

Top EFT

Sebastian Bruggisser

Based on work with:

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T. Plehn, E. Vryonidou, S. Westhoff, C. Zhan

ELERY



MAN AT WORK



Why the Top-sector?

- Couples the strongest to the Higgs → Top-sector influences Higgs-sector and vice-versa.
- The LHC is a top-factory → wealth of data to be explored.
- Many BSM models modify the Top-sector: Light Top partners in SUSY/Composite Higgs, etc.

Why now?

- Existing top-fits:
 - TopFitter collaboration: 1512.03360, 1612.02294, 1901.03164
 - SMEFiT collaboration: 1901.05965
- What we can do:
 - Including ATLAS and CMS 13 TeV differential measurements
 - Studying the impact of NLO predictions
 - Detailed study of degeneracies
 - More honest treatment of theoretical uncertainties
 - Systematic study of the impact of correlated uncertainties (see Rhea's talk)

The Operators

$$\mathcal{L}_{EFT} = \mathcal{L}_{SM} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i^{d=6} + \sum_j \frac{c_j}{\Lambda^4} \mathcal{O}_j^{d=8} + \dots$$

The Operators

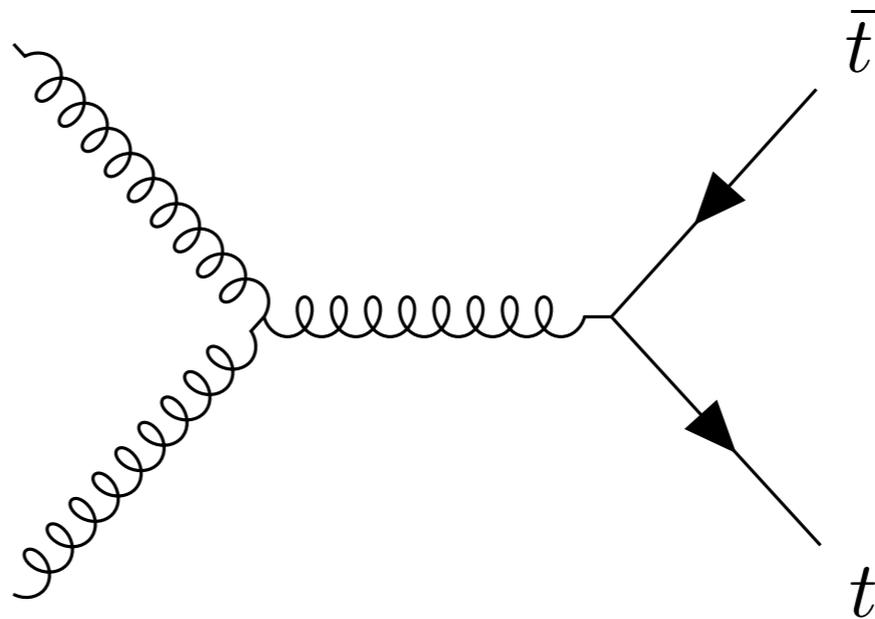
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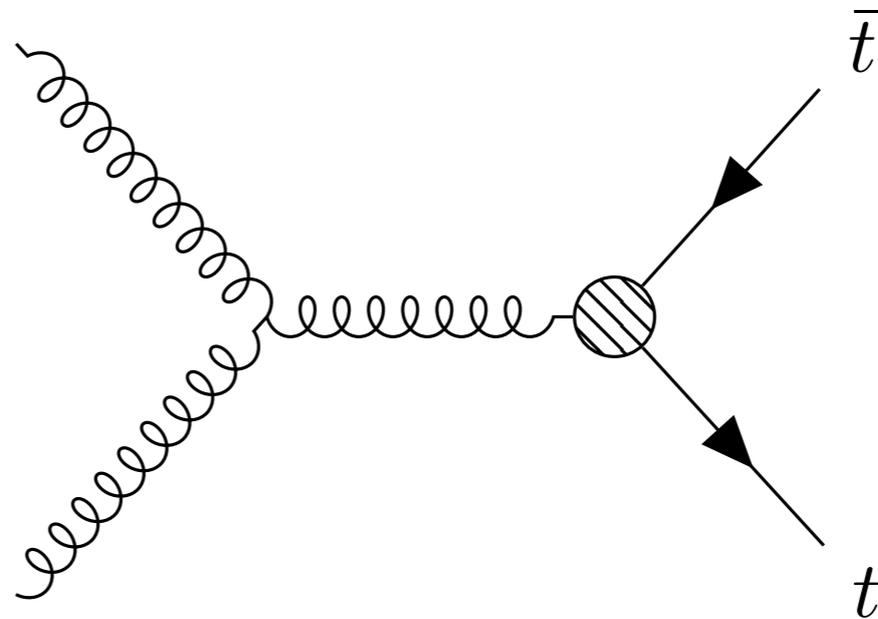
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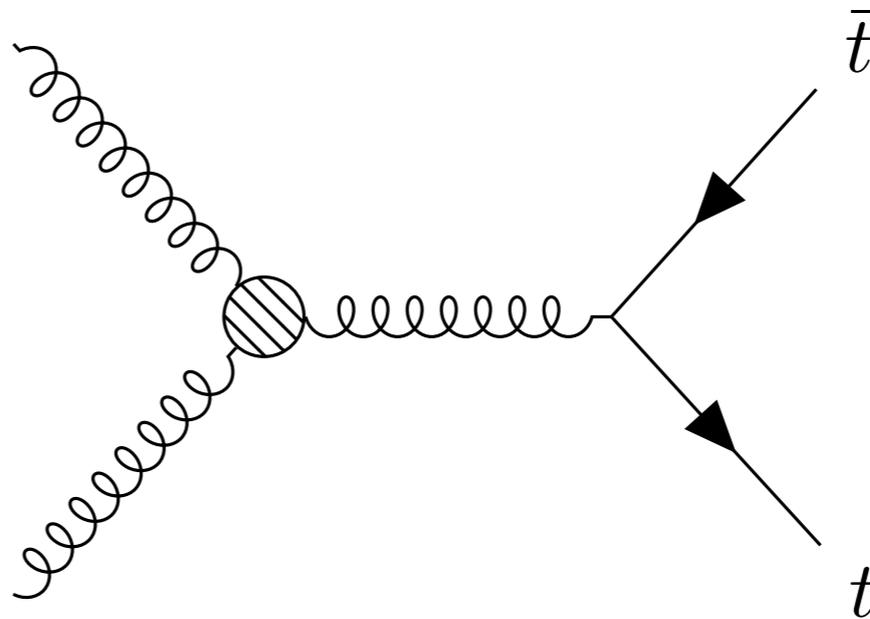
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- All relevant (including at least one Top) operators up to d=6
- Assumptions:
 - $U(2)_u \times U(2)_d \times U(2)_Q$ flavour symmetry
 - MFV
 - Light quarks considered massless (Yukawa=0)
 - Diagonal CKM
 - CP conserving

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- Warsaw-basis operators or linear combinations thereof
- Total of 34 operators considered

The Operators

4 heavy fermions

2 heavy - 2 light fermions

2 heavy fermions - boson

Processes Examples

The Operators

For full list see 1802.07237

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$$C_{qu}^{8(3333)} (\bar{q}_3 \gamma^\mu T^A q_3) (\bar{u}_3 \gamma_\mu T^A u_3)$$

Processes Examples

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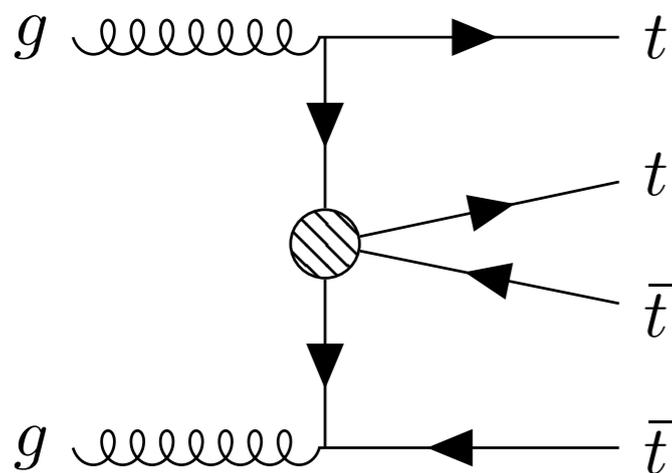
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Examples

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Processes

$t\bar{t}t\bar{t}$



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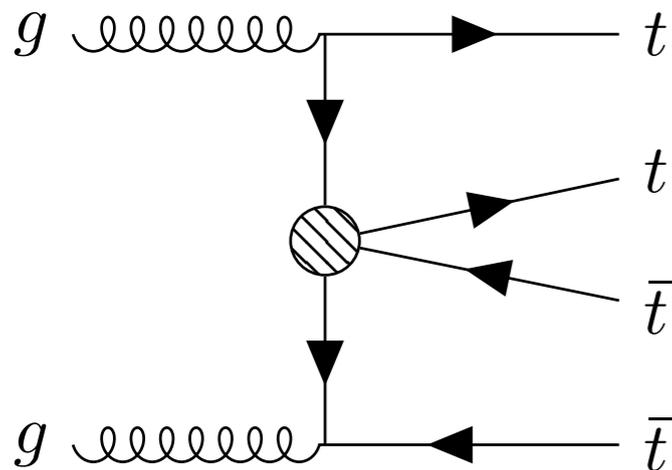
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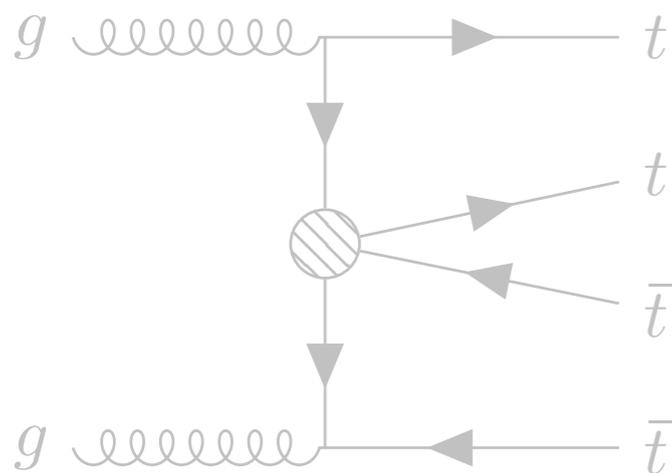
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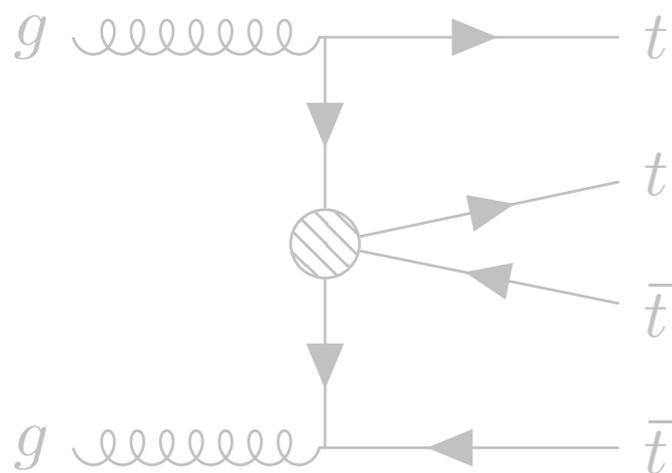
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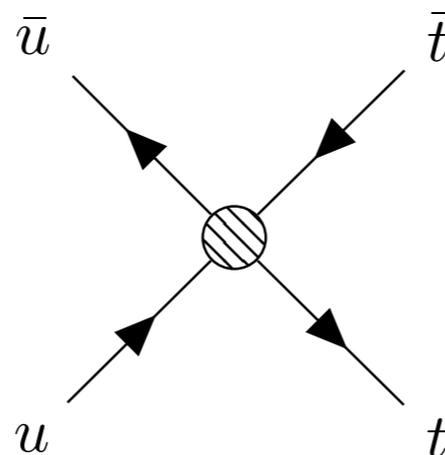
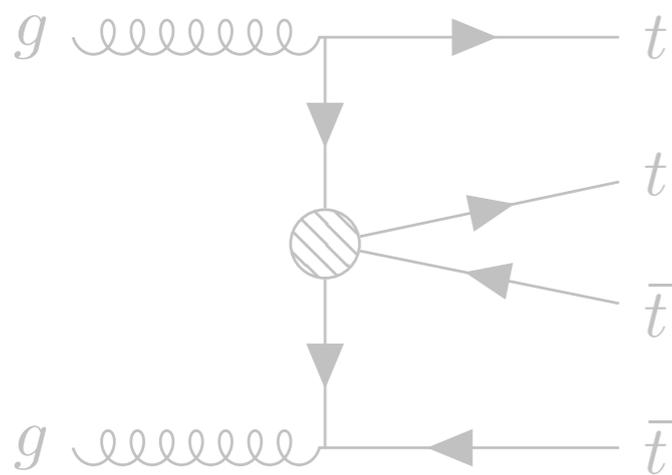
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$t\bar{t}$ production



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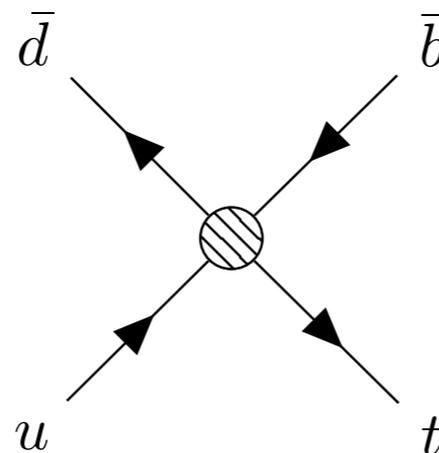
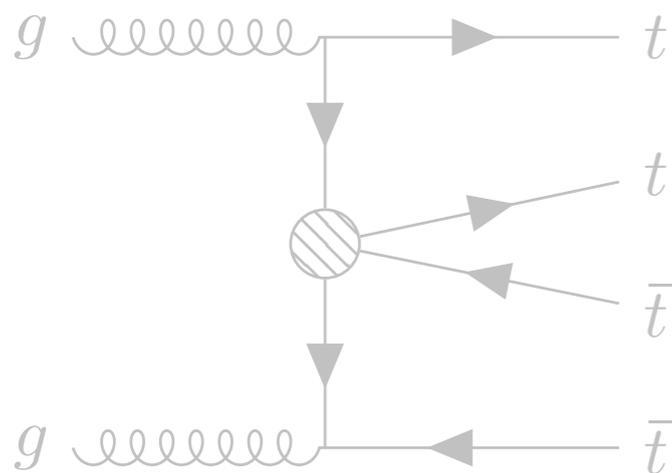
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single t production



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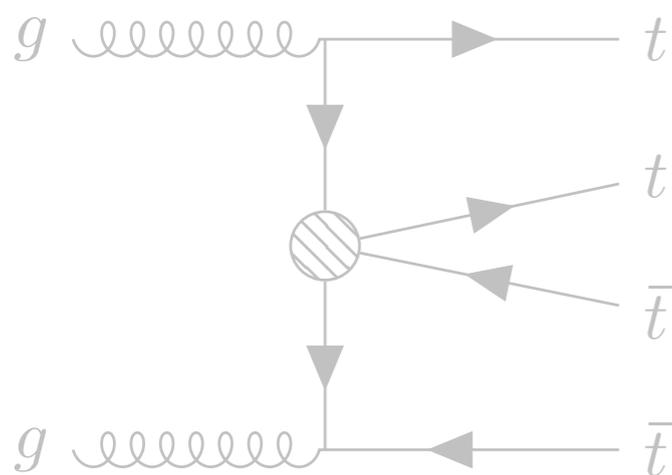
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single t production

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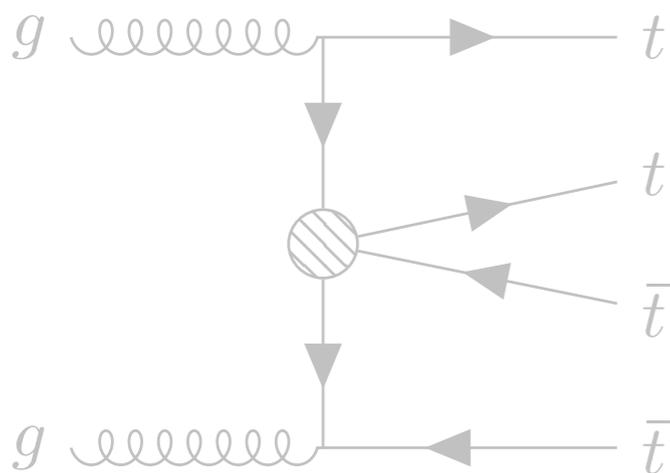
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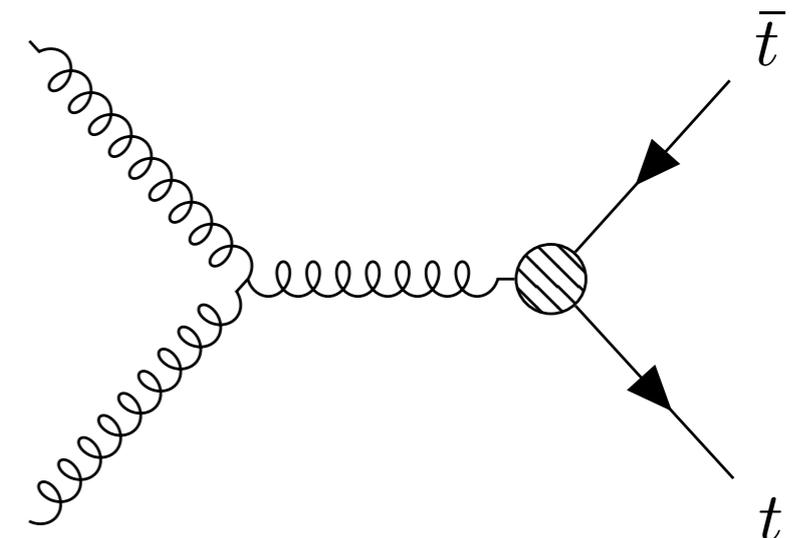
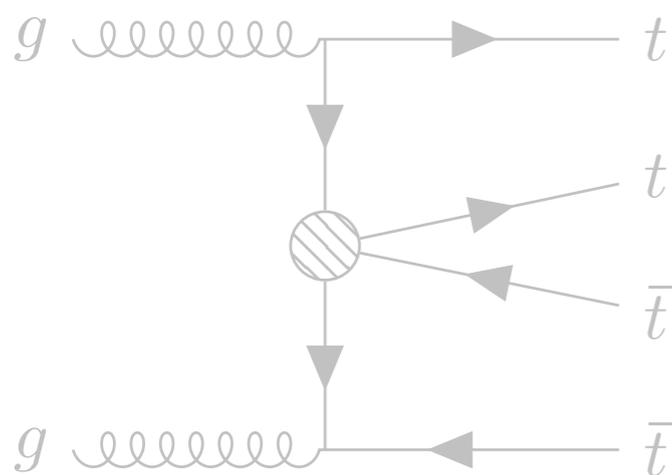
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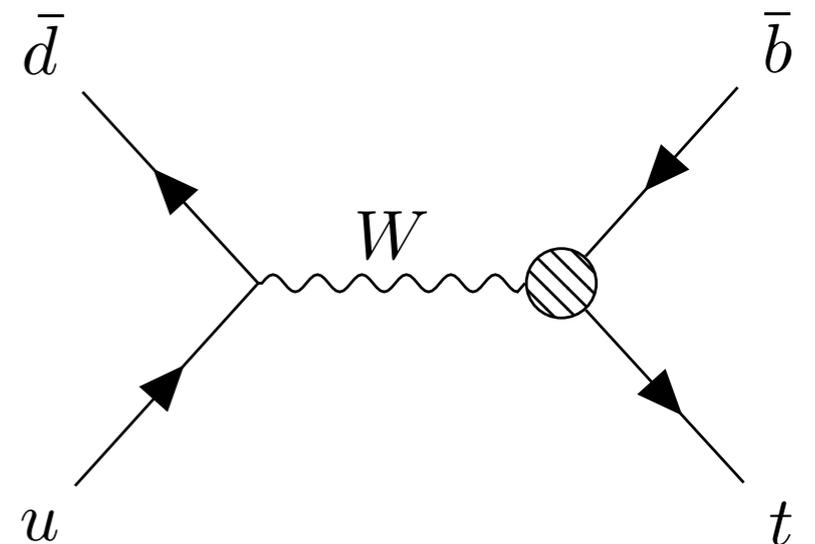
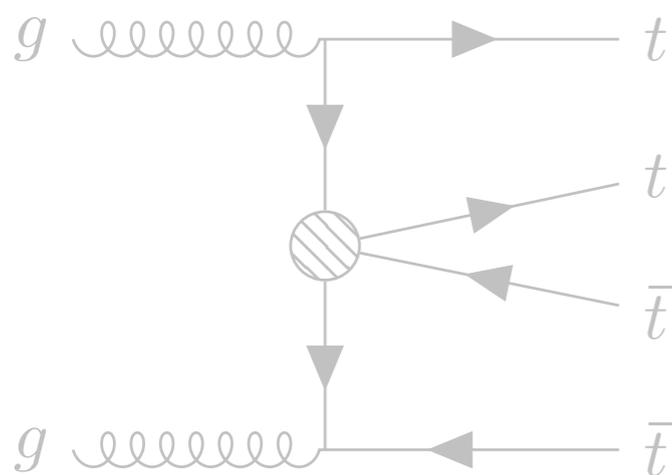
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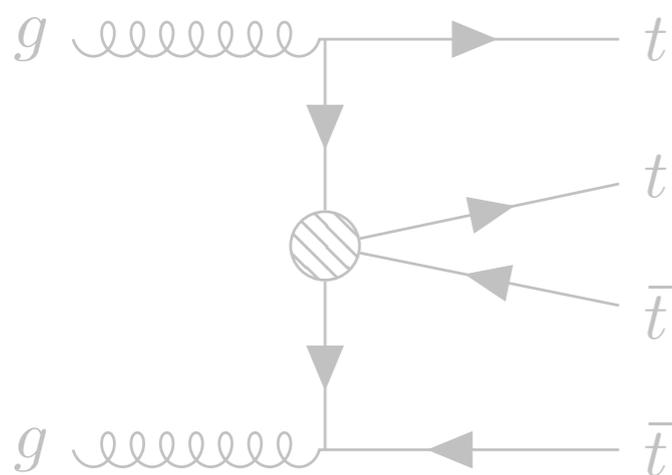
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See Rhea's Talk

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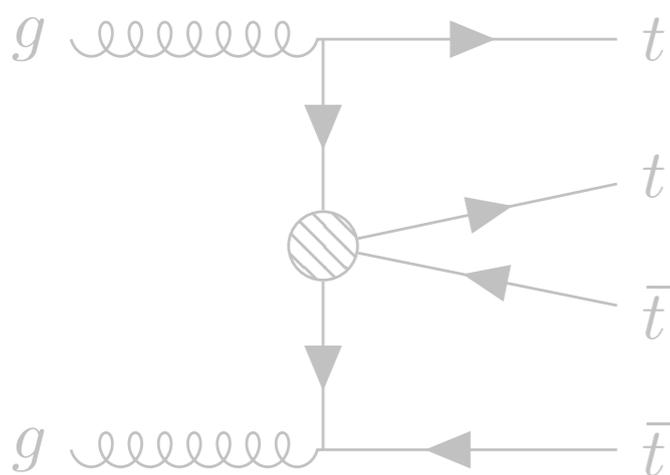
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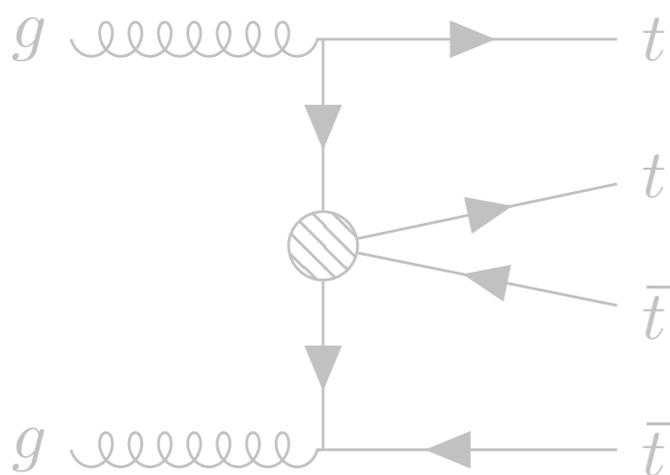
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(Global-) Fitting strategy

Prediction $\sigma_{EFT} = \sigma_{SM} + \sum_{d.o.f.} \sigma_i \frac{c_i}{\Lambda^2} + \sum_{d.o.f.} \sigma_{ij} \frac{c_i c_j}{\Lambda^4} \pm \delta_{th}$

Measurements

(Global-) Fitting strategy

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Measurements

8TeV, ATLAS and CMS
~5-7% precision

See: 1603.02303
1712.06857
1701.06228
1812.10505
1606.02699

Total rates

13TeV, ATLAS and CMS
~5-8% precision

(Global-) Fitting strategy

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Measurements

Differential Measurements

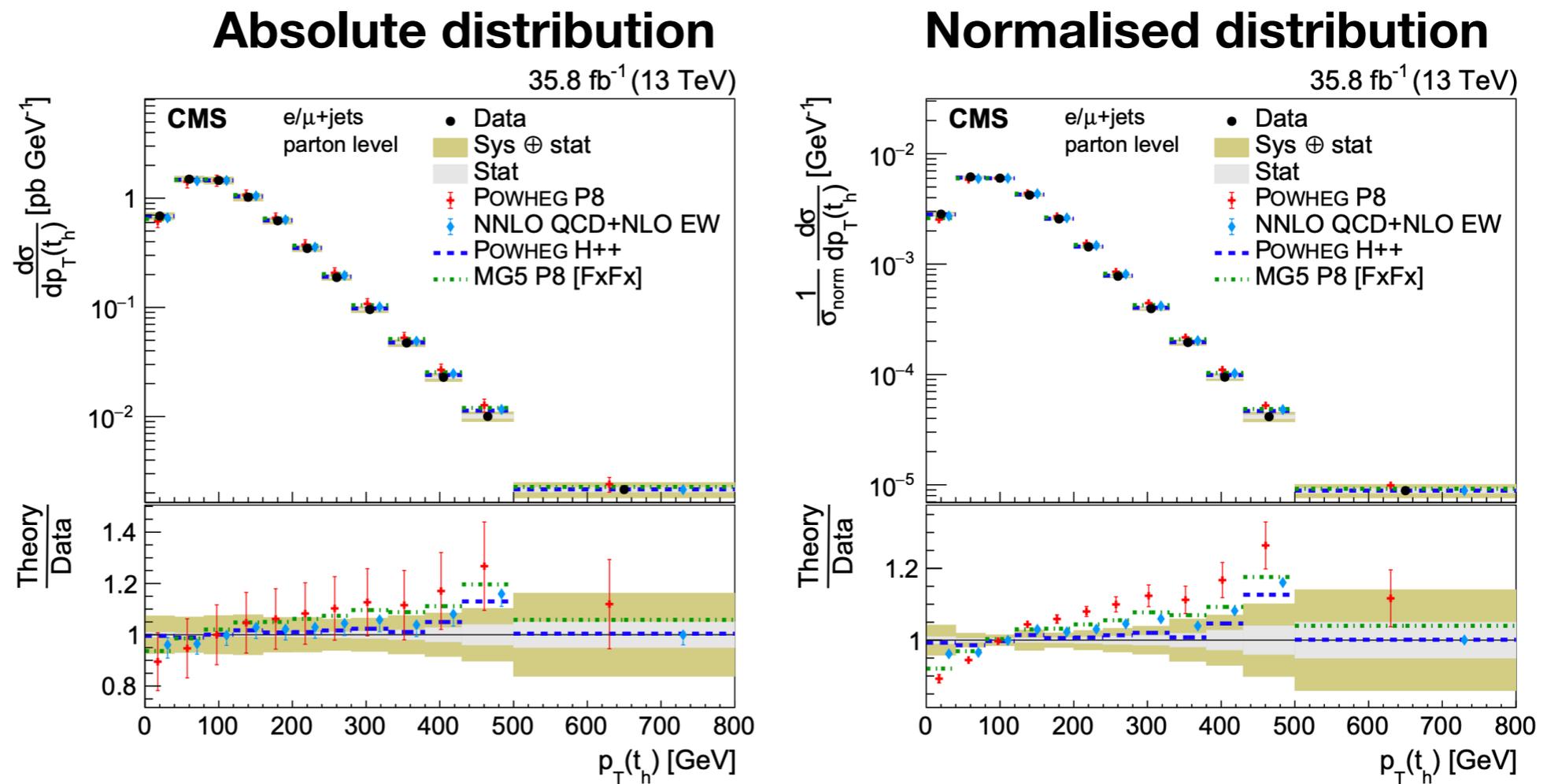


Figure from 1803.08856

SFitter

Toy MC method:

$$\sigma_{toy} = \sigma_{meas} \pm \delta_{th} \pm \delta_{exp}$$

SFitter

Toy MC method:

$$\sigma_{toy} = \sigma_{meas} \pm \delta_{th} \pm \delta_{exp}$$

Uniform



SFitter

Toy MC method:

$$\sigma_{toy} = \sigma_{meas} \pm \delta_{th} \pm \delta_{exp}$$

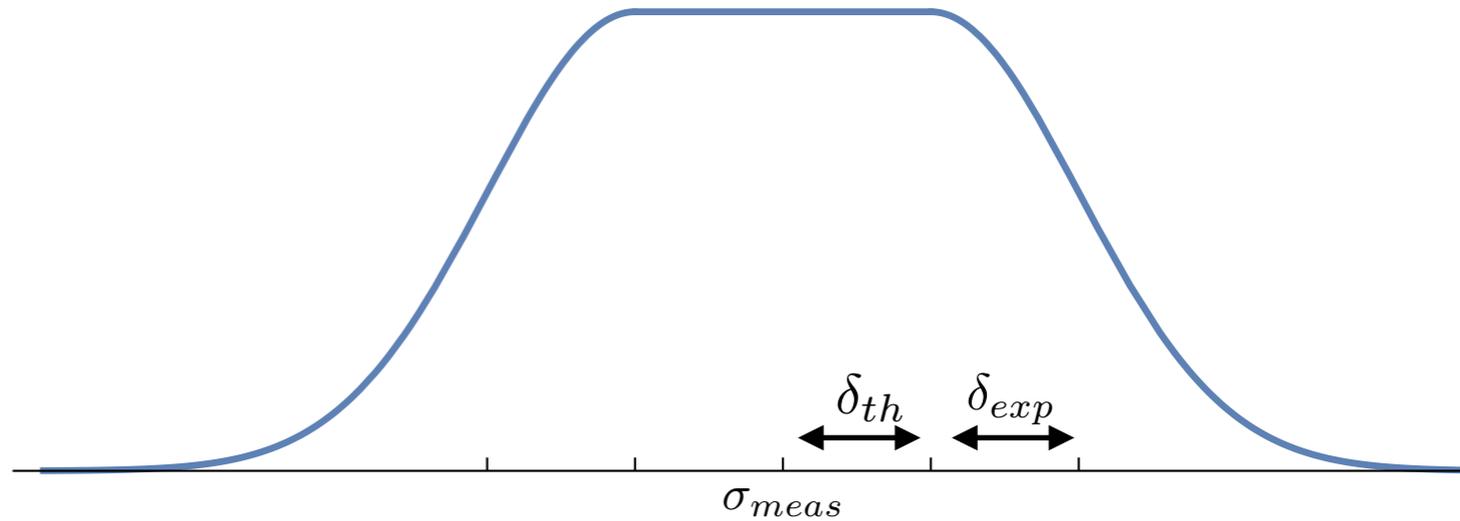
Uniform  
Gauss
(un)correlated

SFitter

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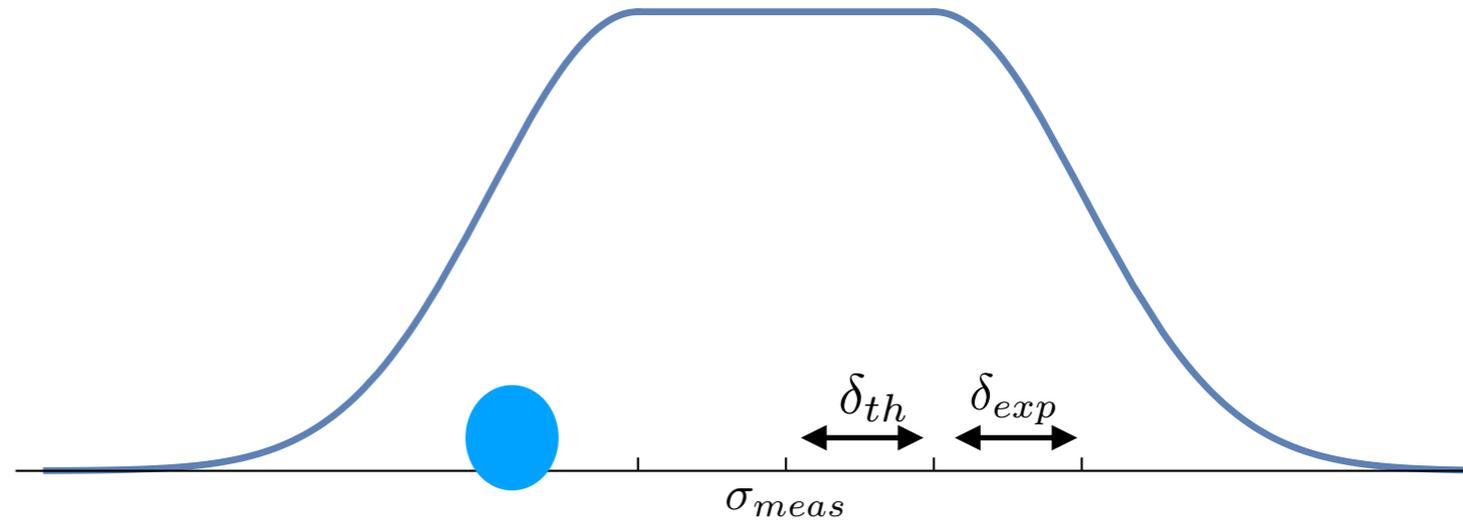


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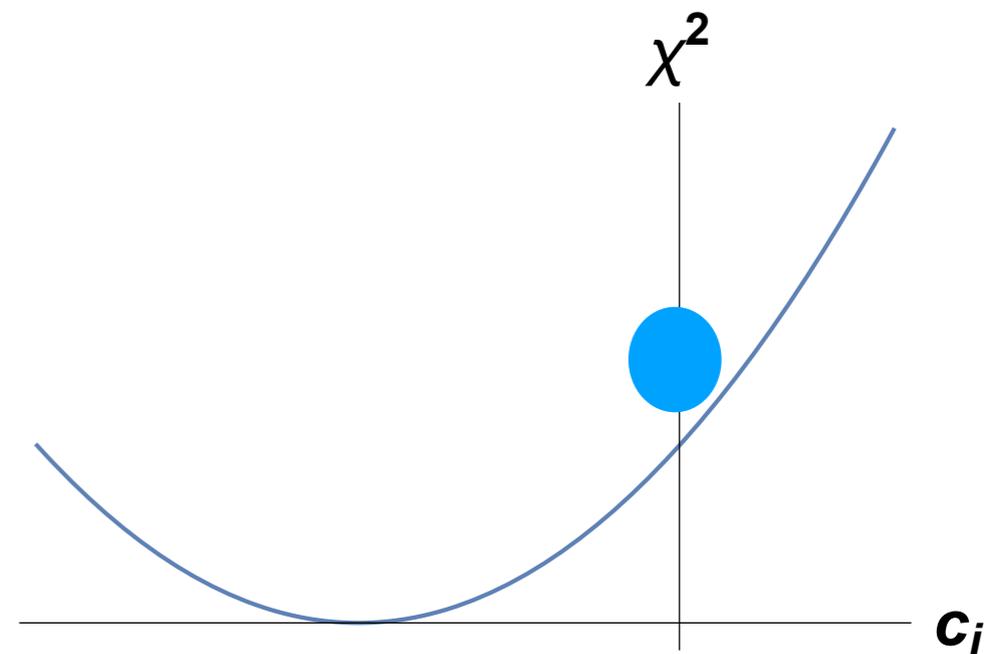
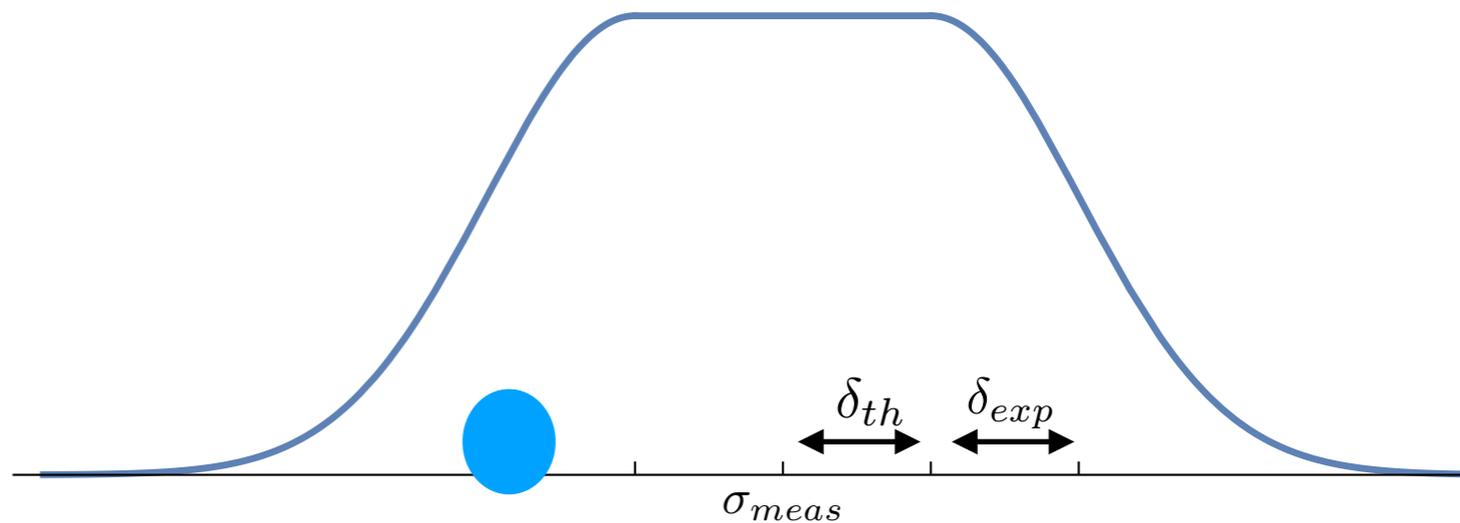


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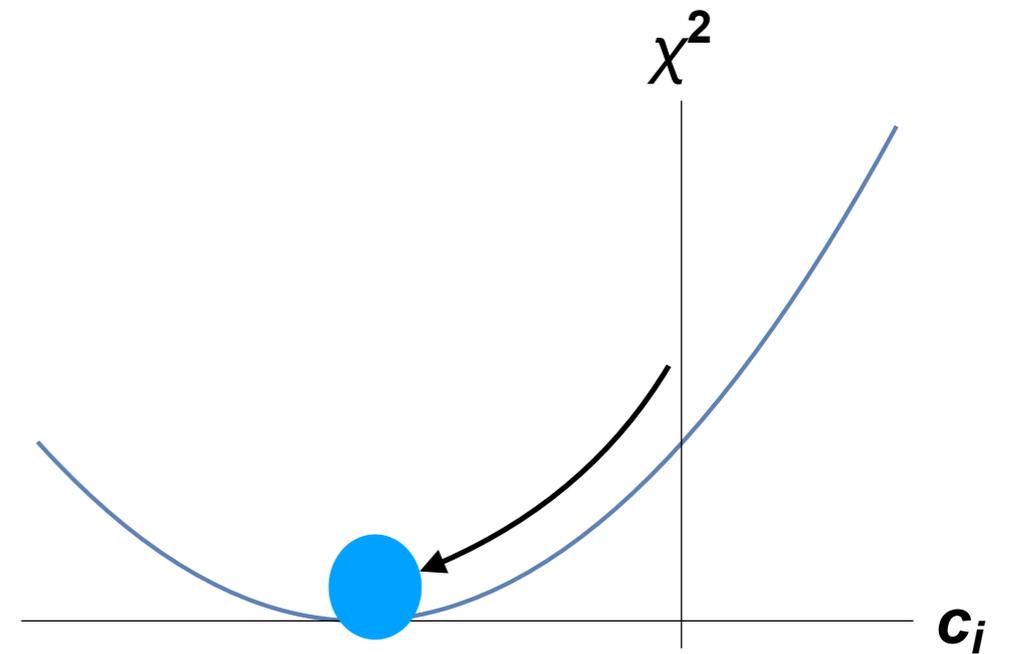
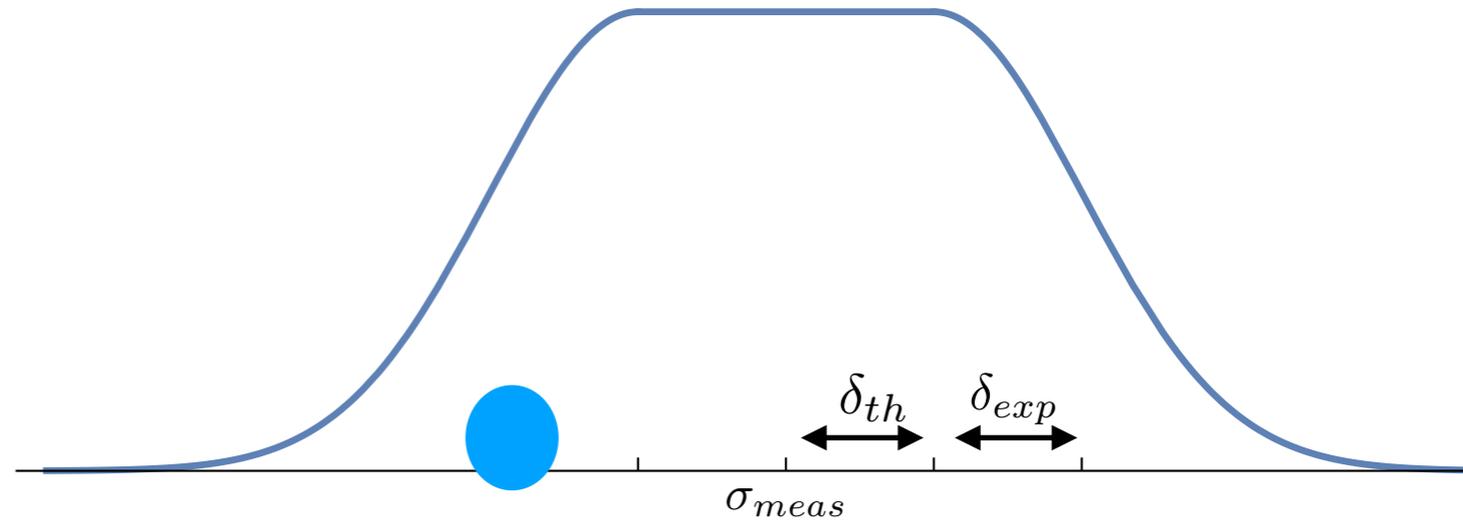


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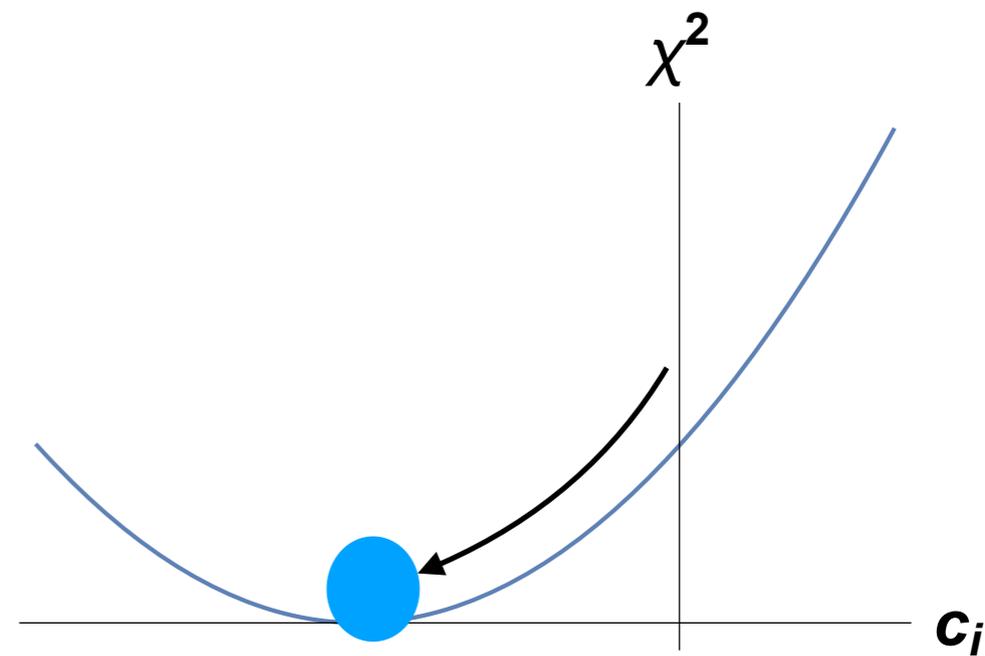
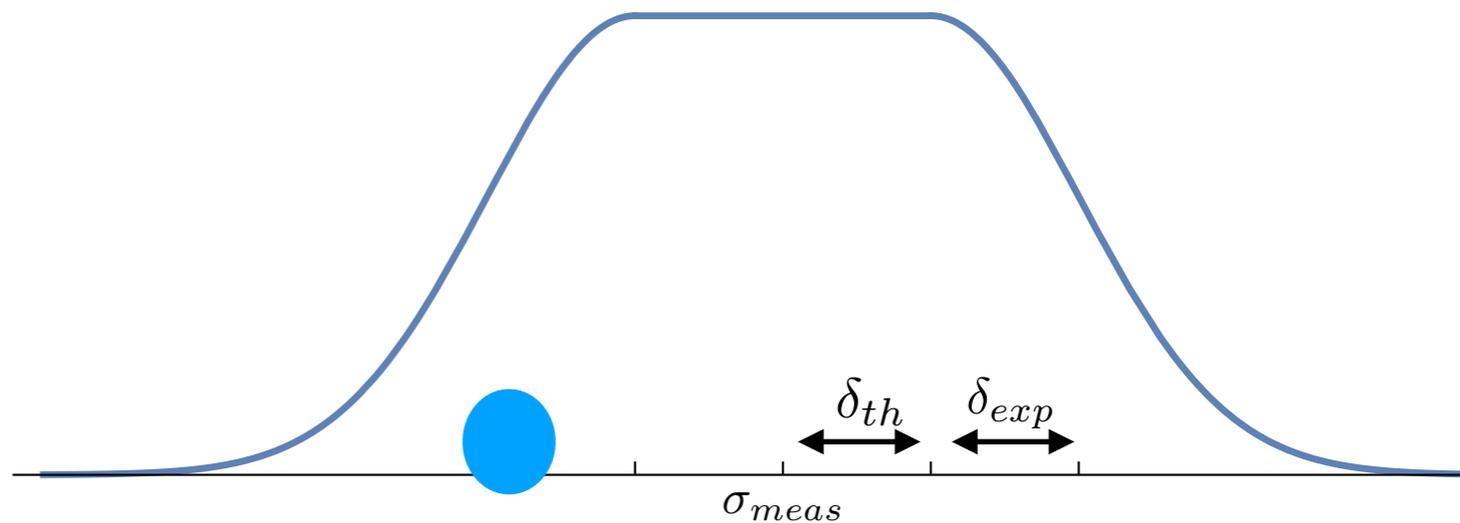
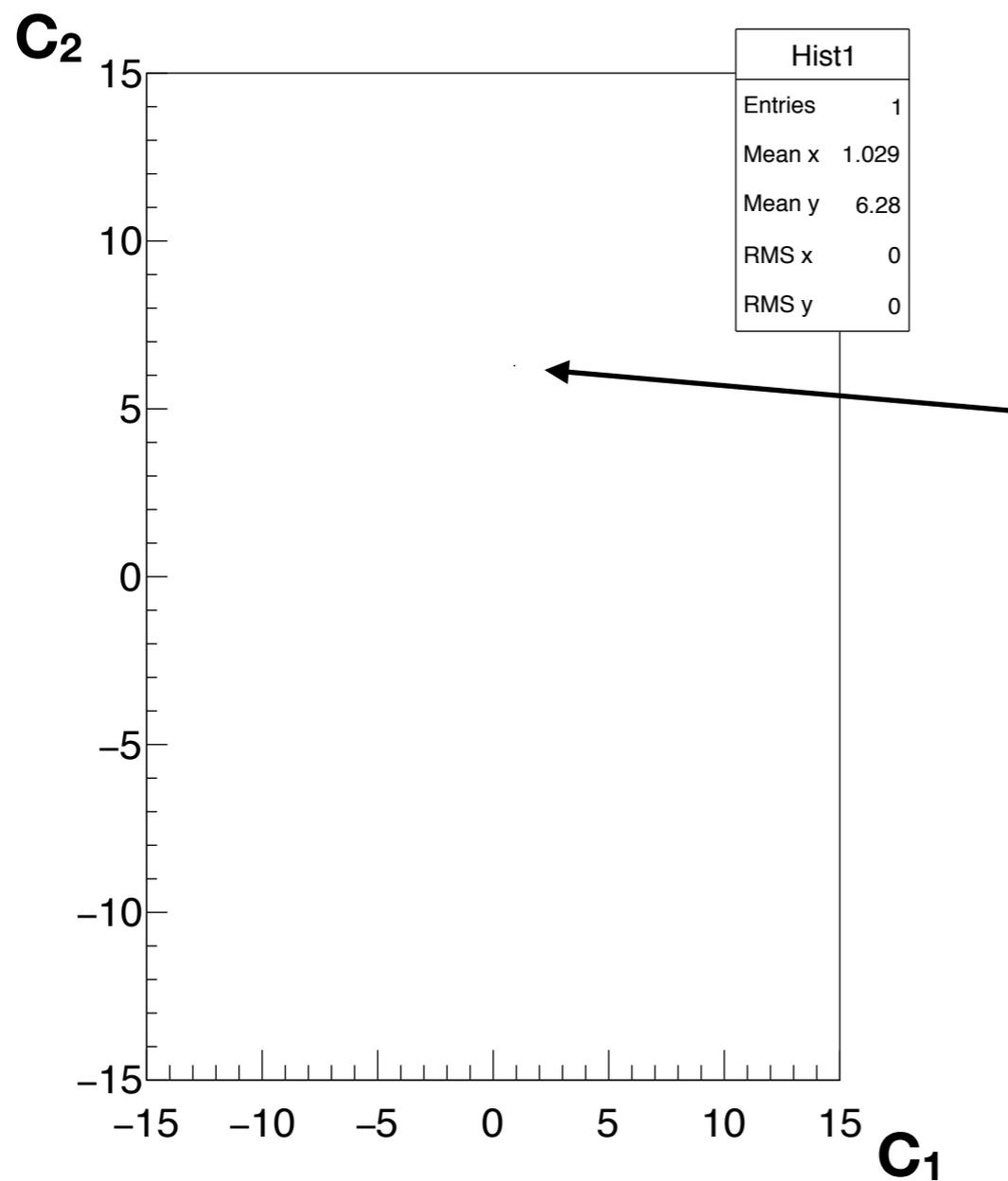
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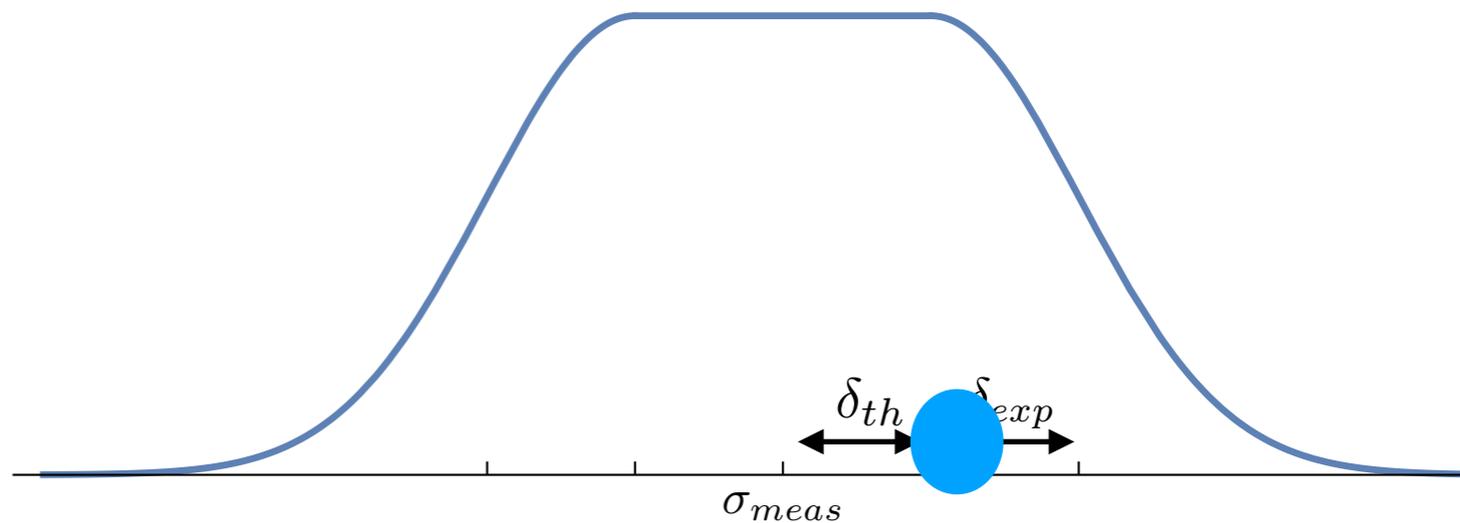
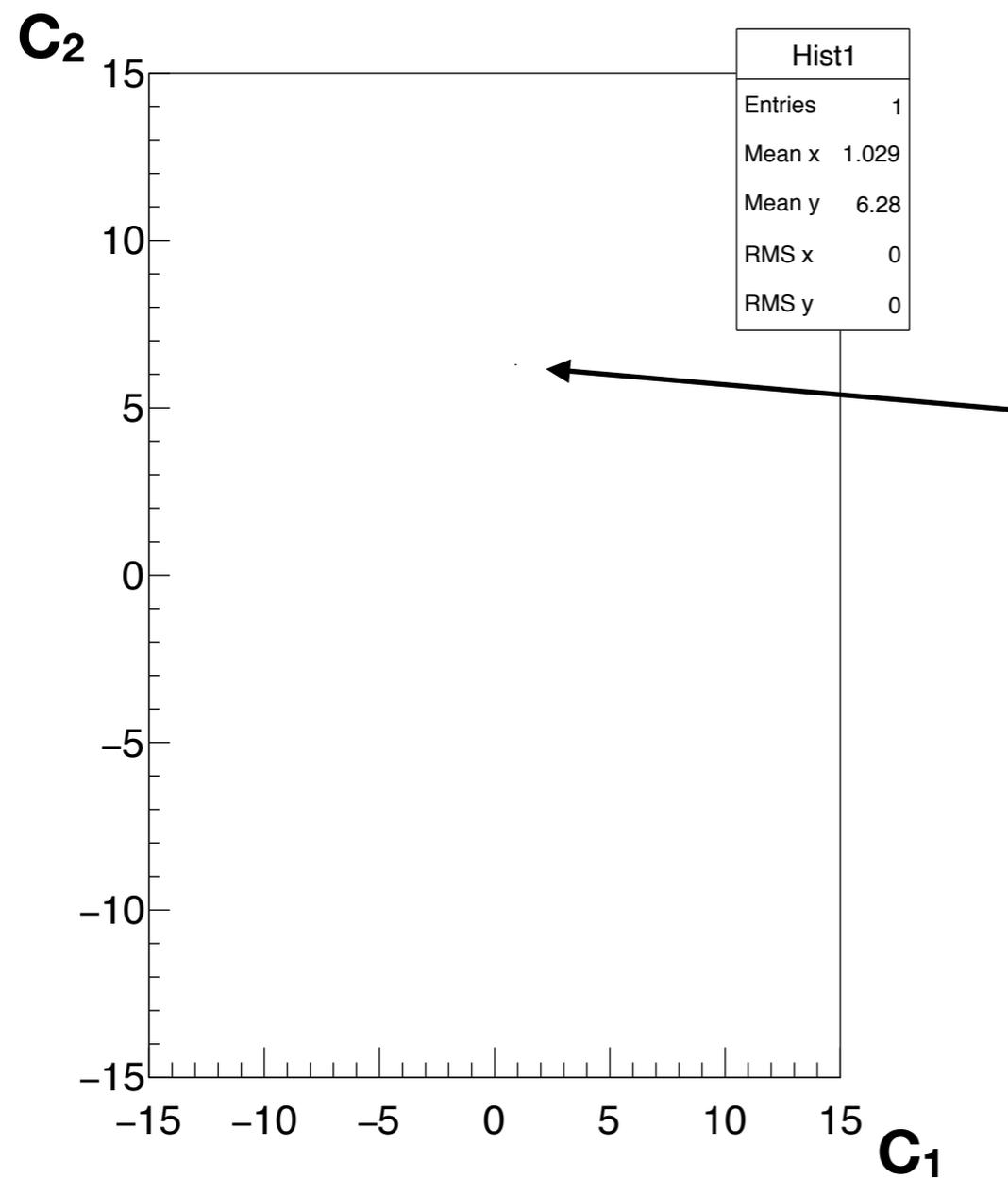
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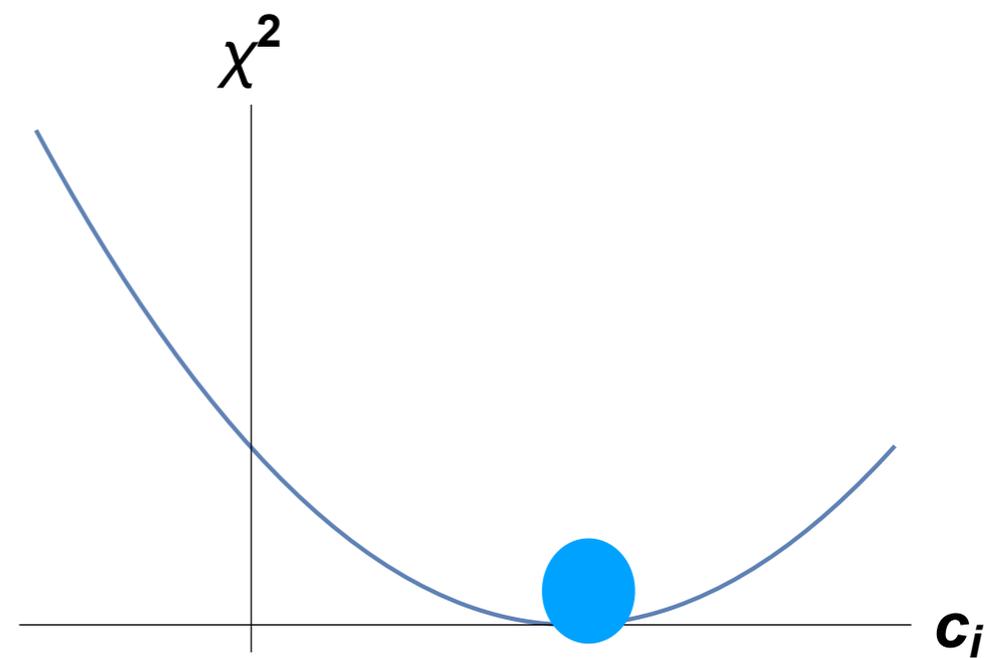
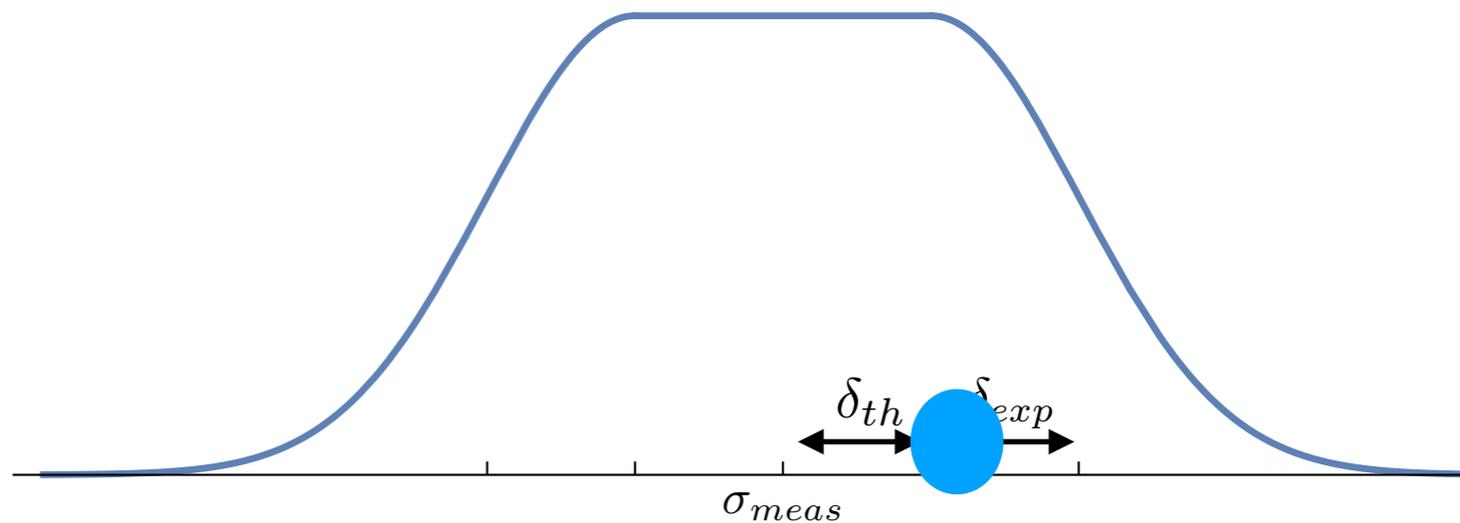
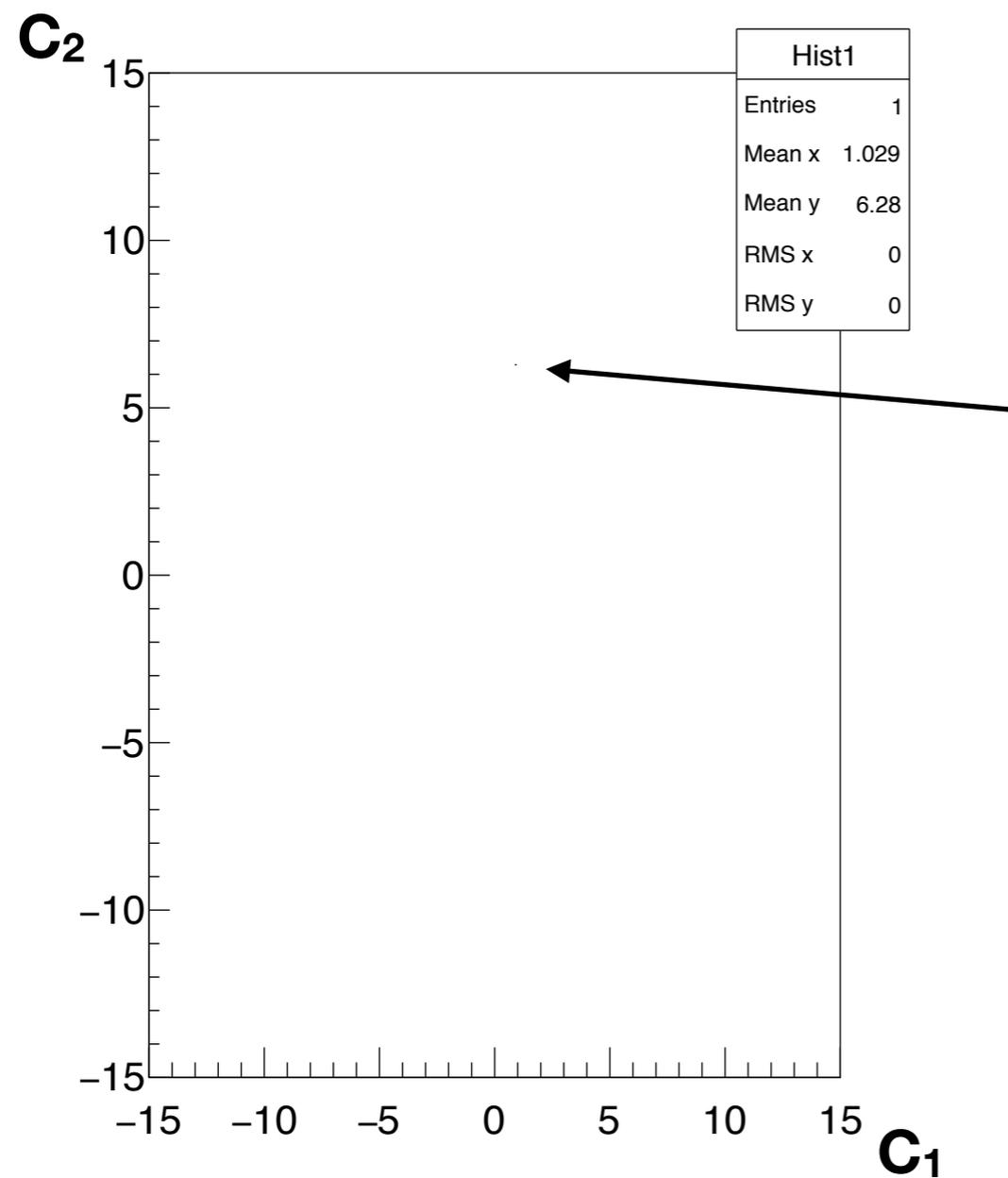
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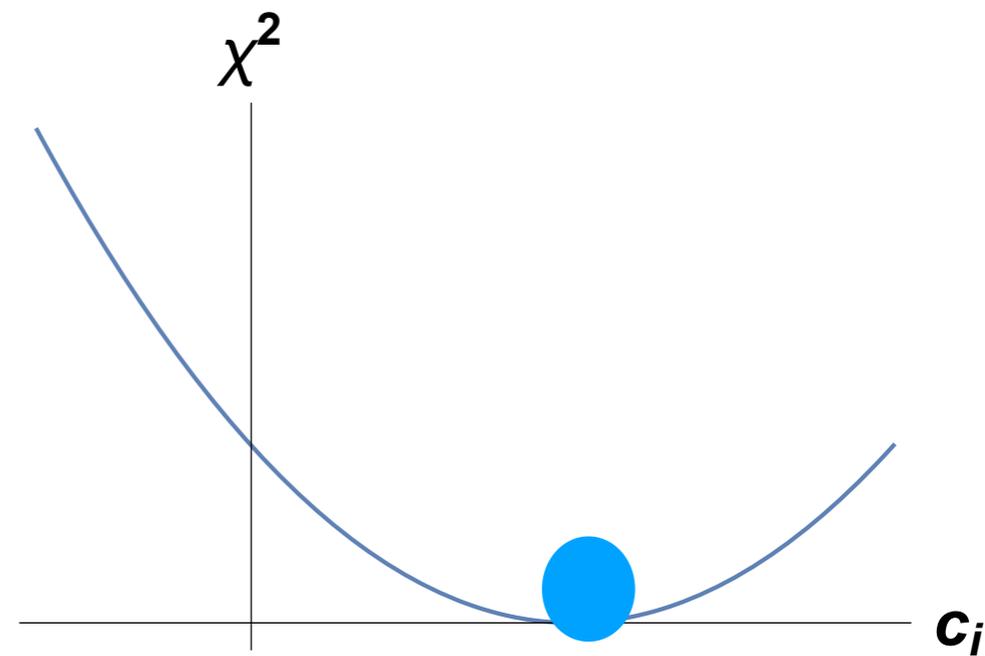
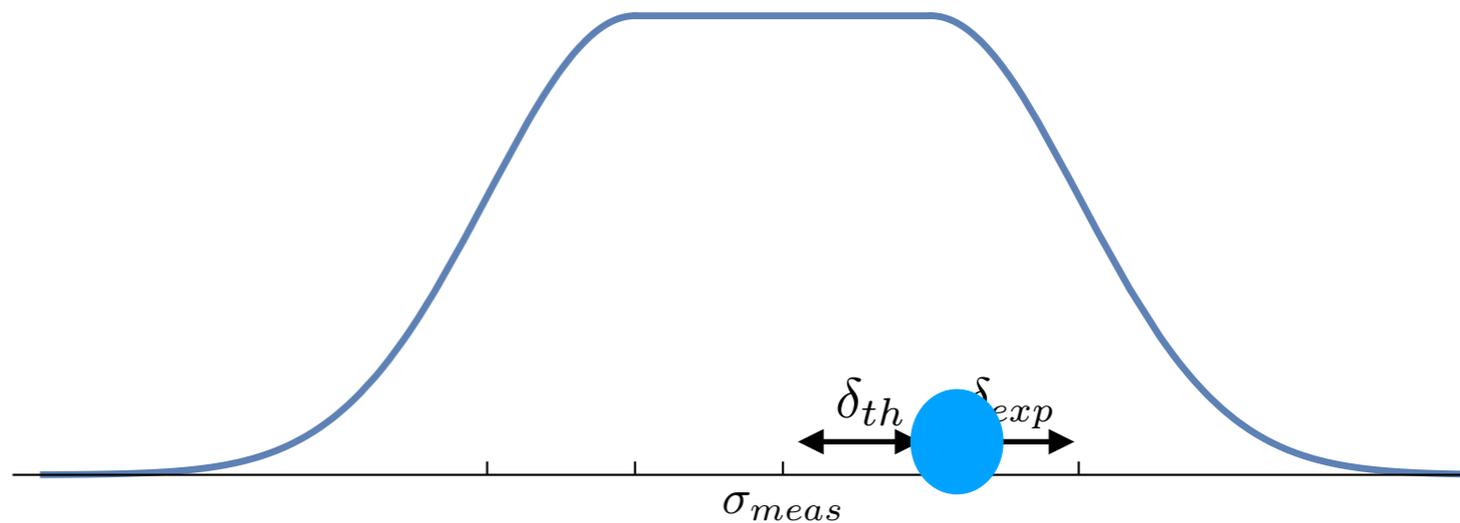
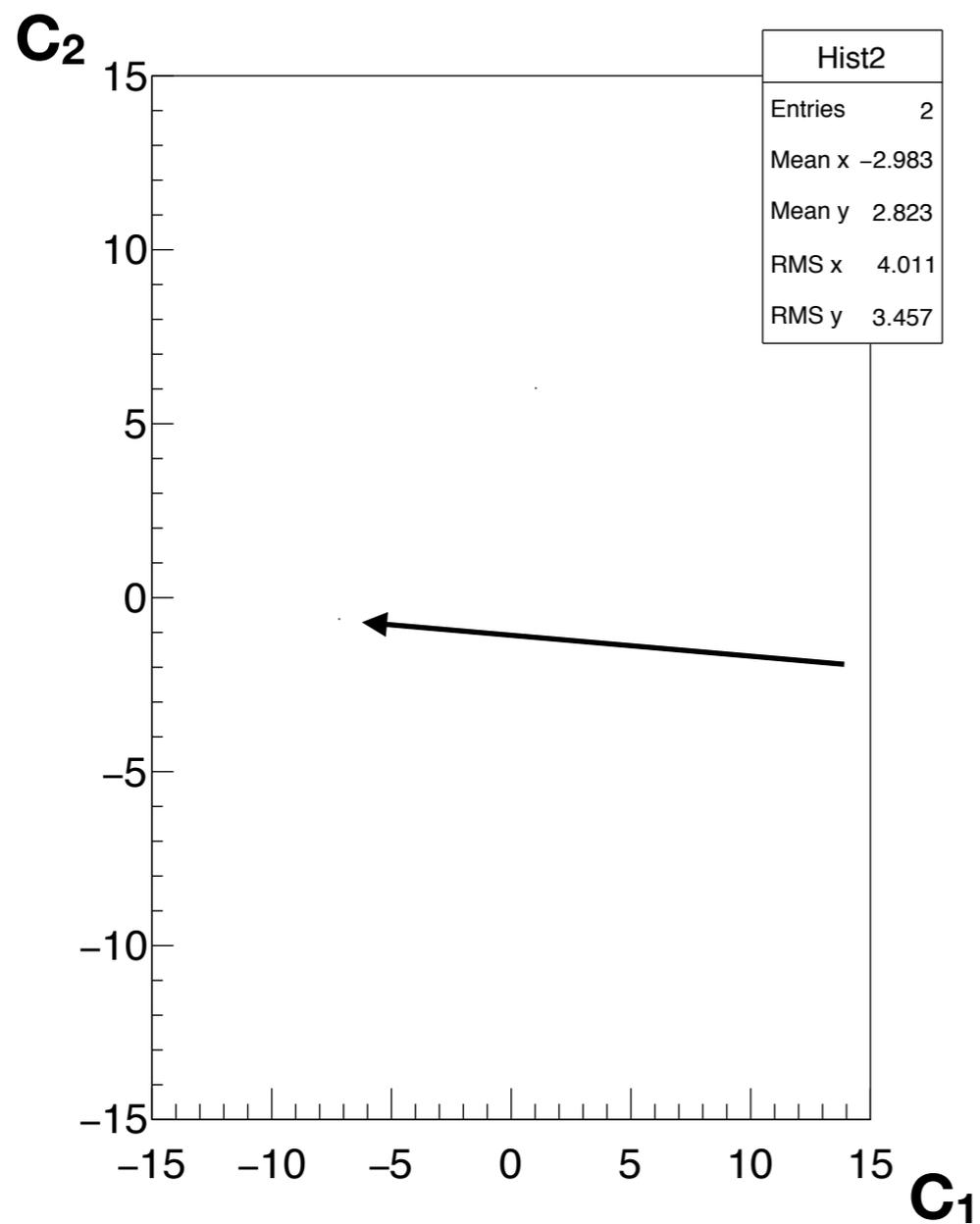
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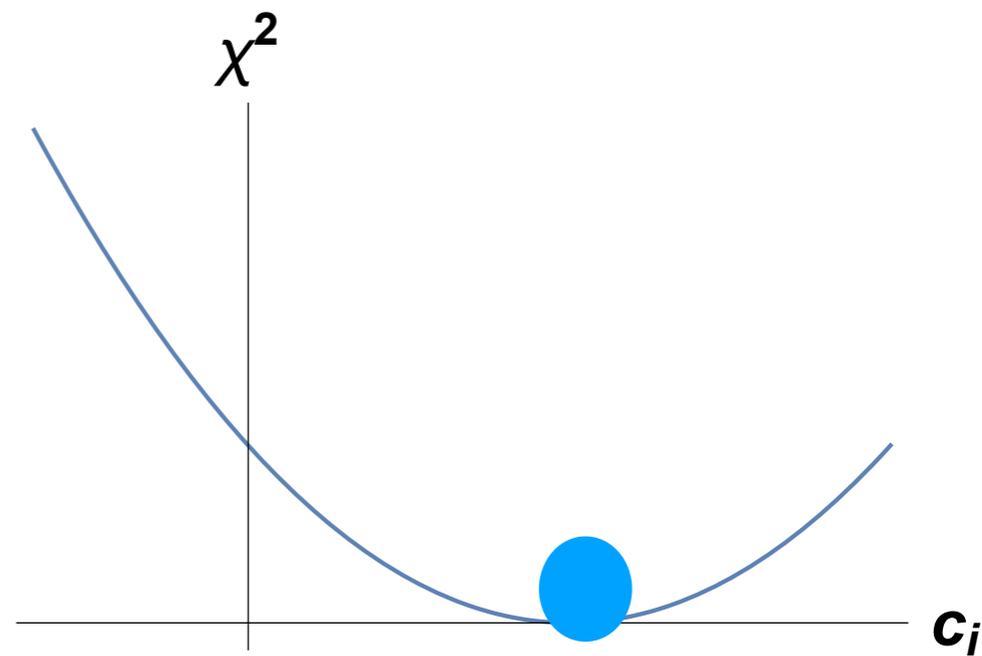
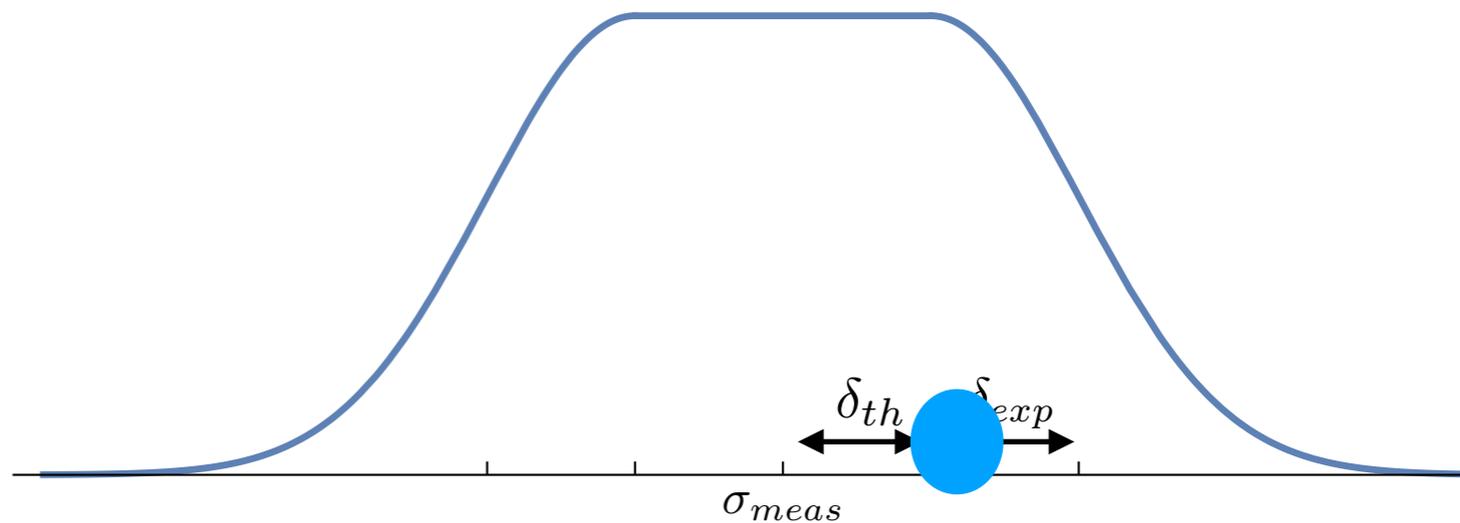
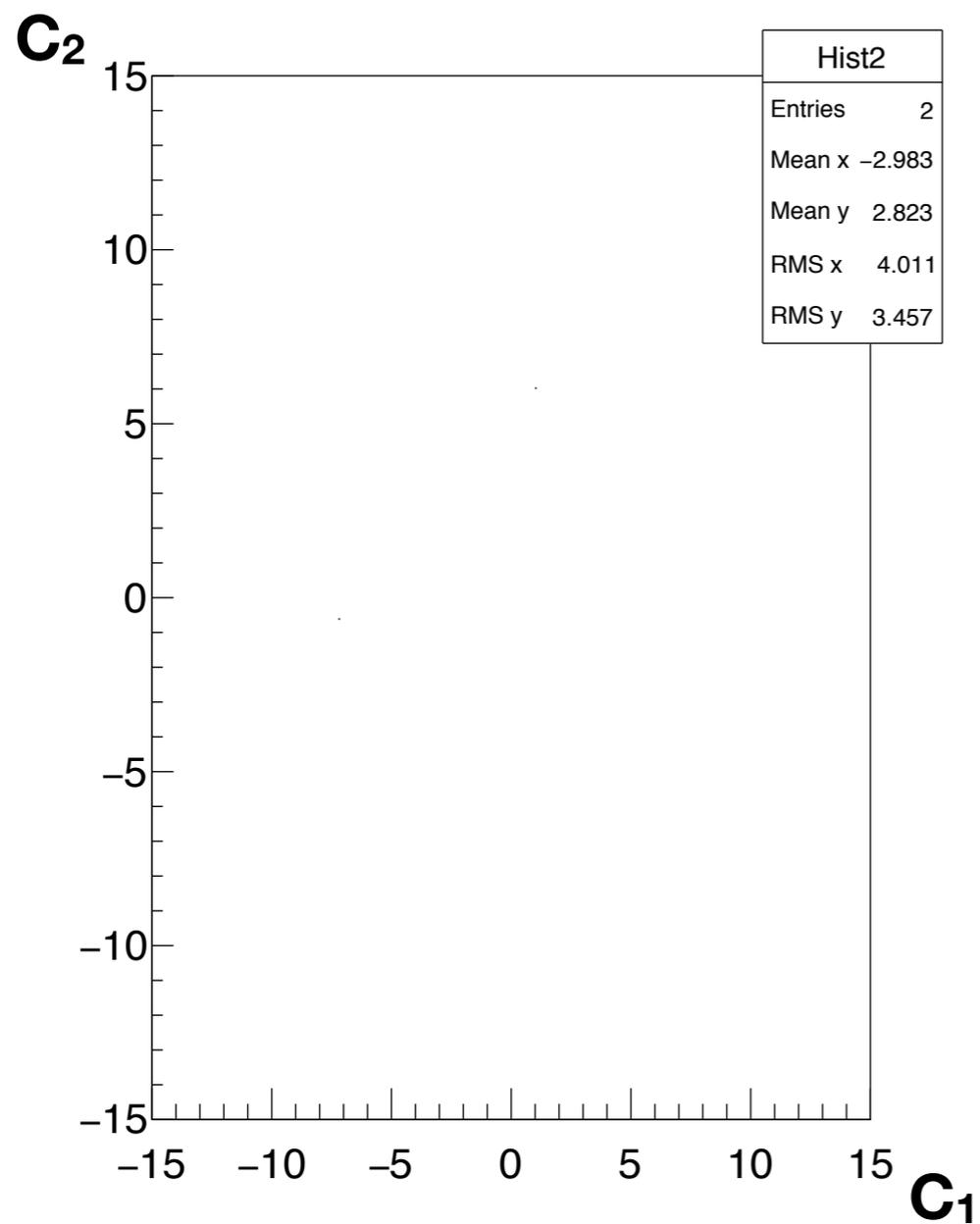
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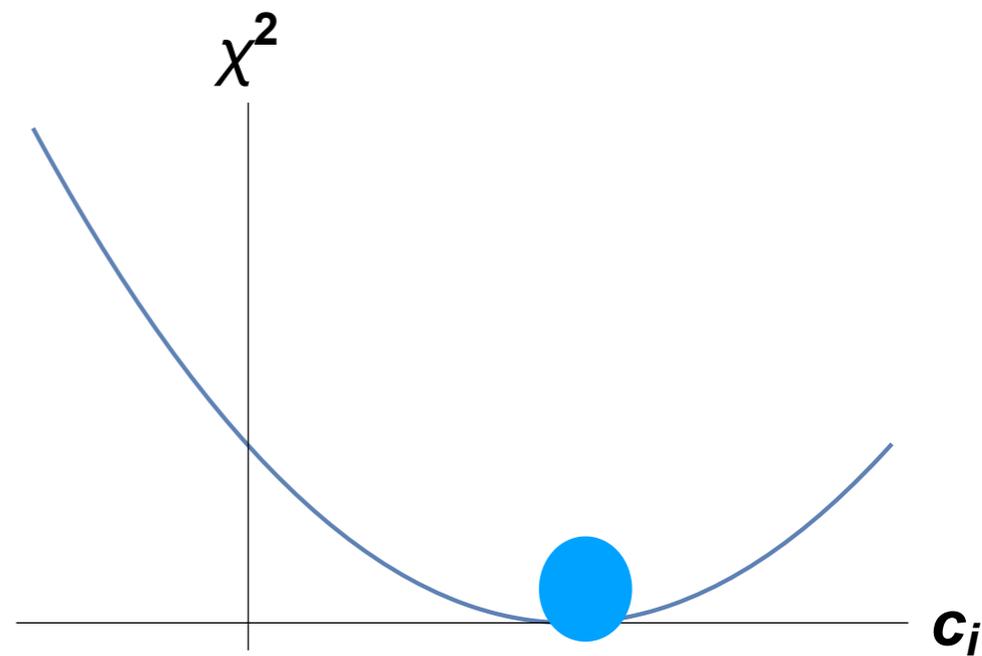
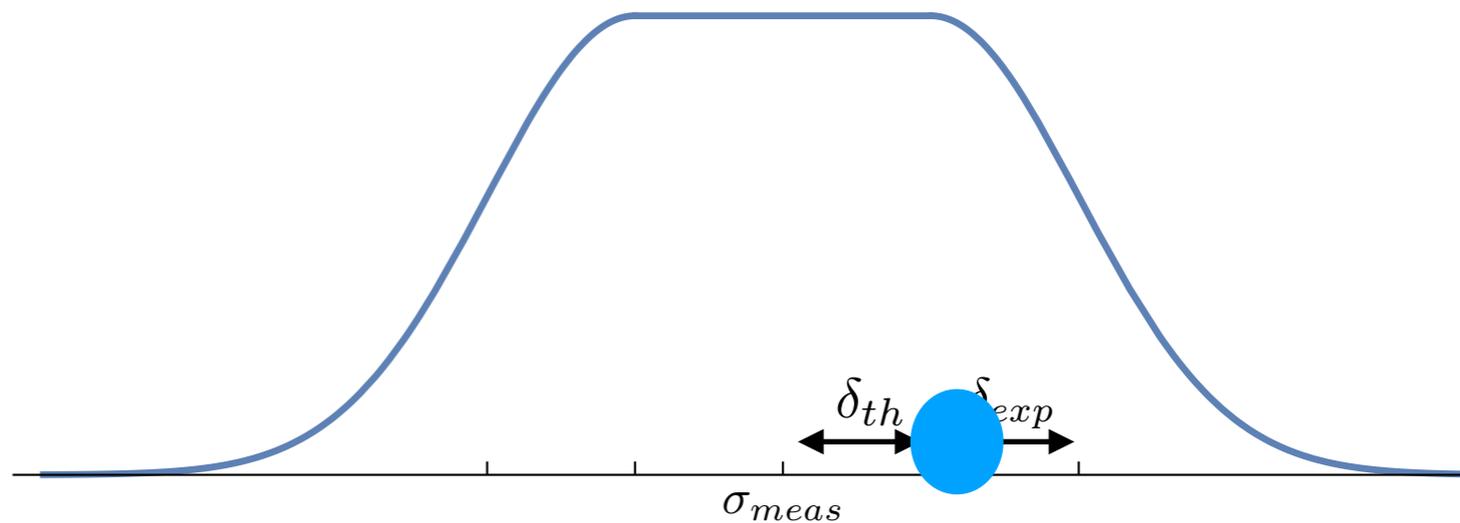
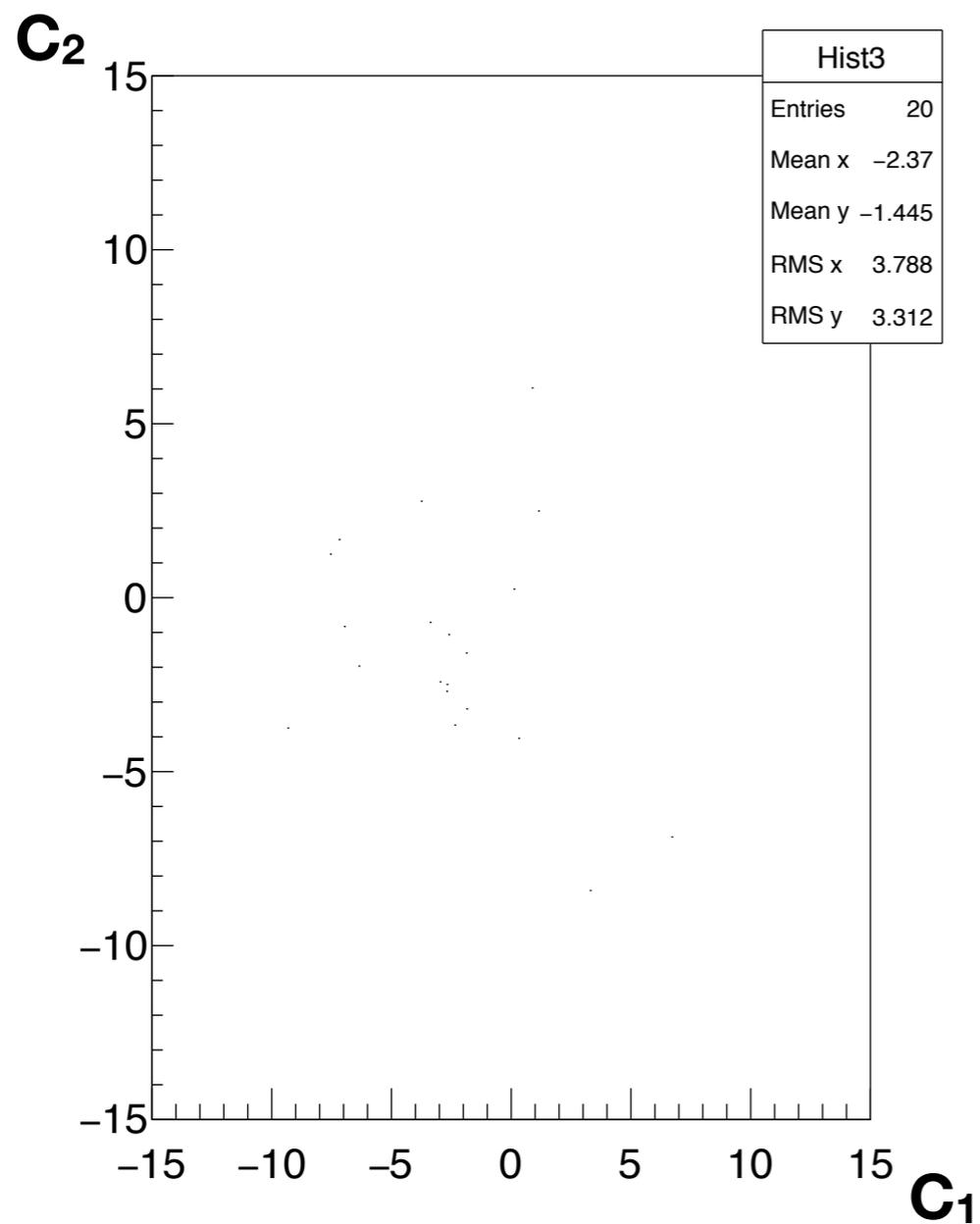
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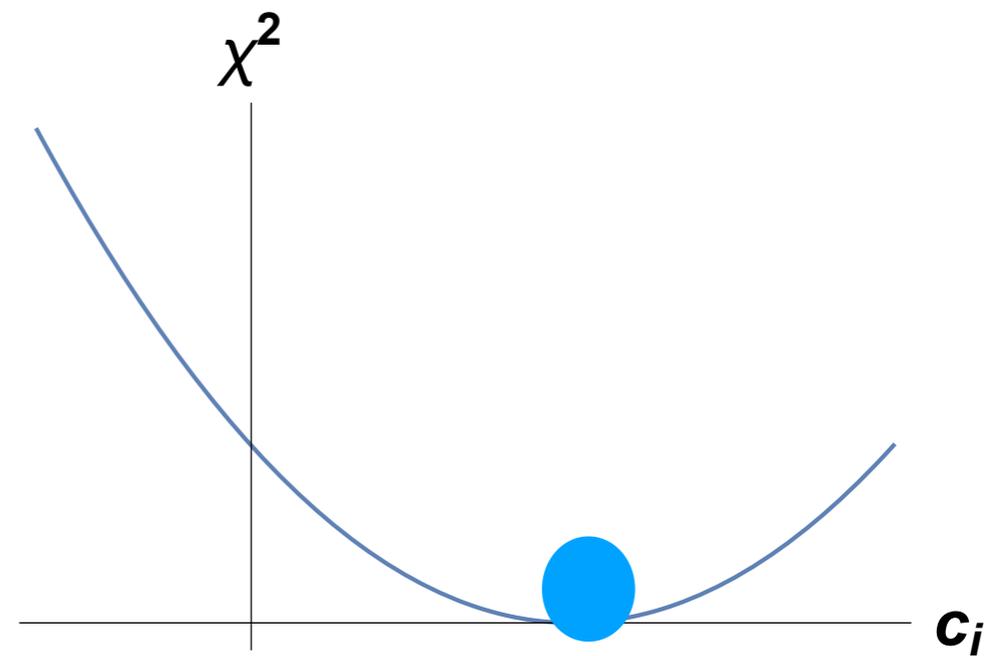
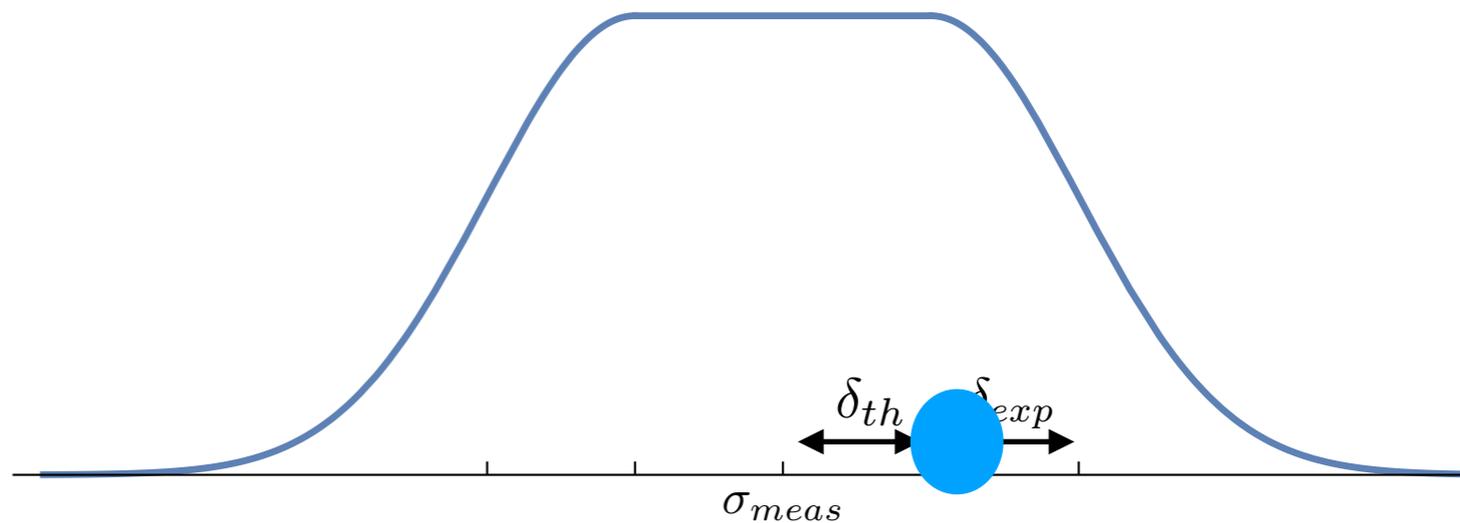
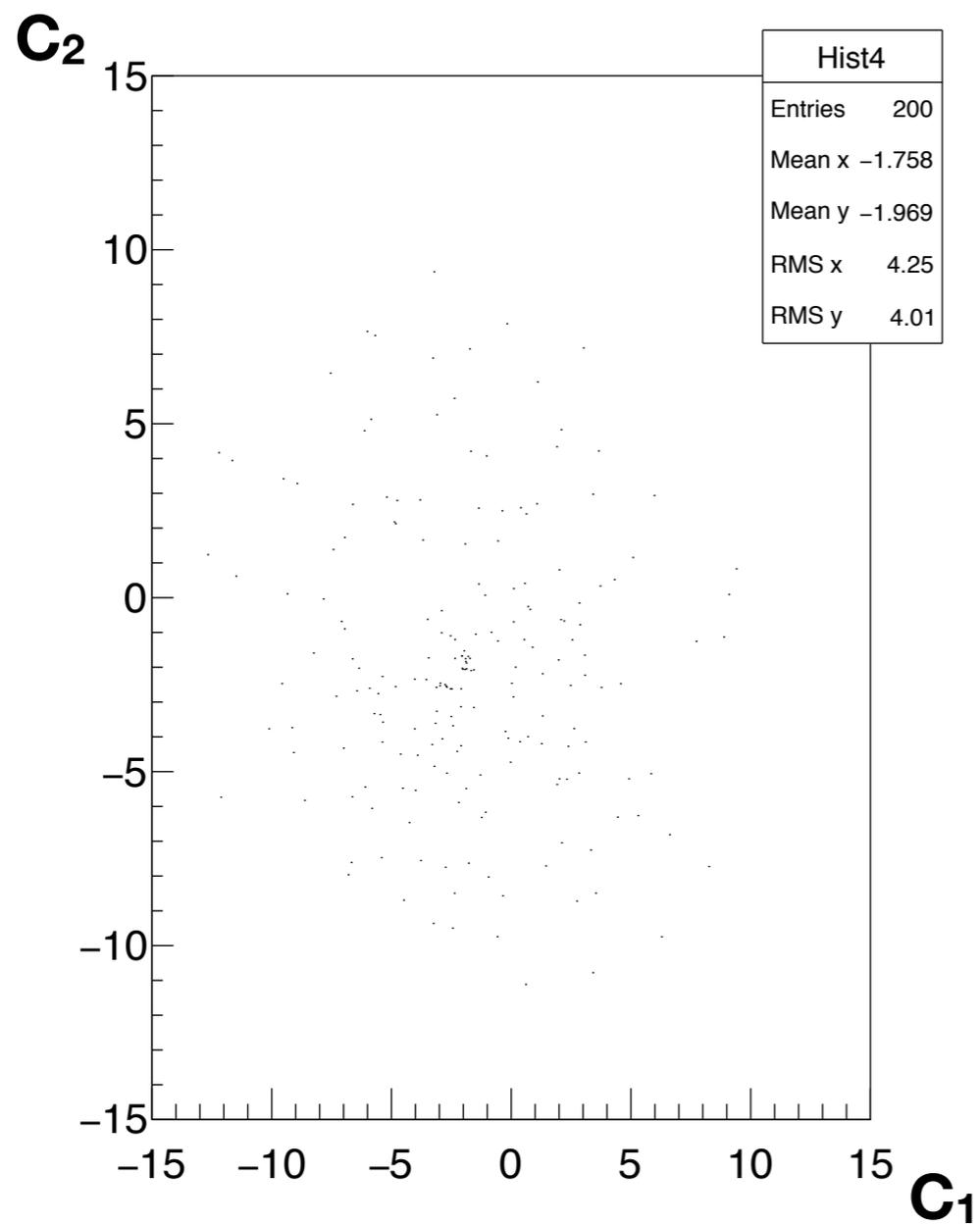
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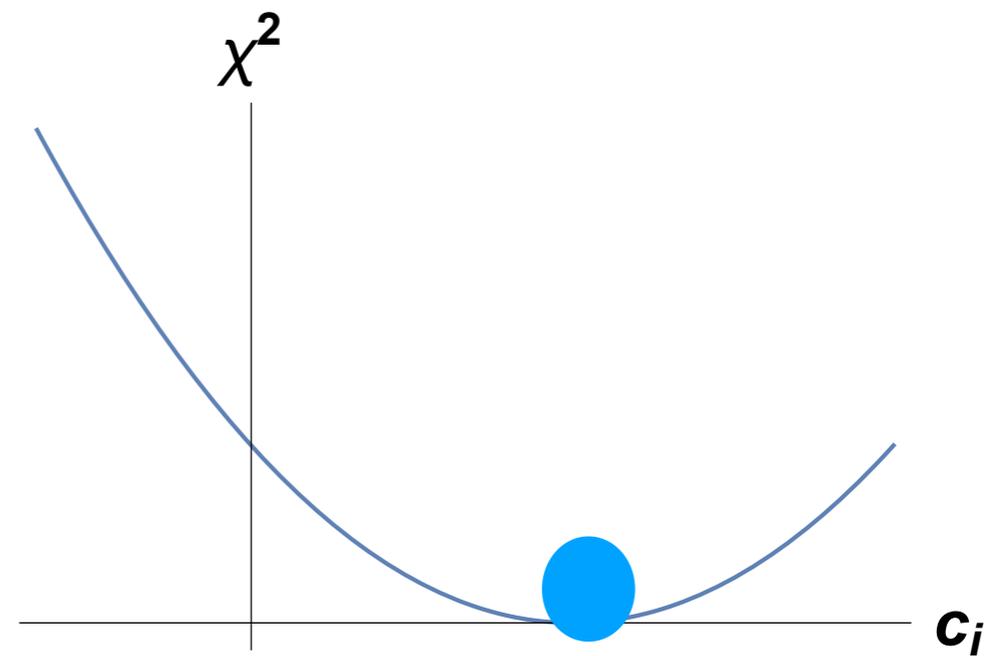
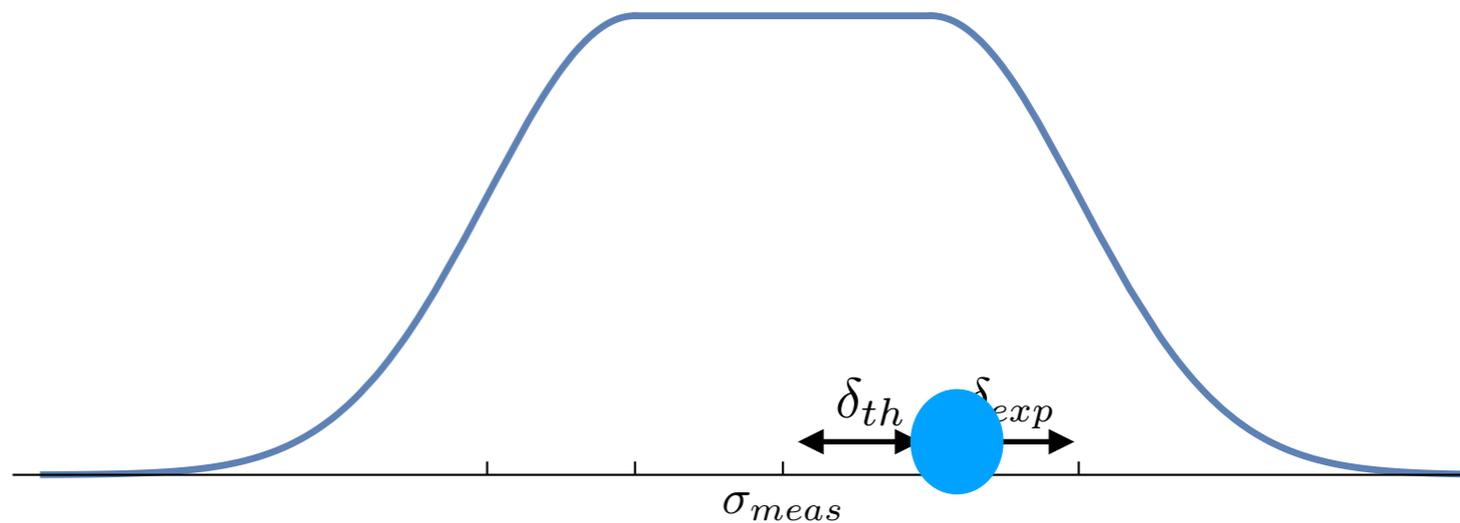
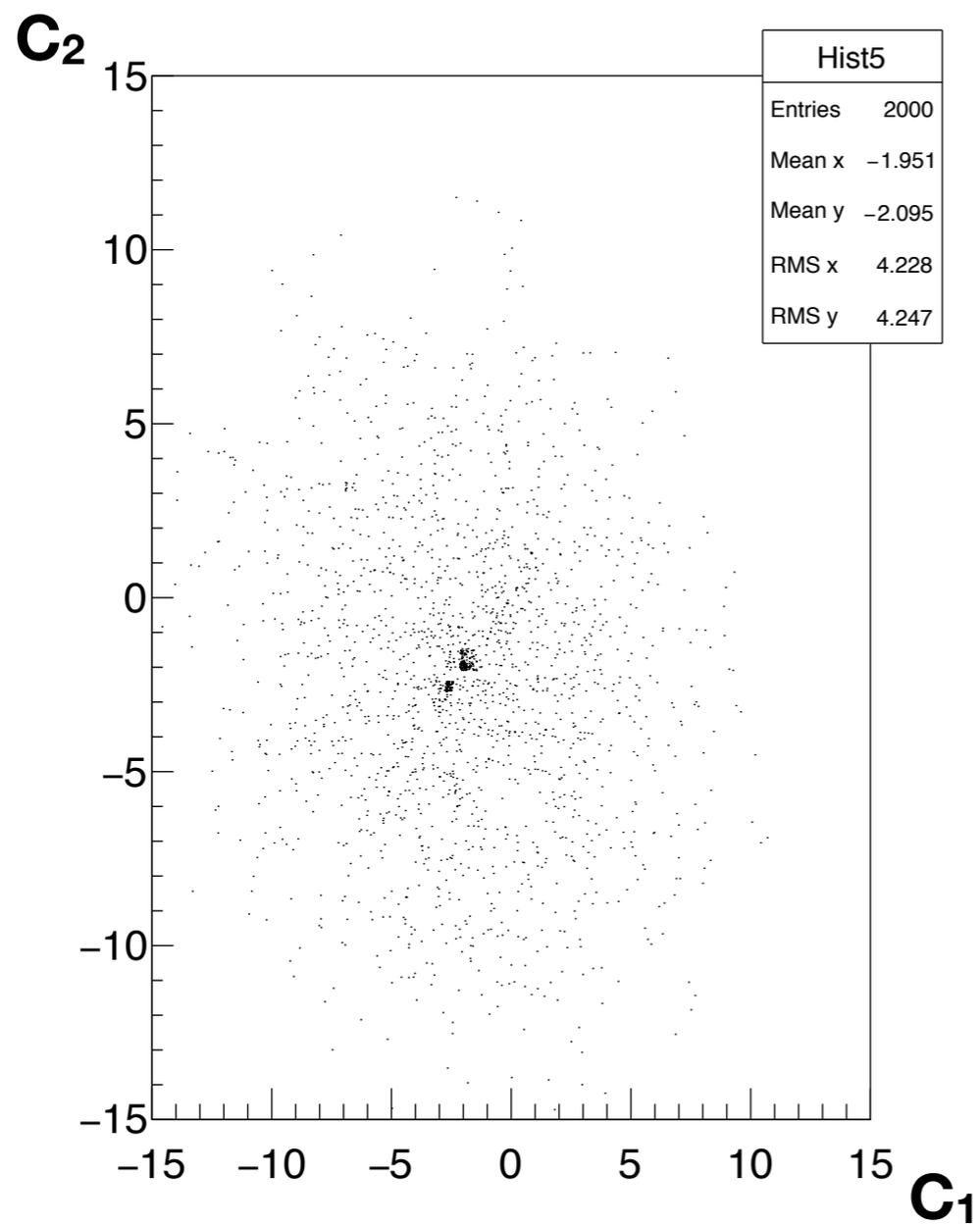
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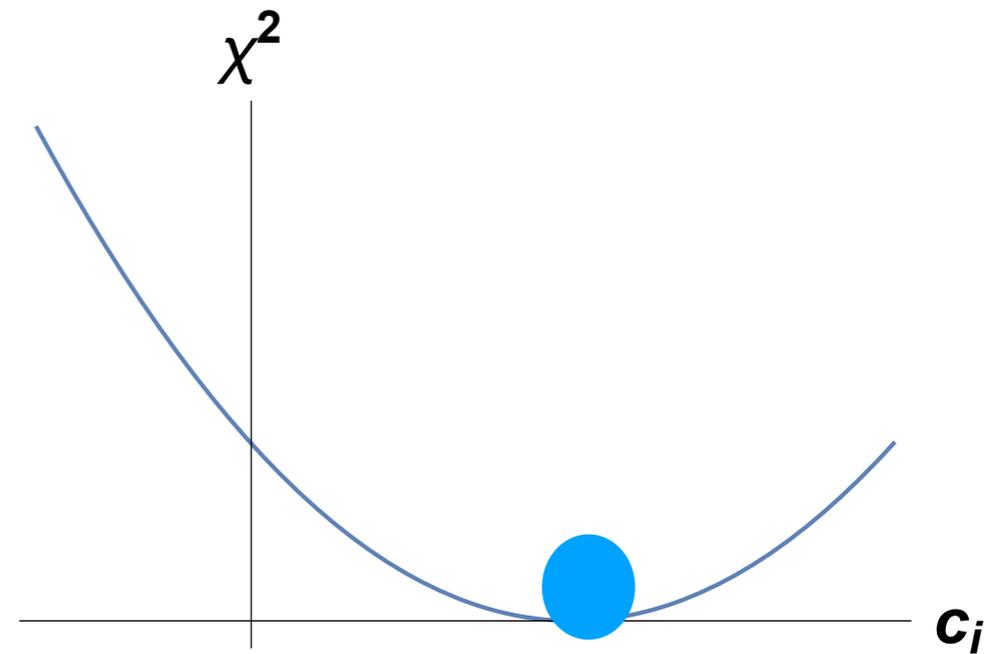
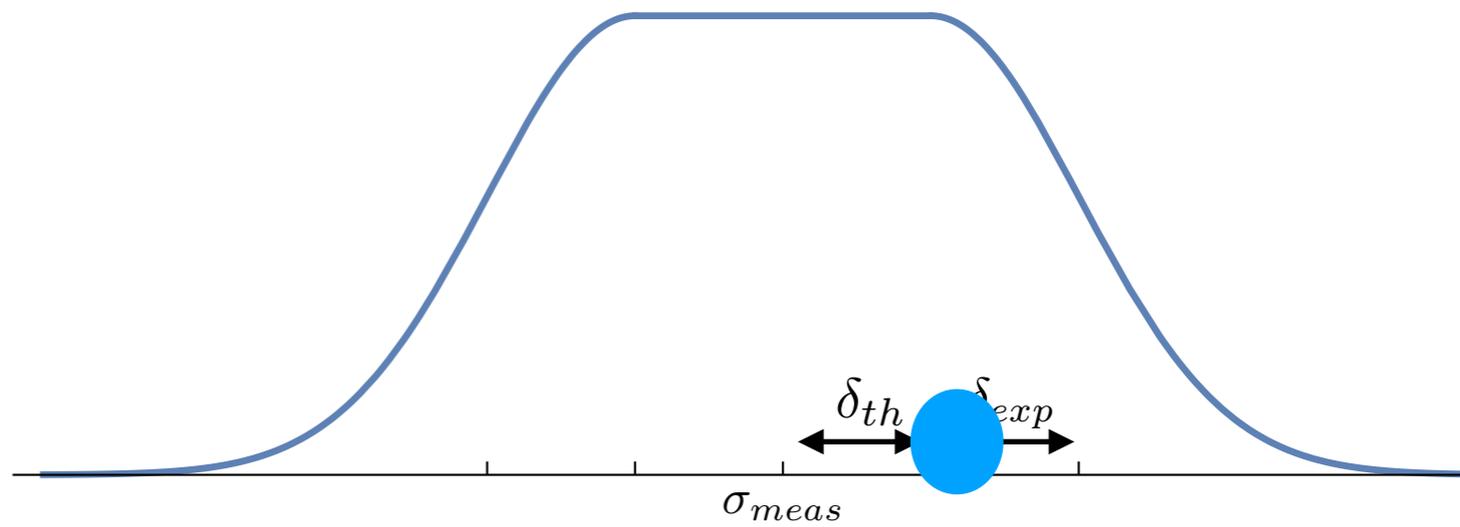
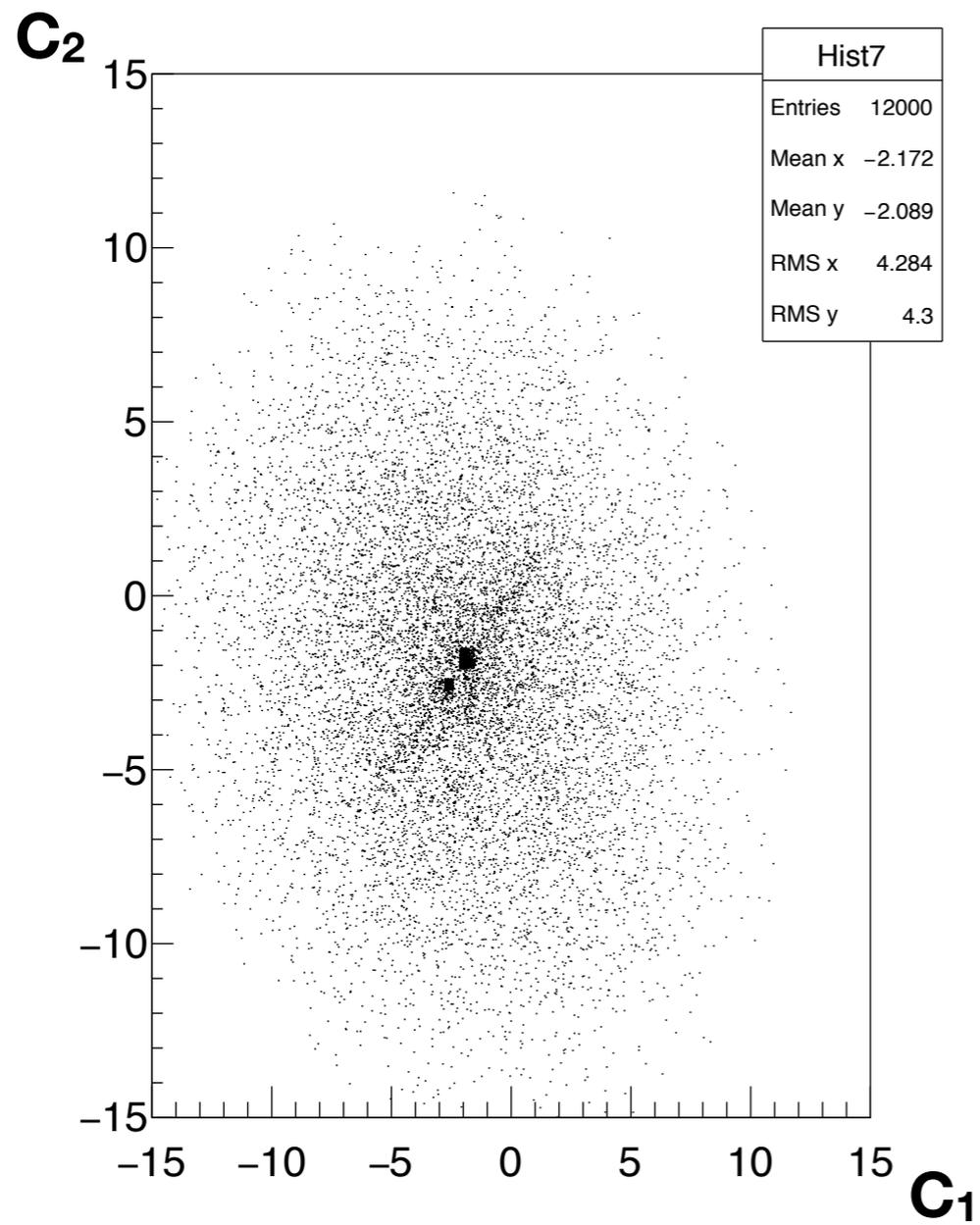
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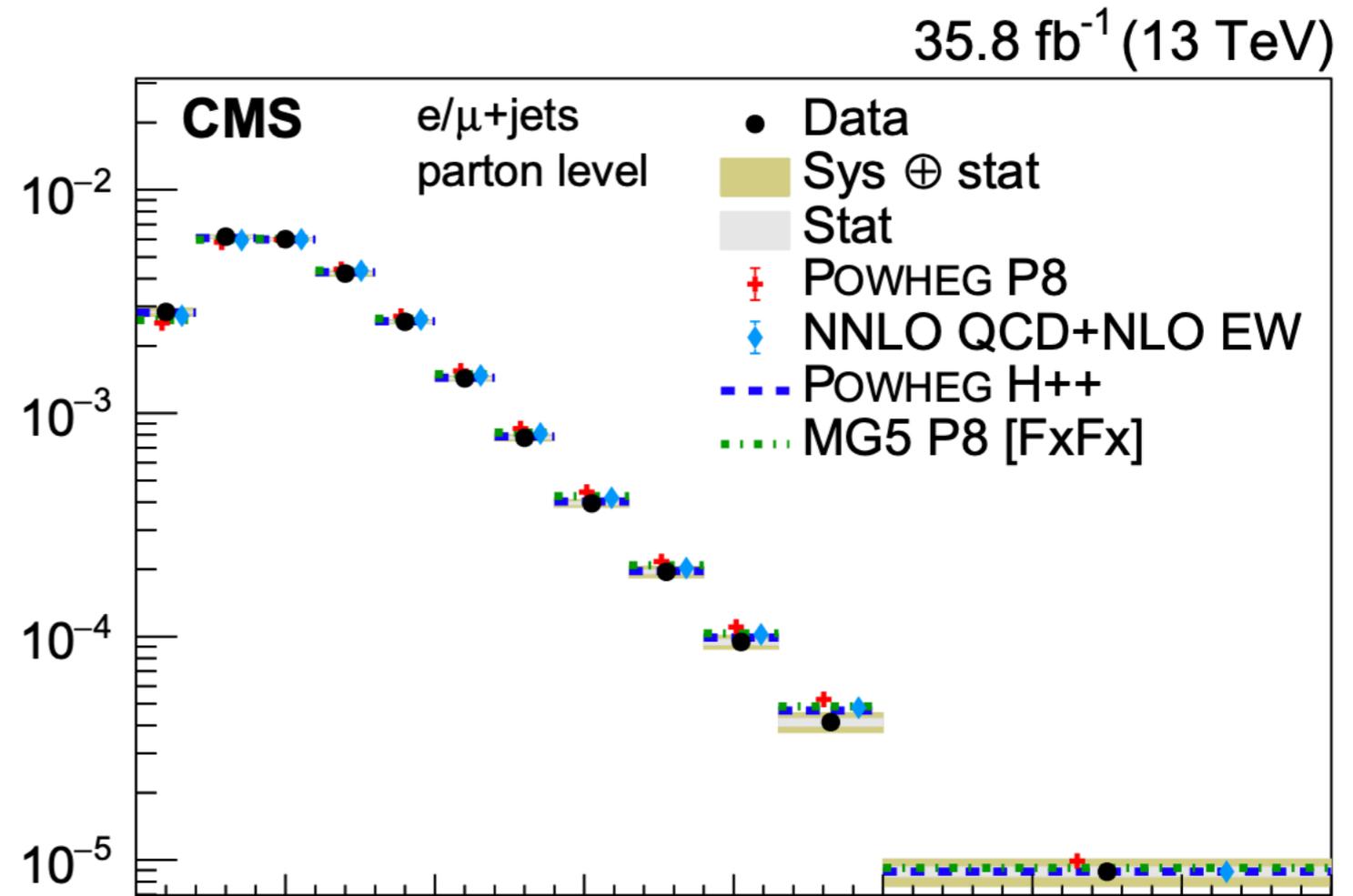


Some aspects of normalising

$$\hat{\sigma}_i = \frac{\sigma_i}{\sum_j \sigma_j \Delta_j} \rightarrow \sum_j \hat{\sigma}_j \Delta_j \equiv 1$$

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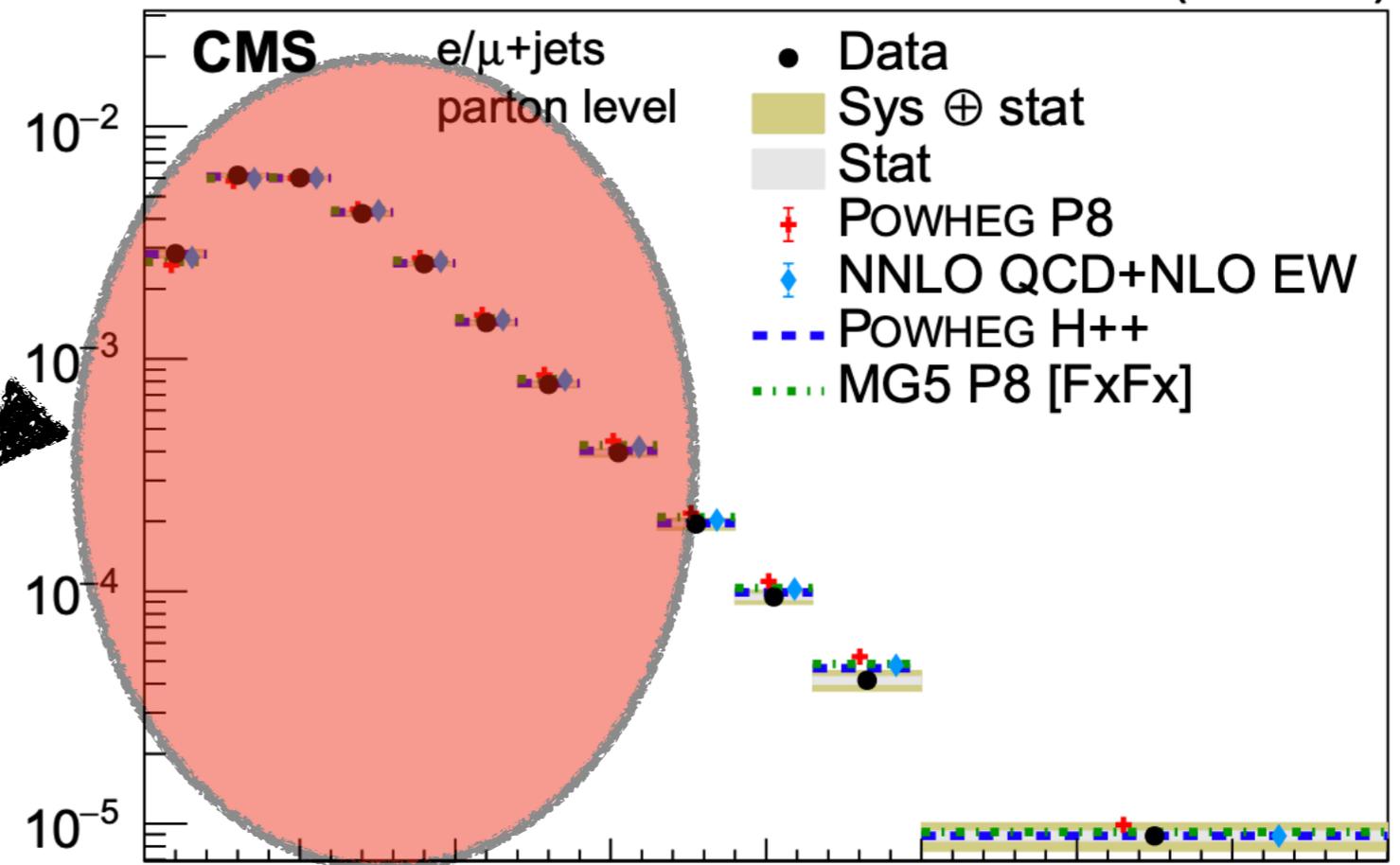
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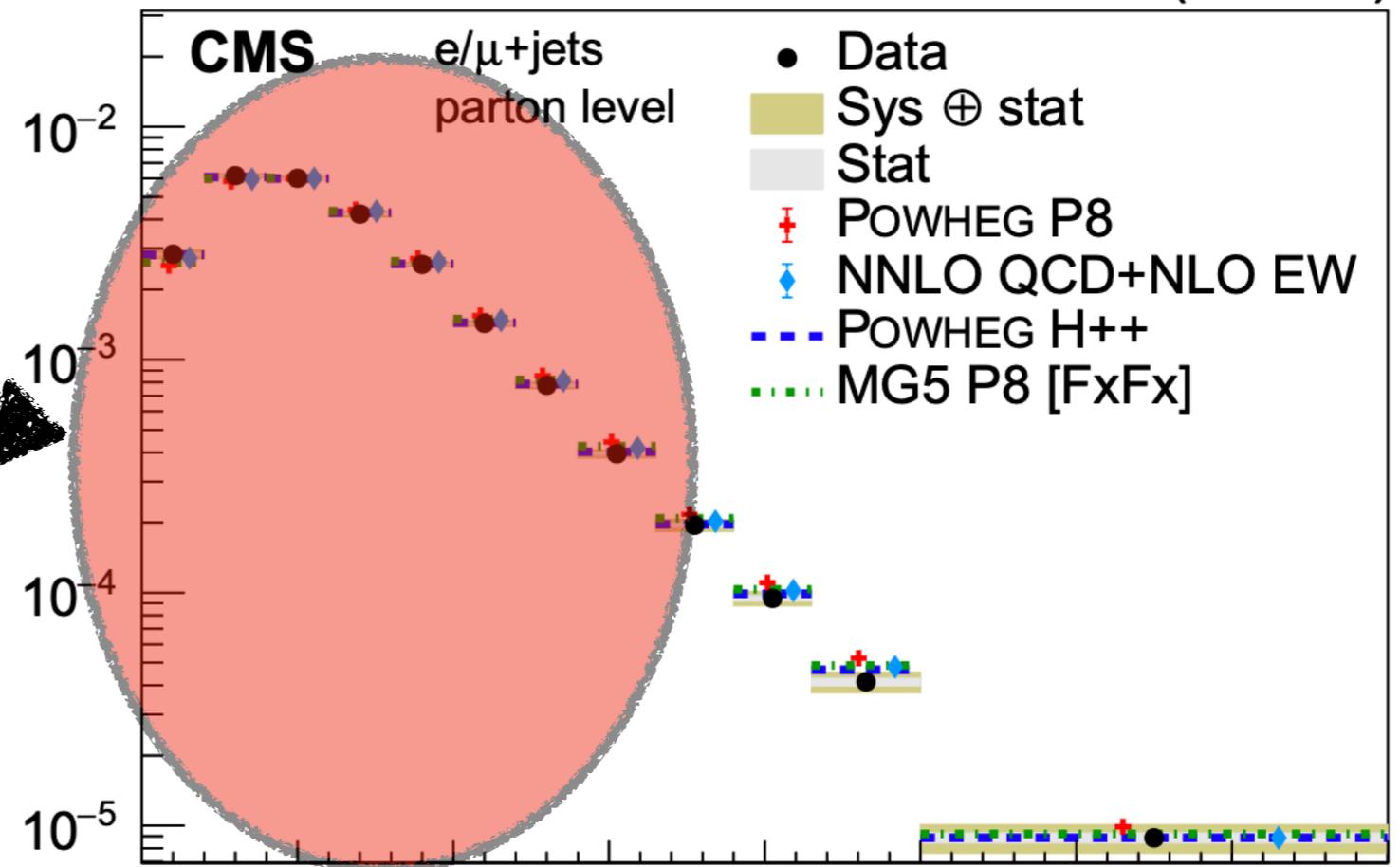
35.8 fb⁻¹ (13 TeV)



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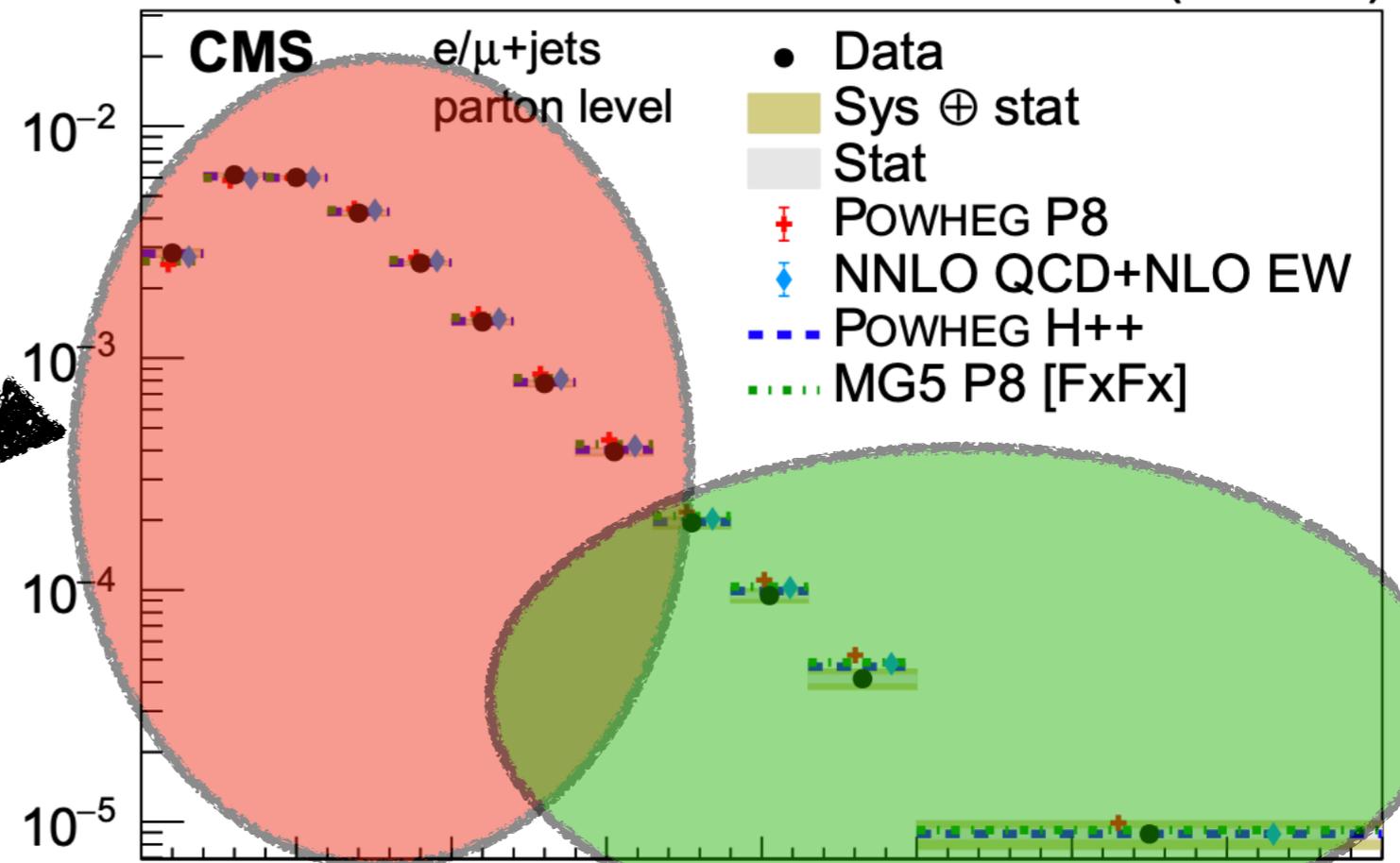


$$\sigma_{EFT} = \sigma_{SM} + \sum_{d.o.f.} \sigma_i \frac{C_i}{\Lambda^2} + \sum_{d.o.f.} \sigma_{ij} \frac{C_i C_j}{\Lambda^4} \pm \delta_{th}$$

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$$\frac{1}{\sum_j \sigma_j \Delta_j} = \#_1 + \sum_j \#_j c_j + \sum_{j,k} \#_{j,k} c_j c_k + \sum_{j,k,l} \#_{j,k,l} c_j c_k c_l + \dots$$

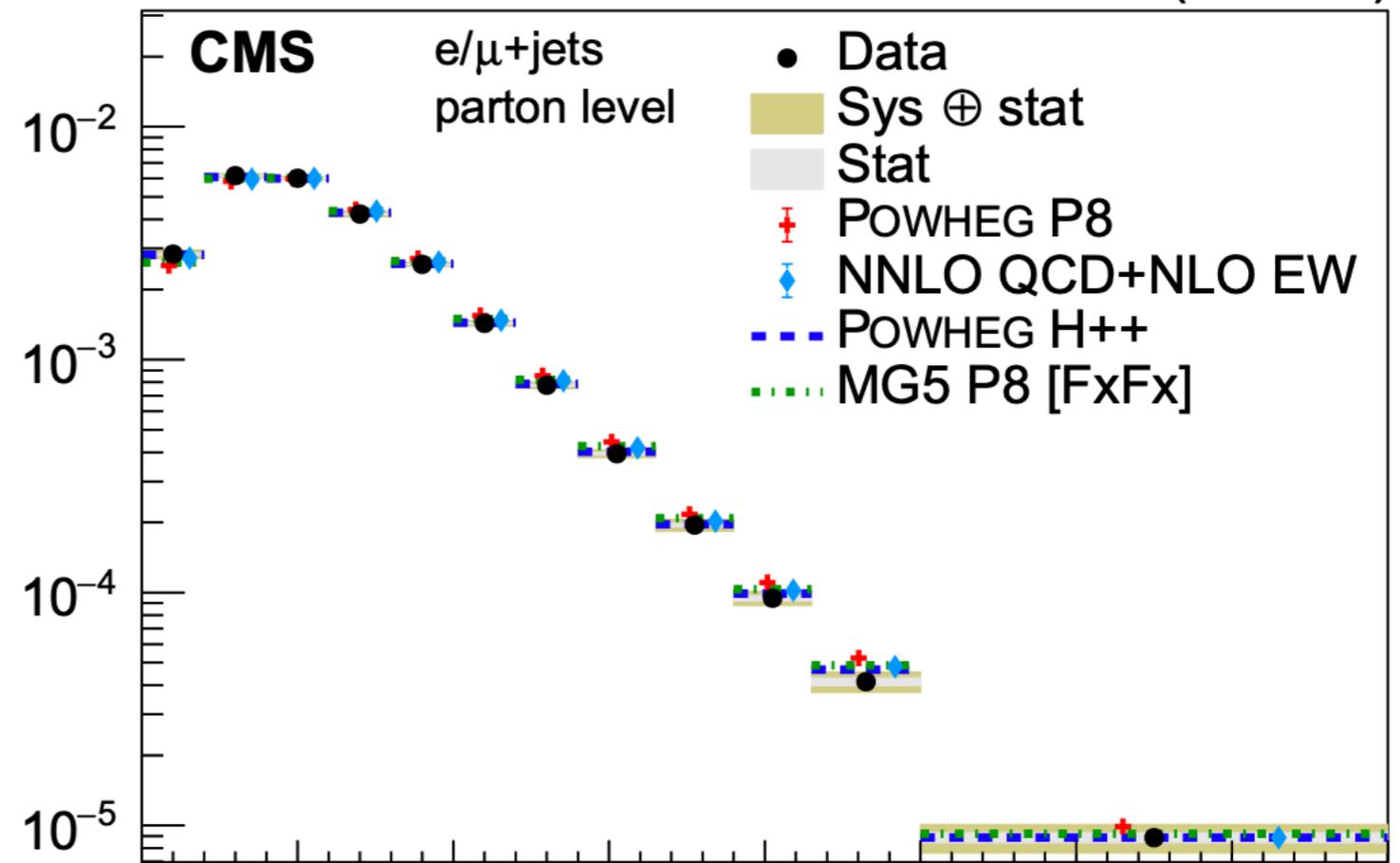
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Two strategies:

35.8 fb⁻¹ (13 TeV)



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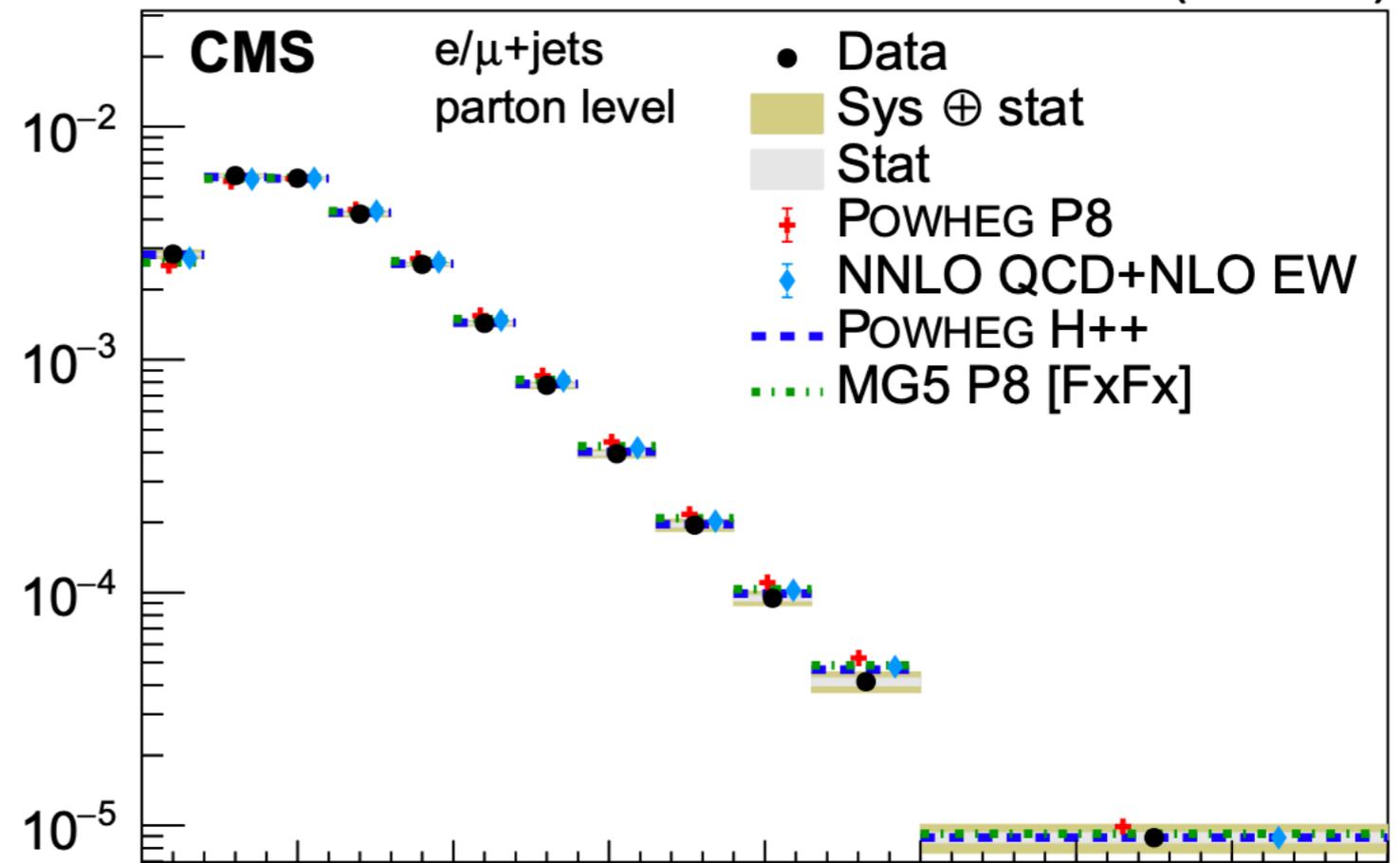
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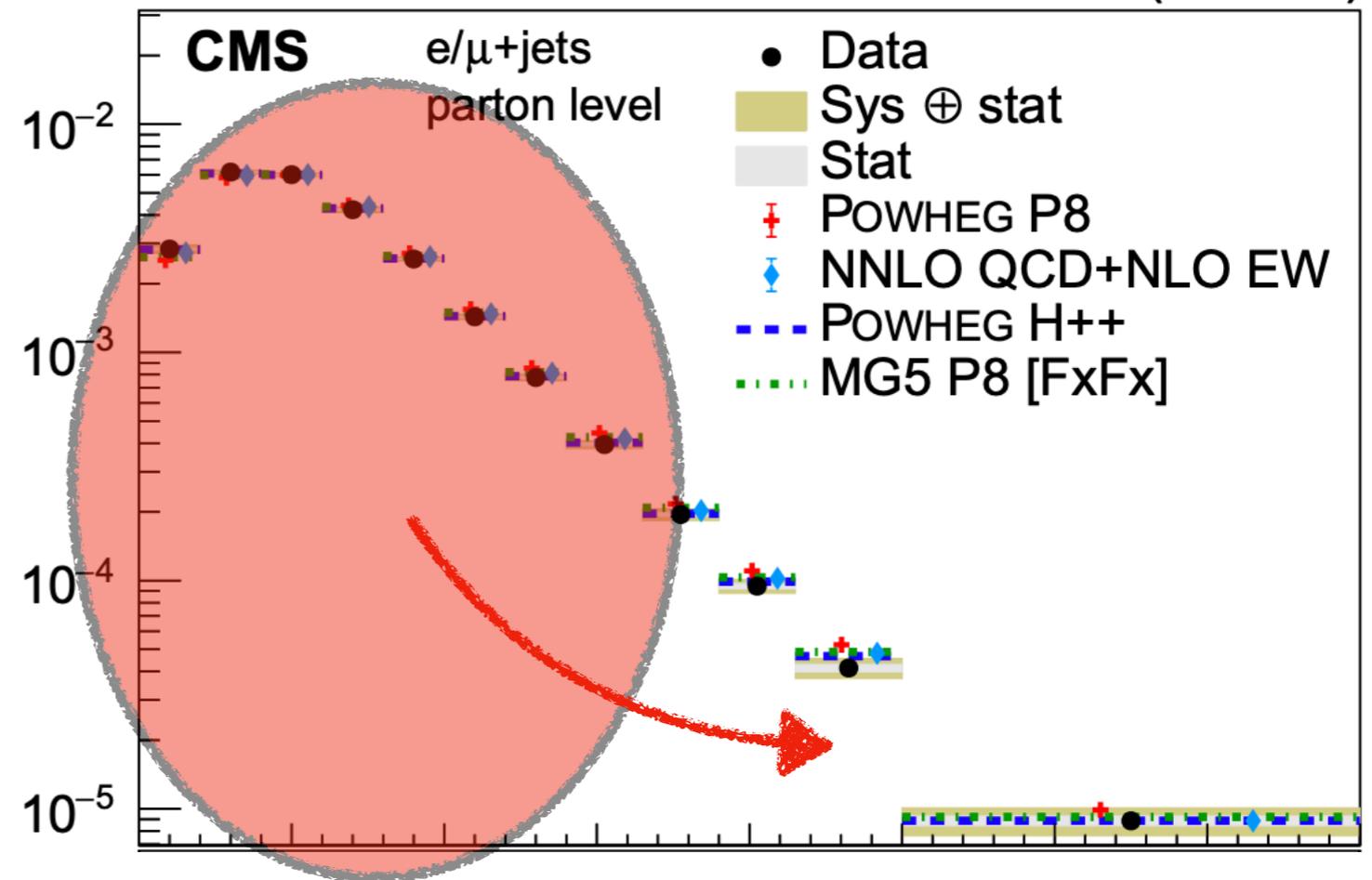
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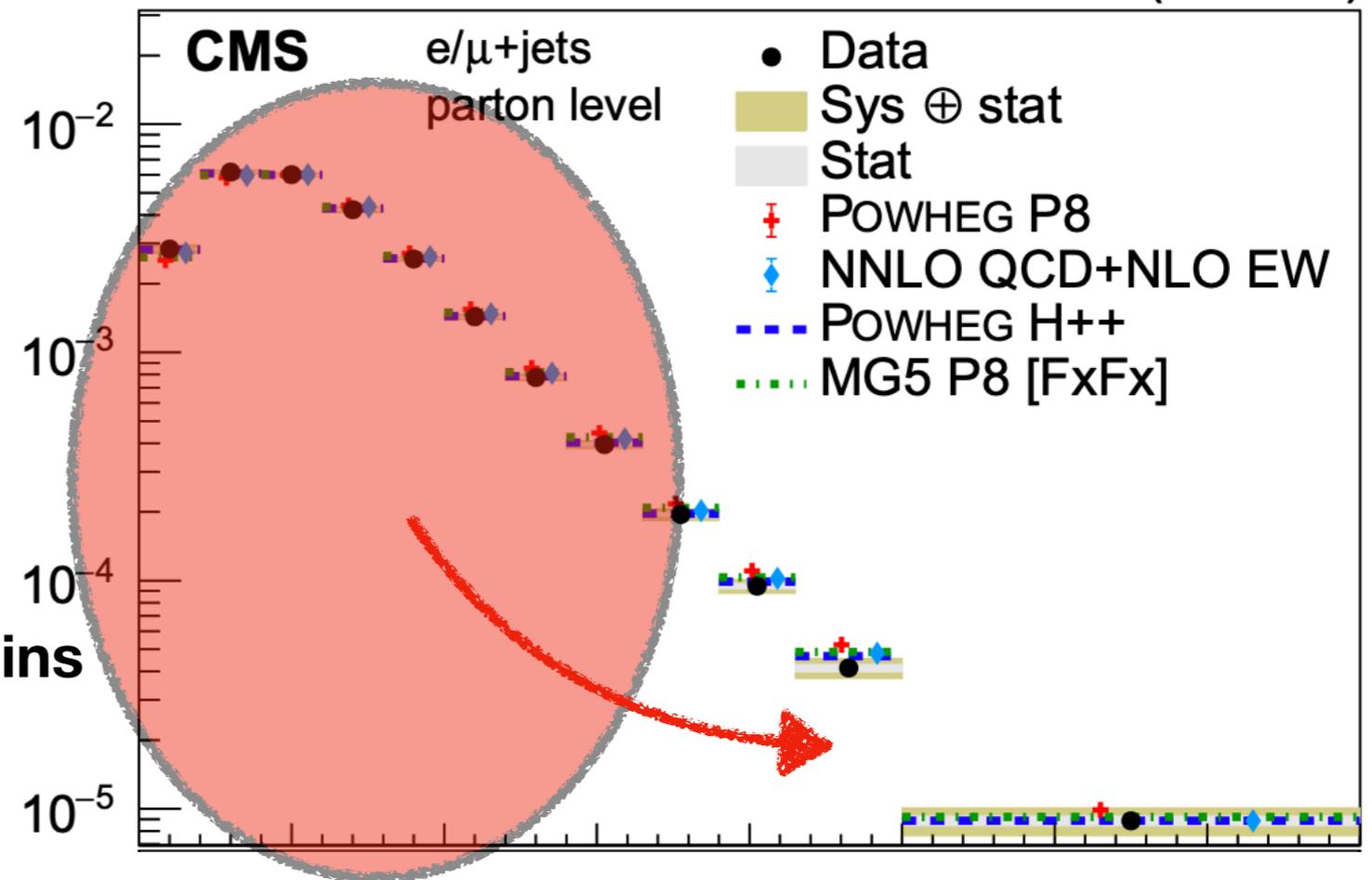
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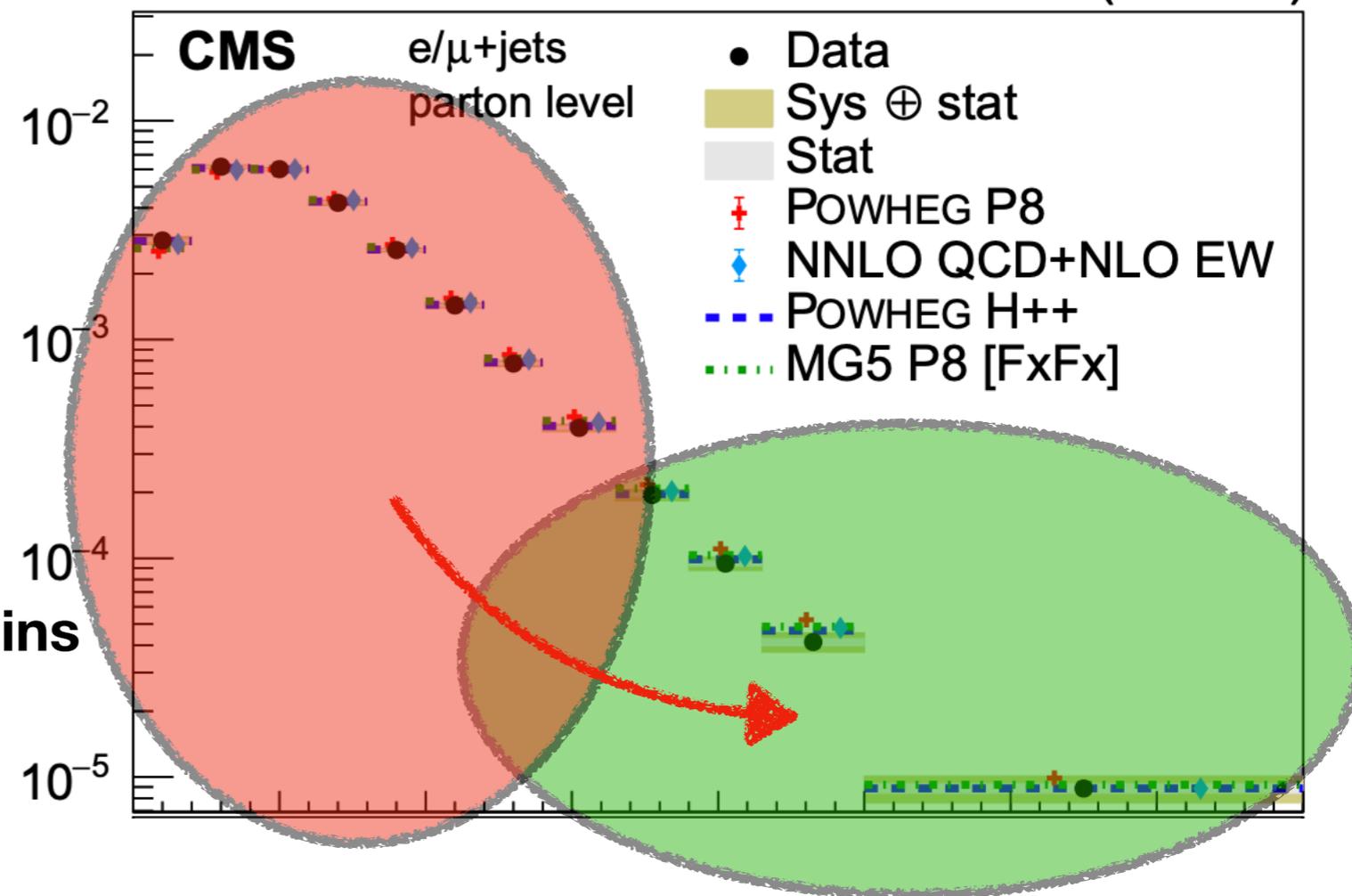
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Resolving Degeneracies

$$Out8 = 2C_{uu}^{8(i33i)} (\bar{u}_i \gamma^\mu T^A u_3) (\bar{u}_3 \gamma_\mu T^A u_i)$$

$$u_R \bar{u}_R \rightarrow t_R \bar{t}_R$$

$$OQu8 = C_{qu}^{1(33ii)} (\bar{q}_3 \gamma^\mu T^A q_3) (\bar{u}_i \gamma_\mu T^A u_i)$$

$$u_R \bar{u}_R \rightarrow t_L \bar{t}_L$$

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Resolving Degeneracies

$$O_{ut8} = 2C_{uu}^{8(i33i)} (\bar{u}_i \gamma^\mu T^A u_3) (\bar{u}_3 \gamma_\mu T^A u_i)$$

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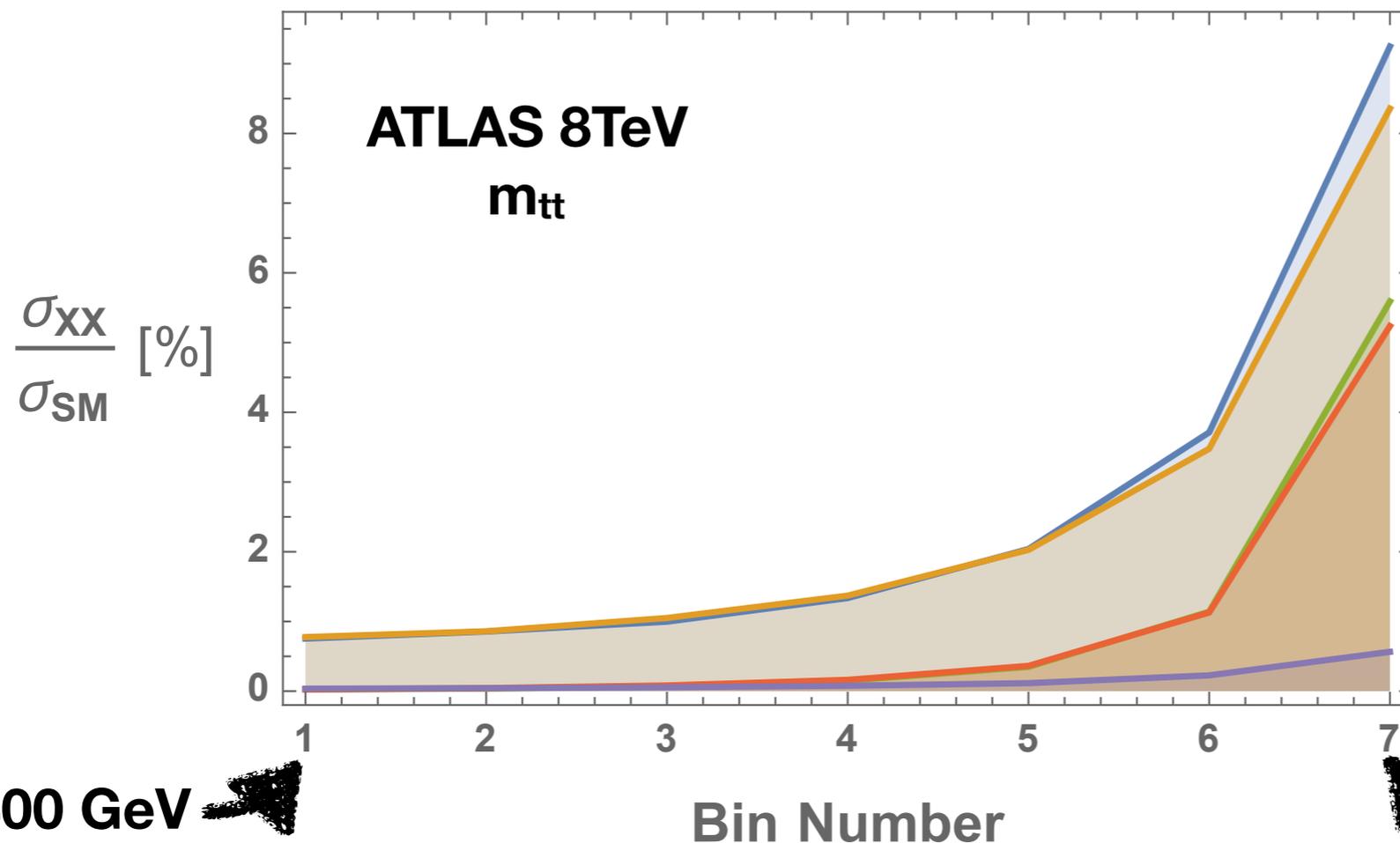
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$$\Lambda = 1 \text{ TeV}$$

LO



345-400 GeV

1100-1600 GeV

Resolving Degeneracies

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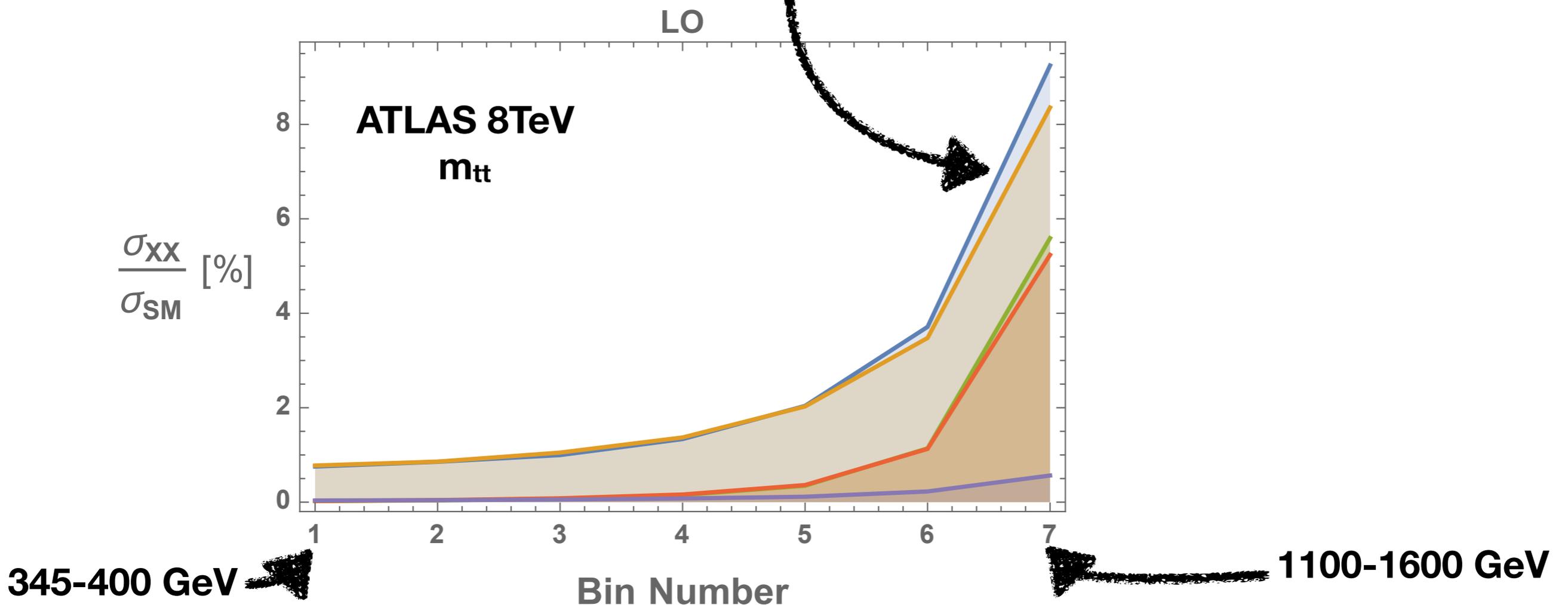
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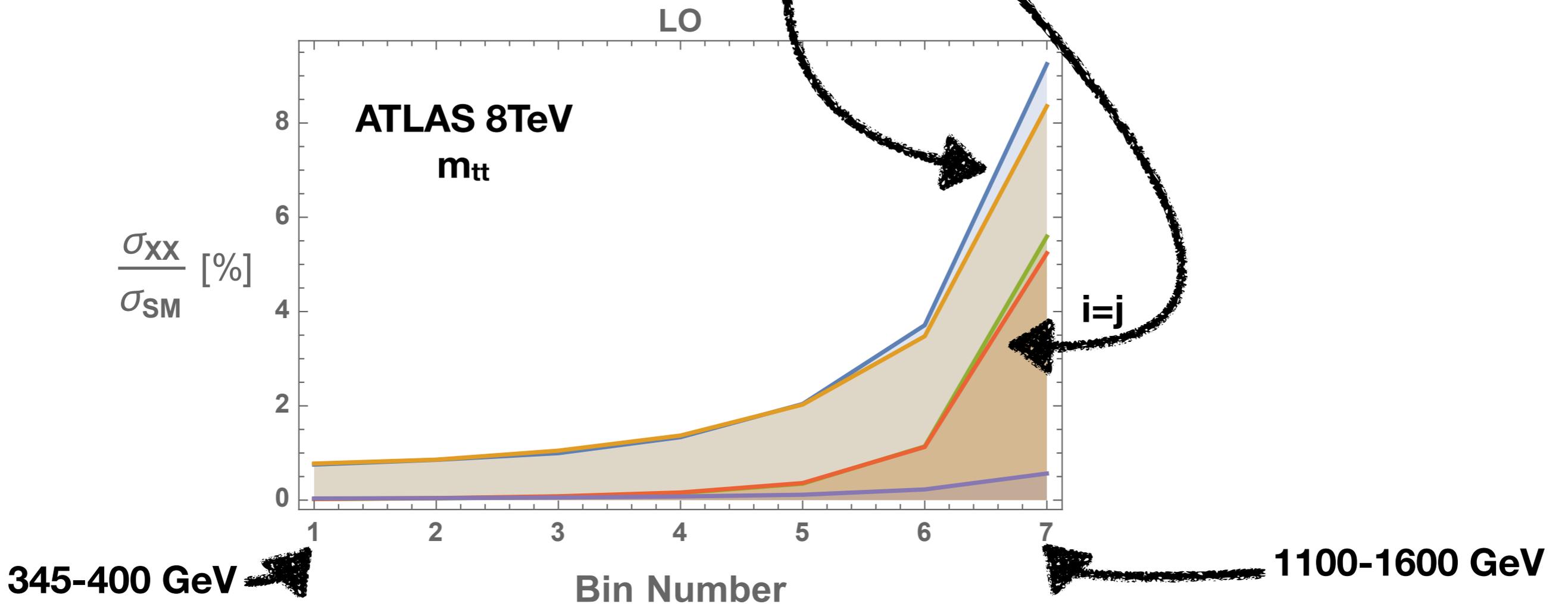
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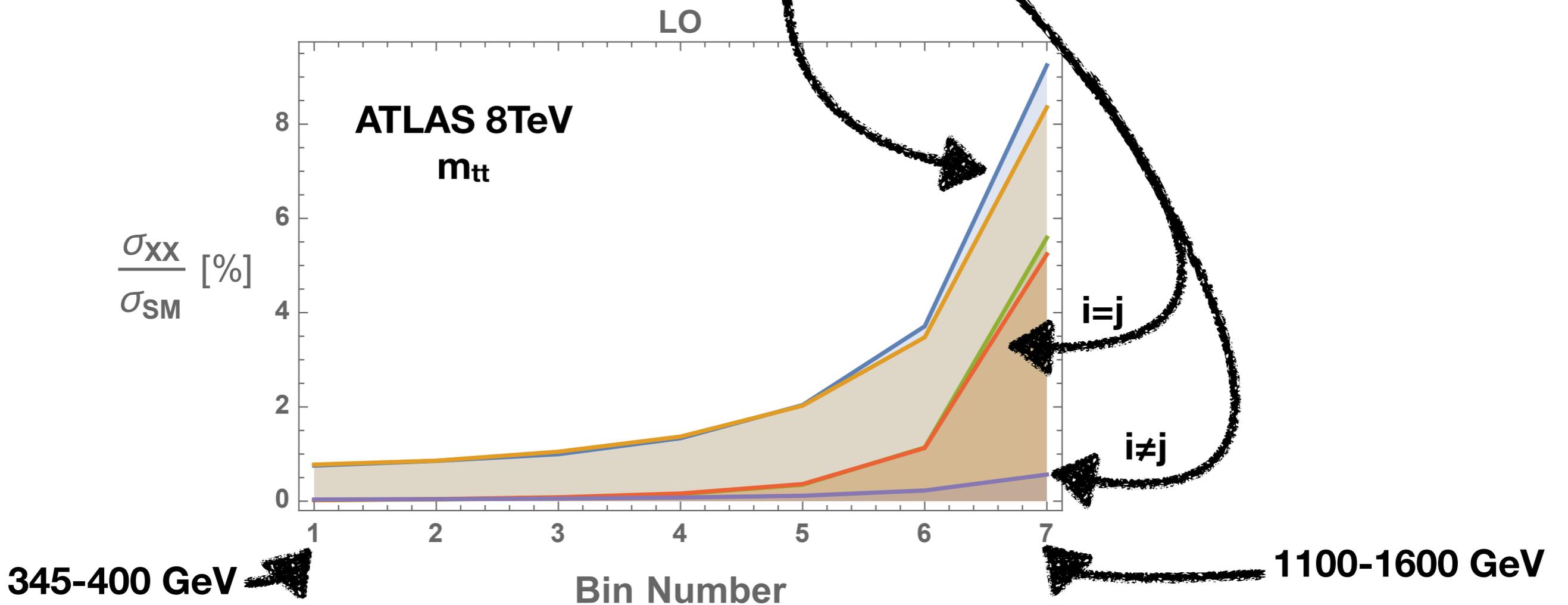
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Resolving Degeneracies

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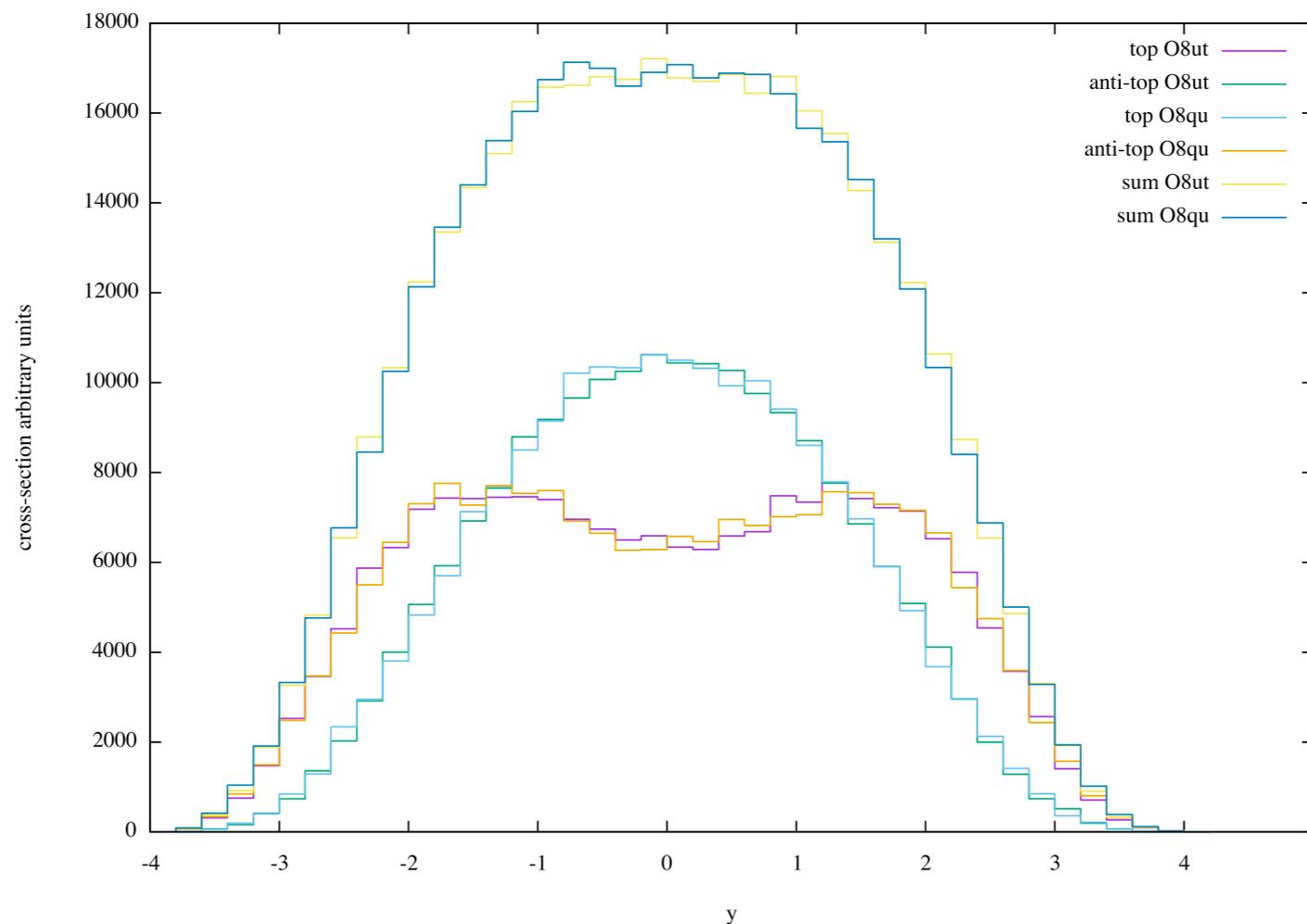


Figure: courtesy of Eleni Vryonidou

Resolving Degeneracies

$$Out8 = 2C_{uu}^{8(i33i)} (\bar{u}_i \gamma^\mu T^A u_i) (\bar{u}_3 \gamma_\mu T^A u_3) \quad \Bigg| \quad OQu8 = C_{qu}^{1(33ii)} (\bar{q}_3 \gamma^\mu T^A q_3) (\bar{u}_i \gamma_\mu T^A u_i)$$

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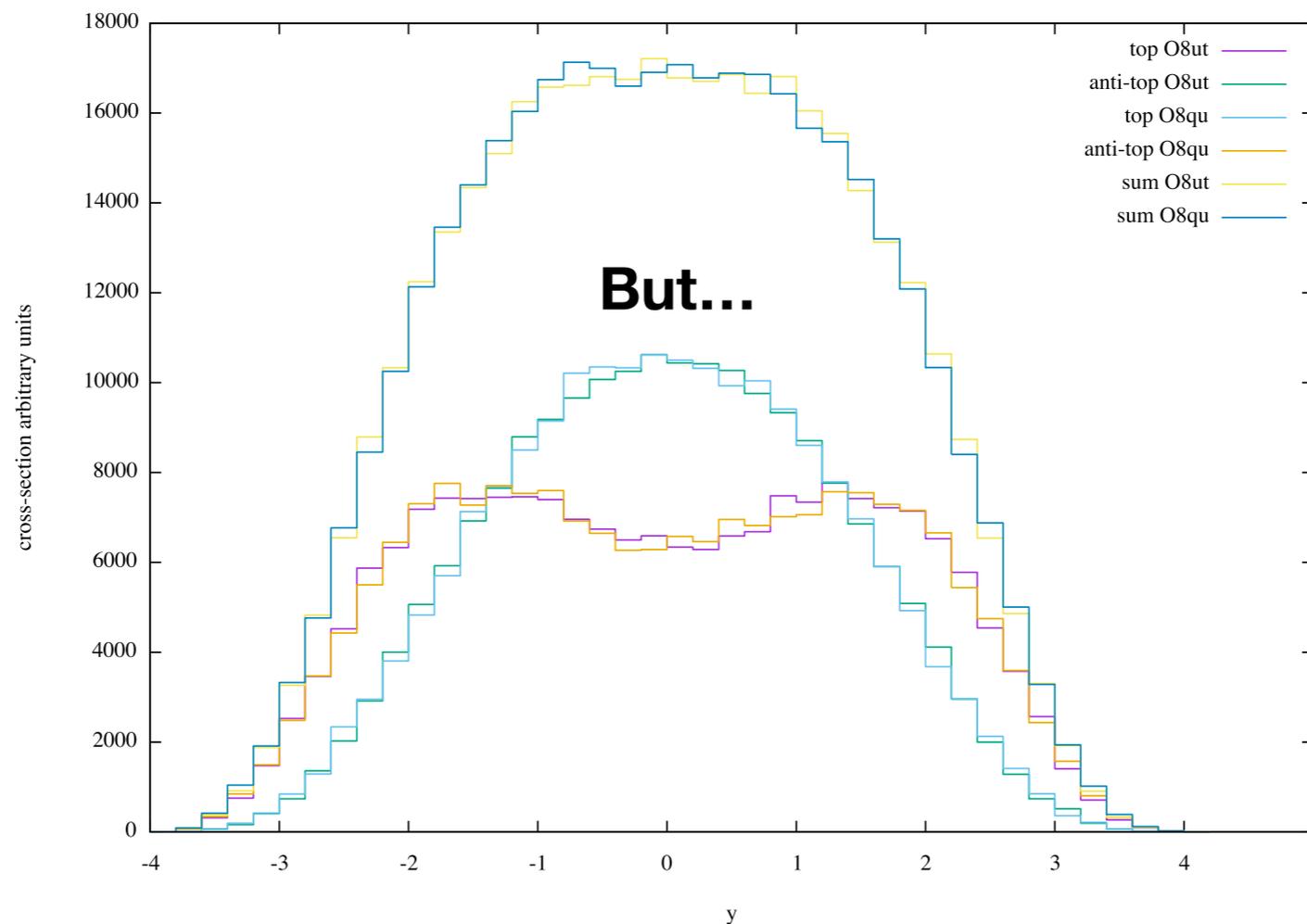


Figure: courtesy of Eleni Vryonidou

Resolving Degeneracies

Preliminary

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$$\sigma_{EFT} = \sigma_{SM} + \frac{\sigma_{L/R}}{\Lambda^2} (c_L + c_R) + \frac{\sigma_{LL/RR}}{\Lambda^4} (c_L^2 + c_R^2) + \frac{\sigma_{LR}}{\Lambda^4} (c_L c_R)$$

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Blind direction

Resolving Degeneracies

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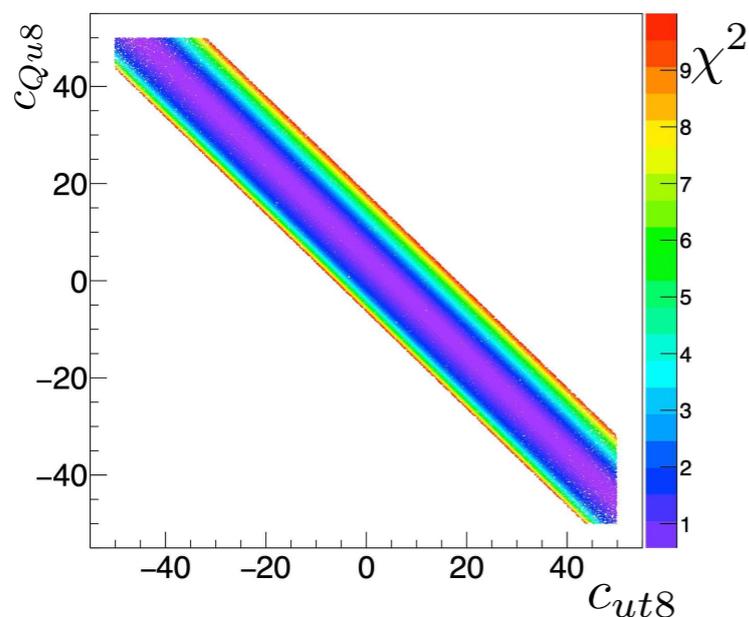
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Resolving Degeneracies

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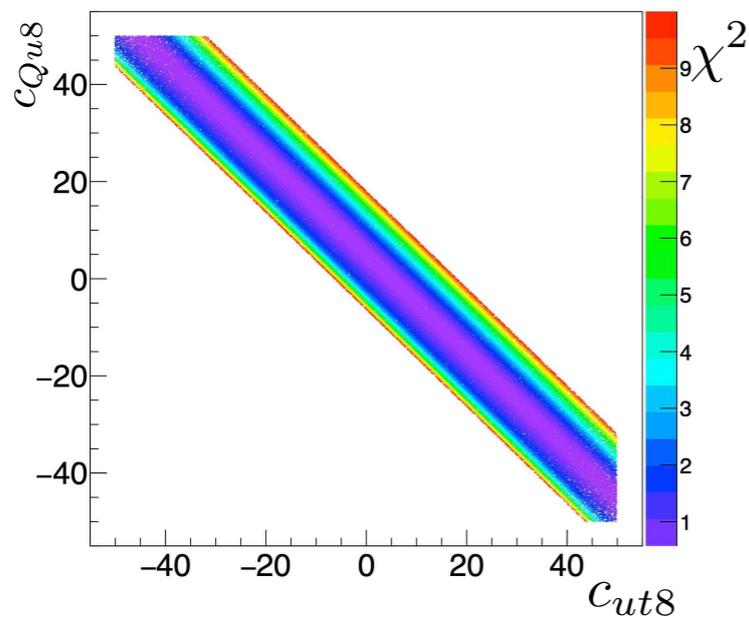
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Blind direction

Blind circle/disk



Resolving Degeneracies

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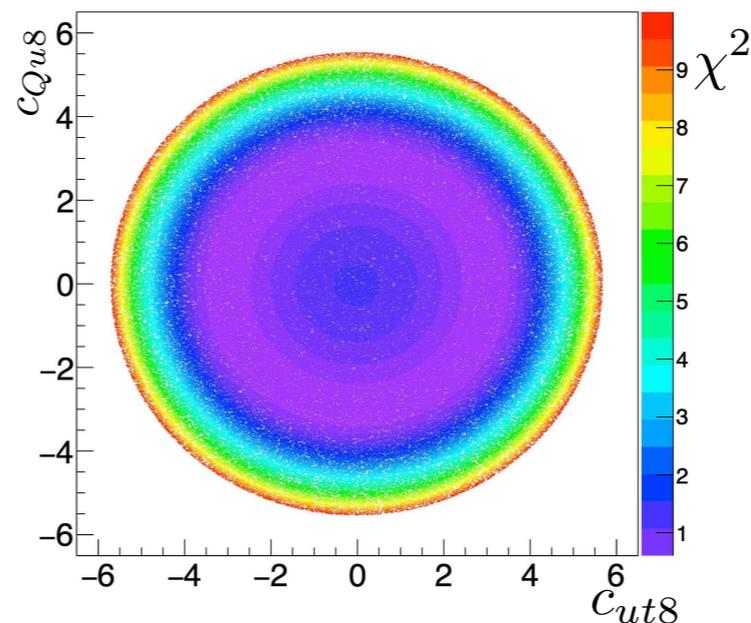
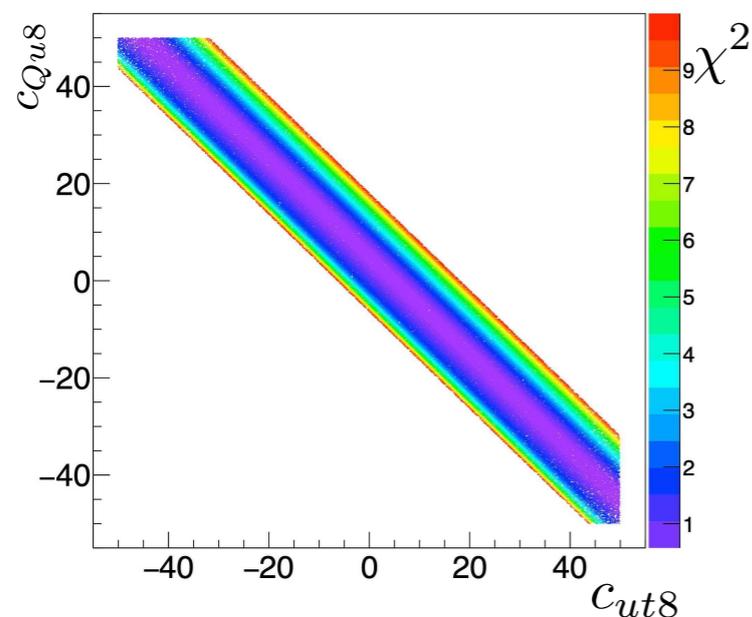
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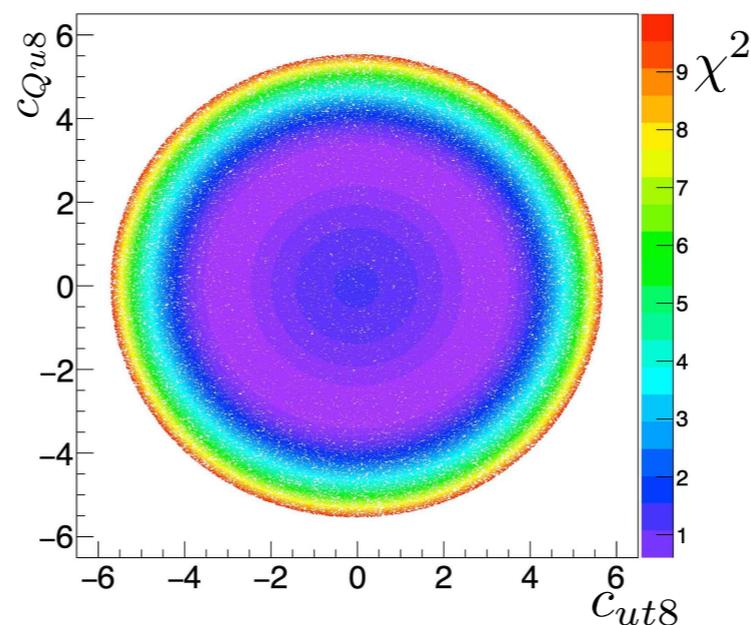
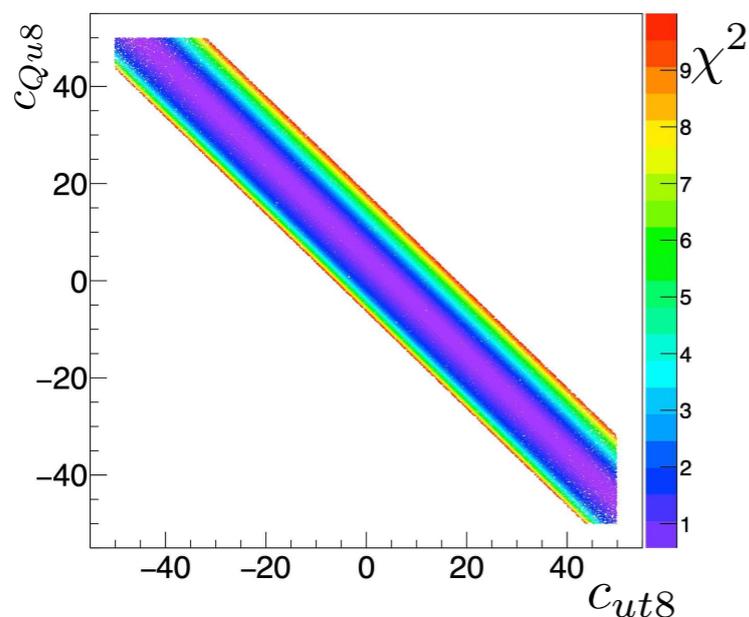
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Blind direction

Blind circle/disk

Blind hyperbola
(negligible)



Resolving Degeneracies

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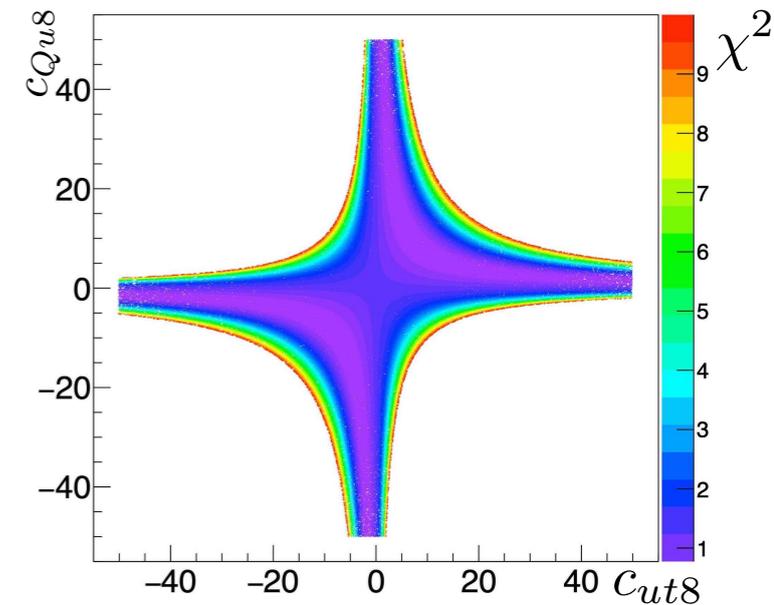
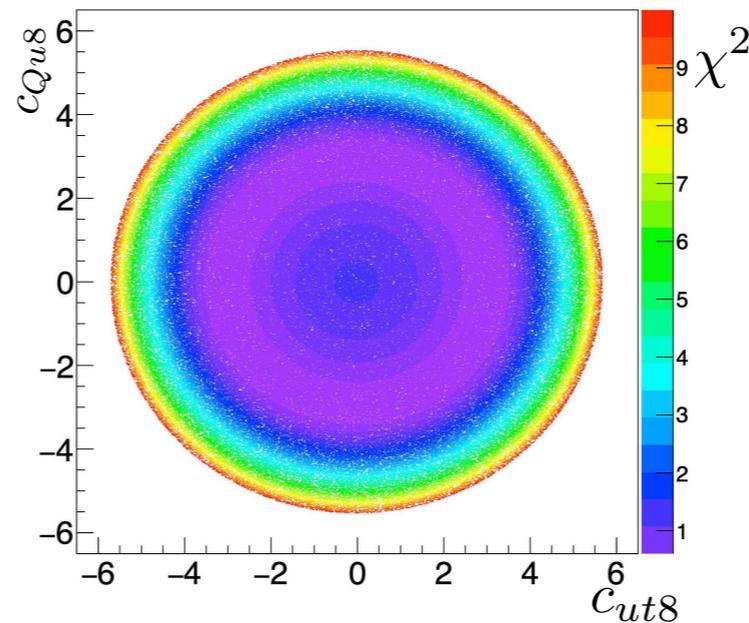
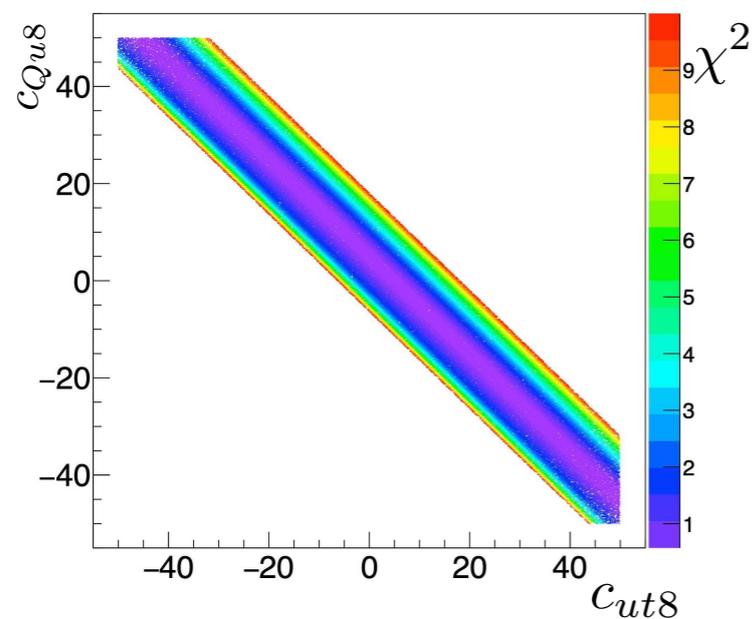
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Blind direction

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Blind hyperbola
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Resolving Degeneracies

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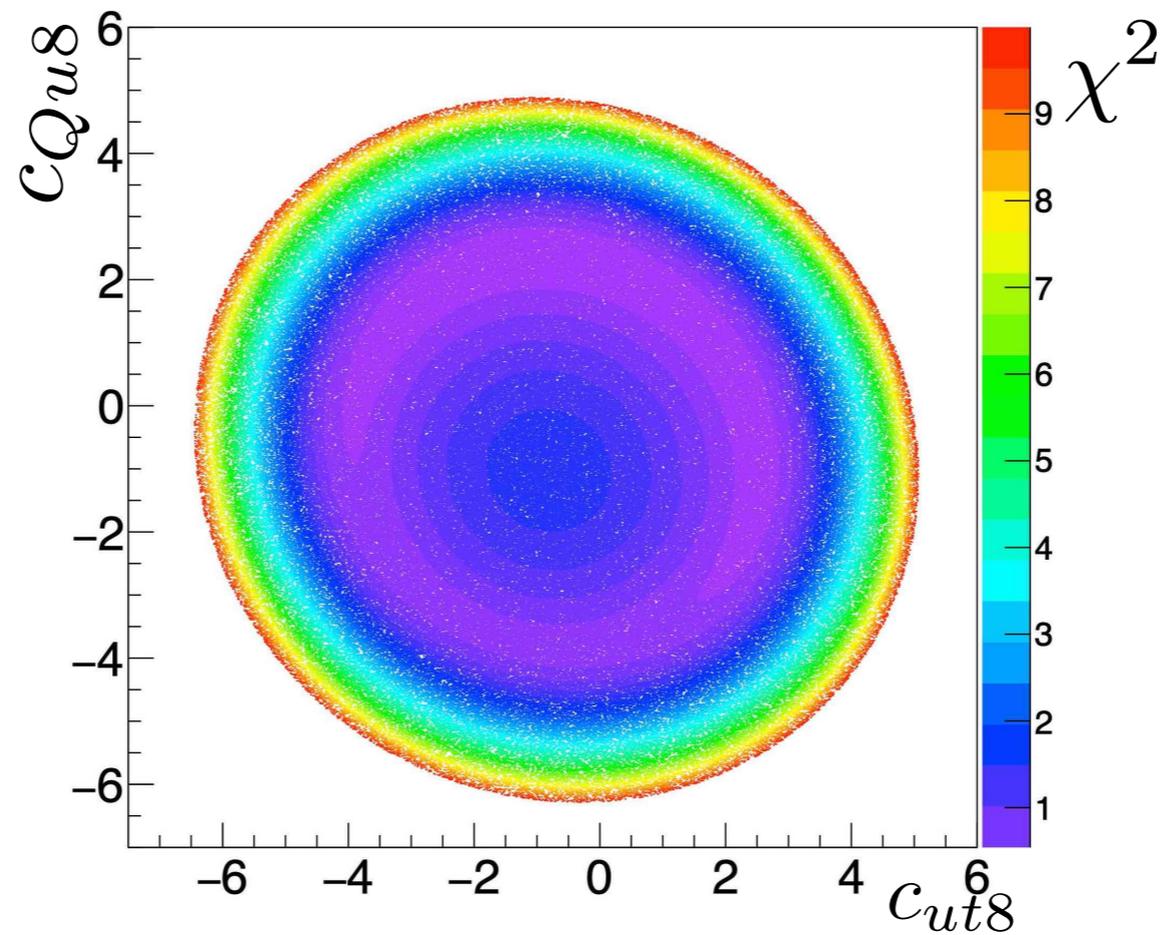
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- $\mathcal{O}(\Lambda^{-4})$ are important in resolving degeneracies due to their rapid growth with energy

Thank you

The Operators

25 four-fermion operators

$$OQq31 = C_{qq}^{3(ii33)} + \frac{1}{6} \left(C_{qq}^{1(i33i)} - C_{qq}^{3(i33i)} \right)$$

$$OQq38 = C_{qq}^{1(i33i)} - C_{qq}^{3(i33i)}$$

$$OQq18 = C_{qq}^{1(i33i)} + 3C_{qq}^{3(i33i)}$$

$$OQq11 = C_{qq}^{1(ii33)} + \frac{1}{6} C_{qq}^{1(i33i)} + \frac{1}{2} C_{qq}^{3(i33i)}$$

$$Oqt8 = C_{qu}^{8(ii33)}$$

$$Oqt1 = C_{qu}^{1(ii33)}$$

$$Out8 = 2C_{uu}^{(i33i)}$$

$$Out1 = C_{uu}^{(ii33)} + \frac{1}{3} C_{uu}^{(i33i)}$$

$$OQu8 = C_{qu}^{8(33ii)}$$

$$OQu1 = C_{qu}^{1(33ii)}$$

$$Odt8 = C_{ud}^{8(33ii)}$$

$$Odt1 = C_{ud}^{1(33ii)}$$

$$Oqd8 = C_{Qd}^{8(33ii)}$$

$$Oqd1 = C_{Qd}^{1(33ii)}$$

$$OQQ1 = 2C_{qq}^{1(3333)} - \frac{2}{3} C_{qq}^{3(3333)}$$

$$OQQ8 = 8C_{qq}^{3(3333)}$$

$$OQt1 = C_{qu}^{1(3333)}$$

$$OQt8 = C_{qu}^{8(3333)}$$

$$OQb1 = C_{qd}^{1(3333)}$$

$$OQb8 = C_{qd}^{8(3333)}$$

$$Ott1 = C_{uu}^{1(3333)}$$

$$Otb1 = C_{ud}^{1(3333)}$$

$$Otb8 = C_{ud}^{8(3333)}$$

$$OQtQb1 = C_{quqd}^{1(3333)}$$

$$OQtQb8 = C_{quqd}^{8(3333)}$$