

Exploring the Quantum-Gravity Connection with Underground Experiments

Nicola Bortolotti



VIP collaboration
INFN Gran Sasso Lab.

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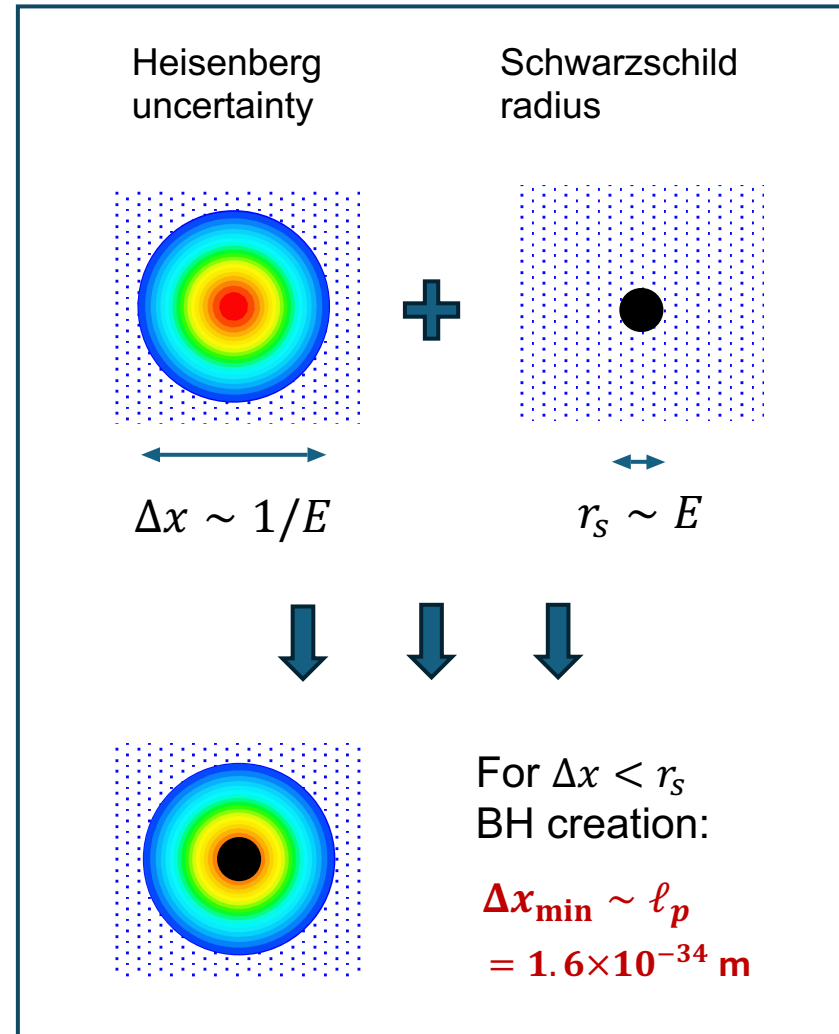
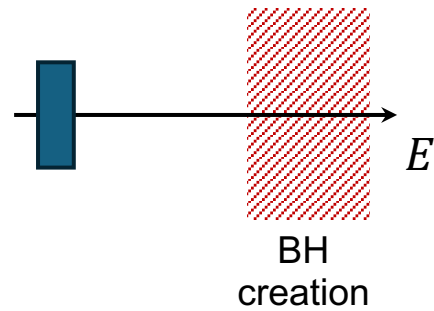
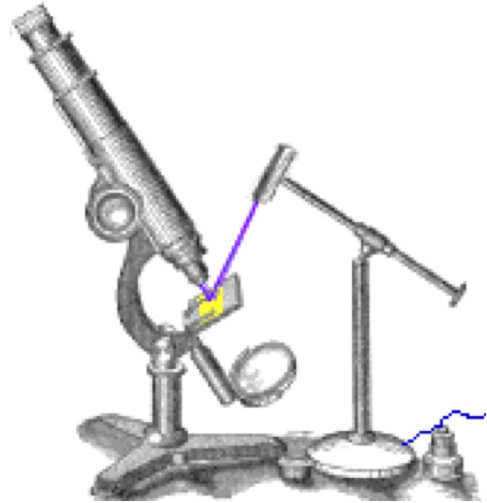
Dr. P. Bosso
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Prof. A. Marcianò
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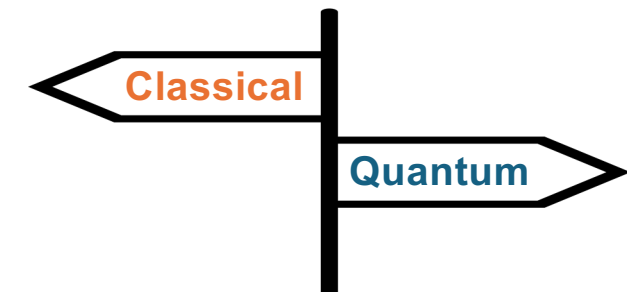
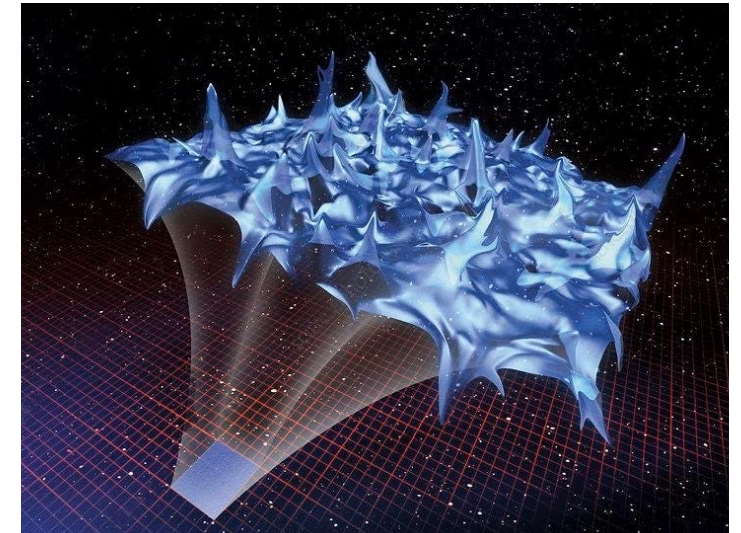
Dr. L. Petruzzello
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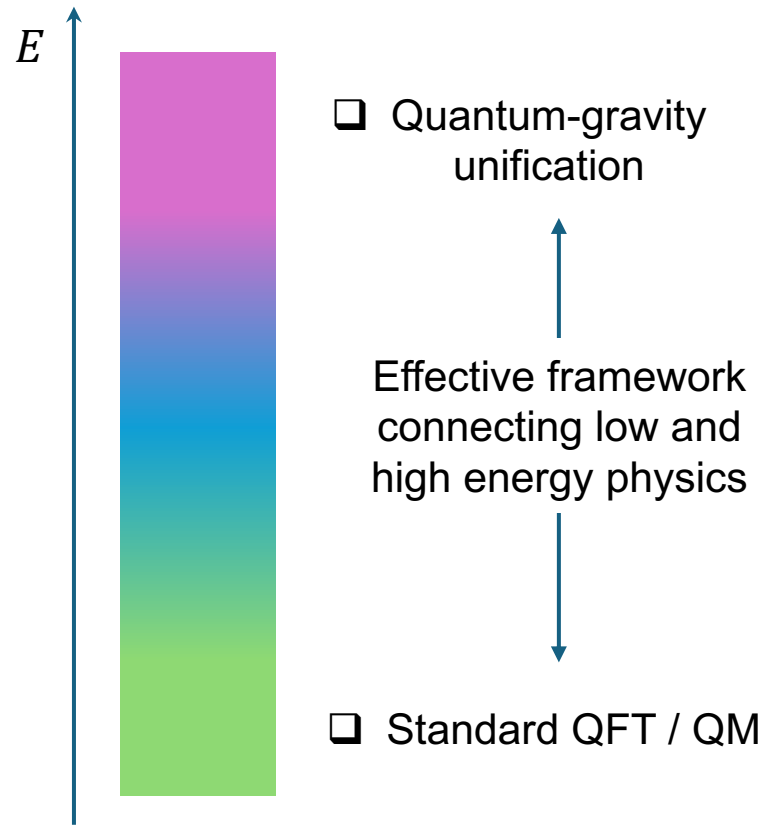
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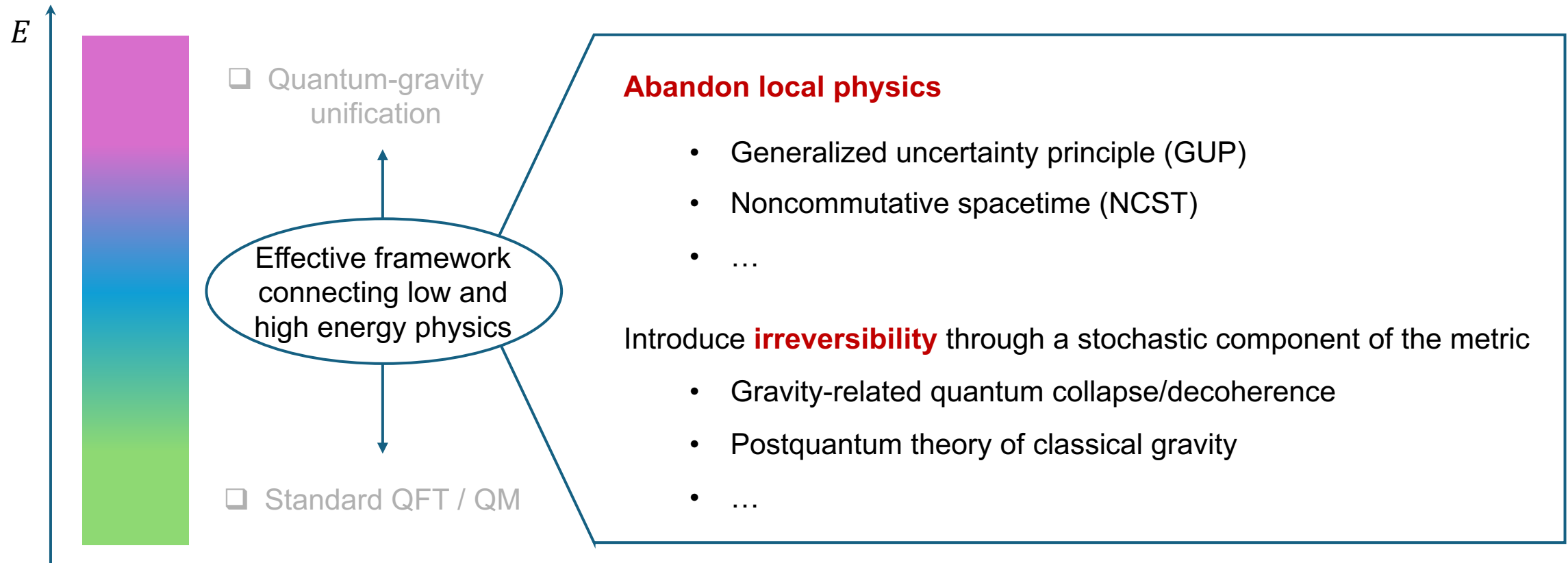
Quantum mechanics + general relativity **do not allow infinite localization!** (Matvei Bronstein 1934)



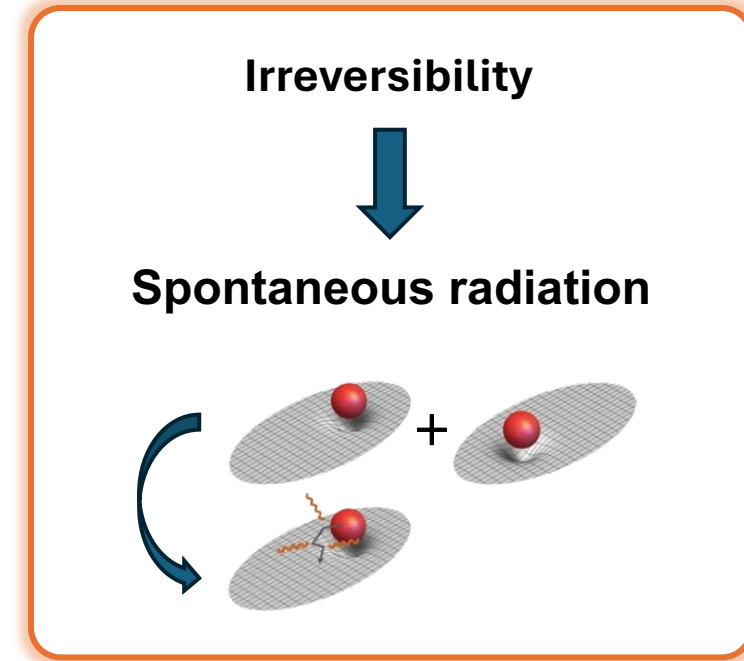
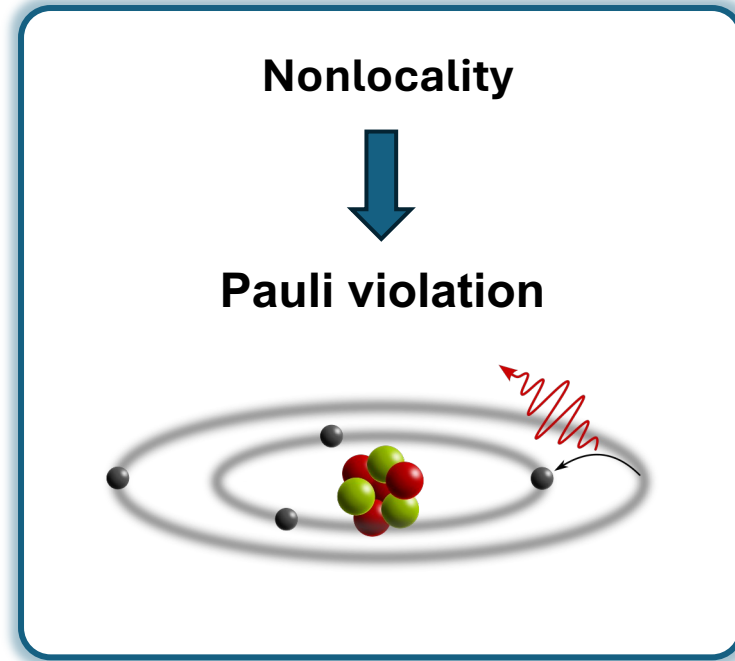
Intrinsic spacetime uncertainty







Goal of the talk



- Characteristic X-ray emission
- Probability of emission is small (e.g. suppressed by the Planck scale)
- All atoms/charged particles can emit: **probability scales with the number of atoms!**

➡ Experimental strategy: **extremely low background + high statistics**

Goal of the talk

Search for anomalous X-ray emission in the low-background environment of the underground Gran Sasso National Laboratory (INFN)

- Overburden corresponding to a minimum thickness of 3100 m w.e.
- **The muon flux is reduced by almost 10^{-6}**
- **The neutron flux by 10^{-3}**

Bayesian analysis to extract pdf $p(S)$ for the # of expected counts S

$$p(S) = \int d\theta p(S, \theta | \text{data}) \leftarrow p(S, \theta | \text{data}) = \frac{\mathcal{L}(\text{data} | S, \theta) P_0(S) P_0(\theta)}{\int dS d\theta \mathcal{L}(\text{data} | S, \theta) P_0(S) P_0(\theta)}$$

- $\mathcal{L}(\text{data} | S, \theta) = \prod_i \text{Pois}(\lambda_i)$

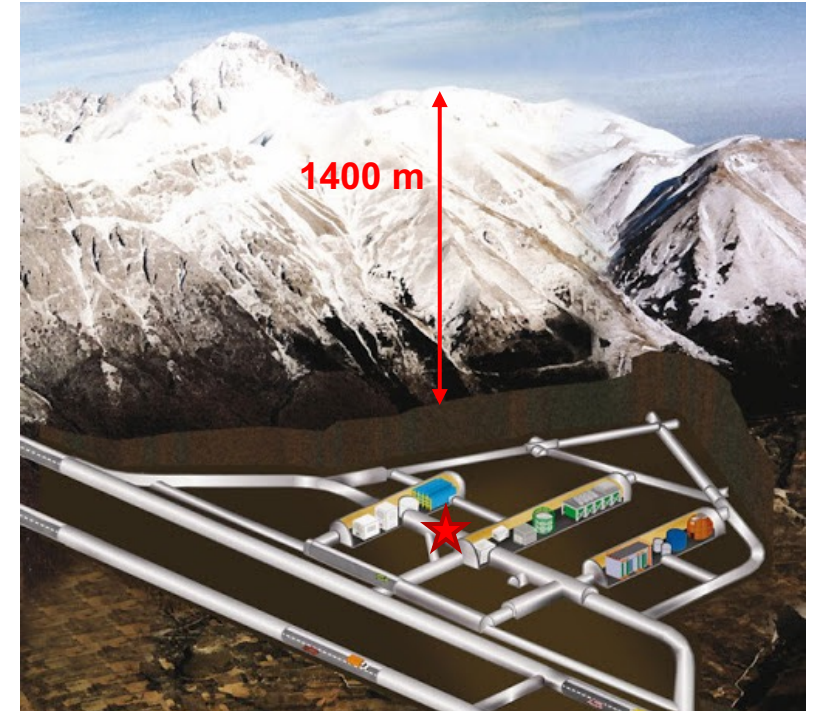
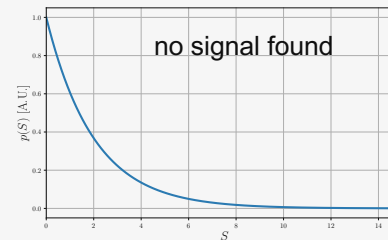
$$\lambda_i = \int_{\Delta E_i} dE f(E; S, \theta): \text{ exp counts at bin-}i$$

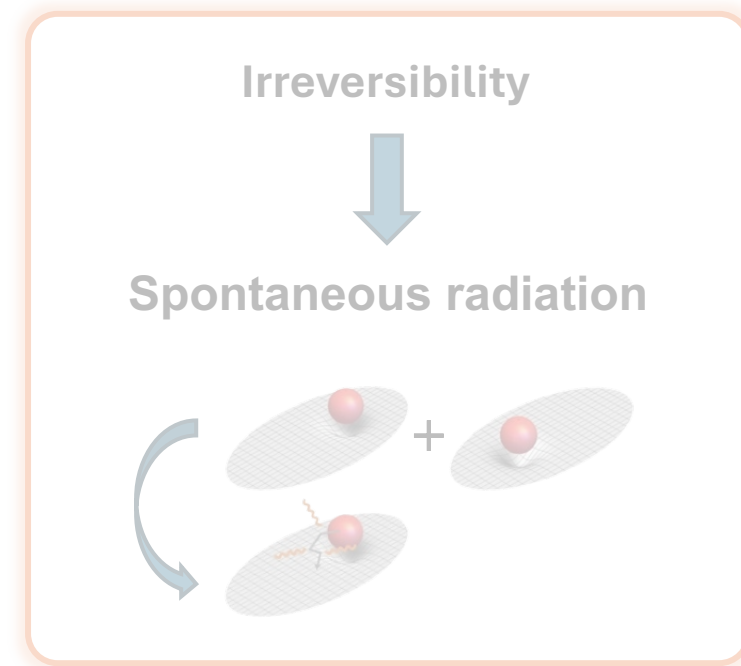
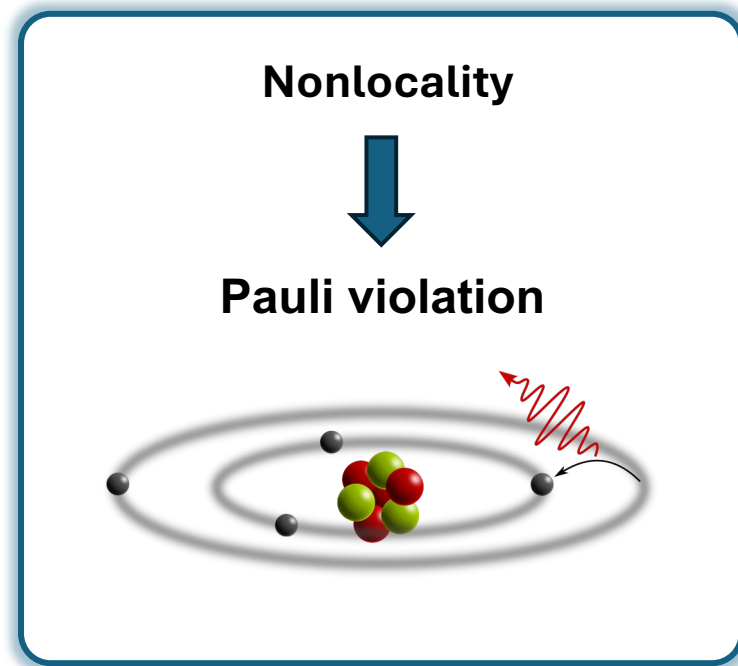
- P_0 : prior

fit function

- Markov-Chain MC numerical integration: $\int_0^S dS p(S) = 0.9$

Connect S to model's parameters $\rightarrow$ **constraint theory**





Leaving the spin-statistics connection toward QG

The spin-statistics theorem is a **necessary manifestation** of:

- **Locality** $\xrightarrow{\text{QG}}$ fails (LQG, strings, causal sets,...)
- **Poincaré covariance** $\xrightarrow{\text{QG}}$ expected either modifications or violations (Hořava gravity,...)



PEP violations provide smoking gun for quantum gravity

Fate of relativistic invariance

- Breaks down: problems with renormalization 
- Holds: which symmetry group?

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Similar to Galilean non-invariance of EM: **Deform Lorentz transformations** s.t. ℓ becomes invariant

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- Holds: which symmetry group? In the presence of a **minimal length** ℓ Lorentz invariance fails (e.g. NCST)

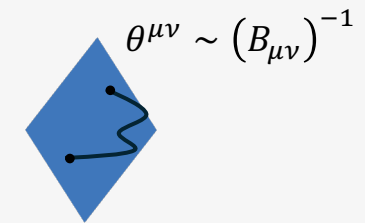
Similar to Galilean non-invariance of EM: **Deform Lorentz transformations** s.t. ℓ becomes invariant

Spacetime uncertainty modeled as: $[x^\mu, x^\nu] = \Theta^{\mu\nu}(x) \sim i\theta^{\mu\nu} + iC_\rho^{\mu\nu}x^\rho + \mathcal{O}(x^2)$ **X**

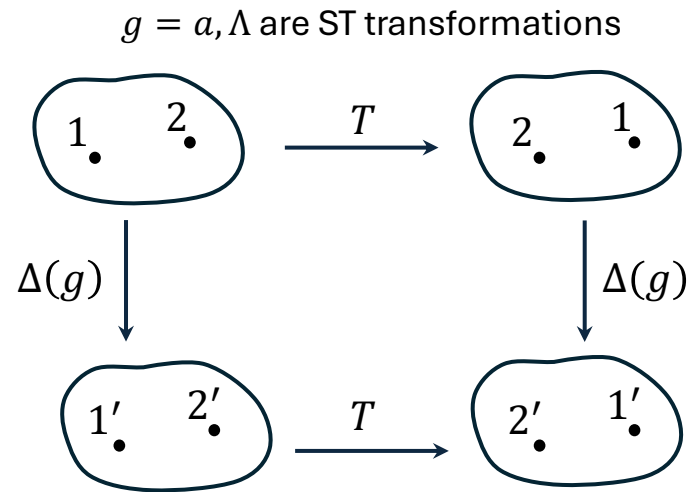
➤ $\theta^{\mu\nu}$ leads to “ **θ -Minkowski**” or “**Moyal plane**” noncommutativity:
Open strings on Dp-branes with a background B-field

➤ $C_\rho^{\mu\nu}x^\rho$ leads to Lie algebra type of noncommutativity. E.g. “ **κ -Minkowski**”:
From **LQG**-modification of the hypersurface-deformation algebra (rigorous proofs only in 3D)

➤ **Deformation** of ST transformations on **multiparticles** (non-trivial coproducts $\Delta(g) \neq g \otimes g$)



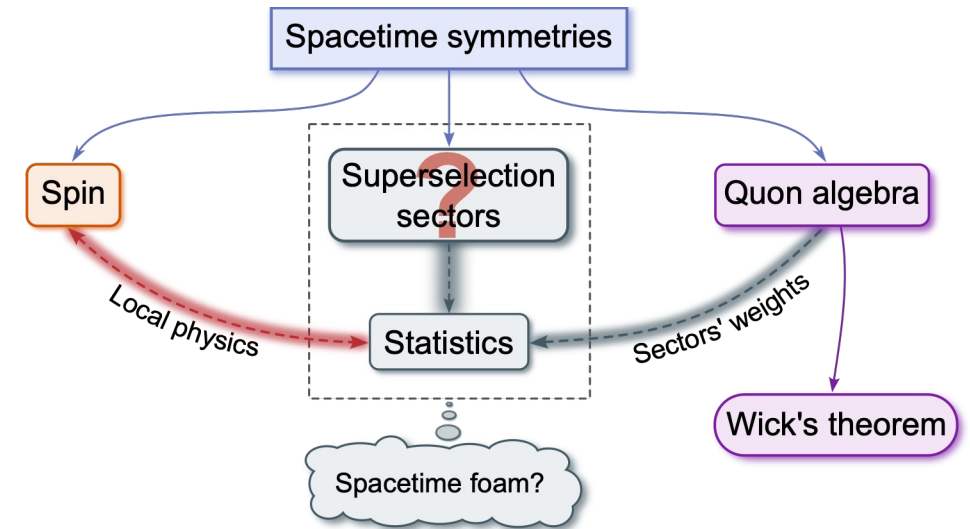
Covariant Fock space



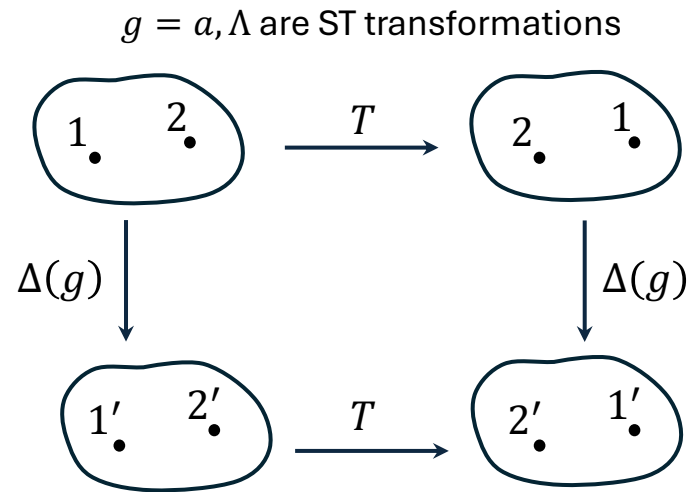
$$[\Delta(g), T] = 0$$

$$T = \tau_R \eta \equiv \tau R \eta$$

fixed by symmetries
 $\tau_R^2 = 1 \text{ vs } T^2 \neq 1$



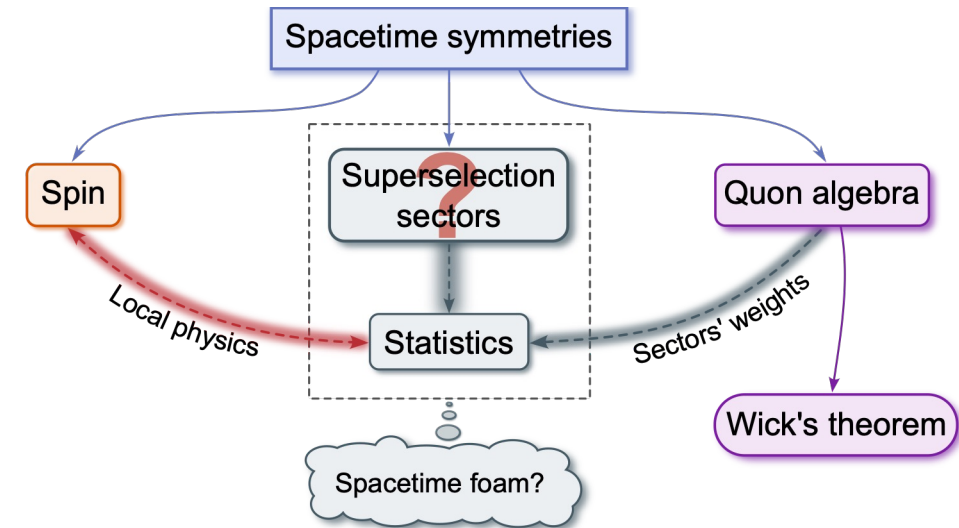
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❖ The state space of a system of **distinguishable** identical particles is the **full Fock space** $\mathfrak{F}(\mathfrak{H}) = \bigoplus_{n=0}^{\infty} \mathfrak{H}^{\otimes n}$

The **inner product** of each $\mathfrak{H}^{\otimes n}$ is **fixed by the T**:

$$a(\tilde{p})a^\dagger(\tilde{q}) - \eta(p, q)R(p, q)a^\dagger(\tilde{q})a(\tilde{p}) = \delta(\tilde{p}, \tilde{q})$$

The **flip operator** τ_R defines **sectors** $\mathfrak{H}^{\otimes n} = \bigoplus_{\lambda} \mathfrak{H}_{\lambda}^{\otimes n}$:

$$|\psi\rangle = \frac{1 + \tau_R}{2} |\psi\rangle + \frac{1 - \tau_R}{2} |\psi\rangle \equiv |\psi\rangle_{s_R} + |\psi\rangle_{a_R}$$

Indistinguishability is guaranteed by **superselection rules (SSRs)**:

$$a_R \langle \psi | O | \phi \rangle_{s_R} = 0 \quad \forall \text{ observables } O$$

Quantum field theory

N.B., et al, arXiv:2603.25552 (2026)

$$\Psi^{(n)}(x) = \sum_{\sigma} \int \widetilde{d}p \left[a_{\sigma}^{(n)}(\mathbf{p}) u_{\sigma}^{(n)}(\mathbf{p}) e^{-ip \cdot x} + b_{\sigma}^{(n)\dagger}(\mathbf{p}) v_{\sigma}^{(n)}(\mathbf{p}) e^{ip \cdot x} \right]$$

$$i\partial_{\mu}\Psi(x) = [\Psi(x), P_{\mu}]$$

Q -deformed algebra, with $|Q_{nm}| < 1$:

$$a^{(n)}(\tilde{p})a^{(m)\dagger}(\tilde{q}) - Q_{nm}^{*}(p, q)a^{(m)\dagger}(\tilde{q})a^{(n)}(\tilde{p}) = \delta_{nm}\delta(\tilde{p}, \tilde{q})$$

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- This scheme of quantization is consistent provided that **operators have infinite expansions in $a^{\#}$**

$$P_{\mu} = \int_{\tilde{p}} p_{\mu} N(\tilde{p}), \quad N(\tilde{p}) = \sum_n \sum_{x=a,b} x^{(n)\dagger}(\tilde{p}) x^{(n)}(\tilde{p}) + \sum_{nm} \sum_{xy} \int_{\tilde{q}} \frac{1}{1 - |Q|_{nm}^2(p, q)} [y^{(m)\dagger}(\tilde{q}), x^{(n)\dagger}(\tilde{p})]_{Q_{mn}} \underbrace{[x^{(n)}(\tilde{p}), y^{(m)}(\tilde{q})]_{Q_{nm}}}_{x^{(n)}(\tilde{p})y^{(m)}(\tilde{q}) - Q_{nm}(p, q)y^{(m)}(\tilde{q}), x^{(n)}(\tilde{p})} + \dots$$

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- Causality breaks down:** $[\mathcal{H}_I(x), \mathcal{H}_I(y)] \neq 0$ at space-like separations
- But the S -matrix is invariant:** $\int dx dy x [\mathcal{H}_I(x, 0), \mathcal{H}_I(y, 0)] \neq 0$, which ensures $U(\Lambda)^{\dagger} S U(\Lambda) = S$

This solves a long-standing problem and extends the quon model to the relativistic regime

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$|Q| < 1$ is crucial
to obtain UV
regularization

This solves a long-standing problem and extends the quon model to the relativistic regime

Atomic states

Rigorous relativistic treatment of atomic states is based on Green functions

- pole structure contains bound states
- treat interactions nonperturbatively
- provide dynamical evolution

Electron exchange is governed only by the Q-commutation relations regardless of interactions:

$$G = \left(G + Q^* \begin{array}{c} \text{red line crossed} \\ \text{purple line} \end{array} \right) + Q^{*'} \left(\begin{array}{c} \text{red line} \\ \text{red line crossed} \end{array} + Q_{\theta}^* \begin{array}{c} \text{red line crossed} \\ \text{red line crossed} \end{array} \right)$$

The kernel preserves superselection rules

$$G_\lambda = \mathcal{K}' G_\lambda$$

The physical states are those with **twisted statistics**

VS

The kernel breaks superselection rules

The diagram shows an equality between two graph representations. On the left, a yellow oval labeled G is connected to four horizontal lines (two red, two purple). On the right, a gray rectangle labeled $\mathcal{K}$ is connected to the same four lines, and a yellow oval labeled G is connected to the two red lines. This represents the decomposition of graph G into a kernel $\mathcal{K}$ and a graph G .

Identical particles are slightly different

Examples

Undeformed Poincaré

$$Q(p, q) = \eta(p, q)$$

Greenberg quon model

$$a(\tilde{p})a^\dagger(\tilde{q}) - \eta(p, q)a^\dagger(\tilde{q})a(\tilde{p}) = \delta(\tilde{p}, \tilde{q})$$

$$\psi_{s,a}(\tilde{p}, \tilde{q}) = \pm \psi_{s,a}(\tilde{q}, \tilde{p})$$

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θ -Poincaré

$$Q(p, q) = \eta(p, q) \exp(i\theta^{\mu\nu} p_\mu q_\nu)$$

$\theta^{\mu\nu}$ defines the *Moyal spacetime* $[x^\mu, x^\nu] = \theta^{\mu\nu}$

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$\eta(p, q)$ can be any function that:

- i) is **Lorentz invariant**
- ii) is **real**
- iii) is bounded $-1 \leq \eta(p, q) \leq 1$ (positivity of norms)
- iv) **reduces to ± 1 at $E \ll E_{pl}$**



$$\eta(p, q) \sim \pm \left(1 - \left(\frac{\sigma(p, q)}{\Lambda_{QG}} \right)^\kappa \right)$$

σ has dimensions of energy, κ a free parameter and Λ_{QG} is the QG scale

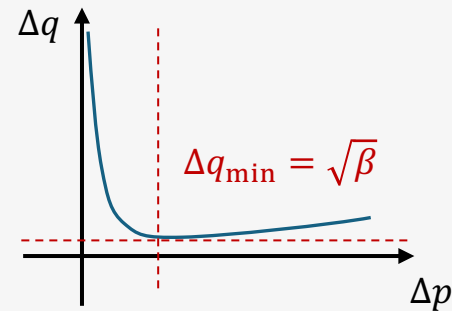
Quon realization from generalized uncertainty principle

By modifying the HUP a **minimal length** appears

$$[\hat{q}, \hat{p}] = i[1 + \beta \hat{p}^2]$$

$$\Delta q \Delta p = \frac{1}{2}[1 + \beta \Delta p^2]$$

from **string theory**



Deformed ladder operators for the h.o.

$$\hat{c}^+ |n\rangle = \sqrt{\frac{E_{n+1} - E_0}{\hbar\omega}} |n+1\rangle, \quad \hat{c} |n\rangle = \sqrt{\frac{E_n - E_0}{\hbar\omega}} |n-1\rangle$$

$$H = \hbar\omega \hat{c}^\dagger \hat{c} + E_0 \mathbb{I}, \quad [\hat{c}, \hat{c}^\dagger] = \sqrt{1 + 2\beta m H} + \frac{\beta \hbar \omega m}{2}$$

(P. Bosso, G.G. Luciano *EPJC* **81**, 982 2021)

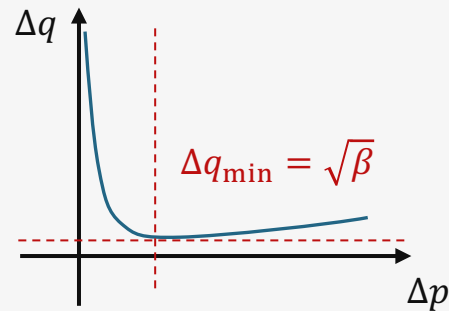
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QFT can be constructed using such operators

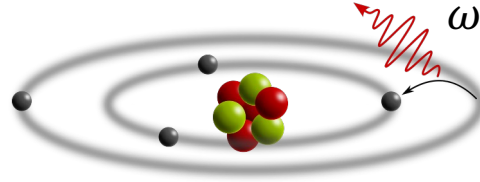
Spinor fields: $a(\tilde{p})a^\dagger(\tilde{q}) + \eta_\beta(\mathbf{p}, \mathbf{p}')a^\dagger(\tilde{q})a(\tilde{p}) = \delta^{(3)}(\tilde{p}, \tilde{q})$

$$\{a(\tilde{p}), a(\tilde{q})\} = 0, \quad \{a^\dagger(\tilde{p}), a^\dagger(\tilde{q})\} = 0, \quad \text{for } \tilde{p} \neq \tilde{q}$$

Quon deformation of fermions: $\eta_\beta(\mathbf{p}, \mathbf{p}') = 1 - \beta m E_p^4 \delta^{(3)}(\mathbf{p} - \mathbf{p}')$

PEP forbidden atomic transitions with SSRs

- One atom



Transition rate per atom

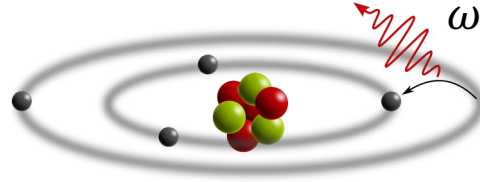
$$d\Gamma^\lambda = 2\pi\delta(E' - E + \omega) |H_{if}^\lambda|^2 \frac{d^3k}{(2\pi)^3}$$

Lorentz-invariant: $\psi_a^{\text{PEPV}}(\tilde{p}, \tilde{q}) = \varphi(\tilde{p})\varphi(\tilde{q}) - \varphi(\tilde{q})\varphi(\tilde{p}) = 0$ $\Rightarrow$ PEP-violation **only in non-antisymmetric sectors**

Lorentz-deformed: $\psi_{a\theta}^{\text{PEPV}}(\tilde{p}, \tilde{q}) = \varphi(\tilde{p})\varphi(\tilde{q})(1 - e^{i\theta^{\mu\nu}p_\mu q_\nu}) \neq 0$ $\Rightarrow$ PEP-violation **also in the antisymmetric sector**

PEP forbidden atomic transitions with SSRs

- One atom



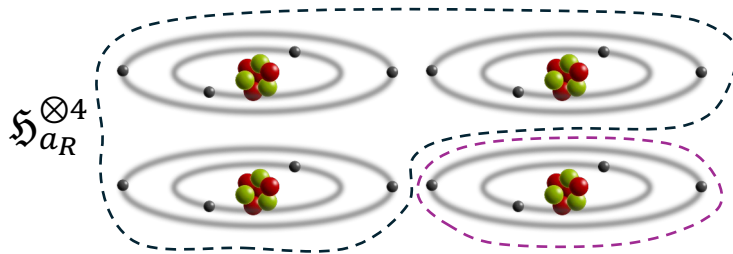
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- N (identical) atoms

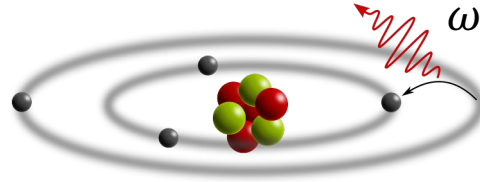


Fraction of atoms in antisymmetric states: $N_a/N = p_a = \frac{\|\psi_{a_R}\|^2}{\sum_{\gamma'} \|\psi_{\gamma'_R}\|^2} \sim 1$

Fraction of atoms with wrong symmetry: $\frac{N_w}{N} = p_w = \sum_{\lambda \neq a} p_\lambda \sim \left(\frac{\sigma}{\Lambda_{QG}}\right)^\kappa \ll 1$

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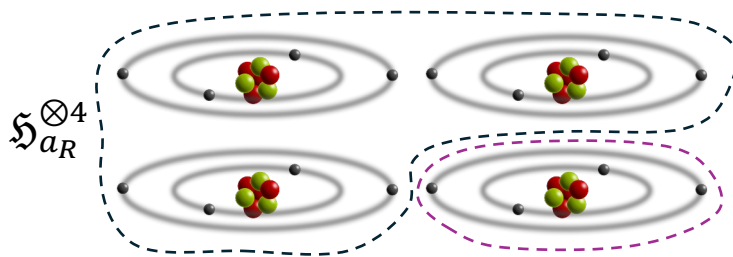
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The **Lorentz-invariant** scenario allows PEP-violations only in the non-antisymmetric sectors: **suppressed probability**

The **Lorentz-deformed** scenario allows PEP-violations in the antisymmetric sector: **large probability**

Pauli forbidden atomic transitions without SSRs

$\psi(p_1, p_2)$ and $\psi(p_2, p_1)$ describe different physical states:

Initial state

$$\psi^\pm(\mathbf{p}, \mathbf{q}) = \psi_s(\mathbf{p}, \mathbf{q}) \pm \psi_a(\mathbf{p}, \mathbf{q})$$

PEPV state

$$\psi'(\mathbf{p}, \mathbf{q}) = \psi'_s(\mathbf{p}, \mathbf{q})$$

$$\left\{ \begin{array}{l} d\Gamma_{\text{PEPV}}^\pm = 2\pi\delta(E' - E + \omega) |H_{if}^s \pm H_{if}^a|^2 \frac{d^3k}{(2\pi)^3} \\ H_{if}^\gamma = \frac{e}{\sqrt{2\omega}} \int d^3p d^3q D^\gamma \psi'_s(\mathbf{p} - \mathbf{k}, \mathbf{q}) \boldsymbol{\alpha}_{(1)} \cdot \boldsymbol{\varepsilon}^* \psi_\lambda(\mathbf{p}, \mathbf{q}) \end{array} \right.$$

Deformation factor due
to modified statistics

QED matrix elements are deformed by

$$D^{s,a} = \frac{[1 \pm Q(p, q)][1 + Q(p - k, q)] \pm [1 - \eta^2(p - k, q)]}{\|\psi'_s\| \|\psi\|}$$

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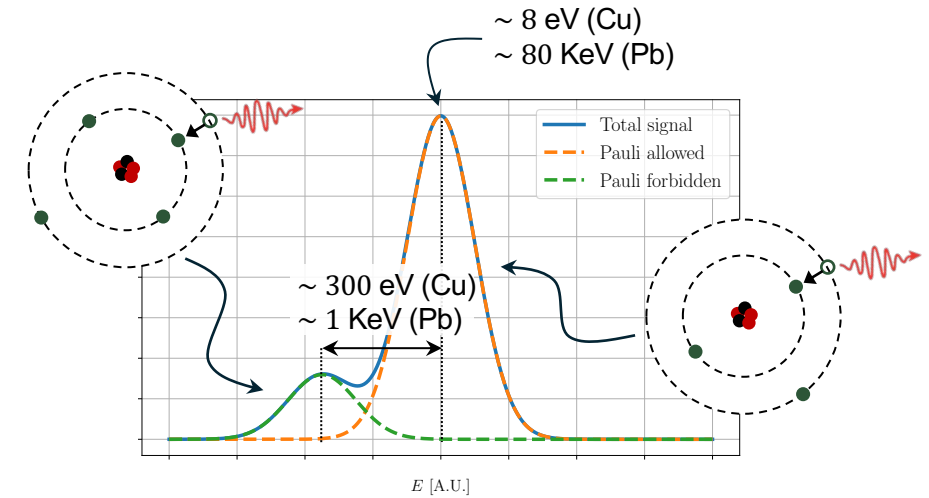
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$$\Gamma_{\text{PEPV}}^\pm \sim \left(\frac{E_{\text{at}}}{\Lambda_{QG}} \right)^{f(\kappa)} \Gamma_0, \quad \text{where } E_{\text{at}} \text{ is an atomic energy scale}$$

The exact expression of Γ_{PEPV} depends on the specific form of $\eta(p, q)$ and spacetime symmetries

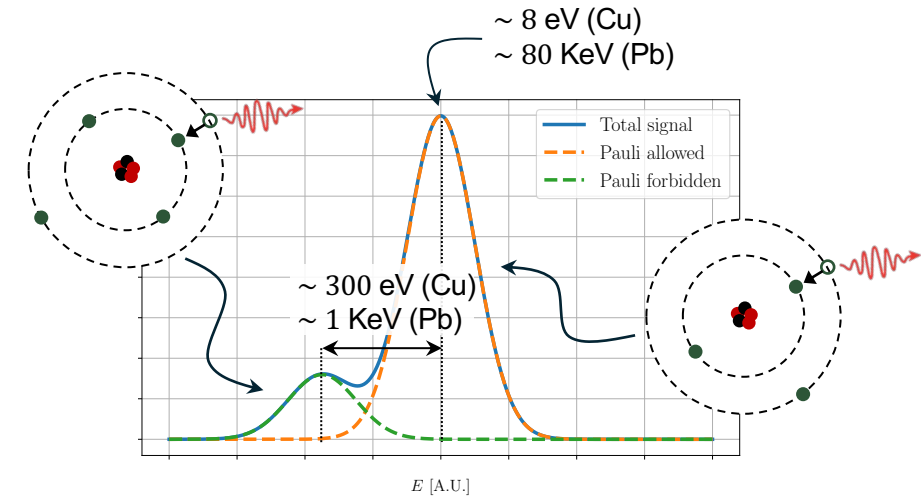
VIP experiments

- Search for the X-rays signature of PEP violating K transitions in Cu and Pb
- **Transition energies are shifted downward** with respect to the standard ones due to additional shielding of the nuclear field



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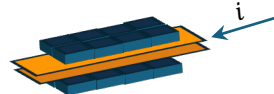


$$N_{\text{events}} = N_{\text{at}} \cdot p_{\text{atom}}^{\text{PEPV}}$$

VIP-Cu “open system”: superselection rules

Fast PEPV transitions but only for a small fraction p_w of atoms:
use a current to enhance the numbers of PEPV transitions

32 Silicon Drift Detectors (SDDs) facing two
 target copper strips (76x20x0.25 mm)



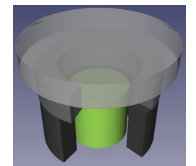
Background provided by data acquisition without current

$$S = p_w N_{\text{new}} N_{\text{int}} \propto (E_{\text{at}}/\Lambda_{\text{QG}})^{\kappa} \Rightarrow \text{lower limit on } \Lambda_{\text{QG}}$$

VIP-Pb “closed system”: no superselection rules (NCST)

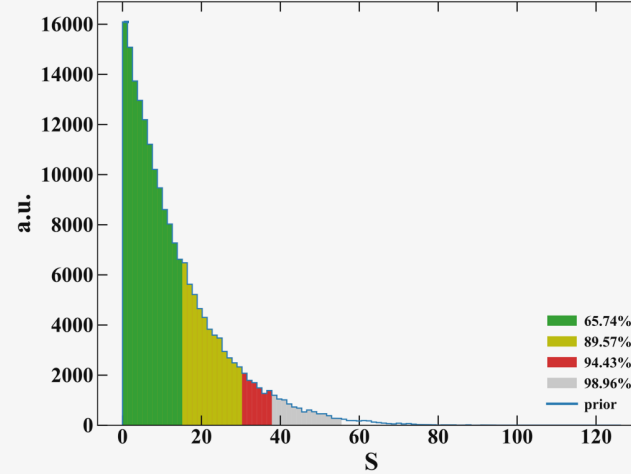
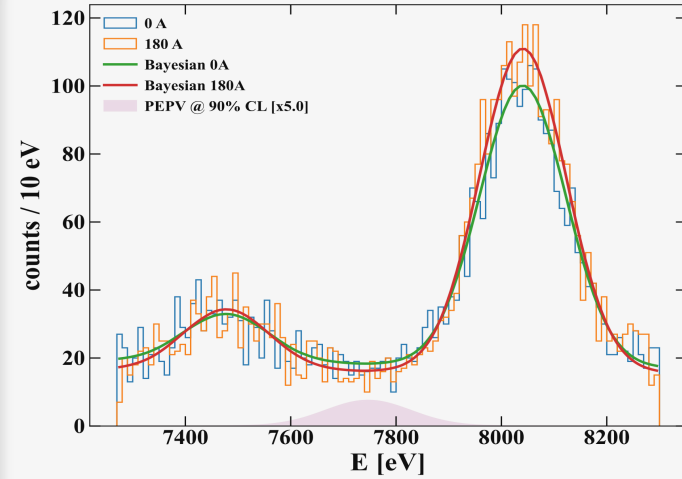
PEPV probability suppressed by $\sim (E_{\text{at}}/\Lambda_{\text{QG}})^a$ but for all atoms

High-purity germanium (HPGe) detector (8x8 cm)
 Target: 3 cylindrical sections of radio-pure Roman
 lead completely surrounding the detector



$$S \sim (E_{\text{at}}/\Lambda_{\text{QG}})^a \Rightarrow \text{lower limit on } \Lambda_{\text{QG}}$$

Test of GUP with VIP-Cu



$$S = p_w N_{\text{new}} N_{\text{int}} \epsilon$$

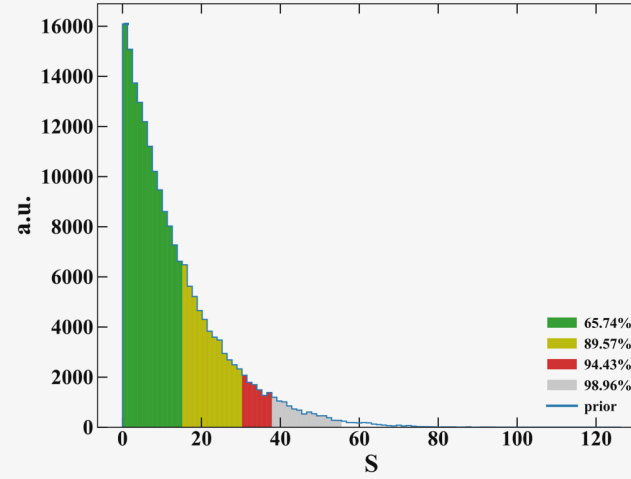
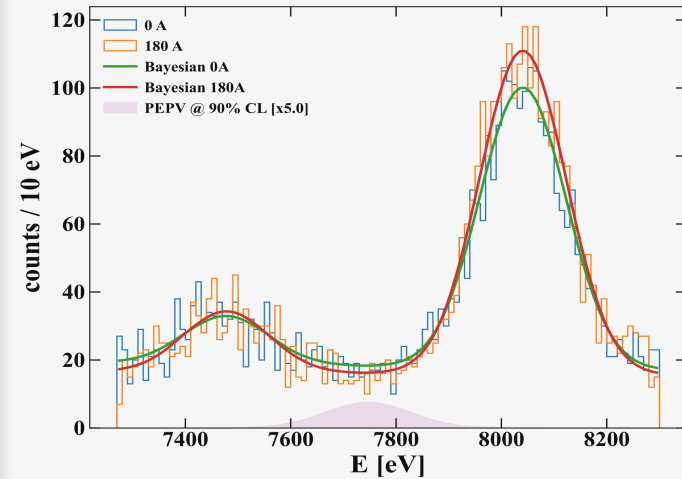
$$\Rightarrow p_w < 6.74 \times 10^{-43}$$

Strongest limit on PEPV
in open systems

A. Porcelli, **N.B.** et al. *EPJC* 84.3 2024

A. Porcelli, **N.B.** et al. *Scientific Reports* 15.1 2025

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GUP PEPV probability: $p_w = \beta \underbrace{\frac{m^5}{\Delta_{(\chi)}^3} \sum_{nl} BR_{nl} I_{nl}}_{\text{known parameters}}$

$$\beta / \ell_p^2 < 4.62 \times 10^{-2}$$

Previous strongest limit:

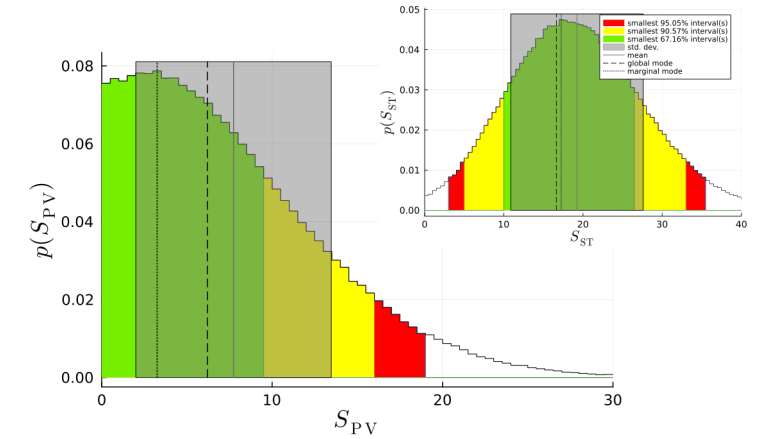
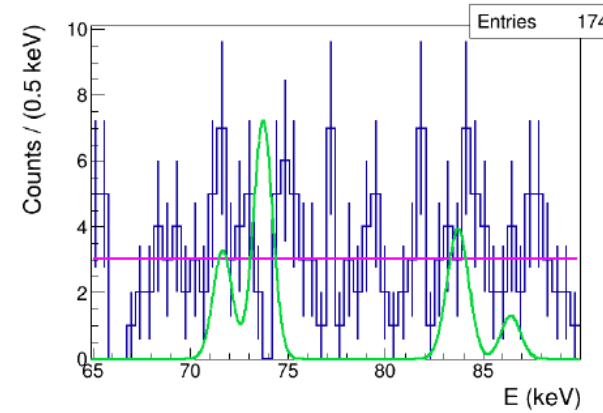
$$\beta / \ell_p^2 < 10^{16}!$$

Paper under finalization in collaboration with A. Porcelli, P. Bosso, L. Petruziello, F. Illuminati

Test of different classes of NCSTs with VIP-Lead

$$\Gamma_{PEPV} = \left(\frac{E_{at}}{\Lambda_{QG}} \right)^a \Gamma_0$$

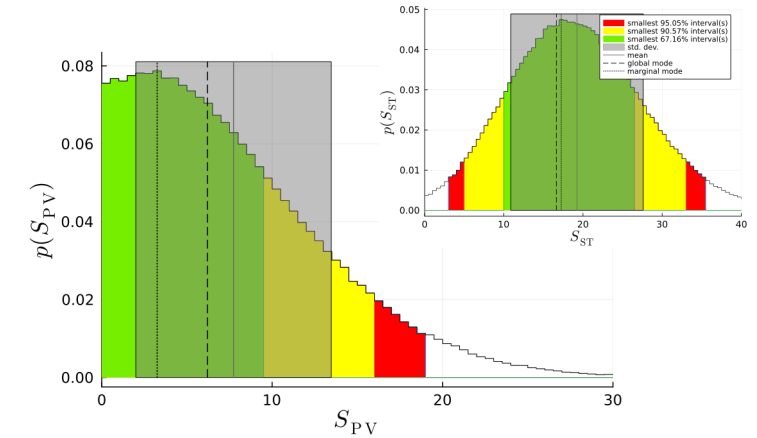
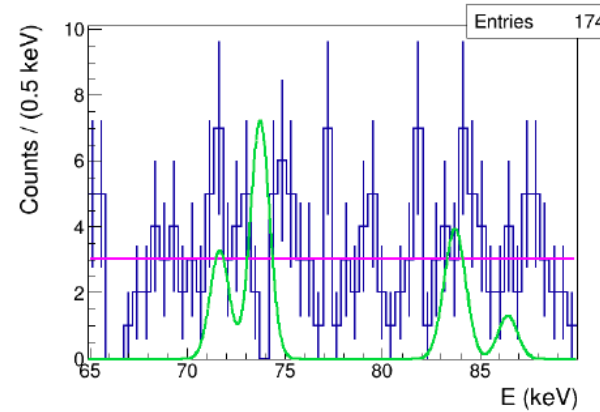
$Z_{Pb} = 82 \rightarrow$ test Λ at the highest transition energy



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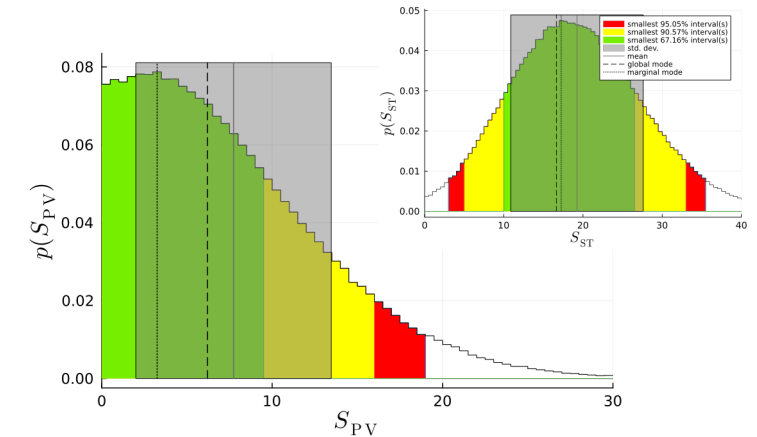
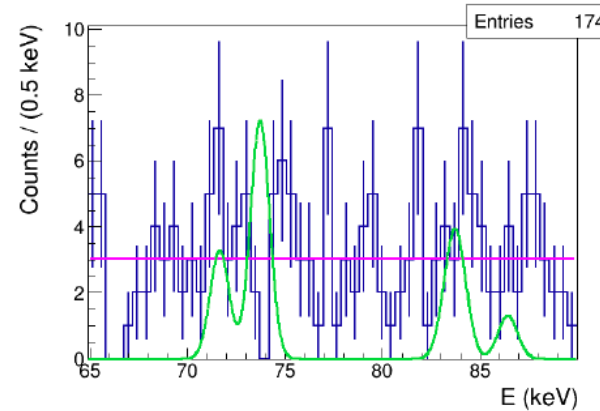
MODEL	Relevant for κ -Minkowski (LQG)	Moyal spacetime (strings with background B-field)	Triply special relativity
Scaling	Linear	Quadratic	Cubic (first bound ever)
$\Lambda_{QG}/E_{pl} >$	4.2×10^{21}	1.6×10^{-1}	5.6×10^{-9}

K. Piscicchia, **N.B.**, et al *Universe*, 9.7, 2023

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Stronger bounds arise in the hadronic sector from DAMA/LIBRA, Borexino and Kamiokande (A. Addazi, et al, Chinese Physics C 42 094001 2018)

Test of both sectors are needed as in principle different particles may have different couplings to noncommutativity

Current experimental improvements

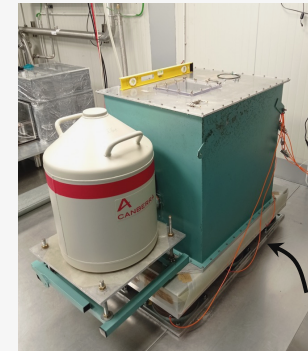
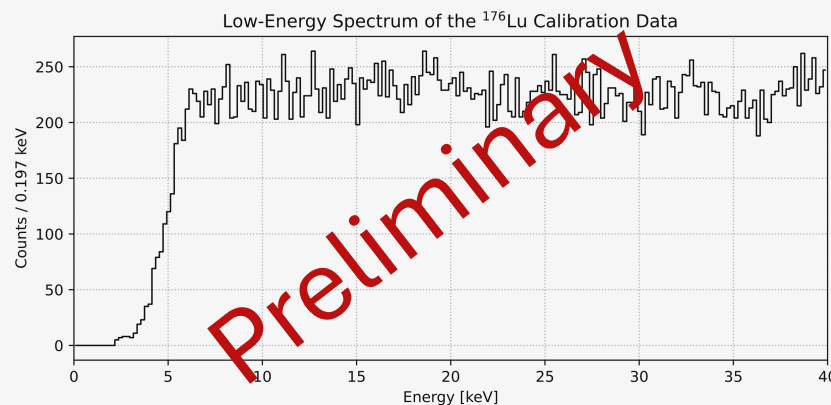
Improve on efficiency: **use Ge detector as active material** → gain of about four orders of magnitude



2 O.o.m. improvement on Λ_{QG} from PEPV
For Ge standard $K_{\alpha} = 9.9$ keV

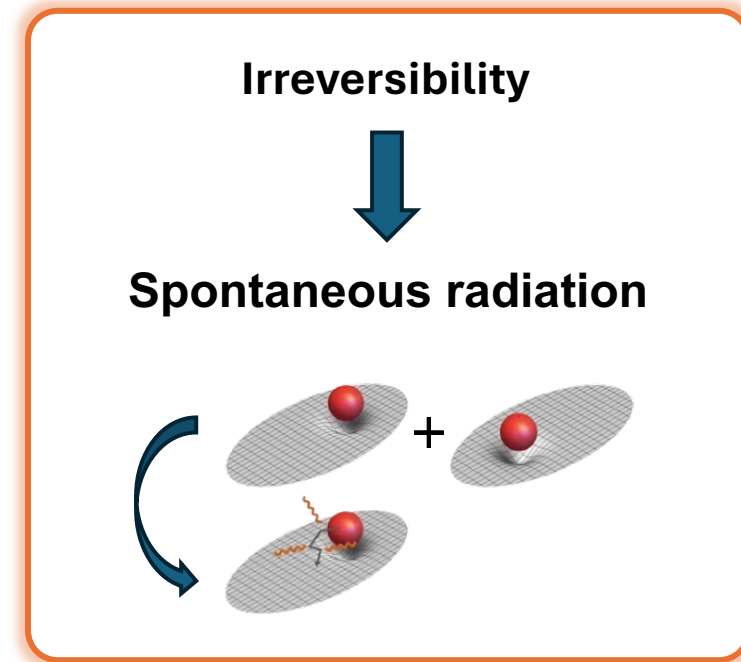
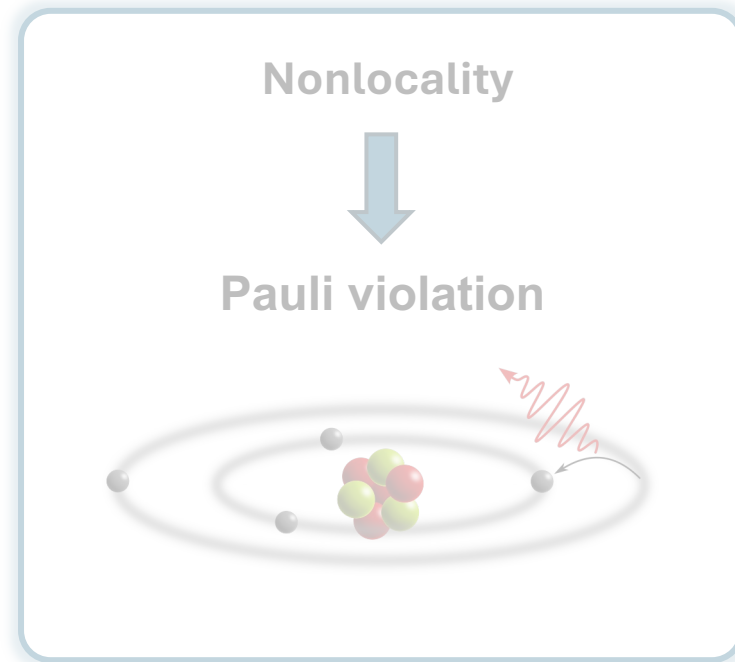
Use a **Broad Energy Germanium (BEGe) detector** to push down the energy range of the spectrum

- Ranges from ~ 1 keV up to several MeV
- Excellent resolution and efficiency at low energies



Ongoing work:

- MC characterization of the background
- ML-based event selection. Already **improved SNR** by 14% and **reduced the energy threshold** (S. Manti, **N.B.**, et al, JINST 21.01 01036 2026)
- Pulse-shape analysis for **directionality effects**



Classical-quantum hybrid dynamics

- Standard approach: $G_{\mu\nu} = \frac{8\pi G}{c^4} \langle \psi | \hat{T}_{\mu\nu} | \psi \rangle$  QFT on curved spacetime

Yields **faster-than-light communication** and **wrong predictions** for large quantum fluctuations of matter

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Newtonian theory constructed by L. Diosi and A. Tilloy
(PRD 93.2 024026 2016)

$$\mathbb{E}[\delta\phi(\mathbf{x}, t)] = 0,$$

$$\mathbb{E}[\delta\phi(\mathbf{x}, t) \delta\phi(\mathbf{y}, t')] = \mathcal{D}_\phi(\mathbf{x} - \mathbf{y}) \delta(t - t')$$

also colored
 $\mathcal{G}(t - t')$

Relativistic extension by J. Oppenheim (PRX 13.4 041040 2023)

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Relativistic extension by J. Oppenheim (PRX 13.4 041040 2023)

- ✓ Consistent coupling between matter & gravity
- ✓ **Solution of the measurement problem**
- ✓ **Experimental signatures**

Irreversibility

In the presence of a stochastic component $\delta\phi$ of the Newtonian field

$$\frac{d}{dt}|\psi_t\rangle = -\frac{i}{\hbar}\left[\hat{H} + \int d^3x \hat{\mu}(\mathbf{x})\delta\phi(\mathbf{x}, t)\right]|\psi_t\rangle, \quad \frac{d\hat{\rho}}{dt} = -\frac{i}{\hbar}[\hat{H}, \hat{\rho}] - \underbrace{\frac{1}{2\hbar^2} \int d^3x d^3y \mathcal{D}_\phi(\mathbf{x} - \mathbf{y}) [\hat{\mu}(\mathbf{x}), [\hat{\mu}(\mathbf{y}), \hat{\rho}]]}_{\text{gravity-induced decoherence}}$$

Standard Hamiltonian

Mass density operator

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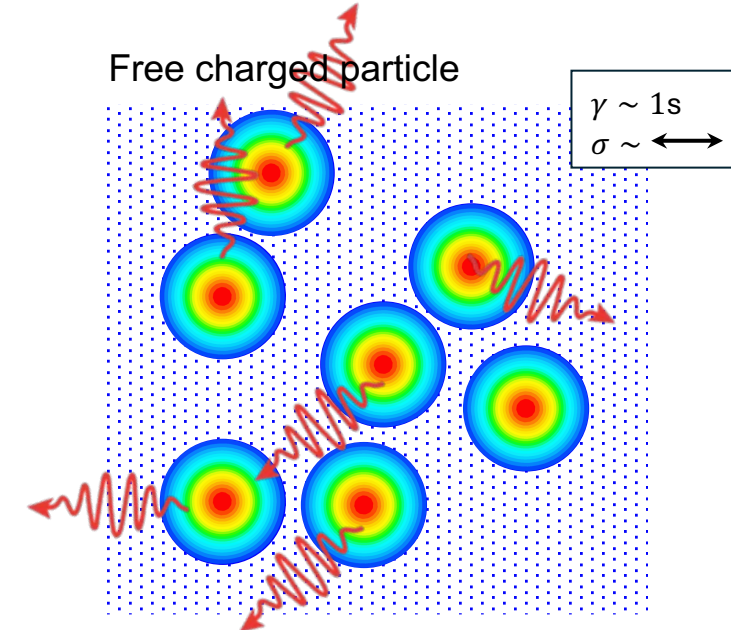
gravity-induced decoherence

Diffusive dynamics

The fluctuating field randomly kicks particles at different times and locations

$\mathcal{D}_\phi$ sets the **localization rate** γ and **spatial resolution** σ

Standard Schrödinger evolution for **microscopic systems**,
instantaneous localization for **macroscopic masses**



Spontaneous collapse models (SCMs)

linear determ.
nonlinear stochastic

$$\frac{d}{dt}|\psi_t\rangle = -\frac{i}{\hbar}\hat{H}|\psi_t\rangle + \left[\int d^3x \hat{M}_t(\mathbf{x}) \delta\phi_t(\mathbf{x}) - \frac{1}{2} \int d^3x d^3y \mathcal{D}(\mathbf{x} - \mathbf{y}) \hat{M}_t(\mathbf{x}) \hat{M}_t(\mathbf{y}) \right] |\psi_t\rangle$$

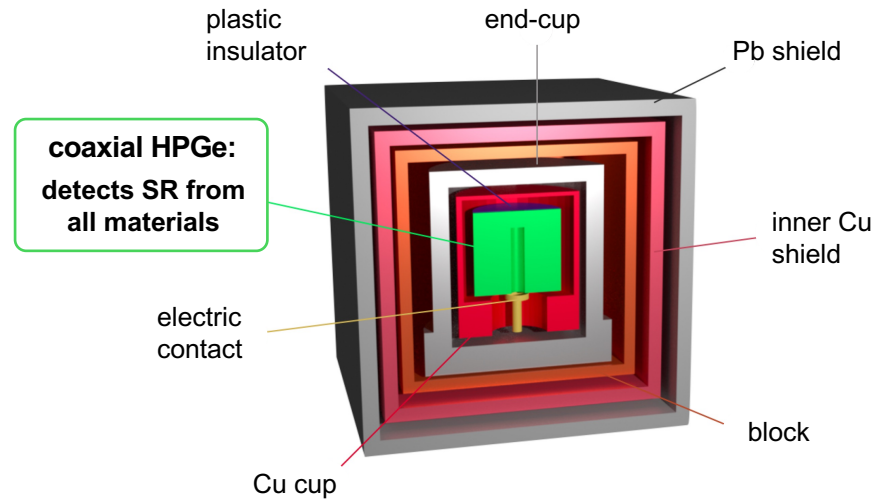
$\hat{M}_t(\mathbf{x}) \equiv \hat{\mu}(\mathbf{x}) - \langle \psi_t | \hat{\mu}(\mathbf{x}) | \psi_t \rangle$

For leading models CSL and Diosi-Penrose:
 $\hat{\mu}$ is the mass density and $\delta\phi$ the Newtonian field

Reproduces the Born rule!

Effective only for macroscopic objects!

VIP experiment



Each material emits with a rate $d\Gamma_{\text{mat}}/dE$

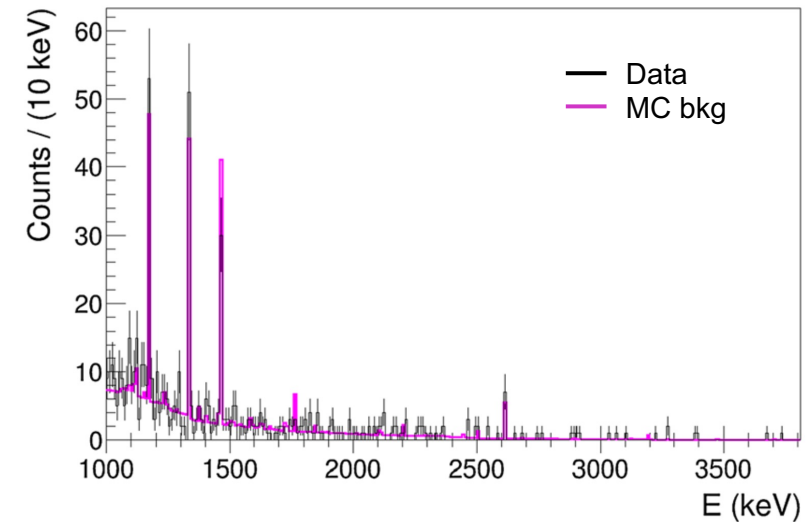
Detection efficiencies $\epsilon_{\text{mat}}(E)$ and background obtained via MC simulation

Analysis

$$1 \text{ parameter: } p(S|data) = \frac{\mathcal{L}(data|S)P_0(S)}{\int dY \mathcal{L}(data|S)P_0(S)},$$

$$\lambda_i = b_i^{\text{MC}} + \int_{\Delta E_i} dE f(E;S): \text{ exp counts at bin- } i$$

$$b_i^{\text{MC}}: \text{ MC simulated bkg, } f(E;S) = T \sum_{\text{mat}} \frac{d\Gamma_{\text{mat}}}{dE} \epsilon_{\text{mat}}(E)$$

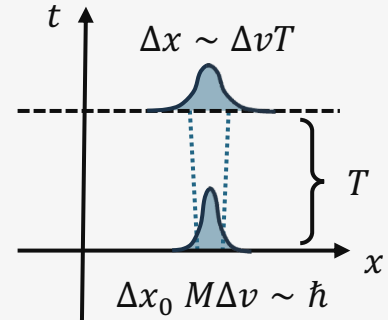


Károlyházy – first gravity-related decoherence model

In 1966 K. derives a limit to the precision a quantum probe can measure a time-like length $s = cT$

- $\Delta s \sim \Delta x$ minimized when $\Delta x = \Delta x_0$ and $M \rightarrow M_{\max}$
- $M_{\max}$ follows requiring that no black hole appears: $\Delta x > r_s$

$$\Delta s^3 = \ell_p^2 \bar{s}$$



stochastic



$$\frac{s}{c} = \int_0^{\bar{s}/c} dt \sqrt{g_{\mu\nu} \dot{x}^\mu \dot{x}^\nu},$$

$$g_{00}(x, t) = 1 + \frac{2}{c^2} \phi(x, t)$$



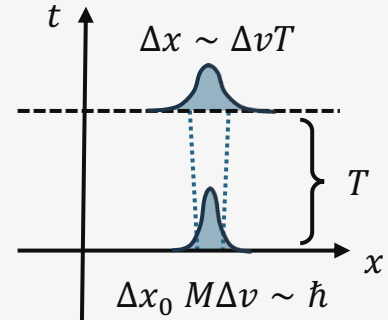
$$\int_0^{\bar{s}/c} dt \int_0^{\bar{s}/c} dt' \mathbb{E}[\phi(x, t) \phi(x, t')] = (\ell_p^2 \bar{s})^{2/3}$$

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$$\int_0^{\bar{s}/c} dt \int_0^{\bar{s}/c} dt' \mathbb{E}[\phi(\mathbf{x}, t) \phi(\mathbf{x}, t')] = (\ell_p^2 \bar{s})^{2/3}$$

- ❖ **The original version** assumes the wave equation for ϕ , but **predicts too much emission of spontaneous radiation!**

(L. Diosi, B. Lukács PRA 181.5 366-368 1993)

- ❖ Assuming instead a generic $\mathbb{E}[\phi(\mathbf{x}, t) \phi(\mathbf{x}', t')] = \mathcal{D}(|\mathbf{x} - \mathbf{x}'|) \mathcal{G}(|t - t'|)$, the K. uncertainty Δs fixes

$$\tilde{\mathcal{G}}(\omega) = \frac{4}{\sqrt{3}} \Gamma\left(\frac{2}{3}\right) t_p^{1/3} \omega^{1/3}$$

and drastically reduces the radiation emitted (L. Figurato, et al, NJP 26.1 013001 2024)

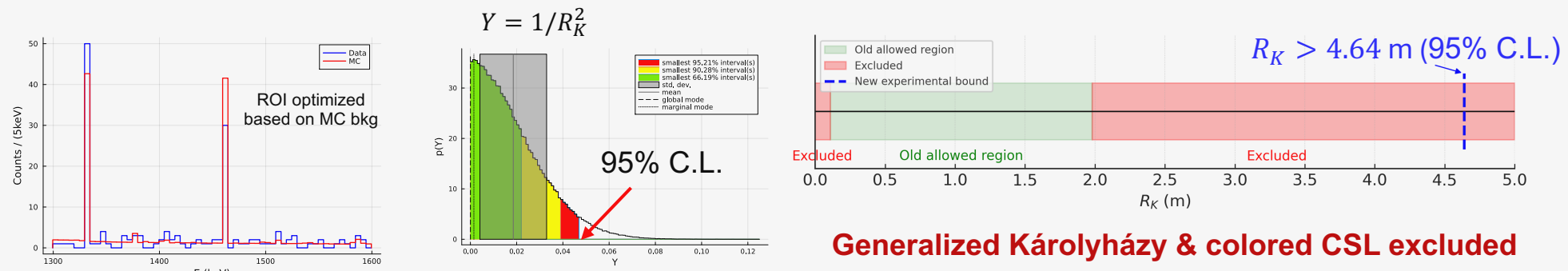
Károlyházy – experimental analysis

The Gaussian K. model is experimentally equivalent to a **non-Markovian version of the CSL!**

Collapse rate fixed by the Planck time $\lambda = \frac{t_p m_0^2 c^4}{4\hbar^2} = 27.5 \text{ kHz}$ $\longleftrightarrow$ **only 1 free parameter:** the correlation length R_K

Exact emission rate at energy $E = \hbar\omega = \hbar ck$:
$$\frac{d\Gamma}{dE} = \frac{\tilde{G}(E)}{6\pi^2 \epsilon_0 c^3 E} \sum_{ij} q_i q_j \frac{\sin kr_{ij}}{kr_{ij}} \left(-\nabla^2 \mathcal{D}(\mathbf{r}_{ij}) \right)$$

Optimal range 10 – 10⁵ keV: protons emit coherently, electrons incoherently
$$\frac{d\Gamma}{dE} = \frac{N_{at}(N_p^2 + N_e)\Gamma(2/3)\alpha_{\text{QED}}c^2 t_p^{4/3}}{\sqrt{3}\pi\hbar^{1/3} R_K^2 E^{2/3}}$$



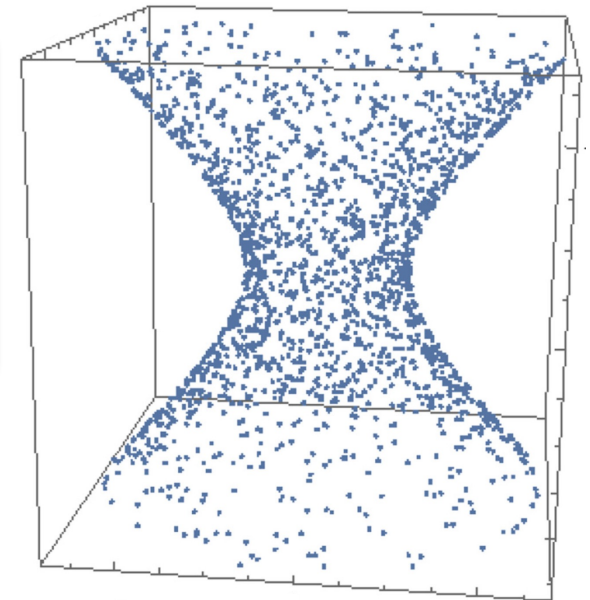
N.B., et al. *New J. Phys.* 28.6 (2026): 064511

Spacetime discreteness

A continuum manifold is an approximation of an underlying causal set, characterized by a fundamental **discrete volume** ℓ_c^3

Lorentz invariance can be preserved by randomly distributing, in the continuum manifold, the elements of the causal set according to a **Poisson process**

Geometric quantities such as the **length** of a geodesic become **stochastic variables**



(S. Surya *Living Rev Relativ* **22**, 5 2019)

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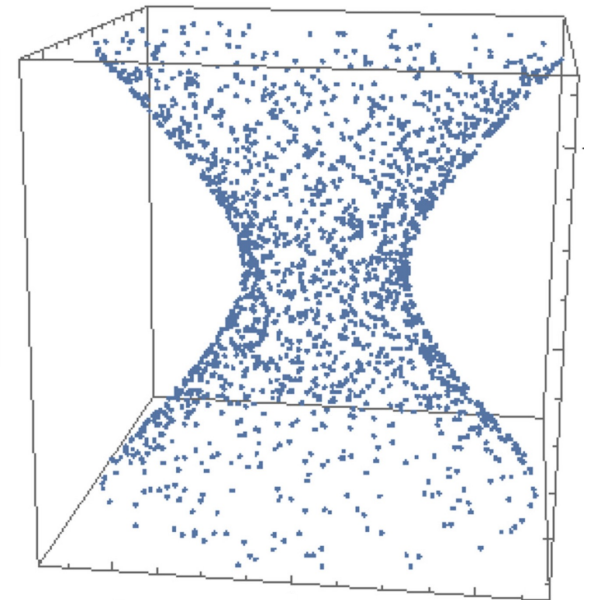
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A coarsened-grained manifold description unavoidably involves a **stochastic metric**

Same situation of **Károlyházy**; the only difference is the uncertainty



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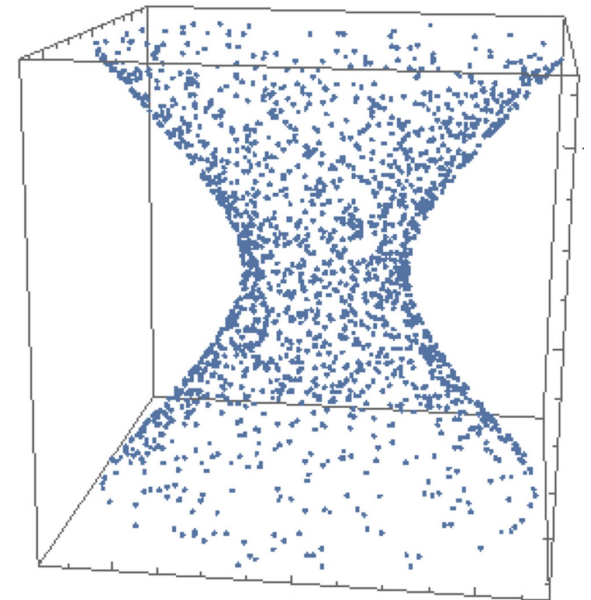
Same situation of **Károlyházy**; the only difference is the uncertainty

For example, assuming **poissonian clock ticks** with average time interval t_c **predicts the rate**

$$\text{(single particle)} \quad \frac{d\Gamma}{dE} \sim t_d \frac{\alpha_{QED} c^2 E}{6\pi^3 \hbar^2}$$

Notably, **κ -Minkowski spacetime** originates from such a time discretization (A. Arzano et al. PRD 111.2 025010 2025)

In general, we can assume the expression $\Delta l = \sqrt{\mathbb{E}[l]^\gamma \ell_c^{2-\gamma}}$, restricting $0 < \gamma < 2$ and yields $\frac{d\Gamma}{dE} \sim (\ell_c E)^{2-\gamma}$



(S. Surya *Living Rev Relativ* **22**, 5 2019)

Conclusions

- ❖ The unification of quantum mechanics and gravity generally predicts **rare EM radiation** from **PEP violation** or fundamental **uncertainty of the gravitational field**. Each process is characterized by a peculiar spectrum
- ❖ Spontaneous radiation probes both **QG scenarios** (e.g. CST and NCST) and **fundamentally classical gravity scenarios** (e.g. SCMs, postquantum theory of classical gravity)
- ❖ **Underground X-ray experiments** provide a unique opportunity to explore the quantum-gravity connection at interesting scales

- Quadratic GUP model $\beta/\ell_p^2 < 4.62 \times 10^{-2}$
- NCSTs must **break indistinguishability**
(κ -Poincaré): $\Lambda_1 > 10^{21}$ **Planck energy**
(θ -Poincaré): $\Lambda_2 > 0.1$ **Planck energy**
(Triply SR): $\Lambda_3 > 5.6 \times 10^{-9}$ **Planck energy**

Excluded models:

- Gaussian K gravity-induced decoherence
- Non-Markovian version of CSL

- ❖ **Ongoing improvements** on the **experimental set up** will either put stronger limits or hopefully see QG effects

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Thank you for your attention!

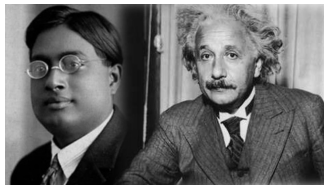
Backup slides

Quantum statistics: A (partial) hystorical perspective



W. Natanson discovers
indistinguishability of
Planck's quanta

1911



Bose-Einstein statistics for
photons and matter

1924

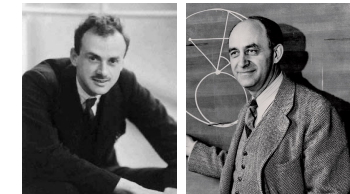


**Pauli's exclusion principle
(PEP)**

1925

1926

Fermi-Dirac statistics for
particles that obey the PEP



1934

Fermi investigates the case
of **"slightly non identical"**
particles

Large violations of statistics

1940



Spin-statistics theorem

G. Gentile Jr looked at intermediate statistics

1953



$$[a_i, [a_j, a_k]_{\pm}] = 0: \begin{array}{|c|c|} \hline \square & \square \\ \hline \end{array}, \begin{array}{|c|} \hline \square \\ \hline \square \\ \hline \end{array}, \begin{array}{|c|c|} \hline \square & \square \\ \hline \square & \square \\ \hline \end{array}$$

H.S. Green shows that **local QFT** is compatible with **parastatistics**

1964



Messiah & Greenberg:
indistinguishability =
parastatistics + selection rules

Color degree of freedom

Large violations of statistics



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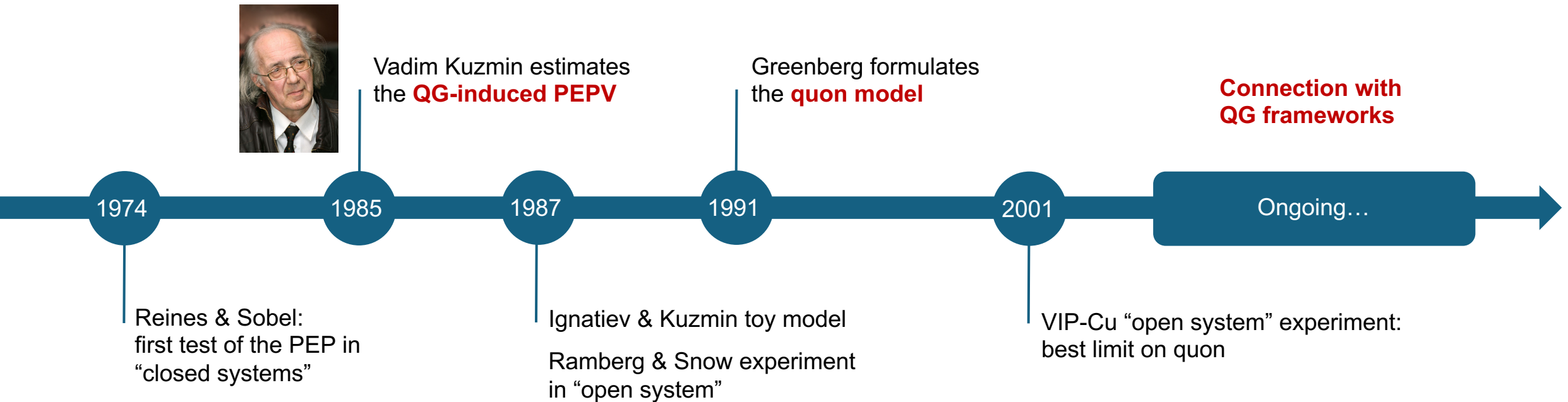
Messiah & Greenberg:
indistinguishability = parastatistics + selection rules
Color degree of freedom

All known particles are either bosons or fermions



Is this the end of the story?

Small violations of statistics



Hilbert space structure

❖ The state space of a system of **distinguishable** identical particles is the **full Fock space** $\mathfrak{F}(\mathfrak{H}) = \bigoplus_{n=0}^{\infty} \mathfrak{H}^{\otimes n}$

For all n , finite linear combinations of product states $|\xi_1, \dots, \xi_n\rangle \equiv |\xi_1\rangle \otimes \dots \otimes |\xi_n\rangle$ span the n -particle Hilbert space $\mathfrak{H}^{\otimes n}$

❖ The inner product of $\mathfrak{H}^{\otimes n}$ can always be written as

$$\left\{ \begin{array}{l} \langle \xi_n, \dots, \xi_1 | \chi_1, \dots, \chi_n \rangle = (\xi_n, \dots, \xi_1 | W_{(n)} | \chi_1, \dots, \chi_n) \\ (\xi_n, \dots, \xi_1 | \chi_1, \dots, \chi_n) = \langle \xi_1 | \chi_1 \rangle \cdots \langle \xi_n | \chi_n \rangle \\ W_{(n)} \text{ is positive: squared norms are non-negative} \end{array} \right.$$

In second quantization, $W_{(n)}$ is determined by the exchange relation

$$a(\tilde{p})a^\dagger(\tilde{q}) - \int_{\tilde{p}\tilde{q}} T(\tilde{k}, \tilde{l} | \tilde{p}, \tilde{q}) a^\dagger(\tilde{k})a(\tilde{l}) = \delta(\tilde{p}, \tilde{q})$$

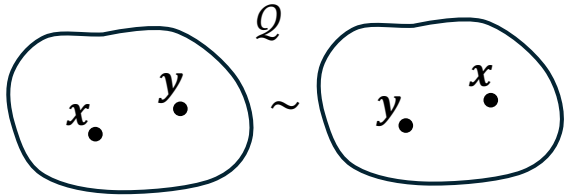
$$\text{e.g. } W_{(2)} = \frac{1}{2}(1 + T)$$

Hilbert space structure

Define the **flip operator** $\tau_R \equiv \tau R$ where $\tau|\tilde{p}, \tilde{q}\rangle = |\tilde{q}, \tilde{p}\rangle$ and $R|\tilde{p}, \tilde{q}\rangle = \int_{\tilde{k}\tilde{l}} R(\tilde{k}, \tilde{l}|\tilde{p}, \tilde{q})|\tilde{k}, \tilde{l}\rangle$

$|\psi\rangle = \int_{\tilde{p}\tilde{q}} \psi(\tilde{p}, \tilde{q})|\tilde{p}, \tilde{q}\rangle \in \mathfrak{H}^{\otimes 2}$ can always be decomposed as: $|\psi\rangle = \frac{1 + \tau_R}{2} |\psi\rangle + \frac{1 - \tau_R}{2} |\psi\rangle \equiv |\psi\rangle_{s_R} + |\psi\rangle_{a_R}$

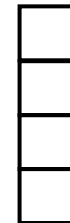
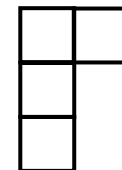
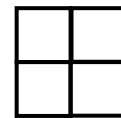
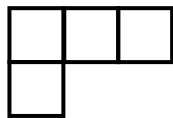
$\hat{\tau}_R$ must generate a unitary representations of the fundamental group $\pi_1(Q)$ of the configuration space



- In $d \geq 3$: Q is simply connected $\rightarrow \pi_1(Q) = \text{symm. group } S_n \rightarrow \tau_R^2 = 1$
- In $d < 3$: Q is multiply connected $\rightarrow \pi_1(Q) = \text{braid group } B_n \rightarrow \tau_R^2 = e^{i\phi}$ (anyons)

For arbitrary n , $|\psi\rangle = \sum_{\lambda} |\psi_{\lambda}\rangle$, where $|\psi_{\lambda}\rangle$ has exchange-symmetry given by the Young diagram λ

$n = 4$:



Indistinguishability of identical particles

❖ At least at energies $\ll$ Planck scale, identical particles are indistinguishable

Indistinguishability DOES NOT require the symmetrization postulate: $|\xi, \chi\rangle \nrightarrow |\chi, \xi\rangle_{\lambda_R}$, $a(\tilde{p})a(\tilde{q}) = \int_{\tilde{p}\tilde{q}} R(\tilde{k}, \tilde{l}|\tilde{p}, \tilde{q})a(\tilde{k})a(\tilde{l})$

It is sufficient the existence of **superselection rules (SSRs)**: $a_R\langle\psi|O|\phi\rangle_{s_R} = 0 \quad \forall \text{ observables } O$

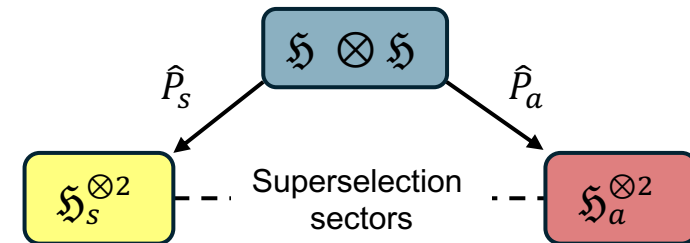
- $\hat{\rho}$ can be written in **block-diagonal** form! $\hat{\rho} = \sum_{\gamma} p_{\gamma} |\psi_{\gamma_R}\rangle\langle\psi_{\gamma_R}|$

- States are incoherent mixtures of different permutation symmetries, with weights**

$$p_{\gamma} = \frac{\|\psi_{\gamma_R}\|^2}{\sum_{\gamma'} \|\psi_{\gamma'_R}\|^2}$$

- $\|\psi_{\gamma_R}\|^2 = \langle\psi_{\gamma_R}|\psi_{\gamma_R}\rangle \Rightarrow p_{\gamma}$ **depend on the T operator**

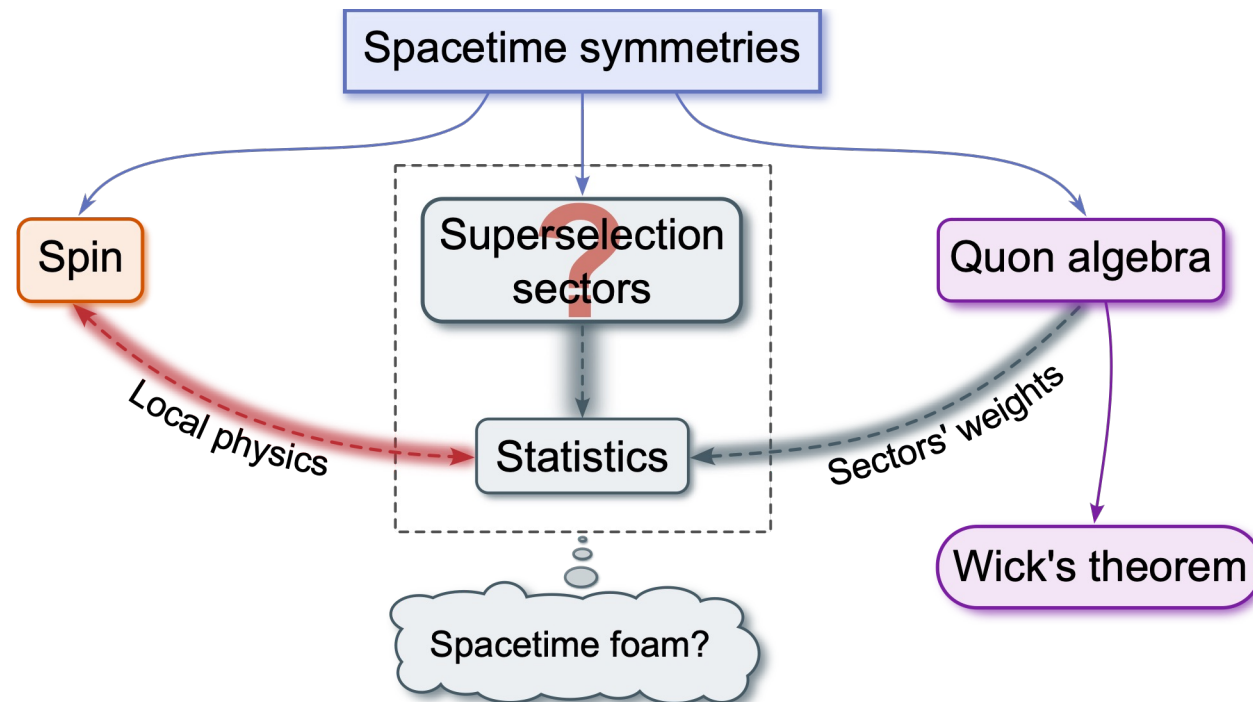
- Superselection sectors $\mathfrak{H}_{\lambda}^{\otimes n}$ + weights $p_{\gamma} =$ **statistics**



Spacetime symmetries

Let $U(g)$ be a unitary representation of the Poincaré group on $\mathfrak{H}^{\otimes n}$, where $g = \{a, \Lambda\}$. Then:

- The inner product must be invariant $(U(g)\psi|W|U(g)\phi) = (\psi|U(g)^\dagger W U(g)|\phi) \Rightarrow U(g)T = TU(g)$
- Permutation of particles must be compatible with spacetime transformations $\Rightarrow U(g)\tau_R = \tau_R U(g)$



Atomic states

Rigorous relativistic treatment of atomic states is based on Green functions

- pole structure contains bound states
- treat interactions nonperturbatively
- provide dynamical evolution

Bethe-Salpeter (BS) amplitudes: $\phi(x, y) = \langle \Omega | T \{ \Psi(x) \Psi(y) \} | B \rangle$

$$G_0 \sim \frac{\phi(p, q) \phi^\dagger(p', q')}{2E_p(P^0 - E_p + i\epsilon)} + G_0 = \text{diagrammatic equation}$$

— electron
— nucleus

BS equation for the amplitude $\phi(p, q)$

❖ The generalization to twisted-quons leads to **two distinct scenarios**:

$$G = \left(G + Q^* \text{crossed } G \right) + Q^{*'} \left(\text{crossed } G + Q_\theta^* \text{crossed } G \right)$$

The kernel preserves superselection rules

$$G_\lambda = \text{diagram with } \mathcal{K}' \text{ and } G_\lambda$$

The physical states are those with **twisted statistics**

The kernel breaks superselection rules

$$G = \text{diagram with } \mathcal{K} \text{ and } G$$

Identical particles are slightly different

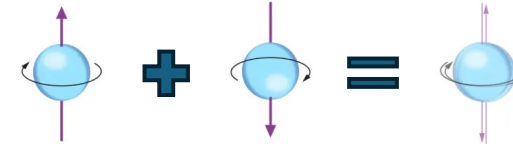
Poincaré Hopf-algebra

Poincaré algebra	
$[P_\mu, P_\nu] = 0$ $[M_{\mu\nu}, M_{\rho\sigma}] = i(\eta_{\nu\rho}M_{\mu\sigma} - \eta_{\mu\rho}M_{\nu\sigma} - \eta_{\nu\sigma}M_{\mu\rho} + \eta_{\mu\sigma}M_{\nu\rho})$ $[M_{\mu\nu}, P_\rho] = -i(\eta_{\mu\rho}P_\nu - \eta_{\nu\rho}P_\mu)$	Action of the generators on single particle states
Poincaré co-algebra	
$\Delta(Y) = Y \otimes \mathbb{1} + \mathbb{1} \otimes Y, \quad Y = \{P_\mu, M_{\mu\nu}\}$	Action of the generators on multi particle states

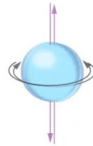
Quantum mechanics à la Copenhagen

Quantum systems:
linear and deterministic

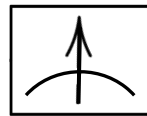
$$\frac{d}{dt}|\psi_t\rangle = -\frac{i}{\hbar}\hat{H}|\psi_t\rangle$$



$(\alpha|\uparrow\rangle + \beta|\downarrow\rangle)$



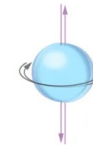
$|m_0\rangle$



Quantum
measurement

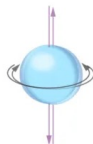


$\alpha|\uparrow\rangle|m_\uparrow\rangle + \beta|\downarrow\rangle|m_\downarrow\rangle$

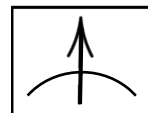


Interaction with measurement devices:
nonlinear and stochastic

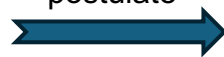
$(\alpha|\uparrow\rangle + \beta|\downarrow\rangle)$



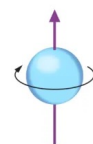
$|m_0\rangle$



Collapse
postulate

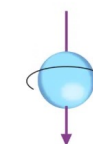


$|\uparrow\rangle|m_\uparrow\rangle \quad p_\uparrow = |\alpha|^2$



OR

$|\downarrow\rangle|m_\downarrow\rangle \quad p_\downarrow = |\beta|^2$



There are other interpretations
but yields same predictions

Current goals

Test of PEP-violation at the Planck scale

Improve on efficiency: use Ge detector as active material → gain of about four orders of magnitude



2 orders of magnitude improvement on Δ from PEPV

For Ge standard $K_\alpha = 9.9$ keV:

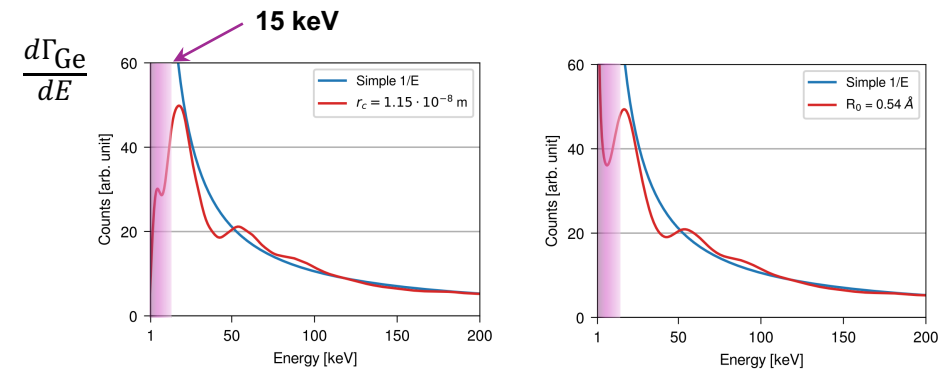
need a lower energy threshold around 6 keV



Use a Broad Energy Germanium (BEGe) detector to push down the energy range of the spectrum

Low energy behavior of spontaneous radiation

- At low energy DP and CSL modulate the rate in different ways!



- Energy cutoff E_c is expected for colored models

- Ranges from ~ 1 keV up to several MeV
- Excellent resolution and efficiency at low energies