

# Electroweak Corrections to Higgs Boson Pair Production: The Light Quark Case [2503.16620]

Marco Bonetti, Philipp Rendler, William J. Torres Bobadilla | July 21, 2025

# Overview

1. Motivation

2. Amplitude

3. Master Integrals

4. Results

5. Conclusion and Outlook

Motivation  
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Amplitude  
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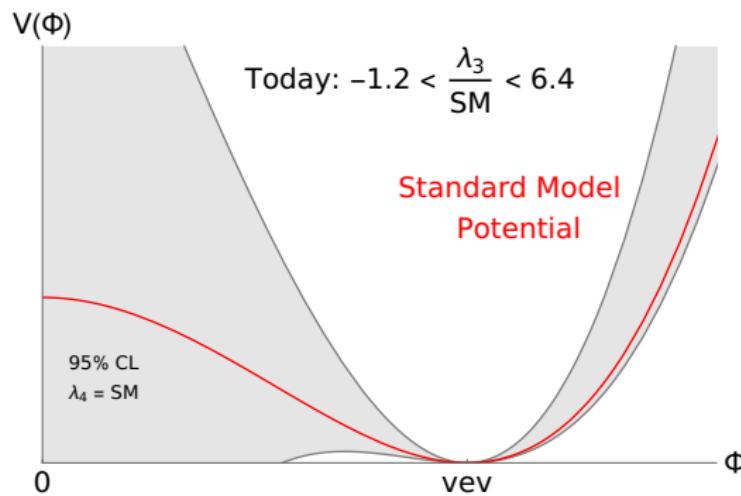
Master Integrals  
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Results  
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Conclusion and Outlook  
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# The Trilinear Higgs Coupling

$$\mathcal{L}_{\text{Higgs}} = \frac{1}{2} (\partial_\mu H) (\partial^\mu H) + \frac{1}{2} m^2 H^2 + \lambda_3 H^3 + \lambda_4 H^4$$



Motivation  
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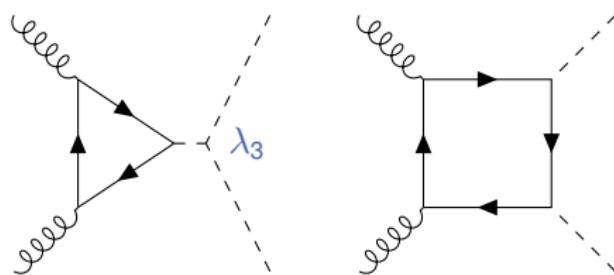
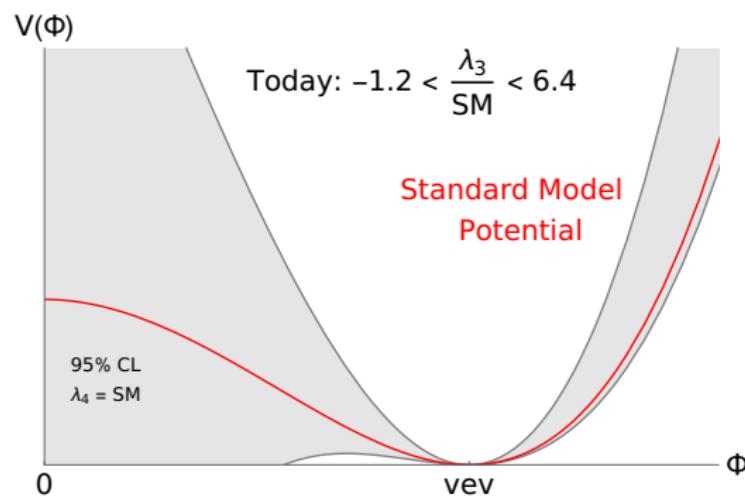
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Conclusion and Outlook  
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## The Trilinear Higgs Coupling

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## Motivation

## Amplitude

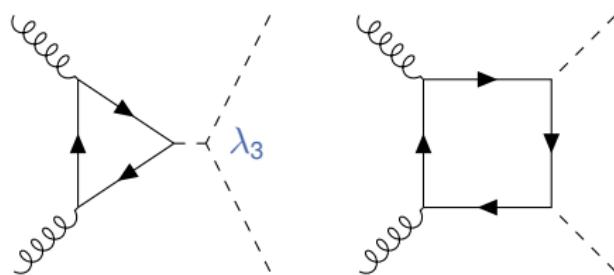
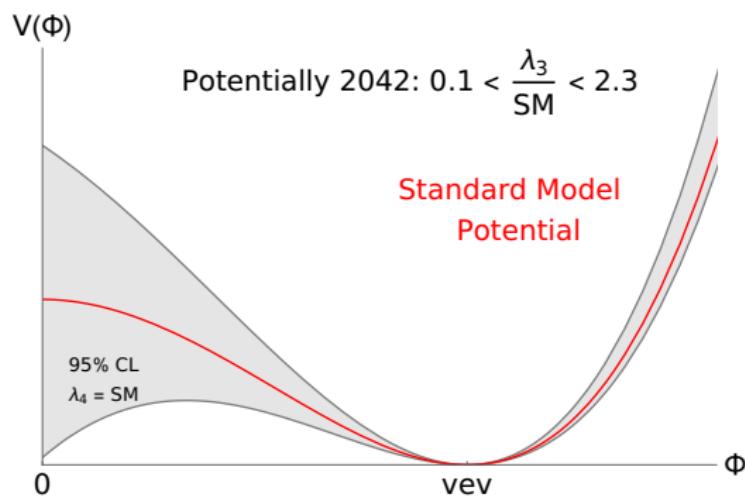
## Master Integrals

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# The Trilinear Higgs Coupling

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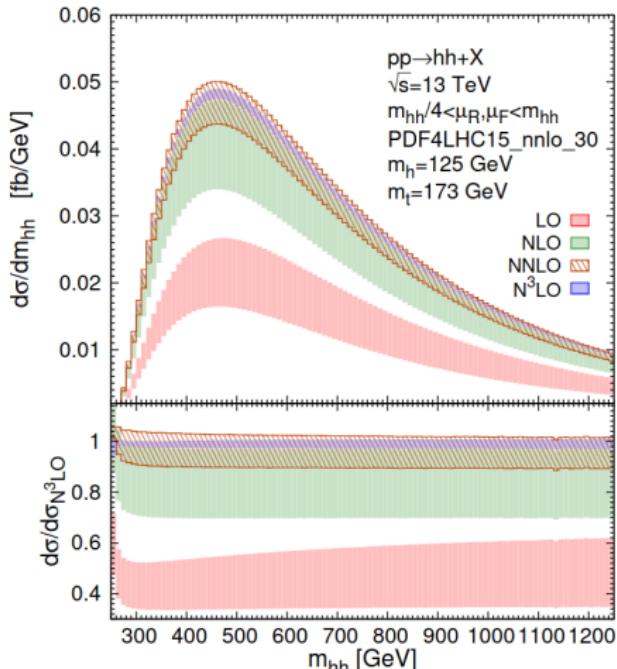
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# QCD Corrections



- QCD: N<sup>3</sup>LO corrections:  
+60 % (NLO) → +30 % (NNLO<sub>HTL</sub>) → +7 % (N<sup>3</sup>LO<sub>HTL</sub>)
  - Currently under investigation: [2501.00587]  
Top mass renormalization uncertainty  $\mathcal{O}(5\%)$
- ⇒ Electroweak corrections are relevant

[1912.13001]

Motivation  
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5/15 July 21, 2025

M. Bonetti, P. Rendler, W. J. Torres Bobadilla: Electroweak Corrections to Higgs Boson Pair Production: The Light Quark Case

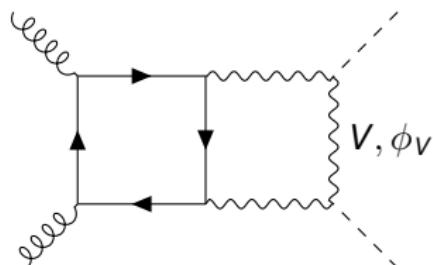
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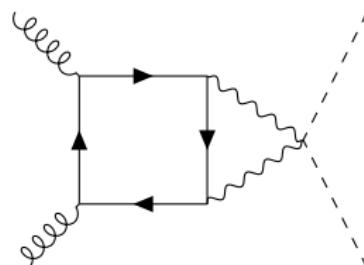
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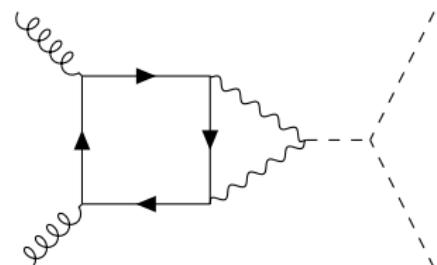
# Electroweak Corrections: The Light Quark Case



(a)  $VVV$



(b)  $VVHH$



(c)  $VH$

Motivation  
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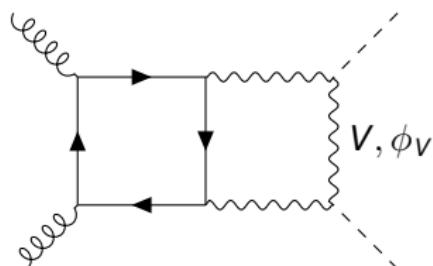
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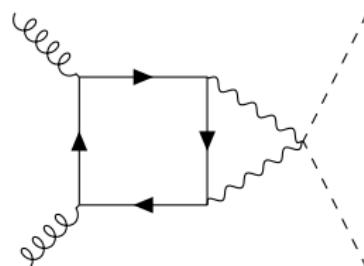
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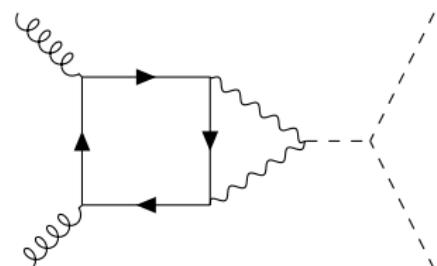
# Electroweak Corrections: The Light Quark Case



(a) **VVV**



(b) **VVHH**



(c) **VVH**

$$\mathcal{M} \propto \begin{cases} \mathcal{F}^{++} = \mathcal{A}_1 + \mathcal{A}_3 + \frac{3m_H^2}{s-m_H^2}\mathcal{A}_3 \\ \mathcal{F}^{+-} = \mathcal{A}_2 \end{cases}$$

Motivation  
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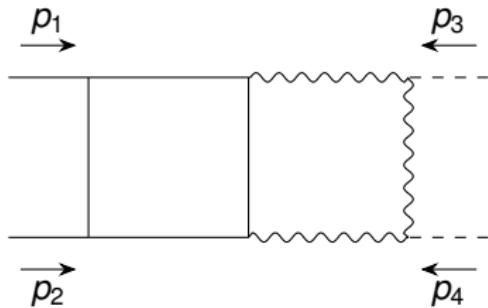
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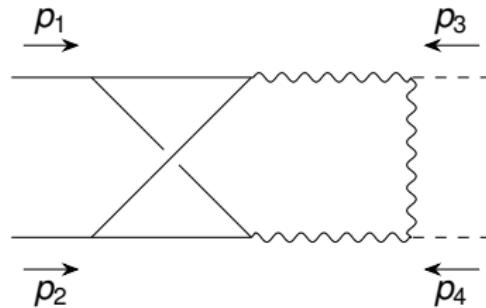
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# Topologies



Planar topology: 45 master integrals



Non-planar topology: 43 master integrals

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# Differential Equations

## DEs in Canonical Form

$$d\mathbf{J} = \varepsilon \sum_{i=1}^{77} \mathbb{A}_i d\log(\alpha_i) \mathbf{J}$$

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# Differential Equations

## DEs in Canonical Form

$$d\mathbf{J} = \varepsilon \sum_{i=1}^{77} \mathbb{A}_i d\log(\alpha_i) \mathbf{J}$$

## Solution: Chen Iterated Integrals

$$\mathbf{J} = \sum_n \varepsilon^n \mathbf{J}^{(n)}$$

$$\mathbf{J}^{(n)} = \int \sum_{i=1}^{77} \mathbb{A}_i d\log(\alpha_i) \mathbf{J}^{(n-1)} + \mathbf{C}^{(n)}$$

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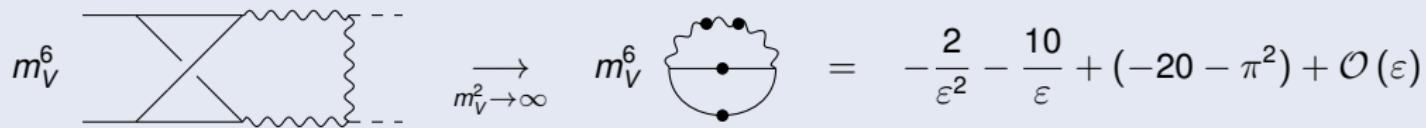
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Conclusion and Outlook  
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# Boundary Conditions

We generate boundary functions with the **large mass expansion**  $m_V^2 \rightarrow \infty$ .

## Example: Large Mass Expansion

$$m_V^6 \begin{array}{c} \text{---} \\ \diagup \quad \diagdown \\ \text{---} \end{array} \xrightarrow{m_V^2 \rightarrow \infty} m_V^6 \begin{array}{c} \text{---} \\ \diagup \quad \diagdown \\ \text{---} \end{array} = -\frac{2}{\varepsilon^2} - \frac{10}{\varepsilon} + (-20 - \pi^2) + \mathcal{O}(\varepsilon)$$


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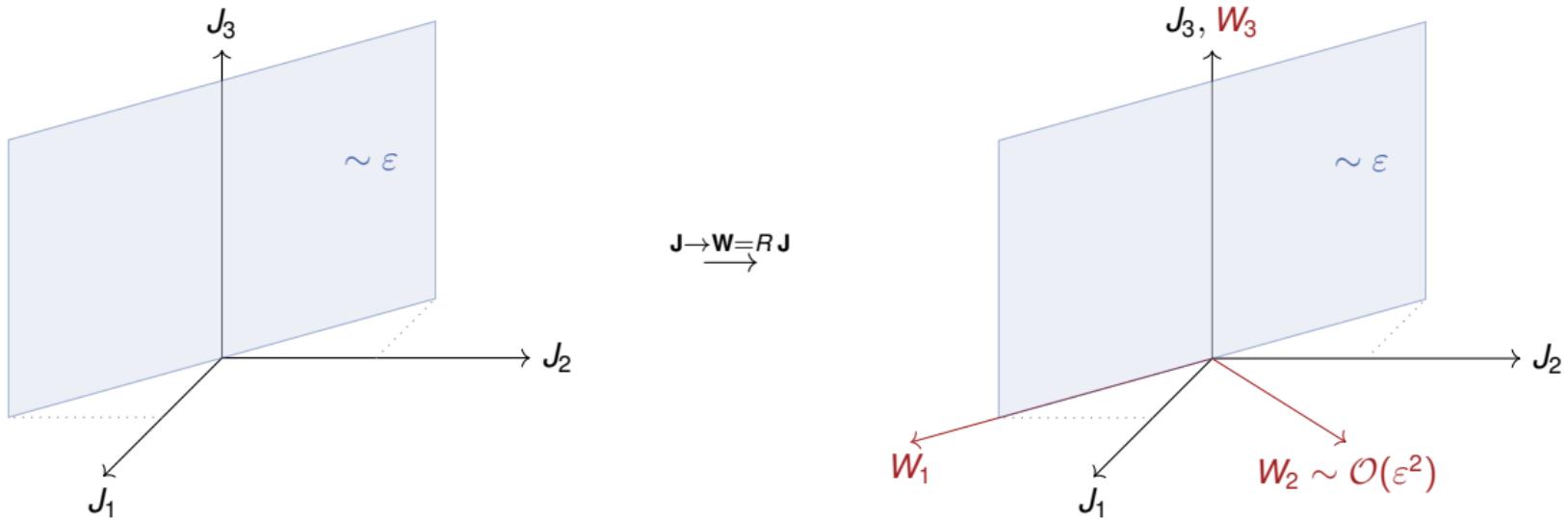
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# Rotation of Canonical Basis



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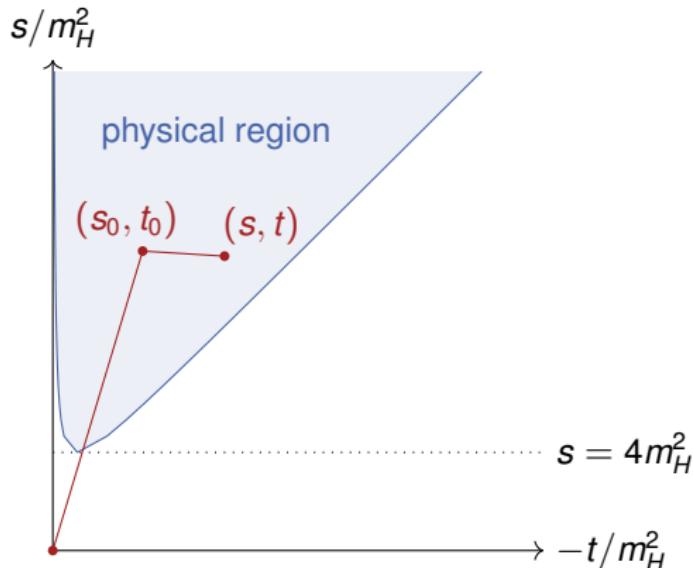
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# Numerical Evaluation



We decompose the rotated basis into **independent functions**,

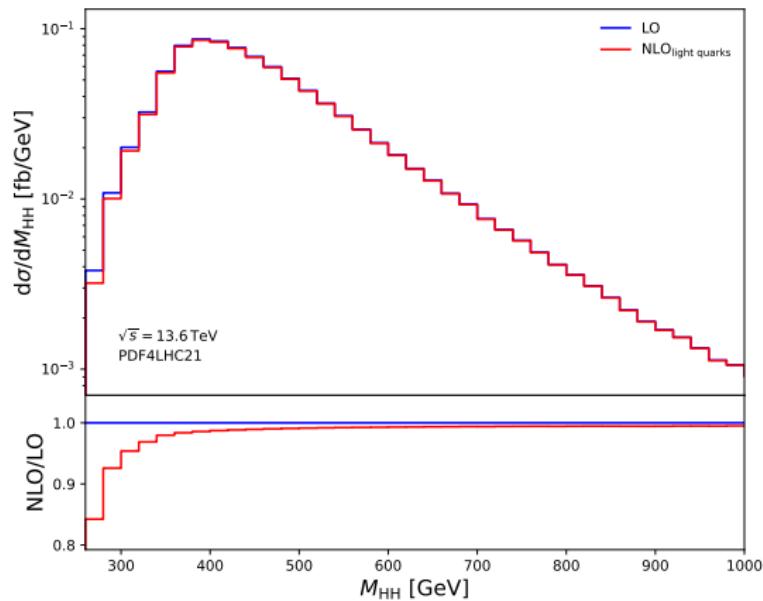
$$W_i(x) = \sum_j \varepsilon^j w_i^{(j)}(x).$$

Then, we construct **differential equations**,

$$dw_i^{(j)} = \sum_k d\Omega_{i,k} w_k^{(j-1)},$$

which we solve with DIFFEXP [2006.05510].

# Results



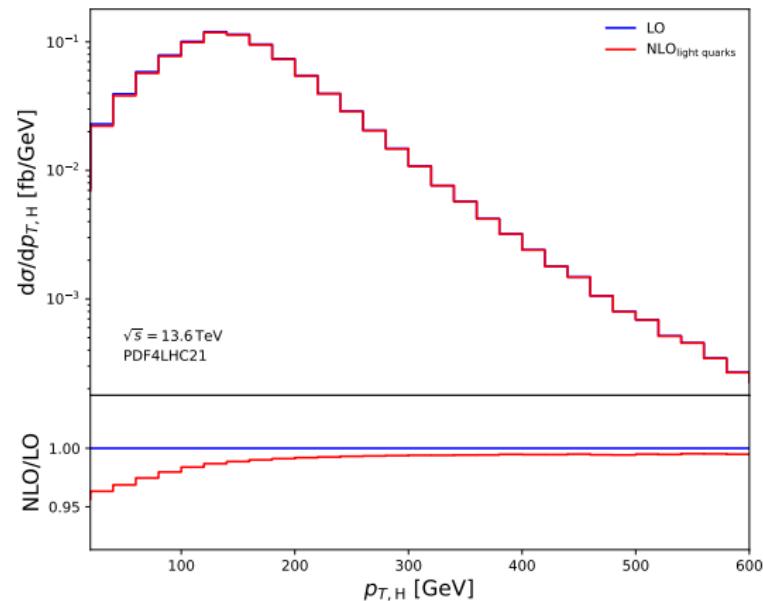
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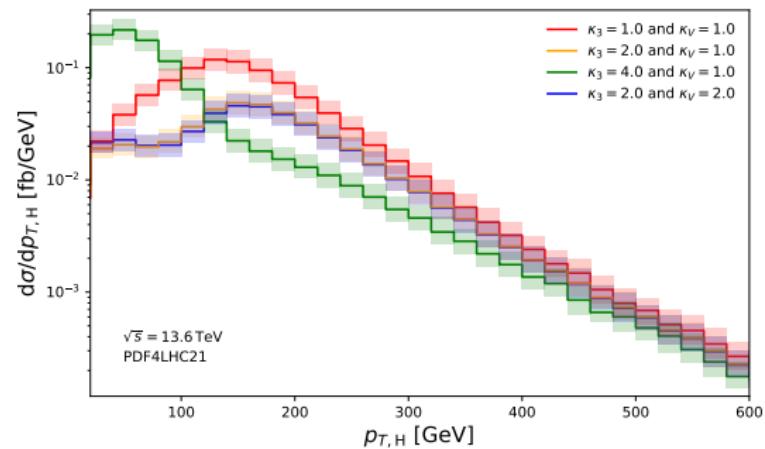
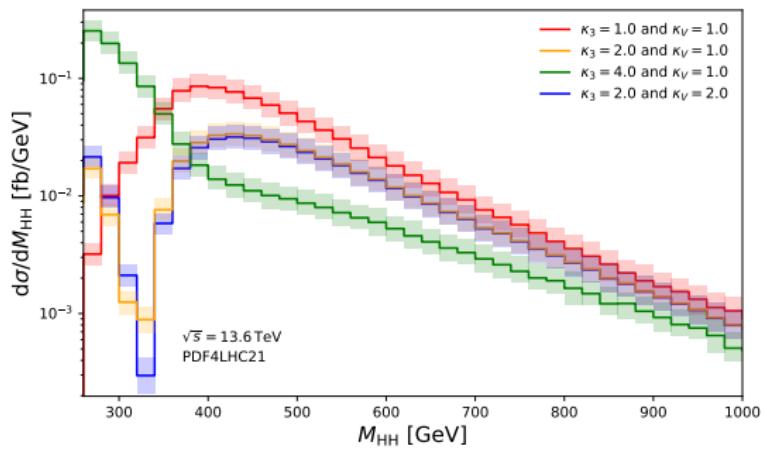
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Conclusion and Outlook  
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# Results



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# Conclusion and Outlook

## Conclusion:

- Constraining  $\lambda_3$  is a main goal at HL LHC

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# Conclusion and Outlook

## Conclusion:

- Constraining  $\lambda_3$  is a main goal at HL LHC
- Theoretical uncertainty makes EW corrections relevant

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# Conclusion and Outlook

## Conclusion:

- Constraining  $\lambda_3$  is a main goal at HL LHC
- Theoretical uncertainty makes EW corrections relevant
- Light quark corrections are **sizeable**, reaching up to 15 % near the production threshold

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# Conclusion and Outlook

## Conclusion:

- Constraining  $\lambda_3$  is a main goal at HL LHC
- Theoretical uncertainty makes EW corrections relevant
- Light quark corrections are **sizeable**, reaching up to 15 % near the production threshold

## Future projects:

- The dependence of the form factors on **coupling variations** will be addressed in a dedicated study
- Combination with further EW and QCD corrections
- The integrals and computational framework will be used for **quark-initiated double Higgs production**.

Motivation



Amplitude



Master Integrals



Results



Conclusion and Outlook



# Thank you!

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