

Extra twisted connected sums and their ν -invariants

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Joyce's orbifold construction and the twisted connected sums by Kovalev and Corti-Haskins-Nordström-Pacini provide many examples of compact Riemannian 7-manifolds with holonomy G_2 . We would like to use this wealth of examples to guess further properties of G_2 -manifolds and to find obstructions against holonomy G_2 , taking into account the underlying topological G_2 -structures.

The Crowley-Nordström ν -invariant distinguishes topological G_2 -structures. It vanishes for all twisted connected sums. By adding an extra twist to this construction, we show that the ν -invariant can assume all of its 48 possible values. This shows that G_2 -bordism presents no obstruction against holonomy G_2 . We also exhibit examples of 7-manifolds with disconnected G_2 -moduli space. Our computation of the ν -invariants involves integration of the Bismuth-Cheeger η -forms for families of tori, which can be done either by elementary hyperbolic geometry, or using modular properties of the Dedekind η -function.

Summary

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