

Theory Overview on Neutrino Physics

José W F Valle



ASTROPARTICLES

Astroparticles and High Energy Physics Group

<https://www.facebook.com/ific.ahep/>



The Future of Particle Physics: A Quest for Guiding Principles (1-2 de octubre de 2018)

neutrinos and what comes next in HEP

José W F Valle



ASTRO PARTICLES

Astroparticles and High Energy Physics Group

<https://www.facebook.com/ific.ahep/>



The Future of Particle Physics: A Quest for Guiding Principles (1-2 de octubre de 2018)

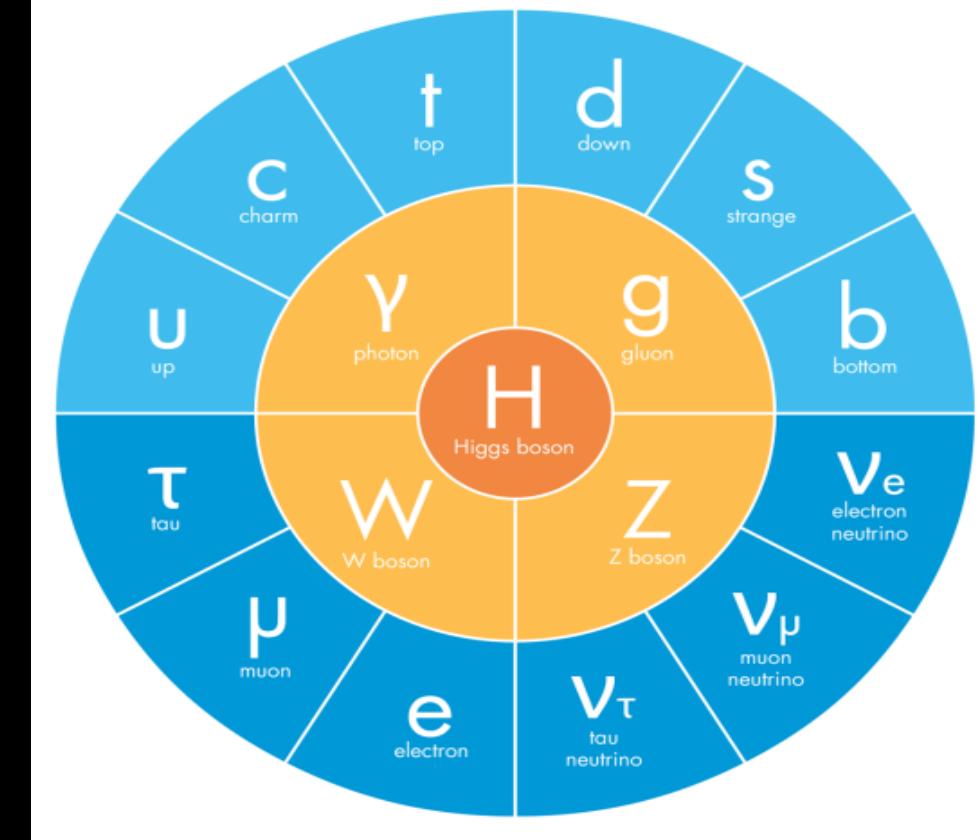
THE STANDARD MODEL

FERMIONS (matter)

● Quarks ● Leptons

BOSONS (force carriers)

● Gauge bosons ● Higgs boson



exciting ...



THE STANDARD MODEL

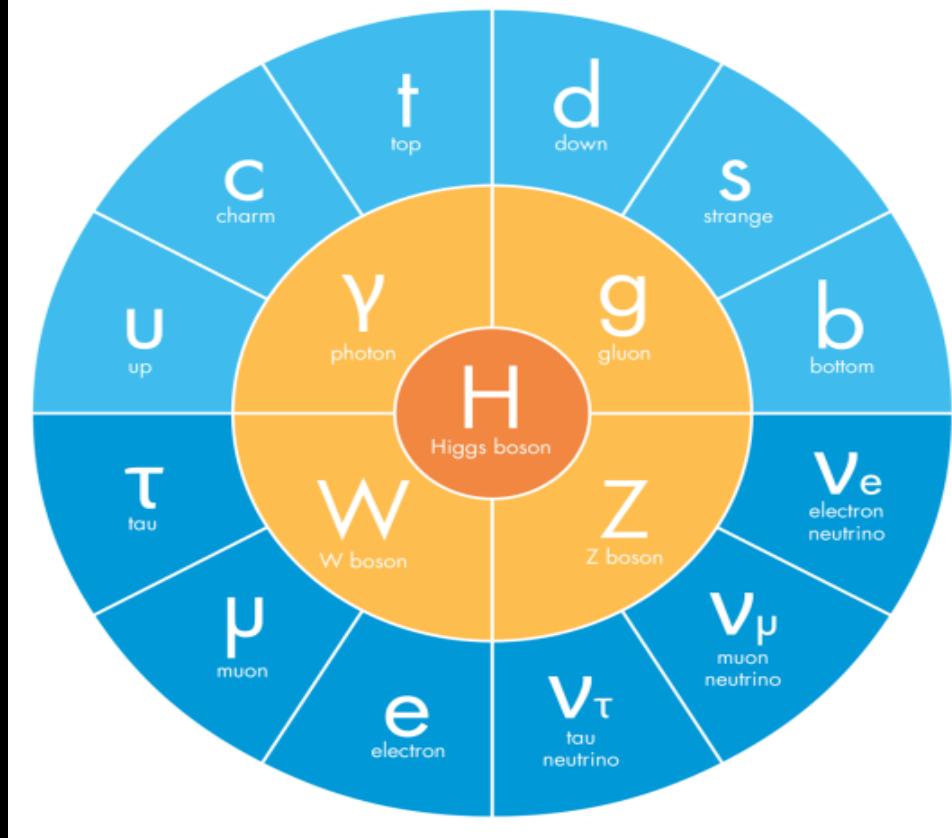
FERMIONS (matter)

● Quarks ● Leptons

BOSONS (force carriers)

● Gauge bosons

● Higgs boson



exciting ...



Higgs not the last brick !

THE STANDARD MODEL

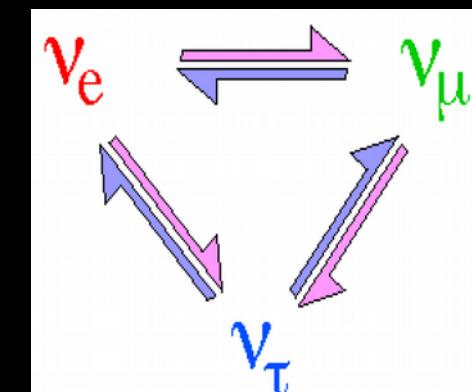
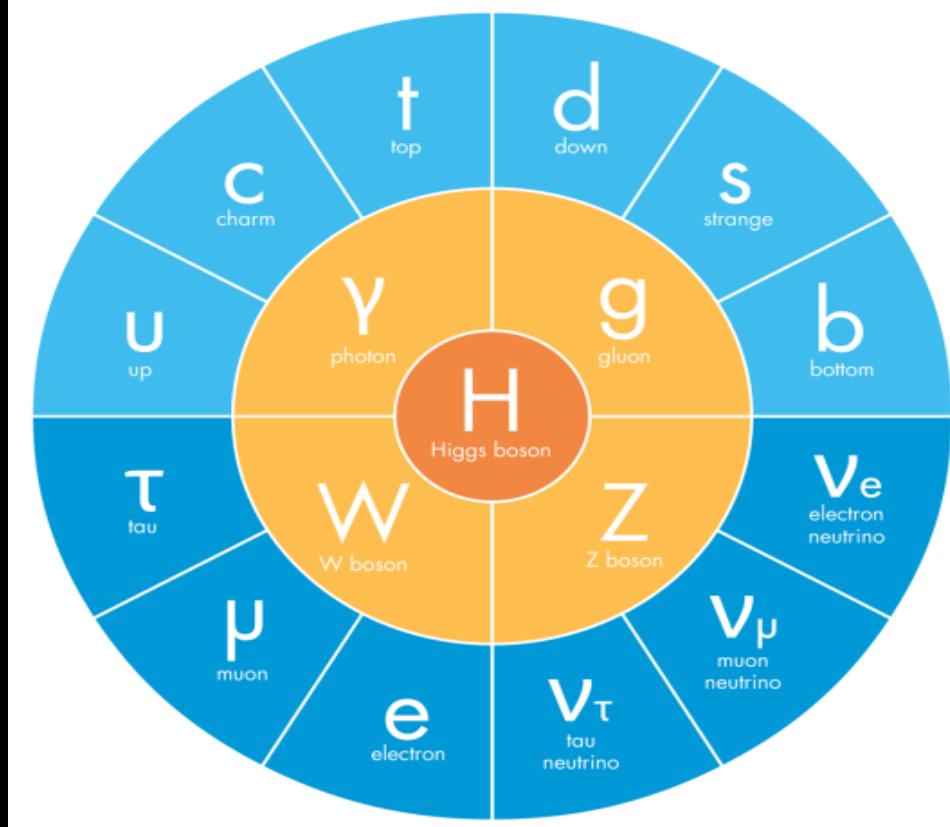
FERMIONS (matter)

● Quarks ● Leptons

BOSONS (force carriers)

● Gauge bosons

● Higgs boson



exciting ...



Higgs not the last brick !

THE STANDARD MODEL

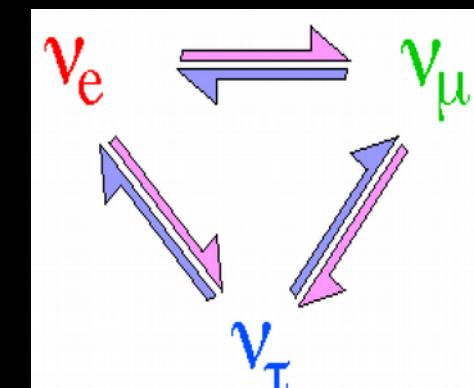
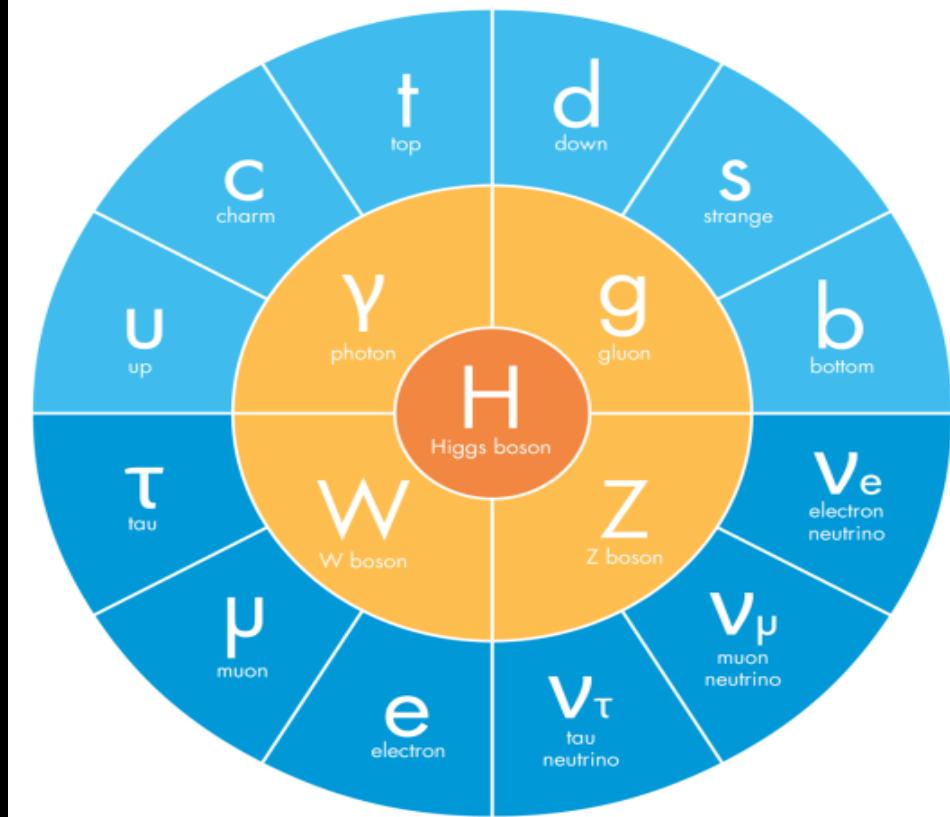
FERMIONS (matter)

● Quarks ● Leptons

BOSONS (force carriers)

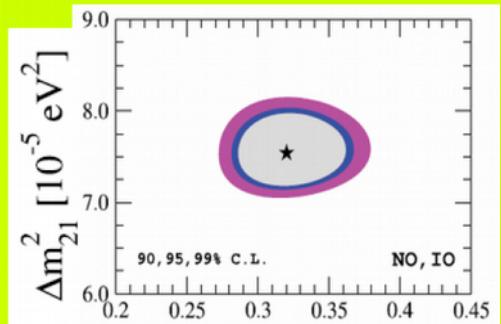
● Gauge bosons

● Higgs boson

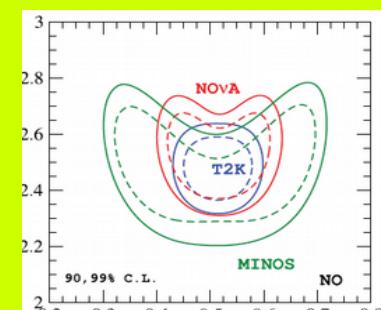
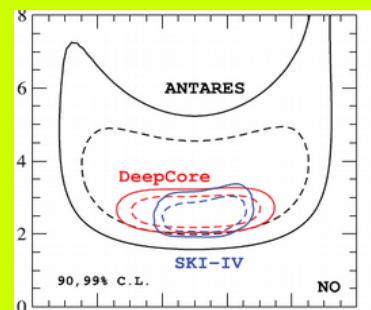


Besides neutrino mass there are many other issues in particle physics & cosmology for which neutrinos may provide key input

status of neutrino oscillations 2018

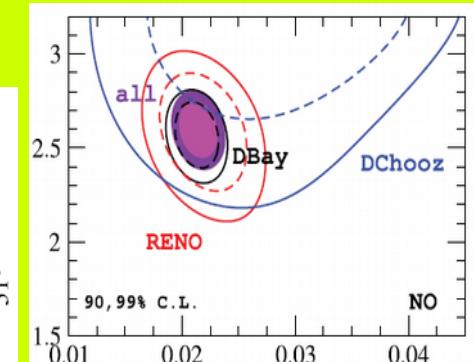
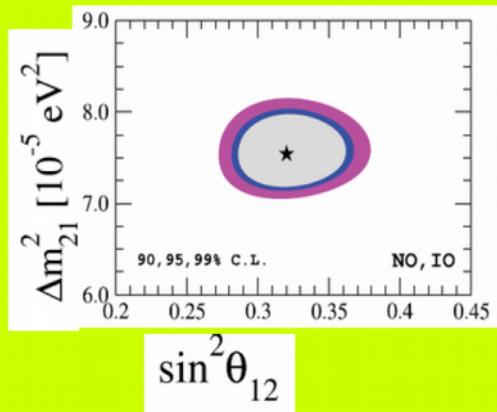


$$\sin^2 \theta_{12}$$



P.F. de Salas et al, PLB782 (2018) 633
<https://globalfit.astroparticles.es/>

status of neutrino oscillations 2018



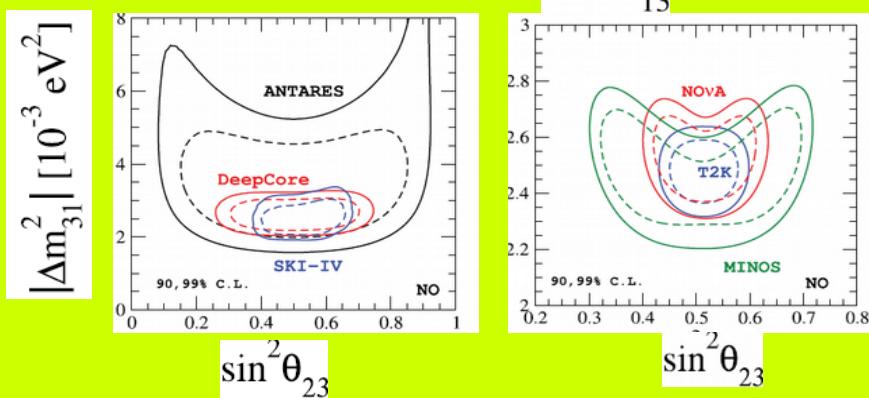
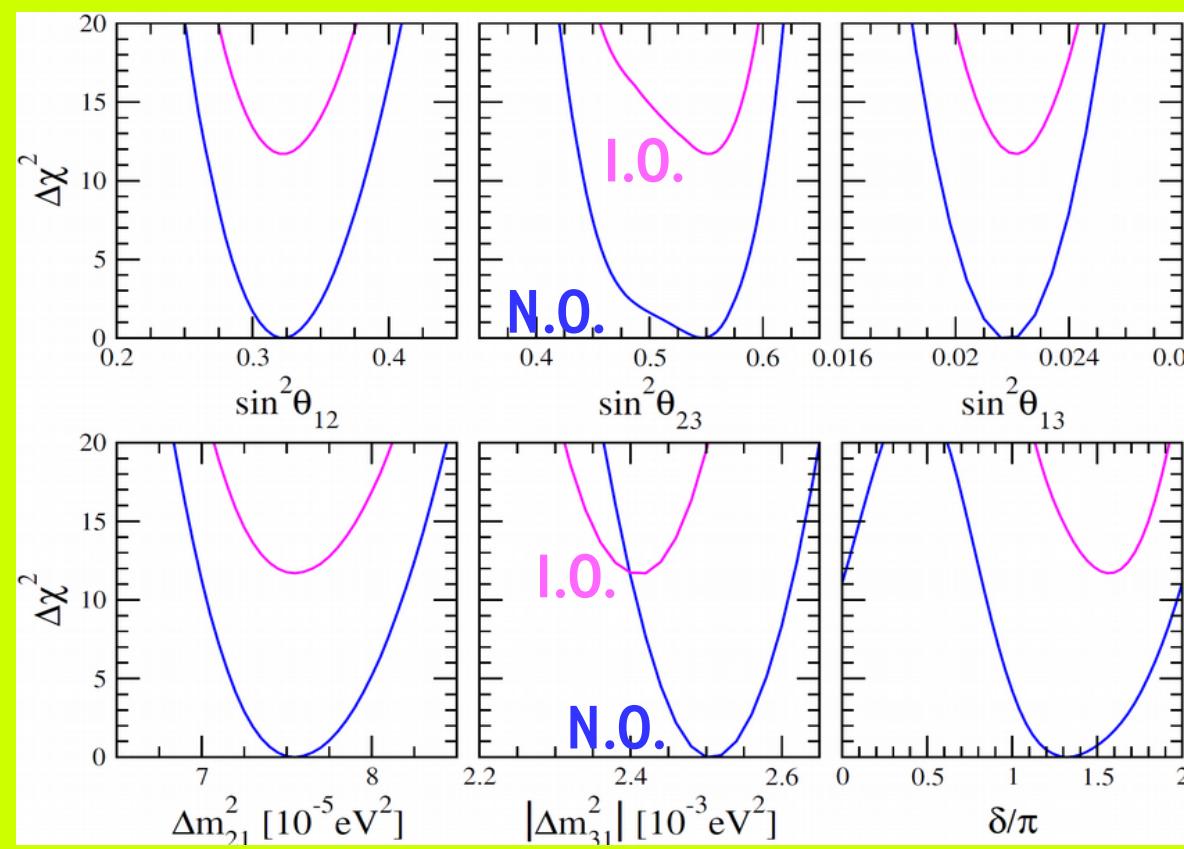
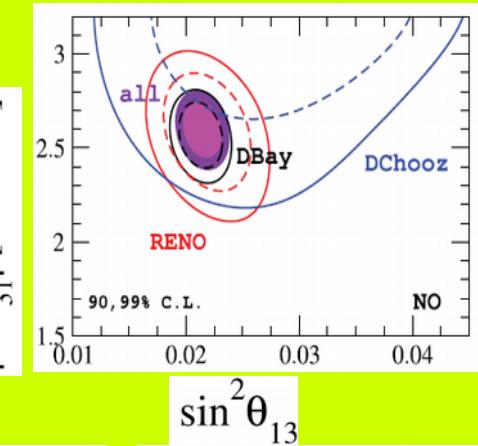
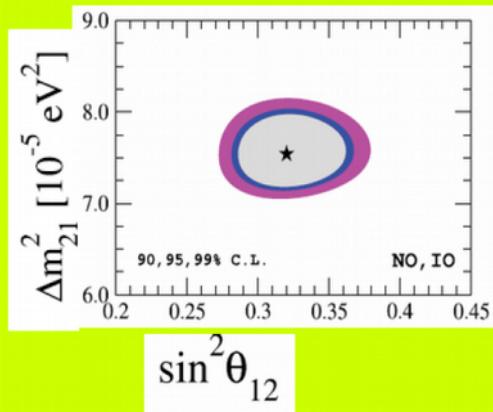
$\sin^2 \theta_{23}$

$\sin^2 \theta_{13}$

$\sin^2 \theta_{23}$

P.F. de Salas et al, PLB782 (2018) 633
<https://globalfit.astroparticles.es/>

status of neutrino oscillations 2018



P.F. de Salas et al, PLB782 (2018) 633
<https://globalfit.astroparticles.es/>

Consistent global picture
 Good agreement
 Good long-term prospects

status of neutrino oscillations 2018

the numbers

precision era requires robustness tests

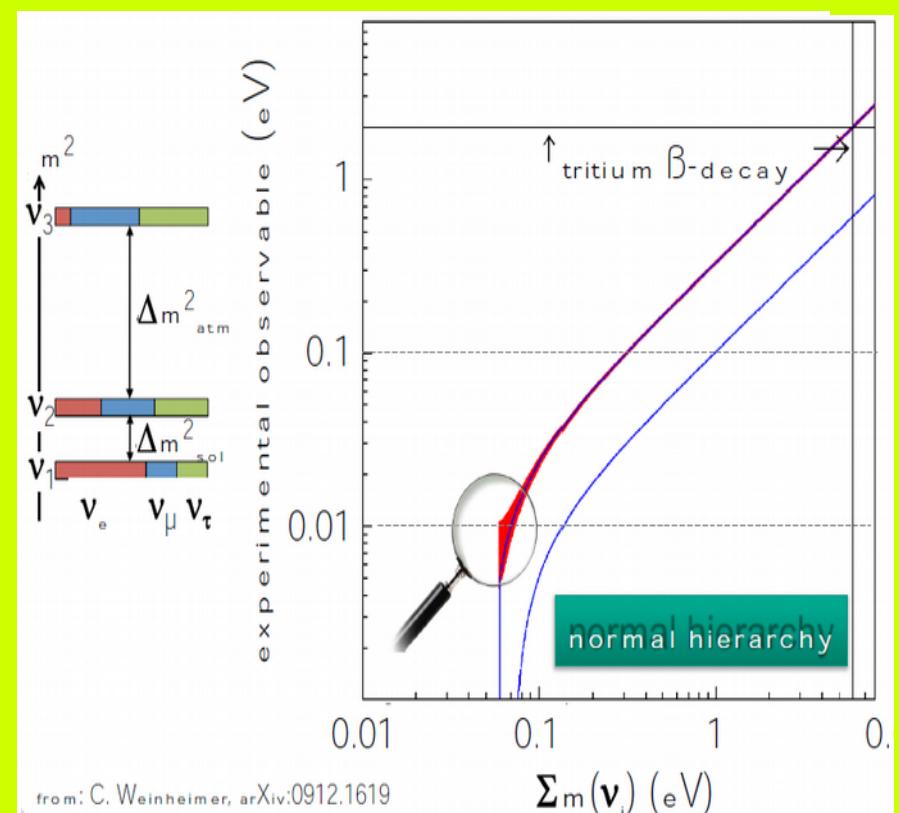
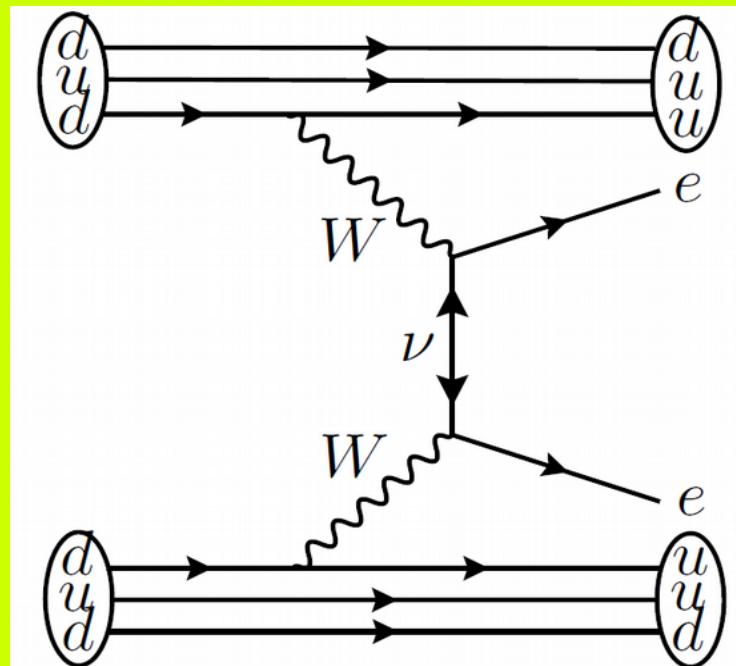
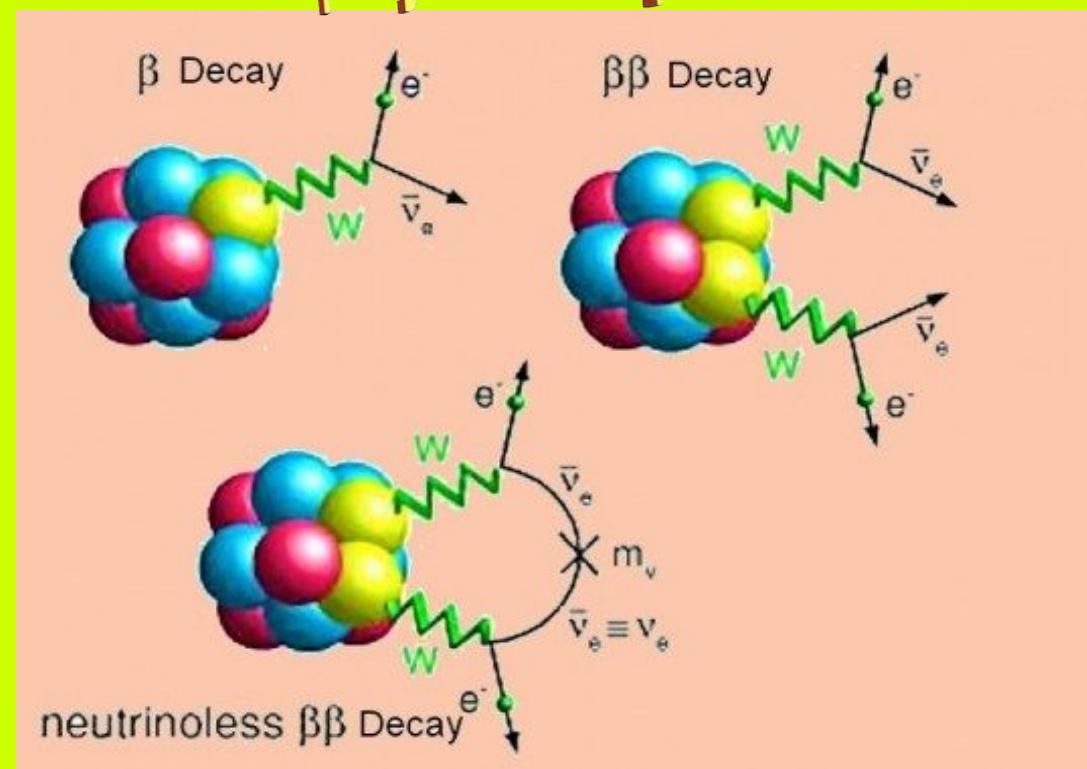
need to go beyond 3-nu paradigm

P.F. de Salas et al, PLB782 (2018) 633
<https://globalfit.astroparticles.es/>

Neutrino oscillation parameters summary determined from this global analysis. The ranges for inverted ordering refer to the local minimum for this neutrino mass ordering.

Parameter	Best fit $\pm 1\sigma$	2σ range	3σ range
Δm_{21}^2 [10^{-5} eV 2]	$7.55^{+0.20}_{-0.16}$	7.20–7.94	7.05–8.14
$ \Delta m_{31}^2 $ [10^{-3} eV 2] (NO)	2.50 ± 0.03	2.44–2.57	2.41–2.60
$ \Delta m_{31}^2 $ [10^{-3} eV 2] (IO)	$2.42^{+0.03}_{-0.04}$	2.34–2.47	2.31–2.51
$\sin^2 \theta_{12}/10^{-1}$	$3.20^{+0.20}_{-0.16}$	2.89–3.59	2.73–3.79
$\theta_{12}/^\circ$	$34.5^{+1.2}_{-1.0}$	32.5–36.8	31.5–38.0
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.47^{+0.20}_{-0.30}$	4.67–5.83	4.45–5.99
$\theta_{23}/^\circ$	$47.7^{+1.2}_{-1.7}$	43.1–49.8	41.8–50.7
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.51^{+0.18}_{-0.30}$	4.91–5.84	4.53–5.98
$\theta_{23}/^\circ$	$47.9^{+1.0}_{-1.7}$	44.5–48.9	42.3–50.7
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.160^{+0.083}_{-0.069}$	2.03–2.34	1.96–2.41
$\theta_{13}/^\circ$	$8.45^{+0.16}_{-0.14}$	8.2–8.8	8.0–8.9
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.220^{+0.074}_{-0.076}$	2.07–2.36	1.99–2.44
$\theta_{13}/^\circ$	$8.53^{+0.14}_{-0.15}$	8.3–8.8	8.1–9.0
δ/π (NO)	$1.32^{+0.21}_{-0.15}$	1.01–1.75	0.87–1.94
$\delta/^\circ$	238^{+38}_{-27}	182–315	157–349
δ/π (IO)	$1.56^{+0.13}_{-0.15}$	1.27–1.82	1.12–1.94
$\delta/^\circ$	281^{+23}_{-27}	229–328	202–349

nuclear physics as probe of neutrino mass scale



from: C. Weinheimer, arXiv:0912.1619

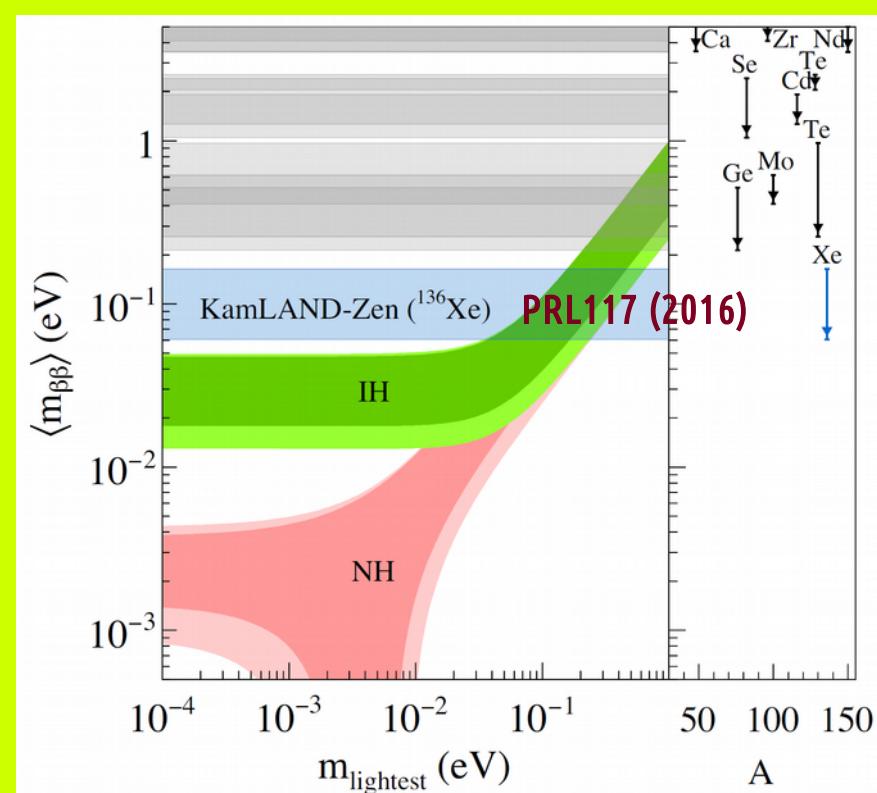
neutrinoless double beta decay

historical review
A.S. Barabash arXiv:1104.2714

symmetric parametrization of lepton mixing matrix

Schechter & JV PRD22 (1980) 2227
Rodejohann, JV Phys.Rev. D84 (2011) 073011

$$\left| \sum_j U_{ej}^2 m_j \right| = |c_{12}^2 c_{13}^2 m_1 + s_{12}^2 c_{13}^2 m_2 e^{2i\phi_{12}} + s_{13}^2 m_3 e^{2i\phi_{13}}|$$



nEXO, CUORE , LEGEND (nGERDA/Majorana) ...

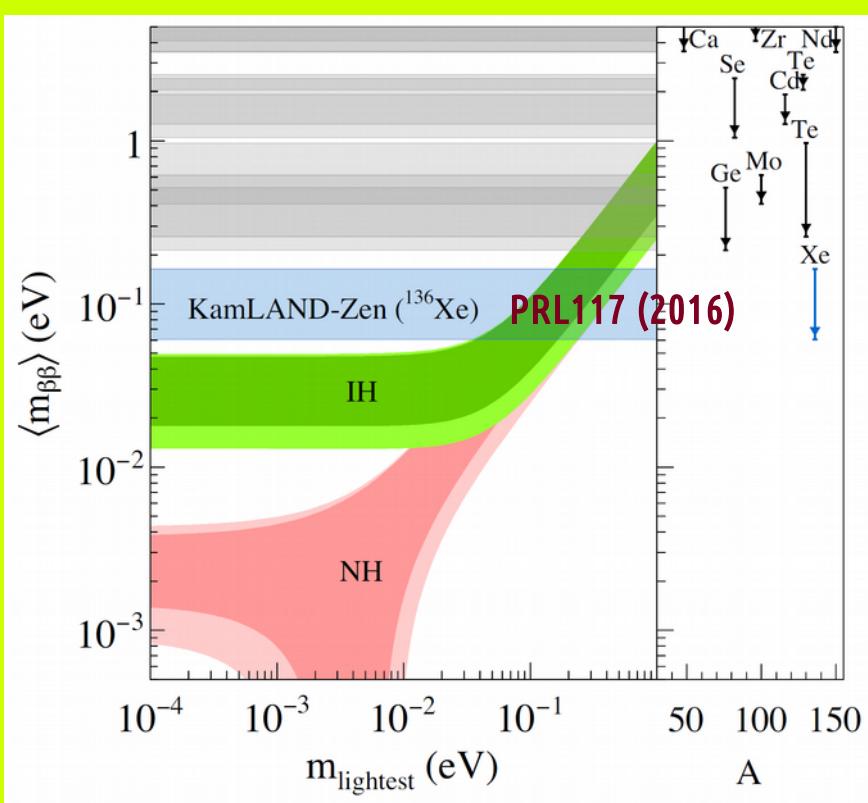
neutrinoless double beta decay

historical review
A.S. Barabash arXiv:1104.2714

symmetric parametrization of lepton mixing matrix

Schechter & JV PRD22 (1980) 2227
Rodejohann, JV Phys.Rev. D84 (2011) 073011

$$\left| \sum_j U_{ej}^2 m_j \right| = |c_{12}^2 c_{13}^2 m_1 + s_{12}^2 c_{13}^2 m_2 e^{2i\phi_{12}} + s_{13}^2 m_3 e^{2i\phi_{13}}|$$



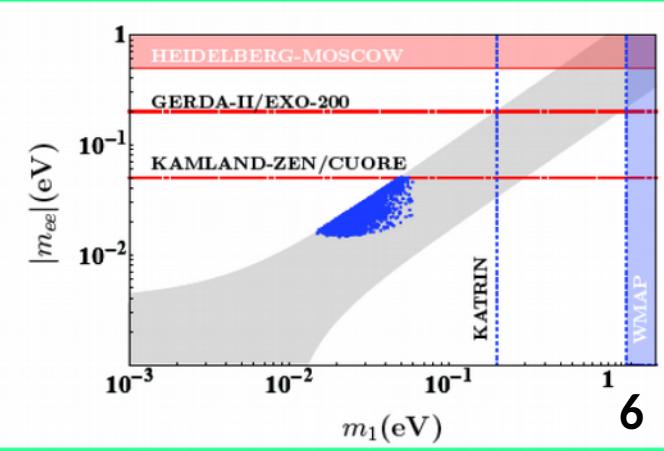
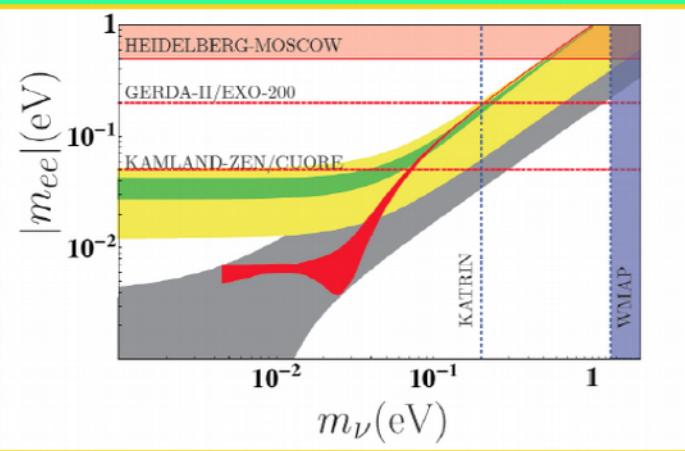
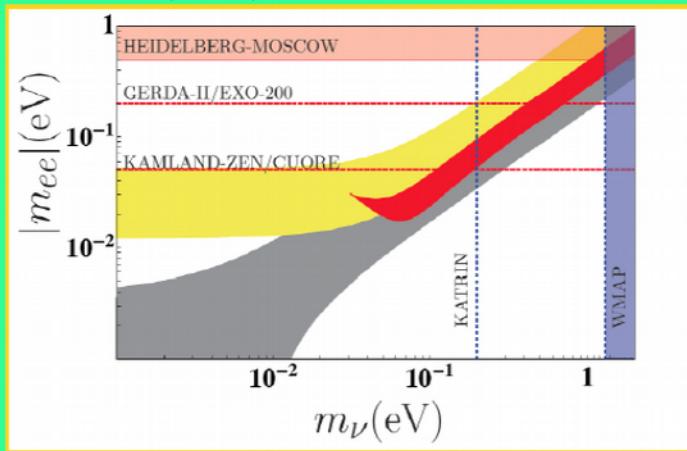
nEXO, CUORE , LEGEND (nGERDA/Majorana) ...

lower bounds even for normal ordering

Dorame et al
NPB861 (2012) 259-270

Dorame et al
PhysRevD.86.056001

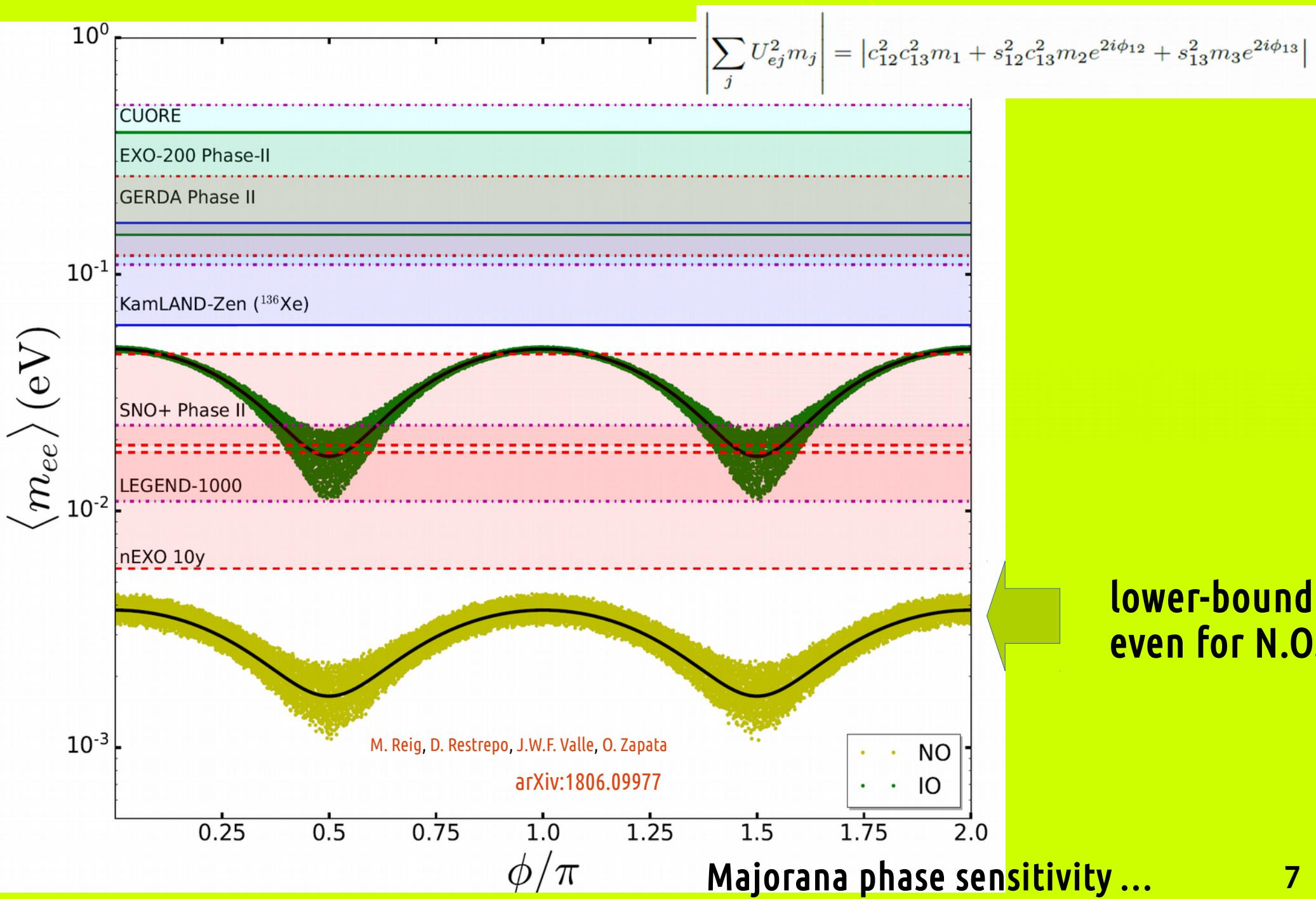
King et al
Phys. Lett. B 724 (2013) 68



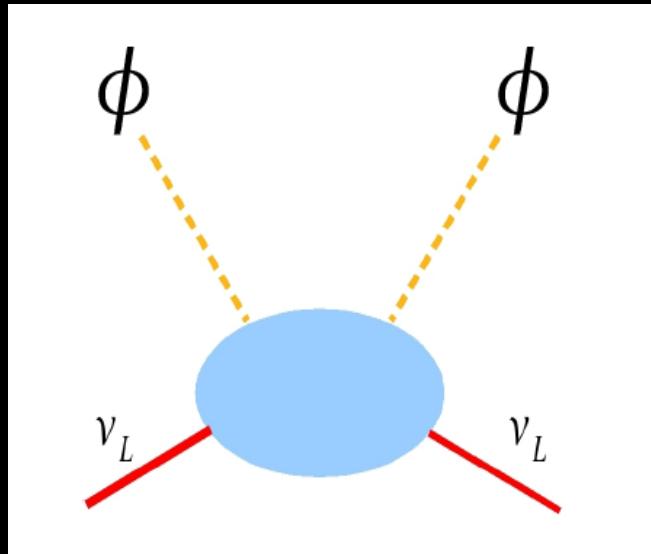
When one neutrino is massless

original symmetric form of lepton mixing matrix

Schechter & JV PRD22 (1980) 2227
Rodejohann, JV Phys.Rev. D84 (2011) 073011

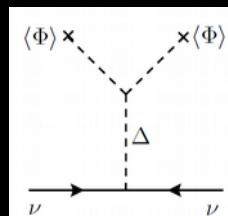
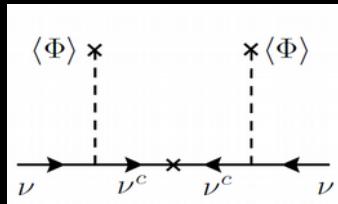
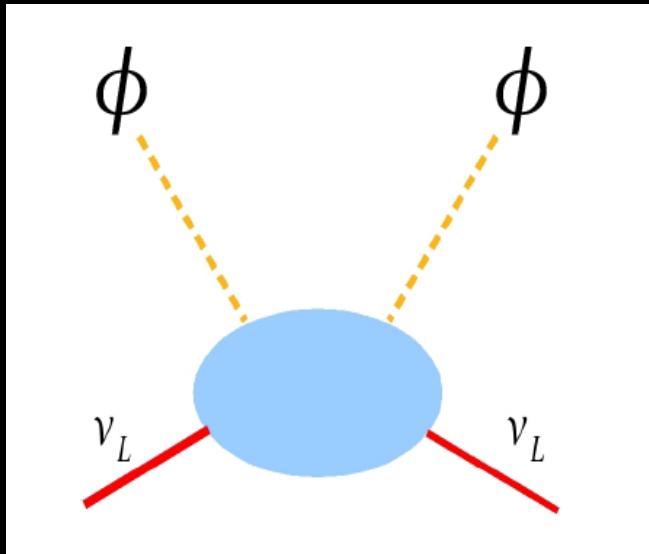


Origin of neutrino mass



coefficient
mechanism
scale
flavor structure

origin of neutrino mass



TYPE I

Minkowski 77
Gellman Ramond Slansky 80
Glashow, Yanagida 79
Mohapatra Senjanovic 80
Lazarides Shafi Weterrich 81
Schechter-Valle 80 & 82

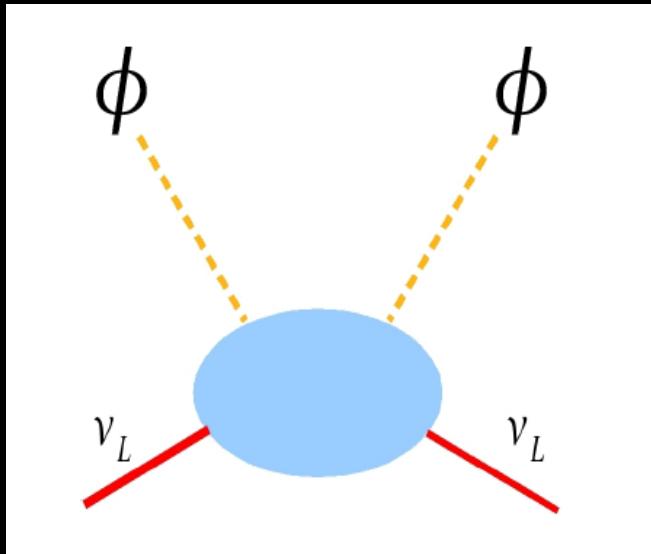
seesaw

Schechter-Valle 80 & 82

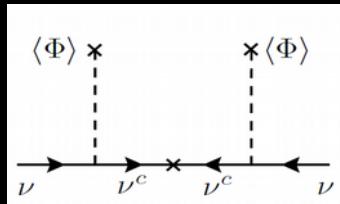
$$v_3 v_1 \sim v_2^2$$

coefficient
mechanism
scale
flavor structure

Origin of neutrino mass



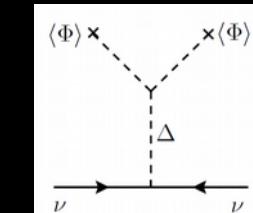
coefficient
mechanism
scale
flavor structure



TYPE I

Minkowski 77
 Gellman Ramond Slansky 80
 Glashow, Yanagida 79
 Mohapatra Senjanovic 80
 Lazarides Shafi Weterrich 81
 Schechter-Valle 80 & 82

seesaw



TYPE II

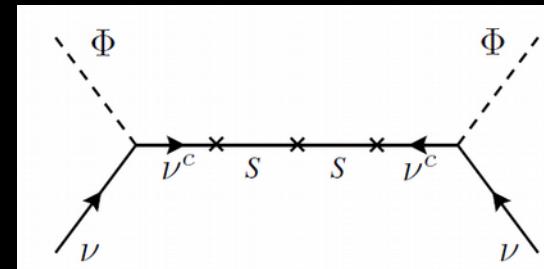
Schechter-Valle 80 & 82

$$v_3 v_1 \sim v_2^2$$

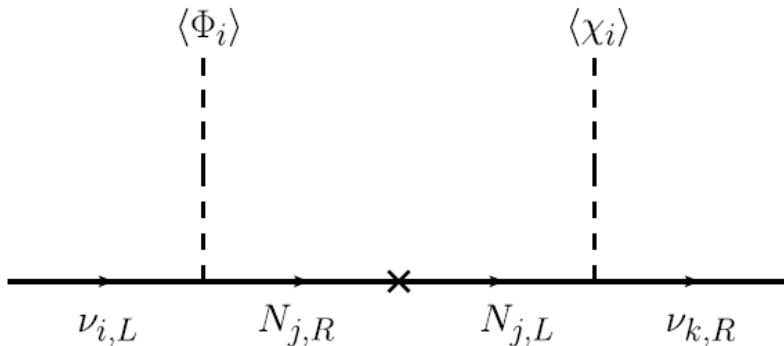
any number of singlet R's w.r.t. L's

LOW-SCALE SEESAW

Mohapatra-Valle 86
 Akhmedov et al PRD53 (1996) 2752
 Malinsky et al PRL95(2005)161801
 Bazzocchi et al, PRD81 (2010) 051701



Seesawing à la Dirac



typeI

Phys.Lett. B761 (2016) 431-436

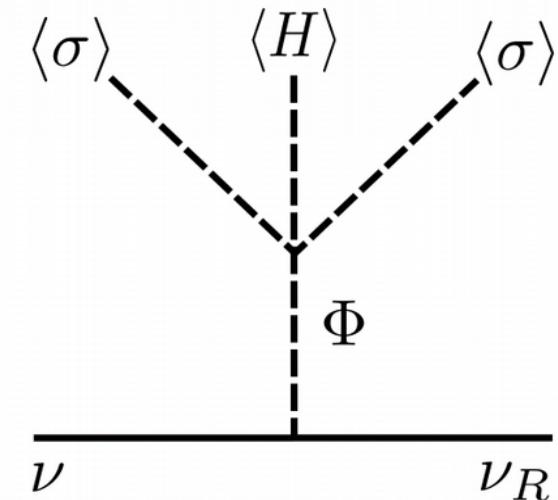
Phys.Lett. B767 (2017) 209-213



**symmetry protects
small neutrino mass**

Phys.Rev. D98 (2018) 035009

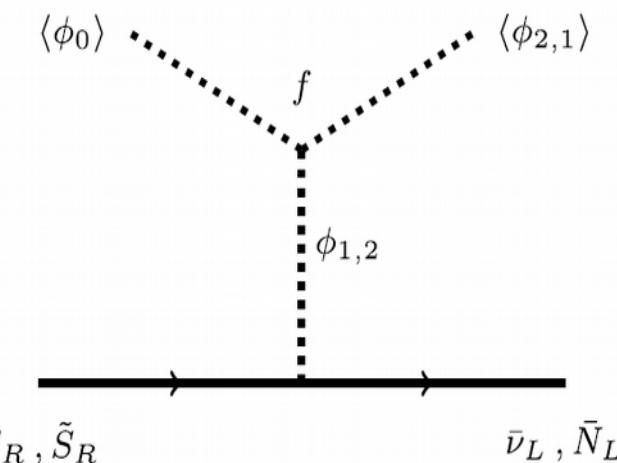
Phys.Lett. B781 (2018) 122-128



type2

Phys.Lett. B762 (2016) 162-165

Phys.Rev. D94 (2016) 033012



Addazi et al Phys.Lett. B759 (2016) 471-478

Phys.Lett. B755 (2016) 363-366

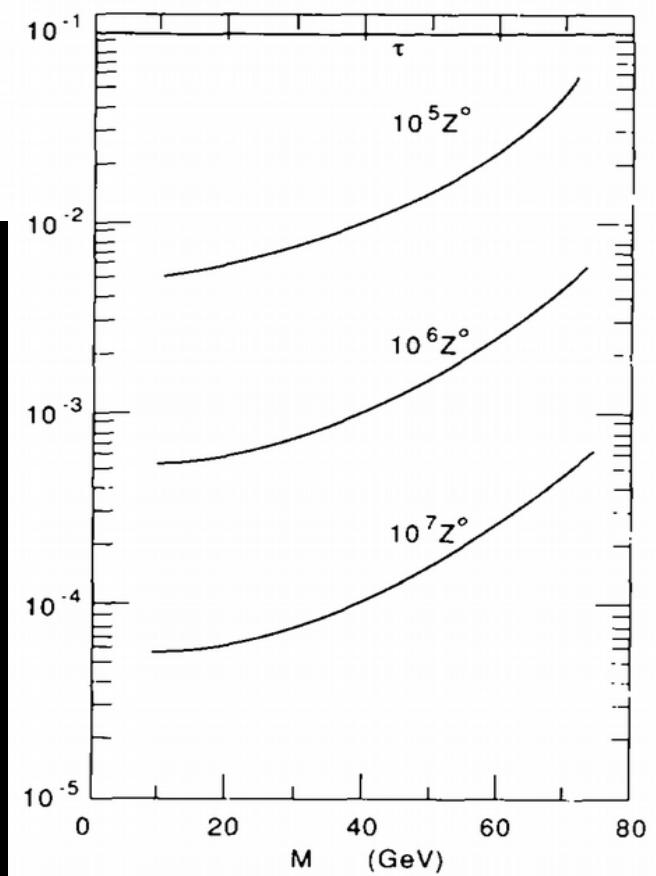
theories of neutrino mass



theories of neutrino mass



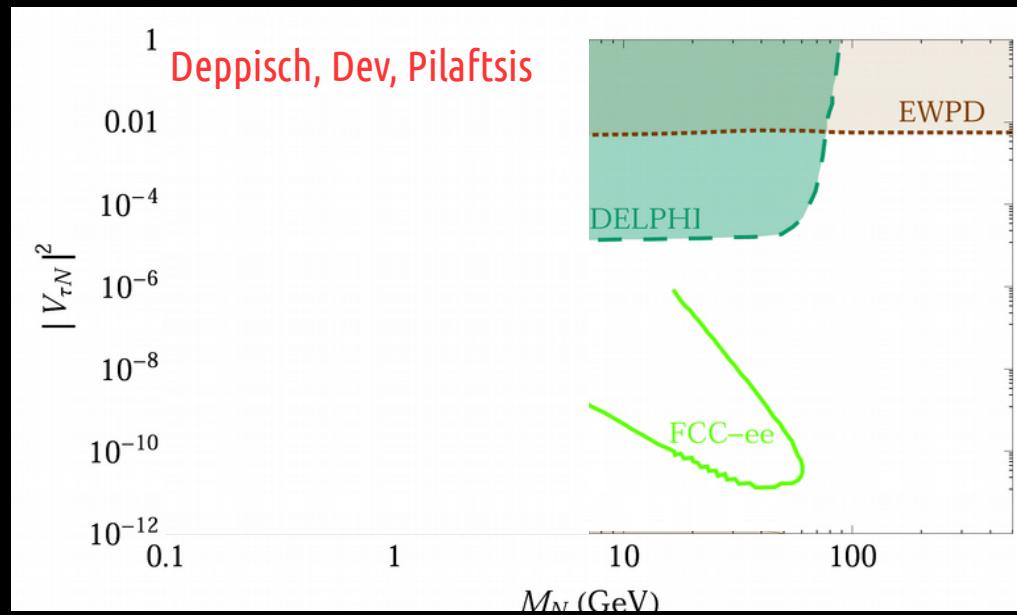
probe neutrino messengers with Displaced Vertices
re-measure neutrino mixing angles @ colliders

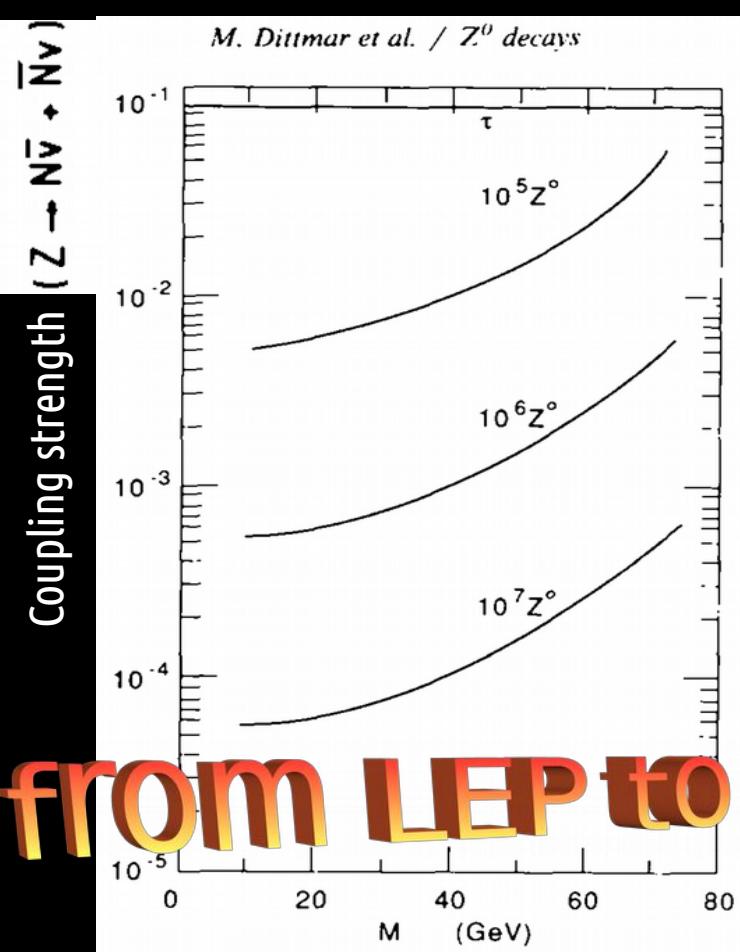
Coupling strength ($Z \rightarrow N\bar{v} + \bar{N}\nu$)

Pre-LEP days

Dittmar et al Nuclear Physics B332 (1990) 1-19

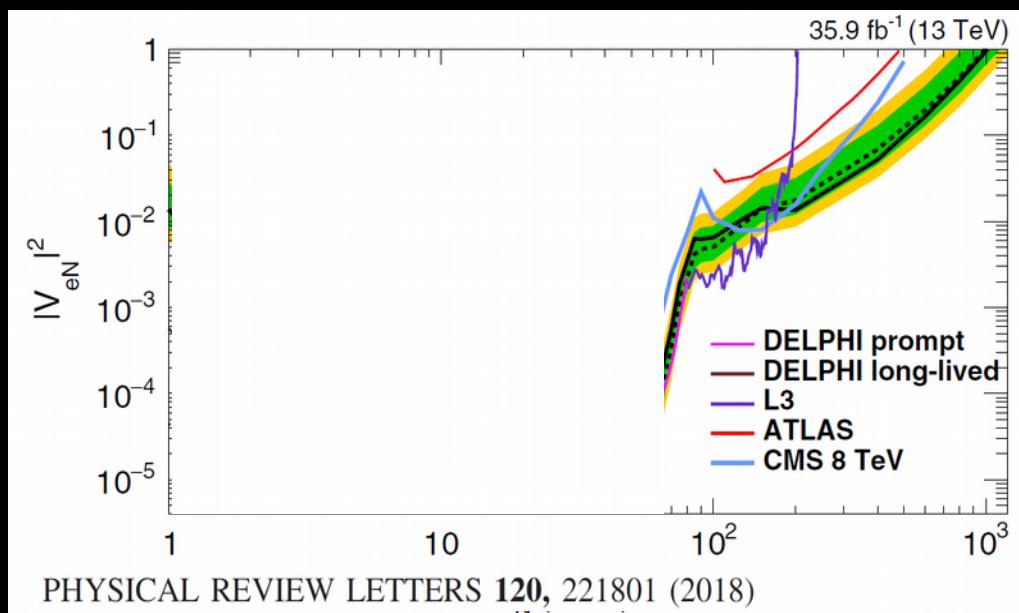
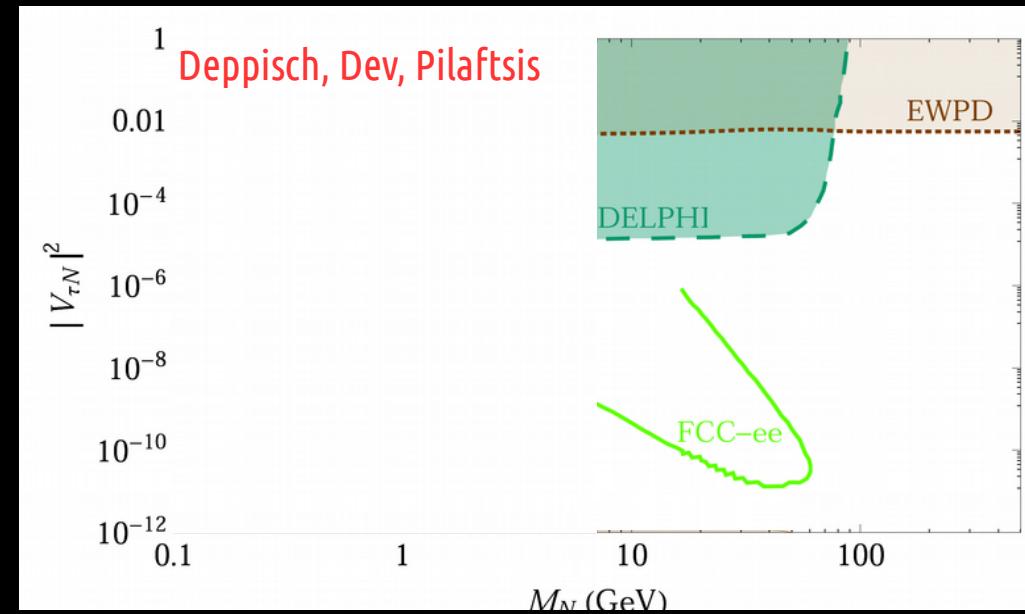
Limits on coupling strength parameter that can be reached for different number of Z s plotted as a function of the NHL mass. Only leptonic final states included. This is for the **tau** type NHL neglecting family mixing. The only relevant constraint in this case comes from weak universality

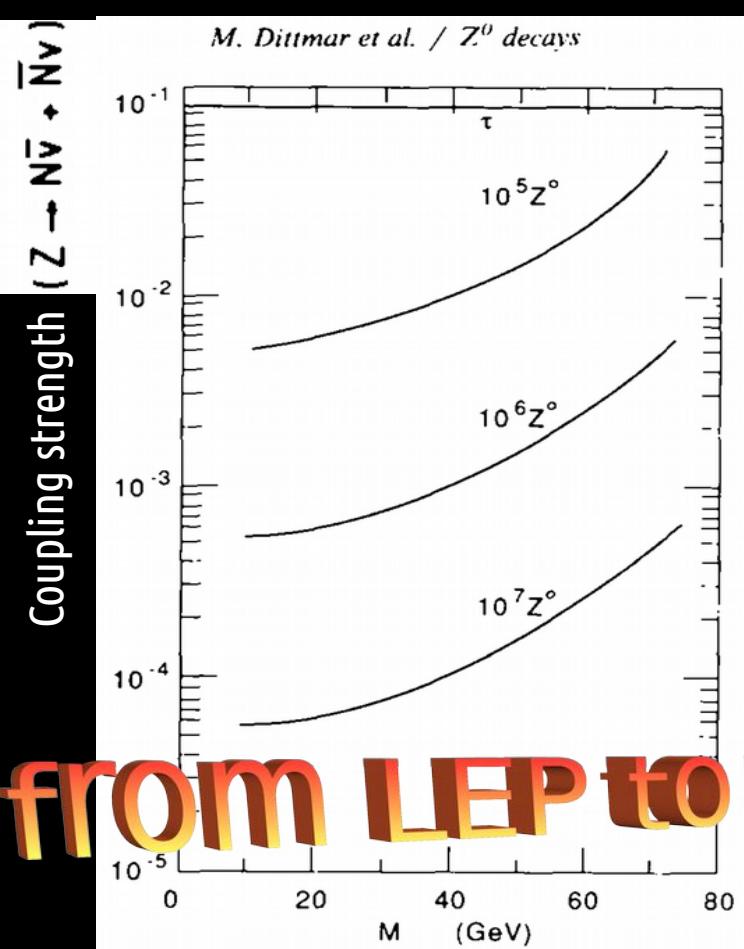


**Pre-LEP days**

Dittmar et al Nuclear Physics B332 (1990) 1-19

Limits on coupling strength parameter that can be reached for different number of Zs plotted as a function of the NHL mass. Only leptonic final states included. This is for the tau type NHL neglecting family mixing. The only relevant constraint in this case comes from weak universality

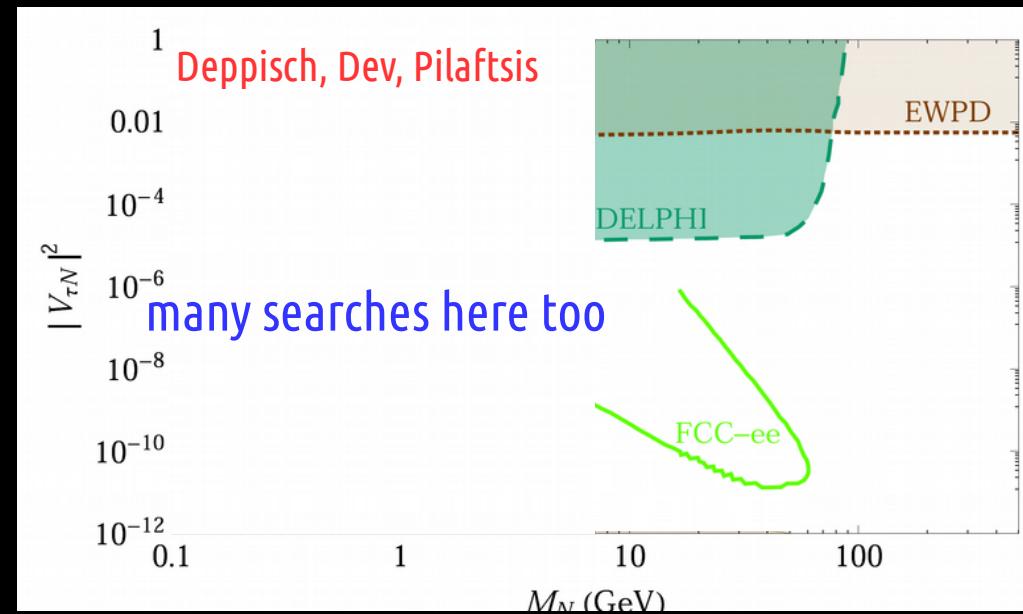
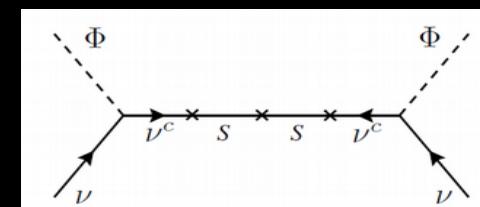
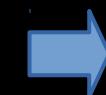
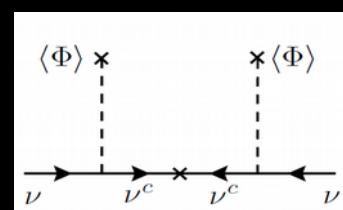
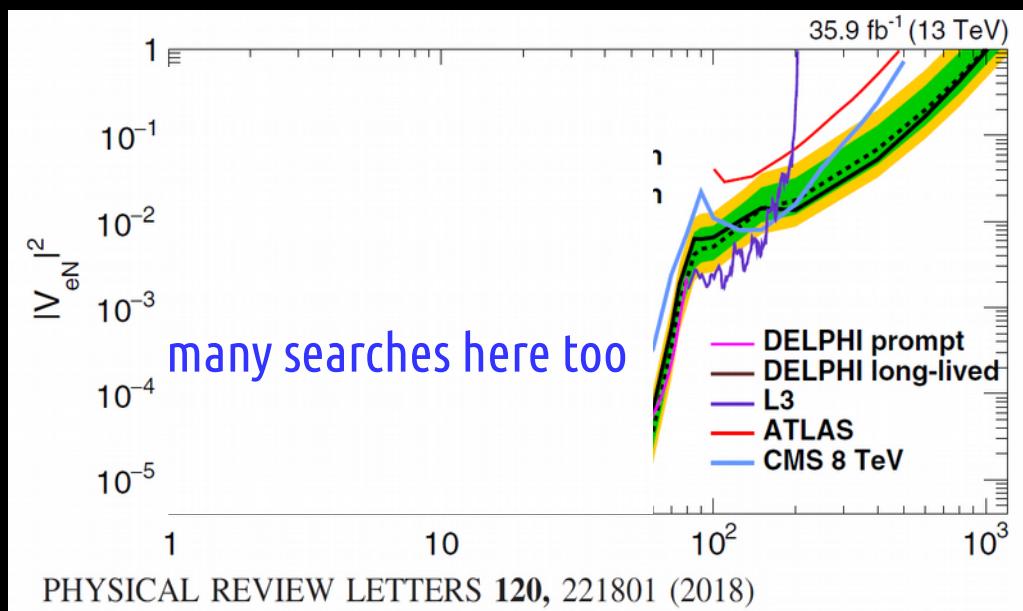




Pre-LEP days

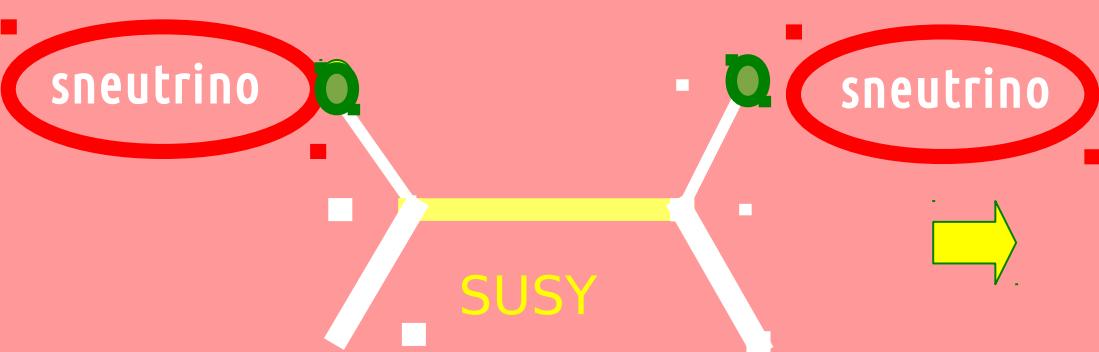
Dittmar et al Nuclear Physics B332 (1990) 1-19

Limits on coupling strength parameter that can be reached for different number of Z s plotted as a function of the NHL mass. Only leptonic final states included. This is for the **tau** type NHL neglecting family mixing. The only relevant constraint in this case comes from weak universality

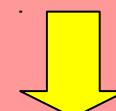
**high VS low****scale seesaw**

SUSY origin of neutrino mass

Masiero & Valle, PLB251 (1990) 273
Bhattacharyya & Pal, PRD82 (2010) 055013



EFF. BILINEAR RPV



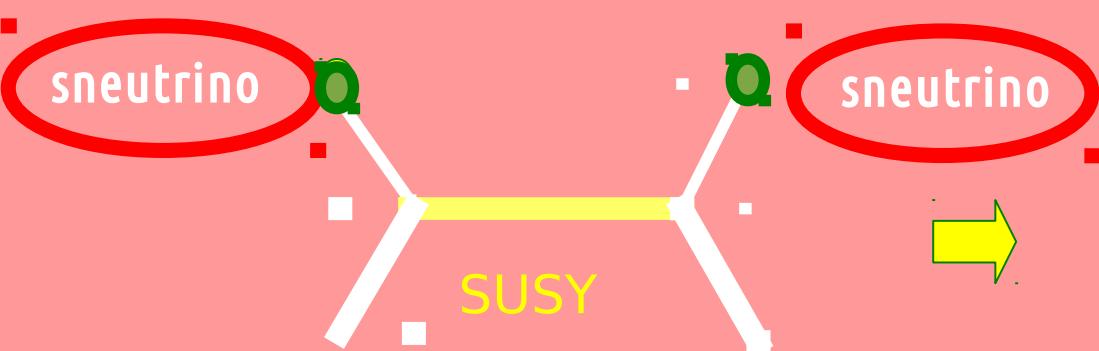
**ATM SCALE
SUSY-SEESAW**

Diaz et al PRD68 (2003) 013009, PRD62 (2000) 113008

Bazzocchi et al JHEP 01 (2013) 033 arXiv:1202.1529

SUSY origin of neutrino mass

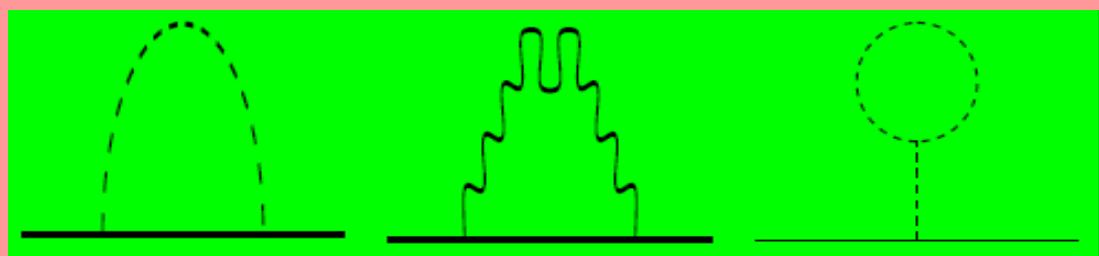
Masiero & Valle, PLB251 (1990) 273
Bhattacharyya & Pal, PRD82 (2010) 055013



EFF. BILINEAR RPV



**ATM SCALE
SUSY-SEESAW**



**SOLAR SCALE
RADIATIVE**

Diaz et al PRD68 (2003) 013009, PRD62 (2000) 113008

Bazzocchi et al JHEP 01 (2013) 033 arXiv:1202.1529

LIGHTEST NEUTRALINO DECAYS from cascade squark & gluino decays

De Campos et al

Phys.Rev. D86 (2012) 075001

$$\tilde{\chi}_1^0 \rightarrow W^\pm l_i^\mp$$

$$\tilde{\chi}_1^0 \rightarrow Z^0 \nu_i$$



LIGHTEST NEUTRALINO DECAYS from cascade squark & gluino decays

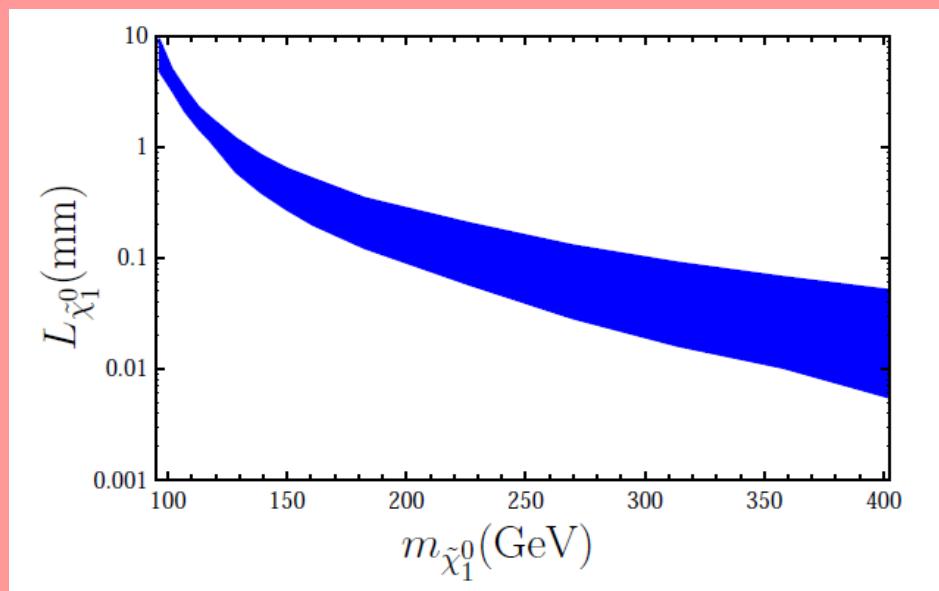
De Campos et al
Phys.Rev. D86 (2012) 075001

$$\tilde{\chi}_1^0 \rightarrow W^\pm l_i^\mp$$

$$\tilde{\chi}_1^0 \rightarrow Z^0 \nu_i$$



Lightest neutralino decay length



LIGHTEST NEUTRALINO DECAYS from cascade squark & gluino decays

De Campos et al
Phys.Rev. D86 (2012) 075001

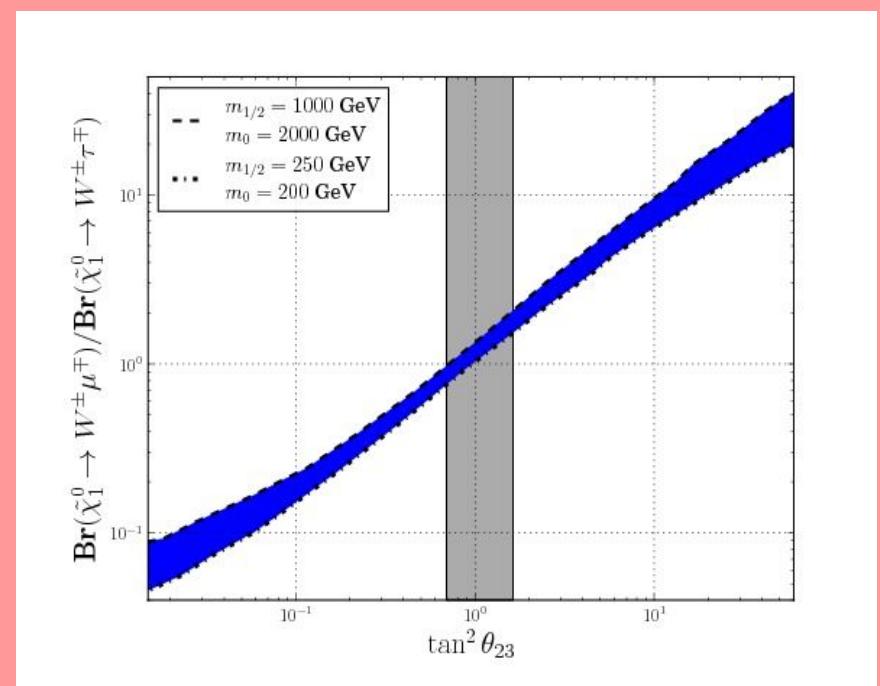
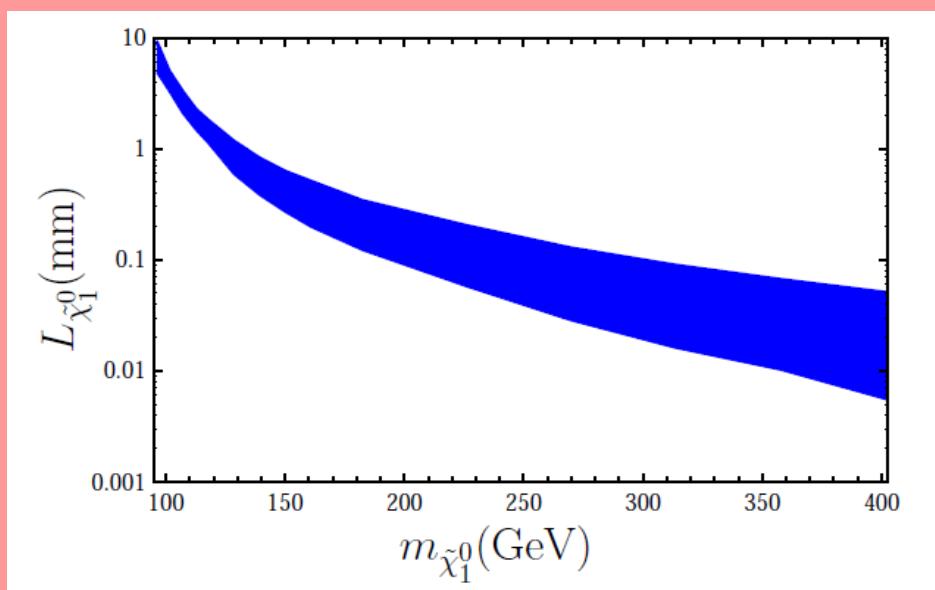
$$\tilde{\chi}_1^0 \rightarrow W^\pm l_i^\mp$$

$$\tilde{\chi}_1^0 \rightarrow Z^0 \nu_i$$



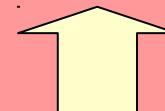
Lightest neutralino decay correlates with atm angle

Lightest neutralino decay length



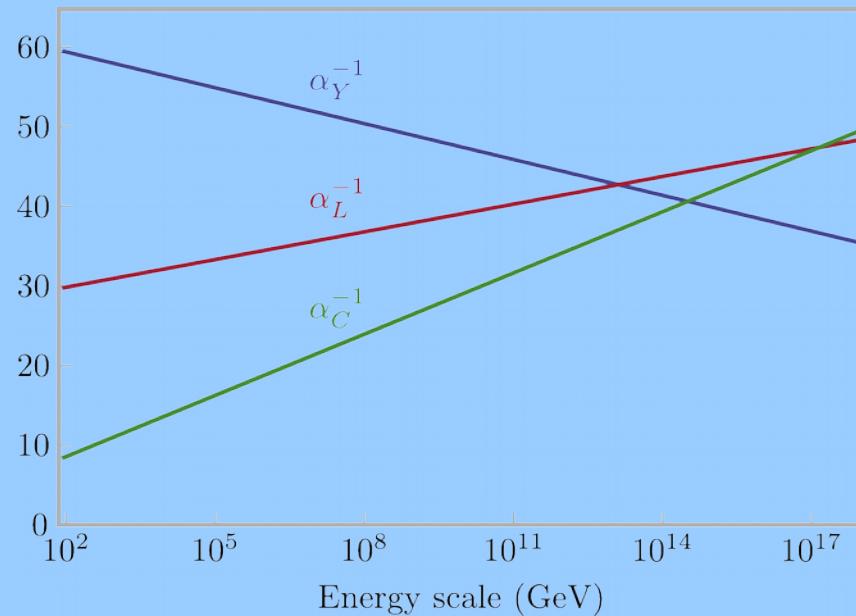
back

PROBING INUS @ LHC



Standard model

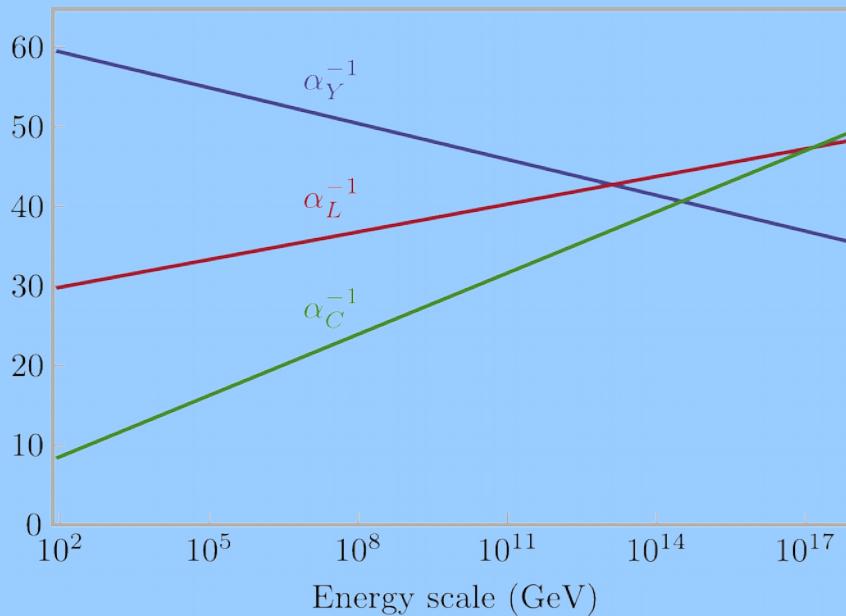
a near miss ...



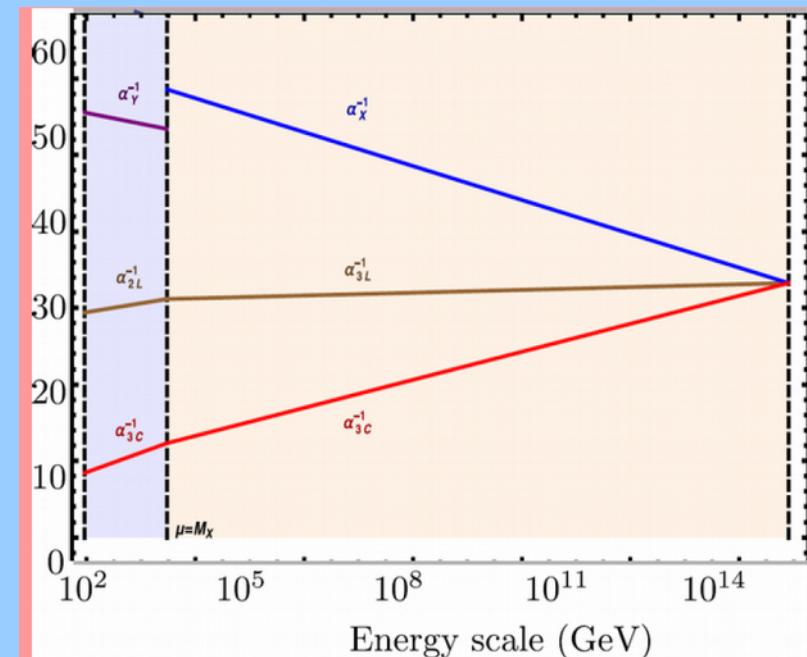
SUSY would make the gauge couplings unify at GUT scale,
But ... so far no p decay nor super-partners ...

Standard model

a near miss ...



SUSY would make the gauge couplings unify at GUT scale,
But ... so far no p decay nor super-partners ...



neutrinos & 331 unification

the physics responsible for neutrino masses
may also induce gauge coupling unification

E(6) F-theory GUT \rightarrow 331-EW theory

Boucenna et al Phys. Rev. D 91, 031702 (2015)

Deppisch et al Phys.Lett. B762 (2016) 432

radiative neutrino mass

In low scale 331 EW theory

331 motivation # families = # colours

Singer, Valle, Schechter, Phys.Rev. D22 (1980) 738

radiative neutrino mass

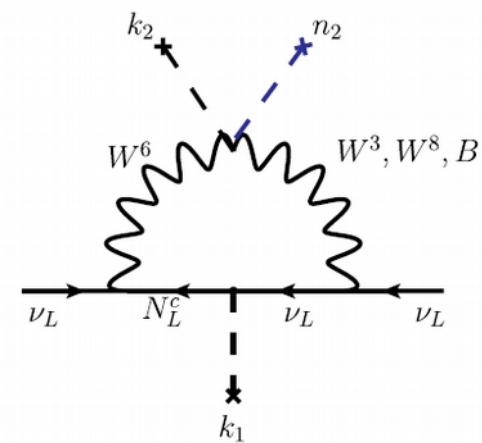
In low scale 331 EW theory

331 motivation # families = # colours

Singer, Valle, Schechter, Phys.Rev. D22 (1980) 738

Gauge vs Higgs origin

PHYSICAL REVIEW D 90, 013005 (2014)



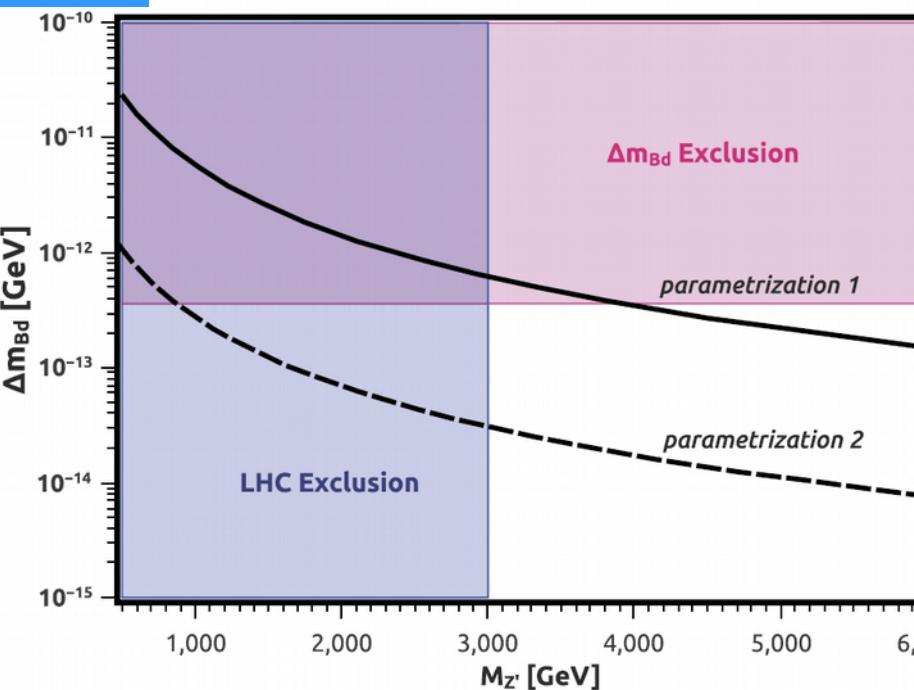
Boucenna, Morisi, JV Phys.Rev. D90 (2014) 013005

radiative neutrino mass

In low scale 331 EW theory

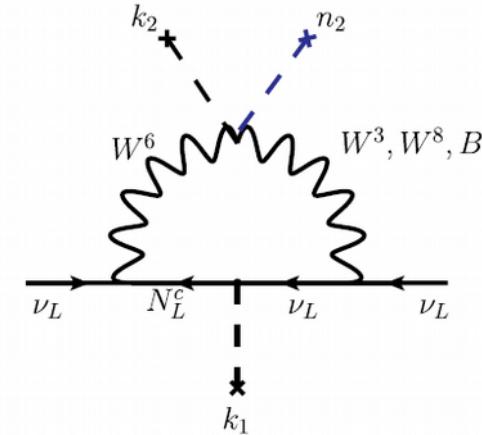
331 motivation # families = # colours
Singer, Valle, Schechter, Phys.Rev. D22 (1980) 738

F.S. Queiroz et al. / Physics Letters B 763 (2016) 269–274



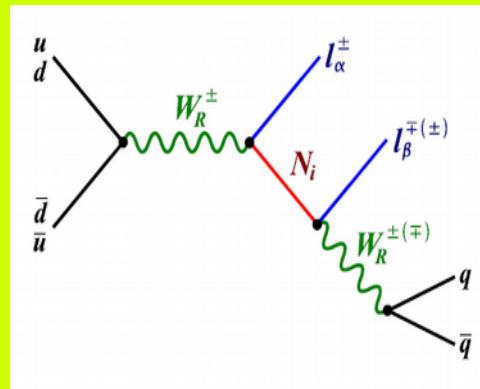
Gauge vs Higgs origin

PHYSICAL REVIEW D 90, 013005 (2014)

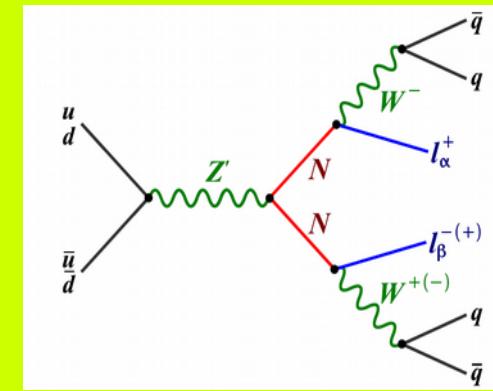


Boucenna, Morisi, JV Phys.Rev. D90 (2014) 013005

seesaw mediator searches with new gauge portal

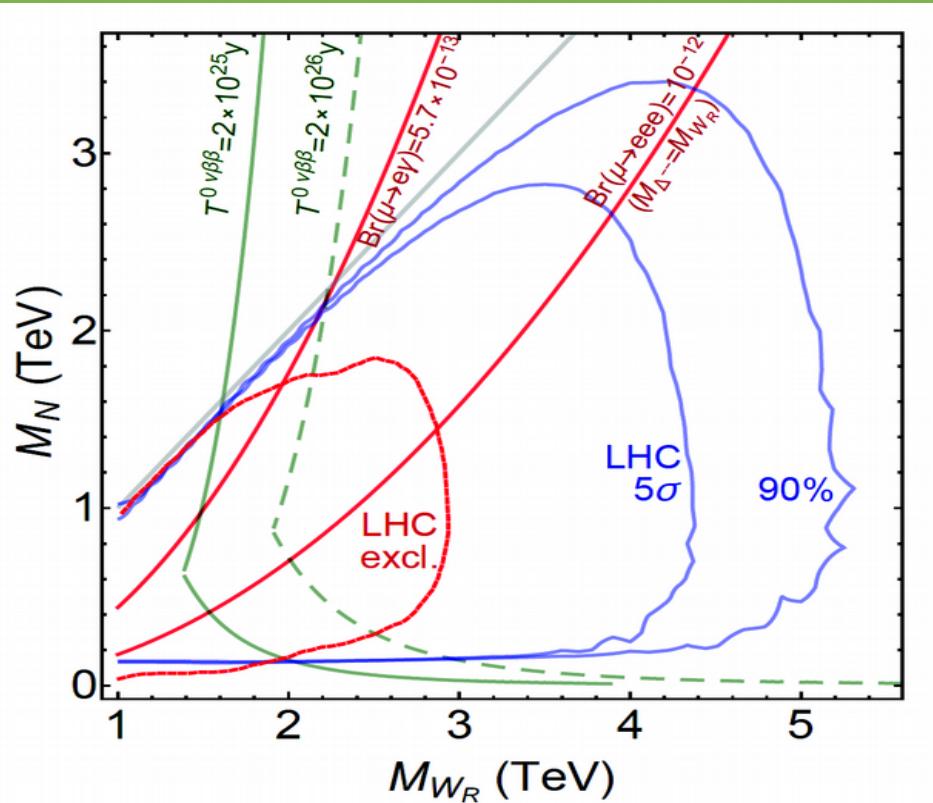


**extended
EW theory
at LHC**

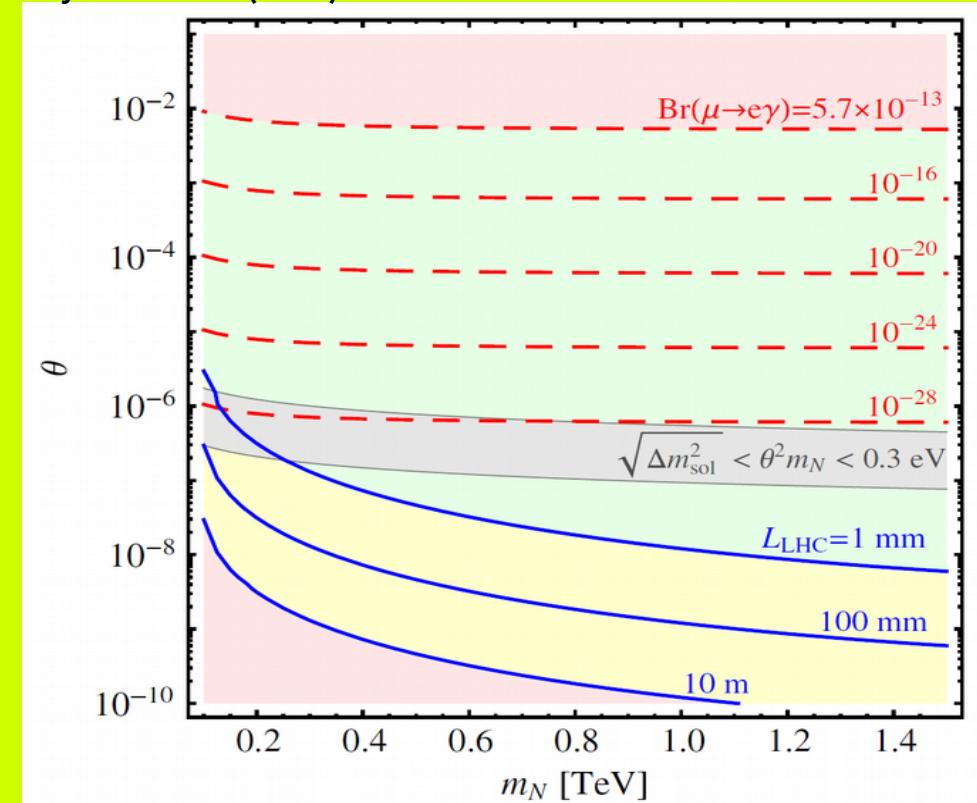


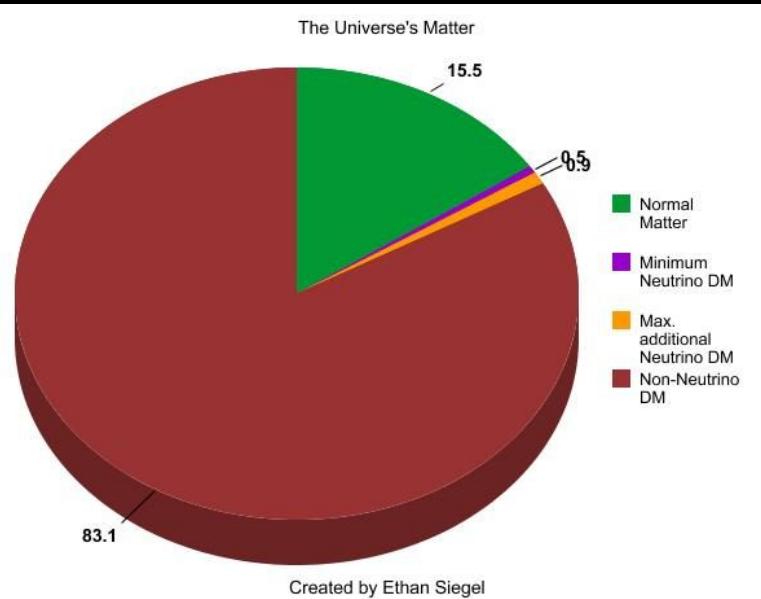
**lepton flavor violation
as a HE phenomenon?**

Phys.Rev. D86 (2012) 055006 & New J.Phys. 17 (2015) 075019



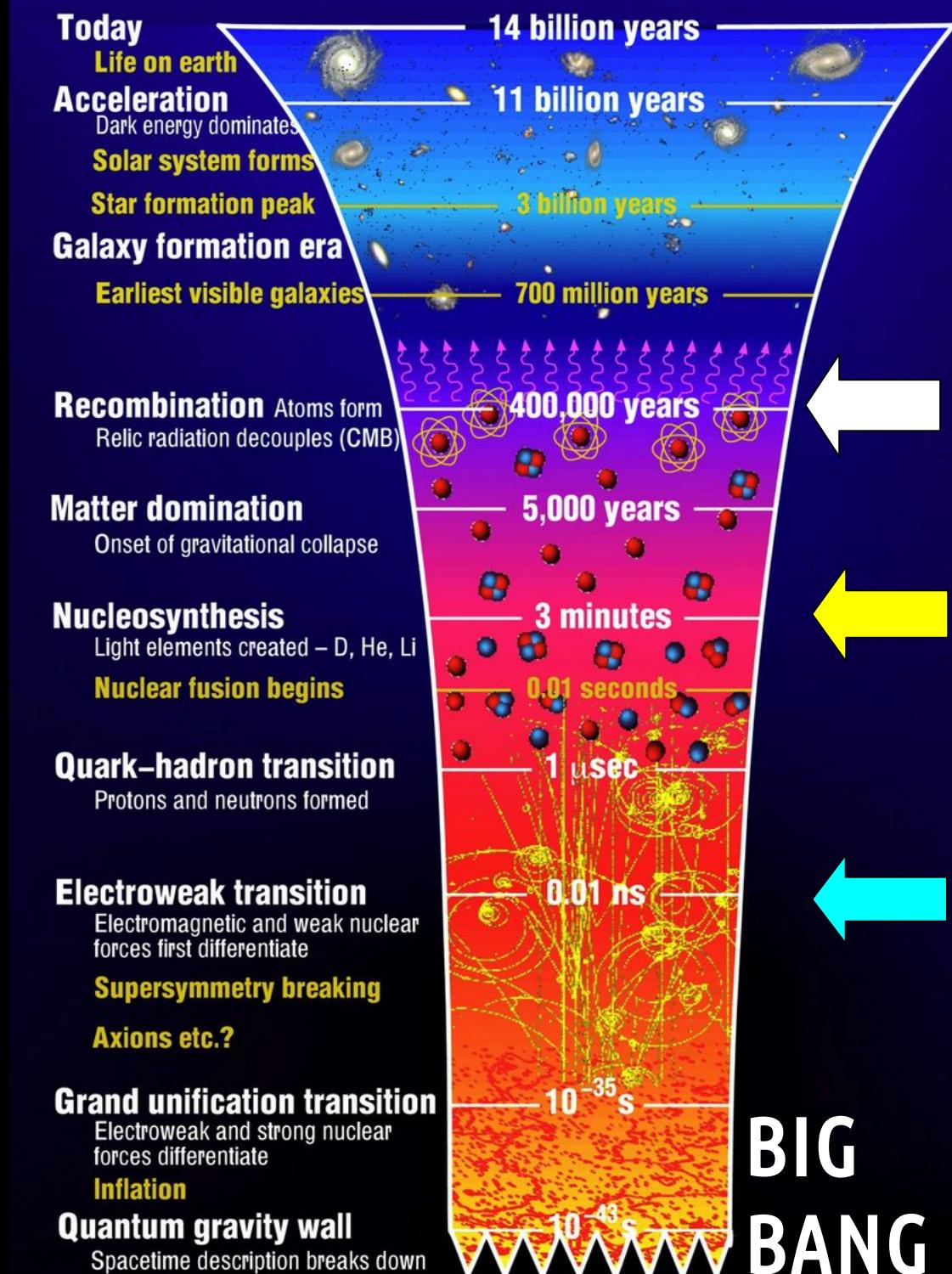
Phys.Rev. D89 (2014) 051302





need for dark matter

nu's at most 1% but can be key to DM

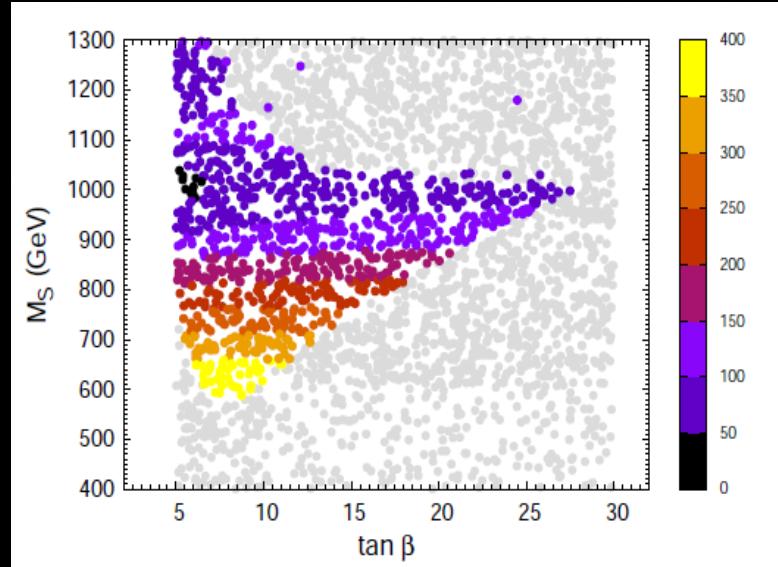


If neutrinos get mass a
la Inverse seesaw susy
Spectrum can change so ...

LSP is SNEUTRINO-like
instead of neutralino ..

Arina et al PRL101 (2008) 161802
Bazzocchi, Cerdeno, Munoz, JV, PRD81 (2010) 051701

SUSY WIMP AS COLD DARK MATTER

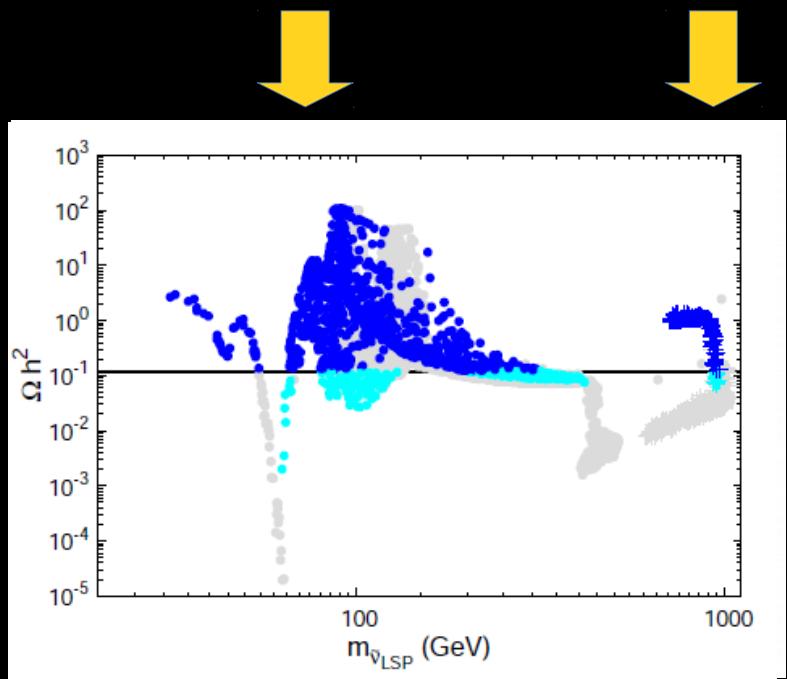
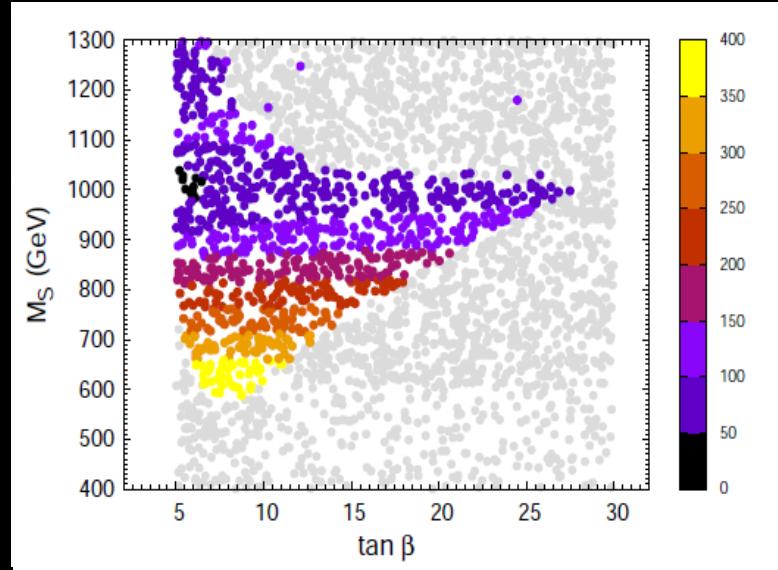


If neutrinos get mass a la Inverse seesaw susy
Spectrum can change so ...

SUSY WIMP AS COLD DARK MATTER

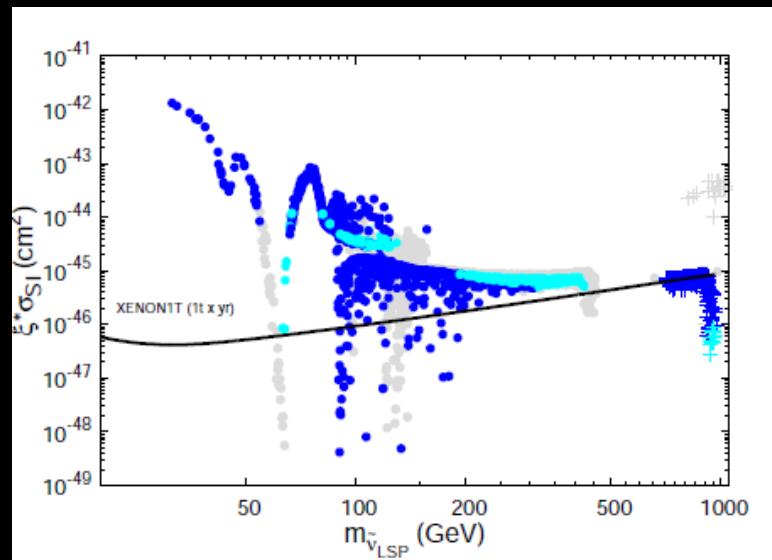
LSP is SNEUTRINO-like
instead of neutralino ..

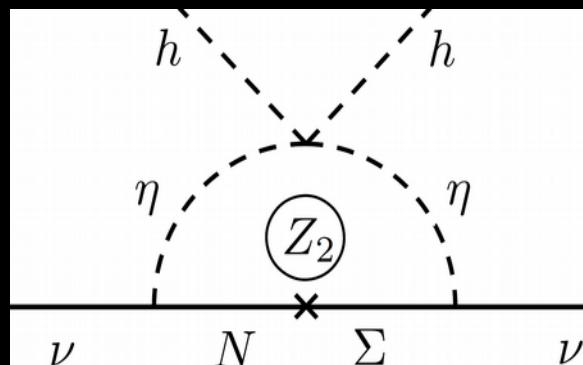
Arina et al PRL101 (2008) 161802
Bazzocchi, Cerdeno, Munoz, JV, PRD81 (2010) 051701



back

De Romeri, Patel, Valle arXiv:1808.01453





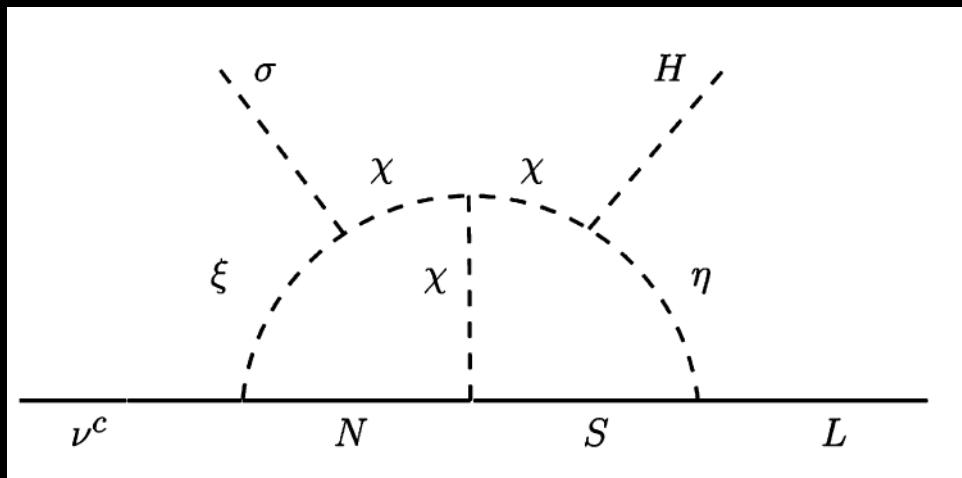
neutrino mass messenger WIMP as dark matter

E Ma 2006 "scotogenic"

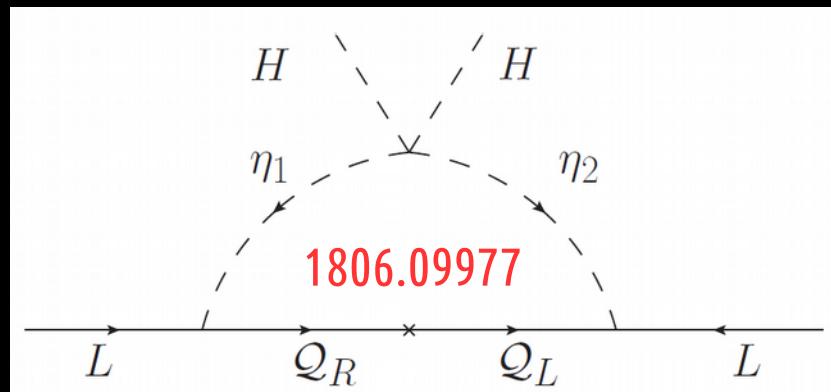
Hirsch et al JHEP 1310 (2013) 149
 Merle et al JHEP 1607 (2016) 013
 Diaz et al JHEP01(2016)007



Z2 preserved by RGE
 many variants, e.g.



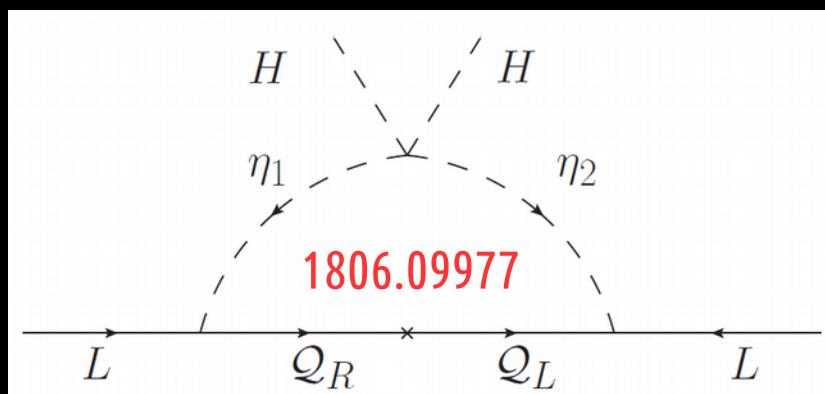
dark matter as bound-state of neutrino mass messenger



Reig, Restrepo, Valle, Zapata

De Luca, Mitridate, Redi, Smirnov, Strumia

dark matter as bound-state of neutrino mass messenger



Reig, Restrepo, Valle, Zapata

De Luca, Mitridate, Redi, Smirnov, Strumia

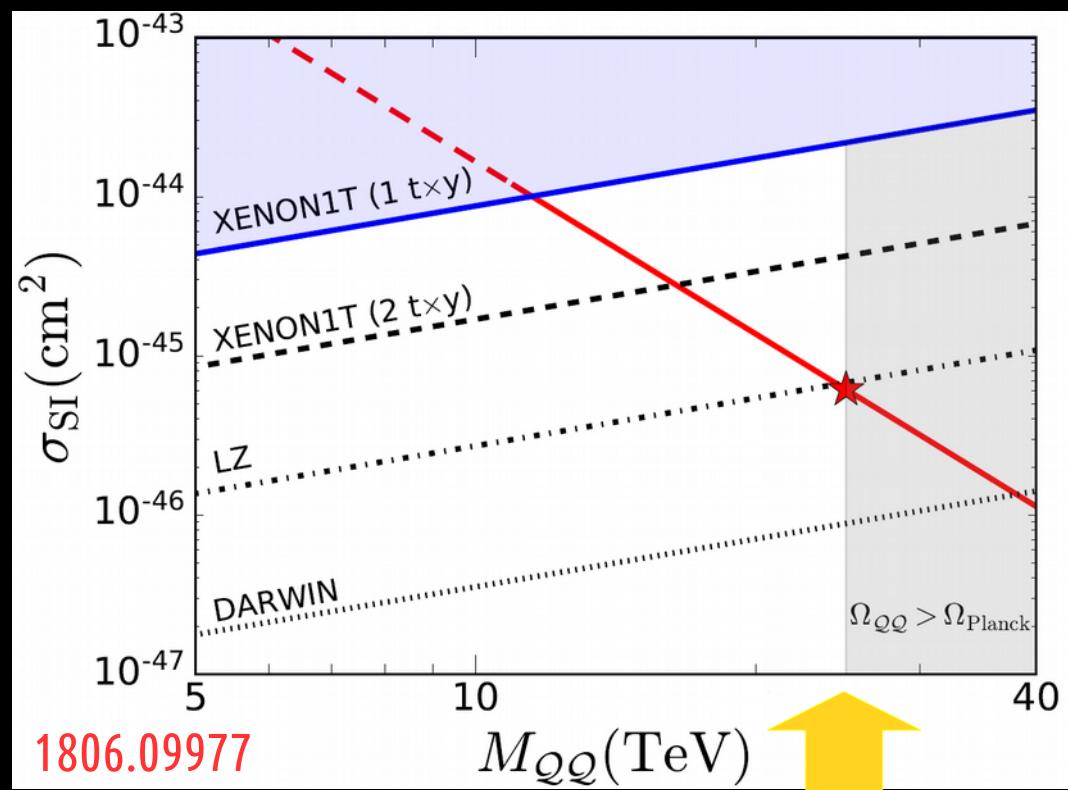
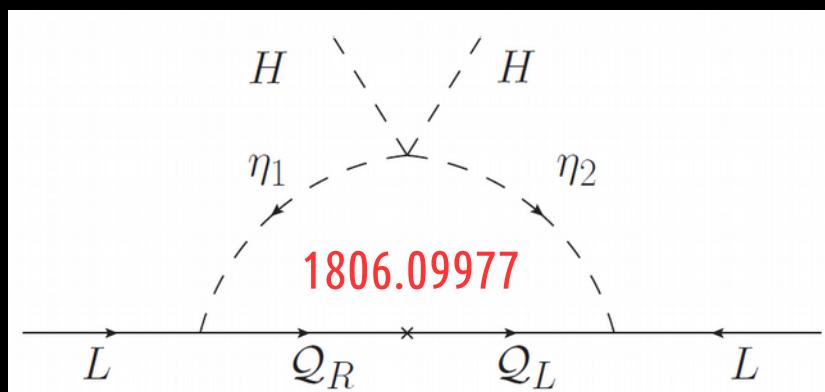


FIG. 2. Spin-independent cross section as a function of $M_{QQ} = 2M_Q$ (red). The star represents the mass required for a thermal bound state 25 TeV dark matter. Lower values can be probed by direct searches, the current bound is indicated in blue, while the black lines (dashed, dotted and dot-dashed) correspond to future sensitivities. **back**

dark matter as bound-state of neutrino mass messenger



Reig, Restrepo, Valle, Zapata

De Luca, Mitridate, Redi, Smirnov, Strumia

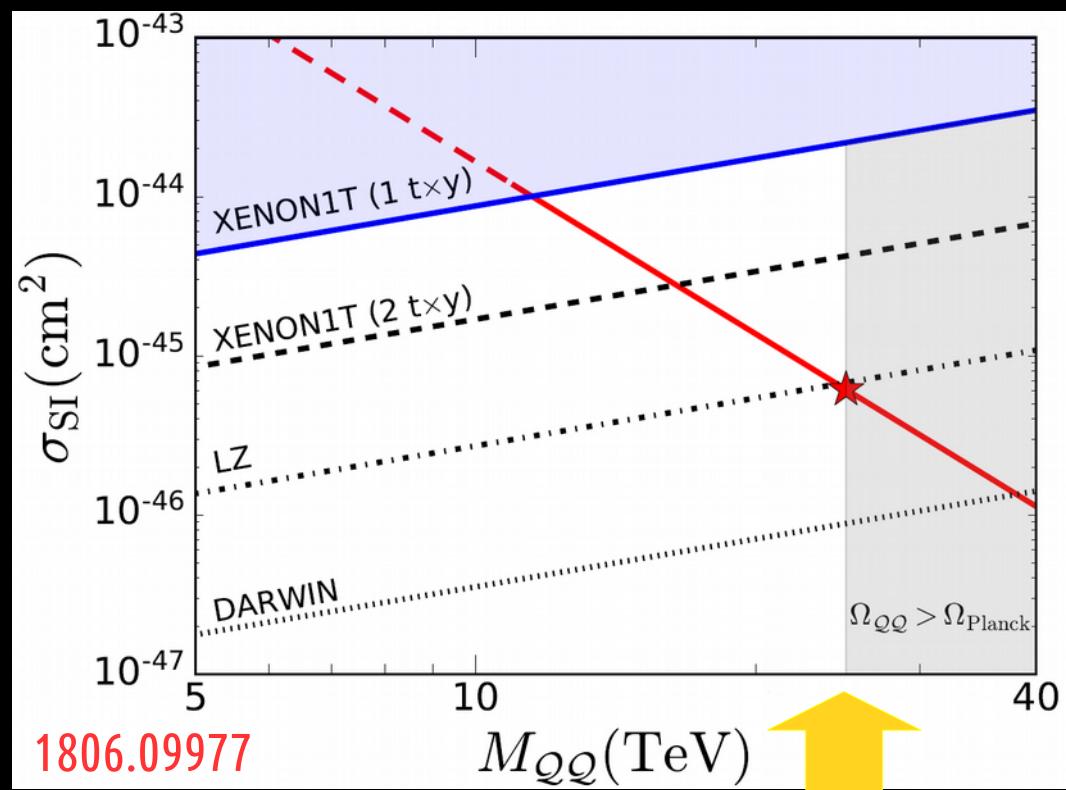


FIG. 2. Spin-independent cross section as a function of $M_{QQ} = 2M_Q$ (red). The star represents the mass required for a thermal bound state 25 TeV dark matter. Lower values can be probed by direct searches, the current bound is indicated in blue, while the black lines (dashed, dotted and dot-dashed) correspond to future sensitivities. **back**

detecting messengers & measuring angles @ high energies
neutrinos lie at the center of particle physics, e.g. EWSB



detecting messengers & measuring angles @ high energies

neutrinos lie at the center of particle physics, e.g. EWSB

comprehensive



**flavor theory
with new physics
above 10 TeV**

detecting messengers & measuring angles @ high energies
neutrinos lie at the center of particle physics, e.g. EWSB



cosmology as emergent theory
implies new physics @ colliders

comprehensive
**flavor theory
with new physics
above 10 TeV**

Sneutrino-like CWDM Gravitino CDM

WIMP DM stability from flavor: discrete DM

WIMP DM stability from Diracness

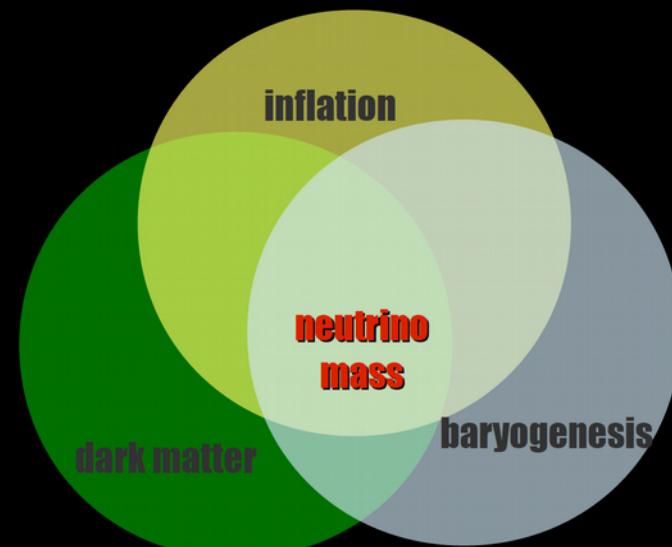
Bound-state dark matter

WIMP DM stability from gauge matter parity

DM can be warm & metastable, e.g. the majoron

majoron DM + inflation

adding dark energy Smoot arXiv:1405.2776 etc etc



THE END

decaying Gravitino dark matter

decays suppressed by Planck mass & smallness of m- ν

$$\Gamma = \Gamma(\tilde{G} \rightarrow \sum_i \nu_i \gamma) \simeq \frac{1}{32\pi} |U_{\tilde{\gamma}\nu}|^2 \frac{m_{\tilde{G}}^3}{M_P^2}$$

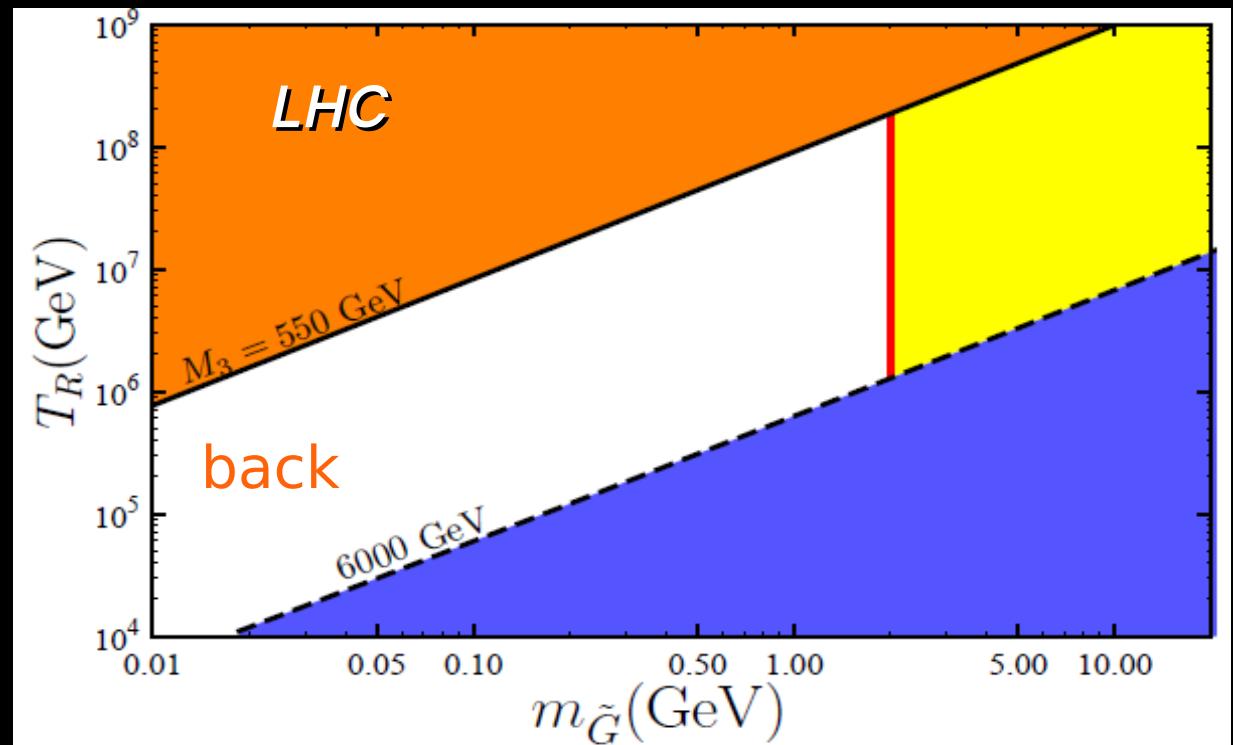
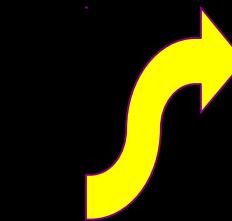
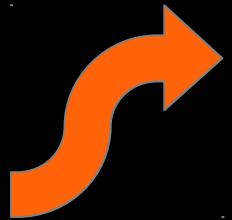
chosen to fit neutrino osc. data



Restrepo et al
PRD85 (2012) 023523

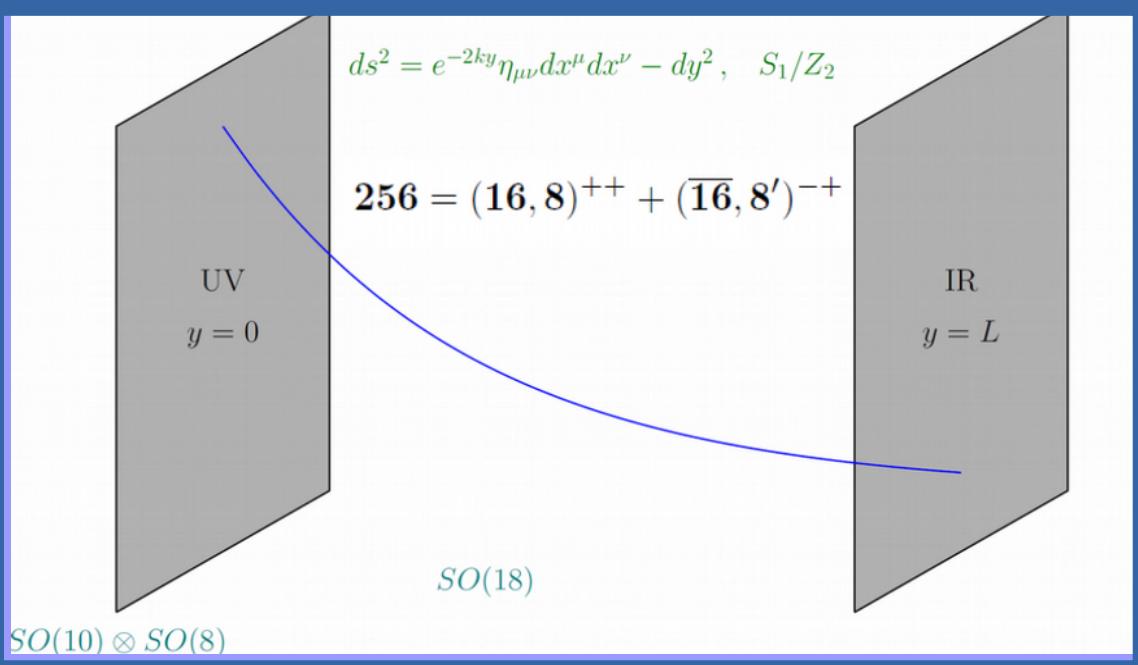
relic abundance
+ LHC searches

excluded by gamma
line searches @
Egret & Fermi-LAT



Unifying forces & families

inspired by beauty of neutrinos in SO10



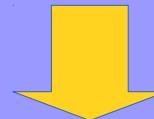
$$16 \rightarrow (3, 2, 1/6) + (1, 2, -1/2) + (\bar{3}, 1, 1/3) \\ + (\bar{3}, 1, -2/3) + (1, 1, 1) + (1, 1, 0),$$

Reig, Valle, Vaquera-Araujo, Wilczek

Phys.Lett. B774 (2017) 667-670

unwanted chiral families bound
by new hypercolor force above TeV

new spectroscopy



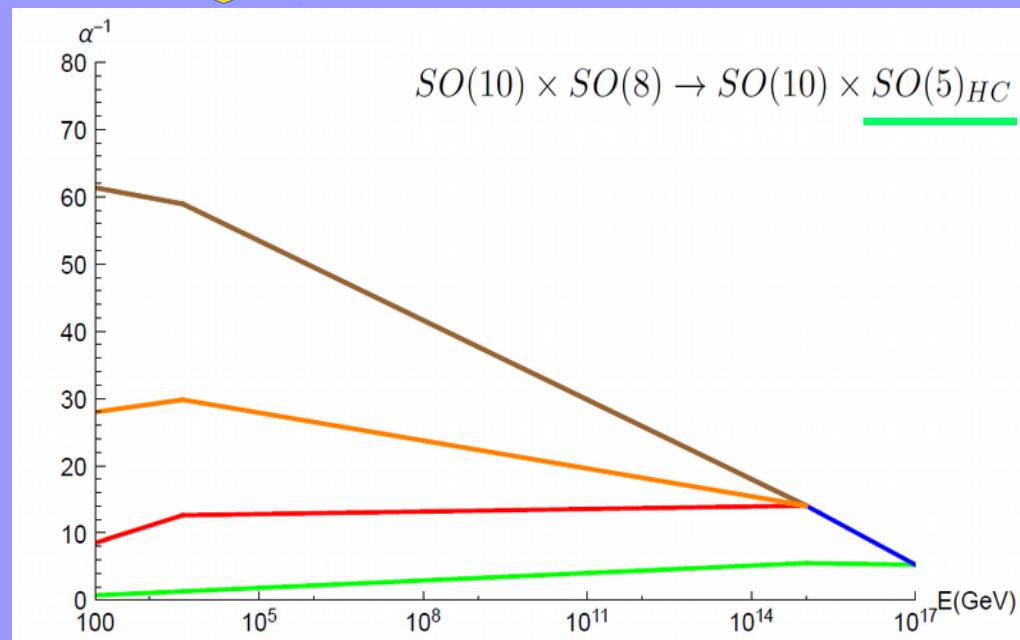
promote M4 to AdS5 & use orbifold BC to decouple mirrors

SO(3) family symmetry

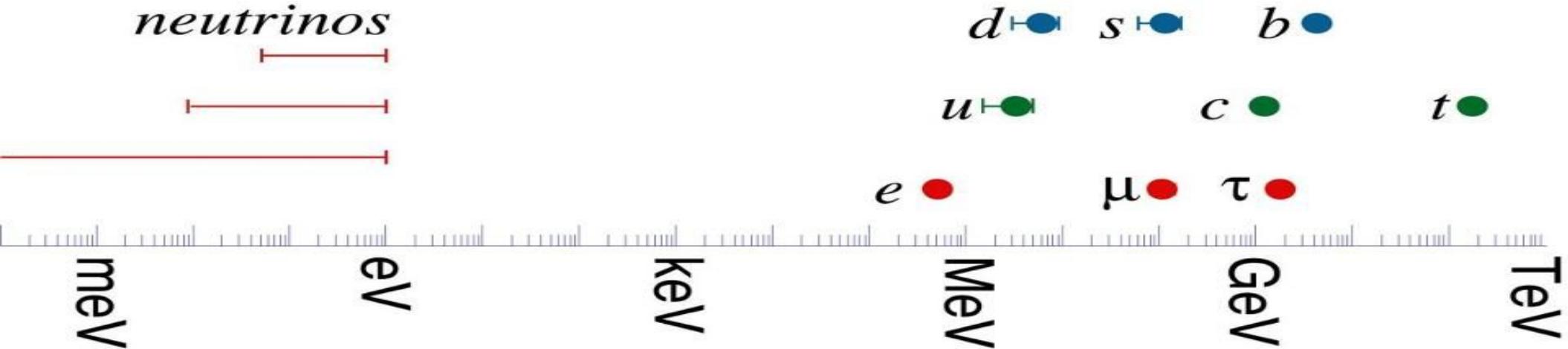
Reig, JV, Wilczek
arXiv:1805.08048

	q_L	u_R	d_R	l_L	e_R	ν_R	Φ^u	Φ^d	Ψ^u	Ψ^d	σ	ρ
$SU(3)_c$	3	3	3	1	1	1	1	1	1	1	1	1
$SU(2)_L$	2	1	1	2	1	1	2	2	2	2	1	1
$U(1)_Y$	$\frac{1}{6}$	$\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{1}{2}$	-1	0	$-\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	0	0
$SO(3)_F$	3	3	3	3	3	3	5	5	3	3	5	1
$U(1)_{PQ}$	1	-1	-1	1	-1	-1	2	2	2	2	2	2

back



$$SO(10) \times SO(8) \rightarrow SO(10) \times SO(5)_{HC}$$

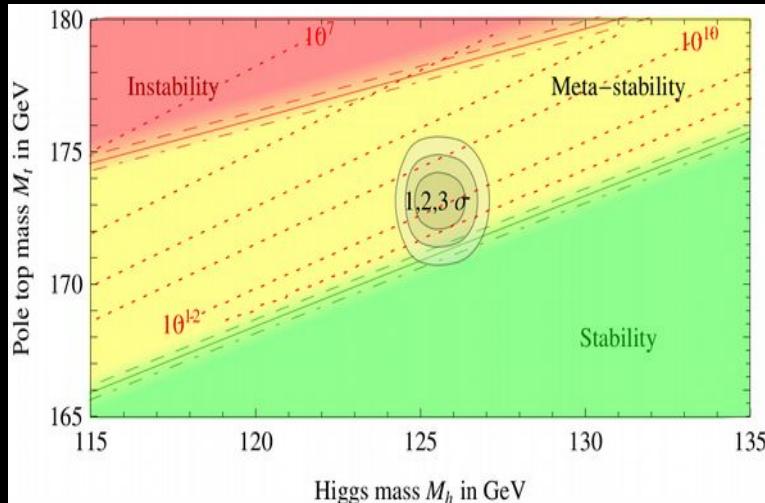


from oscillations to charged fermion masses

- Morisi et al Phys.Rev. D84 (2011) 036003
- King et al Phys. Lett. B 724 (2013) 68
- Morisi et al Phys.Rev. D88 (2013) 036001
- Bonilla et al Phys.Lett. B742 (2015) 99

**Golden Q-L
unification**

$$\frac{m_\tau}{\sqrt{m_e m_\mu}} \approx \frac{m_b}{\sqrt{m_d m_s}}$$



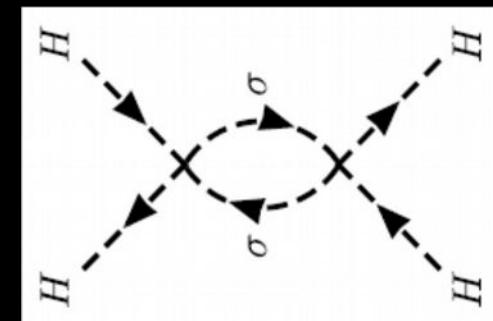
From Degrassi et al: JHEP 1208 (2012) 098

Higgs searches **Bonilla et al**

benchmark for EW studies @ colliders

neutrinos make the EW vacuum **Stable again**

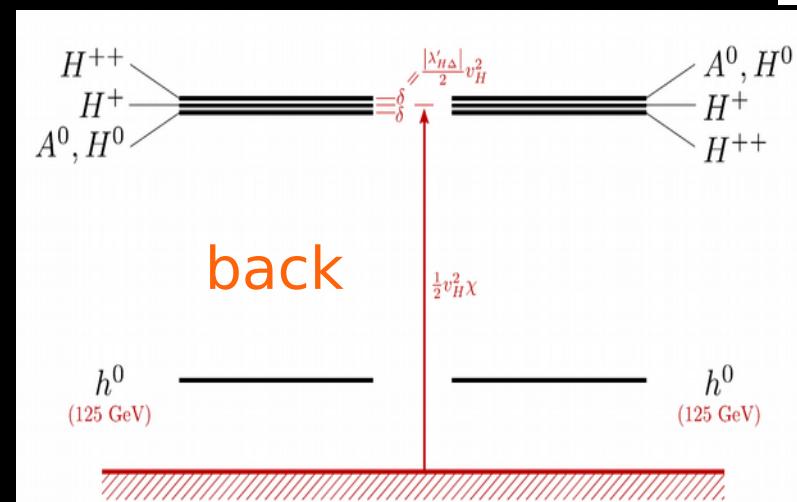
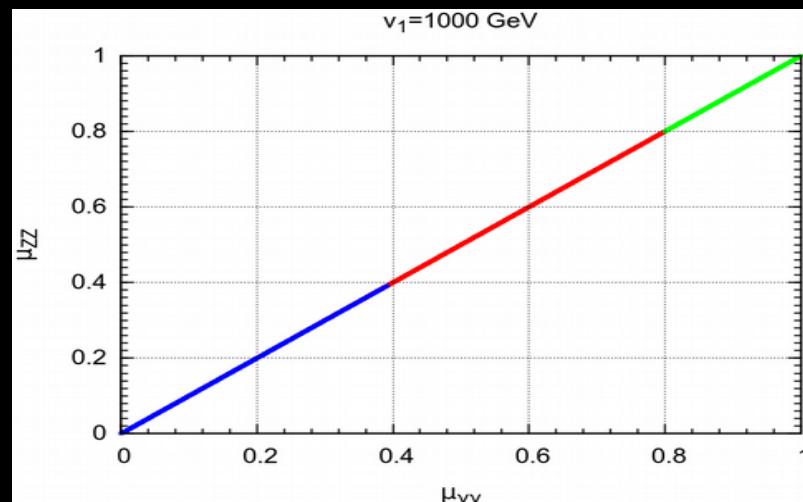
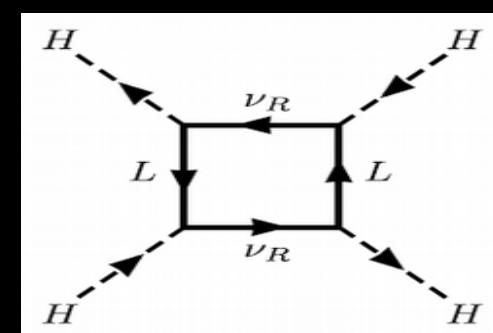
Phys.Rev. D92 (2015) 075028



Phys.Lett. B756 (2016) 345-349

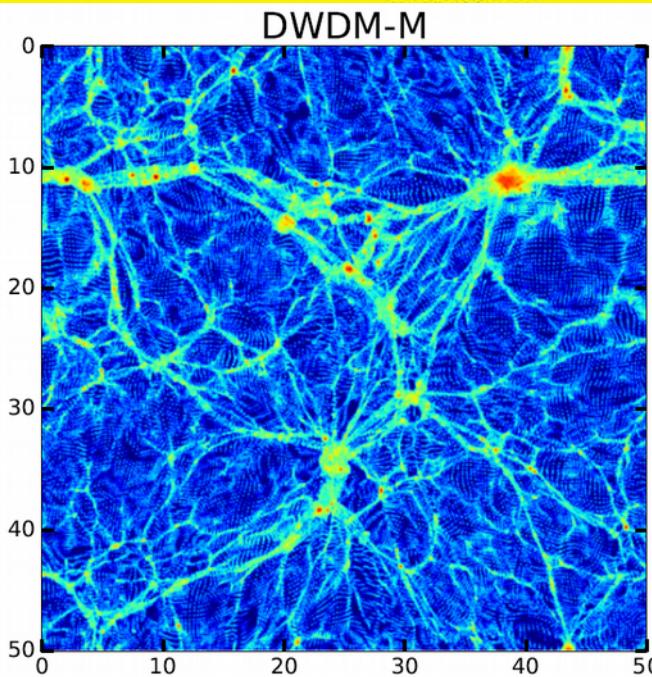
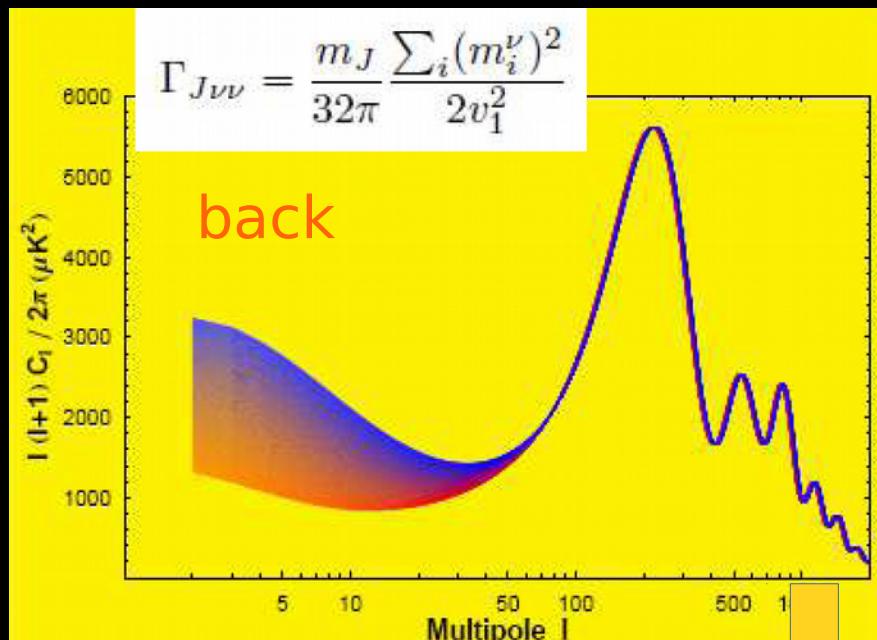
New J. Phys. 18 (2016) 033033

Phys.Rev. D91 (2015) 113015



Consistency with CMB

Lattanzi & Valle, PRL99 (2007) 121301

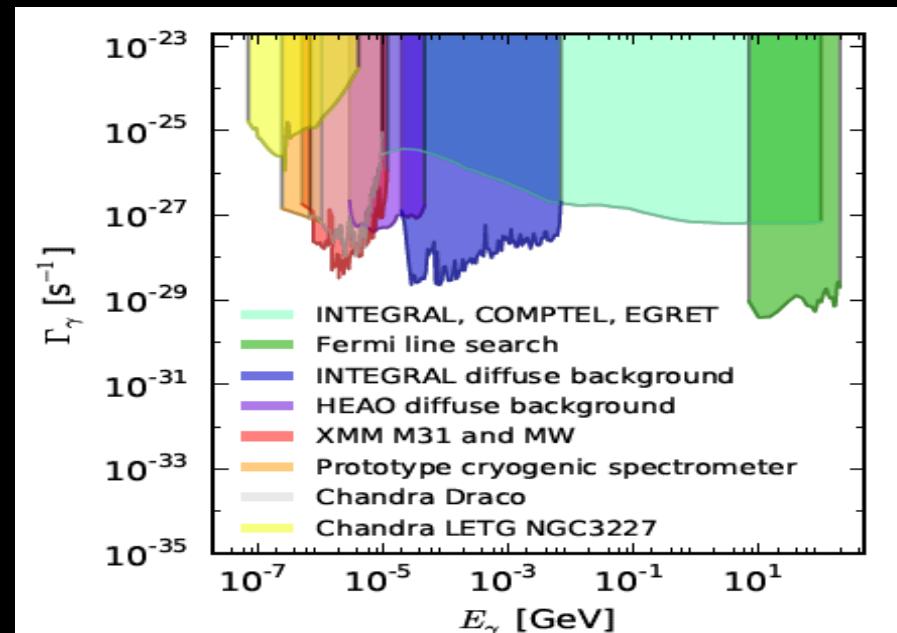


Kuo et al 1803.05650

DWDM picture leads to a viable alternative to the Λ CDM

majorons as dark matter

Berezinsky, Valle PLB318 (1993) 360



$J \rightarrow \gamma\gamma$

X-rays from DM decay

Bazzocchi & al JCAP 0808 (2008) 013

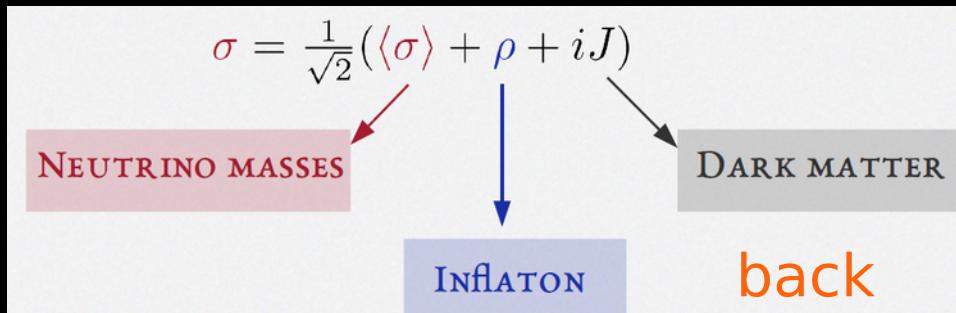
Esteves et al, PRD 82, 073008 (2010)

Lattanzi et al PRD88 (2013) 063528

large scale structure

majoron dark matter & seesaw inflation

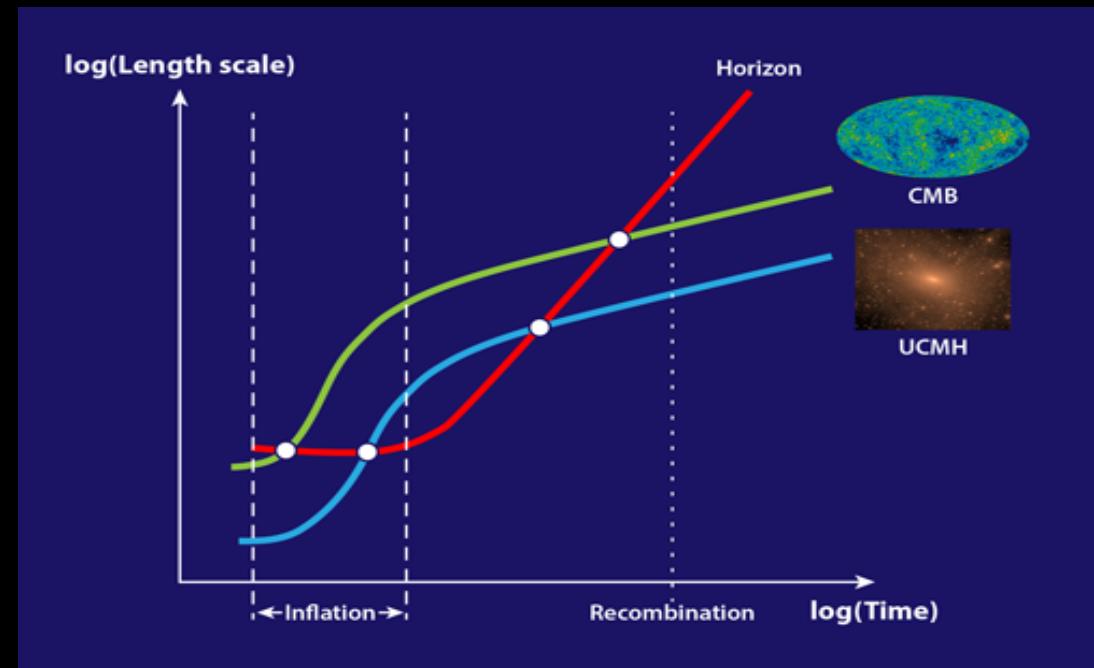
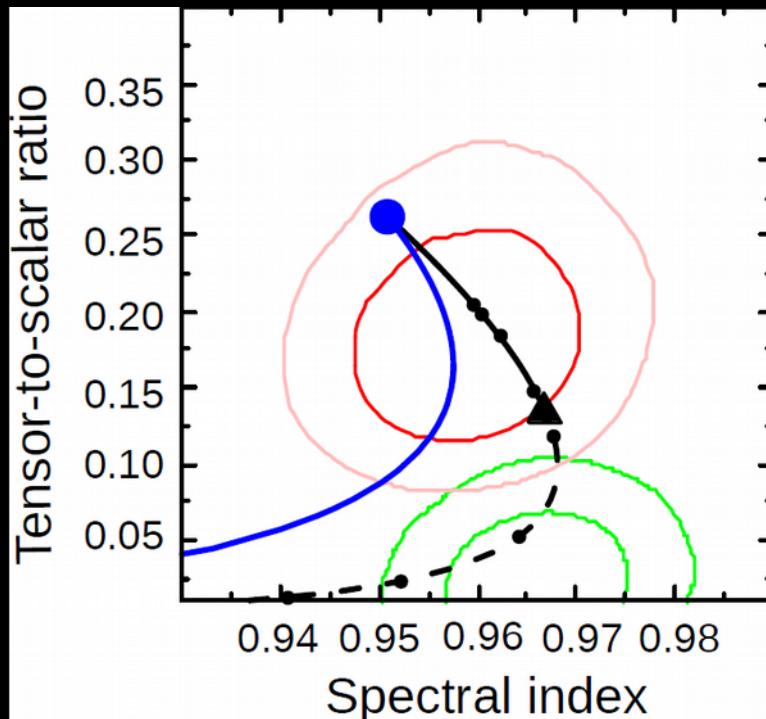
Boucenna, Morisi, Shafi, Valle
Phys.Rev. D90 (2014) 055023



type-I seesaw **Leptogenesis**

Aristizabal et al JCAP 1407 (2014) 052

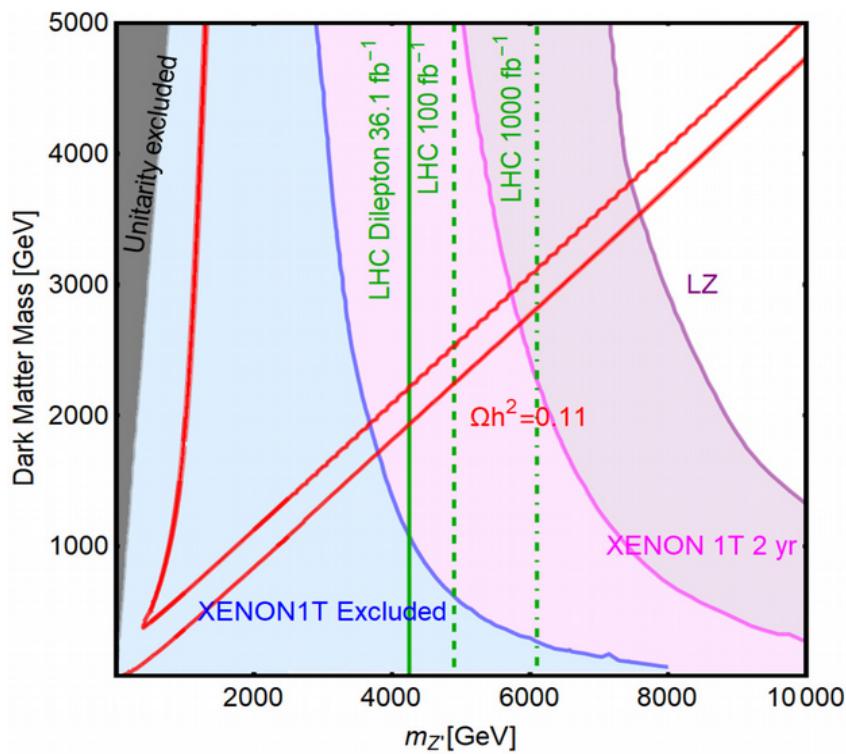
Quartic versus Higgs Inflation



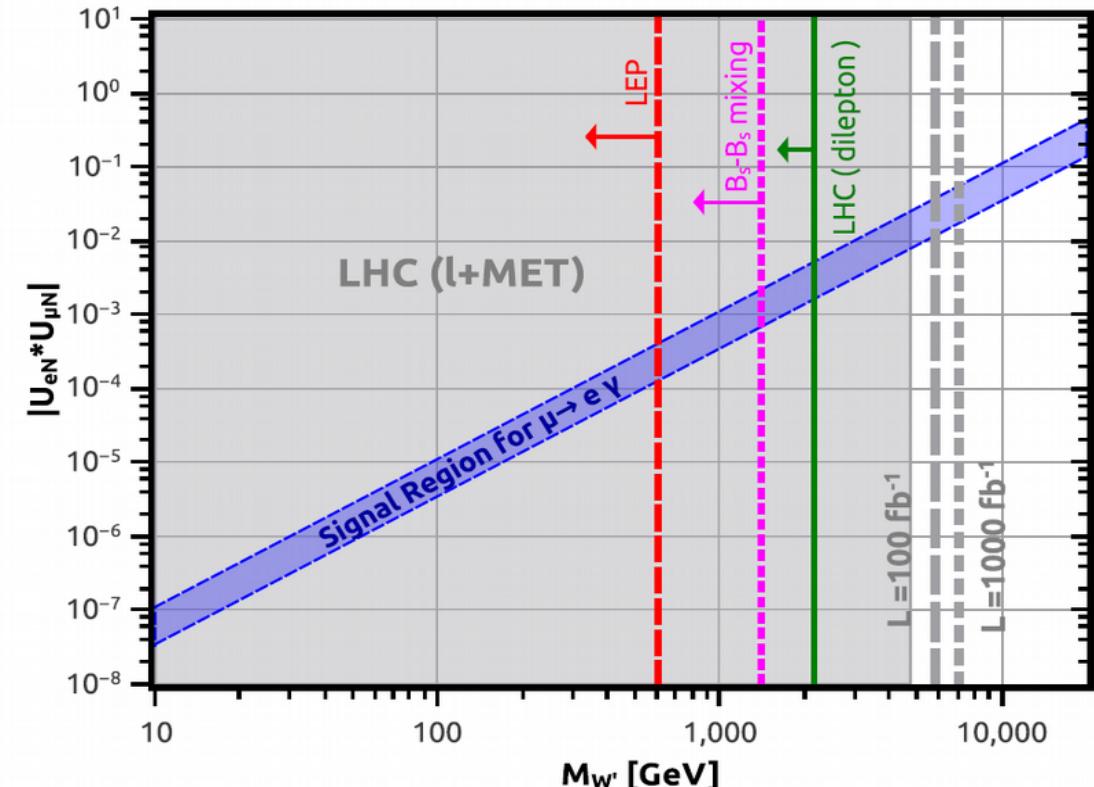
DM stability from gauge matter parity

Alves et al Phys.Lett. B772 (2017) 825–83

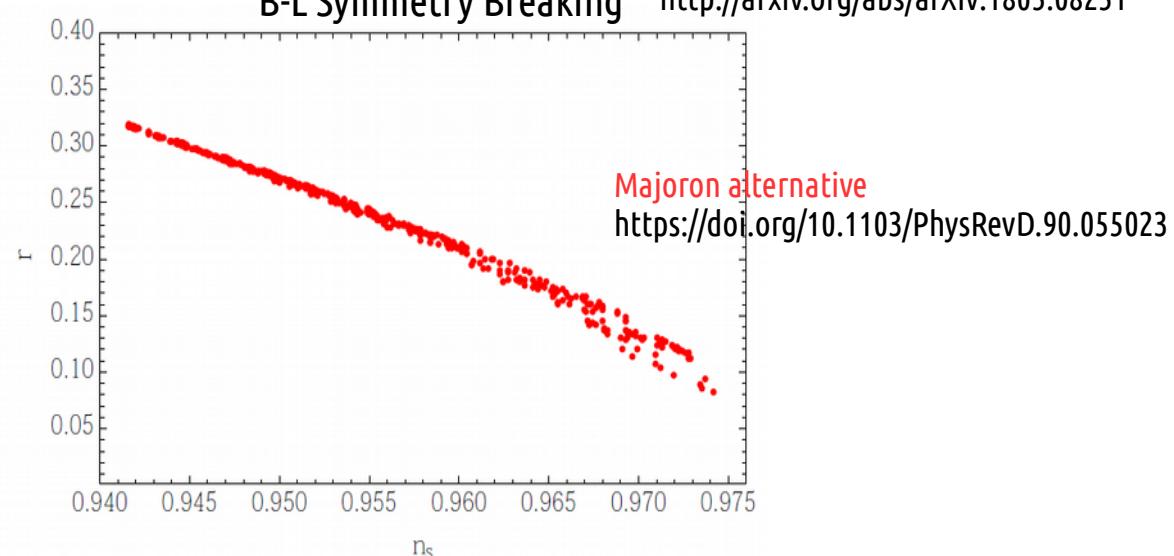
back



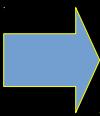
Matter-parity as a residual gauge symmetry: Probing a theory of cosmological dark matter 3-3-1-1 EW extension



Asymmetric Dark Matter, Inflation and Leptogenesis from B-L Symmetry Breaking <http://arxiv.org/abs/arXiv:1805.08251>



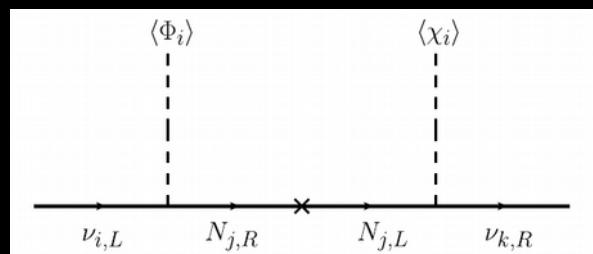
Fields	Z_4	Z_2	Fields	Z_4	Z_2
$\bar{L}_{i,L}$	\mathbf{z}^3	$\mathbf{1}$	$\nu_{i,R}$	\mathbf{z}	-1
$l_{i,R}$	\mathbf{z}	$\mathbf{1}$	$\bar{N}_{i,L}$	\mathbf{z}^3	$\mathbf{1}$
$N_{i,R}$	\mathbf{z}	$\mathbf{1}$			
Φ	$\mathbf{1}$	$\mathbf{1}$	χ	$\mathbf{1}$	-1
ζ	\mathbf{z}	$\mathbf{1}$	η	\mathbf{z}^2	$\mathbf{1}$



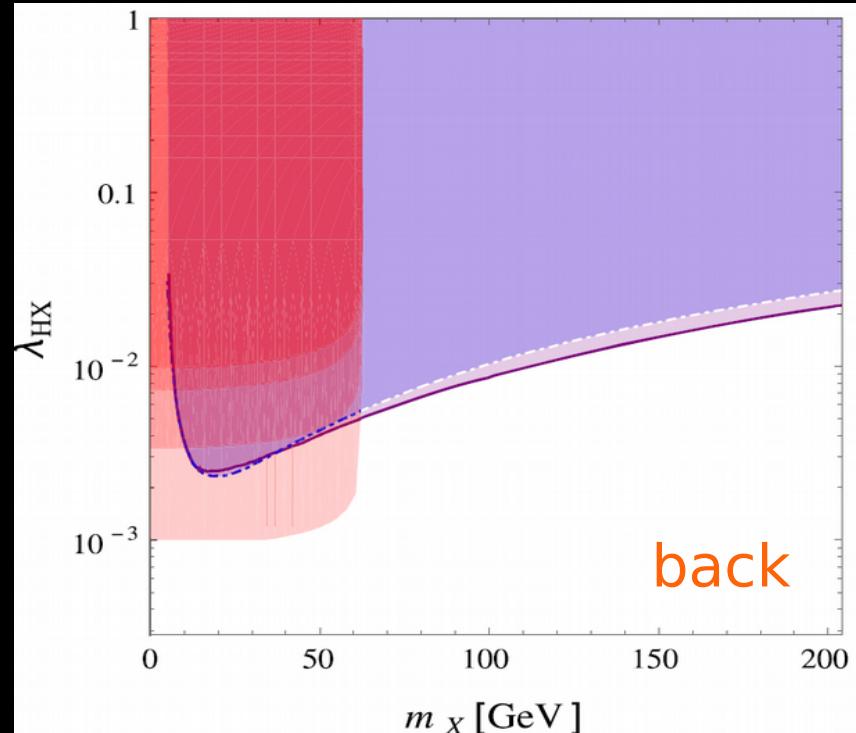
Chiulia et al

arXiv:1606.04543

Phys.Lett. B761 (2016) 431



DM Stability from Diracness



No neutrinoless double- $\beta\beta$ decay

Search for neutrinoless quadruple- $\beta\beta$ decay

<http://arxiv.org/abs/arXiv:1705.08847>

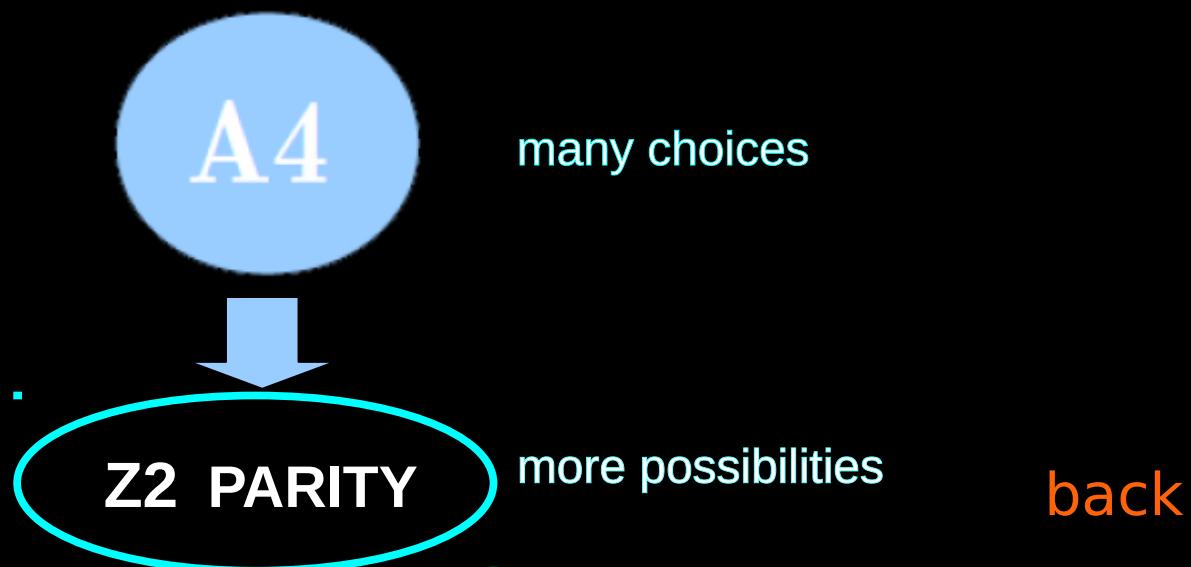
WIMP DARK MATTER FROM FLAVOR SYMMETRY

- accidental ?

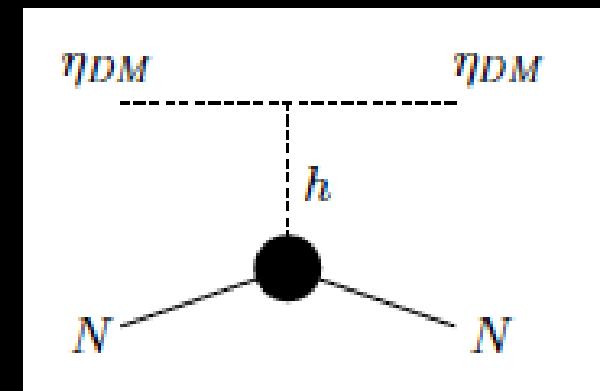
Lavoura, Morisi, JV JHEP 1302(2013) 118

- unbroken subgroup

Boucenna, et al JHEP 1105 (2011) 037
Hirsch, et al Phys.Rev. D82 (2010) 116003

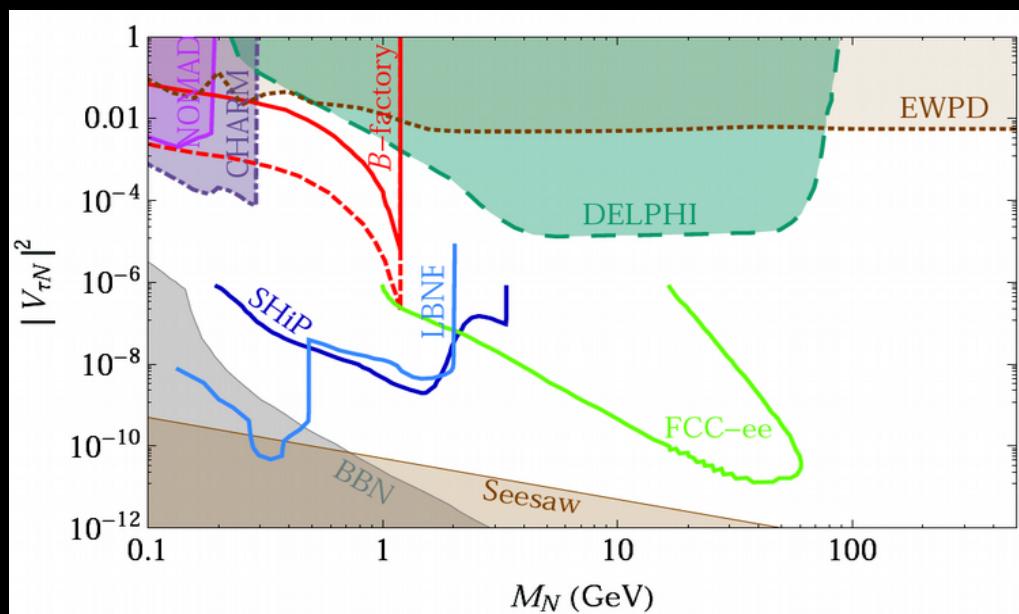
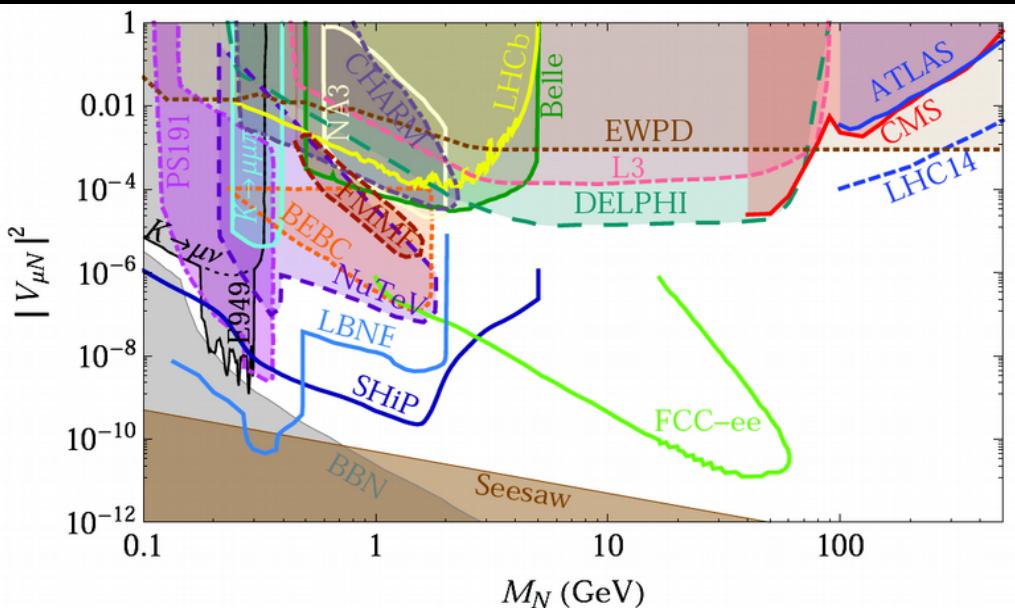
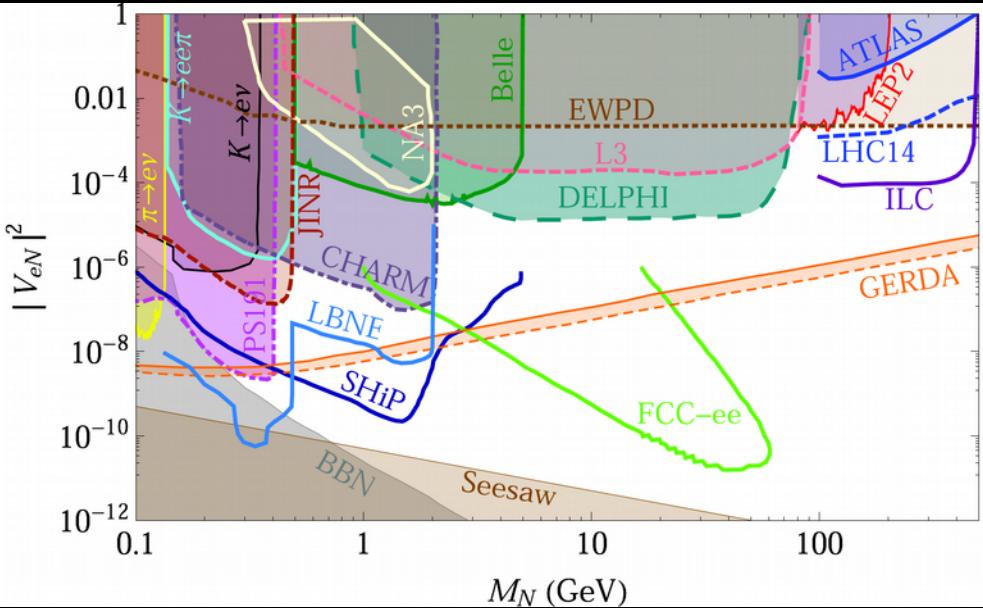


HIGGS PORTAL
DIRECT DETECTION



back

NHL in the Standard model



high vs low
scale seesaw

