

The lepton propagator PROPOSAL and the air shower simulation code CORSIKA

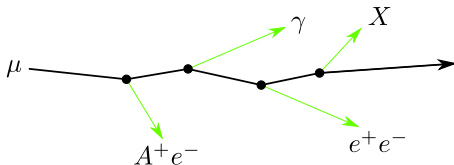
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CORSIKA Cosmic Ray Simulation Workshop Karlsruhe, June 17, 2019

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PROPOSAL

- ▶ Monte Carlo tool for charged lepton propagation through media.
- ▶ Used in the simulation chain of IceCube
- ▶ **PR**opagator with **O**ptimal **P**recision and **O**ptimized **S**peed for **A**ll **L**eptons
 - ▶ Calculate energy losses
 - ▶ Passes interaction points and decay products to further simulation programs



Energy cuts

- ▶ Distinguish between **continuous** and **stochastic** energy losses
- ▶ Cut between continuous and stochastic loss:

$$\text{cut} = \min(e_{\text{cut}}, v_{\text{cut}} \cdot E), \quad v := \text{relative energy loss}$$

- ▶ Set energy cuts before, inside and behind the detector

Energy cuts in IceCube

- ▶ before: $v_{\text{cut}} = 0.05$
- ▶ inside: $e_{\text{cut}} = 500 \text{ MeV}$
- ▶ behind: $v_{\text{cut}} = v_{\text{max}}$

Continuous loss

Describes energy loss in the range
 $v \in [v_{\text{min}}, v_{\text{cut}}]$

$$\begin{aligned} f(E) &:= \sum_{\text{processes}} \frac{dE_{\sigma}}{dx} \\ &= E \cdot \sum_{\text{process}} \sum_{\substack{\text{atom} \\ \text{in medium}}} \frac{N_i}{A_i} \int_{v_{\text{min}}}^{v_{\text{cut}}} v \frac{d\sigma}{dv} dv \end{aligned}$$

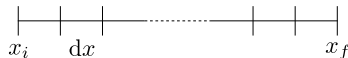
Stochastic loss

Described by the interaction probability
 $v \in [v_{\text{cut}}, v_{\text{max}}]$

$$dP(E) = \sigma(E) dx$$

$$\sigma(E) = \sum_{\text{processes}} \sum_{\substack{\text{atom} \\ \text{in medium}}} \frac{N_i}{A_i} \int_{v_{\text{cut}}}^{v_{\text{max}}} \frac{d\sigma}{dv} dv$$

Determine the occurrence of a stochastic loss



Probability to have
no stochastic loss in
(x_i, x_f), but at x_f
within dx :

$$\left\{ \begin{array}{l} (1 - dP(E(x_i))) \cdot \dots \cdot (1 - dP(E(x_{f-1}))) \cdot dP(E(x_f)) \\ \approx \exp(-dP(E(x_i))) \cdot \dots \cdot \exp(-dP(E(x_{f-1}))) dP(E(x_f)) \\ \approx \exp \left[- \int_{P(E(x_i))}^{P(E(x_f))} dP(E(x)) \right] \cdot dP(E(x_f)) \\ = d \left[- \exp \left(- \int_{E_i}^{E_f} \frac{\sigma(E)}{-f(E)} dE \right) \right] =: d(-\xi) \in (0, 1] \end{array} \right.$$

$$\Rightarrow \text{Sample } E_f \text{ from } \int_{E_i}^{E_f} \frac{\sigma(E)}{-f(E)} dE = -\ln(\xi)$$

Advance the particle according to E_f

- Calculating the displacement

$$x_f = x_i - \int_{E_i}^{E_f} \frac{dE}{f(E)}$$

- the elapsed time

$$t_f = t_i - \int_{t_i}^{t_f} \frac{dx}{v(x)} = t_i - \int_{E_i}^{E_f} \frac{dE}{f(E)v(E)}$$

- and the deviation from the shower axis (multiple scattering)

$$u_{x,y} = \frac{1}{2} \left(\frac{1}{\sqrt{3}} \xi_{x,y}^{(1)} + \xi_{x,y}^{(2)} \right), \quad \xi_{x,y}^{(1,2)} \sim \mathcal{N}(0, \theta_0^2)$$

Calculate the stochastic loss

- Calculate the interaction probability for each process

$$\sigma_i = \sum_{\substack{\text{atom} \\ \text{in medium}}} \frac{N_i}{A_i} \int_{v_{\text{cut}}}^{v_{\text{max}}} \frac{d\sigma}{dv} dv$$

- Calculate the amount of stochastic loss for each atom in the medium

$$\frac{1}{\sigma} \int_{v_{\text{cut}}}^{v(\xi)} \frac{d\sigma}{dv} dv = \xi$$

$$E_{\text{stochastic loss}} = v(\xi) \cdot E_{\text{particle}}$$

- Choose the Component, at which the energy loss takes place

Summary of the algorithm

Basic loop

Do:

Calculate the energy until a stochastic loss



Advance the particle according to E_f



Calculate the amount of the stochastic loss

Until: The particle decays

Specific Features

- **Interpolation tables**
- Continuous Randomization
- Multiple parametrizations of cross sections for systematic studies
- Further parameters for the trade-off between performance and precision (e.g. stop propagating the particle, if the energy is below a threshold)

Use of Interpolation tables

e.g. sampling of energy until next stochastic loss E_f

$$\int_{E_i}^{E_f} \frac{\sum \frac{N_i}{A_i} \int_{v_{\text{cut}}}^{v_{\text{max}}} \frac{d\sigma_j}{dv} dv}{E \sum \frac{N_i}{A_i} \int_{v_{\text{cut}}}^{v_{\text{max}}} v \frac{d\sigma_j}{dv} dv} dE = -\ln(\xi)$$

$$\text{where } \sigma_{\text{pair}}(v) = \int \frac{d\sigma}{dv d\rho} dv d\rho$$

⇒ Calculation of many integrals

- Instead use 1D Interpolation → huge performance gain

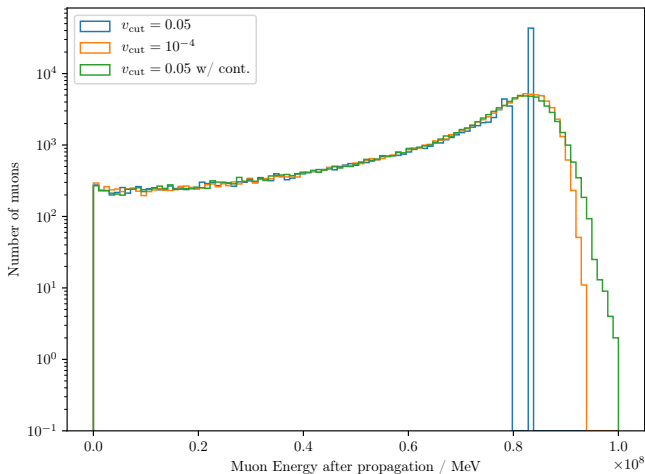
Continuous Randomization

Problem with energy cut:

- ▶ low: high precision, but slow and many (unnecessary) secondaries
- ▶ high: fast, but less precision and artifacts in muon flux
- ▶ muons without a stochastic loss are all treated the same

⇒ continuous randomization of the muon energy till next stochastic loss E_f

$$\langle (\Delta(\Delta E)) \rangle \approx \int_{e_0}^{e_{\text{cut}}} \frac{dE}{-f(E)} \left(\int_0^{e_{\text{cut}}} e^2 \frac{d\sigma}{dv} dv \right)$$



Cross section parametrizations for systematic studies

Bremsstrahlung

Parametrizations

- ▶ KelnerKokoulinPetrukhin
- ▶ AndreevBezrukovBugaev
- ▶ PetrukhinShestakov
- ▶ CompleteScreening
- ▶ SandrocksSoedingreksoRhode

also consider LPM and TM Effect

e^+e^- Pair Production

Parametrizations

- ▶ KelnerKokoulinPetrukhin
- ▶ SandrocksSoedingreksoRhode

and LPM Effect

Nuclear inelastic Interaction

- ▶ Vector meson dominance

- ▶ Kokoulin
- ▶ Rhode
- ▶ BezrukovBugaev
- ▶ Zeus

with hard and soft component

- ▶ Regge Theory

- ▶ AbramowiczLevinLevyMaor91
- ▶ AbramowiczLevinLevyMaor97
- ▶ ButkevichMikheyev
- ▶ RenoSarcevicSu (spin 0)

with shadowing parametrizations of

- ▶ ButkevichMikheyev
- ▶ DuttaRenoSarcevicSeckel

Propagation

- ▶ propagation through dense media
- ▶ requires media of uniform density
- ▶ propagation is fast
- ▶ adding new particles is relatively simple

Decay

- ▶ particles can decay based on lifetime
- ▶ final state particles calculated using Raubold-Lynch algorithm

Multiple Scattering

- ▶ Coulomb scattering on atoms in the medium
- ▶ several algorithms available
 - ▶ Molière scattering
 - ▶ Highland approximation to Molière scattering

Electromagnetic cascades

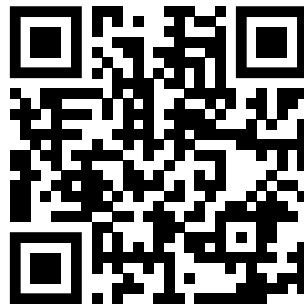
- ▶ MC-simulation requires propagation of many electrons, positrons and photons
- ▶ currently based on EGS4 (Nelson, Hirayama, and Rogers 1985)
- ▶ photon cross sections similar to lepton cross sections

Necessary extensions

- ▶ Density currently part of medium
 - ▶ each medium has its own interpolation tables
- ▶ Magnetic field deflection
 - ▶ We have basically worked out how to implement this
- ▶ Propagation of electrons/positrons
 - ▶ Some processes need to be added (Annihilation; Bhabha and Møller scattering compared to μe scattering)
- ▶ Propagation of photons
 - ▶ in principle similar to propagation of charged particles, but without continuous losses



<https://github.com/tudo-astroparticlephysics/PROPOSAL>



<https://arxiv.org/abs/1809.07740>

PROPOSAL may be modified and distributed under terms of a modified LGPL license.
More information on our GitHub page.

References



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Koehne, J.-H. et al. (2013). “PROPOSAL: A tool for propagation of charged leptons”. In: *Comput. Phys. Commun.* 184, pp. 2070–2090.



Nelson, W. R., H. Hirayama, and D. W. O. Rogers (1985). *The EGS4 Code System*. Tech. rep. Report SLAC-265. Stanford, CA: Stanford Linear Accelerator Center.



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Creating custom particle

- ▶ use pre-defined particles
 - ▶ electrons
 - ▶ muons
 - ▶ taus
 - ▶ sTaus, etc.
- ▶ or create new particle with properties
 - ▶ lifetime
 - ▶ mass
 - ▶ charge
 - ▶ decay channels
- ▶ combination of both

```
import pyPROPOSAL as pp
mu_def_builder = pp.particle.ParticleDefBuilder()
mu_def_builder.SetParticleDef(
    pp.particle.MuMinusDef.get()
mu_def_builder.SetLow(1e3) # MeV
mu_def_builder.SetName('new_mu')
mu_def_builder.SetMass(1e4) # MeV
mu_def_builder.SetLifetime(1e-5) # sec
mu_def_builder.SetCharge(2)
# create Leptonic decay table
decay_table = pp.decay.DecayTable()
products = [pp.particle.EMinusDef.get(),
            pp.particle.NuMuDef.get(),
            pp.particle.NuEBarDef.get()]
ldec = pp.decay.LeptonicDecayChannel(*products)
decay_table.add_channel(1, ldec)
mu_def_builder.SetDecayTable(decay_table)

particle_def = mu_def_builder.build()
```

Usage of new Structure

- Initialization of a Propagator
 - a Configuration file (json)
 - and a Particle Definition

The Interpolation files are build

- Propagation through different sectors
consisting of a geometry and a medium

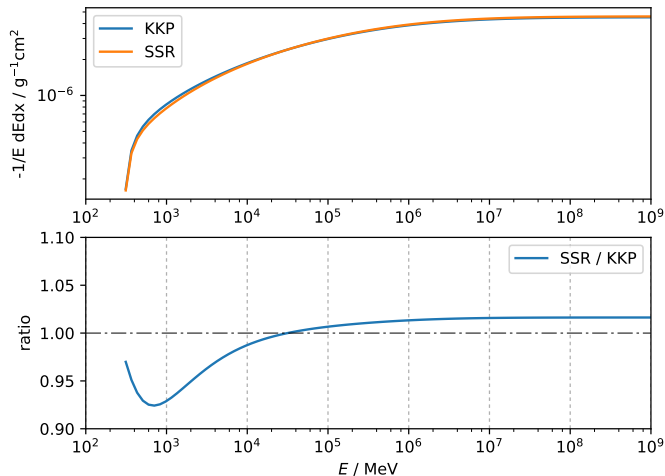
```
prop = pp.Propagator(particle_def,
                    config_file)

mu = prop.particle
mu.position = pp.Vector3D(0, 0, 0)
mu.direction = pp.Vector3D(0, 0, 1)
mu.energy = 1e10 # MeV
max_distance = 1e5 # cm
secondaries = prop.propagate(max_distance)
```

```
"global":
{
    "interpolation":
    {
        "do_interpolation" : true,
        "path_to_tables" : ["resources/tables"],
        "do_binary_tables" : false
    },
    "stopping_decay" : true,
    "scattering" : "Highland",
    "brems" : "BremsAndreevBezrukovBugaev",
    "photo" : "PhotoBezrukovBugaev",
    "lpm" : false,
    "photo_shadow" : "ShadowDuttaRenoSarcevicSeckel"
},
"sectors": [
{
    "hierarchy" : 0,
    "medium" : "ice",
    "density_correction" : 1,
    "geometry" :
    {
        "shape" : "sphere",
        "origin" : [0, 0, 0],
        "outer_radius" : 6374134000000,
        "inner_radius" : 0
    }
},
}
```

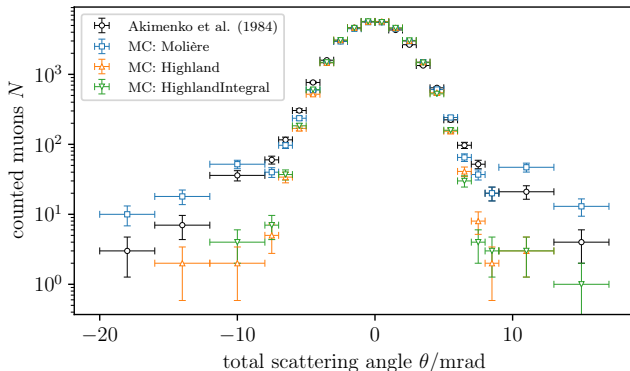
New Cross Sections

- ▶ improved atomic screening functions for
 - ▶ bremsstrahlung
 - ▶ pair production
 - ▶ radiative corrections for bremsstrahlung
- ⇒ corrections of several percent



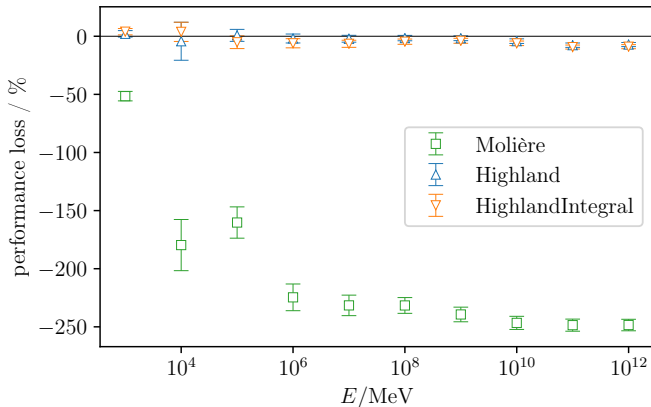
Multiple Scattering

- ▶ Molière
 - ▶ precise description
 - ▶ slow, especially for many components in medium
- ▶ Highland parametrization
 - ▶ Gaussian approximation to Molière's theory
 - ▶ two types available: one including continuous losses and one without
- ▶ no scattering



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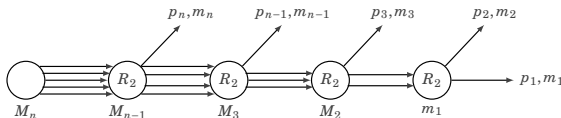
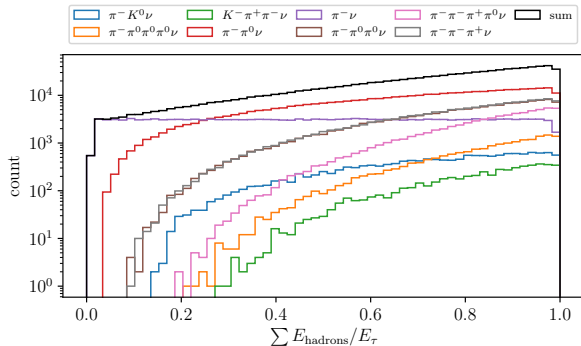
Hadronic Decay

- Before: two-body decay
- Calculate N -body decay phase space
- Constant matrix element

$$\Gamma = \frac{(2\pi)^4}{2M} \underbrace{\int \prod_{i=1}^n \frac{d^3 p_i}{2E_i} \delta^4 \left(p - \sum_{i=1}^n p_i \right)}_{N\text{-body phase space}} \overbrace{|\langle M(\mathbf{p}_i) \rangle|^2}^{\text{set to 1}}$$

Raubold-Lynch algorithm

- Iterative integration over intermediate two-body phase spaces
- Exactly calculable



Decay

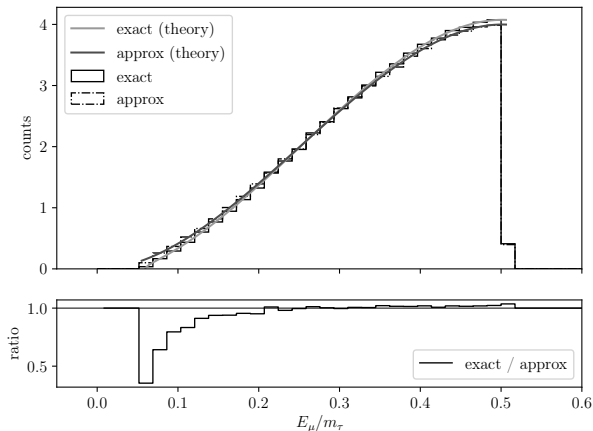
Leptonic Decay

- Muon decay and electronic tau decay
($m_l^2/M^2 \approx 0$)

$$\frac{d\Gamma}{dx} = \frac{G_F^2 M^5}{192\pi^3} (3 - 2x)x^2, \quad x = \frac{E_l}{E_{\max}}$$

- muonic tau decay ($m_\mu/m_\tau \approx 1/17$)

$$\frac{d\Gamma}{dx} = \frac{G_F^2}{12\pi^3} E_{\max} \sqrt{E_l^2 - m_l^2} \times \\ [ME_l(3M - 4E_l) + m_l^2(3E_l - 2M)]$$



Rare Processes

Implementation of rare processes, but with different signature in detector

- Muon pair production: Creation of muon bundles originating by a single muon
- Weak interaction: disappearance of a muon in a cascade

