

Measurement of top quark CKM elements at FCC-ee

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$|V_{ts}|$ introduction

Current measurements on $|V_{ts}|$

- ▶ PDG value: $|V_{ts}| = (41.5 \pm 0.9) \times 10^{-3}$
 - From $B_s^0 - \bar{B}_s^0$ mixing, mediated via t - W box diagrams
 - Assume no NP in the loop
 - Dominated by theory uncertainty from lattice QCD
- ▶ Also keep $|V_{cb}|$ in mind
 - Inclusive $(42.2 \pm 0.5) \times 10^{-3}$ vs exclusive $(39.8 \pm 0.6) \times 10^{-3}$ (6% tension)

Potential at e^+e^- colliders

- Model-independent direct measurement
- FCC-ee expects $2 \times 10^6 \times 2 \times |V_{ts}|^2 \sim 6400$ cases of $t \rightarrow Ws$
 - s-tagging is the core
 - Limited by statistical uncertainty

FCC project

New infrastructure

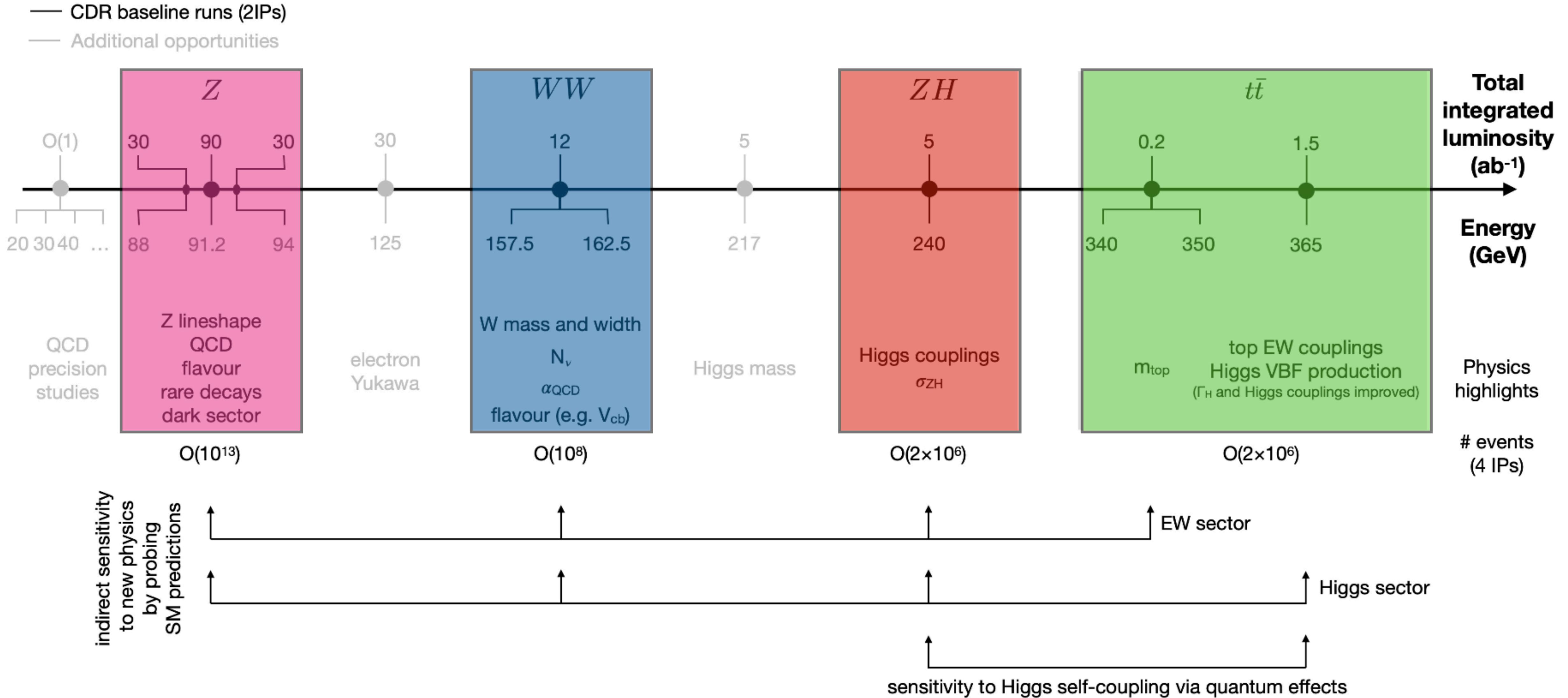
- 90.7 km tunnel
- 8 surface points
- 4 experimental sites
- Deepest shaft 400 m, average 240 m

Two stages

- FCC-ee (~15 years)
- FCC-hh (>20 years)



FCC-ee program



jet clustering

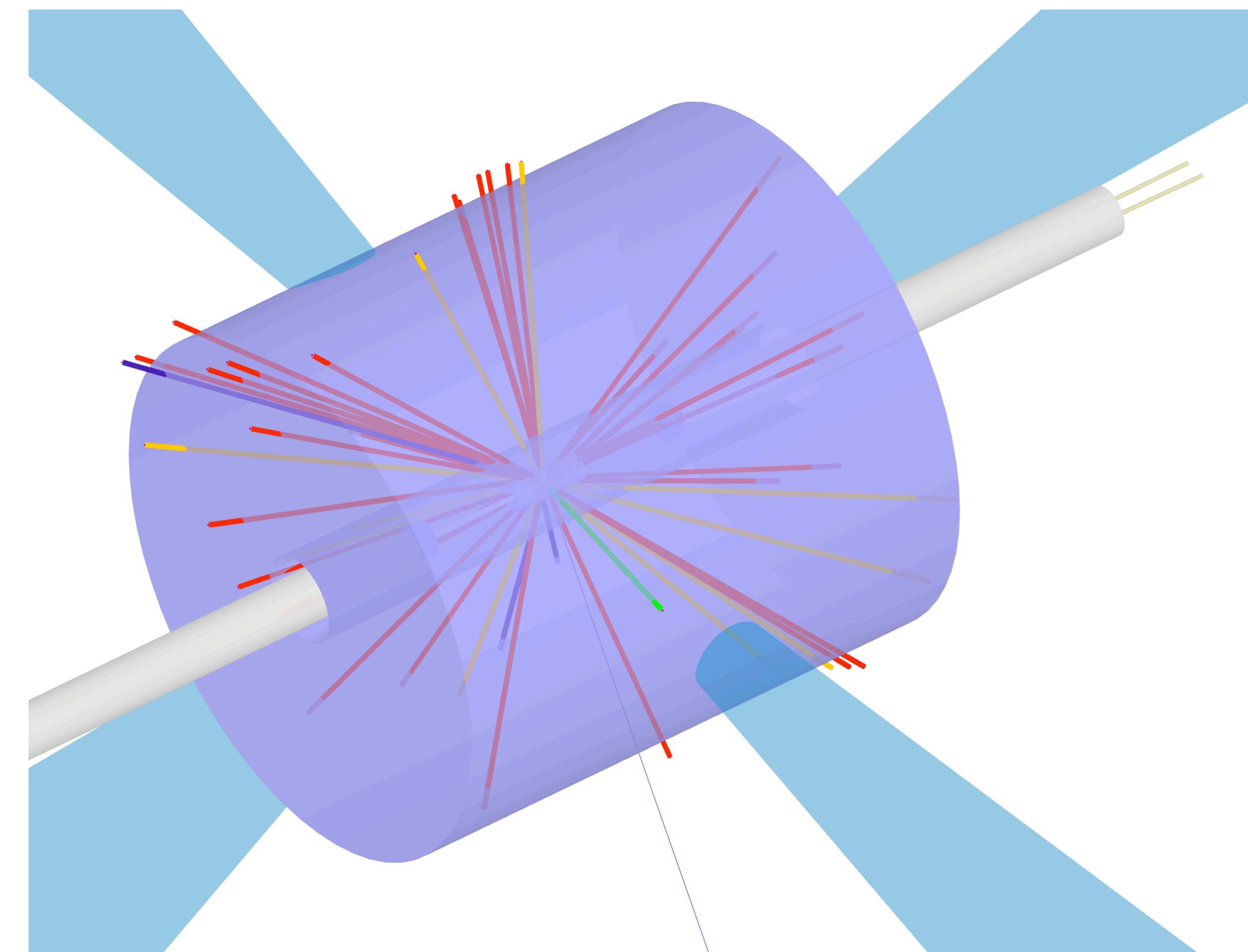
Crucial ingredient of this analysis

- Correctly categorize dileptonic, semi-leptonic, fully hadronic $t\bar{t}$ decays
- Well-defined jets for flavor tagging

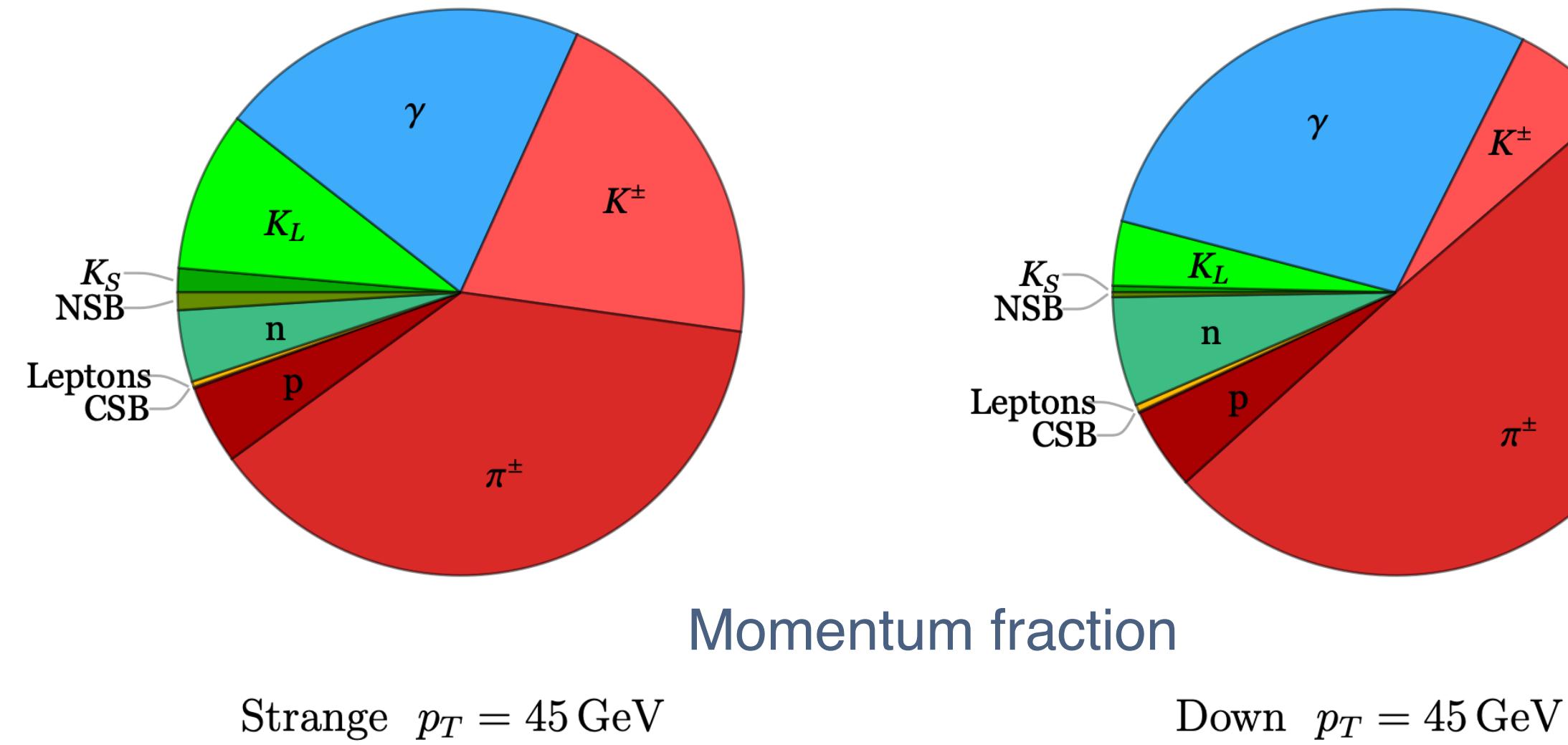
Two types considered

- Exclusive clustering (fixed number of jets in events)
 - subjet distance $d_{ij} = 2\min(E_i^2, E_j^2)(1 - \cos\theta_{ij})$
- Inclusive clustering (roughly fixed cone size)
 - subjet distance $d_{ij} = \min(E_i^{2p}, E_j^{2p}) \frac{1 - \cos\theta_{ij}}{1 - \cos R}$
 - merge i, j until $\forall d_{ij} > E_i^{2p}$

Inclusive jet with $R=0.5$ as nominal choice in this work

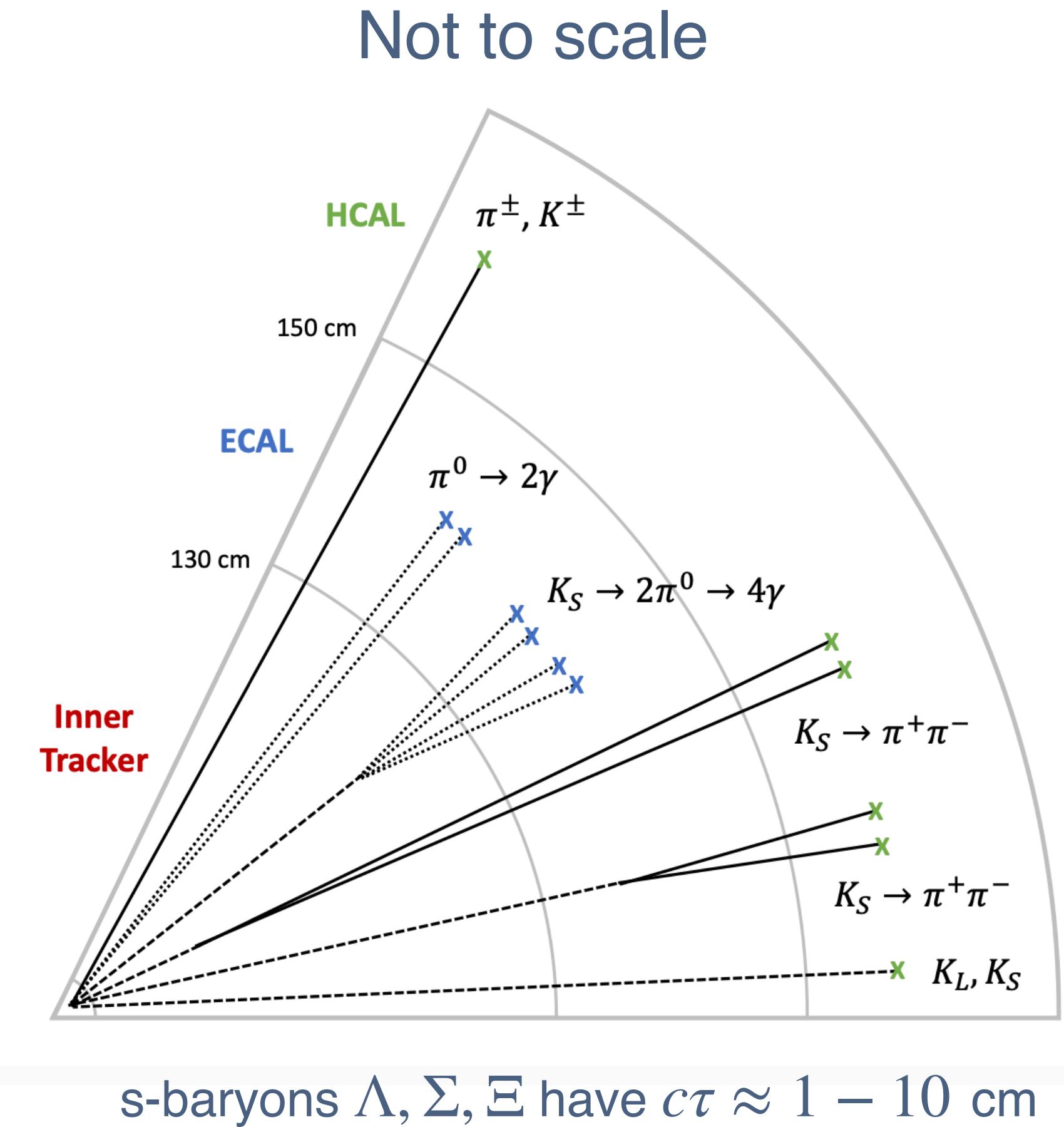


Strange jet tagging

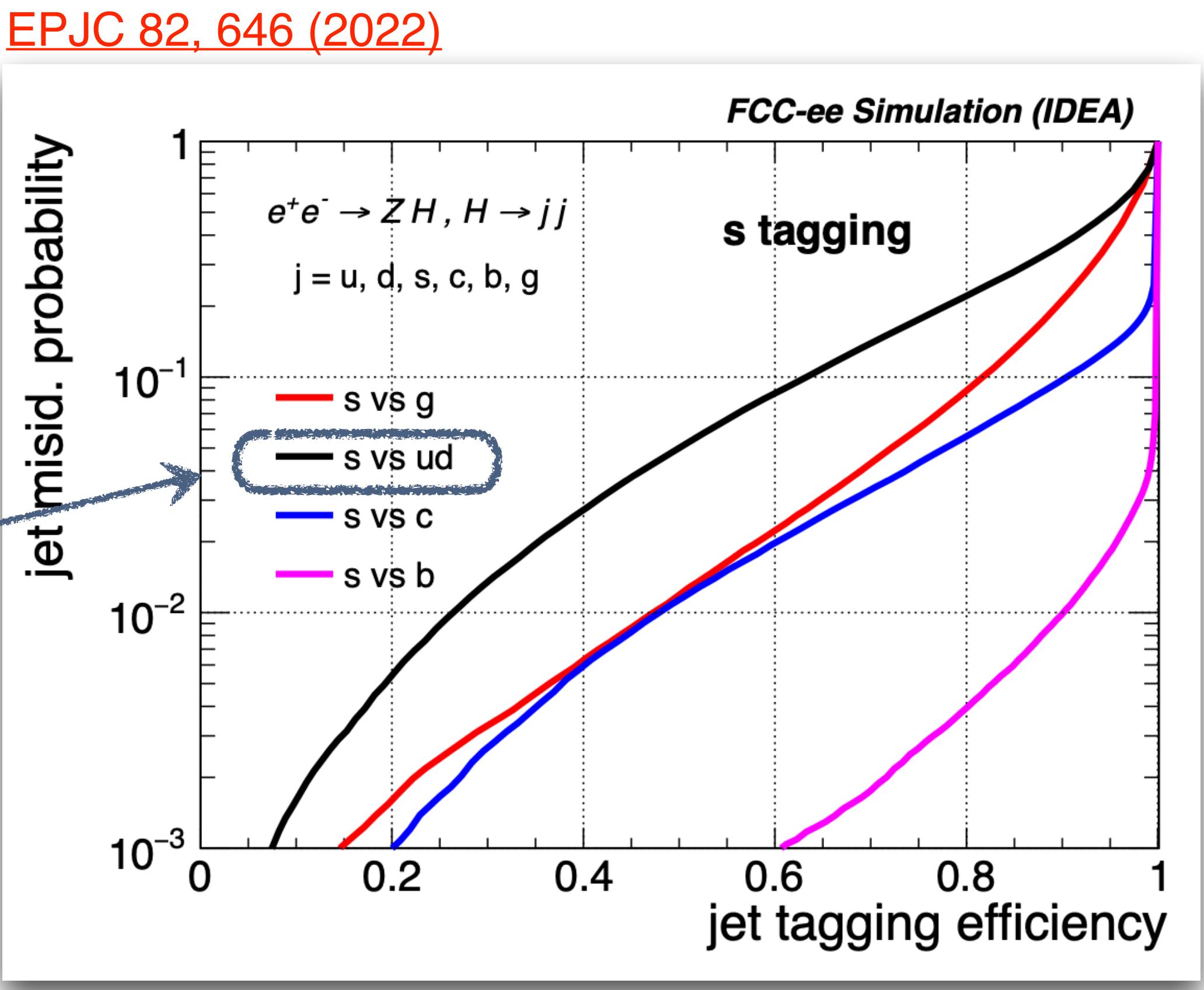
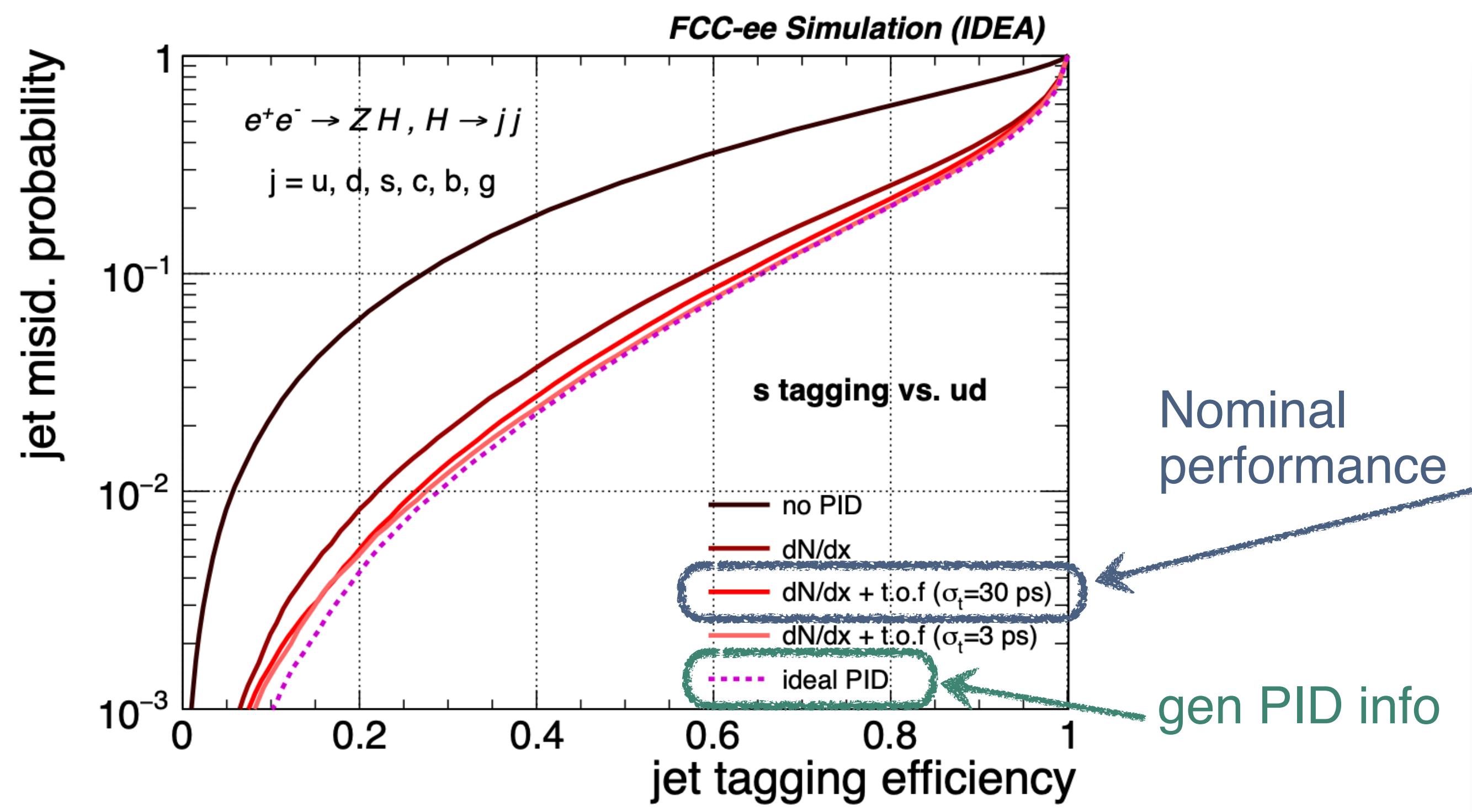


[arxiv:2003.09517](https://arxiv.org/abs/2003.09517)

- Higher fraction of momentum carried by **kaons**
 - K^+/π^+ separation is the key
- Neutral kaons and s-baryons are long-lived
 - $c\tau(b/c) \approx 0.5 \text{ mm}$, $c\tau(s) \approx 50 \text{ mm}$
 - Depends on reco efficiency of highly displaced vertices



Strange tagging at FCC-ee



- Most improvement from dN/dx
- With nominal design ($dN/dx, \sigma(\text{TOF}) = 30 \text{ ps}$), already close to perfect PID
- Limited natural separation between s and ud

	Eff (s)	Mistag (g)	Mistag (ud)	Mistag (c)	Mistag (b)
Loose	90%	20%	40%	10%	1%
Medium	80%	9%	20%	6%	0.4%

Samples and selection

Samples

- Signal: all decay modes of $t\bar{t} \rightarrow WbWs$
- Backgrounds: $t\bar{t} \rightarrow WbWb, Z, WW, ZZ, \text{Higgs}, WWZ$

Event selection

- Require exactly 1 s-tagged jet and 1 b-tagged jet
- Further divide into 6 **categories** based on **number of objects**: e, μ , and tagged jets
 - **1 dileptonic category**
 - **2 semileptonic categories**: $W \rightarrow ud$ and $W \rightarrow cs$
 - **3 fully hadronic categories**: $WW \rightarrow uudu$, $WW \rightarrow udcs$, $WW \rightarrow cscs$

e/μ selection

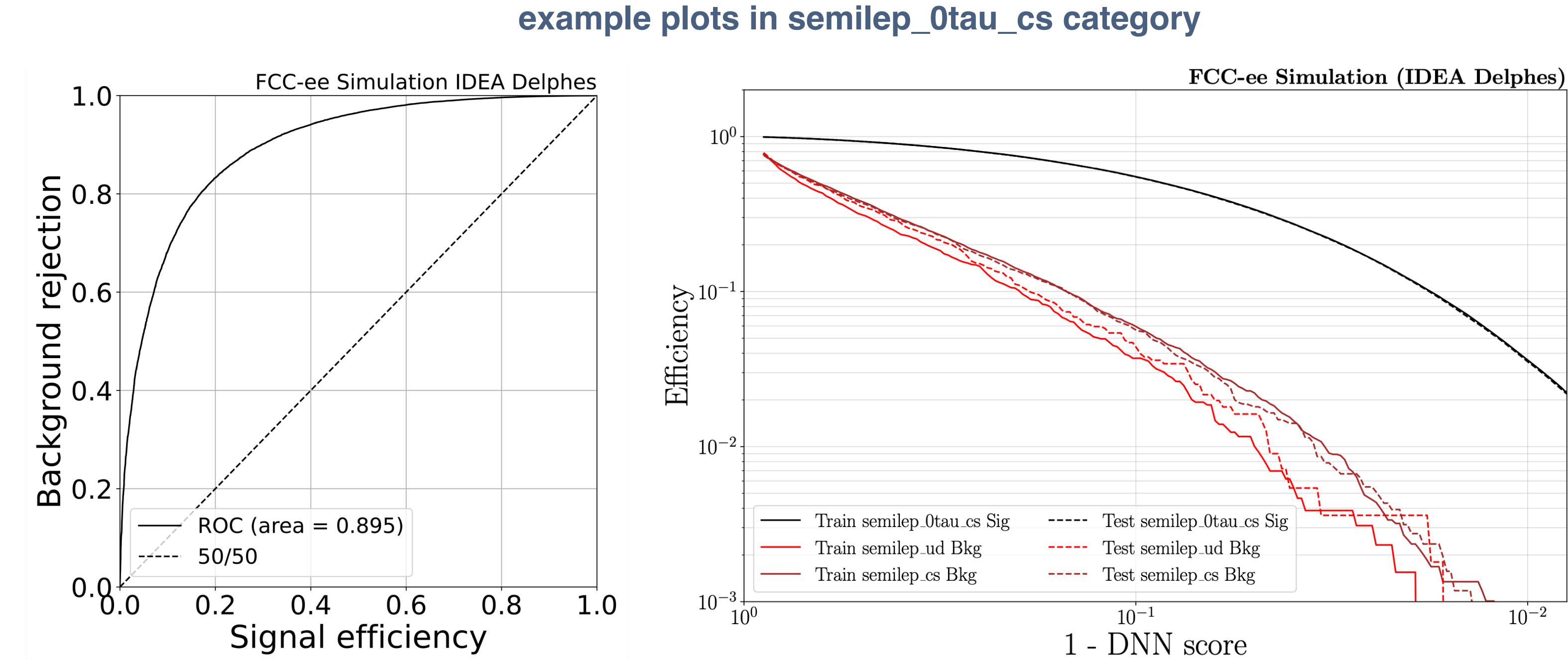
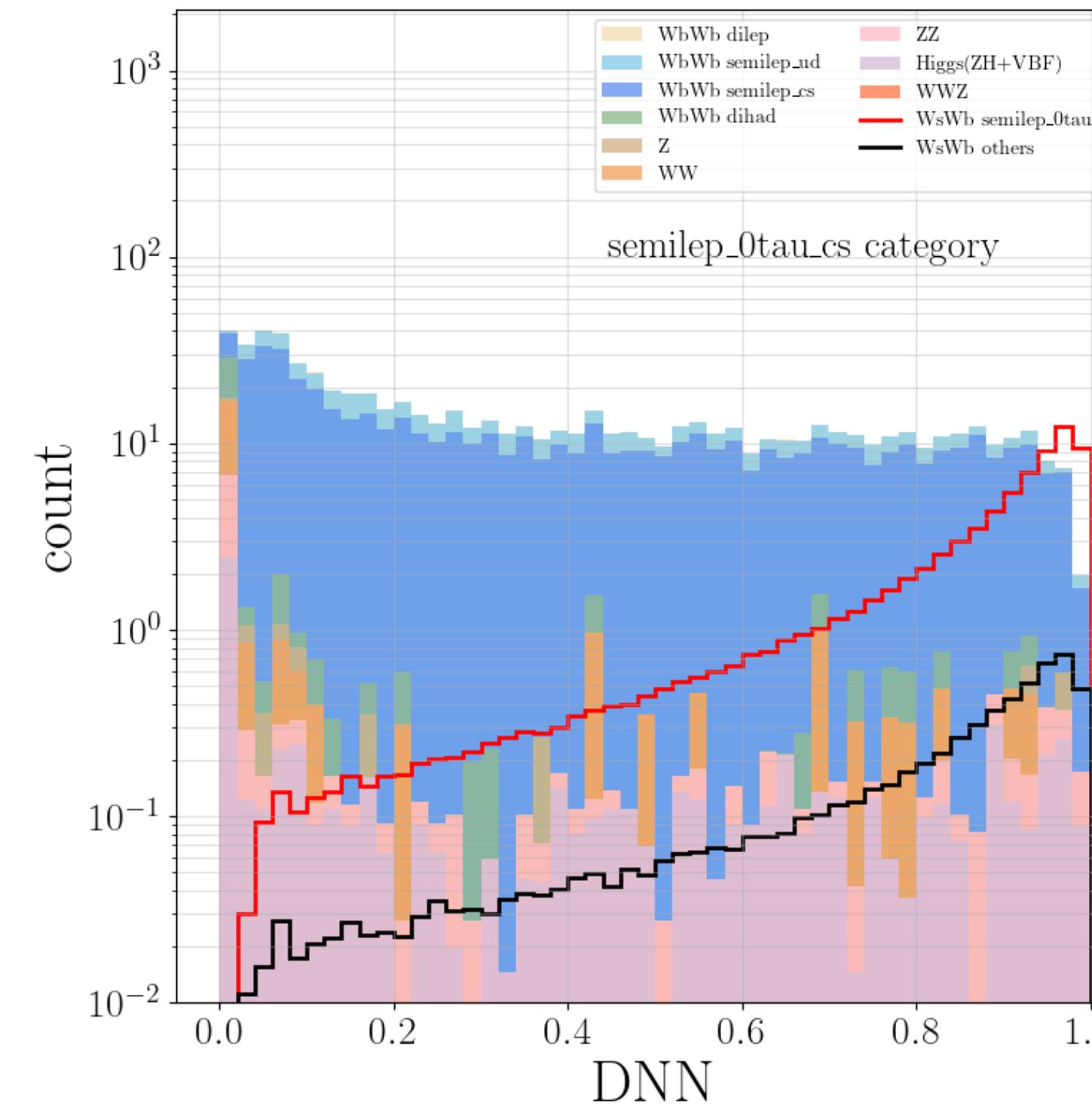
- $p_\ell > 20 \text{ GeV}$
- $\text{Iso}_{R<0.5} < 0.25$

jet selection

- ee_gen_kt R=0.5
- $E_J > 15 \text{ GeV}$
- $m_J < 50 \text{ GeV}$
- $\tau\text{-score} < 0.5$
- flavor tag if score > 0.5

DNN training

- Fully connected 3 hidden layers (#inputs \rightarrow $2 \times \text{#inputs}$ \rightarrow $4 \times \text{#inputs}$ \rightarrow 8 \rightarrow 1)
- For tt processes (sig and bkg), independent events for training, testing, and statistical analysis
- For other bkgs, training and testing events are also used for analysis.
- DNN performance consistent with previous analysis, but more reliable



Results

- Binned likelihood fit on DNN output with Asimov dataset
- Only take categories without taus. —> Not affected by bkg issue
- Consider 1% bkg norm uncertainty to be the nominal case
- **6.3% relative uncertainty on $\mathcal{B}(t \rightarrow Ws)$**

Fit config	Free bkg	bkg $\pm 20\%$	bkg $\pm 5\%$	bkg $\pm 2\%$	bkg $\pm 1\%$
category					
dilep_0tau	14.5%	12.4%	12.0%	11.9%	11.8%
semilep_0tau_ud	13.2%	10.8%	10.2%	9.9%	9.7%
semilep_0tau_cs	30.3%	18.9%	18.3%	17.8%	17.7%
dihad_ud_only	25.4%	20.2%	19.8%	19.1%	18.6%
dihad_udcs	32.4%	26.0%	25.6%	24.7%	24.1%
dihad_cs_only	108%	83.1%	78.4%	76.5%	76.2%
combined	6.8%	6.6%	6.5%	6.4%	6.3%

Conclusions and outlook

Measurement of $\mathcal{B}(t \rightarrow Ws)$ at 365 GeV

- First opportunity for model-independent measurement of $| V_{ts} |$
- Nominal precision $\sigma(t \rightarrow Ws) = 6.3\%$, $\sigma(| V_{ts} |) = 3.1\%$

Outlook

- Simultaneous measurement of $\mathcal{B}(t \rightarrow Ws)$ and $\mathcal{B}(t \rightarrow Wb)$
- Benchmark for jet clustering and flavor tagging performance
- Rich discussion in pheno interpretation

Backups

Sample considered

Sig: SM $t \rightarrow Ws$ decay

- wzp6_ee_SM_tt_tWsTWb_tlepTall_ecm365
- wzp6_ee_SM_tt_tWsTWb_tlightTall_ecm365
- wzp6_ee_SM_tt_tWsTWb_theavyTall_ecm365
- wzp6_ee_SM_tt_tWbTWs_tallTlep_ecm365
- wzp6_ee_SM_tt_tWbTWs_tallTlight_ecm365
- wzp6_ee_SM_tt_tWbTWs_tallTheavy_ecm365

Bkg: SM $t \rightarrow Wb$ samples

- wzp6_ee_SM_tt_tlepTlep_noCKMmix_keepPollInfo_ecm365
- wzp6_ee_SM_tt_thadThad_noCKMmix_keepPollInfo_ecm365
- wzp6_ee_SM_tt_tlepThad_noCKMmix_keepPollInfo_ecm365
- wzp6_ee_SM_tt_thadTlep_noCKMmix_keepPollInfo_ecm365

Bkg: other SM processes

WW

- p8_ee_WW_ecm365

Z

- p8_ee_Zbb_ecm365
- wzp6_ee_tautau_ecm365

ZZ

- p8_ee_ZZ_ecm365

Higgs

- wzp6_ee_bbH_ecm365
- wzp6_ee_ccH_ecm365
- wzp6_ee_ssH_ecm365
- wzp6_ee_qqH_ecm365
- wzp6_ee_tautauH_ecm365
- wzp6_ee_mumuH_ecm365
- wzp6_ee_eeH_ecm365
- wzp6_ee_nunuH_ecm365

WWZ

- wzp6_ee_WWZ_Zbb_ecm365

Signal efficiency

x axis: truth of decay

y axis: reco selection category

- Each cell shows fraction per column (truth), reflecting acceptance and reconstruction efficiency
- Last column is the fraction of diagonal yield wrt its row. I.e. the accuracy of reco categories.

		Confusion matrix																								
		Actual																								
		dilep_0tau	dilep_1tau	dilep_2tau	semilep_0tau_ud	semilep_0tau_cs	semilep_1tau_ud	semilep_1tau_cs	dihad_ud_only	dihad_udcs	dihad_cs_only	sum_col	dilep_0tau	dilep_1tau	dilep_2tau	semilep_0tau_ud	semilep_0tau_cs	semilep_0tau_CKMMix	semilep_1tau_ud	semilep_1tau_cs	semilep_1tau_CKMMix	dihad_ud_only	dihad_udcs	dihad_cs_only	dihad_CKMMix	cat_accuracy
		42.4%	61.3%	74.4%	50.3%	53.9%	57.2%	68.8%	71.1%	73.3%	54.0%	54.3%	57.4%	57.7%	0.0%											
		54.0%	7.0%	0.9%	0.0%	0.0%																			91.2%	
		3.1%	29.7%	7.6%	0.1%	0.1%	0.1%	0.0%	0.0%	0.0%															82.8%	
		0.0%	0.8%	15.9%	0.0%	0.0%																				69.9%
		0.4%	0.6%	0.1%	40.7%	9.5%	7.6%	5.3%	1.2%	0.8%	0.0%	0.0%	0.0%	0.0%											79.2%	
		0.1%	0.4%	0.1%	6.8%	34.7%	33.6%	0.9%	4.5%	4.5%	0.0%	0.0%	0.0%	0.0%											74.5%	
		0.0%	0.1%	0.5%	1.1%	0.3%	0.1%	19.0%	4.3%	3.6%	0.4%	0.1%	0.1%	0.1%											73.0%	
		0.0%	0.0%	0.4%	0.2%	0.9%	0.8%	3.3%	16.2%	15.9%	0.1%	0.3%	0.1%	0.2%											67.8%	
		0.0%	0.0%	0.0%	0.5%	0.1%	0.1%	1.2%	0.4%	0.1%	36.2%	8.7%	2.7%	4.7%											67.8%	
		0.0%	0.0%	0.0%	0.1%	0.4%	0.4%	1.2%	1.3%	0.5%	8.4%	31.1%	14.3%	22.2%											72.6%	
		0.0%	0.0%	0.0%	0.0%	0.1%	0.1%	0.2%	0.9%	1.1%	0.8%	5.5%	25.5%	15.2%											57.2%	
		1846914	1342736	209662	5164930	3979155	5909	2584198	1988043	2959	3602226	5691537	1944802	14954												
		54.0%	29.7%	15.9%	40.7%	34.7%	0.0%	19.0%	16.2%	0.0%	36.2%	31.1%	25.5%	0.0%												
		46.0%	70.3%	84.1%	59.3%	65.3%	100.0%	81.0%	83.8%	100.0%	63.8%	68.9%	74.5%	100.0%												

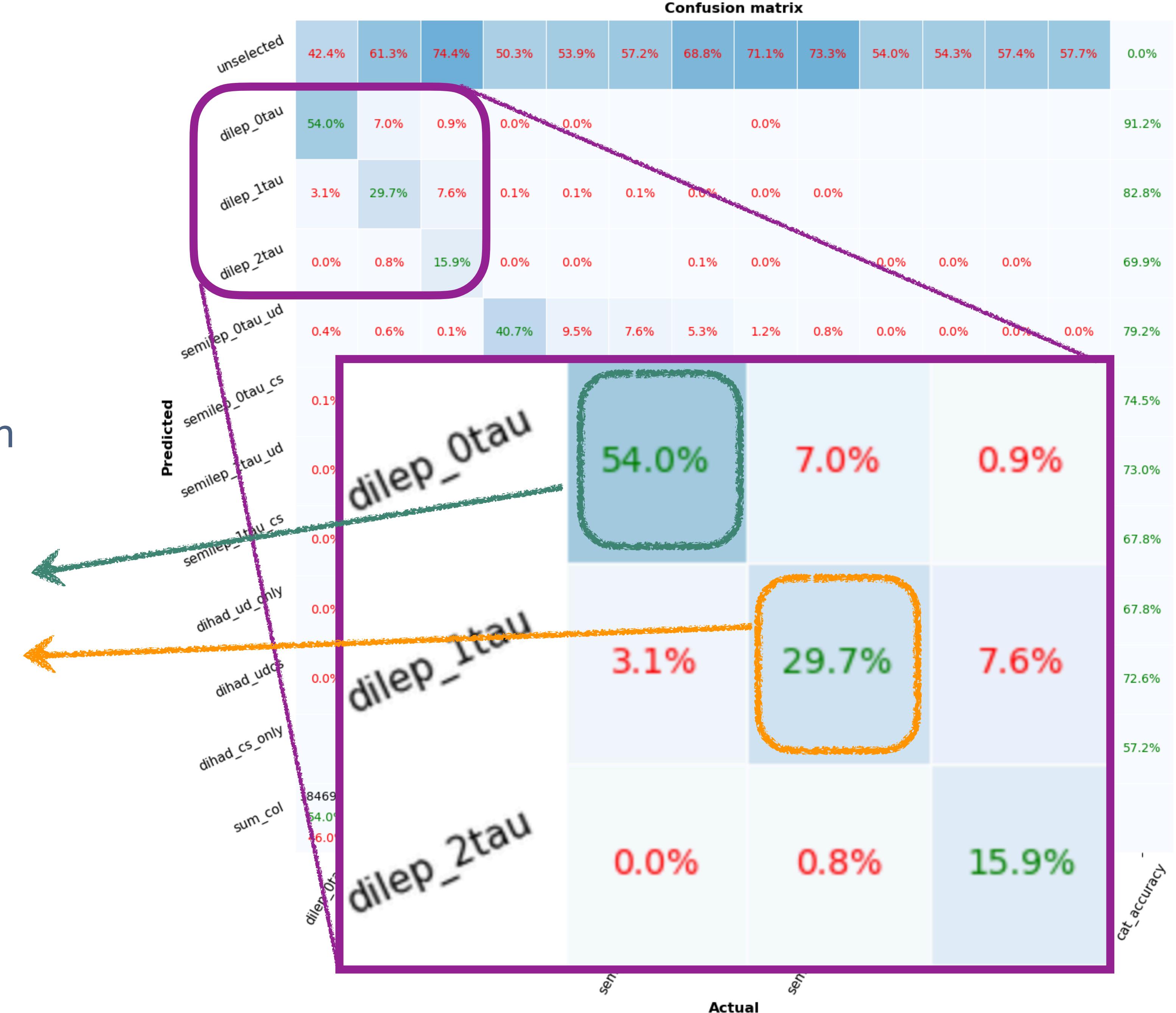
Full yield table and discussion in backup

Signal efficiency

x axis: truth of decay

y axis: reco selection category

- Each cell shows fraction per column (truth), reflecting acceptance and reconstruction efficiency
 - $\epsilon(2 \text{ leptons}) = 75\%$, $\epsilon(2 \text{ jets}) = 71\%$
 - $\epsilon(\tau_h) \sim 50\%$



Full yield table and discussion in backup

Signal efficiency

x axis: truth of decay

y axis: reco selection category

- Last column is the fraction of diagonal yield wrt its row. I.e. the accuracy of reco categories.
 - Selected events match the target decay modes well

		Confusion matrix																								
		Actual															Predicted									
		dilep_0tau	dilep_1tau	dilep_2tau	semilep_0tau_ud	semilep_0tau_cs	semilep_1tau_ud	semilep_1tau_cs	dihad_ud_only	dihad_udcs	dihad_cs_only	sum_col	dilep_0tau	dilep_1tau	dilep_2tau	semilep_0tau_ud	semilep_0tau_cs	semilep_0tau_CKMMix	semilep_1tau_ud	semilep_1tau_cs	semilep_1tau_CKMMix	dihad_ud_only	dihad_udcs	dihad_cs_only	dihad_CKMMix	cat_accuracy
		42.4%	61.3%	74.4%	50.3%	53.9%	57.2%	68.8%	71.1%	73.3%	54.0%	54.3%	57.4%	57.7%	0.0%											
		54.0%	7.0%	0.9%	0.0%	0.0%											0.0%									91.2%
		3.1%	29.7%	7.6%	0.1%	0.1%	0.1%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%										82.8%
		0.0%	0.8%	15.9%	0.0%	0.0%											0.1%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	69.9%	
		0.4%	0.6%	0.1%	40.7%	9.5%	7.6%	5.3%	1.2%	0.8%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%									79.2%	
		0.1%	0.4%	0.1%	6.8%	34.7%	33.6%	0.9%	4.5%	4.5%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%									74.5%	
		0.0%	0.1%	0.5%	1.1%	0.3%	0.1%	19.0%	4.3%	3.6%	0.4%	0.1%	0.1%	0.1%	0.1%	0.1%									73.0%	
		0.0%	0.0%	0.4%	0.2%	0.9%	0.8%	3.3%	16.2%	15.9%	0.1%	0.3%	0.1%	0.2%	0.2%	0.2%									67.8%	
		0.0%	0.0%	0.0%	0.5%	0.1%	0.1%	1.2%	0.4%	0.1%	36.2%	8.7%	2.7%	4.7%	4.7%	4.7%									67.8%	
		0.0%	0.0%	0.0%	0.1%	0.4%	0.4%	1.2%	1.3%	0.5%	8.4%	31.1%	14.3%	22.2%	22.2%	22.2%									72.6%	
		0.0%	0.0%	0.0%	0.0%	0.1%	0.1%	0.2%	0.9%	1.1%	0.8%	5.5%	25.5%	15.2%	15.2%	15.2%									57.2%	
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