

Project B1b: Top-Quark Physics

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*Kick-off Meeting of the Collaborative Research Centre/Transregio 257
P³H - Particle Physics Phenomenology after the Higgs Discovery*

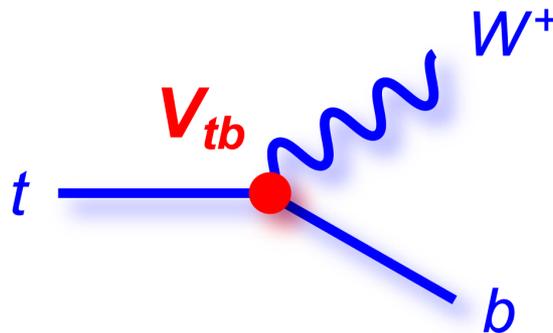
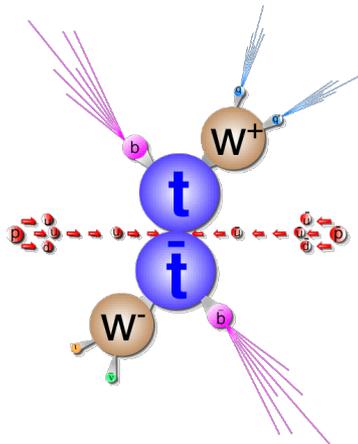
Plan

- ❖ Introduction
- ❖ Setting the stage...
- ❖ State-of-the-art NLO & NNLO results for top quark physics @ LHC

$$pp \rightarrow t\bar{t}$$

$$pp \rightarrow t\bar{t} + X, X = j, \gamma, Z, W^\pm, H, b\bar{b}, jj, t\bar{t}$$

- ❖ Future projects within the CRC/TRR

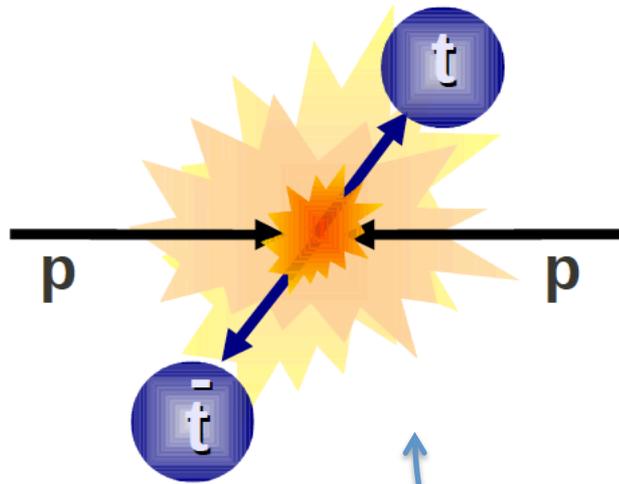


LHC Top-Quark Factory

	Collider	$\sigma(tt)$ [pb]	L [fb ⁻¹]	N _{event}
LHC Run 1	LHC _{7 TeV}	180	5	9 x 10 ⁵
	LHC _{8 TeV}	256	20	5 x 10 ⁶
LHC Run 2	LHC _{13 TeV}	835	36	3 x 10 ⁷
	LHC _{14 TeV}	987	100	1 x 10 ⁸
High Luminosity	HL-LHC _{14 TeV}	987	3000	3 x 10 ⁹
High Energy	HE-LHC _{27 TeV}	3840	15000	6 x 10 ¹⁰

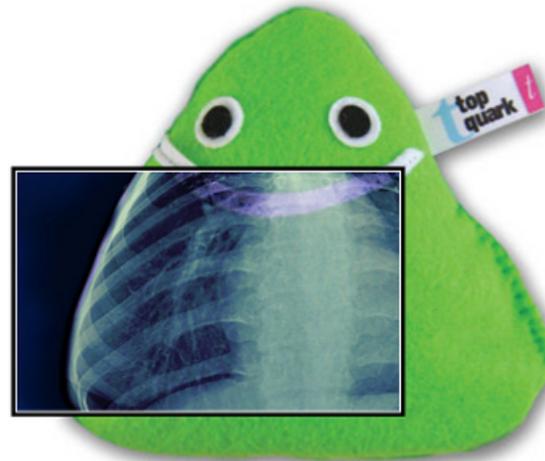
*Top quark pair production @ NNLO with **TOP++**
CT14 PDF, $m_t = 173.2$ GeV*

Czakon, Mitov '14



Intrinsic properties:

- Mass
- Charge
- Lifetime
- Width

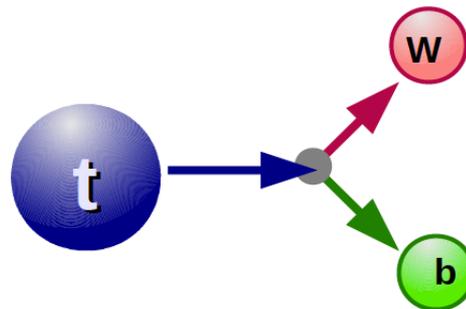


Production:

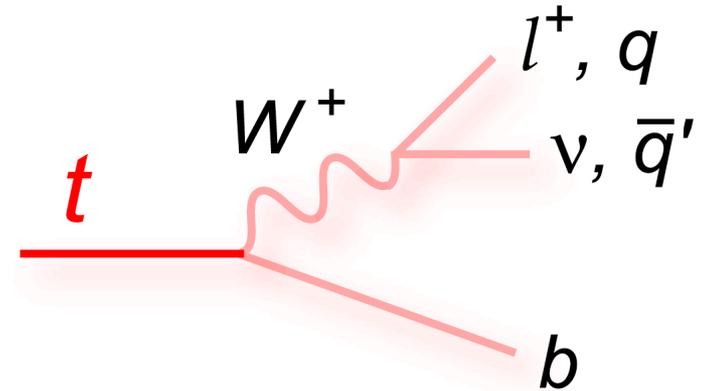
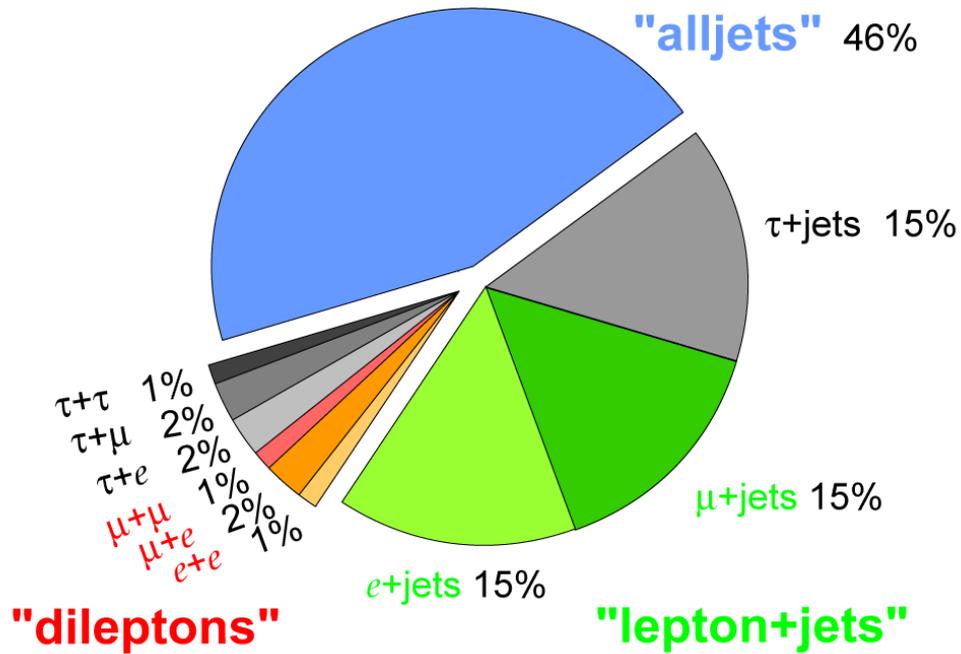
- Production rate
- Differential distributions
- New production mechanisms

Decays:

- Decay channels (SM & new)
- Couplings W, Z, γ & H
- Spin correlations



Top Pair Branching Fractions



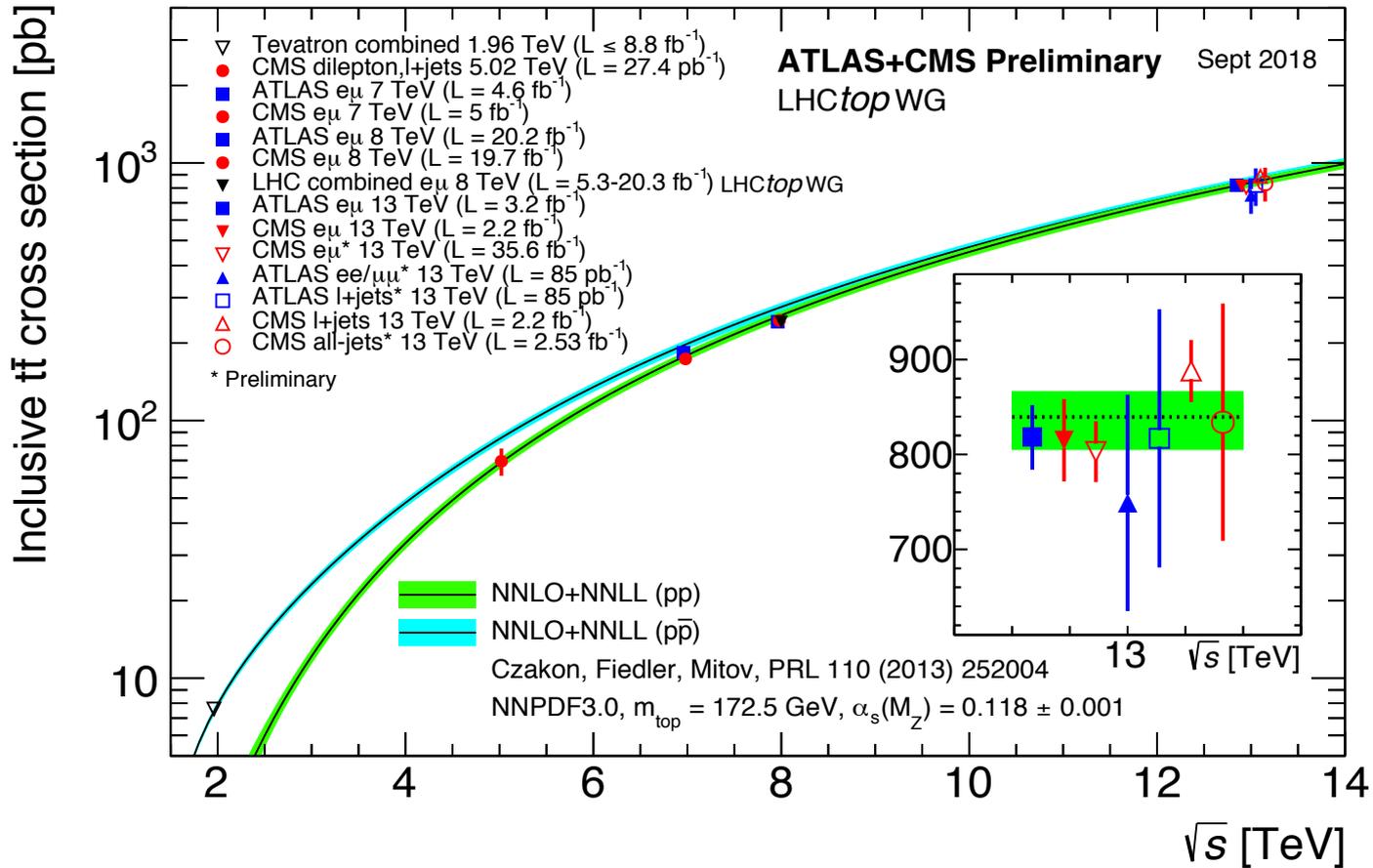
- ❖ Top quark produced via QCD interaction decay through weak interaction
- ❖ Producing W-boson and a down-type quark (down, strange, or bottom)

$$BR(t \rightarrow Wb) = \frac{\Gamma(t \rightarrow Wb)}{\Gamma(t \rightarrow Wq)} = \frac{|V_{tb}|^2}{|V_{td}|^2 + |V_{ts}|^2 + |V_{tb}|^2} \approx 0.99$$

SM : $t \rightarrow Wb \approx 100\%$

Top-Quark Pair Production

On-shell Tops

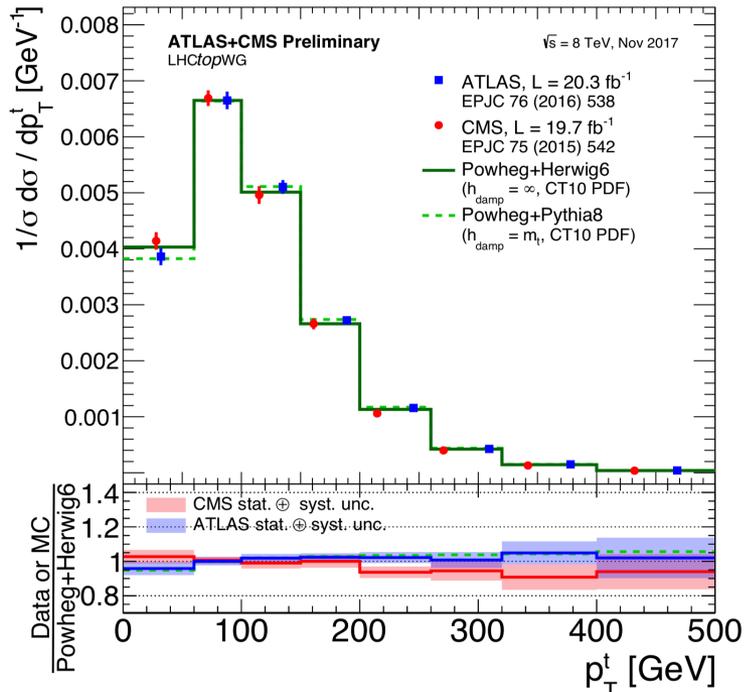


Summary of LHC and Tevatron measurements of $t\bar{t}$ cross-section compared to NNLO QCD calculation complemented with NNLL resummation - **TOP++**

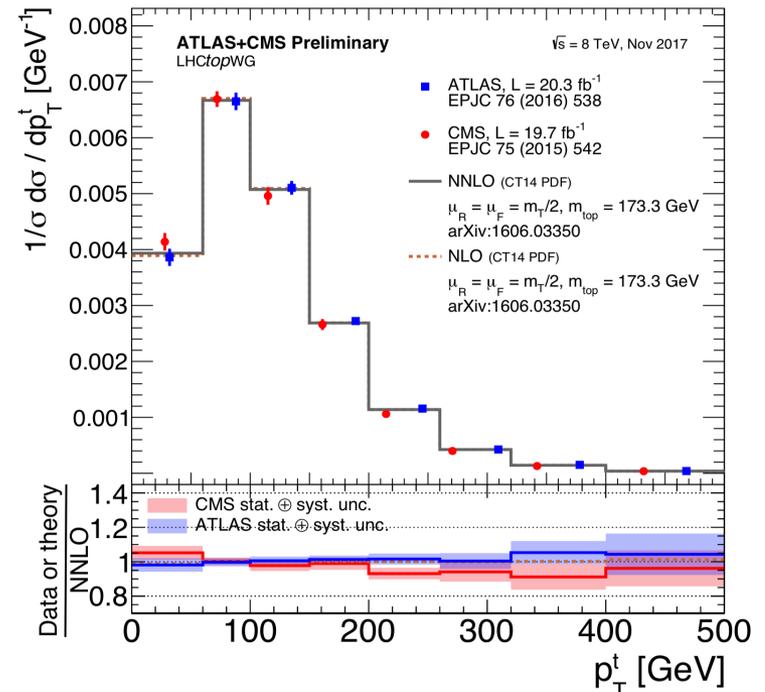
Top-Quark Pair Production

On-shell Tops

Full phase-space normalized differential $t\bar{t}$ cross-section as a function of $p_T(t)$



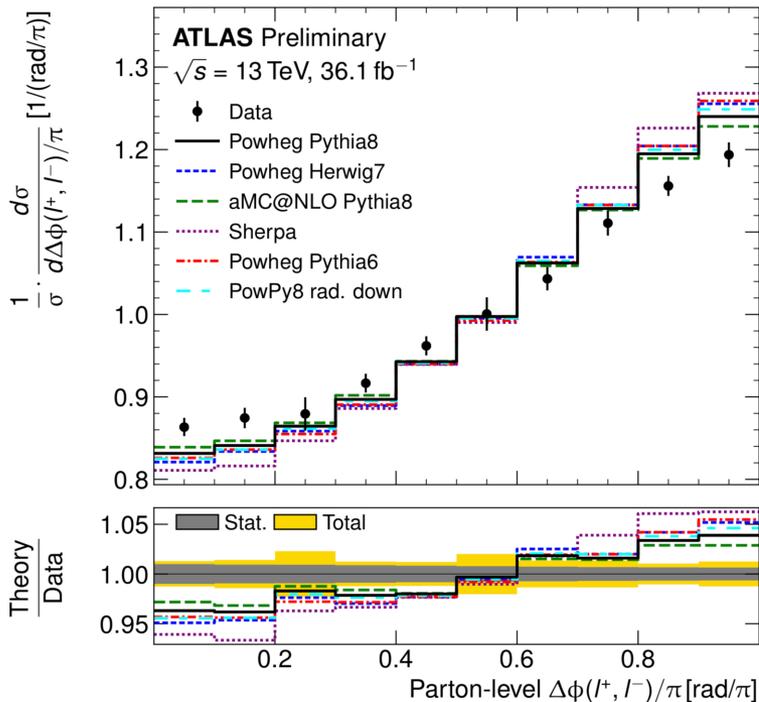
The **CMS** and **ATLAS** results are compared to Powheg+Herwig6 & Powheg+Pythia8 MC generators.



The **CMS** and **ATLAS** results are compared to the NLO & NNLO calculations.

Top-Quark Production & Decays

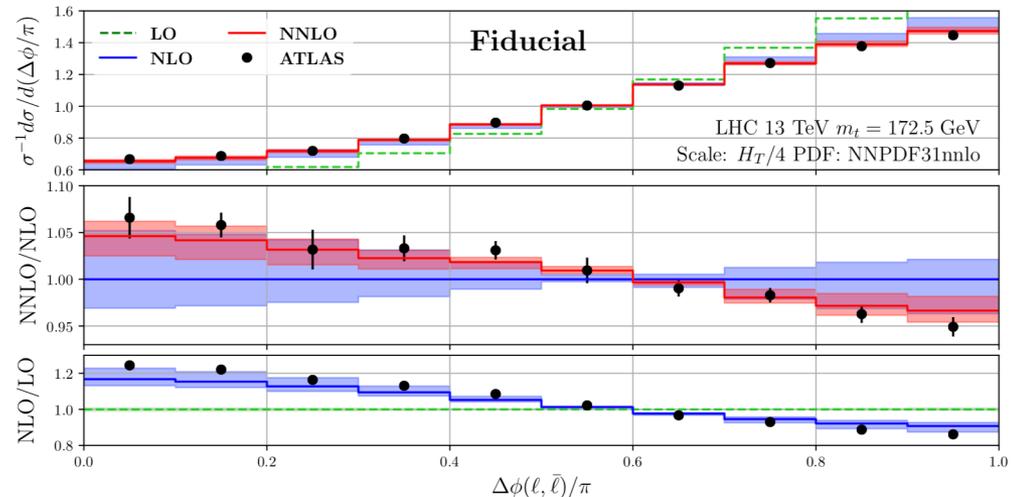
Normalized differential $t\bar{t}$ cross-section as a function of azimuthal opening angle between two leptons



ATLAS-CONF-2018-027

Comparison to Powheg, Mad-Graph5_aMC@NLO & Sherpa

Tops in NWA



Behring, Czakon, Mitov, Papanastasiou, Poncelet '19

Comparison to NNLO QCD predictions in NWA

tt & $tt+X$ @ LHC

❖ *Proper modeling of top decays essential already in presence of inclusive cuts:*

- ❖ Higher order QCD corrections \rightarrow Corrections to production & decays
- ❖ Full NWA or complete off-shell effects for top quarks
- ❖ tt spin correlations
- ❖ Possibility of using kinematic-dependent μ_R & μ_F scales

❖ *Even more important for:*

- ❖ High luminosity & Exclusive cuts
- ❖ New Physics searches & SM parameter extraction

❖ *tt & $tt+X$ status:*

- ❖ NNLO QCD predictions for $pp \rightarrow tt$ in NWA (di-lepton)
- ❖ NLO QCD with off-shell effects: $pp \rightarrow tt$, $pp \rightarrow tty$, $pp \rightarrow ttj$, $pp \rightarrow ttH$
- ❖ NLO QCD in NWA: $pp \rightarrow ttZ$ & $pp \rightarrow ttW^\pm$ Röntsch, Schulze '14
Campbell, Ellis '12
- ❖ NLO QCD with on-shell tops: $pp \rightarrow ttbb$, $pp \rightarrow ttjj$, $pp \rightarrow tttt$

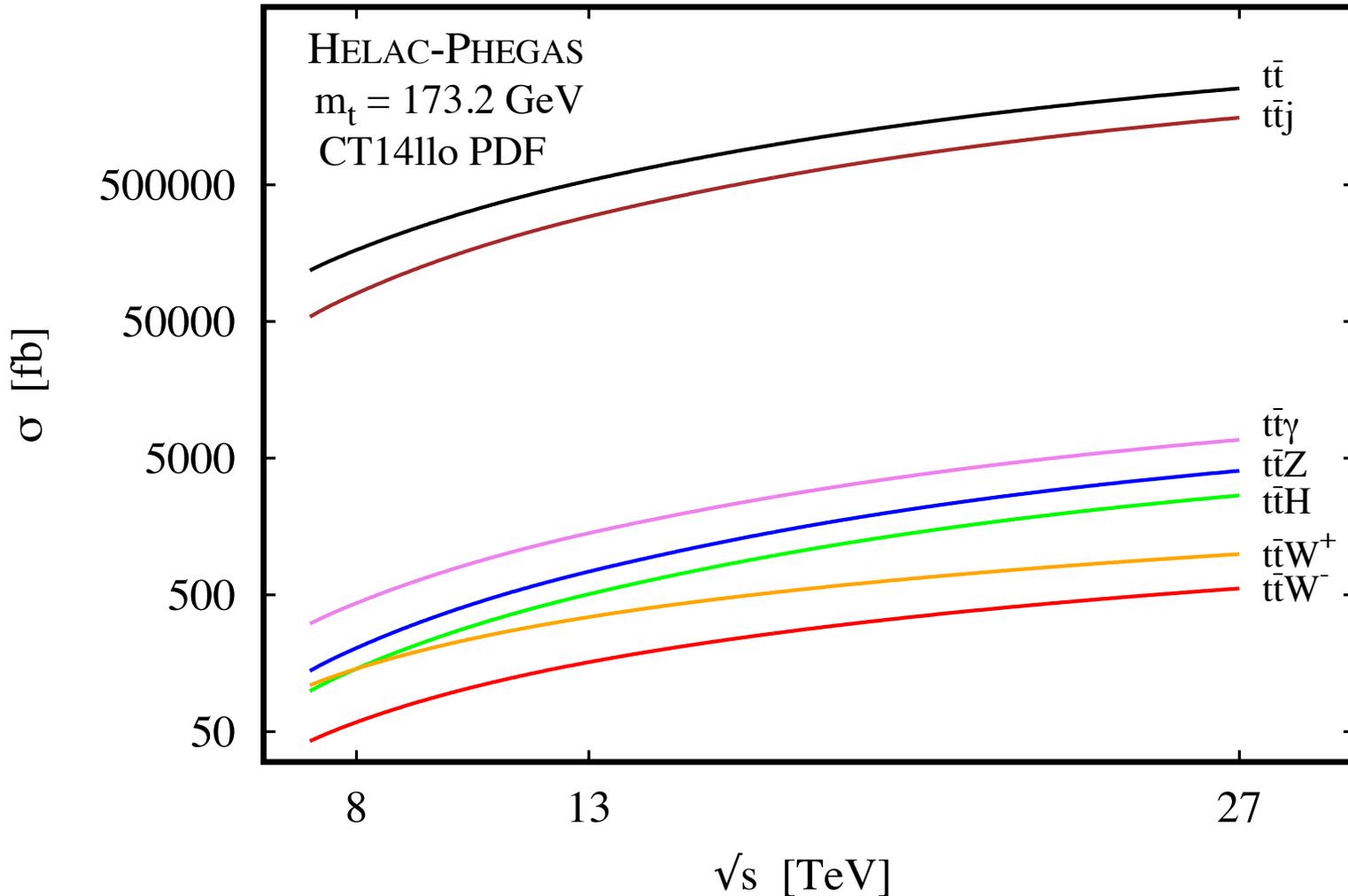
***We plan to improve predictions
for all these processes !***

Bredenstein, Denner, Dittmaier, Pozzorini '09
Bevilacqua, Czakon, Papadopoulos, Pittau, Worek '09
Bevilacqua, Czakon, Papadopoulos, Worek '10 '11
Bevilacqua, Worek '12

$t\bar{t}$ & $t\bar{t}+X$ @ LHC

On-shell Tops

$t\bar{t}$, $t\bar{t}j$, $t\bar{t}\gamma$, $t\bar{t}Z$, $t\bar{t}H$, $t\bar{t}W^+$, $t\bar{t}W^-$ @ LHC



How Good Is NWA ?

- ❖ In NWA tops are restricted to on-shell states
- ❖ Approximation is controlled by the ratio $\Gamma_t/m_t \approx 0.8\%$
- ❖ Should be accurate for sufficiently inclusive observables
- ❖ *Off-shell effects for integrated σ_{tt} at few % level @ NLO in QCD*

Off-shell Tops

<i>tt (di-lepton)</i>	<i>Denner, Dittmaier, Kallweit, Pozzorini '11 '12 Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek '11 Denner, Pellen '16 (EW) Jezo, Lindert, Nason, Oleari, Pozzorini '16 (PS)</i>
<i>tt (semi-leptonic)</i>	<i>Denner, Pellen '18</i>
<i>ttH (di-lepton)</i>	<i>Denner, Feger '15 Denner, Lang, Pellen, Uccirati '17 (EW+QCD)</i>
<i>ttj (di-lepton)</i>	<i>Bevilacqua, Hartanto, Kraus, Worek '16 '18</i>
<i>tty (di-lepton)</i>	<i>Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19</i>

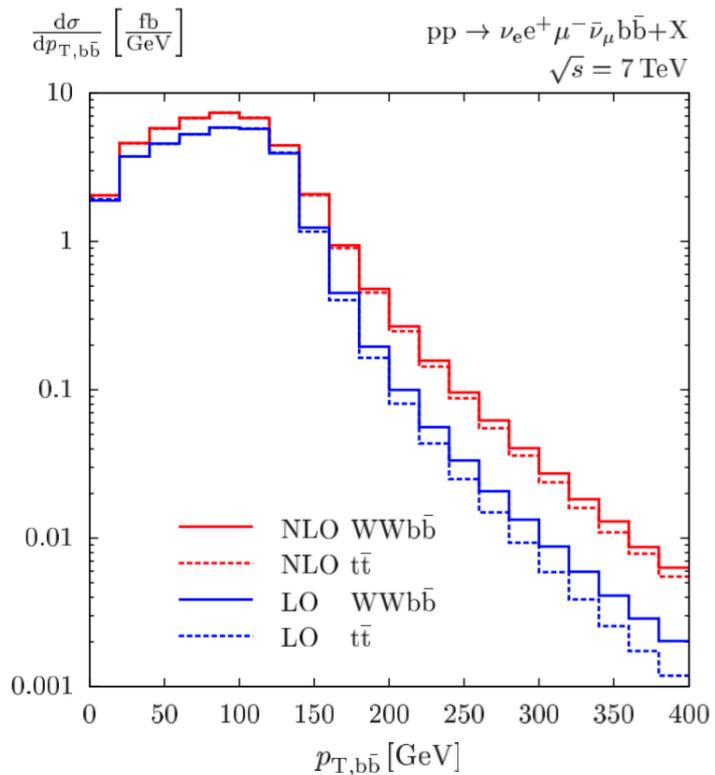
NWA & Off-Shell Effects

❖ Off-shell results vs. results with (spin-correlated) NWA

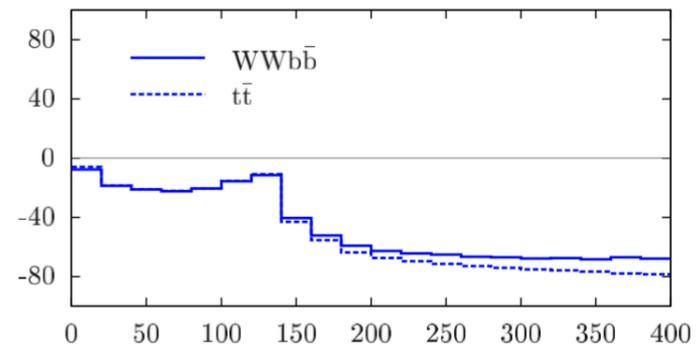
Off-shell Tops

❖ *Tens of per cent* in phase-space regions where $t\bar{t}$ suppressed as signal

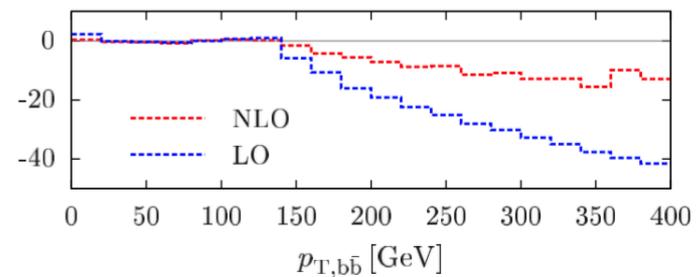
❖ Important as background to *Higgs & BSM searches*



LO/NLO - 1 [%]



$t\bar{t}/WWb\bar{b} - 1$ [%]

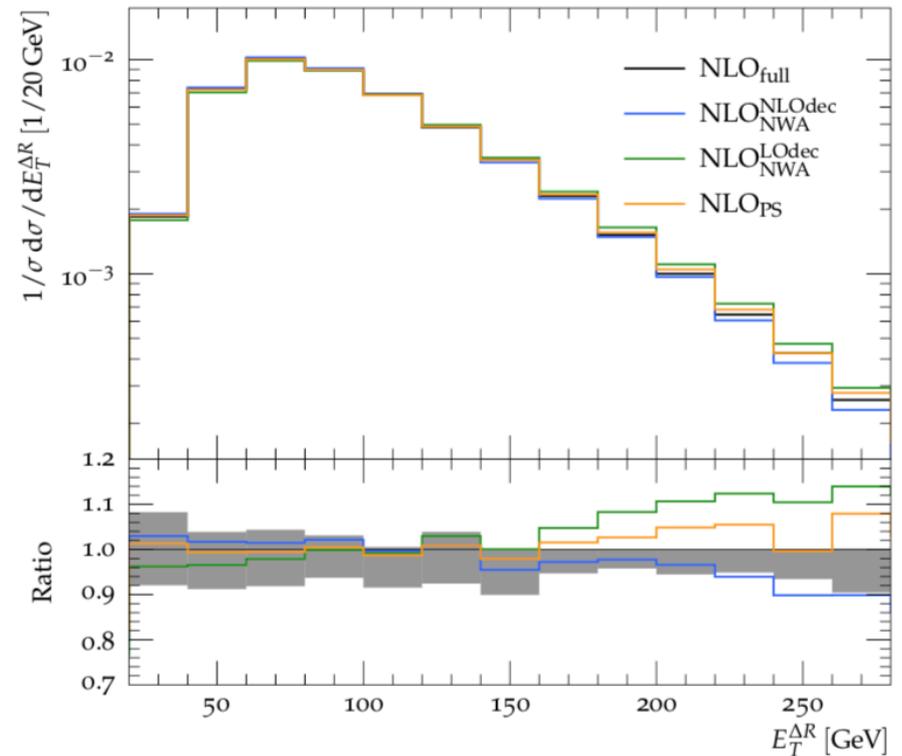
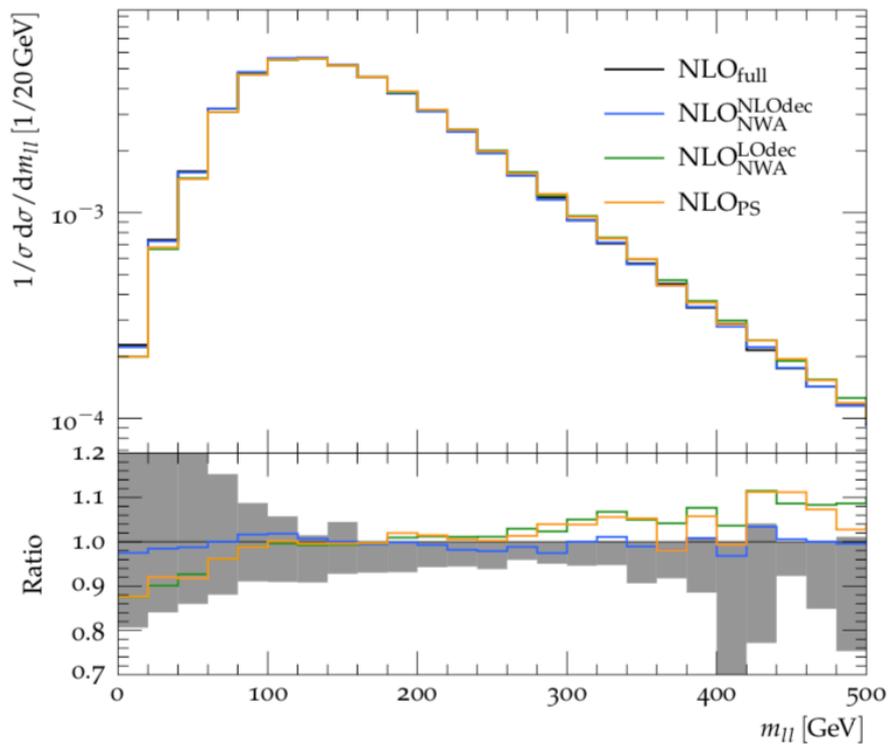


NWA & Off-Shell Effects

- ❖ Observables used for a recent top quark mass determination

Off-shell, NWA, PS

$pp \rightarrow t\bar{t} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} @ 13 \text{ TeV LHC}$

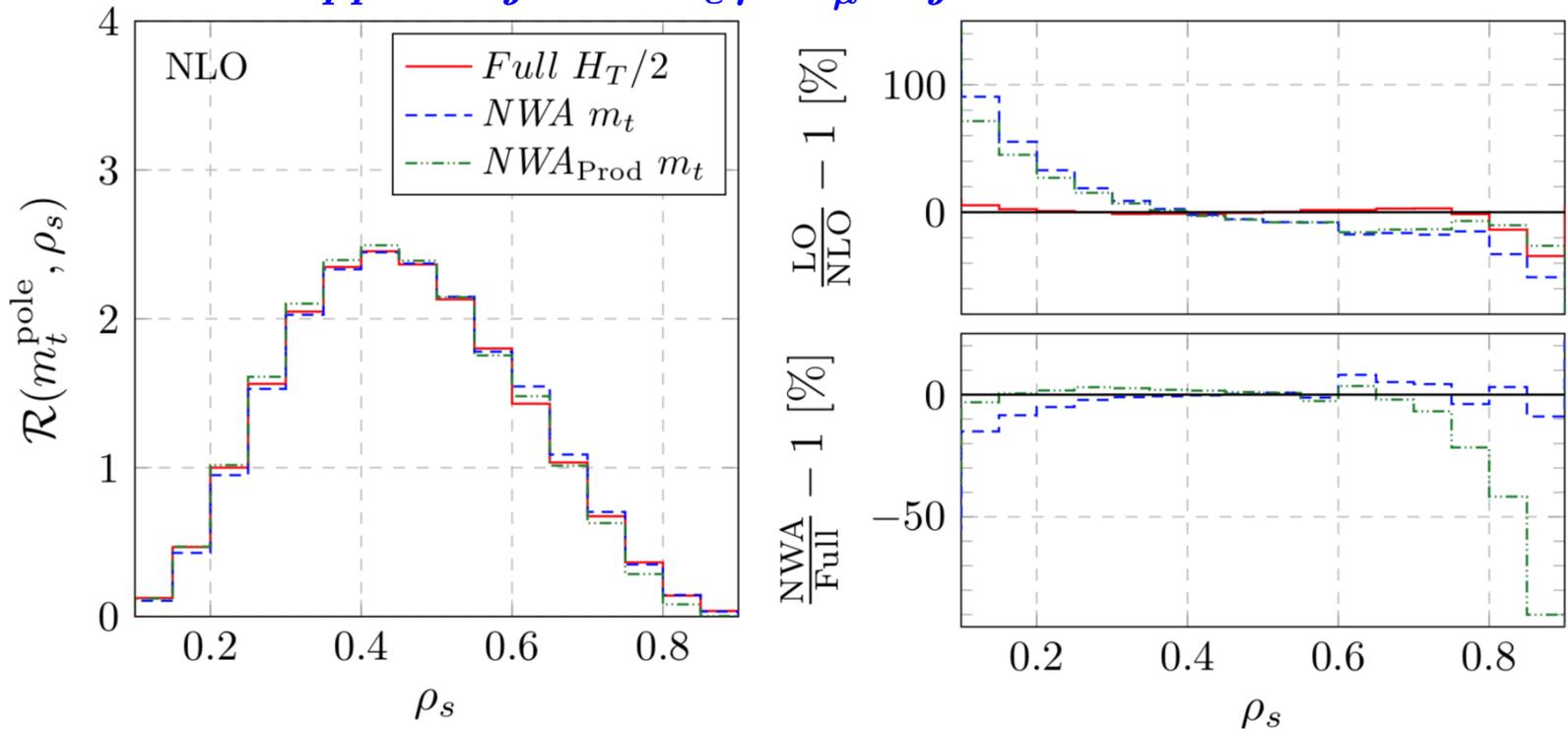


NWA & Off-Shell Effects

❖ Observable used for a recent top quark mass determination

Off-shell, NWA

$pp \rightarrow t\bar{t}j \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j$ @ 13 TeV LHC



$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}j}} \frac{d\sigma_{t\bar{t}j}}{d\rho_s}(m_t^{\text{pole}}, \rho_s)$$

$$\rho_s = \frac{2m_0}{M_{t\bar{t}j}}$$

Alioli, Fernandez, Fuster, Irles, Moch, Uwer, Vos '13

NWA & Off-Shell Effects

2.5 fb⁻¹

$pp \rightarrow t\bar{t}j \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j$ @ 13 TeV LHC

Theory, NLO QCD CT14 PDF	$m_t^{\text{out}} \pm \delta m_t^{\text{out}}$ [GeV]	Averaged $\chi^2/\text{d.o.f.}$	Probability $p\text{-value}$	$m_t^{\text{in}} - m_t^{\text{out}}$ [GeV]
<i>31 bins</i>				
<i>Full, $\mu_0 = H_T/2$</i>	173.38 ± 1.34	1.04	0.40 (0.8 σ)	-0.18
<i>Full, $\mu_0 = E_T/2$</i>	172.84 ± 1.33	1.05	0.39 (0.9 σ)	+0.36
<i>Full, $\mu_0 = m_t$</i>	174.11 ± 1.39	1.07	0.37 (0.9 σ)	-0.91
<i>NWA, $\mu_0 = m_t$</i>	175.70 ± 0.96	1.17	0.24 (1.2 σ)	-2.50
<i>NWA_{Prod.}, $\mu_0 = m_t$</i>	169.93 ± 0.98	1.20	0.20 (1.3 σ)	+3.27
<i>5 bins</i>				
<i>Full, $\mu_0 = H_T/2$</i>	173.15 ± 1.32	0.93	0.44 (0.8 σ)	+0.05
<i>Full, $\mu_0 = E_T/2$</i>	172.55 ± 1.18	1.07	0.37 (0.9 σ)	+0.65
<i>Full, $\mu_0 = m_t$</i>	173.92 ± 1.38	1.48	0.20 (1.3 σ)	-0.72
<i>NWA, $\mu_0 = m_t$</i>	175.54 ± 0.97	1.38	0.24 (1.2 σ)	-2.34
<i>NWA_{Prod.}, $\mu_0 = m_t$</i>	169.37 ± 1.43	1.16	0.33 (1.0 σ)	+3.83

NWA & Off-Shell Effects

25 fb⁻¹

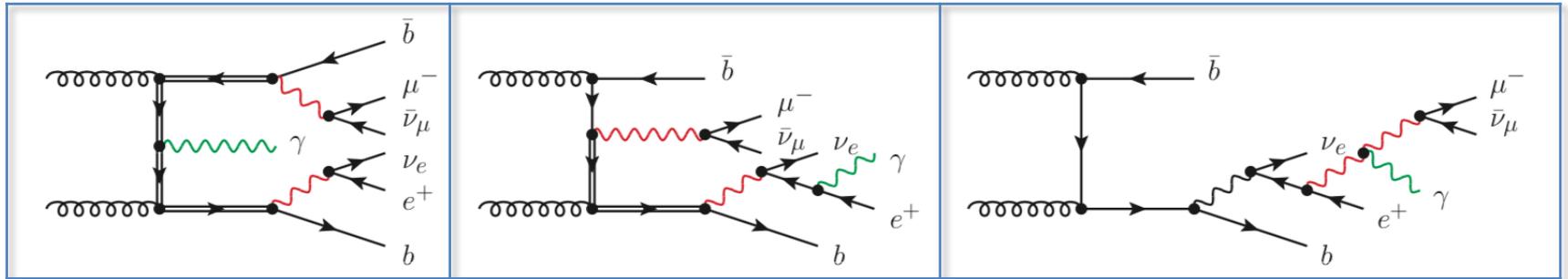
$pp \rightarrow t\bar{t}j \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j$ @ 13 TeV LHC

Theory, NLO QCD CT14 PDF	$m_t^{\text{out}} \pm \delta m_t^{\text{out}}$ [GeV]	Averaged $\chi^2/\text{d.o.f.}$	Probability $p\text{-value}$	$m_t^{\text{in}} - m_t^{\text{out}}$ [GeV]
<i>31 bins</i>				
<i>Full, $\mu_0 = H_T/2$</i>	173.09 ± 0.42	1.04	0.41 (0.8 σ)	+0.11
<i>Full, $\mu_0 = E_T/2$</i>	172.45 ± 0.39	1.12	0.30 (1.0 σ)	+0.75
<i>Full, $\mu_0 = m_t$</i>	173.76 ± 0.40	1.87	0.003 (3.0 σ)	-0.56
<i>NWA, $\mu_0 = m_t$</i>	175.65 ± 0.31	2.99	$7 \cdot 10^{-8}$ (5.4 σ)	-2.45
<i>NWA_{Prod.}, $\mu_0 = m_t$</i>	169.59 ± 0.30	3.10	$2 \cdot 10^{-8}$ (5.6 σ)	+3.61
<i>5 bins</i>				
<i>Full, $\mu_0 = H_T/2$</i>	173.08 ± 0.40	0.94	0.44 (0.8 σ)	+0.12
<i>Full, $\mu_0 = E_T/2$</i>	172.48 ± 0.38	1.58	0.18 (1.3 σ)	+0.72
<i>Full, $\mu_0 = m_t$</i>	173.75 ± 0.40	6.76	$2 \cdot 10^{-5}$ (4.3 σ)	-0.55
<i>NWA, $\mu_0 = m_t$</i>	175.49 ± 0.30	5.31	$2 \cdot 10^{-4}$ (3.7 σ)	-2.29
<i>NWA_{Prod.}, $\mu_0 = m_t$</i>	169.39 ± 0.47	3.42	$8 \cdot 10^{-3}$ (2.6 σ)	+3.81

NWA & Off-Shell Effects

❖ Feynman Diagrams → 628 @ LO for gg channel

$$t\bar{t}\gamma + X @ \mathcal{O}(\alpha_s^2\alpha^5)$$

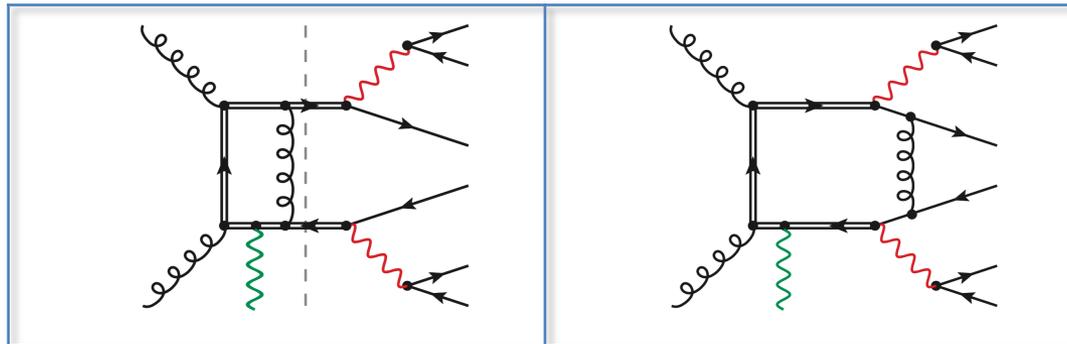


❖ NLO → 4348 real emission & 36032 @ 1-loop for gg channel

❖ Most complicated → 90 heptagons & 958 hexagons

$$t\bar{t}\gamma + X @ \mathcal{O}(\alpha_s^3\alpha^5)$$

*tty in NWA
up to pentagons*



*tty full
up to heptagons*

Top-Quark Resonances

- ❖ Putting simply $\Gamma_t \neq 0$ violates gauge invariance
- ❖ Gauge-invariant treatment \rightarrow *Complex Mass Scheme*
- ❖ In the amplitude the substitution is performed for top quark

$$(\not{p} - m_t + i\epsilon)^{-1} \longrightarrow (\not{p} - \mu_t + i\epsilon)^{-1}$$

$$\mu_t^2 = m_t^2 - i m_t \Gamma_t$$

Denner, Dittmaier, Roth, Wackerath '99
Denner, Dittmaier, Roth, Wieders '05

- ❖ All matrix elements evaluated using complex masses
- ❖ Another non trivial aspect \rightarrow Evaluation of one-loop scalar integrals
- ❖ Scalar integrals with complex masses \rightarrow Supported e.g. by **ONELOOP**

van Hameren '11

HELAC-NLO

Ossola, Papadopoulos, Pittau '08

van Hameren, Papadopoulos, Pittau '09



van Hameren '11



Bevilacqua, Czakon, Garzelli, van Hameren, Kardos, Papadopoulos, Pittau, Worek '13



van Hameren '10

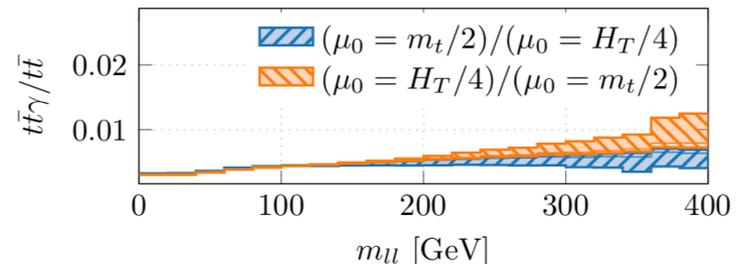
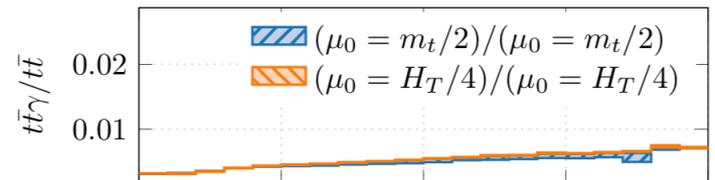
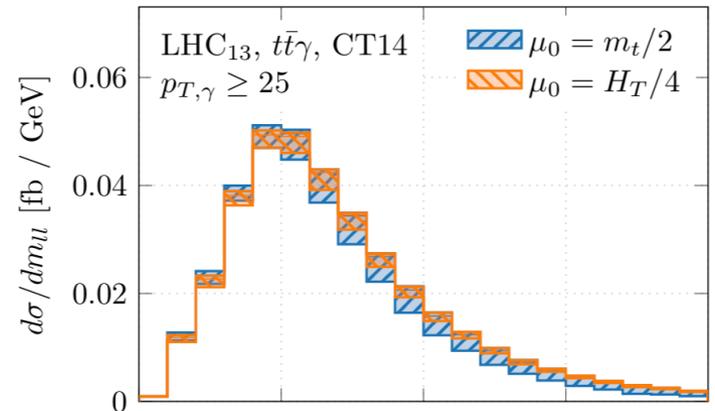
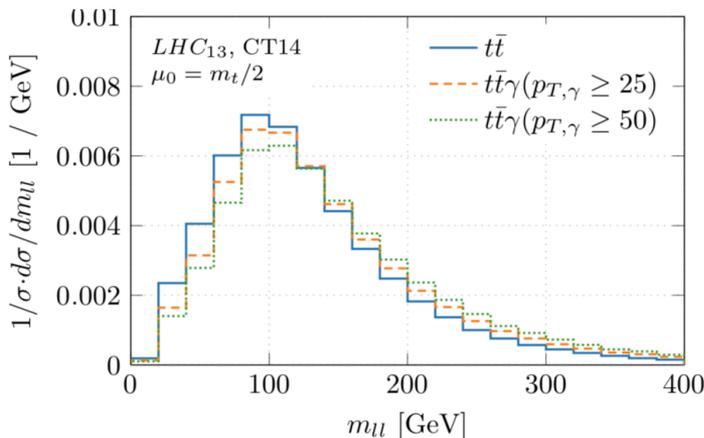
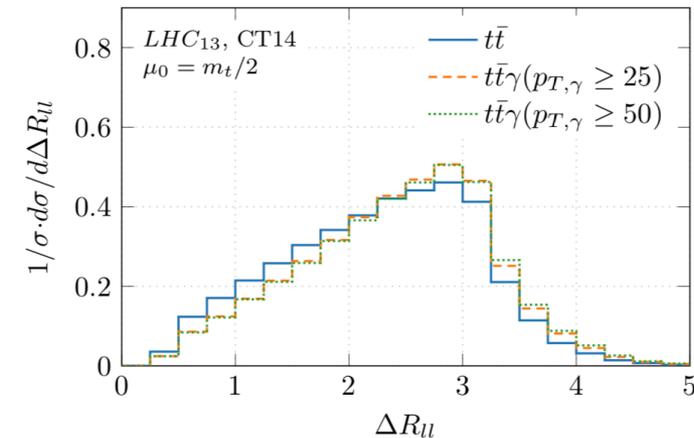
*Czakon, Papadopoulos, Worek '09
Bevilacqua, Czakon, Kubocz, Worek '13*

Cross Section Ratios: $t\bar{t}\gamma/t\bar{t}$

- ❖ 1% – 3% precision for *Integrated Cross Section Ratios*
- ❖ *Differential Ratios* with 1% – 6% precision:
- ❖ Such high precision has only been reserved till now for NNLO !

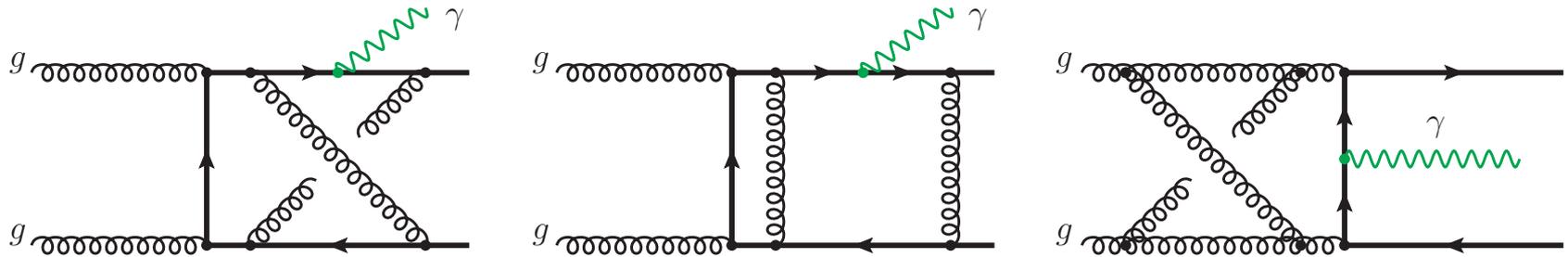
Off-shell Tops

$M_{b\bar{b}}, M_{\ell\ell}, \Delta\phi_{\ell\ell}, p_{T,\ell_1}$



NNLO & Open Questions

- ❖ NNLO QCD to on-shell $pp \rightarrow tty$
 - ❖ 2-loop virtual amplitude ❌



- ❖ Double-real radiation @ NNLO: sector-improved residue subtraction scheme with **STRIPPER** ✅

Czakon '10 '11 & Czakon, Heymes '14

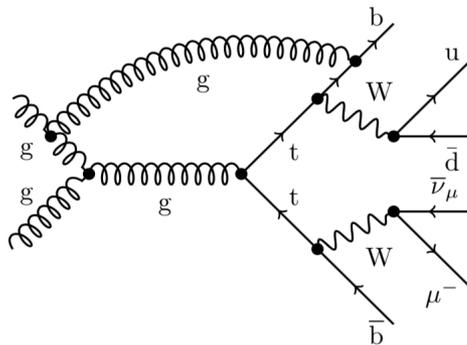
- ❖ Phenomenological applications for tty & tty/tt
 - ❖ Measuring top quark charge, various asymmetries
 - ❖ Constraining exotic physics scenarios
 - ❖ Probing strength & structure of tty vertex, ...
- ❖ *Long term goal* \rightarrow NNLO QCD to tty & tth in NWA - *di-lepton* channel
 - ❖ Polarized 2-loop virtual amplitudes for tty & tth ❌

NLO & Open Questions

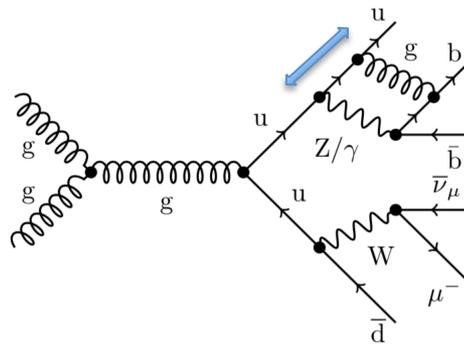
❖ Top off-shell effects @ NLO QCD $pp \rightarrow tt$ & $pp \rightarrow tt + X$ for *lepton+jets* channel

- ❖ **HELAC-DIPOLES** → Dipole subtraction method for both **QCD** ✓ & **QED** ✗
→ Soft or collinear photon emission *Dittmaier '00*
- ❖ **HELAC-1LOOP** → W, Z, γ in 1-loop diagrams, rational parts, ... ✗

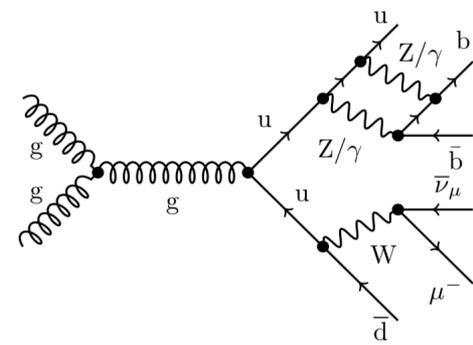
QCD correction



Mixed correction



EW correction



One-loop Feynman diagrams contributing to $gg \rightarrow \mu^- \bar{\nu}_\mu b \bar{b} jj$ @ $\mathcal{O}(\alpha_s^3 \alpha^4)$

Denner, Pellen '18

❖ *Long term goal* → EW + QCD for tt , tty , ttH , ttj , ttZ , ttW^\pm

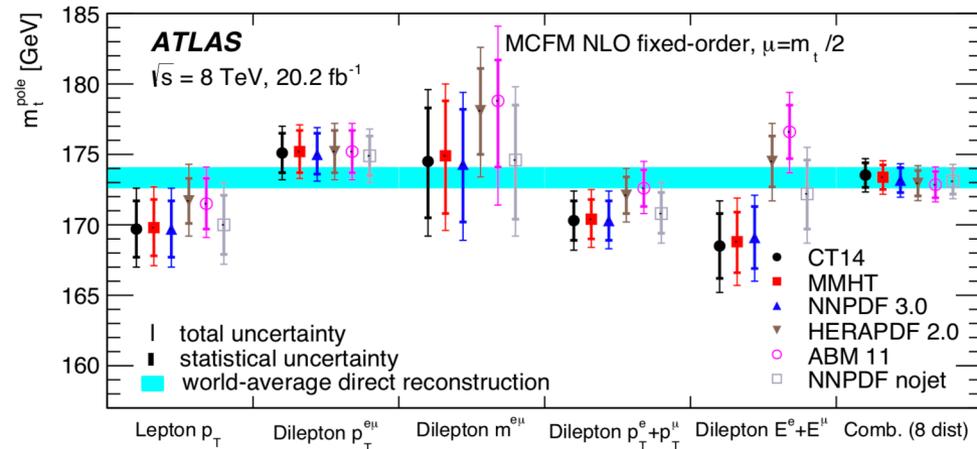
NNLO-NLO & Open Questions

- ❖ Merging off-shell top quark effects @ NLO in QCD with NNLO QCD top quark predictions for $pp \rightarrow tt$ in *di-lepton* channel

- ❖ Determination of the top quark mass from leptonic observables \rightarrow Fiducial σ_{tt}

$$p_T^{\ell^+}, p_T^{\ell\ell}, M_{\ell\ell}, (E^{\ell^+} + E^{\ell^-}), (p_T^{\ell^+} + p_T^{\ell^-}), \eta^{\ell^+}, \eta^{\ell\ell}, \Delta\phi_{\ell\ell}$$

$$m_t = 172.2 \pm 0.9 \text{ (stat.)} \pm 0.8 \text{ (syst.)} \pm 1.2 \text{ (th.) GeV}$$



CERN-EP-2017-200
TOP2018 Workshop

- ❖ Various tt NLO generators interfaced to PS used

- ❖ $d\sigma_{tt}/dX$ modeled poorly by NLO+PS

- ❖ The most precise result obtained from fixed-order NLO predictions

- ❖ *Measurements limited by theory uncertainties stemming from modeling of top quark decays!*

NLO & Open Questions

- ❖ Effects of New Physics at high scale Λ described by effective Lagrangian

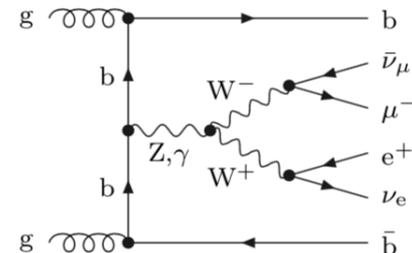
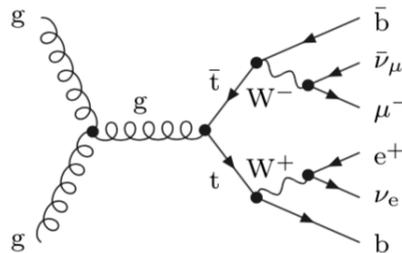
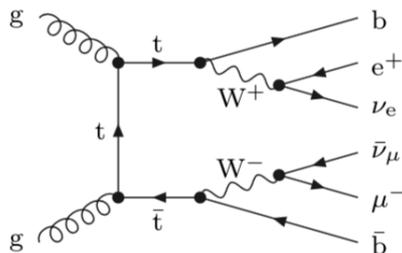
$$\mathcal{L}_{\text{SM}}^{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum_i C_i^{(6)} \mathcal{O}_i^{(6)} + \dots$$

\mathcal{O}_i - effective operators
 C_i - Wilson coefficients

- ❖ Minimal set of top anomalous couplings \rightarrow *Aguilar-Saavedra '09*
- ❖ $t\bar{t}\gamma$ vertex with contributions from dim-6 effective operators parameterized as

$$\mathcal{L}_{t\bar{t}\gamma} = -eQ_t \bar{t} \gamma^\mu t A_\mu - e \bar{t} \frac{i\sigma^{\mu\nu} (p_t - p_{\bar{t}})_\nu}{m_t} (d_V^\gamma + i d_A^\gamma \gamma_5) t A_\mu$$

- ❖ **HELAC-NLO** \rightarrow Top anomalous couplings $Wtb, Ztt, t\bar{t}\gamma, t\bar{t}H$ & $g\bar{t}t$ ☒
- ❖ **HELAC-NLO** \rightarrow NWA ☒
- ❖ How meaningful is this approach when top off-shell effects are included? ☒



Summary

❖ *Very ambition program for top-quark physics at NNLO & NLO*

❖ *Modeling of top quark decays crucial*

- ❖ Full NWA or complete top quark off-shell effects
- ❖ *tt* spin correlations
- ❖ Possibility of using kinematic-dependent scales

❖ Improving predictions for: $pp \rightarrow tt+X$, $X=\gamma, Z, W^\pm, H, j, bb, jj, tt, \dots$

❖ *di-lepton & lepton + jets* top-quark decay channels

❖ Plethora of phenomenological applications

❖ *Important input for New Physics searches*

❖ *Simplified top-philic dark matter & SUSY models*

- ❖ Signal: $pp \rightarrow ttXX \rightarrow tt p_T^{miss}$
- ❖ Dominant reducible SM background: $pp \rightarrow tt$
- ❖ Irreducible SM background: $pp \rightarrow ttZ \rightarrow tt\nu_l\nu_l \rightarrow tt p_T^{miss}$

