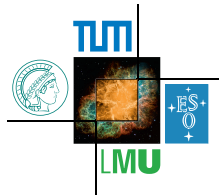


SMEFT-WET matching

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Outline

- 1 Introduction
- 2 Tree-level Matching
- 3 1-Loop Matching
- 4 Codes
- 5 Summary

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Motivation

No direct NP

NP indirectly through loops

Number of parameters

SMEFT: 2499

WET: 5963

Logs

Resummed: $\sum_N \alpha_s^N \log^N \left(\frac{\mu}{M_W} \right)$

Weak effective theory

(also LEFT, WEFT, weak Hamiltonians...)

Symmetry

$$SU(3)_C \times U(1)_{em}$$

Fields

$$u, d, c, s, b, \ell, \nu_\ell, g, \gamma$$

Poincaré invariance

Dim 6 operators

WET: Operators $d \leq 5$

d=3

fermion mass terms, $\mathcal{O}_\nu = (\nu_L^T C \nu_L)$

d=4

Kinetic terms, $\theta_{\text{QCD}} G_{\mu\nu}^A \tilde{G}^{A\mu\nu}$, $\theta_{\text{QED}} F_{\mu\nu} \tilde{F}^{\mu\nu}$

d=5

Dipoles: $(\bar{f} \sigma^{\mu\nu} f) F_{\mu\nu}$, $(\bar{q} \sigma^{\mu\nu} T^A q) G_{\mu\nu}^A$

WET: Operators $d = 6$

Gluonic

$$\mathcal{O}_G = f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$$

$$\mathcal{O}_{\tilde{G}} = f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$$

4 Fermi

$$(\bar{\psi}\Gamma_1\psi)(\bar{\psi}\Gamma_2\psi)$$

Vectors: $(\bar{L}L)(\bar{L}L)$, $(\bar{R}R)(\bar{R}R)$, $(\bar{L}L)(\bar{R}R)$

Scalars, Tensors: $(\bar{L}R)(\bar{L}R)$, $(\bar{L}R)(\bar{R}L) + \text{h.c.}$

\mathcal{B}, \mathcal{L}

4 leptons: $(\bar{\ell}^c\Gamma_1\ell)(\bar{\ell}\Gamma_2\ell)$, $(\bar{\ell}^c\Gamma_1\ell)(\bar{\ell}^c\Gamma_2\ell)$

2 leptons, 2 quarks: $(\bar{\ell}^c\Gamma_1\ell)(\bar{q}\Gamma_2q)$

1 lepton, 3 quarks: $(\bar{q}^c\Gamma_1q)(\bar{\ell}\Gamma_2q)$, $(\bar{q}^c\Gamma_1q)(\bar{q}^c\Gamma_2\ell)$

Dim ≤ 5 operators

$\nu\nu + \text{h.c.}$	$(\nu\nu)X + \text{h.c.}$	$(\bar{L}R)X + \text{h.c.}$	X^3
$\mathcal{O}_\nu \left (\nu_{Lp}^T C \nu_{Lr}) \right.$	$\mathcal{O}_{\nu\gamma} \left (\nu_{Lp}^T C \sigma^{\mu\nu} \nu_{Lr}) F_{\mu\nu} \right.$	$\mathcal{O}_{e\gamma} \left \bar{e}_{Lp} \sigma^{\mu\nu} e_{Rr} F_{\mu\nu} \right.$	$\mathcal{O}_G \left f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu} \right.$
		$\mathcal{O}_{u\gamma} \left \bar{u}_{Lp} \sigma^{\mu\nu} u_{Rr} F_{\mu\nu} \right.$	$\mathcal{O}_{\tilde{G}} \left f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu} \right.$
		$\mathcal{O}_{d\gamma} \left \bar{d}_{Lp} \sigma^{\mu\nu} d_{Rr} F_{\mu\nu} \right.$	
		$\mathcal{O}_{uG} \left \bar{u}_{Lp} \sigma^{\mu\nu} T^A u_{Rr} G_{\mu\nu}^A \right.$	
		$\mathcal{O}_{dG} \left \bar{d}_{Lp} \sigma^{\mu\nu} T^A d_{Rr} G_{\mu\nu}^A \right.$	

$(\overline{LL})(\overline{LL})$		$(\overline{LL})(\overline{RR})$		$(\overline{LR})(\overline{LR}) + \text{h.c.}$	
$\mathcal{O}_{\nu\nu}^{V,LL}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{\nu}_{Ls}\gamma_\mu\nu_{Lt})$	$\mathcal{O}_{\nu e}^{V,LR}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{e}_{Rs}\gamma_\mu e_{Rt})$	$\mathcal{O}_{ee}^{S,RR}$	$(\bar{e}_{Lp}e_{Rr})(\bar{e}_{Ls}e_{Rt})$
$\mathcal{O}_{ee}^{V,LL}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{e}_{Ls}\gamma_\mu e_{Lt})$	$\mathcal{O}_{e\bar{e}}^{V,LR}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{e}_{Rs}\gamma_\mu e_{Rt})$	$\mathcal{O}_{eu}^{S,RR}$	$(\bar{e}_{Lp}e_{Rr})(\bar{u}_{Ls}u_{Rt})$
$\mathcal{O}_{\nu e}^{V,LL}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{e}_{Ls}\gamma_\mu e_{Lt})$	$\mathcal{O}_{\nu u}^{V,LR}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$	$\mathcal{O}_{eu}^{T,RR}$	$(\bar{e}_{Lp}\sigma^{\mu\nu}e_{Rr})(\bar{u}_{Ls}\sigma_{\mu\nu}u_{Rt})$
$\mathcal{O}_{\nu u}^{V,LL}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{u}_{Ls}\gamma_\mu u_{Lt})$	$\mathcal{O}_{\nu d}^{V,LR}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$	$\mathcal{O}_{ed}^{S,RR}$	$(\bar{e}_{Lp}e_{Rr})(\bar{d}_{Ls}d_{Rt})$
$\mathcal{O}_{\nu d}^{V,LL}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{d}_{Ls}\gamma_\mu d_{Lt})$	$\mathcal{O}_{eu}^{V,LR}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$	$\mathcal{O}_{ed}^{T,RR}$	$(\bar{e}_{Lp}\sigma^{\mu\nu}e_{Rr})(\bar{d}_{Ls}\sigma_{\mu\nu}d_{Rt})$
$\mathcal{O}_{eu}^{V,LL}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{u}_{Ls}\gamma_\mu u_{Lt})$	$\mathcal{O}_{ed}^{V,LR}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$	$\mathcal{O}_{\nu u}^{S,RR}$	$(\bar{\nu}_{Lp}e_{Rr})(\bar{d}_{Ls}u_{Rt})$
$\mathcal{O}_{ed}^{V,LL}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{d}_{Ls}\gamma_\mu d_{Lt})$	$\mathcal{O}_{ue}^{V,LR}$	$(\bar{u}_{Lp}\gamma^\mu u_{Lr})(\bar{e}_{Rs}\gamma_\mu e_{Rt})$	$\mathcal{O}_{\nu u}^{T,RR}$	$(\bar{\nu}_{Lp}\sigma^{\mu\nu}e_{Rr})(\bar{d}_{Ls}\sigma_{\mu\nu}u_{Rt})$
$\mathcal{O}_{vedu}^{V,LL}$	$(\bar{\nu}_{Lp}\gamma^\mu e_{Lr})(\bar{d}_{Ls}\gamma_\mu u_{Lt}) + \text{h.c.}$	$\mathcal{O}_{de}^{V,LR}$	$(\bar{d}_{Lp}\gamma^\mu d_{Lr})(\bar{e}_{Rs}\gamma_\mu e_{Rt})$	$\mathcal{O}_{uu}^{S1,RR}$	$(\bar{u}_{Lp}u_{Rr})(\bar{u}_{Ls}u_{Rt})$
$\mathcal{O}_{uu}^{V,LL}$	$(\bar{u}_{Lp}\gamma^\mu u_{Lr})(\bar{u}_{Ls}\gamma_\mu u_{Lt})$	$\mathcal{O}_{vedu}^{V,LR}$	$(\bar{\nu}_{Lp}\gamma^\mu e_{Lr})(\bar{d}_{Rs}\gamma_\mu u_{Rt}) + \text{h.c.}$	$\mathcal{O}_{uu}^{S8,RR}$	$(\bar{u}_{Lp}T^A u_{Rr})(\bar{u}_{Ls}T^A u_{Rt})$
$\mathcal{O}_{ud}^{V,LL}$	$(\bar{d}_{Lp}\gamma^\mu d_{Lr})(\bar{d}_{Ls}\gamma_\mu d_{Lt})$	$\mathcal{O}_{uu}^{V1,LR}$	$(\bar{u}_{Lp}\gamma^\mu u_{Lr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$	$\mathcal{O}_{ud}^{S1,RR}$	$(\bar{u}_{Lp}u_{Rr})(\bar{d}_{Ls}d_{Rt})$
$\mathcal{O}_{ud}^{V1,LL}$	$(\bar{u}_{Lp}\gamma^\mu u_{Lr})(\bar{d}_{Ls}\gamma_\mu d_{Lt})$	$\mathcal{O}_{uu}^{V8,LR}$	$(\bar{u}_{Lp}\gamma^\mu T^A u_{Lr})(\bar{u}_{Rs}\gamma_\mu T^A u_{Rt})$	$\mathcal{O}_{ud}^{S8,RR}$	$(\bar{u}_{Lp}T^A u_{Rr})(\bar{d}_{Ls}T^A d_{Rt})$
$\mathcal{O}_{ud}^{V8,LL}$	$(\bar{u}_{Lp}\gamma^\mu T^A u_{Lr})(\bar{d}_{Ls}\gamma_\mu T^A d_{Lt})$	$\mathcal{O}_{ud}^{V1,LR}$	$(\bar{u}_{Lp}\gamma^\mu u_{Lr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$	$\mathcal{O}_{dd}^{S1,RR}$	$(\bar{d}_{Lp}d_{Rr})(\bar{d}_{Ls}d_{Rt})$
$(\overline{RR})(\overline{RR})$		$\mathcal{O}_{ud}^{V8,LR}$	$(\bar{u}_{Lp}\gamma^\mu T^A u_{Lr})(\bar{d}_{Rs}\gamma_\mu T^A d_{Rt})$	$\mathcal{O}_{dd}^{S8,RR}$	$(\bar{d}_{Lp}T^A d_{Rr})(\bar{d}_{Ls}T^A d_{Rt})$
$\mathcal{O}_{ee}^{V,RR}$	$(\bar{e}_{Rp}\gamma^\mu e_{Rr})(\bar{e}_{Rs}\gamma_\mu e_{Rt})$	$\mathcal{O}_{du}^{V1,LR}$	$(\bar{d}_{Lp}\gamma^\mu d_{Lr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$	$\mathcal{O}_{uddu}^{S1,RR}$	$(\bar{u}_{Lp}d_{Rr})(\bar{d}_{Ls}u_{Rt})$
$\mathcal{O}_{eu}^{V,RR}$	$(\bar{e}_{Rp}\gamma^\mu e_{Rr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$	$\mathcal{O}_{du}^{V8,LR}$	$(\bar{d}_{Lp}\gamma^\mu T^A d_{Lr})(\bar{u}_{Rs}\gamma_\mu T^A u_{Rt})$	$\mathcal{O}_{uddu}^{S8,RR}$	$(\bar{u}_{Lp}T^A d_{Rr})(\bar{d}_{Ls}T^A u_{Rt})$
$\mathcal{O}_{ed}^{V,RR}$	$(\bar{e}_{Rp}\gamma^\mu e_{Rr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$	$\mathcal{O}_{dd}^{V1,LR}$	$(\bar{d}_{Lp}\gamma^\mu d_{Lr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$	$(\overline{LR})(\overline{RL}) + \text{h.c.}$	
$\mathcal{O}_{uu}^{V,RR}$	$(\bar{u}_{Rp}\gamma^\mu u_{Rr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$	$\mathcal{O}_{dd}^{V8,LR}$	$(\bar{d}_{Lp}\gamma^\mu T^A d_{Lr})(\bar{d}_{Rs}\gamma_\mu T^A d_{Rt})$	$\mathcal{O}_{eu}^{S,RL}$	$(\bar{e}_{Lp}e_{Rr})(\bar{u}_{Rs}u_{Lt})$
$\mathcal{O}_{dd}^{V,RR}$	$(\bar{d}_{Rp}\gamma^\mu d_{Rr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$	$\mathcal{O}_{uddu}^{V1,LR}$	$(\bar{u}_{Lp}\gamma^\mu d_{Lr})(\bar{d}_{Rs}\gamma_\mu u_{Rt}) + \text{h.c.}$	$\mathcal{O}_{ed}^{S,RL}$	$(\bar{e}_{Lp}e_{Rr})(\bar{d}_{Rs}d_{Lt})$
$\mathcal{O}_{ud}^{V1,RR}$	$(\bar{u}_{Rp}\gamma^\mu u_{Rr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$	$\mathcal{O}_{uddu}^{V8,LR}$	$(\bar{u}_{Lp}\gamma^\mu T^A d_{Lr})(\bar{d}_{Rs}\gamma_\mu T^A u_{Rt}) + \text{h.c.}$	$\mathcal{O}_{vedu}^{S,RL}$	$(\bar{\nu}_{Lp}e_{Rr})(\bar{d}_{Rs}u_{Lt})$
$\mathcal{O}_{ud}^{V8,RR}$	$(\bar{u}_{Rp}\gamma^\mu T^A u_{Rr})(\bar{d}_{Rs}\gamma_\mu T^A d_{Rt})$				

$\Delta L = 4 + \text{h.c.}$

$$\mathcal{O}_{\nu\nu}^{S,LL} \left| (\nu_{Lp}^T C \nu_{Lr}) (\nu_{Ls}^T C \nu_{Lt}) \right.$$

$\Delta L = 2 + \text{h.c.}$

$\Delta B = \Delta L = 1 + \text{h.c.}$

$\Delta B = -\Delta L = 1 + \text{h.c.}$

$\mathcal{O}_{\nu e}^{S,LL}$	$(\nu_{Lp}^T C \nu_{Lr})(\bar{e}_{Rs} e_{Lt})$	$\mathcal{O}_{udd}^{S,LL}$	$\epsilon_{\alpha\beta\gamma} (u_{Lp}^{\alpha T} C d_{Lr}^{\beta}) (d_{Ls}^{\gamma T} C \nu_{Lt})$	$\mathcal{O}_{ddd}^{S,LL}$	$\epsilon_{\alpha\beta\gamma} (d_{Lp}^{\alpha T} C d_{Lr}^{\beta}) (\bar{e}_{Rs} d_{Lt}^{\gamma})$
$\mathcal{O}_{\nu e}^{T,LL}$	$(\nu_{Lp}^T C \sigma^{\mu\nu} \nu_{Lr})(\bar{e}_{Rs} \sigma_{\mu\nu} e_{Lt})$	$\mathcal{O}_{duu}^{S,LL}$	$\epsilon_{\alpha\beta\gamma} (d_{Lp}^{\alpha T} C u_{Lr}^{\beta}) (u_{Ls}^{\gamma T} C e_{Lt})$	$\mathcal{O}_{udd}^{S,LR}$	$\epsilon_{\alpha\beta\gamma} (u_{Lp}^{\alpha T} C d_{Lr}^{\beta}) (\bar{\nu}_{Ls} d_{Rt}^{\gamma})$
$\mathcal{O}_{\nu e}^{S,LR}$	$(\nu_{Lp}^T C \nu_{Lr})(\bar{e}_{Ls} e_{Rt})$	$\mathcal{O}_{uud}^{S,LR}$	$\epsilon_{\alpha\beta\gamma} (u_{Lp}^{\alpha T} C u_{Lr}^{\beta}) (d_{Rs}^{\gamma T} C e_{Rt})$	$\mathcal{O}_{ddu}^{S,LR}$	$\epsilon_{\alpha\beta\gamma} (d_{Lp}^{\alpha T} C d_{Lr}^{\beta}) (\bar{\nu}_{Ls} u_{Rt}^{\gamma})$
$\mathcal{O}_{\nu u}^{S,LL}$	$(\nu_{Lp}^T C \nu_{Lr})(\bar{u}_{Rs} u_{Lt})$	$\mathcal{O}_{duu}^{S,LR}$	$\epsilon_{\alpha\beta\gamma} (d_{Lp}^{\alpha T} C u_{Lr}^{\beta}) (u_{Rs}^{\gamma T} C e_{Rt})$	$\mathcal{O}_{ddd}^{S,LR}$	$\epsilon_{\alpha\beta\gamma} (d_{Lp}^{\alpha T} C d_{Lr}^{\beta}) (\bar{e}_{Ls} d_{Rt}^{\gamma})$
$\mathcal{O}_{\nu u}^{T,LL}$	$(\nu_{Lp}^T C \sigma^{\mu\nu} \nu_{Lr})(\bar{u}_{Rs} \sigma_{\mu\nu} u_{Lt})$	$\mathcal{O}_{uud}^{S,RL}$	$\epsilon_{\alpha\beta\gamma} (u_{Rp}^{\alpha T} C u_{Rr}^{\beta}) (d_{Ls}^{\gamma T} C e_{Lt})$	$\mathcal{O}_{ddd}^{S,RL}$	$\epsilon_{\alpha\beta\gamma} (d_{Rp}^{\alpha T} C d_{Rr}^{\beta}) (\bar{e}_{Rs} d_{Lt}^{\gamma})$
$\mathcal{O}_{\nu u}^{S,LR}$	$(\nu_{Lp}^T C \nu_{Lr})(\bar{u}_{Ls} u_{Rt})$	$\mathcal{O}_{duu}^{S,RL}$	$\epsilon_{\alpha\beta\gamma} (d_{Rp}^{\alpha T} C u_{Rr}^{\beta}) (u_{Ls}^{\gamma T} C e_{Lt})$	$\mathcal{O}_{udd}^{S,RR}$	$\epsilon_{\alpha\beta\gamma} (u_{Rp}^{\alpha T} C d_{Rr}^{\beta}) (\bar{\nu}_{Ls} d_{Rt}^{\gamma})$
$\mathcal{O}_{\nu d}^{S,LL}$	$(\nu_{Lp}^T C \nu_{Lr})(\bar{d}_{Rs} d_{Lt})$	$\mathcal{O}_{dud}^{S,RL}$	$\epsilon_{\alpha\beta\gamma} (d_{Rp}^{\alpha T} C u_{Rr}^{\beta}) (d_{Ls}^{\gamma T} C \nu_{Lt})$	$\mathcal{O}_{ddd}^{S,RR}$	$\epsilon_{\alpha\beta\gamma} (d_{Rp}^{\alpha T} C d_{Rr}^{\beta}) (\bar{e}_{Ls} d_{Rt}^{\gamma})$
$\mathcal{O}_{\nu d}^{T,LL}$	$(\nu_{Lp}^T C \sigma^{\mu\nu} \nu_{Lr})(\bar{d}_{Rs} \sigma_{\mu\nu} d_{Lt})$	$\mathcal{O}_{ddu}^{S,RL}$	$\epsilon_{\alpha\beta\gamma} (d_{Rp}^{\alpha T} C d_{Rr}^{\beta}) (u_{Ls}^{\gamma T} C \nu_{Lt})$		
$\mathcal{O}_{\nu d}^{S,LR}$	$(\nu_{Lp}^T C \nu_{Lr})(\bar{d}_{Ls} d_{Rt})$	$\mathcal{O}_{duu}^{S,RR}$	$\epsilon_{\alpha\beta\gamma} (d_{Rp}^{\alpha T} C u_{Rr}^{\beta}) (u_{Rs}^{\gamma T} C e_{Rt})$		
$\mathcal{O}_{\nu du}^{S,LL}$	$(\nu_{Lp}^T C e_{Lr})(\bar{d}_{Rs} u_{Lt})$				
$\mathcal{O}_{\nu du}^{T,LL}$	$(\nu_{Lp}^T C \sigma^{\mu\nu} e_{Lr})(\bar{d}_{Rs} \sigma_{\mu\nu} u_{Lt})$				
$\mathcal{O}_{\nu du}^{S,LR}$	$(\nu_{Lp}^T C e_{Lr})(\bar{d}_{Ls} u_{Rt})$				
$\mathcal{O}_{\nu du}^{V,RL}$	$(\nu_{Lp}^T C \gamma^{\mu} e_{Rr})(\bar{d}_{Ls} \gamma_{\mu} u_{Lt})$				
$\mathcal{O}_{\nu du}^{V,RR}$	$(\nu_{Lp}^T C \gamma^{\mu} e_{Rr})(\bar{d}_{Rs} \gamma_{\mu} u_{Rt})$				

Matching

Degrees of freedom reduced

$$\mathcal{L}_{\text{SMEFT}}(l, \nu_l, u, d, c, s, v, t, g, \gamma, W, Z, h)$$
$$\hookrightarrow \mathcal{L}_{\text{WET}}(l, \nu_l, u, d, c, s, v, \cancel{\lambda}, g, \gamma, \cancel{W}, \cancel{Z}, \cancel{h})$$

Matching scale μ_W

$$A_{\text{WET}} \stackrel{!}{=} A_{\text{SMEFT}}$$

Basis

Up-mass basis

Big picture

Energy scale

Theory

Λ

$$\mathcal{L}_{full} = ?$$

Integrating out
unknown fields

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM}^{(4)} + \frac{1}{\Lambda} \sum_k \tilde{C}_k^{(5)} Q_k^{(5)} + \frac{1}{\Lambda^2} \sum_k \tilde{C}_k^{(6)} Q_k^{(6)} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right)$$

μ_W

Integrating out heavy
SM fields W,Z,h,t

$$\mathcal{L}_{WET} = \mathcal{L}_{QED+QCD} + \sum_k C_k^{(6)} \mathcal{O}_k^{(6)}$$

μ_b

Big picture

Energy scale

Theory

Λ

$$\mathcal{L}_{full} = ?$$

Integrating out
unknown fields

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM}^{(4)} + \frac{1}{\Lambda} \sum_k \tilde{C}_k^{(5)} Q_k^{(5)} + \frac{1}{\Lambda^2} \sum_k \tilde{C}_k^{(6)} Q_k^{(6)} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right)$$

μ_W

Integrating out heavy
SM fields W,Z,h,t

$$\mathcal{L}_{WET} = \mathcal{L}_{QED+QCD} + \sum_k C_k^{(6)} \mathcal{O}_k^{(6)}$$

μ_b

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Tree-level

Expansion

External momenta, masses

Power counting

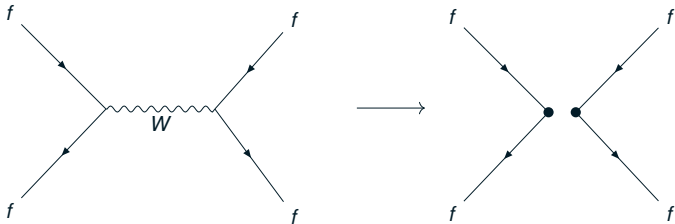
$$\dots \frac{1}{\Lambda^n} = \dots \underbrace{\frac{1}{v^n}}_{\text{WETcounting}} \times \underbrace{\frac{v^n}{\Lambda^n}}_{\text{SMEFTcounting}}$$

Tree-level Matching

Completely known

Jenkins/Manohar/Stoffer: 1709.04486

Tree-level: Example



$$\frac{1}{p^2 - M_W^2} = \frac{-1}{M_W^2} \frac{1}{1 - \frac{p^2}{M_W^2}} = \frac{-1}{M_W^2} (1 + \mathcal{O}(p^2/M_W^2))$$

Tree-level matching

Couplings

Shifted after EWSB

Contact terms

one-to-one

Modified Z, W, H exchange

Tree-diagrams

Couplings

Masses

$$M_f = \frac{\bar{v}}{\sqrt{2}} \left[Y_f - \frac{1}{2} v^2 C_{\psi\varphi}^* \right], \quad \mathcal{O}_{\psi\varphi} = (\varphi^\dagger \varphi) (\bar{\psi}_L \psi_R \varphi)$$

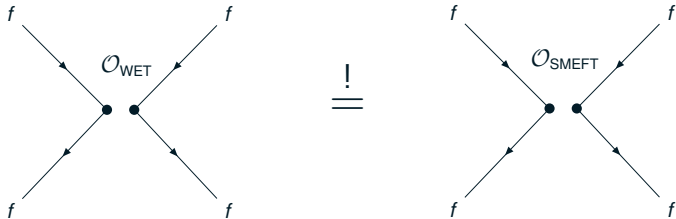
$$\bar{v} = v \left(1 + \frac{3C_\varphi v^2}{8\lambda} \right), \quad \mathcal{O}_\varphi = (\varphi^\dagger \varphi)^3$$

Gauge couplings

$$g_s = \bar{g}_3 = g_3 (1 + C_{\varphi G} \bar{v}^2), \quad \mathcal{O}_{\varphi G} = (\varphi^\dagger \varphi) G_{\mu\nu}^A G^{A, \mu\nu}$$

$$e = \bar{g}_2 \sin \bar{\theta} - \frac{1}{2} \cos \bar{\theta} \bar{g}_2 \bar{v}^2 C_{\varphi WB}, \quad \mathcal{O}_{\varphi WB} = (\varphi^\dagger \tau^I \varphi) W_{\mu\nu}^I B^{\mu\nu}$$

Contact terms



4-Fermi

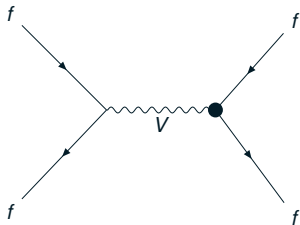
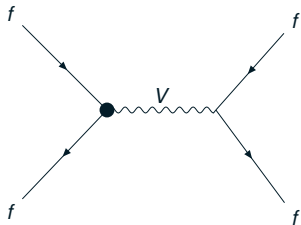
All sectors: V,S,T

Others

dipoles: $C_{f\gamma}$, C_{fG}

gluonic: C_G , $C_{\tilde{G}}$

Tree-level: Vectors



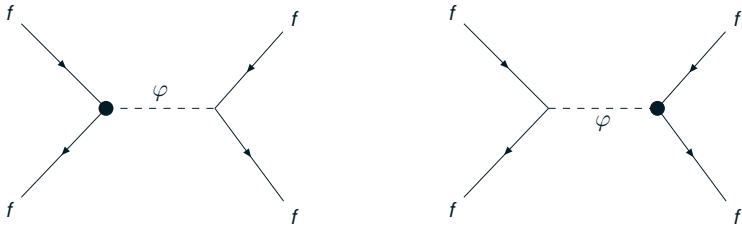
Modified W

$\mathcal{O}_{\varphi q}^{(3)}, \mathcal{O}_{\varphi l}^{(3)}, \mathcal{O}_{\varphi ud}$: Example: $\mathcal{O}_{\varphi ud} = (\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}\gamma^\mu d) \rightarrow \frac{1}{2}v^2 C_{\varphi ud}(\bar{u}\gamma^\mu d)$

Modified Z

$\mathcal{O}_{\varphi q}^{(1),(3)}, \mathcal{O}_{\varphi l}^{(1),(3)}, \mathcal{O}_{\varphi u}, \mathcal{O}_{\varphi d}, \mathcal{O}_{\varphi e}$

Tree-level: Higgs



Higgs

vertex² $\sim (m/v)^2, mv/\Lambda^2, v^4/\Lambda^4 \rightarrow$ dim 7 or 8 contribution

No tree-level contribution

Vector 4-fermi

$$O_{uddu}^{V8,LR}$$

Scalars, Tensors

$$O_{eu}^{S,RL}, O_{ee}^{S,RL}, O_{ed}^{S,RR}, O_{ed}^{T,RR}, O_{dd,uu}^{S1,RR}, O_{dd,uu}^{S8,RR}$$

$$\Delta L = 4, 3, \pm 1 \text{ and } \Delta B = 1$$

$$\text{e.g. } O_{\nu\gamma}$$

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1-Loop Matching

Motivation

larger parameter space explored

Many partial results

Weinberg operator

LFV

TGC

$\Delta F = 2$, B physics

...

Full 1-Loop Matching

still missing

Checks

Gauge invariance

Unitary, R_ξ

Renormalization

Alonso/Jenkins/Manohar/Trott: 1308.2627, 1310.4838, 1312.2014

Stoffer/Jenkins/Manohar: 1711.05270

Anomalous dimension matrix

IR behaviour

Divergences

Dipole to Weinberg operator

Kamenik/Papucci/Weiler: 1107.3143

Top dipole

Neutron EDM

Operator

\mathcal{O}_{uG}

Matched

$$\mathcal{O}_{\tilde{G}} = f^{ABC} \tilde{G}_{\mu}^{A,\nu} G_{\nu}^{B,\rho} G_{\rho}^{C,\mu}$$



Lepton flavour violation

Crivellin/Najjari/Rosiek: 1312.0634

LFV

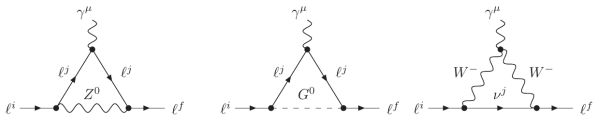
$l \rightarrow l' \gamma$, $Z \rightarrow ll'$, 3-body decays

Operators

4-lepton, semileptonic, Modified Z- W couplings, \mathcal{O}_{eB} , \mathcal{O}_{eW}

Matched

$\mathcal{O}_{e\gamma}$, $\mathcal{O}_{ee}^{V,LL}$, $\mathcal{O}_{ee}^{V,RR}$, $\mathcal{O}_{ee}^{V,LR}$, $\mathcal{O}_{ee}^{S,RR}$



Triple gauge couplings

Bobeth/Haisch: 1503.04829

Dipole and semileptonic operators

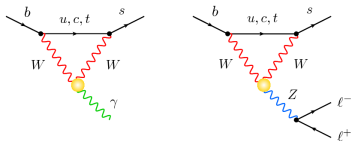
$$b \rightarrow s\gamma, K \rightarrow \pi\nu\bar{\nu}, \epsilon'/\epsilon$$

Operators

$$\mathcal{O}_{\varphi B}, \mathcal{O}_{\varphi W}, \mathcal{O}_W$$

Matched

$$\mathcal{O}_{e\gamma}, \mathcal{O}_{ed}^{V,LL}, \mathcal{O}_{ed}^{V,RR}$$



$b \rightarrow s, b \rightarrow c$

JA/Crivellin/Fael/Greub: 1512.02830

Full tree-level

$$\Delta B = \Delta S = 2, 1, \Delta B = \Delta C = 1$$

'NLO' 1loop

Only t_R in loop

Matched

$O_{d\gamma}, O_{dG}$, 4-quark, semileptonic

Tree-level

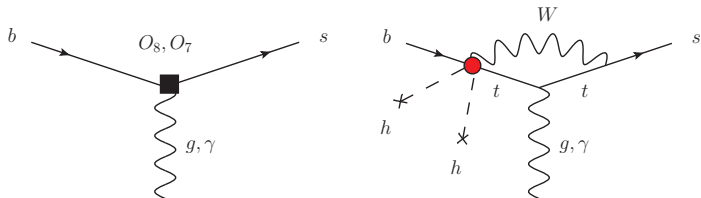
$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$		$(\bar{L}R)(\bar{R}L)$ or $(\bar{L}R)(\bar{L}R)$	
Q_{dW}	$(\bar{q}_i \sigma^{\mu\nu} d_j) \tau^I \varphi W'_{\mu\nu}$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_i \gamma^\mu q_j)$	$Q_{\ell edq}$	$(\bar{\ell}_i^a e_j)(\bar{d}_k q_l^a)$
Q_{dB}	$(\bar{q}_i \sigma^{\mu\nu} d_j) \varphi B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_i \tau^I \gamma^\mu q_j)$	$Q_{quqd}^{(1)}$	$(\bar{q}_i^a u_j) \varepsilon_{ab} (\bar{q}_k^b d_l)$
Q_{dG}	$(\bar{q}_i \sigma^{\mu\nu} T^A d_j) \varphi G_{\mu\nu}^A$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_i \gamma^\mu d_j)$	$Q_{quqd}^{(3)}$	$(\bar{q}_i^a T^A u_j) \varepsilon_{ab} (\bar{q}_k^b T^A d_l)$
$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{qq}^{(1)}$	$(\bar{q}_i \gamma_\mu q_j)(\bar{q}_k \gamma^\mu q_l)$	Q_{dd}	$(\bar{d}_i \gamma_\mu d_j)(\bar{d}_k \gamma^\mu d_l)$	$Q_{\ell d}$	$(\bar{\ell}_i \gamma_\mu \ell_j)(\bar{d}_k \gamma^\mu d_l)$
$Q_{qq}^{(3)}$	$(\bar{q}_i \gamma_\mu \tau^I q_j)(\bar{q}_k \gamma^\mu \tau^I q_l)$	Q_{ed}	$(\bar{e}_i \gamma_\mu e_j)(\bar{d}_k \gamma^\mu d_l)$	Q_{qe}	$(\bar{q}_i \gamma_\mu q_j)(\bar{e}_k \gamma^\mu e_l)$
$Q_{\ell q}^{(1)}$	$(\bar{\ell}_i \gamma_\mu \ell_j)(\bar{q}_k \gamma^\mu q_l)$	$Q_{ud}^{(1)}$	$(\bar{u}_i \gamma_\mu u_j)(\bar{d}_k \gamma^\mu d_l)$	$Q_{qu}^{(1)}$	$(\bar{q}_i \gamma_\mu q_j)(\bar{u}_k \gamma^\mu u_l)$
$Q_{\ell q}^{(3)}$	$(\bar{\ell}_i \gamma_\mu \tau^I \ell_j)(\bar{q}_k \gamma^\mu \tau^I q_l)$	$Q_{ud}^{(8)}$	$(\bar{u}_i \gamma_\mu T^A u_j)(\bar{d}_k \gamma^\mu T^A d_l)$	$Q_{qu}^{(8)}$	$(\bar{q}_i \gamma_\mu T^A q_j)(\bar{u}_k \gamma^\mu T^A u_l)$
				$Q_{qd}^{(1)}$	$(\bar{q}_i \gamma_\mu q_j)(\bar{d}_k \gamma^\mu d_l)$
				$Q_{qd}^{(8)}$	$(\bar{q}_i \gamma_\mu T^A q_j)(\bar{d}_k \gamma^\mu T^A d_l)$

One-loop

Q_{uW}	$(\bar{q}_i \sigma^{\mu\nu} u_j) \tau^I \tilde{\varphi} W'_{\mu\nu}$	$Q_{ud}^{(1)}$	$(\bar{u}_i \gamma_\mu u_j)(\bar{d}_k \gamma^\mu d_l)$	Q_{uu}	$(\bar{u}_i \gamma_\mu u_j)(\bar{u}_k \gamma^\mu u_l)$
Q_{uB}	$(\bar{q}_i \sigma^{\mu\nu} u_j) \tilde{\varphi} B_{\mu\nu}$	$Q_{ud}^{(8)}$	$(\bar{u}_i \gamma_\mu T^A u_j)(\bar{d}_k \gamma^\mu T^A d_l)$	$Q_{\ell u}$	$(\bar{\ell}_i \gamma_\mu \ell_j)(\bar{u}_k \gamma^\mu u_l)$
Q_{uG}	$(\bar{q}_i \sigma^{\mu\nu} T^A u_j) \tilde{\varphi} G^A_{\mu\nu}$	$Q_{qu}^{(1)}$	$(\bar{q}_i \gamma_\mu q_j)(\bar{u}_k \gamma^\mu u_l)$	Q_{eu}	$(\bar{e}_i \gamma_\mu e_j)(\bar{u}_k \gamma^\mu u_l)$
$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger iD_\mu \varphi)(\bar{u}_i \gamma^\mu d_j)$	$Q_{qu}^{(8)}$	$(\bar{q}_i \gamma_\mu T^A q_j)(\bar{u}_k \gamma^\mu T^A u_l)$	$Q_{\varphi u}$	$(\varphi^\dagger i\overleftrightarrow{D}_\mu \varphi)(\bar{u}_i \gamma^\mu u_j)$

Example: O_7, O_8

$$Q_{\varphi ud}^{33} = (\tilde{\varphi}^\dagger iD_\mu \varphi)(\bar{t}\gamma^\mu b)$$



$$C_7 = \frac{m_t}{m_b} \frac{v^2}{\Lambda^2} E_{\varphi ud}^7(x_t) \tilde{C}_{\varphi ud}^{33} V_{ts}^*$$

$$C_8 = \frac{m_t}{m_b} \frac{v^2}{\Lambda^2} E_{\varphi ud}^8(x_t) \tilde{C}_{\varphi ud}^{33} V_{ts}^*$$

$$\Delta S = \Delta B = 2$$

FCNC

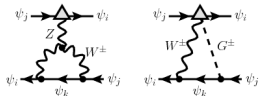
$$\Delta S = \Delta B = 2$$

Operators

4-lepton, semileptonic, Modified Z- W couplings, $\mathcal{O}_{\varphi q}^{(1)}$, $\mathcal{O}_{\varphi q}^{(3)}$, $\mathcal{O}_{\varphi d}$

Matched

$\mathcal{O}_{dd}^{V,LL}$, $\mathcal{O}_{dd}^{V,RR}$, $\mathcal{O}_{dd}^{V1,LR}$, $\mathcal{O}_{dd}^{V8,LR}$, $\mathcal{O}_{dd}^{S1,RR}$, $\mathcal{O}_{dd}^{S8,RR}$



$$\Delta F = 2$$

Top quark effects in $\Delta F = 2$

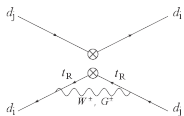
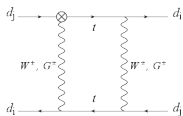
Complete 1-loop matching

Operators

4-quark, Modified Z and W couplings

Matched

$$\mathcal{O}_{dd}^{V,LL}, \mathcal{O}_{dd}^{V,RR}, \mathcal{O}_{dd}^{V1,LR}, \mathcal{O}_{dd}^{V8,LR}, \mathcal{O}_{dd}^{S1,RR}, \mathcal{O}_{dd}^{S8,RR}$$



FCNC

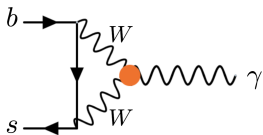
$$\Delta B = \Delta S = 1, 2$$

Flavour symmetry

$$U(3)^5$$

Additional 1-loop operators

4-fermi with t_L , $\mathcal{O}_{\varphi WB} = (\varphi^\dagger \tau^I \varphi) W_{\mu\nu}^I B^{\mu\nu}$, $\mathcal{O}_{\varphi D} = (\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$,



Outline

- 1 Introduction
- 2 Tree-level Matching
- 3 1-Loop Matching
- 4 Codes**
- 5 Summary

Python module

Numerical in- and output

Running

Full SMEFT running

Full WET running

Matching

Complete tree-level matching

Mathematica package

Symbolic expressions for matching, running

Running

Full SMEFT running

Full WET running

Matching

Complete tree-level matching

Python Module

Symbolic matching

General

Every full onto every effective theory

Path integral formalism

Provide \mathcal{L}

Python Module

Numerical matching

Bases

SMEFT and WET

Interfacing with codes

EOS, SMEFTSim, flavio, wilson, DsixTools, FlavorKit...

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Summary

Tree-level Matching

completely known

1-Loop Matching

partially known

Codes

wilson, DsixTools,...