
Can even be lighter than the Z

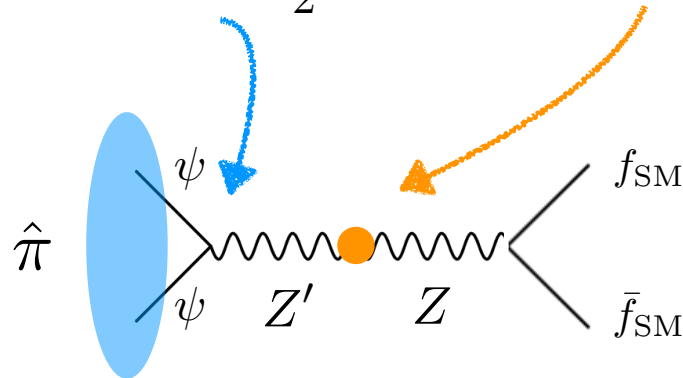
[Cheng, Jiang, Li, Salvioni, 2310.xxxxxx]

In both models, there are corrections to electroweak precision observables
What dark pion signatures can we expect, after taking the bounds into account?

Mass-mixed Z'

Gauge boson of dark $U(1)_D$ symmetry

$$\mathcal{L}_{\text{BSM}} \supset g_D \bar{\psi} \gamma^\mu \mathbf{X} \psi + \frac{1}{2} \hat{M}_{Z'}^2 Z'^\mu Z'_\mu + \delta \hat{M}^2 Z^\mu Z'_\mu$$



$$-\frac{\varepsilon}{2} Z'_{\mu\nu} B^{\mu\nu}$$

[Essig, Schuster, Toro 2009]

Kinetic mixing does not mediate decay of dark pions

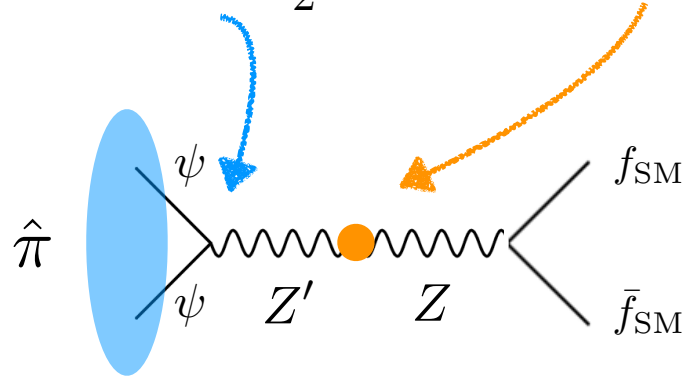
ε affects transverse modes, while dark pion mixes with longitudinal modes

Need mass mixing (assumed to originate from second doublet with $U(1)_D$ charge)

Mass-mixed Z'

Gauge boson of dark $U(1)_D$ symmetry

$$\mathcal{L}_{\text{BSM}} \supset g_D \bar{\psi} \gamma^\mu \mathbf{X} \psi + \frac{1}{2} \hat{M}_{Z'}^2 Z'^\mu Z'_\mu + \delta \hat{M}^2 Z^\mu Z'_\mu$$



Integrating out Z and Z' , find effective decay constant $\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu \hat{\pi}_i}{f_a^{(i)}} T_L^3(f) \bar{f} \gamma^\mu \gamma_5 f$

$$f_a^{(i)} = \frac{2M_Z^2 M_{Z'}^2}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D g_Z f_{\hat{\pi}} \delta \hat{M}^2} \approx 1 \text{ PeV} \frac{1}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D} \left(\frac{1 \text{ GeV}}{f_{\hat{\pi}}} \right) \left(\frac{10^{-2}}{\delta \hat{M}^2 / M_Z^2} \right) \left(\frac{M_{Z'}}{60 \text{ GeV}} \right)^2$$

focus on light Z' , below M_Z

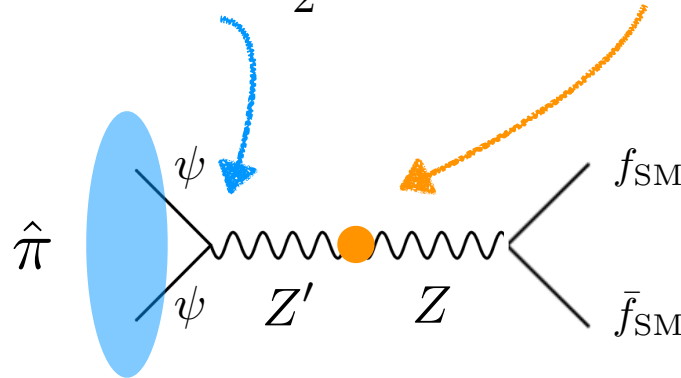
assume $N_f = 2$ dark flavors

$\rightarrow N_f^2 - 1 = 3$ dark pions

Mass-mixed Z'

Gauge boson of dark $U(1)_D$ symmetry

$$\mathcal{L}_{\text{BSM}} \supset g_D \bar{\psi} \gamma^\mu \mathbf{X} \psi + \frac{1}{2} \hat{M}_{Z'}^2 Z'^\mu Z'_\mu + \delta \hat{M}^2 Z^\mu Z'_\mu$$



Integrating out Z and Z' , find effective decay constant $\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu \hat{\pi}_i}{f_a^{(i)}} T_L^3(f) \bar{f} \gamma^\mu \gamma_5 f$

$$f_a^{(i)} = \frac{2M_Z^2 M_{Z'}^2}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D g_Z f_{\hat{\pi}} \delta \hat{M}^2} \approx 1 \text{ PeV} \frac{1}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D} \left(\frac{1 \text{ GeV}}{f_{\hat{\pi}}} \right) \left(\frac{10^{-2}}{\delta \hat{M}^2 / M_Z^2} \right) \left(\frac{M_{Z'}}{60 \text{ GeV}} \right)^2$$

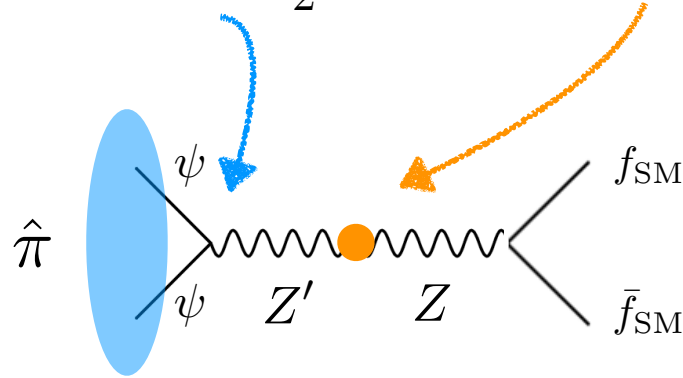
upper bound on Z - Z' mixing
from electroweak precision

assume $N_f = 2$ dark flavors
 $\rightarrow N_f^2 - 1 = 3$ dark pions

Mass-mixed Z'

Gauge boson of dark $U(1)_D$ symmetry

$$\mathcal{L}_{\text{BSM}} \supset g_D \bar{\psi} \gamma^\mu \mathbf{X} \psi + \frac{1}{2} \hat{M}_{Z'}^2 Z'^\mu Z'_\mu + \delta \hat{M}^2 Z^\mu Z'_\mu$$



Integrating out Z and Z' , find effective decay constant $\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu \hat{\pi}_i}{f_a^{(i)}} T_L^3(f) \bar{f} \gamma^\mu \gamma_5 f$

$$f_a^{(i)} = \frac{2M_Z^2 M_{Z'}^2}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D g_Z f_{\hat{\pi}} \delta \hat{M}^2} \approx 1 \text{ PeV} \frac{1}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D} \left(\frac{1 \text{ GeV}}{f_{\hat{\pi}}} \right) \left(\frac{10^{-2}}{\delta \hat{M}^2 / M_Z^2} \right) \left(\frac{M_{Z'}}{60 \text{ GeV}} \right)^2$$

decay constant of dark pions

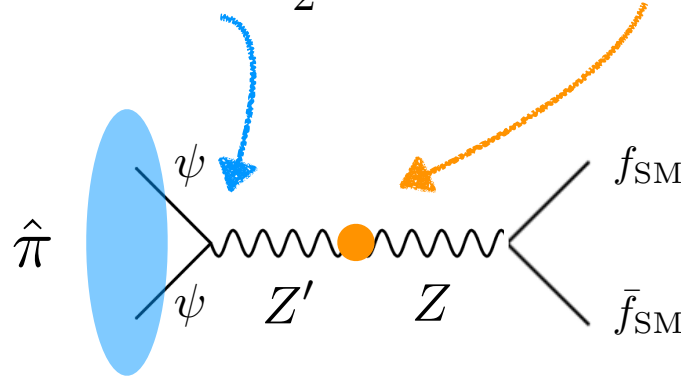
assume $N_f = 2$ dark flavors

$\rightarrow N_f^2 - 1 = 3$ dark pions

Mass-mixed Z'

Gauge boson of dark $U(1)_D$ symmetry

$$\mathcal{L}_{\text{BSM}} \supset g_D \bar{\psi} \gamma^\mu \mathbf{X} \psi + \frac{1}{2} \hat{M}_{Z'}^2 Z'^\mu Z'_\mu + \delta \hat{M}^2 Z^\mu Z'_\mu$$



Integrating out Z and Z' , find effective decay constant $\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu \hat{\pi}_i}{f_a^{(i)}} T_L^3(f) \bar{f} \gamma^\mu \gamma_5 f$

$$f_a^{(i)} = \frac{2M_Z^2 M_{Z'}^2}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D g_Z f_{\hat{\pi}} \delta \hat{M}^2} \approx 1 \text{ PeV} \frac{1}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D} \left(\frac{1 \text{ GeV}}{f_{\hat{\pi}}} \right) \left(\frac{10^{-2}}{\delta \hat{M}^2 / M_Z^2} \right) \left(\frac{M_{Z'}}{60 \text{ GeV}} \right)^2$$

axial-vector coupling of Z' to physical dark quarks

(generated by dark Yukawas $y_{ij} \bar{\psi}_i \Phi \psi_j$)

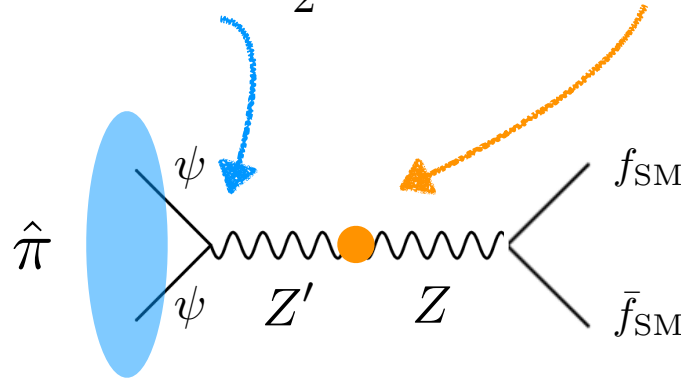
assume $N_f = 2$ dark flavors

$\rightarrow N_f^2 - 1 = 3$ dark pions

Mass-mixed Z'

Gauge boson of dark $U(1)_D$ symmetry

$$\mathcal{L}_{\text{BSM}} \supset g_D \bar{\psi} \gamma^\mu \mathbf{X} \psi + \frac{1}{2} \hat{M}_{Z'}^2 Z'^\mu Z'_\mu + \delta \hat{M}^2 Z^\mu Z'_\mu$$



Integrating out Z and Z' , find effective decay constant $\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu \hat{\pi}_i}{f_a^{(i)}} T_L^3(f) \bar{f} \gamma^\mu \gamma_5 f$

$$f_a^{(i)} = \frac{2M_Z^2 M_{Z'}^2}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D g_Z f_{\hat{\pi}} \delta \hat{M}^2} \approx 1 \text{ PeV} \frac{1}{\text{Tr}(\sigma_i \mathbf{X}'_A) g_D} \left(\frac{1 \text{ GeV}}{f_{\hat{\pi}}} \right) \left(\frac{10^{-2}}{\delta \hat{M}^2 / M_Z^2} \right) \left(\frac{M_{Z'}}{60 \text{ GeV}} \right)^2$$

typical decay constant is at $\sim \text{PeV}$: dark pions are
interesting target for present & future LHC experiments

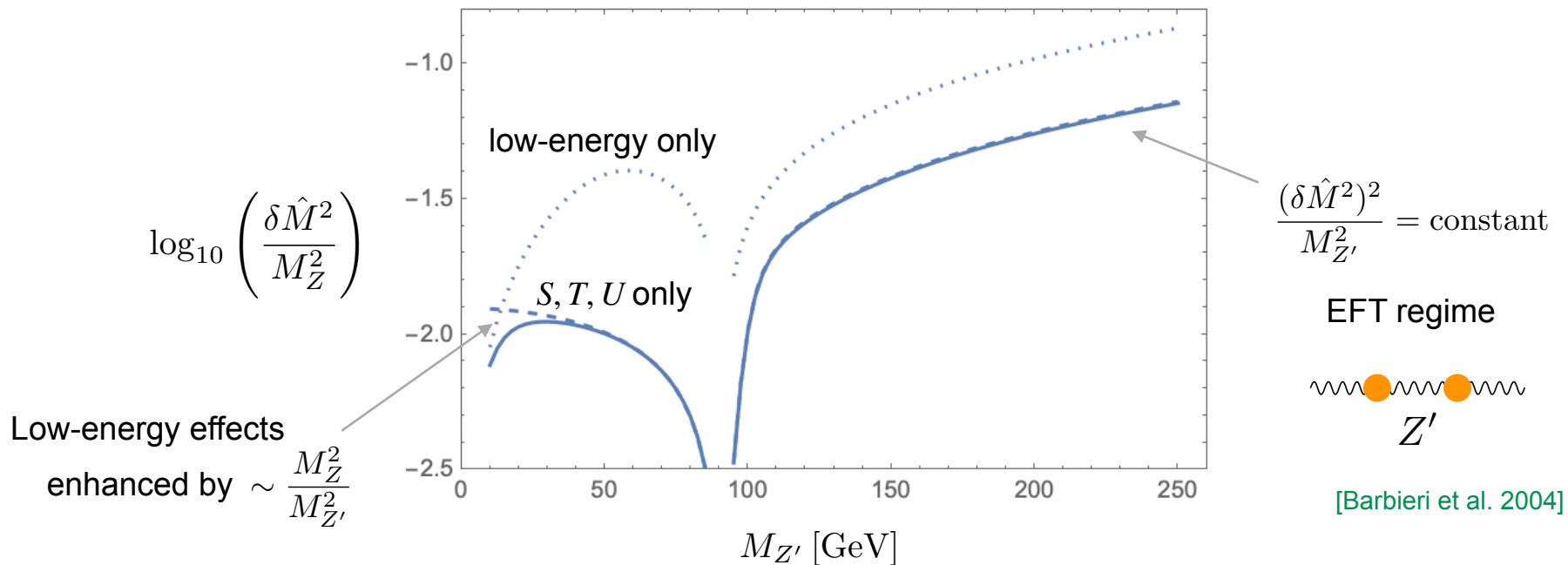
assume $N_f = 2$ dark flavors
 $\rightarrow N_f^2 - 1 = 3$ dark pions

Electroweak precision constraints

- Z pole couplings and W mass $\rightarrow S, T, U$ parameters
- Add low-energy data (atomic parity violation, ee, ep scattering)

[Peskin, Takeuchi 1992]

[Altarelli et al. 1991]



[Barbieri et al. 2004]

[Here results for zero kinetic mixing, complete analysis in paper.]

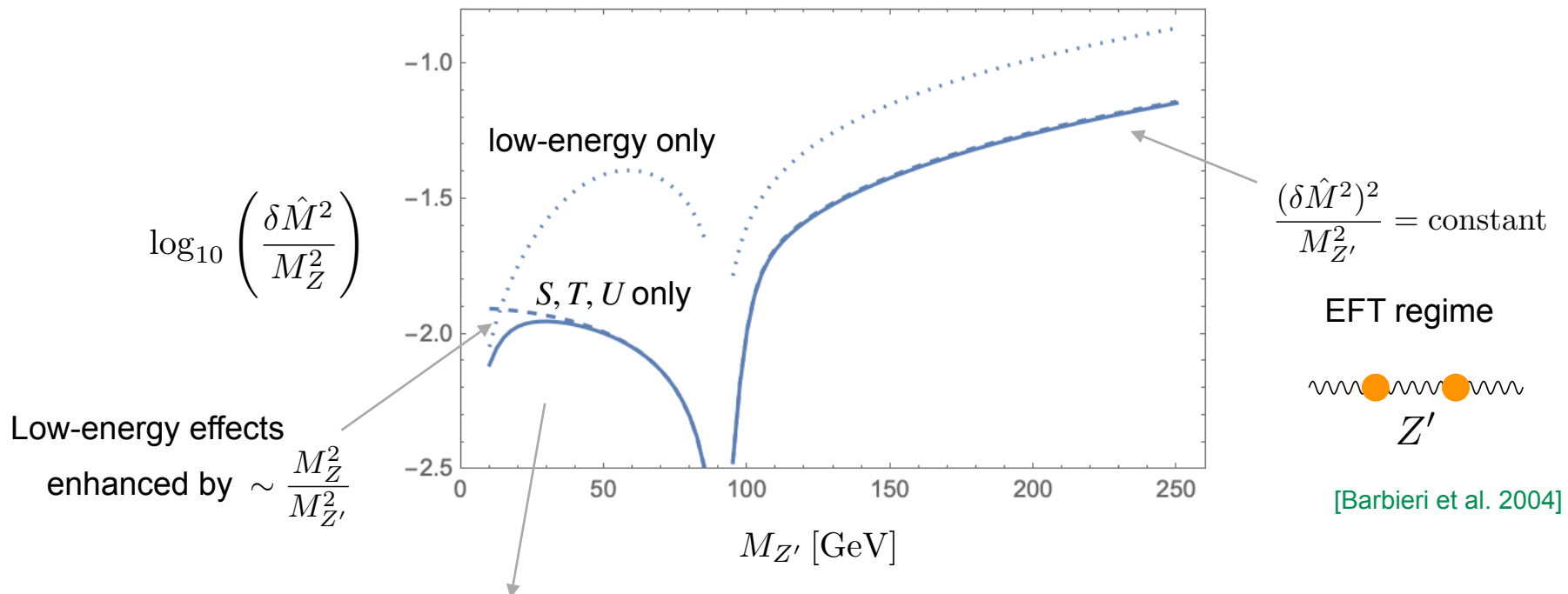
S, T, U fit has flat direction for $\varepsilon \approx -\delta \hat{M}^2 / (s_W M_Z^2)$, lifted by low-energy data]

Electroweak precision constraints

- Z pole couplings and W mass $\rightarrow S, T, U$ parameters
- Add low-energy data (atomic parity violation, ee, ep scattering)

[Peskin, Takeuchi 1992]

[Altarelli et al. 1991]



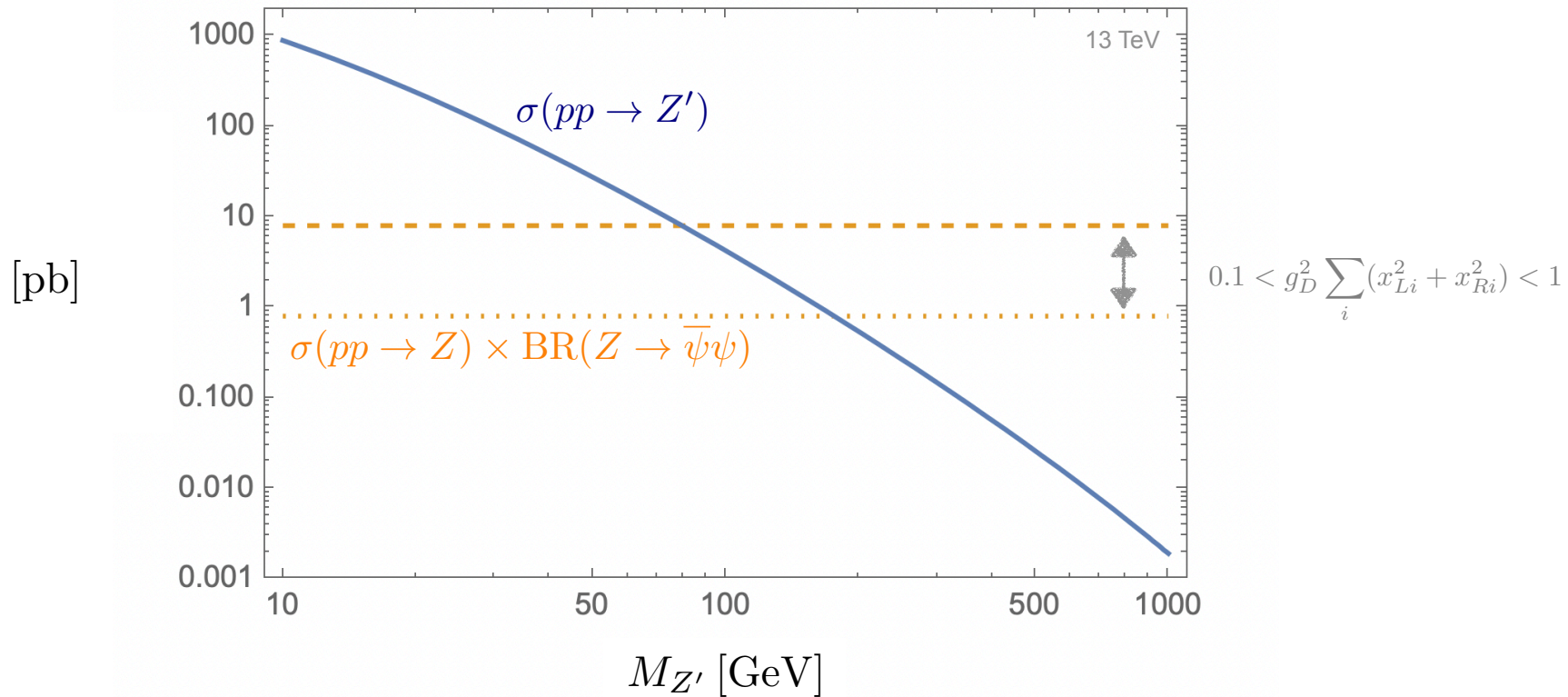
For light Z' , bound is approximately $\frac{\delta \hat{M}^2}{M_Z^2} \approx \xi \lesssim 10^{-2}$

mixing angle between Z and Z'

Phenomenology

Dark sector production at the LHC: Z' versus Z

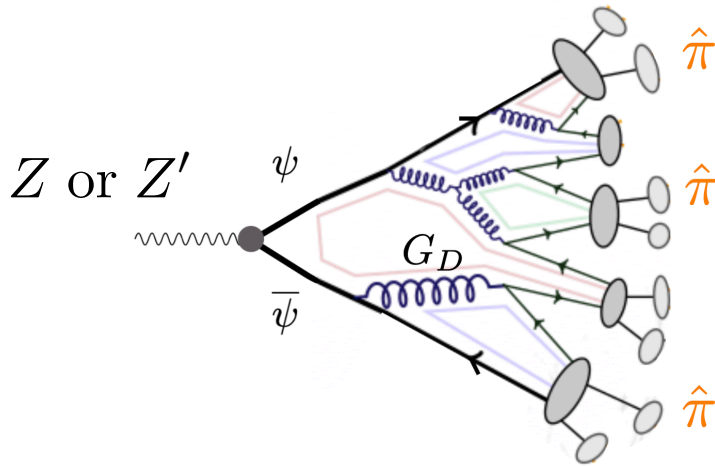
(mixing angle $\xi = 0.01$)



A light Z' gives a large rate of dark sector events, consistently with EW precision

Phenomenology

Signals: dark shower events versus FCNC decays of SM mesons



$$B \rightarrow K \hat{\pi}$$

$$\text{BR} \approx 10^{-8} \left(\frac{1 \text{ PeV}}{f_a} \right)^2 \left(\frac{\mathcal{K}_t}{10} \right)^2$$

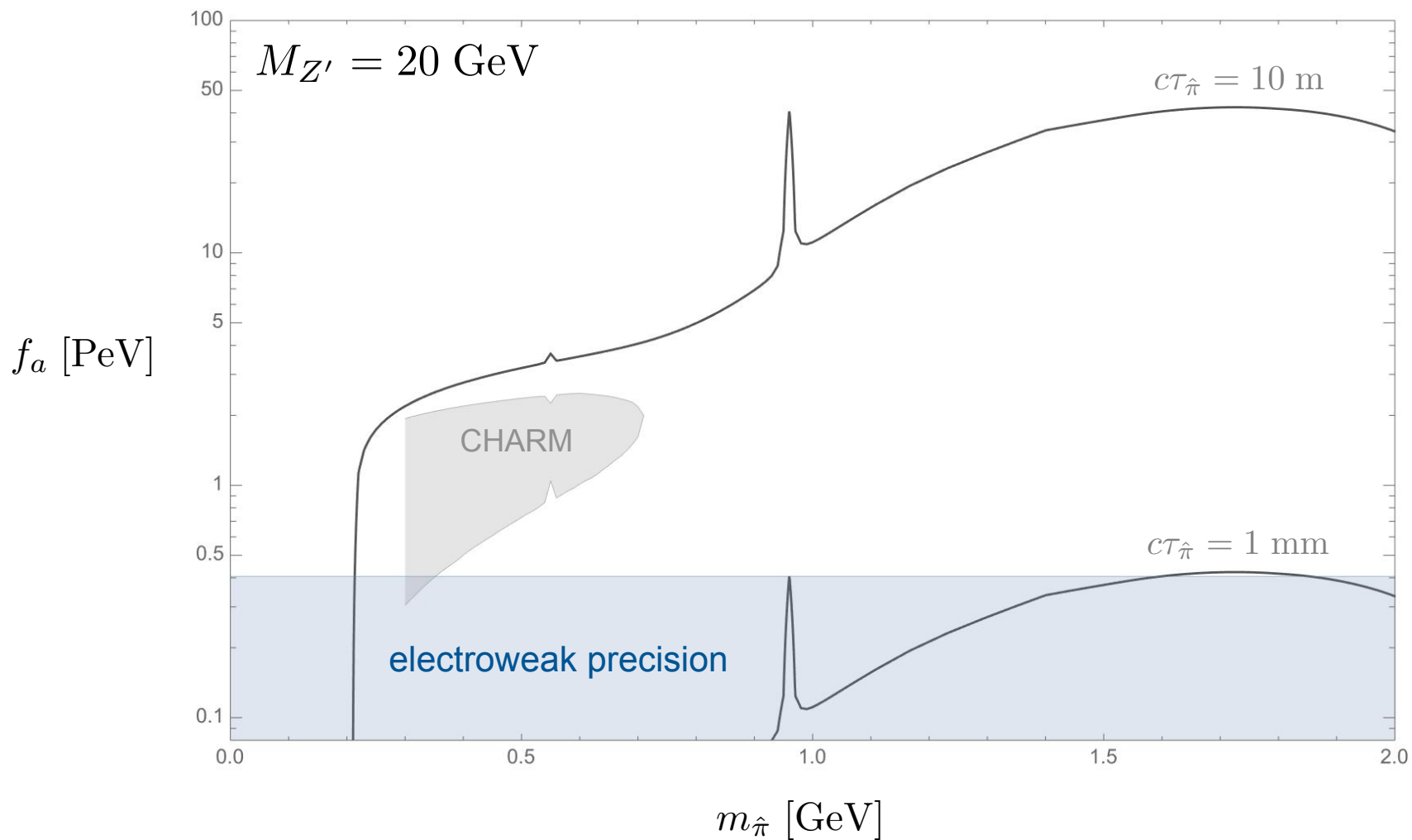
loop function
↖

Emerging jets (mix of macroscopic lifetimes)
 No hard SM objects automatically associated
 → **trigger** is key issue, focus on $\hat{\pi} \rightarrow \mu^+ \mu^-$
 Distinctive feature of confining dark sector

General probe of light
 new particles

Only sensitive to f_a

Constraints: pre-LHC



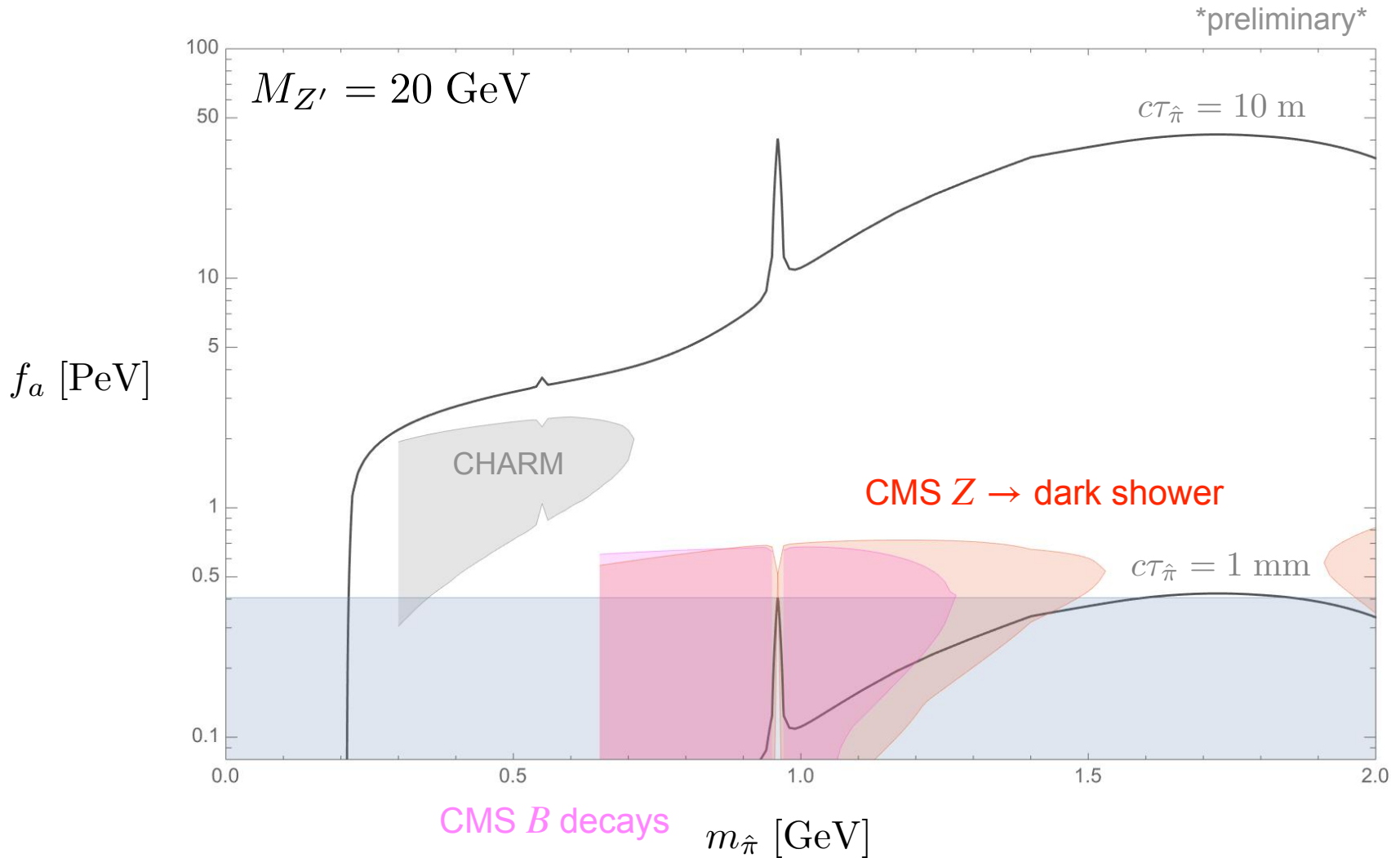
(traded $Z - Z'$ mixing for f_a)

$$\text{Tr}(\sigma_{1,3} \mathbf{X}'_A) = 1$$

$\hat{\pi}_2$ collider stable

$$g_D = 0.25, f_{\hat{\pi}} = 1 \text{ GeV}$$

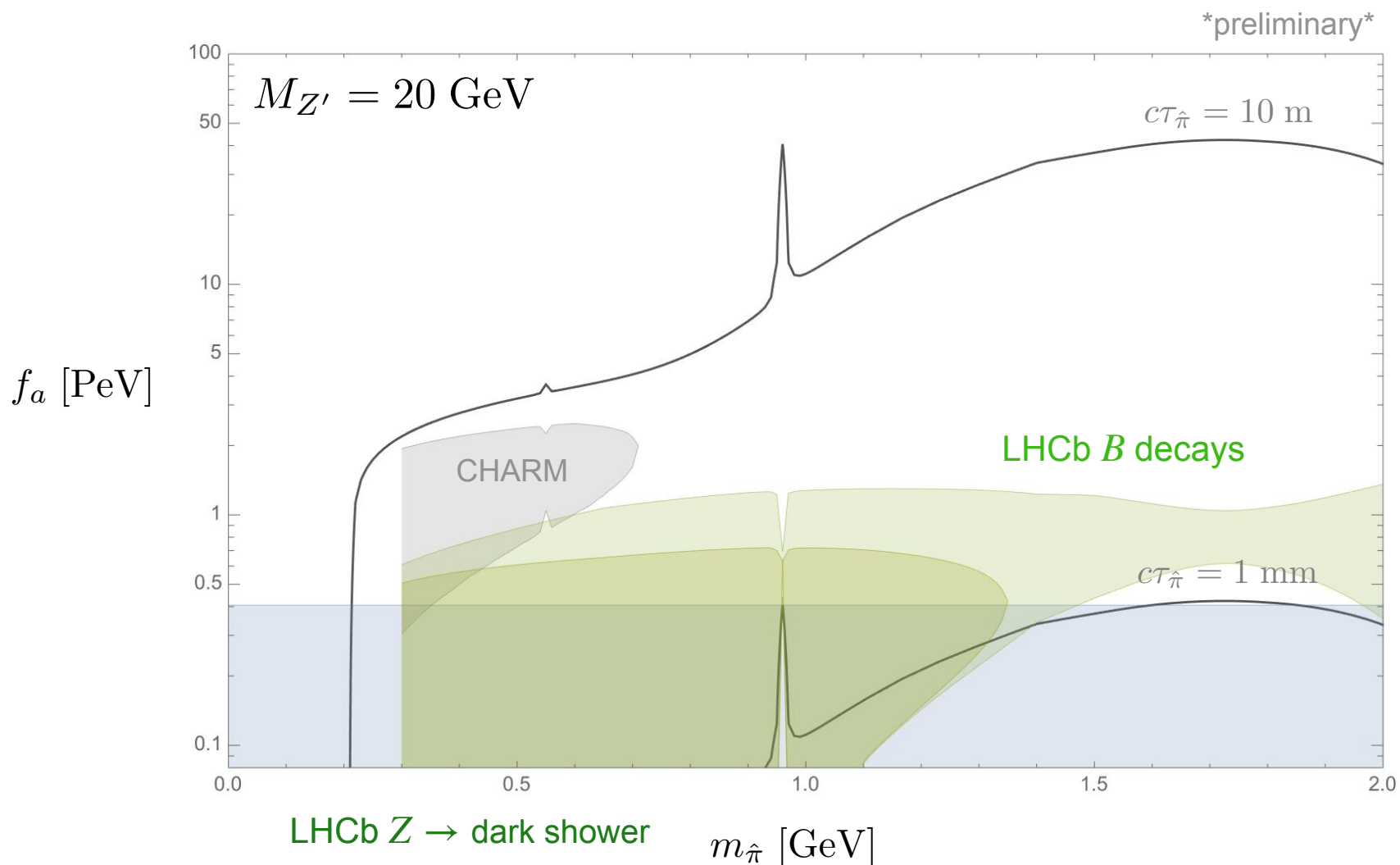
Constraints: CMS



We recast the CMS scouting search for displaced dimuons
to dark shower signal

[CMS 2112.13769]

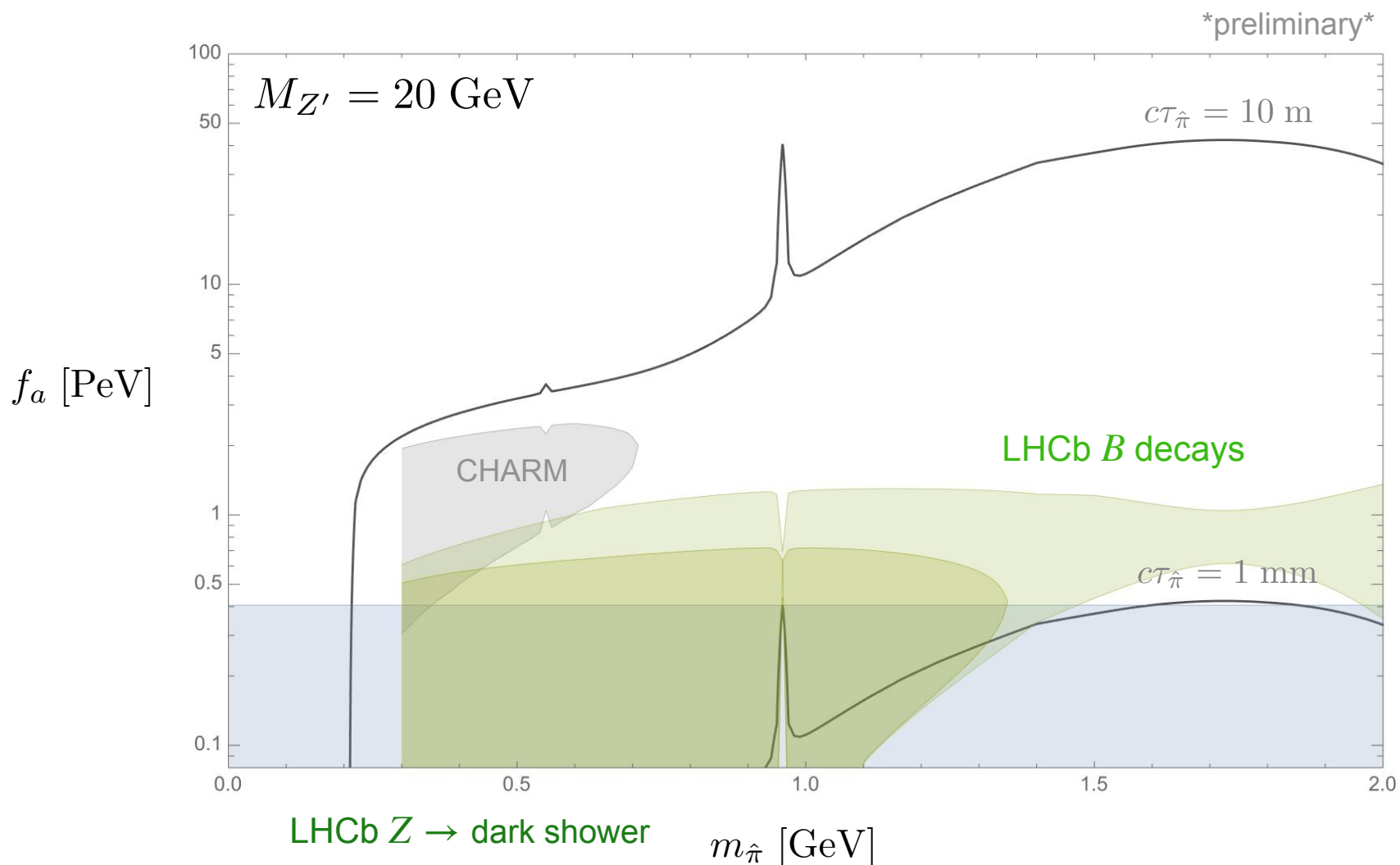
Constraints: LHCb



We recast the LHCb search for low-mass dimuon resonances
to dark shower signal

[LHCb 2007.03923]

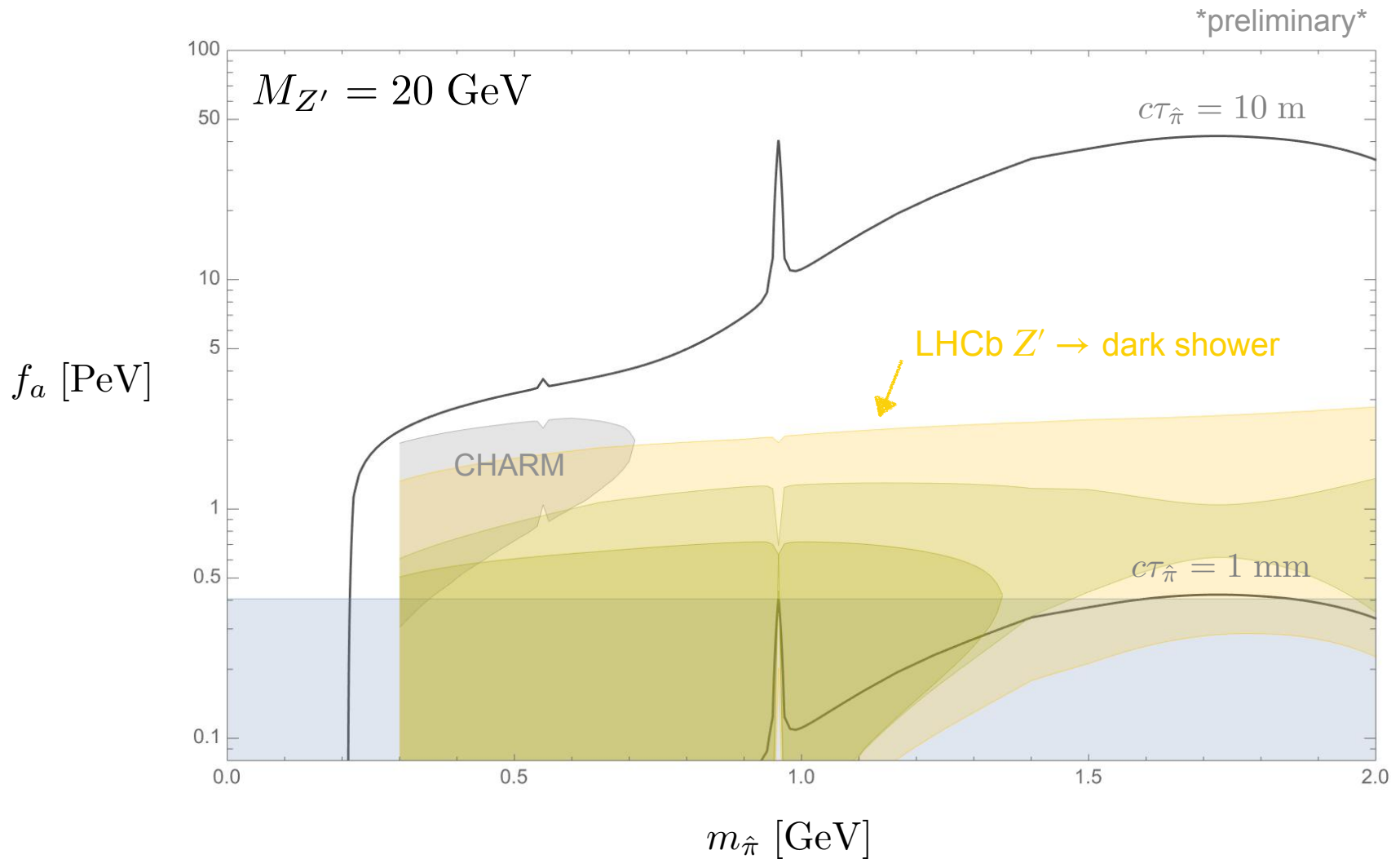
Constraints: LHCb



Z decay exclusions depend on underlying parameters (e.g. $f_{\hat{\pi}}$)

B decay exclusions do not

Constraints: LHCb



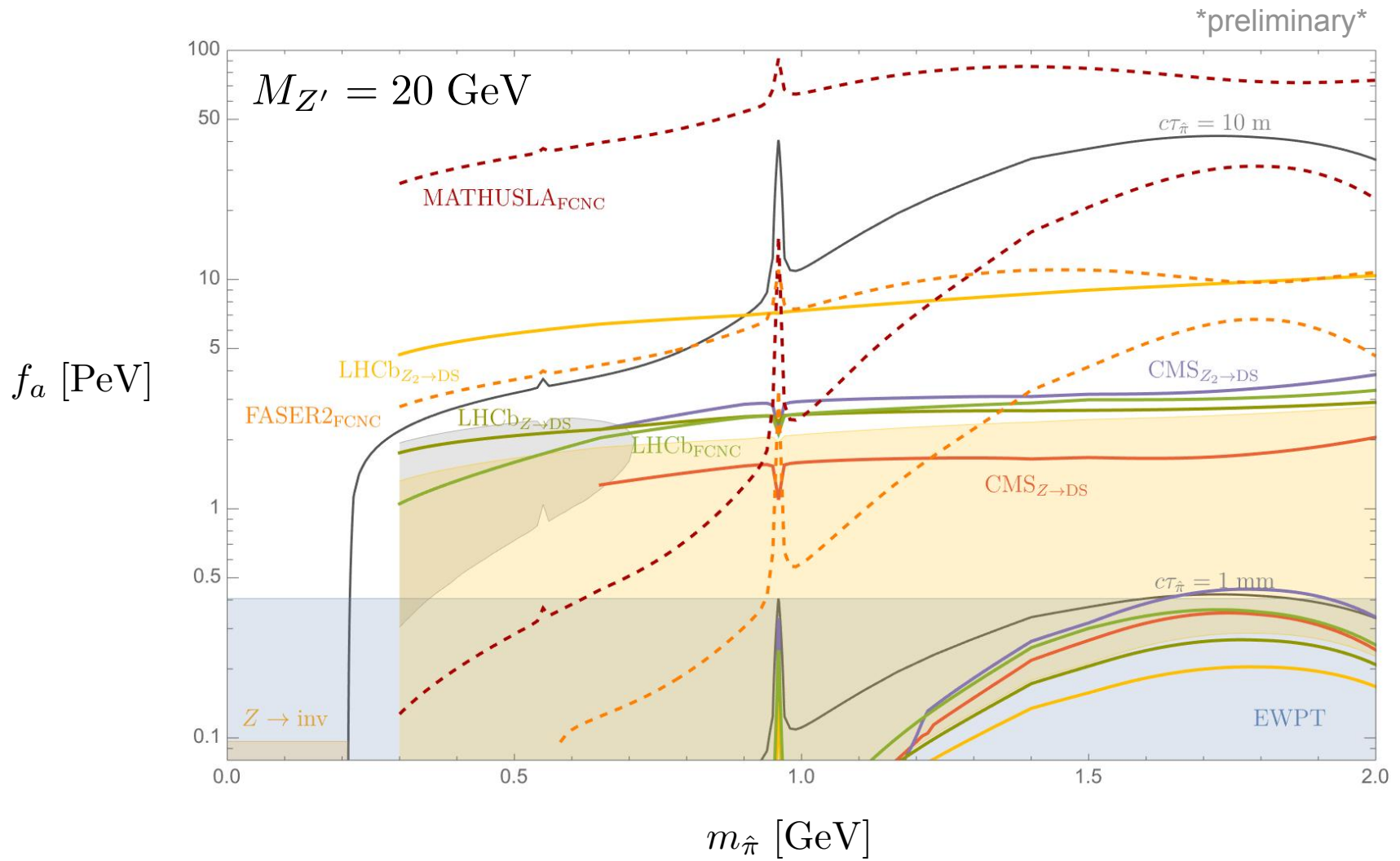
Dark shower signal initiated by light Z' can be powerfully tested by LHCb

Summary

- More than 10^{11} Z bosons @ LHC: can it be the portal to a confining dark sector?
- Dark pions behave as composite ALPs. Electroweak precision constraints automatically make them LLPs, leading to dark shower signatures
- Two classes of models. Here focused on completion by (light) Z' with mass mixing
- Presented recasts of CMS and LHCb searches for light dimuon resonances: dark shower sensitivity competes with FCNC B meson decays
- Much left to do, starting with hadronic ALP decays.
For instance, we find $a \rightarrow \pi^+ \pi^- \pi^0$ dominates for $m_a \gtrsim 1$ GeV

Extra slides

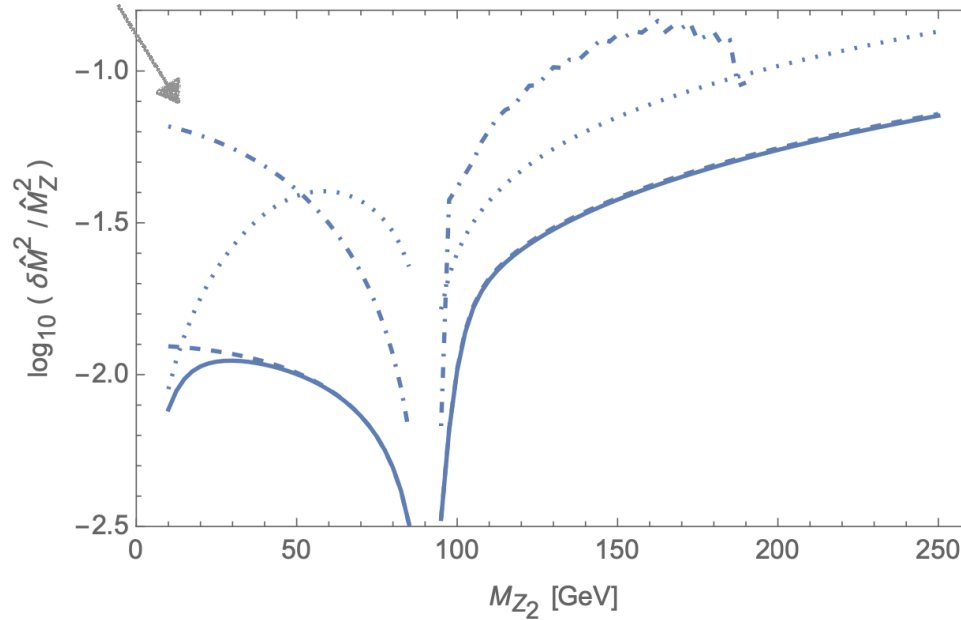
Partial set of projections



(here the Z' is called Z_2)

More on EW precision

DELPHI $e^+e^- \rightarrow \gamma(Z_2 \rightarrow \text{inv})$



$$S = \frac{4s_W^2}{\alpha} \left(\frac{c_W^2}{s_W} \xi t_\chi - c_W^2 \xi^2 \right), \quad T = \frac{1}{\alpha} \left(2s_W \xi t_\chi + \xi^2 \left(\frac{M_{Z_2}^2}{M_{Z_1}^2} - 2 \right) \right), \quad U = \frac{4s_W^2}{\alpha} c_W^2 \xi^2,$$

$$\mathcal{L}_{Z_1 f \bar{f}} = -\frac{\bar{Z} e}{s_W c_W} \bar{f} \gamma^\mu (T_{L f}^3 - s_*^2 Q_f) f Z_{1\mu},$$

$$\bar{Z} = 1 + \frac{\alpha T}{2}, \quad s_*^2 = s_W^2 + \frac{\alpha}{c_W^2 - s_W^2} \left(\frac{S}{4} - s_W^2 c_W^2 T \right),$$

$$\frac{M_W^2}{M_Z^2} = c_W^2 + \frac{\alpha c_W^2}{c_W^2 - s_W^2} \left(-\frac{S}{2} + c_W^2 T + \frac{c_W^2 - s_W^2}{4s_W^2} U \right).$$

(here the Z is called Z_1
and $\varepsilon \equiv \sin \chi$)

More on EW precision/2

B.1 Oblique parameters for heavy dark Z'

For $M_{Z_2} \gg M_{Z_1}$, the dark Z' can be integrated out to obtain an effective Lagrangian at the weak scale. In the parametrization of Ref. [10], Eqs. (3.5) and (3.6) are replaced by expressions that depend on W, Y, V, X in addition to \hat{S}, \hat{T} and \hat{U} ,

$$\bar{Z} = 1 + \frac{1}{2} \left[\hat{T} - W - \frac{s_W^2}{c_W^2} Y + 2 \frac{s_W}{c_W} X \right], \quad (\text{B.11})$$

$$s_*^2(M_Z^2) - s_W^2 = \frac{1}{c_W^2 - s_W^2} \left[s_W^2 \hat{S} - s_W^2 c_W^2 \hat{T} - s_W^4 W + \frac{s_W}{c_W} (1 - 2s_W^2 c_W^2) X - s_W^2 c_W^2 Y \right],$$

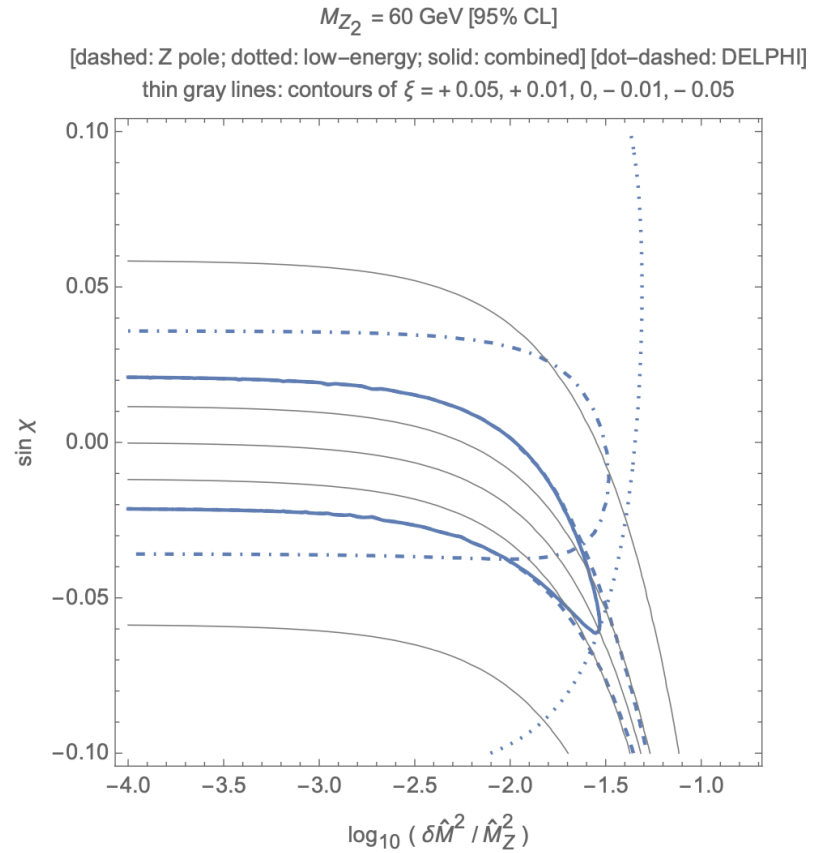
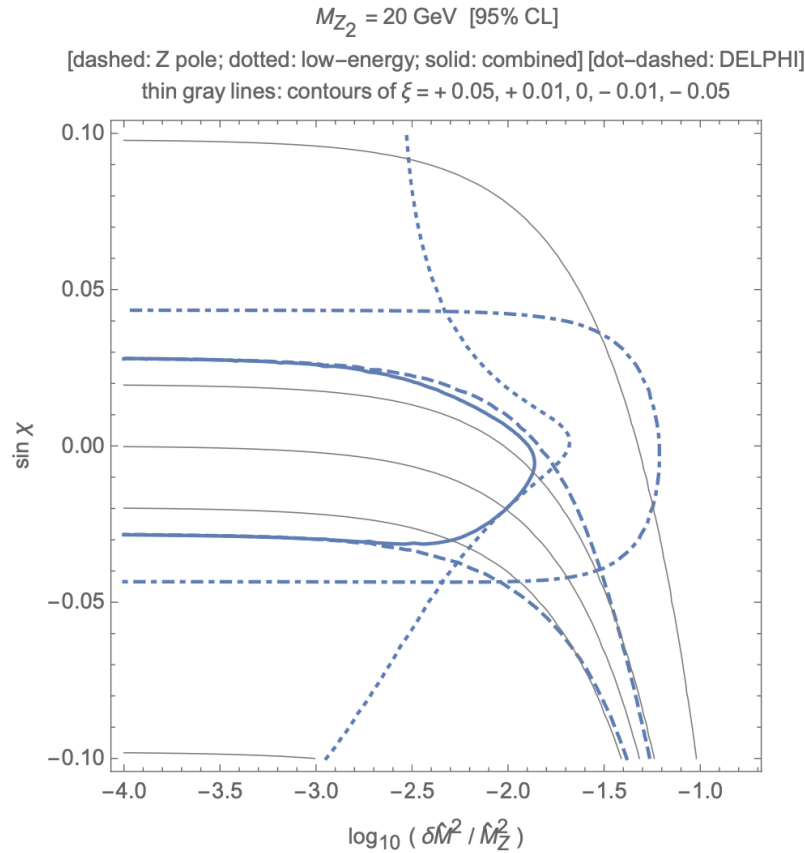
$$\frac{M_W^2}{M_Z^2} - c_W^2 = \frac{c_W^2}{c_W^2 - s_W^2} \left[-2s_W^2 \hat{S} + c_W^2 \hat{T} - (c_W^2 - s_W^2)(\hat{U} - V) - 2s_W c_W X + s_W^2 (W + Y) \right].$$

Integrating out the \hat{Z}' at tree level from Eqs. (2.3) and (2.4), we obtain

$$\begin{aligned} \hat{S} &= -\frac{\hat{c}_W^2}{\hat{s}_W} \frac{\delta \hat{M}^2}{\hat{M}_{Z'}^2} \left(\sin \chi + \hat{s}_W \frac{\delta \hat{M}^2}{\hat{M}_{Z'}^2} \right), & \hat{T} &= \hat{c}_W^2 \frac{(\delta \hat{M}^2)^2}{M_W^2 \hat{M}_{Z'}^2}, \\ \hat{U} &= -\hat{c}_W^2 \frac{(\delta \hat{M}^2)^2}{\hat{M}_{Z'}^4}, & W = V &= \hat{c}_W^2 \frac{M_W^2 (\delta \hat{M}^2)^2}{\hat{M}_{Z'}^6}, & Y &= \frac{M_W^2}{\hat{M}_{Z'}^2} \left(\sin \chi + \hat{s}_W \frac{\delta \hat{M}^2}{\hat{M}_{Z'}^2} \right)^2, \\ X &= -\hat{c}_W \frac{M_W^2 \delta \hat{M}^2}{\hat{M}_{Z'}^4} \left(\sin \chi + \hat{s}_W \frac{\delta \hat{M}^2}{\hat{M}_{Z'}^2} \right). \end{aligned} \quad (\text{B.12})$$

We observe that $\hat{S} = (\hat{c}_W/\hat{s}_W)(\hat{M}_{Z'}^2/M_W^2)X$ and $\hat{T} = -(\hat{M}_{Z'}^2/M_W^2)\hat{U} = (\hat{M}_{Z'}^4/M_W^4)V$, explicitly illustrating the well-known fact that \hat{S}, \hat{T}, W, Y are sufficient to describe heavy universal new physics [10].

More on EW precision/3



FCNC B meson decays

$$\mathcal{L}_{\text{eff}}^{\text{FCNC}} = -g_D \hat{g}_Z \frac{\delta \hat{M}^2}{M_{Z_1}^2 M_{Z_2}^2 \cos^2 \chi} \frac{\hat{g}^2}{128\pi^2} J_D^\mu \bar{d}_j \gamma_\mu P_L d_i \sum_{q \in u, c, t} V_{qj}^* V_{qi} \mathcal{K}_q + \text{h.c.} , \quad (6.1)$$

where

$$\mathcal{K}_q \equiv x_q \log \frac{\Lambda_{\text{UV}}^2}{M_W^2} + \frac{-7x_q + x_q^2}{2(1-x_q)} - \frac{4x_q - 2x_q^2 + x_q^3}{(1-x_q)^2} \log x_q , \quad (6.2)$$

with the definition $x_q \equiv m_q^2/M_W^2$. The contribution from $q = t$ dominates. The residual divergence appears because our treatment of the Z - Z' mixing is not UV complete. The divergence will be removed in a complete model where the new fields inducing $\delta \hat{M}^2$, such as a second Higgs doublet, are included dynamically. In that case Λ_{UV} would be set by the mass of the charged Higgs scalar, possibly up to $O(1)$ factors. Numerically, the dimensionless quantity \mathcal{K}_t varies from 5.0 to 16 as Λ_{UV} is increased from 300 GeV to 1 TeV, signaling an important theoretical uncertainty.

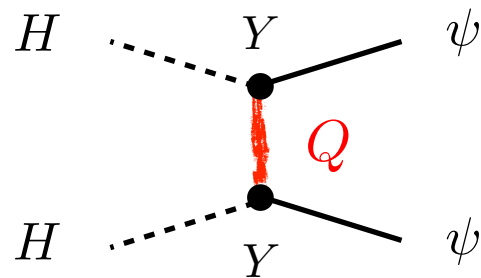
$$\text{BR}(B^{+,0} \rightarrow \{K^+ \hat{\pi}_b, K^{*0} \hat{\pi}_b\}) \approx \{0.92, 1.1\} \times 10^{-8} \left(\frac{1 \text{ PeV}}{f_a^{(b)}} \right)^2 \left(\frac{\mathcal{K}_t}{10} \right)^2 \{ \lambda_{BK\hat{\pi}}^{1/2}, \lambda_{BK^*\hat{\pi}}^{3/2} \}$$

Model with heavy fermions Q

- Dark QCD with confinement scale Λ
- N light dark quarks ψ , SM singlets
- N heavy dark quarks Q , with SM electroweak charges

$$\mathcal{L}_{\text{UV}} = \overline{Q}_L \mathbf{Y} \psi_R H + \overline{Q}_R \tilde{\mathbf{Y}} \psi_L H + \overline{Q}_L \mathbf{M} Q_R + \overline{\psi}_L \boldsymbol{\omega} \psi_R$$

$$\omega, \frac{Y \tilde{Y} v^2}{M} \ll \Lambda \quad \rightarrow \quad (N^2 - 1) \text{ pNGBs} \quad \text{“dark pions”}$$

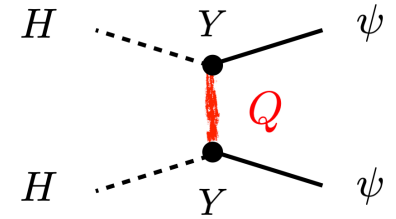


$$M \gtrsim \text{TeV}$$

heavy mediators

Dark pions

- Integrate out heavy fermions Q



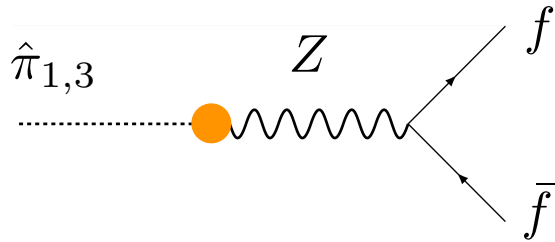
$$\mathcal{L}_{\text{EFT}} \sim (\bar{\psi}_R \mathbf{Y}^\dagger M^{-2} \mathbf{Y} \gamma^\mu \psi_R) (iH^\dagger D_\mu H) + (\bar{\psi}_L \tilde{\mathbf{Y}}^\dagger M^{-2} \tilde{\mathbf{Y}} \gamma^\mu \psi_L) (iH^\dagger D_\mu H)$$

Z portal (dim-6)

$$- \bar{\psi}_L \boldsymbol{\omega} \psi_R + \bar{\psi}_L \tilde{\mathbf{Y}}^\dagger M^{-1} \mathbf{Y} \psi_R |H|^2$$

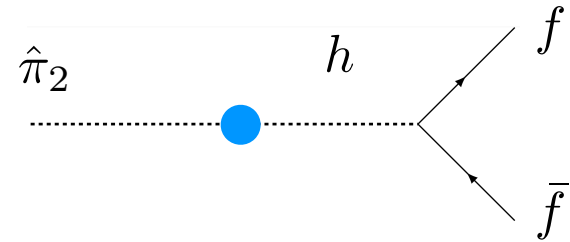
Higgs portal (dim-5)

- $N = 2$ flavors: dark pions $\hat{\pi}_a \sim \bar{\psi} i \sigma_a \gamma_5 \psi$



$$J^{PC} = 0^{-+}$$

composite ALP

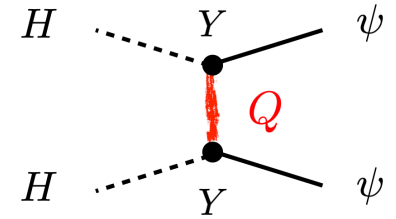


$$J^{PC} = 0^{--}$$

composite Higgs-mixed scalar

Dark pions

- Integrate out heavy fermions Q



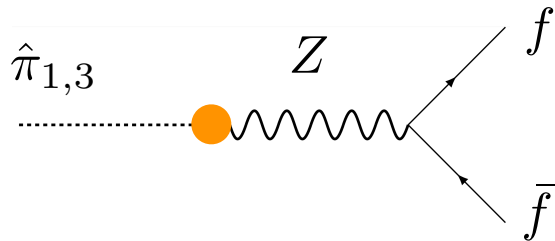
$$\mathcal{L}_{\text{EFT}} \sim (\bar{\psi}_R \mathbf{Y}^\dagger \mathbf{M}^{-2} \mathbf{Y} \gamma^\mu \psi_R) (iH^\dagger D_\mu H) + (\bar{\psi}_L \tilde{\mathbf{Y}}^\dagger \mathbf{M}^{-2} \tilde{\mathbf{Y}} \gamma^\mu \psi_L) (iH^\dagger D_\mu H)$$

Z portal (dim-6)

$$- \bar{\psi}_L \omega \psi_R + \bar{\psi}_L \tilde{\mathbf{Y}}^\dagger \mathbf{M}^{-1} \mathbf{Y} \psi_R |H|^2$$

Higgs portal (dim-5)

- $N = 2$ flavors: dark pions $\hat{\pi}_a \sim \bar{\psi} i \sigma_a \gamma_5 \psi$



$$J^{PC} = 0^{-+}$$

composite ALP

$$\mathcal{L}_{\text{eff}} \supset -\frac{\partial_\mu a}{f_a} \sum_f c_f \bar{f} \gamma^\mu \gamma_5 f$$

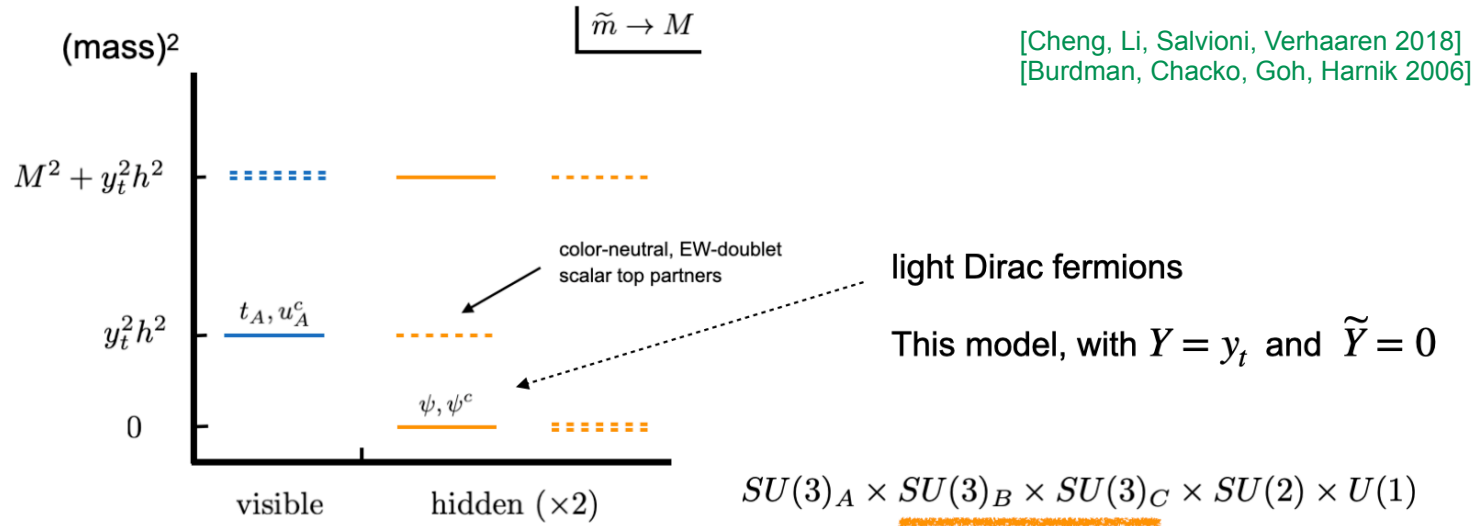
$$c_f = T_L^3(f)$$

isospin-violating couplings
to SM fermions

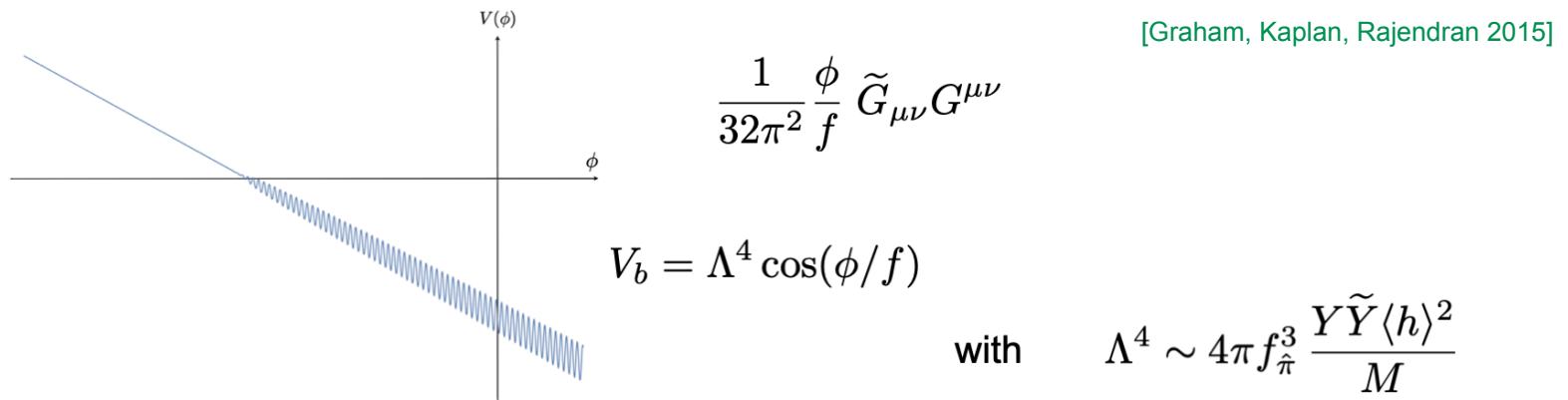
$$f_a \sim \frac{M^2}{Y^2 f_{\hat{\pi}}} = 1 \text{ PeV} \left(\frac{M/Y}{\text{TeV}} \right)^2 \left(\frac{1 \text{ GeV}}{f_{\hat{\pi}}} \right)$$

Ultraviolet motivations

“Tripled Top” framework for neutral naturalness: accidental SUSY of the spectrum



Non-QCD version of the relaxion: new fermions generate backreaction potential



Dark showers @ LHCb

$Z \rightarrow$ dark jets probes new direction in parameter space

