

# Exclusive $b$ -quark decays

– Projects C2a and C2b –

CRC Annual Meeting  
March 2024

Thorsten Feldmann

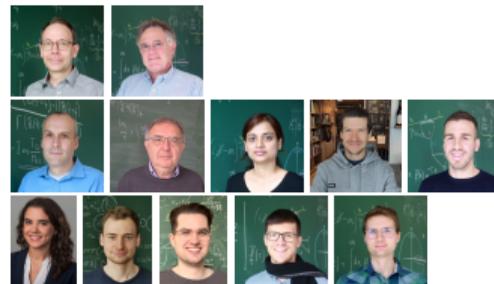
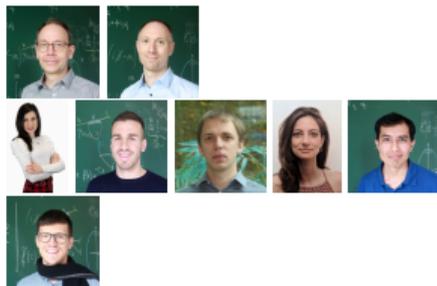


TP1 Theoretical  
Particle Physics  
CPPS Center for Particle  
Physics Siegen



### C2a: Hadronic matrix elements and exclusive semileptonic decays

- WA1: Factorization and light-cone distributions
- WA2: QCD sum rules and related methods
- WA3: New channels and multi-hadron final states
- WA4: Inclusive rates and the sum over exclusive channels, Semi-inclusive decays



### C2b: Exclusive non-leptonic and rare $b$ -quark decays

- WA1: Higher-order QCD corrections
- WA2: Phenomenology of non-leptonic decays
- WA3: Phenomenology of rare decays, BSM flavour structures

new members since fall 2023: Anshika Bansal (C2a), Jack Jenkins (C2b)

- 1 T. Feldmann, P. Lüghausen and N. Seitz,  
“Strange-quark mass effects in the  $B_s$  meson’s light-cone distribution amplitude,”  
JHEP **08** (2023), 075 [arXiv:2306.14686 [hep-ph]].
- 2 T. Feldmann and N. Gubernari,  
“Non-factorisable Contributions of Strong-Penguin Operators in  $\Lambda_b \rightarrow \Lambda \ell^+ \ell^-$  Decays,” ↔ C2b  
[arXiv:2312.14146 [hep-ph]] (to appear in JHEP).
- 3 P. Böer, G. Bell, T. Feldmann, D. Horstmann and V. Shtabovenko,  
“Soft-overlap contribution to  $B_c \rightarrow \eta_c$  form factors: diagrammatic resummation of double logarithms,”  
PoS **RADCOR2023** (2024), 086 [arXiv:2309.08410 [hep-ph]] ↔ B1e  
(detailed write-up in preparation)

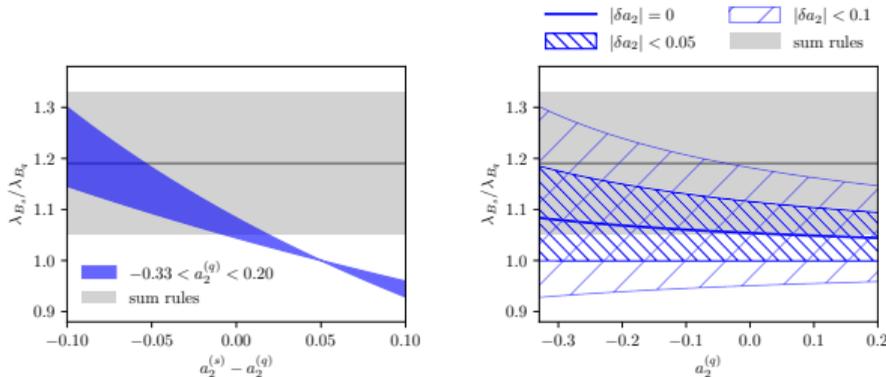
short-distance OPE of light-ray operator in HQET: ( $n^2 = 0$ )

$$\begin{aligned} & \bar{q}(\tau n)[\tau n, 0] \not{n} \gamma_5 h_v(0) \\ = & c_1^{(3)}(\tau) \bar{q} \not{n} \gamma_5 h_v + c_1^{(4)}(\tau) \bar{q} (i n \cdot \overleftarrow{D}) \not{n} \gamma_5 h_v \\ & + c_2^{(4)}(\tau) \bar{q} (i v \cdot \overleftarrow{D}) \not{n} \gamma_5 h_v + c_3^{(4)}(\tau) m_s \bar{q} \not{n} \gamma_5 h_v \\ & + \dots \end{aligned}$$

T. Feldmann, P. Lüghausen and N. Seitz, JHEP **08** (2023), 075

- short-distance behaviour of LCDA  $\tilde{\phi}_{B_s}^+(\tau)$  in terms of HQET parameters ( $\bar{\Lambda}_s = m_{B_s} - m_b$  etc.)
- 1-loop calculation of Wilson coefficient  $c_3^{(4)}(\tau)$
- extrapolation to large  $\tau \sim 1/\Lambda_{\text{had}}$  by means of generic parametrization

[TF, P. Lüghausen and D. van Dyk, JHEP **10** (2022), 162]



estimates for first inverse moments

$$\lambda_B^{-1} = \int \frac{d\omega}{\omega} \phi_B^+(\omega)$$

- our results for  $\lambda_{B_q}$  and  $\lambda_{B_s}$  compare well with QCD sum rule estimates ✓

[A. Khodjamirian, R. Mandal and T. Mannel, JHEP **10** (2020), 043]

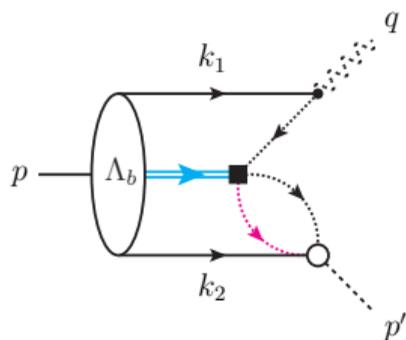
- OPE and QCD-SR constraints can be used consistently in global fits ✓

[TF, Lüghausen, van Dyk, [work in progress](#)]

T. Feldmann and N. Gubernari, arXiv:2312.14146 (to appear in JHEP)

- sum-rule approach to  $\Lambda_b \rightarrow \Lambda \gamma^*$  with interpolating current for  $\Lambda$
- leads to "annihilation-like" decay topologies with 4-quark operators:

$$\blacksquare = (\bar{s} \dots b)(\bar{q} \dots q)$$



- light-quark momenta  $(k_1, k_2)$  couple to external momenta  $(q, p')$  in *different* light-cone directions
- requires specific "soft  $\Lambda_b$  functions", where light-quark fields are separated along *different* light rays

$$\langle 0 | d(\tau_2 \bar{n}) u(\tau_1 n) h_v^{(b)}(0) | \Lambda_b(p) \rangle$$

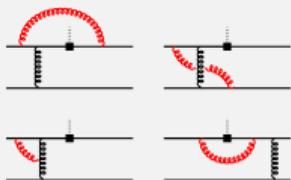
- need to generalize and model 3-quark LCDAs for  $\Lambda_b$  ✓
- expect similar new features as for soft  $B$ -meson functions, with additional photons or gluons in opposite light-cone direction

e.g. [M. Beneke, P. Böer, J. N. Toelstede and K. K. Vos, JHEP **08** (2022), 020],

[Y. K. Huang, Y. Ji, Y. L. Shen, C. Wang, Y. M. Wang and X. C. Zhao, arXiv:2312.15439 [hep-ph]]

to be worked out ...

Sudakov logs from (on-shell) soft gluons:



standard exponentiation:

$$\exp \left[ -\frac{\alpha_s C_F}{2\pi} \ln \frac{p_-}{k_-} \ln \frac{\ell_+}{k_+} \right]$$

endpoint logs from (on-shell) soft quarks:

iterative pattern  
of double convolutionssimilar to  $e\mu$  backward scattering[Bell, Böer, Feldmann, JHEP **09** (2022), 183]tower of large double logs  $(\alpha_s \ln^2 \frac{p_-}{m})^n$  encoded in coupled integral equations for "soft form factors"

$$f(\ell_+, \ell_-) = 1 + \frac{\alpha_s C_F}{2\pi} \int_{\ell_-}^{p_-} \frac{dk_-}{k_-} \int_{m^2/k_-}^{\ell_+} \frac{dk_+}{k_+} e^{-S(k_+, k_-)} \left( f(k_+, k_-) - \frac{C_{FA}}{2C_F} f_m(k_+, k_-) + \frac{C_A}{4C_F} \right)$$

$$f_m(\ell_+, \ell_-) = 1 + \frac{\alpha_s C_F}{2\pi} \int_{\ell_-}^{p_-} \frac{dk_-}{k_-} \int_{m^2/k_-}^{\ell_+} \frac{dk_+}{k_+} e^{-S(k_+, k_-)} f_m(k_+, k_-)$$

→ iterative solution ✓

asymptotic behaviour ✓

→ see also Guido Bell's presentation

- 1 N. Gubernari, A. Khodjamirian, R. Mandal and T. Mannel,  
“ $B \rightarrow D_0^*$  and  $B_s \rightarrow D_{s0}^*$  form factors from QCD light-cone sum rules,”  
JHEP **12**, 015 (2023)
- 2 S. Descotes-Genon, A. Khodjamirian, J. Virto and K. K. Vos,  
“Light-Cone Sum Rules for  $S$ -wave  $B \rightarrow K\pi$  Form Factors,”  
JHEP **06** (2023), 034. [arXiv:2304.02973 [hep-ph]].

N. Gubernari, A. Khodjamirian, R. Mandal and T. Mannel, JHEP **12** (2023), 015

- estimates of  $b \rightarrow c\ell\nu$  decays into excited D-mesons are important to understand the gap between inclusive  $b \rightarrow c\ell\nu$  and sum over exclusive channels

→ WA4

- previous analysis for axial-vector mesons ( $J^P = 1^+$ )
- here: for scalar D-mesons ( $J^P = 0^+$ )

[Gubernari, Khodjamirian, Mandal, Mannel, JHEP **05**, 029 (2022)]

## calculational setup:

- use LCSRs with  $B$ -meson LCDAs (i.e. large recoil, finite charm mass)
- include 2- and 3-particle LCDAs (incl. twist-4)
- decay constants from 2-point sum rules
- $z$ -expansion to extrapolate to small recoil

two different scenarios for scalar  $D$ -mesons:

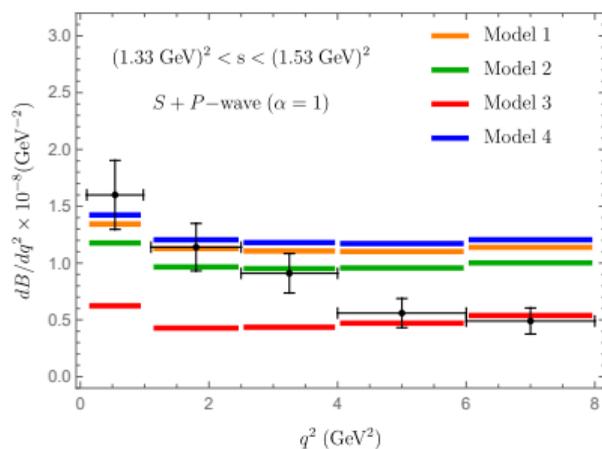
- one single broad resonance (PDG)
- two individual resonances (from  $B \rightarrow D\pi\pi$ ) → WA3

Scenario	Meson	Mass [MeV]	Width [MeV]
1	$D_0^* \equiv D_0^*(2300)$	$2343 \pm 10$	$229 \pm 16$
	$D_{s0}^* \equiv D_{s0}^*(2317)$	$2317.8 \pm 0.5$	$< 3.8$
2	$D_0^* \equiv D_0^*(2105)$	$2105_{-6}^{+8}$	$204_{-22}^{+20}$
	$D_0^* \equiv D_0^*(2451)$	$2451_{-35}^{+26}$	$268_{-16}^{+14}$
	$D_{s0}^* \equiv D_{s0}^*(2317)$	$2317.8 \pm 0.5$	$< 3.8$
	$D_{s0}^* \equiv D_{s0}^*(2660)$	$\sim 2660$	—

Scenario 1	Scenario 2
$\mathcal{B}(\bar{B}^0 \rightarrow D_0^* \ell \bar{\nu}) = (3.6_{-3.0}^{+5.1}) \cdot 10^{-3}$	$\mathcal{B}(\bar{B}^0 \rightarrow D_0^* \ell \bar{\nu}) = (1.6_{-1.4}^{+3.2}) \cdot 10^{-3}$
$\mathcal{B}(\bar{B}^0 \rightarrow D_0^* \tau \bar{\nu}) = (3.9_{-3.1}^{+5.1}) \cdot 10^{-4}$	$\mathcal{B}(\bar{B}^0 \rightarrow D_0^* \tau \bar{\nu}) = (2.4_{-2.1}^{+4.7}) \cdot 10^{-4}$
$\mathcal{B}(\bar{B}_s \rightarrow D_{s0}^* \ell \bar{\nu}) = (1.9_{-1.7}^{+3.8}) \cdot 10^{-3}$	$\mathcal{B}(\bar{B}^0 \rightarrow D_0^* \ell \bar{\nu}) = (2.3_{-1.8}^{+1.4}) \cdot 10^{-3}$
$\mathcal{B}(\bar{B}_s \rightarrow D_{s0}^* \tau \bar{\nu}) = (2.6_{-2.2}^{+4.9}) \cdot 10^{-4}$	$\mathcal{B}(\bar{B}^0 \rightarrow D_0^* \tau \bar{\nu}) = (1.9_{-1.4}^{+1.1}) \cdot 10^{-4}$

S. Descotes-Genon, A. Khodjamirian, J. Virto and K. K. Vos, JHEP **06** (2023), 034

- estimate of (non-resonant)  $B \rightarrow K\pi\ell^+\ell^-$  important for accurate analysis of  $B \rightarrow K^*\ell^+\ell^-$  → C2b
- earlier studies focused on P-wave contributions [Descotes-Genon, Khodjamirian, Virto, JHEP 12, 083 (2019)]
- standard LCSR setup with B-meson LCDAs (incl. twist-4)
- $S$ -wave  $K\pi$  spectrum from coupled-channel analysis, [Von Detten, Noel, Hanhart, Hoferichter, Kubis, Eur. Phys. J. C 81, no.5, 420 (2021)]  
→ 4 different models, fitted to  $K\pi$  scattering data

Comparison with LHCb data around  $K^*(1410)$ ,  $K^*(1430)$ 

- significant S-wave contribution (incl. interference with P-wave)
- correct order of magnitude
- unsatisfactory  $q^2$  dependence

→ refine the model for the  $K\pi$  spectrum

→ implications for other multi-hadron channels → WA3

$(B \rightarrow \pi\pi\ell\bar{\nu}, B \rightarrow \pi\pi\ell^+\ell^-, B \rightarrow K\pi\nu\bar{\nu}, B \rightarrow K\pi\pi,$   
 $B \rightarrow K\pi a, B \rightarrow K\pi\gamma', \dots)$

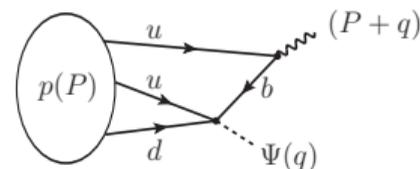
- A. Boushmelev and M. Wald,  
“Higher twist corrections to  $B$ -meson decays into a proton and dark antibaryon ...,”  
arXiv:2311.13482 [hep-ph]

- Mannel, Tetlalmatzi-Xolocotzi, Descotes-Genon, LHCb (Paris, LPTHE)  
improved description of non-resonant region for  $B^0 \rightarrow K^+ K^- K_S$   
including  $c\bar{c}$  threshold effects  
work in progress

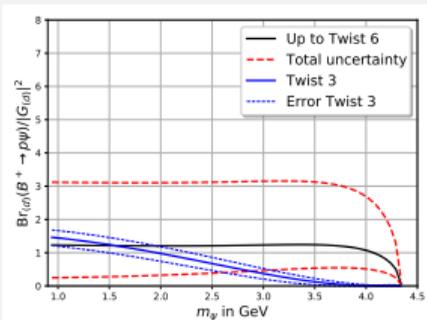
builds on [Mannel, Olschewsky, Vos, JHEP **06**, 073 (2020)]

[A. Bouchmelev and M. Wald, arXiv:2311.13482]

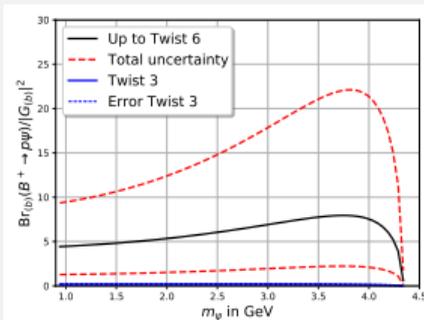
- certain NP models ("Mesogenesis") entertain the possibility of *B*-meson decays into dark baryons
- described in terms of (model-dependent) 4-fermion operators:
- focus on  $B^+ \rightarrow p\Psi$ : LCSR analysis with nucleon LCDAs (incl. twist-6)



$$-i G_{(d)} \epsilon_{ijk} (\bar{u}_R^i b_R^{cj}) (\bar{d}_R^k \psi_R^c) + \text{h.c.}$$



$$-i G_{(b)} \epsilon_{ijk} (\bar{u}_R^i d_R^{cj}) (\bar{b}_R^k \psi_R^c) + \text{h.c.}$$



- substantial uncertainties from higher-twist contributions
- branching fraction lies within the sensitivity range for Belle-II

- Mannel, Gubernari, Khodjamirian, Mandal,  
quantitative analysis of rates and decay spectra of  $B \rightarrow D^{**} \ell \nu$ ,  
work in progress ...

← input from WA2/WA3

- Huber et al., in the pipeline:
  - calculation of power-suppressed penguin coefficient  $a_6$  in QCDF
  - pheno update of charmless non-leptonics  
(requires better treatment of non-factorizable effects)

- 1 A. Biswas, S. Descotes-Genon, J. Matias and G. Tetlalmatzi-Xolocotzi,  
“A new puzzle in non-leptonic B decays,”  
JHEP **06** (2023), 108 [arXiv:2301.10542 [hep-ph]]
- 2 M. L. Piscopo and A. V. Rusov,  
“Non-factorisable effects in the decays  $\bar{B}_s^0 \rightarrow D_s^+ \pi^-$  and  $\bar{B}^0 \rightarrow D^+ K^-$  from LCSR,”  
JHEP **10** (2023), 180 [arXiv:2307.07594 [hep-ph]].

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more activities:

- E. Malami,  
“Theoretical Highlights of CP Violation in  $B$  Decays,”  
proceedings HQL2023, arXiv:2402.16976 [hep-ph]
  - E. Malami,  
“Manifestations of CP Violation in the B Meson System:  
Theoretical Perspective,”  
proceedings Beauty2023, arXiv:2402.10023 [hep-ph]
  - G. Tetlalmatzi-Xolocotzi,  
“QCDF Amplitudes from  $SU(3)$  Symmetries,”  
proceedings PoS **DISCRETE2022** (2024), 040
- also: Huber, Malami, GTX, **work in progress**
- include  $SU(3)_F$  breaking effects:  
 $(\bar{3} \oplus 6 \oplus \overline{15}) \otimes (1 \oplus 8) = \bar{3} \oplus 6 \oplus \overline{15} \oplus 24 \oplus \overline{42}$
  - translation to QCDF amplitudes
-

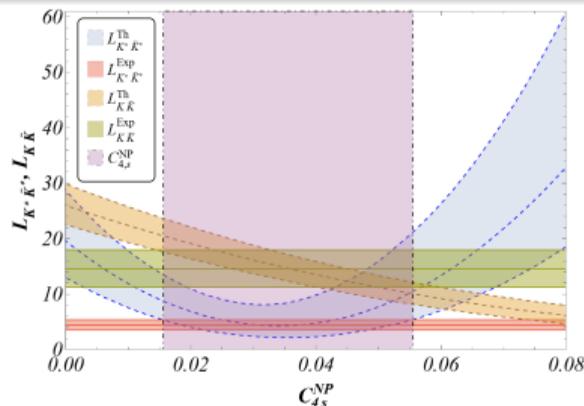
[A. Biswas, S. Descotes-Genon, J. Matias and G. Tetlalmatzi-Xolocotzi, JHEP **06** (2023), 108]

- starting point: ratio of longitudinal amplitudes of two U-spin related decays:

$$L_{K^* \bar{K}^*} = \rho(m_{K^{*0}}, m_{\bar{K}^{*0}}) \frac{\mathcal{B}(\bar{B}_s \rightarrow K^{*0} \bar{K}^{*0})}{\mathcal{B}(\bar{B}_d \rightarrow K^{*0} \bar{K}^{*0})} \frac{f_L^{B_s}}{f_L^{B_d}} = \frac{|A_0^s|^2 + |\bar{A}_0^s|^2}{|A_0^d|^2 + |\bar{A}_0^d|^2},$$

(expected to have reduced sensitivity to power corrections in QCDF)

- $K^* K^*$  and  $KK$  modes show  $\mathcal{O}(2.5\sigma)$  deviations from SM expectations
- could be explained by NP in strong penguins  $C_{4,6}$  or chromomagnetic penguin  $\mathcal{O}_8^g$   
e.g. variation of  $L_{K^* \bar{K}^*}$  and  $L_{K\bar{K}}$  w.r.t.  $C_{4s}^{\text{NP}} \rightarrow$
- may lead to large deviations for  $L_{K^* K}$



Coming out soon:

- similar analysis for  $B_{s,d} \rightarrow K^{(*)} \phi$

- how sensitive to  $SU(3)$  flavour-symmetry breaking ?
- NP interpretation requires inclusion of less robust observables

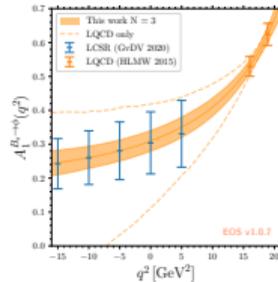
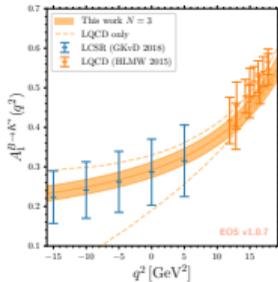
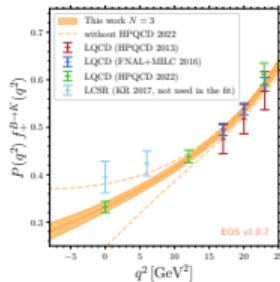


- 1 N. Gubernari, M. Reboud, D. van Dyk and J. Virto,  
“Dispersive analysis of  $B \rightarrow K^{(*)}$  and  $B_s \rightarrow \phi$  form factors,”  
JHEP **12** (2023), 153 [arXiv:2305.06301 [hep-ph]]
- 2 T. Feldmann and N. Gubernari,  
“Non-factorisable contributions of strong-penguin operators in  $\Lambda_b \rightarrow \Lambda \ell^+ \ell^-$ ”  
arXiv:2312.14146 (to appear in JHEP)
- 3 R. Fleischer, E. Malami, A. Rehult and K. K. Vos,  
“New perspectives for testing electron-muon universality,”  
JHEP **06** (2023), 033 [arXiv:2303.08764 [hep-ph]]

improve on Boyd-Grinstein-Lebed approach:

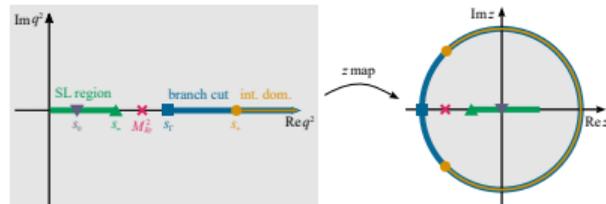
- individual bounds for different helicity projections ( $\lambda$ )

$$\frac{\chi^{(\lambda)} \Big|_{1\text{pt}}}{\chi^{(\lambda)} \Big|_{\text{OPE}}} + \sum_{\mathcal{F}_\lambda} \sum_n |a_n^{\mathcal{F}_\lambda}|^2 < 1$$



⇒ essential improvement for predictions at *negative* (unphysical) values of  $q^2$ ,  
important input to the analysis of non-local hadronic matrix elements in  $b \rightarrow sl^+l^-$  transitions

- below-threshold branch-cuts from  $B_s\pi$  and  $B_s\pi\pi$  accounted for in "z-parametrization"



Fit to lattice and sum-rule FFs:

- tighter unitarity bounds
- unwanted correlations removed

T. Feldmann and N. Gubernari, arXiv:2312.14146 (to appear in JHEP)

- local form factors:

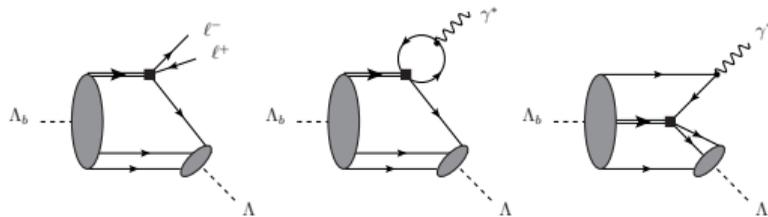
$$\langle \Lambda(p', s') | \bar{s}(0) \Gamma b(0) | \Lambda_b(p, s) \rangle$$

(for semileptonic operators  $\mathcal{O}_{9,10}$ )

- "non-local form factors":

$$\langle \Lambda(p', s') | T(\mathcal{O}_i(0) J_{em}(x)) | \Lambda_b(p, s) \rangle$$

(for hadronic penguin operators)



- factorizing quark-loop topologies
- non-factorizing "annihilation-type" of topologies  
→  $q^2$ -dependent shifts of Wilson coefficient  $C_9$

$$C_9 f_+(q^2) \rightarrow f_+(q^2) (C_9 + \Delta C_{9,+}(q^2)) \quad \text{etc.}$$

estimate of "annihilation" topology with LSCRs: (C2a, see above)

- only operators  $\mathcal{O}_5$  and  $\mathcal{O}_6$  contribute at leading power (opposite to annihilation in mesonic decays)
- transverse photons:  $|\Delta C_{9,\perp}|/\Delta C_9 \sim \mathcal{O}(1\%)$  as expected
- longitudinal photons:  $\Delta C_{9,+}$  is power-suppressed

	$10^2 \cdot \Delta C_{9,\perp}$
$2 \text{ GeV}^2$	$(0.6 \pm 2.5) + i(6.9 \pm 1.3)$
$4 \text{ GeV}^2$	$-(0.97 \pm 0.98) + i(1.89 \pm 0.62)$
$6 \text{ GeV}^2$	$-(0.64 \pm 0.39) + i(0.63 \pm 0.42)$

- uncertainties dominated by LCDAs of  $\Lambda_b$

[R. Fleischer, E. Malami, A. Rehult and K. K. Vos, JHEP **06** (2023), 033]

- recent LHCb results in agreement with electron-muon universality [2212.09152, 2212.09153]

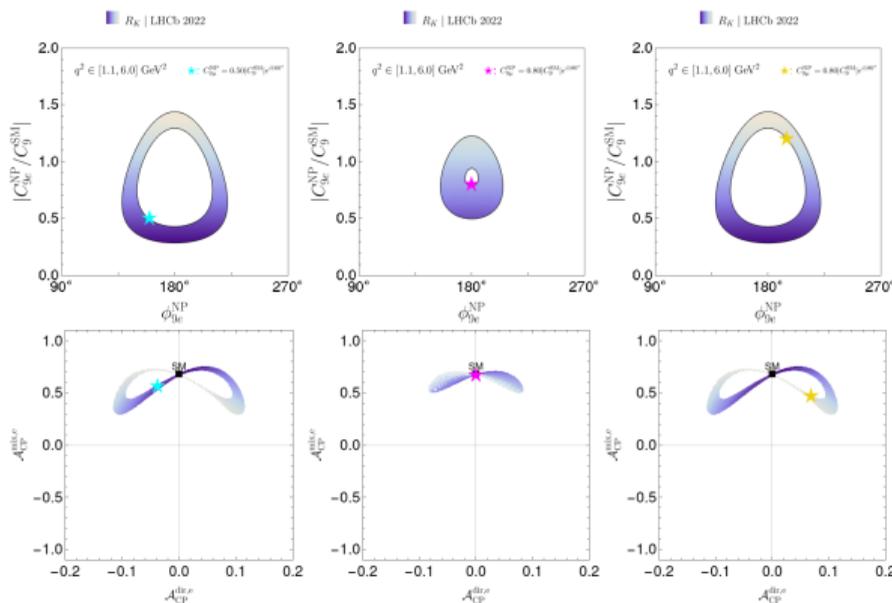
$$\langle R_K \rangle_{[1.1, 6.0]} = 0.949 \pm 0.05$$

- individual rates still somewhat below SM
  - how much space left for LFU violation ?
- include **CP-violating observables** in fits (i.e. allow for complex NP Wilson coefficients)

⇒ *large* differences between CP asymmetries for electron and muon modes are still allowed !

- it would be useful to have a measurement of direct CP violation in  $R_K$ , defined by

$$\mathcal{A}_{CP}^{R_K} \equiv \frac{\bar{R}_K - R_K}{\bar{R}_K + R_K},$$



Scenario 1: Constraints on  $C_{9e}^{NP}$  for different benchmark points and the corresponding constraints on the CP asymmetries

still plenty of room for electron-muon universality violation!

[R. Fleischer, E. Malami, A. Rehult and K. K. Vos, JHEP 06 (2023), 033]

- recent LHCb results in agreement with electron-muon universality [2212.09152, 2212.09153]

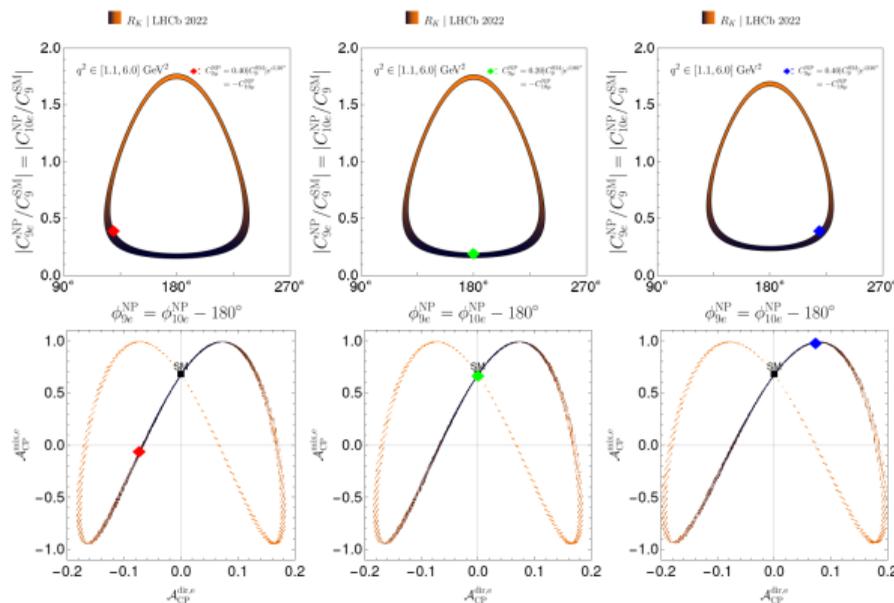
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Scenario 2: Constraints on  $C_{9e}^{NP}$  for different benchmark points and the corresponding constraints on the CP asymmetries

still plenty of room for electron-muon universality violation!

Contributions to Special Topic in EPJC:

“b-Quark Physics as a Precision Laboratory: Present Status and Future Prospects”

- 1 T. Mannel,  
“Introduction to B physics,”  
Eur. Phys. J. Spec. Top. (2023)
- 2 A. Khodjamirian, B. Melić and Y. M. Wang,  
“A guide to the QCD light-cone sum rule for  $b$ -quark decays,”  
arXiv:2311.08700, published in Eur. Phys. J. Spec. Top. (2023)
- 3 P. Böer and T. Feldmann,  
“Structure-dependent QED effects in exclusive  $B$ -meson decays,”  
arXiv:2312.12885, published in Eur. Phys. J. Spec. Top. (2024)

## C2a:

- WA1: Factorization and light-cone distributions ✓✓✓
- WA2: QCD sum rules and related methods ✓✓
- WA3: New channels and multi-hadron final states ✓
- WA4: Inclusive rates and the sum over exclusive channels, semi-inclusive decays ✗

## C2b:

- WA1: Higher-order QCD corrections ✗
- WA2: Phenomenology of non-leptonic decays ✓✓
- WA3: Phenomenology of rare decays, BSM flavour structures ✓✓✓

→ intensify work in C2a/WA4 and C2b/WA1 ...

→ initiate more interactions within CRC, in particular in C2b/WA3

→ see next slide

- V. Cirigliano, W. Dekens, J. de Vries, E. Mereghetti and T. Tong,  
“Anomalies in global SMEFT analyses: a case study of first-row CKM unitarity,”  
JHEP **03** (2024) 033, [arXiv:2311.00021 [hep-ph]]
- R. Mandal and T. Tong,  
“Exploring freeze-out and freeze-in dark matter via effective Froggatt-Nielsen theory,”  
JCAP **11** (2023), 074, [arXiv:2307.14972 [hep-ph]]



- 
- Atkinson, Englert, Kirk, Tetlalmatzi-Xolocotzi,  
comparison/interplay between  $B$ -physics and top-collider constraints within SMEFT,  
in preparation

