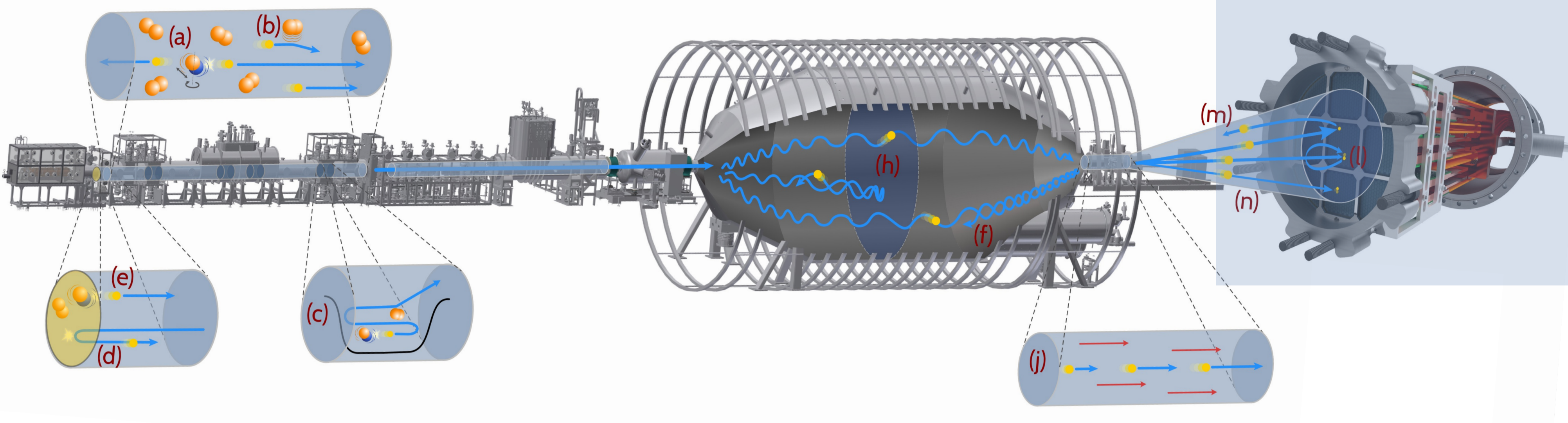
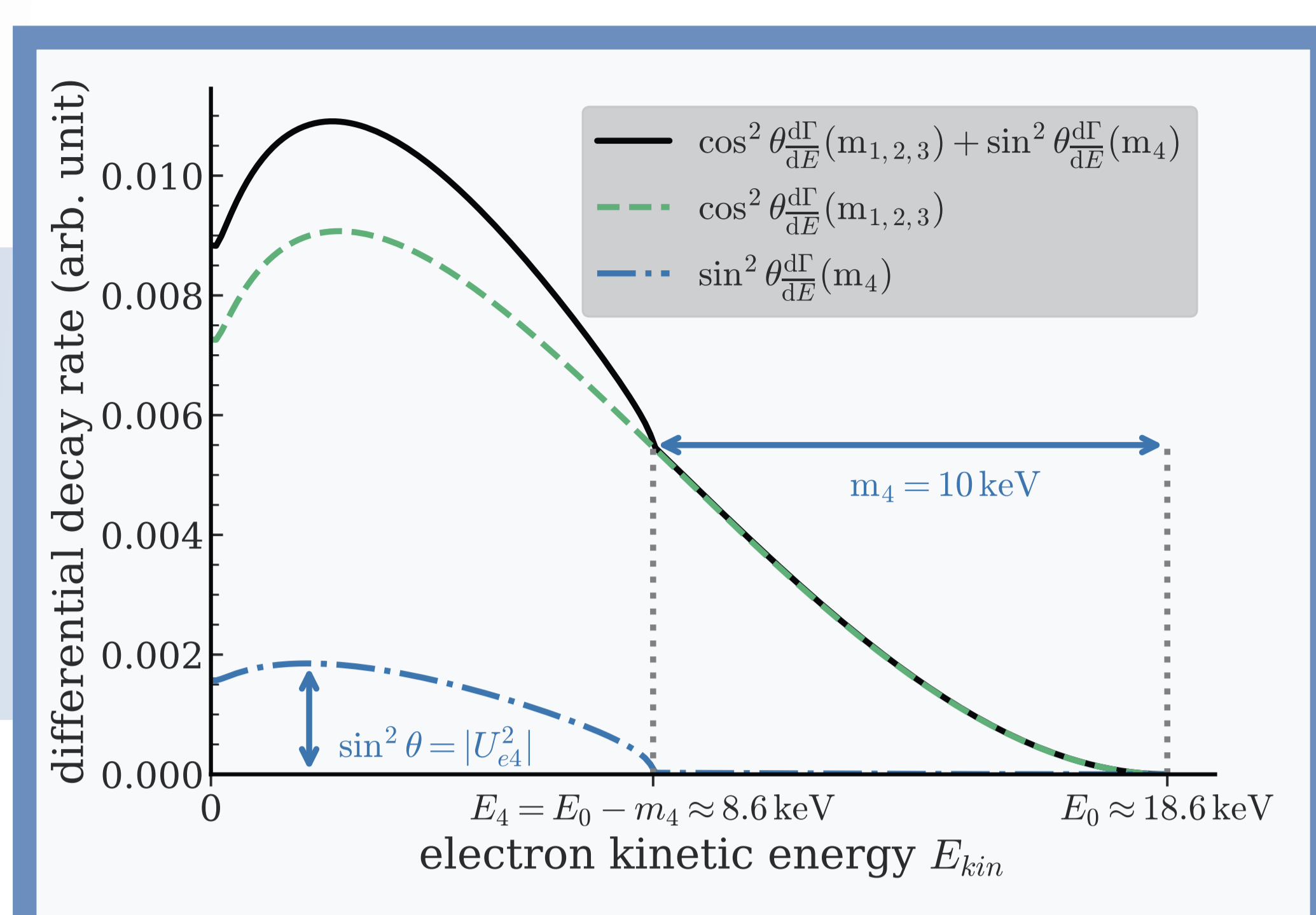


Starting 2026: KeV-scale sterile neutrino search



TRISTAN Detector



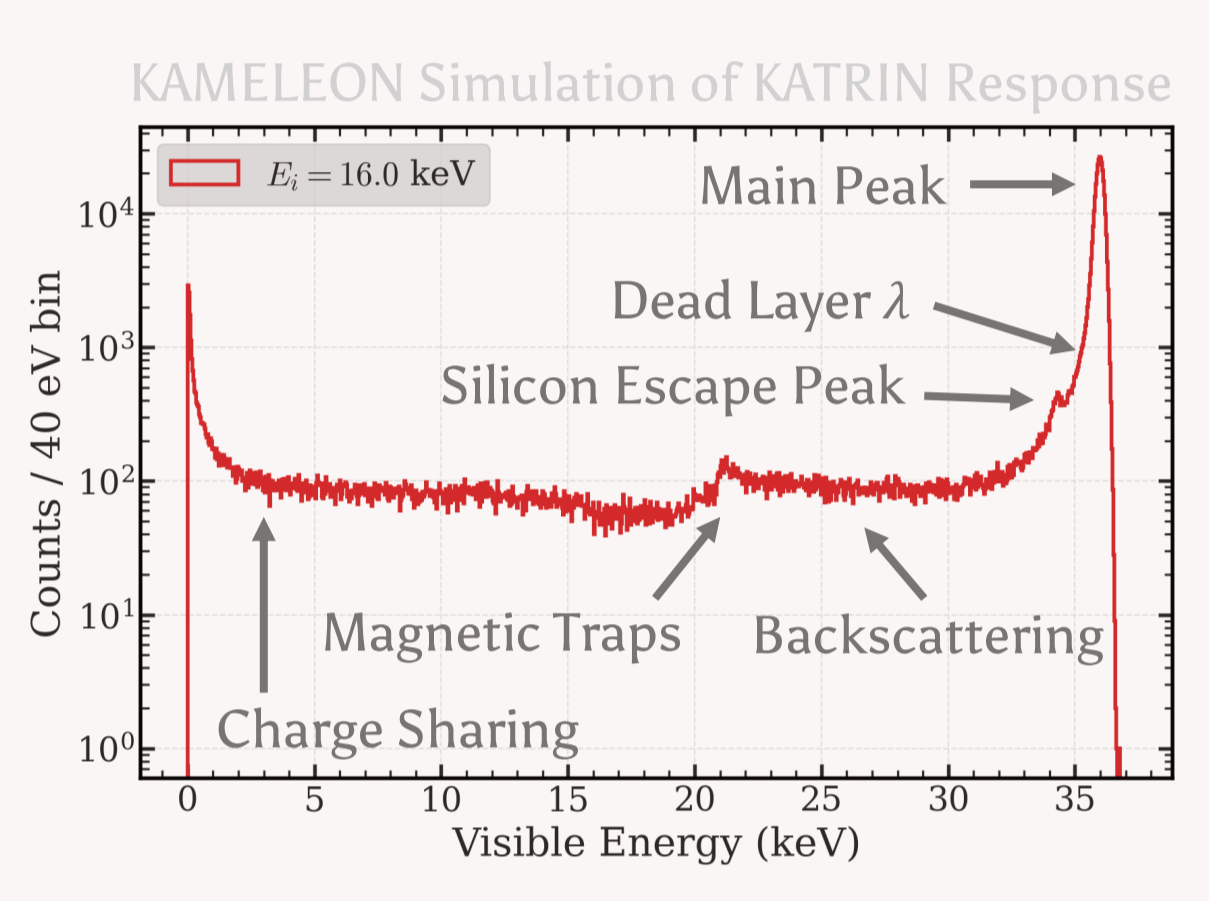
keV-sterile-neutrino search:

- Kink-like sterile neutrino signature
- Deep into the differential T_2 β -decay spectrum
- Extremely high rates ($\sim 10^8$ cps)
- With silicon drift detector array with ~ 1 k pixels
- Designed to be sensitive to ppm-level $\sin^2\theta$

Analysis Goal: Fit Prediction to Data „Response Function“

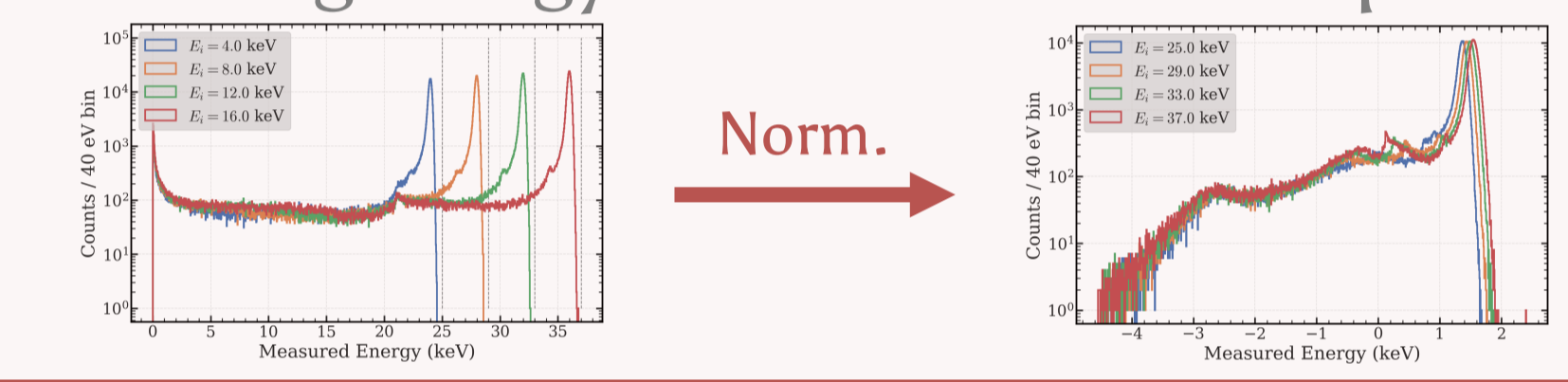
$$\text{Prediction} = A \times \Gamma_{\text{vis}}(E, m_4, \sin^2\theta, y_{\text{nuis}}) = A \times \int R(E', E, y_{\text{nuis}}) \Gamma_{\text{theo}}(E, m_4, \sin^2\theta) dE'$$

Modelling Challenge: Systematic Effects (a – l)

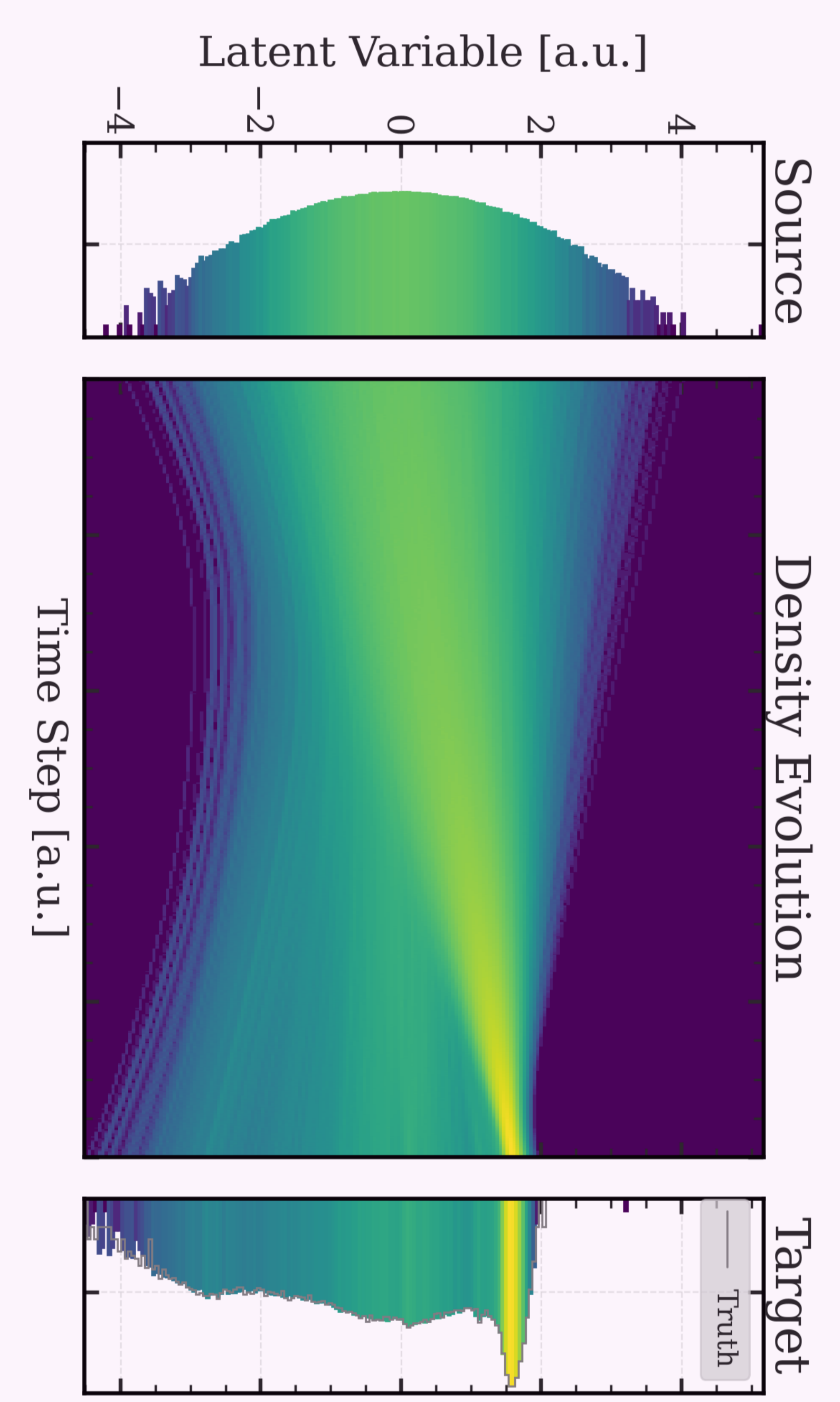


Challenges:

- Some systematic effects act at the percent level on the spectrum (vs. possibly ppm-level signal)
- Many systematic effects have to be simulated
- Systematic uncertainties (systematic effects need to be conditionals of response)
- e^- starting energy as conditional of response



Continuous Normalizing Flow Trained via Flow Matching



Flow Matching:

- NN learns to predict the „probability flow“ vector field connecting a simple distribution to the target distribution (i.e. the response)
- Is trained **only using samples**
- Provides an unbinned conditional response

Modelling Approaches

- Precise and accurate at high stat.
- Conditioned on E_{in}, y_{nuis}
- unbinned

Empirical Model (by hand / symbolic regression)

- Expensive (high stat. simulations for each E_{in}, y_{nuis})
- Very hard

Normalizing Flows

- Focus of this poster
- ✓
- ✓
- ✓

Difficulties and Solutions for Continuous Normalizing Flows

- High peak with long tail containing high frequency features
- High variance in probability flow vector field due to conditionals and crossing paths
- Large Number of Samples

- 1 Adding Gaussian Fourier Features
- 2 Conditional Optimal Transport
- 3 Amortizing Optimal Transport

1 & 2 Gaussian Fourier Projection:

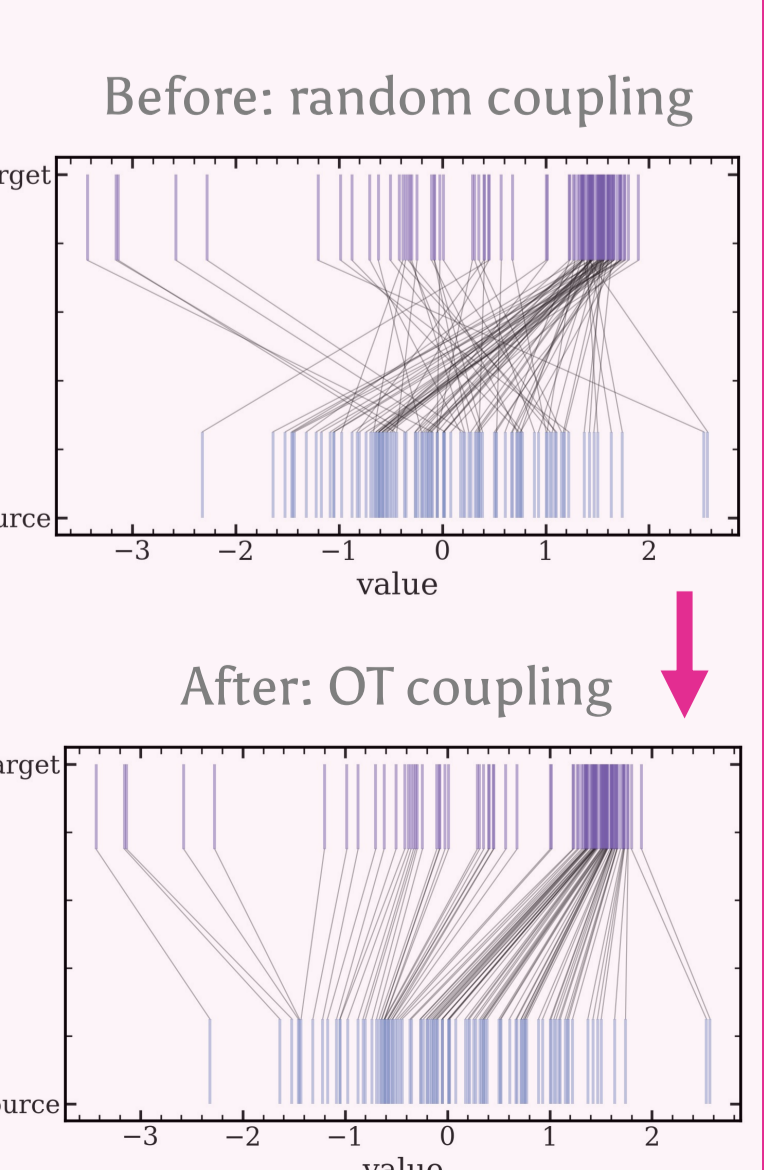
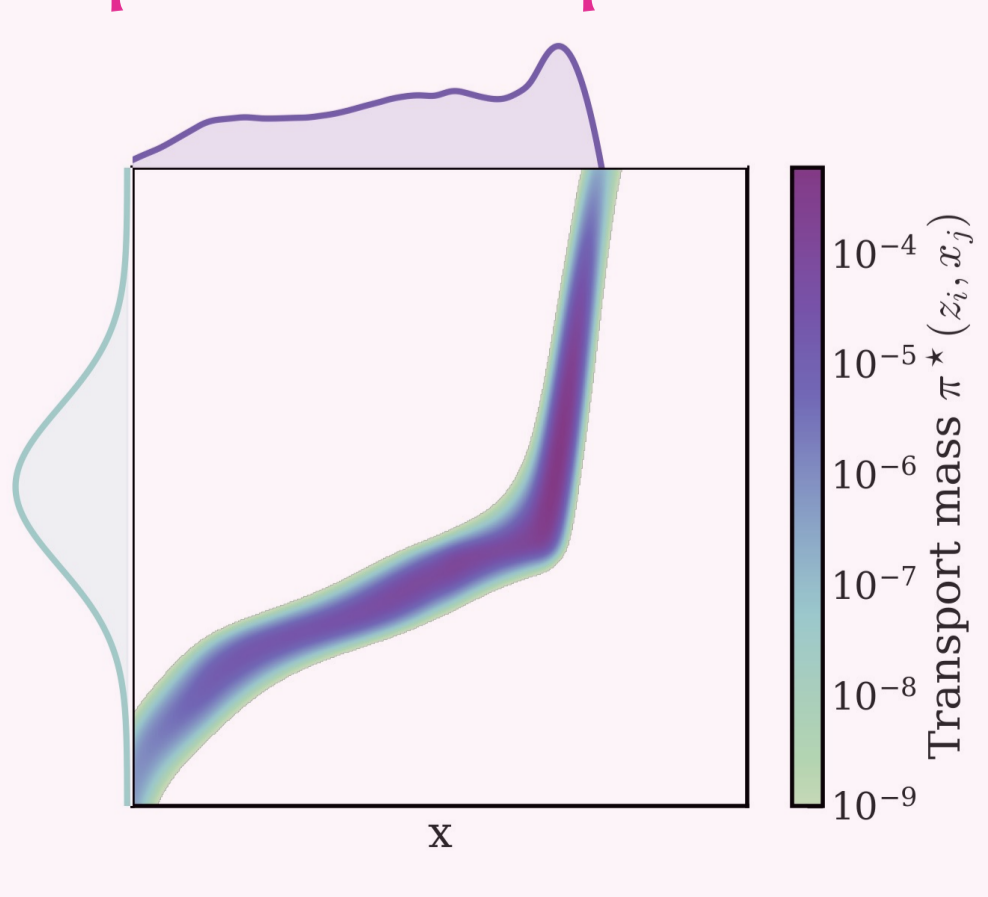
Gaussian Fourier Projection

$$\gamma(v) = [\cos 2\pi Bv, \sin 2\pi Bv]^T$$

$$B_{ij} \sim \mathcal{N}(0, \sigma^2)$$

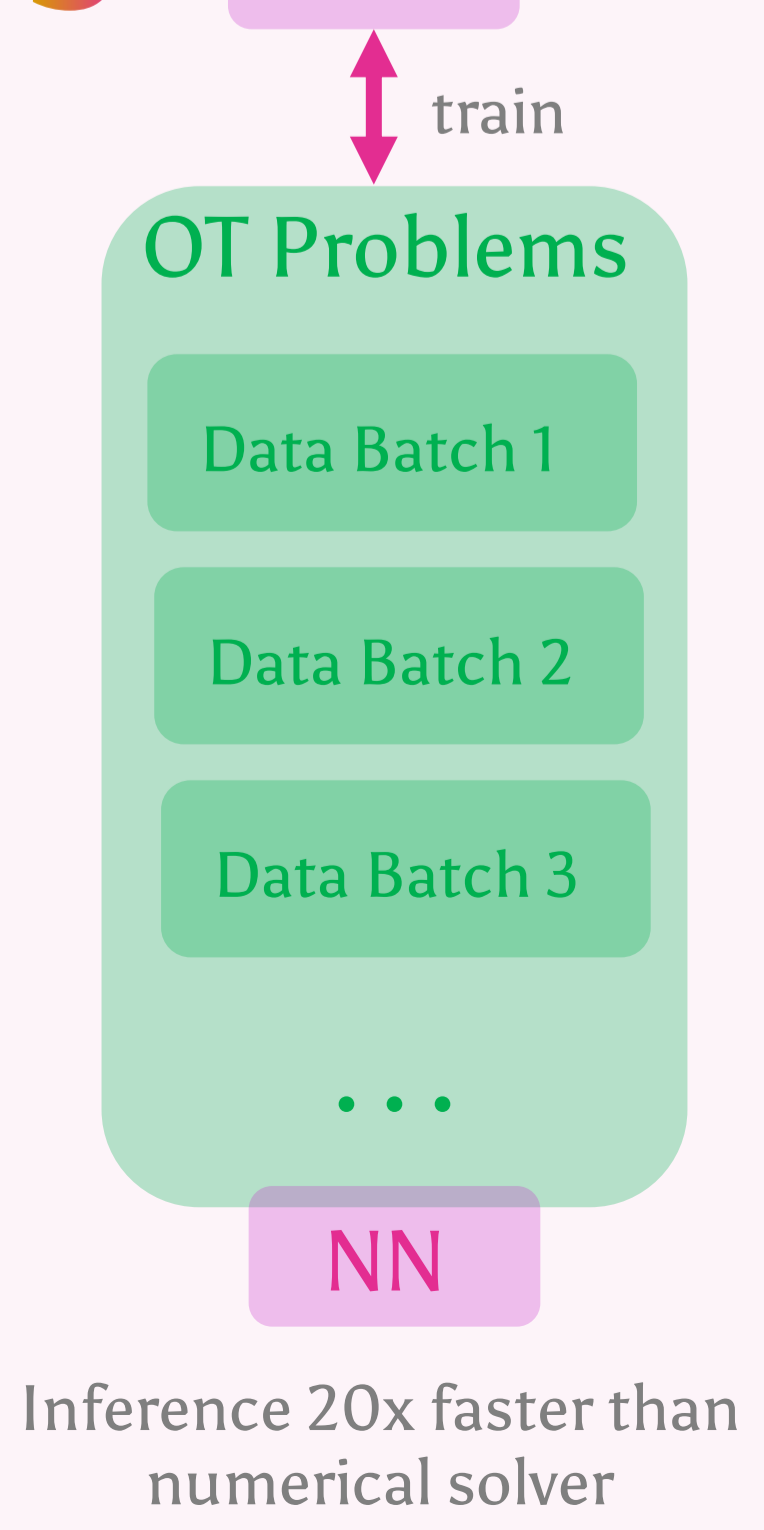
Overcomes NNs natural bias towards learning low frequencies first

Optimal Transport Plan:



Using Euclidean and Conditional Cost

3 NN



Results (preliminary) Takeaway:

Good first step, need to extend to more y_{nuis} and fine-tune hyperparameters

