

The SM EFT

- a global approach -

Ilaria Brivio

Institut für Theoretische Physik,
Universität Heidelberg

work mostly developed at the
Niels Bohr Institute, University of Copenhagen
with M. Trott and T. Corbett



The Niels Bohr
International Academy



- fundamental assumptions:
- ▶ new physics nearly decoupled: $\Lambda \gg (v, E)$
 - ▶ at the accessible scale: **SM** fields + symmetries

☞ a Taylor expansion in canonical dimensions (v/Λ or E/Λ):

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$$

$$\mathcal{L}_n = \sum_i C_i \mathcal{O}_i^{d=n}$$

C_i free parameters (Wilson coefficients)

$\mathcal{O}_i$ invariant operators that form
a complete, non redundant basis

The SMEFT – recent developments

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B cons. $N_f = 1 \rightarrow$

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$$

$N_f = 3 \rightarrow$

12

2499

948

36971

- ▶ # of parameters known for all orders

Lehman 1410.4193

Lehman, Martin 1510.00372

Henning, Lu, Melia, Murayama 1512.03433

The SMEFT – recent developments

Weinberg PRL43(1979)1566

Lehman 1410.4193

Henning,Lu,Melia,Murayama 1512.03433

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Leung,Love,Rao Z.Ph.C31(1986)433

Buchmüller,Wyler Nucl.Phys.B268(1986)621

Grzadkowski et al 1008.4884

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↪ Benjamin's talk

Henning, Lu, Murayama 1412.1837, 1604.01019
del Aguila, Kunszt, Santiago 1602.00126
Drozd, Ellis, Quevillon, You 1512.03003
Ellis, Quevillon, You, Zhang 1604.02445, 1706.07765
Fuentes-Martin, Portoles, Ruiz-Femenia 1607.02142
Zhang 1610.00710

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Shadmi, Weiss 1809.09644

Henning, Melia 1901.06747, 1902.06754, 1902.06747

Ma, Shu, Xiao 1902.06752

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$\mathcal{L}_6$: leading deviations from SM

- ▶ complete RGE available

Alonso, Jenkins, Manohar, Trott 1308.2627, 1310.4838, 1312.2014
Grojean, Jenkins, Manohar, Trott 1301.2588
Alonso, Chang, Jenkins, Manohar, Shotwell 1405.0486
Ghezzi, Gomez-Ambrosio, Passarino, Uccirati 1505.03706

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Pruna, Signer 1408.3565
Hartmann, (Shepherd), Trott 1505.02646, 1507.03568, 1611.09879
Ghezzi, Gomez-Ambrosio, Passarino, Uccirati 1505.03706
Gauld, Pecjak, Scott 1512.02508, Dawson, Giardino 1801.01136
Deutschmann, Duhr, Maltoni, Vryonidou 1708.00460
Dedes, Paraskevas, Rosiek, Suxho, Trifyllis 1805.00302 ...

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↪ Ben's talk

Dedes, Materkowska, Paraskevas, Rosiek, Suxho 1704.03888
Helset, Paraskevas, Trott 1803.08001

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- ▶ complete RGE available
 - ▶ many tree-level calculations of Higgs / EW / flavor observables
 - ▶ 1-loop results available for selected processes
 - ▶ formulation in R_ξ gauge
 - ▶ various tools available for numerical analysis
- [MC generation, analytic calculation, fitting, matching, RGE running...]

↪ Ben's talk

↪ SMEFT-Tools

X^3		φ^6 and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	Q_φ	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
Q_W	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	Q_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{j k} [(d_p^\alpha)^T C u_r^\beta] [(q_s^j)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{j k} (\bar{q}_s^k d_t)$	Q_{qqqu}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{j k} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^j)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{j k} (\bar{q}_s^k T^A d_t)$	Q_{qqq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{j k} \varepsilon_{m n} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^m)^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{j k} (\bar{q}_s^k u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^j)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{j k} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

More than a parameterization

the complete SMEFT Lagrangian, truncated at a given order,
is always* **a well-defined QFT** and
a valid description of Nature

* assuming nearly-decoupled BSM matching SM sym + fields and evaluating at $E \ll \Lambda$

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- ▶ model-independent (within assumptions)
- ▶ allows systematic **one-loop improvement** , RG evolution ...

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- ▶ model-independent (within assumptions)
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- ▶ a general, systematic **probe of new physics**
- ▶ a **universal language** for data interpretation

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global = all operators contributing to measured processes are retained *a priori*.
only selection criterion: physical impact.

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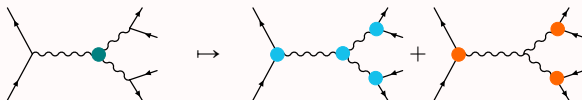
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$$W_{\mu\nu}^a D^\mu H^\dagger \sigma^a D^\nu H \xrightarrow{EOM} \mathcal{Q}_{HW}, \mathcal{Q}_{HWB}, \mathcal{Q}_{Hq}^{(3)}, \mathcal{Q}_{HI}^{(3)} + \text{Higgs ops.}$$



A global approach

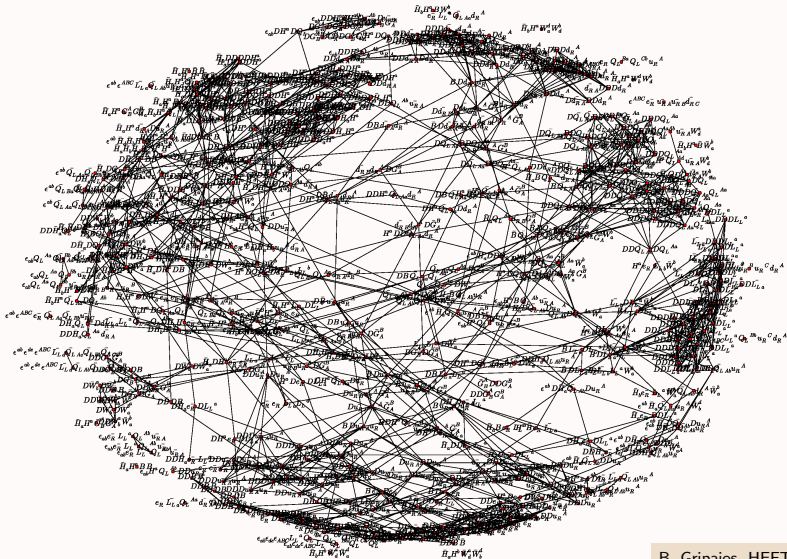
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$$D_\mu G^{a\mu\nu} D^\rho G_{\rho\nu}^a \xrightarrow{EOM} (\bar{q} T^a q + \bar{u} T^a u + \bar{d} T^a d)^2$$



The need for a global analysis



B. Gripaios, HEFT2018

The SMEFTsim package

an UFO & FeynRules model with*:

Brivio, Jiang, Trott 1709.06492
feynrules.irmp.ucl.ac.be/wiki/SMEFT

1. the complete B-conserving Warsaw basis for 3 generations ,
including all complex phases and ~~CP~~ terms
set up for unitary gauge, fermion mass basis
2. automatic field redefinitions to have **canonical kinetic terms**
3. automatic **parameter shifts** due to the choice of an input parameters set

↪ **backup**

Main scope:

estimate **LO SMEFT effects**: uncertainty is $\mathcal{O}\left(\frac{v^4}{\Lambda^4}\right) \rightarrow$ theo. accuracy $\gtrsim 1\%$

NLO not supported.

The SMEFTsim package

6 different implementations available

Brivio, Jiang, Trott 1709.06492

$$\textcircled{3} \text{ flavor structures } \left\{ \begin{array}{l} \text{general} \\ U(3)^5 \text{ symmetric} \\ \text{linear MFV} \end{array} \right. \times \textcircled{2} \text{ input schemes } \left\{ \begin{array}{l} \hat{\alpha}_{\text{em}}, \hat{m}_Z, \hat{G}_f \\ \hat{m}_W, \hat{m}_Z, \hat{G}_f \end{array} \right.$$

feynrules.irmp.ucl.ac.be/wiki/SMEFT

Pre-exported UFO files (include restriction cards)

	Set A		Set B	
	α scheme	m_W scheme	α scheme	m_W scheme
Flavor general SMEFT	SMEFTsim_A_general_alphaScheme_UFO.tar.gz	SMEFTsim_A_general_MwScheme_UFO.tar.gz	SMEFT_alpha_UFO.zip	SMEFT_mW_UFO.zip
MFV SMEFT	SMEFTsim_A_MFV_alphaScheme_UFO.tar.gz	SMEFTsim_A_MFV_MwScheme_UFO.tar.gz	SMEFT_alpha_MFV_UFO.zip	SMEFT_mW_MFV_UFO.zip
$U(3)^5$ SMEFT	SMEFTsim_A_U35_alphaScheme_UFO.tar.gz	SMEFTsim_A_U35_MwScheme_UFO.tar.gz	SMEFT_alpha_FLU_UFO.zip	SMEFT_mW_FLU_UFO.zip

web: [SMEFT](#)

Standard Model Effective Field Theory – The SMEFTsim package

Authors

Ilaria Brivio, Yun Jiang and Michael Trott

ilaria.brivio@nbi.ku.dk, yunjiang@nbi.ku.dk, michael.trott@cern.ch

NBIA and Discovery Center, Niels Bohr Institute, University of Copenhagen

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Depends on choices of low energy symmetries. e.g. flavor

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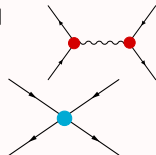
Focusing on **interference** $\mathcal{A}_{SM}\mathcal{A}_6^*$ (assume subdominant quadratic terms)

Selection due to SM kinematics / symmetries in the presence of:

- ▶ resonances in SM
- ▶ FCNCs op.
- ▶ dipole op. (interf. $\sim m_f$)
- ▶ ...

ψ^4 operators generally **suppressed** wrt. “pole operators” by

$$\left(\frac{\Gamma_B m_B}{v^2}\right)^n \sim \begin{array}{ll} 1/300 & (Z,W) \\ 1/10^6 & (h) \end{array}$$



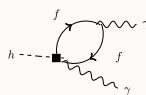
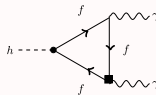
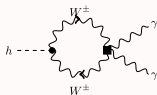
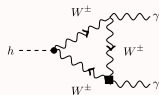
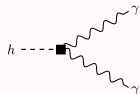
How many relevant parameters?

Depends on choices of low energy symmetries. e.g. flavor

observables

SMEFT accuracy

loop order



C_{HW}, C_{HB}, C_{HWB}

$+ C_W, C_{HD}, C_{eW},$
 $C_{eB}, C_{uW}, C_{uB}, C_{dW},$
 $C_{dB}, C_{eH}, C_{uH}, C_{dH}$

EFT
order

+ dimension 8 + ...

Hartmann, Trott 1505.02646, 1507.03568

Ghezzi, Gomez-Ambrosio, Passarino, Uccirati 1505.03706

Dedes, Paraskevas, Rosiek, Suxho, Trifyllis 1805.00302

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observables

SMEFT accuracy

resonant-dominated (**pole**)
observables @LO

	total $N_f = 3$	WZH pole obs.
general	2499	~ 46
MFV	~ 108	~ 30
$U(3)^5$	~ 70	~ 24

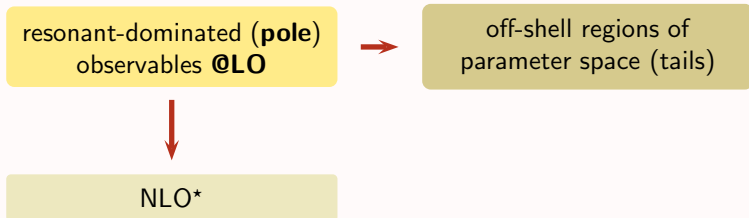
Brivio, Jiang, Trott 1709.06492

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SMEFT accuracy



*NLO QCD corrections can be significant!

EW + Higgs - mostly pole obs. → 23 parameters

Brivio,Hays,Smith,Trott,Žemaitytė in preparation

Z,W couplings

$$\begin{aligned}Q_{Hl}^{(1)} &= (iH^\dagger \overleftrightarrow{D}_\mu H)(\bar{l}\gamma^\mu l) \\Q_{He} &= (iH^\dagger \overleftrightarrow{D}_\mu H)(\bar{e}\gamma^\mu e) \\Q_{Hq}^{(1)} &= (iH^\dagger \overleftrightarrow{D}_\mu H)(\bar{q}\gamma^\mu q) \\Q_{Hq}^{(3)} &= (iH^\dagger \overleftrightarrow{D}_\mu^i H)(\bar{q}\sigma^i\gamma^\mu q) \\Q_{Hu} &= (iH^\dagger \overleftrightarrow{D}_\mu H)(\bar{u}\gamma^\mu u) \\Q_{Hd} &= (iH^\dagger \overleftrightarrow{D}_\mu H)(\bar{d}\gamma^\mu d)\end{aligned}$$

$$\begin{aligned}Q_{HD} &= (D_\mu H^\dagger H)(H^\dagger D^\mu H) \\Q_{HWB} &= (H^\dagger \sigma^i H)W_{\mu\nu}^i B^{\mu\nu} \\Q_{Hl}^{(3)} &= (iH^\dagger \overleftrightarrow{D}_\mu^i H)(\bar{l}\sigma^i\gamma^\mu l) \\Q'_{ll} &= (\bar{l}_p\gamma^\mu l_r)(\bar{l}_r\gamma^\mu l_p)\end{aligned}$$

input quantities

$$Q_W = \varepsilon_{ijk} W_\mu^{i\nu} W_\nu^{j\rho} W_\rho^{k\mu}$$

TGC

Bhabha scattering

$$\begin{aligned}Q_{ee} &= (\bar{e}\gamma^\mu e)(\bar{e}\gamma^\mu e) \\Q_{le} &= (\bar{l}\gamma^\mu l)(\bar{e}\gamma^\mu e) \\Q_{ll} &= (\bar{l}_p\gamma^\mu l_p)(\bar{l}_r\gamma^\mu l_r)\end{aligned}$$

$$\begin{aligned}Q_{Hbox} &= (H^\dagger H) \square (H^\dagger H) \\Q_{HG} &= (H^\dagger H)G_{\mu\nu}^a G^{a\mu\nu} \\Q_{HB} &= (H^\dagger H)B_{\mu\nu} B^{\mu\nu} \\Q_{HW} &= (H^\dagger H)W_{\mu\nu}^i W^{i\mu\nu} \\Q_{uH} &= (H^\dagger H)(\bar{q}\tilde{H}u) \\Q_{dH} &= (H^\dagger H)(\bar{q}\tilde{H}d) \\Q_{eH} &= (H^\dagger H)(\bar{l}He) \\Q_G &= \varepsilon_{abc} G_\mu^{a\nu} G_\nu^{b\rho} G_\rho^{c\mu} \\Q_{uG} &= (\bar{q}\sigma^{\mu\nu} T^a \tilde{H}u)G_{\mu\nu}^a\end{aligned}$$

H processes

Application: global fits

large number of global SMEFT fits in the literature,
with different observable and operator sets.

examples:

EW

Berthier, Trott 1508.05060

Berthier, Bjørn, Trott 1606.06693

Brivio, Trott 1701.06424

Higgs + EW

Butter, Éboli, Gonzalez-Fraile, Gonzalez-Garcia,
Plehn, Rauch 1604.03105

→ Anke's talk

Ellis, Murphy, Sanz, You 1803.03252

da Silva, Alves, Rosa, Éboli, Gonzalez-Garcia 1812.01009

Biekötter, Corbett, Plehn 1812.07587

Brivio, Hays, Smith, Trott, Žemaitytė in preparation

top sector

Hartland, Maltoni, Nocera, Rojo, Slade, Vryonidou, Zhang
1901.05965

→ Sebastian's talk

Brivio, Bruggisser, Maltoni, Moutafis, Plehn, Vryonidou,
Westhoff, Zerwas, Zhang in preparation

→ Rhea's talk

An important observable: the Higgs width

a crucial observable for the Higgs sector

SM: $\Gamma_H \simeq 4 \text{ MeV} \quad \rightarrow \quad \frac{\Gamma_H}{m_H} \simeq 3 \cdot 10^{-5} \ll 1$

$\Rightarrow$ Higgs measurements can be factored into

$$\sigma(i \rightarrow H) \times Br(H \rightarrow f)$$

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SMEFT: probe separately production and decay



$$Br(H \rightarrow f) = \frac{\Gamma(H \rightarrow f)}{\Gamma_H^{\text{tot}}}$$

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SMEFT: probe separately production and decay



$$Br_{\text{SMEFT}}(H \rightarrow f) = \left[\frac{\Gamma(H \rightarrow f)}{\Gamma_H^{\text{tot}}} \right]_{\text{SM}} \left[1 + \frac{\delta\Gamma(H \rightarrow f)}{\Gamma_{\text{SM}}(H \rightarrow f)} - \frac{\delta\Gamma_H^{\text{tot}}}{\Gamma_{H,\text{SM}}^{\text{tot}}} \right]$$

- ▶ both $\delta\Gamma(H \rightarrow f)$ and $\delta\Gamma_H^{\text{tot}}$ need to be determined
- ▶ $\delta\Gamma_H^{\text{tot}}$ enters all processes $\rightarrow$ **strong impact** on global SMEFT analyses!

The Higgs width in the SMEFT

Analytic calculation of the inclusive Γ_H :

Brivio, Corbett, Trott 1906.06949

- ▶ LO in the EFT: up to Λ^{-2} .
- ▶ **tree level.**
SM couplings $H\gamma\gamma, HZ\gamma, Hgg$ included for $H \rightarrow f\bar{f}\gamma / \gamma\gamma / gg$.
- ▶ Warsaw basis with **$U(3)^5$ flavor symmetry**
- ▶ EW input scheme: $\{m_Z, m_W, G_F\}$
- ▶ full calculation for $h \rightarrow 4f$: narrow width approximation for W, Z avoided

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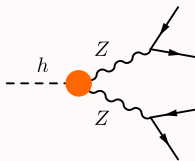
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Why analytic?

- ▶ control over different contributions
- ▶ easier to linearize in $\delta\Gamma_V, \delta m_V$
- ▶ more stable than MC for the massless fermions case with γ diagrams
- ▶ calculation can be **automated** once and for all
→ much faster than running MC every time

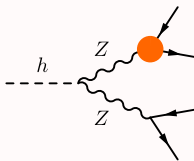
H $\rightarrow$ 4f in the SMEFT

① corrections to SM diagrams

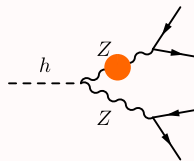


$$\propto g_{\mu\nu} \text{ (SM-like)}$$

$$\propto g_{\mu\nu} p \cdot q - p_\nu q_\mu$$



$$\delta g_L, \delta g_R$$



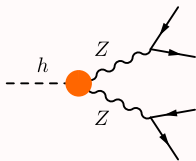
$$\frac{-im_Z \delta \Gamma_Z + (2m_Z - i\Gamma_Z) \delta m_Z}{p^2 - m_Z^2 + i\Gamma_Z m_Z}$$



hard to extract from
MC simulation!
full treatment requires
analytic calculation

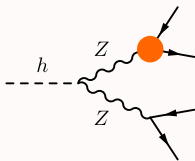
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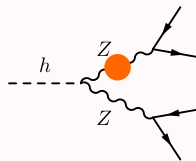


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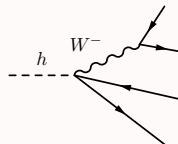
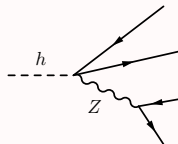
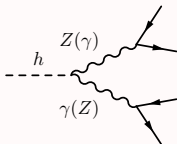
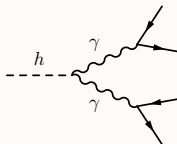


$$\delta g_L, \delta g_R$$



$$\frac{-im_Z \delta \Gamma_Z + (2m_Z - i\Gamma_Z) \delta m_Z}{p^2 - m_Z^2 + i\Gamma_Z m_Z}$$

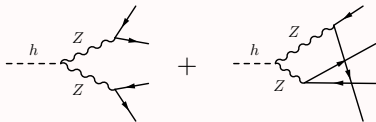
② genuine SMEFT diagrams



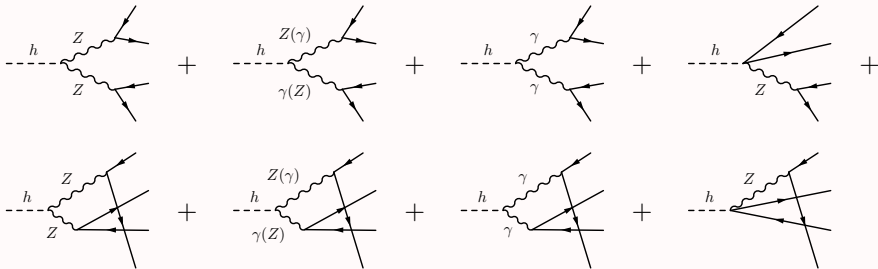
H $\rightarrow$ 4f in the SMEFT - complexity

$$h \rightarrow e^+ e^- e^+ e^-$$

SM



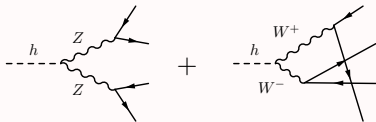
interfering with



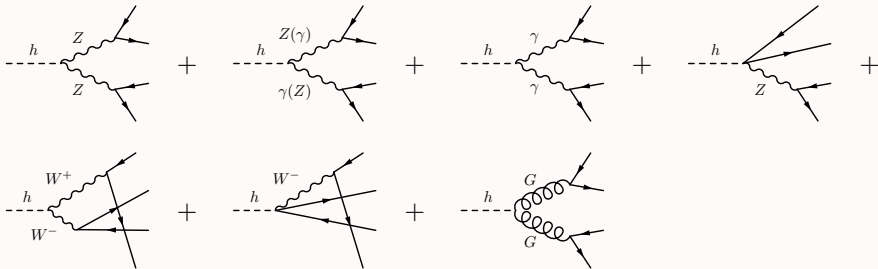
H $\rightarrow$ 4f in the SMEFT - complexity

$$h \rightarrow \bar{u} u \bar{d} d$$

SM



interfering with



H $\rightarrow$ 4f - results

Example: $H \rightarrow e^+ e^- \mu^+ \mu^-$ $m_i, m_j, m_k, m_l = 0$

$$\frac{\delta\Gamma(H \rightarrow e^+ e^- \mu^+ \mu^-)}{\Gamma_{\text{SM}}(H \rightarrow e^+ e^- \mu^+ \mu^-)} = \sum_i a_i \bar{C}_i = \sum_i a_i \left(C_i \frac{v^2}{\Lambda^2} \right)$$

	$\bar{C}_{HW}$	$\bar{C}_{HB}$	$\bar{C}_{HWB}$	$\bar{C}_{H\Box}$	$\bar{C}_{HD}$	$\bar{C}_{Hl}^{(1)}$	$\bar{C}_{Hl}^{(3)}$	$\bar{C}_{He}$	$\bar{C}_{Hq}^{(1)}$	$\bar{C}_{Hq}^{(3)}$	$\bar{C}_{Hu}$	$\bar{C}_{Hd}$	$\bar{C}'_{ll}$
Z	-0.78	-0.22	0.30	2	0.17	4.38	-1.62	-3.52					3.
A	1.04	-1.08	-0.68										
E						-2.23	-2.23	1.80					
Γ			-0.38		0.06	0.15	1.14	0.15	-0.39	-1.34	-0.20	0.15	-0.83
tot	0.26	-1.30	-0.76	2.	0.23	2.30	-2.71	-1.58	-0.39	-1.34	-0.20	0.15	2.17

Z	corrections to SM diagram
A	γ diagrams
E	contact diagrams ($HZee$)
Γ	$\delta\Gamma_Z^{\text{tot}}/\Gamma_{Z,SM}$ on + off-shell Z

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Impact of photon diagrams

☞ main contribution missed in the narrow width approx.

turns out to be a $\mathcal{O}(1 - 250)\%$ effect!

	with γ			without γ		
	$\bar{C}_{HW}$	$\bar{C}_{HB}$	$\bar{C}_{HWB}$	$\bar{C}_{HW}$	$\bar{C}_{HB}$	$\bar{C}_{HWB}$
$h \rightarrow e^+ e^- \mu^+ \mu^-$	0.26	-1.30	-0.38	-0.77	-0.22	0.30
$h \rightarrow \bar{u} u \bar{c} c$	1.45	-2.63	-0.29	-0.77	-0.22	1.33
$h \rightarrow e^+ e^- \bar{d} d$	0.50	-1.55	-0.37	-0.77	-0.22	0.47
$h \rightarrow e^+ e^- e^+ e^-$	0.02	-2.28	0.27	-0.76	-0.21	0.44
$h \rightarrow \bar{u} u \bar{u} u$	1.39	-2.72	-0.14	-0.76	-0.21	1.19
$h \rightarrow e^+ e^- \bar{\nu}_e \nu_e$	-1.49	0.01	-0.06	-1.48	-0.007	-0.07

The total Higgs width in the SMEFT

putting together all the main contributions* we obtain

$$\Gamma_H^{\text{tot}} = \Gamma_{H,SM}^{\text{tot}} \left[1 + \frac{\delta\Gamma_H^{\text{tot}}}{\Gamma_{H,SM}^{\text{tot}}} \right]$$

$$\Gamma_{H,SM}^{\text{tot}} = 4.100 \text{ MeV}$$

$$\begin{aligned} \frac{\delta\Gamma_H^{\text{tot}}}{\Gamma_{H,SM}^{\text{tot}}} = & -1.50 \tilde{C}_{HB} - 1.21 \tilde{C}_{HW} + 1.21 \tilde{C}_{HWB} + 50.6 \tilde{C}_{HG} \\ & + 1.83 \tilde{C}_{H\Box} - 0.43 \tilde{C}_{HD} + 1.17 \tilde{C}'_{II} \\ & - 7.85 Y_c \text{Re} \tilde{C}_{uH} - 48.5 Y_b \text{Re} \tilde{C}_{dH} - 12.3 Y_\tau \text{Re} \tilde{C}_{eH} \\ & + 0.002 \tilde{C}_{Hq}^{(1)} + 0.06 \tilde{C}_{Hq}^{(3)} + 0.001 \tilde{C}_{Hu} - 0.0007 \tilde{C}_{Hd} \\ & - 0.0009 \tilde{C}_{Hl}^{(1)} - 2.32 \tilde{C}_{Hl}^{(3)} - 0.0006 \tilde{C}_{He}, \end{aligned}$$

* $gg + \gamma\gamma + \bar{b}b + \bar{c}c + \tau^+\tau^- + 4f + \bar{f}f\gamma$

- ▶ The **SMEFT** is a well-defined, general framework for BSM searches

Summary & take-home

- ▶ The **SMEFT** is a well-defined, general framework for BSM searches
- ▶ It is worth using its full power with a truly global analysis
 - ▶ most general BSM characterization (assuming SM sym + fields)
 - ▶ universal parameterization for data interpretation

Summary & take-home

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 - ▶ universal parameterization for data interpretation
- ▶ SMEFTsim is a powerful tool specifically designed for this purpose @LO

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- ▶ The **SMEFT** is a well-defined, general framework for BSM searches
- ▶ It is worth using its full power with a truly global analysis
 - ▶ most general BSM characterization (assuming SM sym + fields)
 - ▶ universal parameterization for data interpretation
- ▶ SMEFTsim is a powerful tool specifically designed for this purpose @LO
- ▶ the Higgs inclusive width has been computed at LO in the SMEFT, including relevant, previously neglected contributions

Backup slides

Shifts from input parameters

SM case.

Parameters in the canonically normalized Lagrangian : $\bar{v}, \bar{g}_1, \bar{g}_2, s_{\bar{\theta}}$

The values can be inferred from the measurements e.g. of $\{\alpha_{\text{em}}, m_Z, G_f\}$:

$$\begin{aligned}\alpha_{\text{em}} &= \frac{\bar{g}_1 \bar{g}_2}{\bar{g}_1^2 + \bar{g}_2^2} \\ m_Z &= \frac{\bar{g}_2 \bar{v}}{2c_{\bar{\theta}}} \\ G_f &= \frac{1}{\sqrt{2}\bar{v}^2}\end{aligned} \quad \rightarrow \quad \begin{aligned}\hat{v}^2 &= \frac{1}{\sqrt{2}G_f} \\ \sin \hat{\theta}^2 &= \frac{1}{2} \left(1 - \sqrt{1 - \frac{4\pi\alpha_{\text{em}}}{\sqrt{2}G_f m_Z^2}} \right) \\ \hat{g}_1 &= \frac{\sqrt{4\pi\alpha_{\text{em}}}}{\cos \hat{\theta}} \\ \hat{g}_2 &= \frac{\sqrt{4\pi\alpha_{\text{em}}}}{\sin \hat{\theta}}\end{aligned}$$

in the SM at tree-level $\bar{\kappa} = \hat{\kappa}$

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$$\begin{aligned}\alpha_{\text{em}} &= \frac{\bar{g}_1 \bar{g}_2}{\bar{g}_1^2 + \bar{g}_2^2} \left[1 + \bar{v}^2 C_{HWB} \frac{\bar{g}_2^3 / \bar{g}_1}{\bar{g}_1^2 + \bar{g}_2^2} \right] & \hat{v}^2 &= \frac{1}{\sqrt{2} G_f} \\ m_Z &= \frac{\bar{g}_2 \bar{v}}{2 c_{\bar{\theta}}} + \delta m_Z(C_i) & \sin \hat{\theta}^2 &= \frac{1}{2} \left(1 - \sqrt{1 - \frac{4\pi\alpha_{\text{em}}}{\sqrt{2} G_f m_Z^2}} \right) \\ G_f &= \frac{1}{\sqrt{2} \bar{v}^2} + \delta G_f(C_i) & \hat{g}_1 &= \frac{\sqrt{4\pi\alpha_{\text{em}}}}{\cos \hat{\theta}} \\ & & \hat{g}_2 &= \frac{\sqrt{4\pi\alpha_{\text{em}}}}{\sin \hat{\theta}}\end{aligned}$$

in the SM at tree-level $\bar{\kappa} = \hat{\kappa}$

in the SMEFT $\bar{\kappa} = \hat{\kappa} + \delta\kappa(C_i)$

Shifts from input parameters

To have numerical predictions it is necessary to replace $\bar{\kappa} \rightarrow \hat{\kappa} + \delta\kappa(C_i)$ for all the parameters in the Lagrangian.

$\{\alpha_{\text{em}}, m_Z, G_f\}$ scheme

$$\delta m_Z^2 = m_Z^2 \hat{v}^2 \left(\frac{c_{HD}}{2} + 2c_{\hat{\theta}} s_{\hat{\theta}} c_{HWP} \right)$$

$$\delta G_f = \frac{\hat{v}^2}{\sqrt{2}} \left((c_{HI}^{(3)})_{11} + (c_{HI}^{(3)})_{22} - (c_{II})_{1221} \right)$$

$$\delta g_1 = \frac{s_{\hat{\theta}}^2}{2(1-2s_{\hat{\theta}}^2)} \left(\sqrt{2}\delta G_f + \delta m_Z^2/m_Z^2 + 2\frac{c_{\hat{\theta}}^3}{s_{\hat{\theta}}} c_{HWP} \hat{v}^2 \right)$$

$$\delta g_2 = -\frac{c_{\hat{\theta}}^2}{2(1-2s_{\hat{\theta}}^2)} \left(\sqrt{2}\delta G_f + \delta m_Z^2/m_Z^2 + 2\frac{s_{\hat{\theta}}^3}{c_{\hat{\theta}}} c_{HWP} \hat{v}^2 \right)$$

$$\delta s_{\hat{\theta}}^2 = 2c_{\hat{\theta}}^2 s_{\hat{\theta}}^2 (\delta g_1 - \delta g_2) + c_{\hat{\theta}} s_{\hat{\theta}} (1 - 2s_{\hat{\theta}}^2) c_{HWP} \hat{v}^2$$

$$\delta m_h^2 = m_h^2 \hat{v}^2 \left(2c_{H\Box} - \frac{c_{HD}}{2} - \frac{3c_H}{2\lambda m} \right)$$

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$$\delta g_1 = -\frac{1}{2} \left(\sqrt{2} \delta G_f + \frac{1}{s_{\hat{\theta}}^2} \frac{\delta m_Z^2}{m_Z^2} \right)$$

$$\delta g_2 = -\frac{1}{\sqrt{2}} \delta G_f$$

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Implemented frameworks

We implemented 6 different frameworks:

$$3 \text{ flavor structures} \left\{ \begin{array}{l} \text{general} \\ U(3)^5 \text{ symmetric} \\ \text{linear MFV} \end{array} \right. \times 2 \text{ input schemes} \left\{ \begin{array}{l} \hat{\alpha}_{\text{em}}, \hat{m}_Z, \hat{G}_f \\ \hat{m}_W, \hat{m}_Z, \hat{G}_f \end{array} \right.$$

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completely general flavor indices:

2499 parameters including all complex phases

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assume an **exact flavor symmetry**

$$U(3)^5 = U(3)_q \times U(3)_u \times U(3)_d \times U(3)_l \times U(3)_e$$

under which: $\psi \mapsto U_\psi \psi$ for $\psi = \{u, d, q, l, e\}$

► The Yukawas are the only **spurions** breaking the symmetry:

$$Y_u \mapsto U_u Y_u U_q^\dagger \quad Y_d \mapsto U_d Y_d U_q^\dagger \quad Y_l \mapsto U_e Y_l U_l^\dagger.$$

► flavor indices contractions are fixed by the symmetry $\rightarrow$ less parameters

Examples:

$$\mathcal{Q}_{Hu} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{u}_r \gamma^\mu u_s) \delta_{rs}$$

$$\mathcal{Q}_{eB} = B_{\mu\nu} (\bar{l}_r H \sigma^{\mu\nu} e_s) (\mathbf{Y}_l)_{rs}$$

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$$3 \text{ flavor structures} \left\{ \begin{array}{l} \text{general} \\ U(3)^5 \text{ symmetric} \\ \text{linear MFV} \end{array} \right. \times 2 \text{ input schemes} \left\{ \begin{array}{l} \hat{\alpha}_{\text{em}}, \hat{m}_Z, \hat{G}_f \\ \hat{m}_W, \hat{m}_Z, \hat{G}_f \end{array} \right.$$

assume $U(3)^5$ symmetry + CKM only source of ~~CP~~

- ▶ all Wilson coefficients $\in \mathbb{R}$
- ▶ CP odd bosonic operators are absent ($\propto J_{CP} \simeq 10^{-5}$)
- ▶ includes the first order in flavor violation expansion. E.g.:

$$\mathcal{Q}_{Hu} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}_r \gamma^\mu u_s) \left[\mathbb{1} + (\mathbf{Y}_u \mathbf{Y}_u^\dagger) \right]_{rs}$$

$$\mathcal{Q}_{Hq}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{q}_r \gamma^\mu q_s) \left[\mathbb{1} + (\mathbf{Y}_u^\dagger \mathbf{Y}_u) + (\mathbf{Y}_d^\dagger \mathbf{Y}_d) \right]_{rs}$$

$$\begin{aligned} \hookrightarrow & \bar{u}_L \gamma^\mu \left[\mathbb{1} + Y_u^\dagger Y_u + V_{\text{CKM}} Y_d^\dagger Y_d V_{\text{CKM}}^\dagger \right] u_L \\ & + \bar{d}_L \gamma^\mu \left[\mathbb{1} + V_{\text{CKM}}^\dagger Y_u^\dagger Y_u V_{\text{CKM}} + Y_d^\dagger Y_d \right] d_L \end{aligned}$$