



Using Proper Scoring Rules for training Neural Networks

how to get honest uncertainties

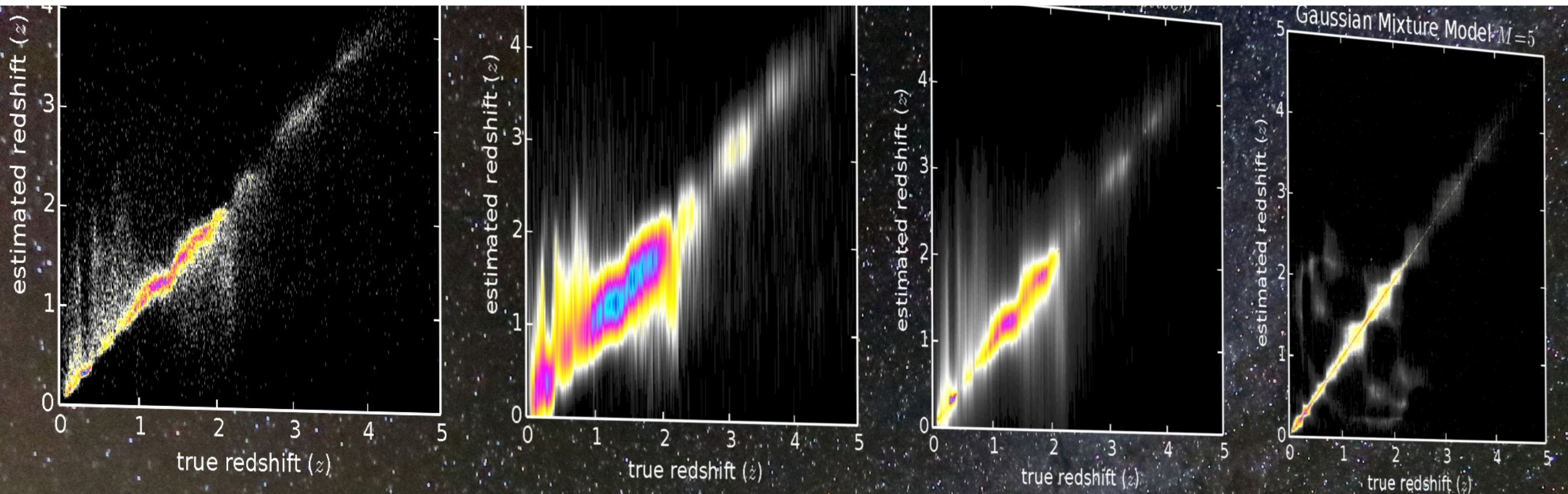


model

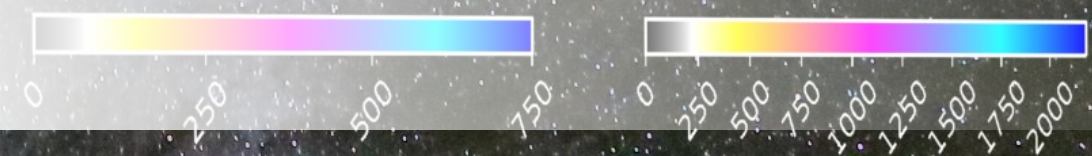
estimate


$$f(\vec{x}) \rightarrow y, \text{ where } \vec{x} \in \mathbb{R}^n, y \in \mathbb{R}$$

features



Regression Problems in Astronomy



summed probability density

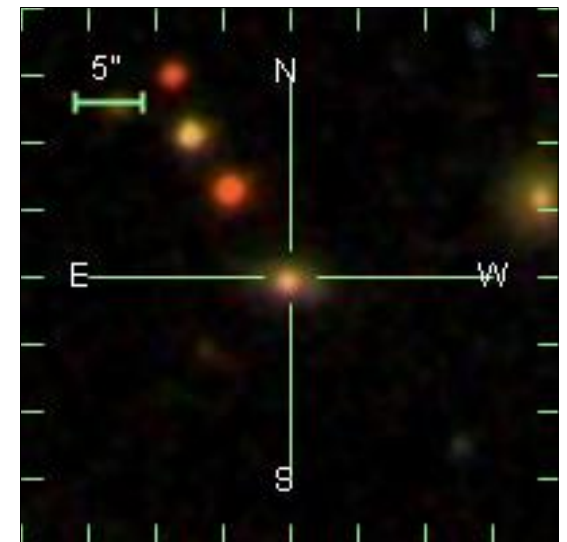
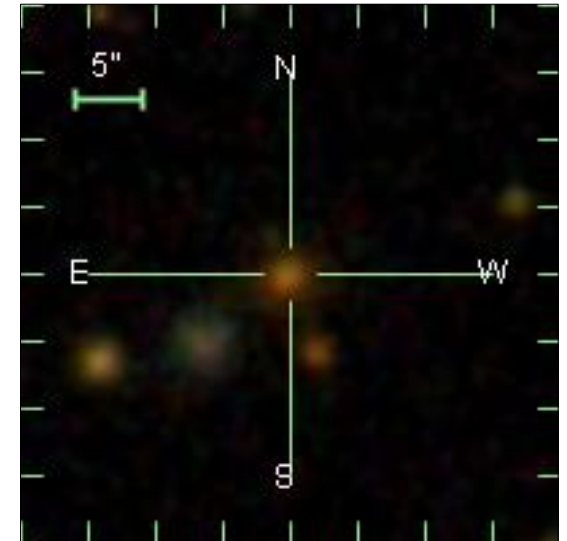
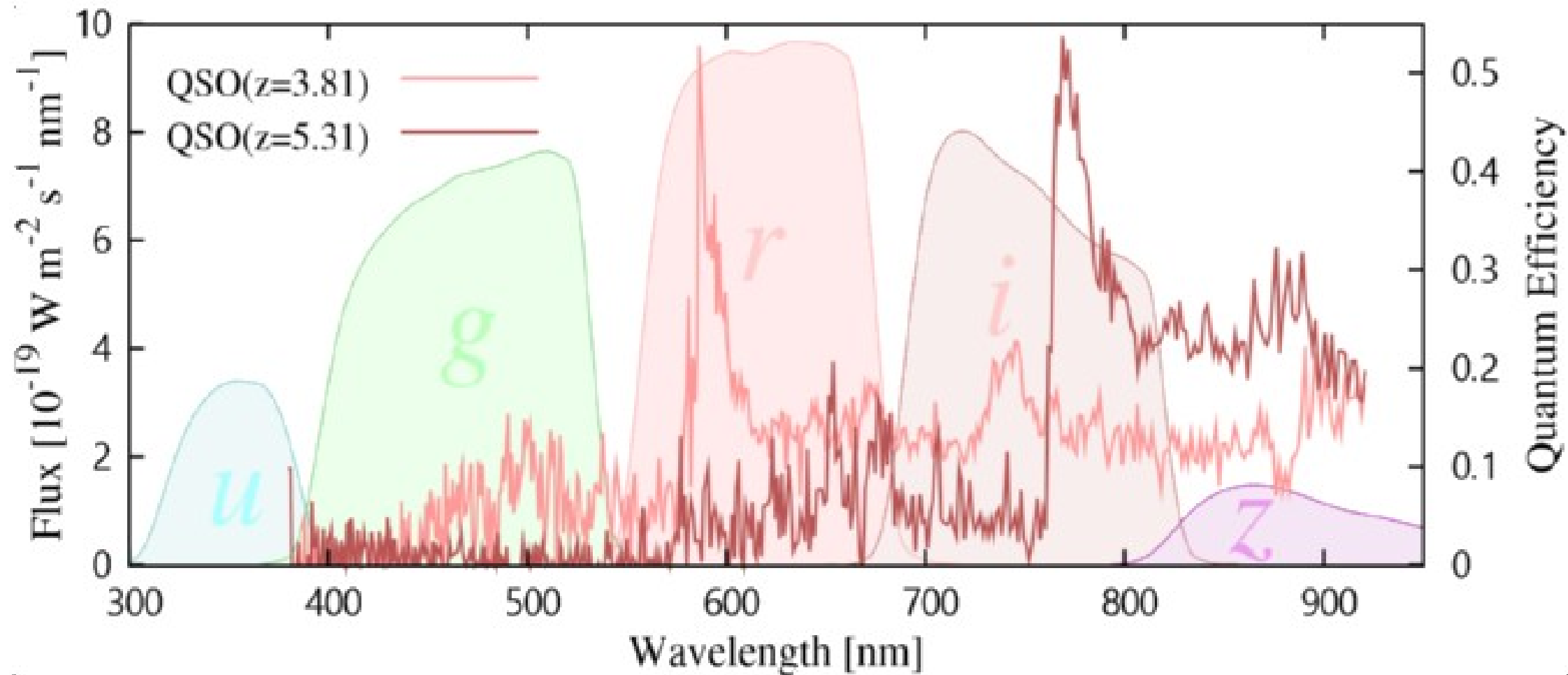
summed probability density

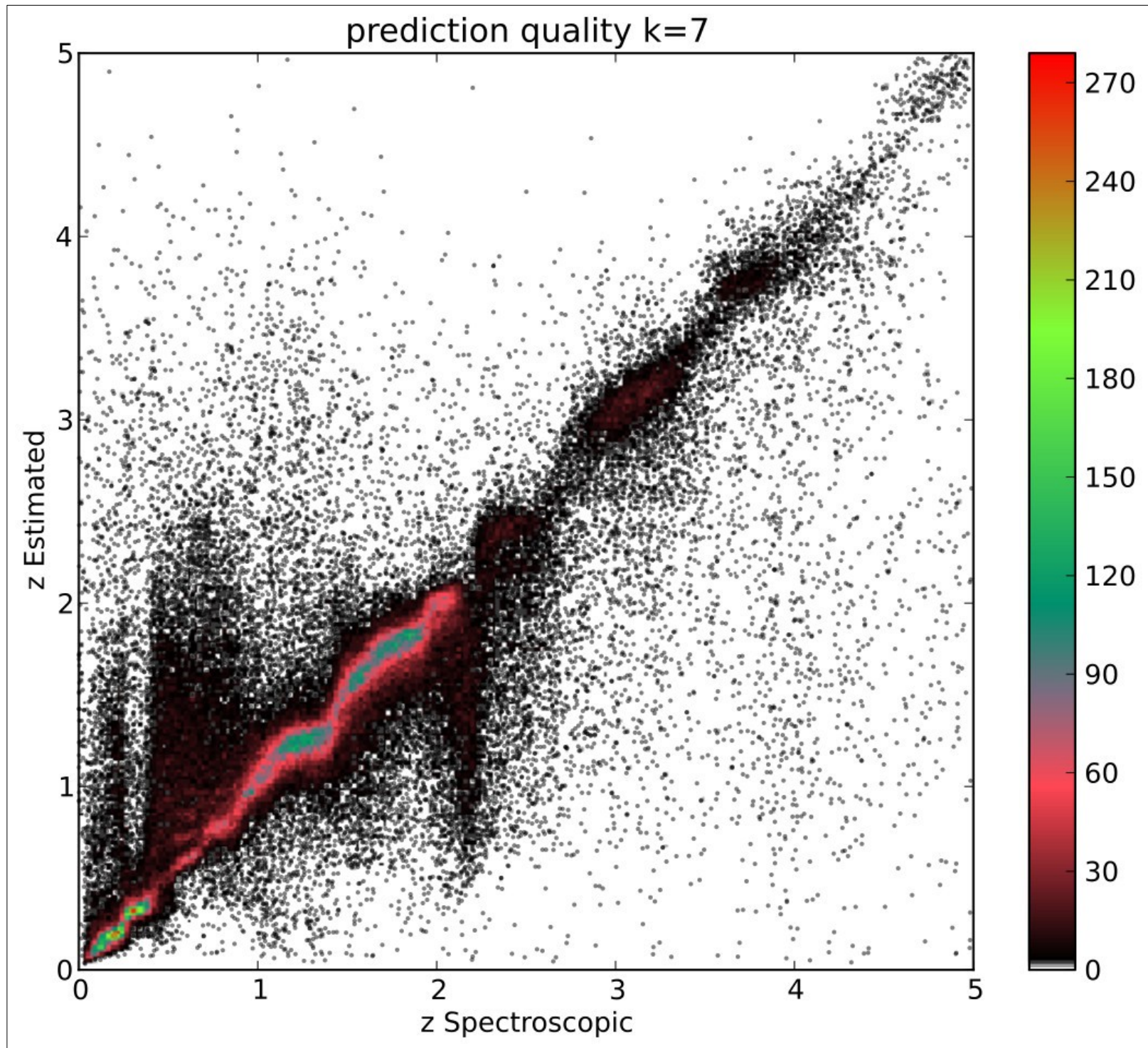
photometric redshift estimation

Estimating Redshift Photometrically



$$1 + z = \frac{\lambda}{\lambda_0}$$





Experiment with all
quasars in SDSS DR7

Uncertainties

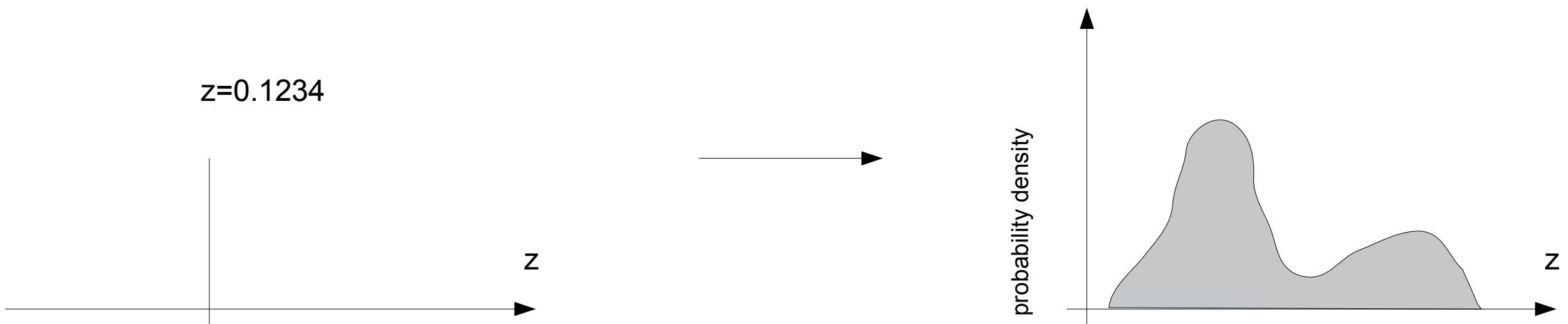


$$f(\vec{x}) \rightarrow y, \text{ where } \vec{x} \in \mathbb{R}^n, y \in \mathbb{R}$$

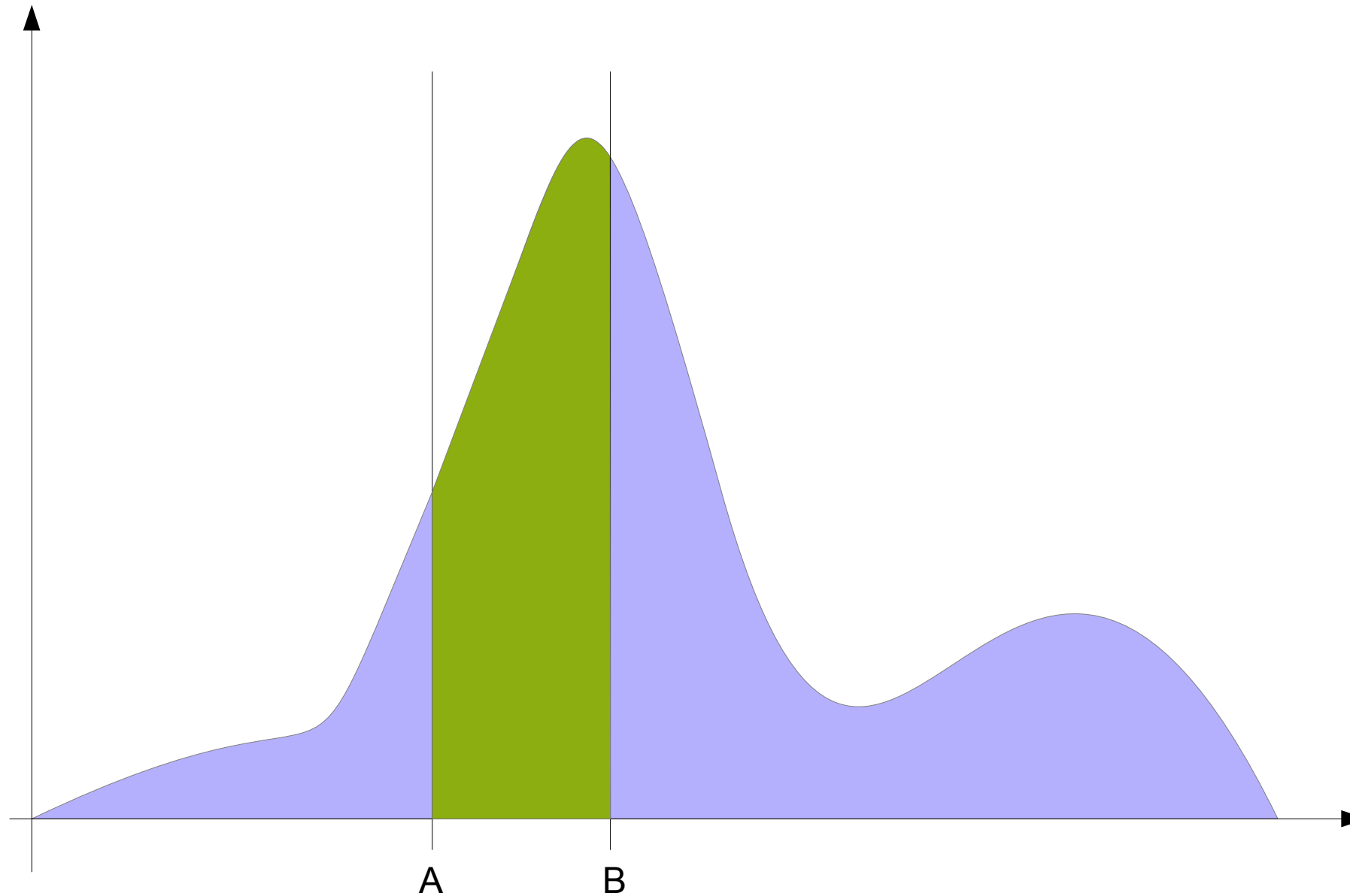
model uncertainty

input uncertainty

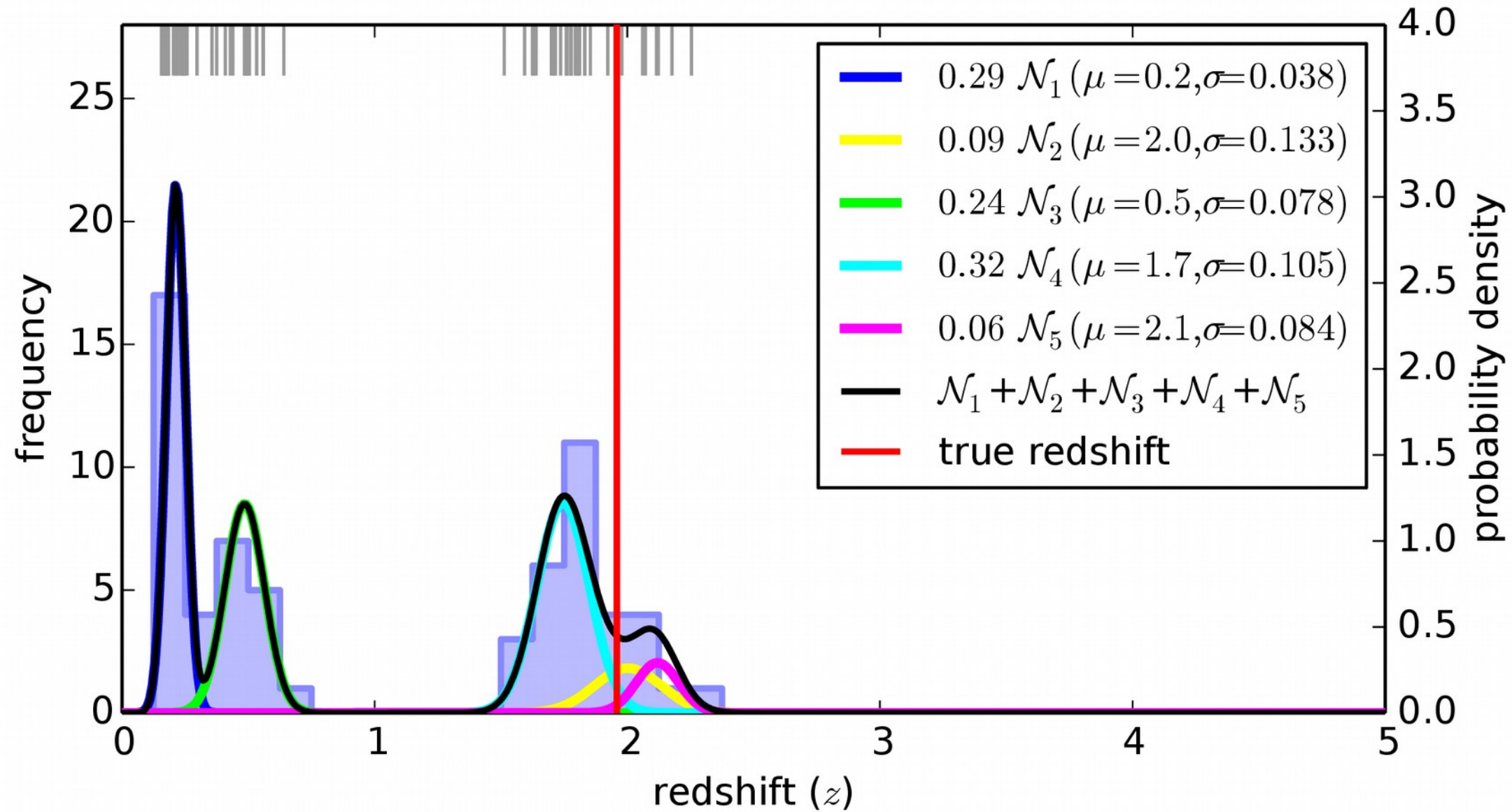
uncertain estimate



Probability Density Function



Multi-Modalities

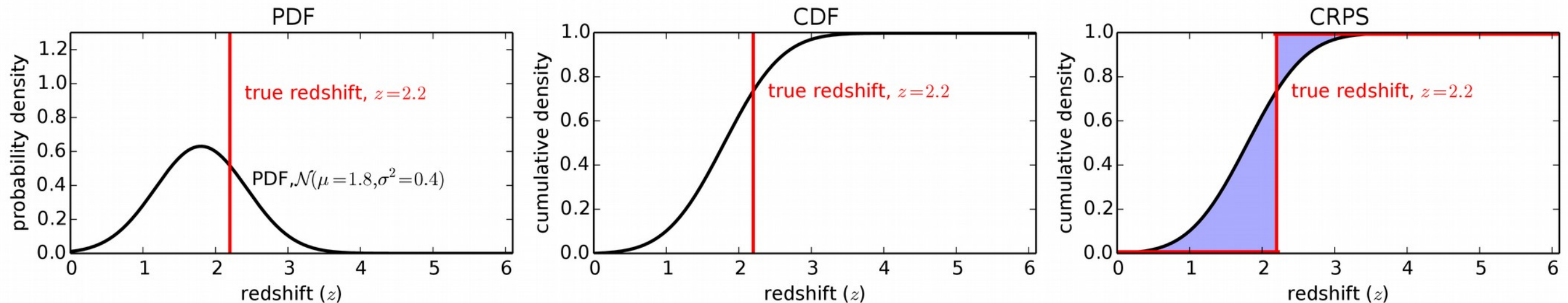


Proper Evaluation Tools / CRPS

continuous rank probability score

$$CRPS = \frac{1}{N} \sum_{t=1}^N crps(CDF_t, z_t),$$

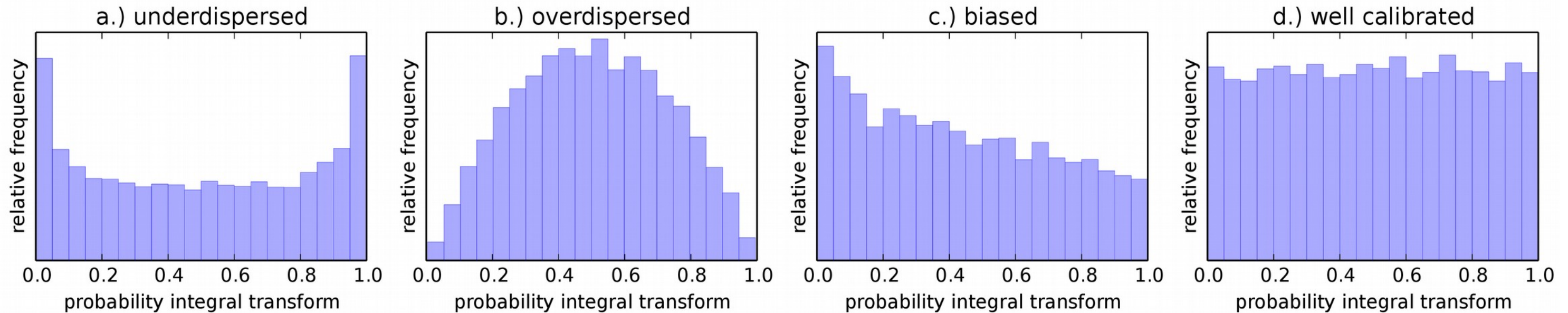
$$\text{with } crps(CDF_t, z_t) = \int_{-\infty}^{+\infty} [CDF_t(z) - CDF_{z_t}(z)]^2 dz$$



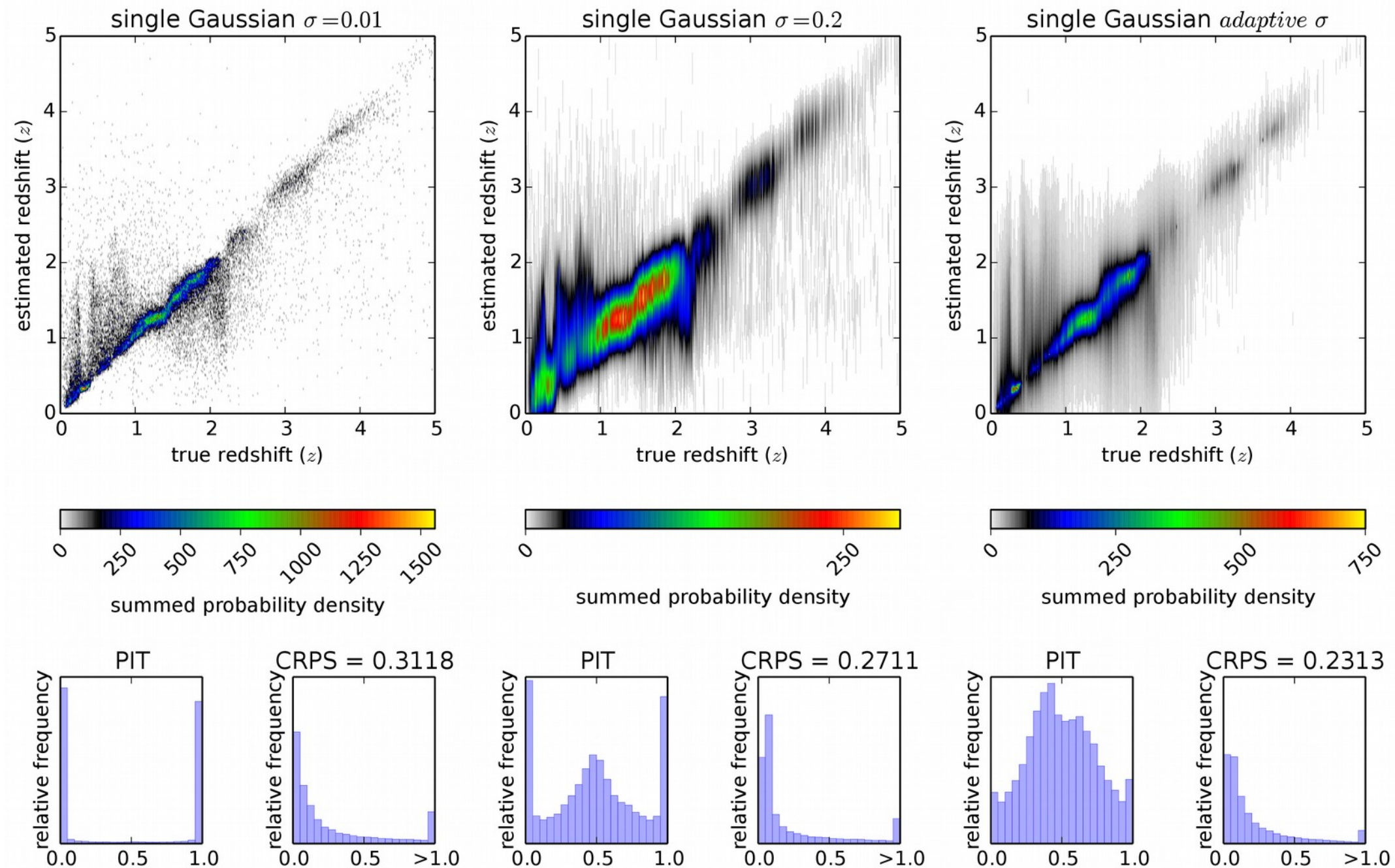
Proper Evaluation Tools / PIT



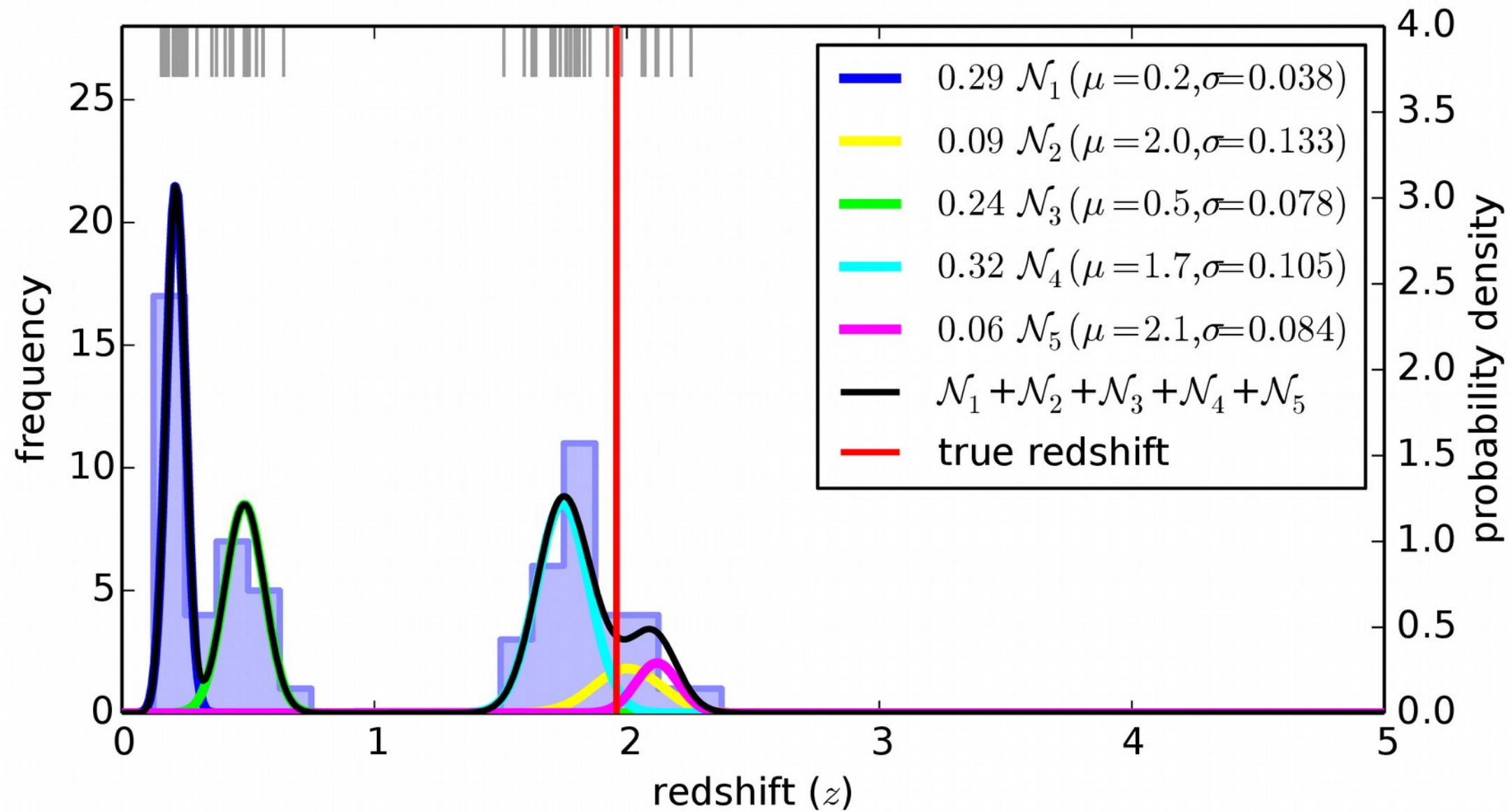
probability integral transform



Uncertain Results / kNN



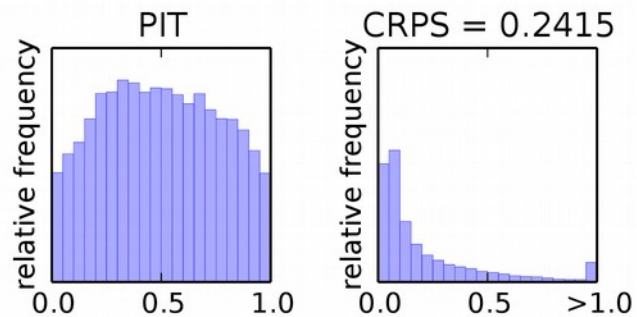
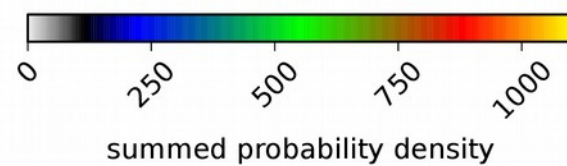
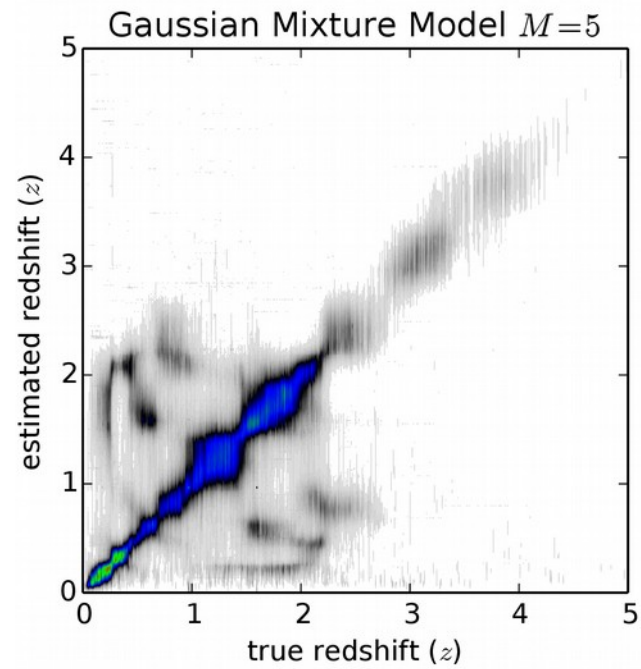
Multi-Modalities



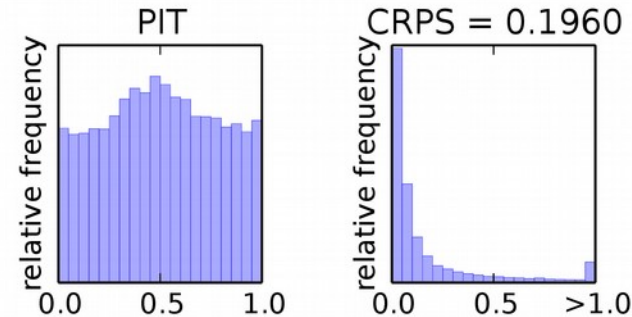
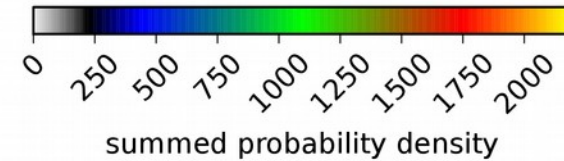
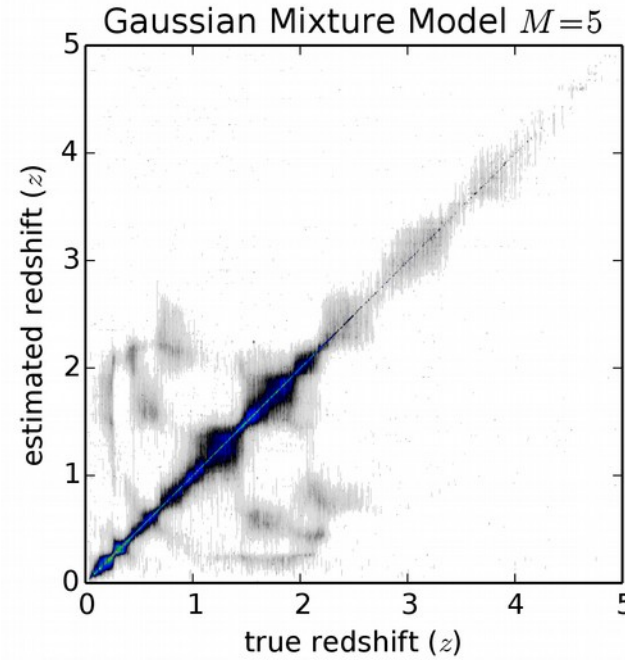
Results



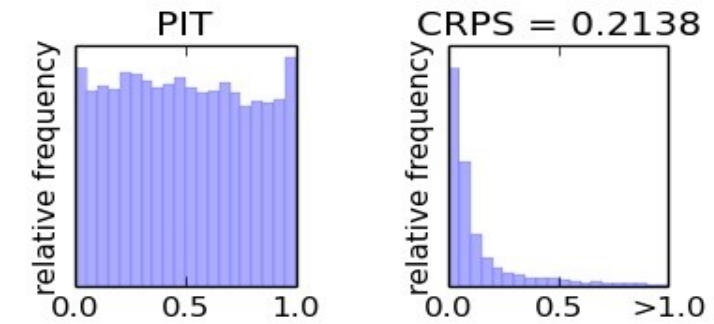
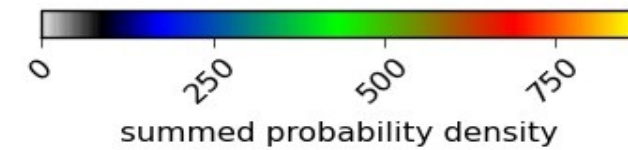
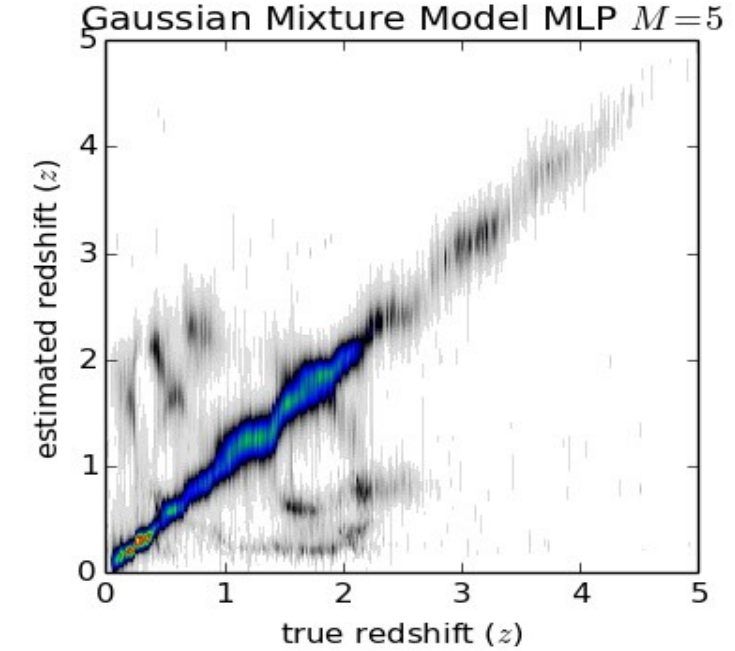
Nearest Neighbors



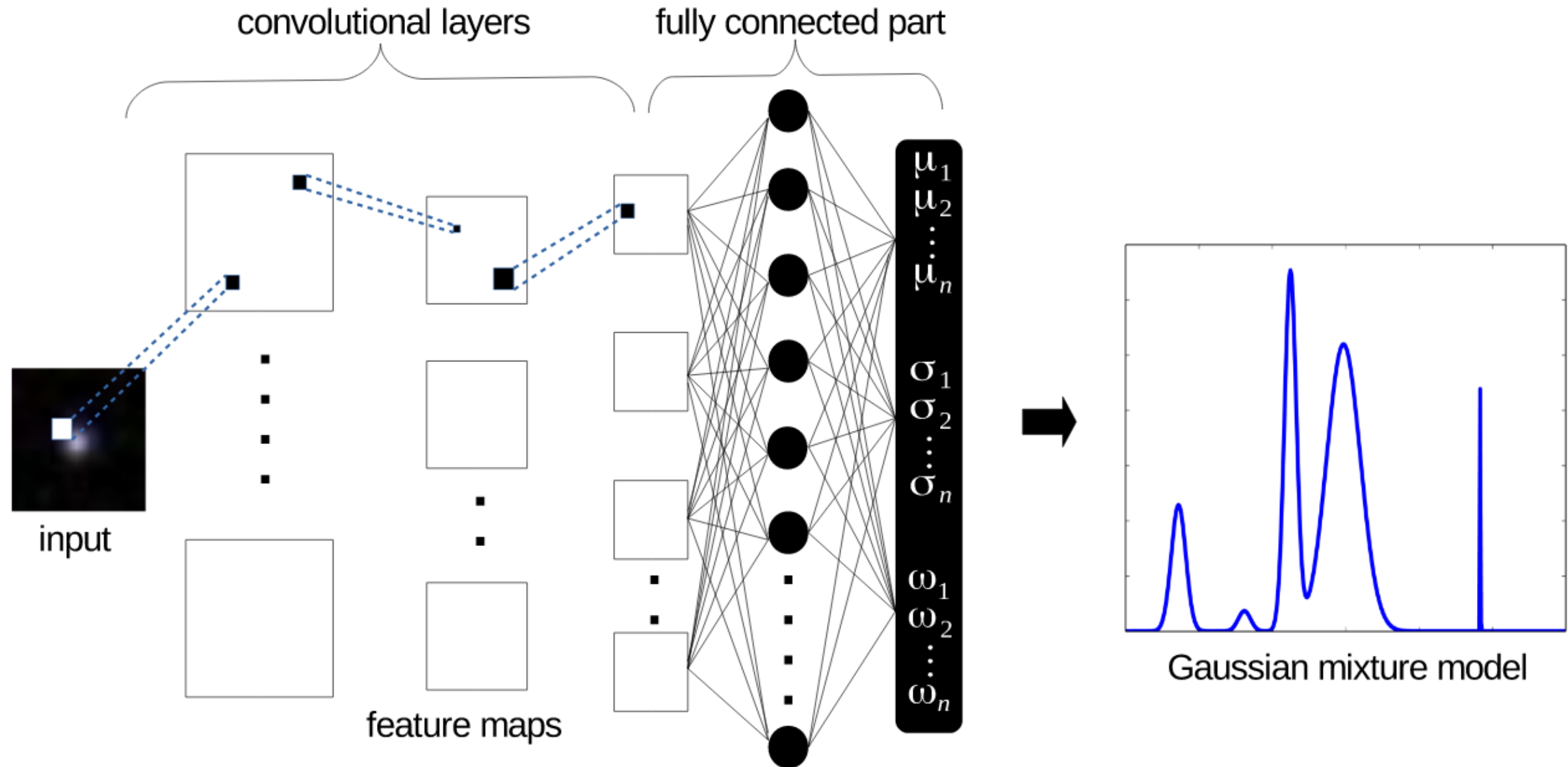
Random Forest



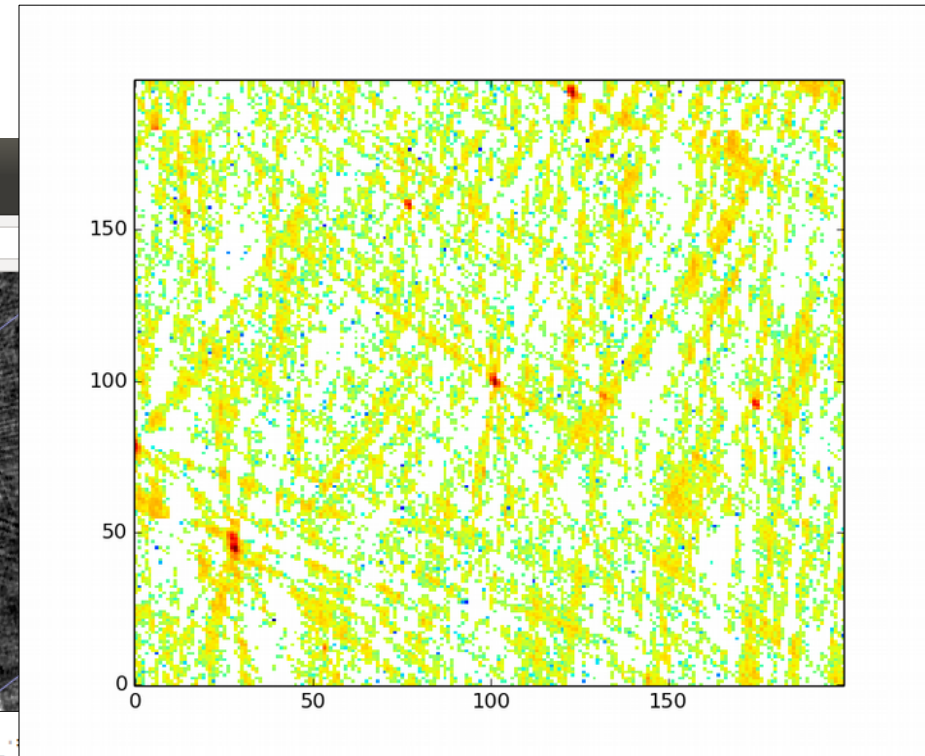
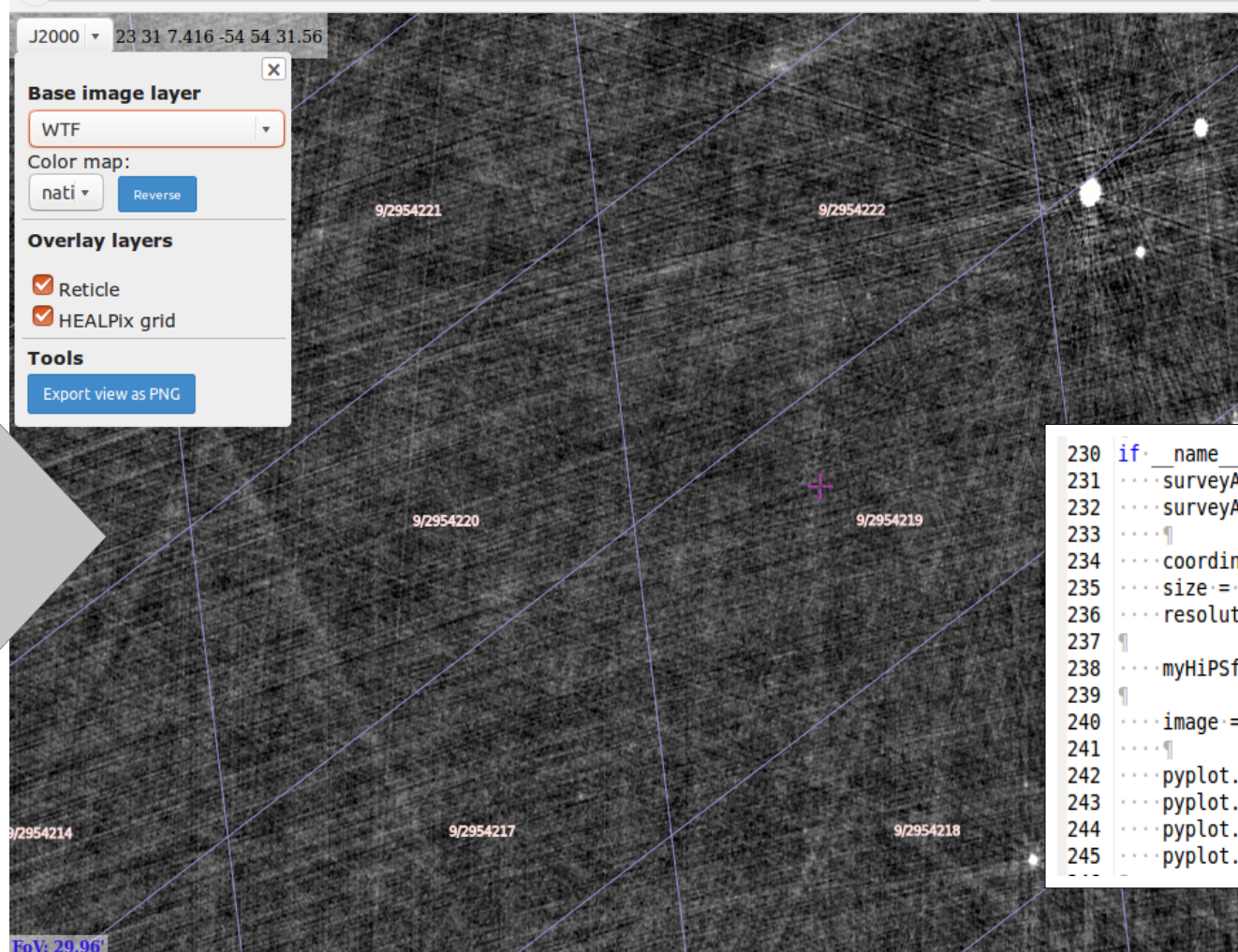
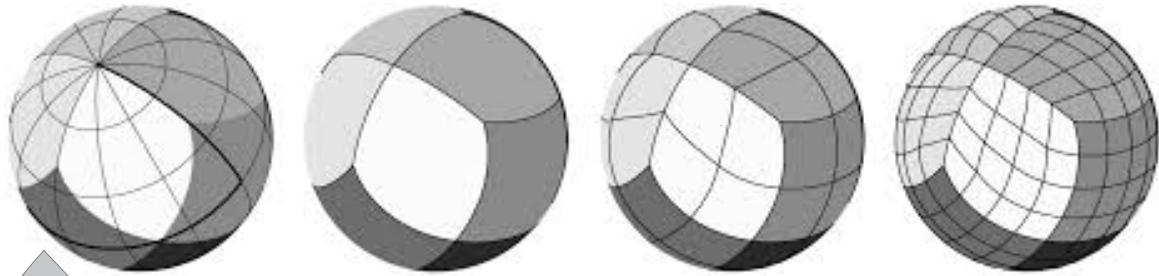
Mixture Density Network



DCN meet MDN

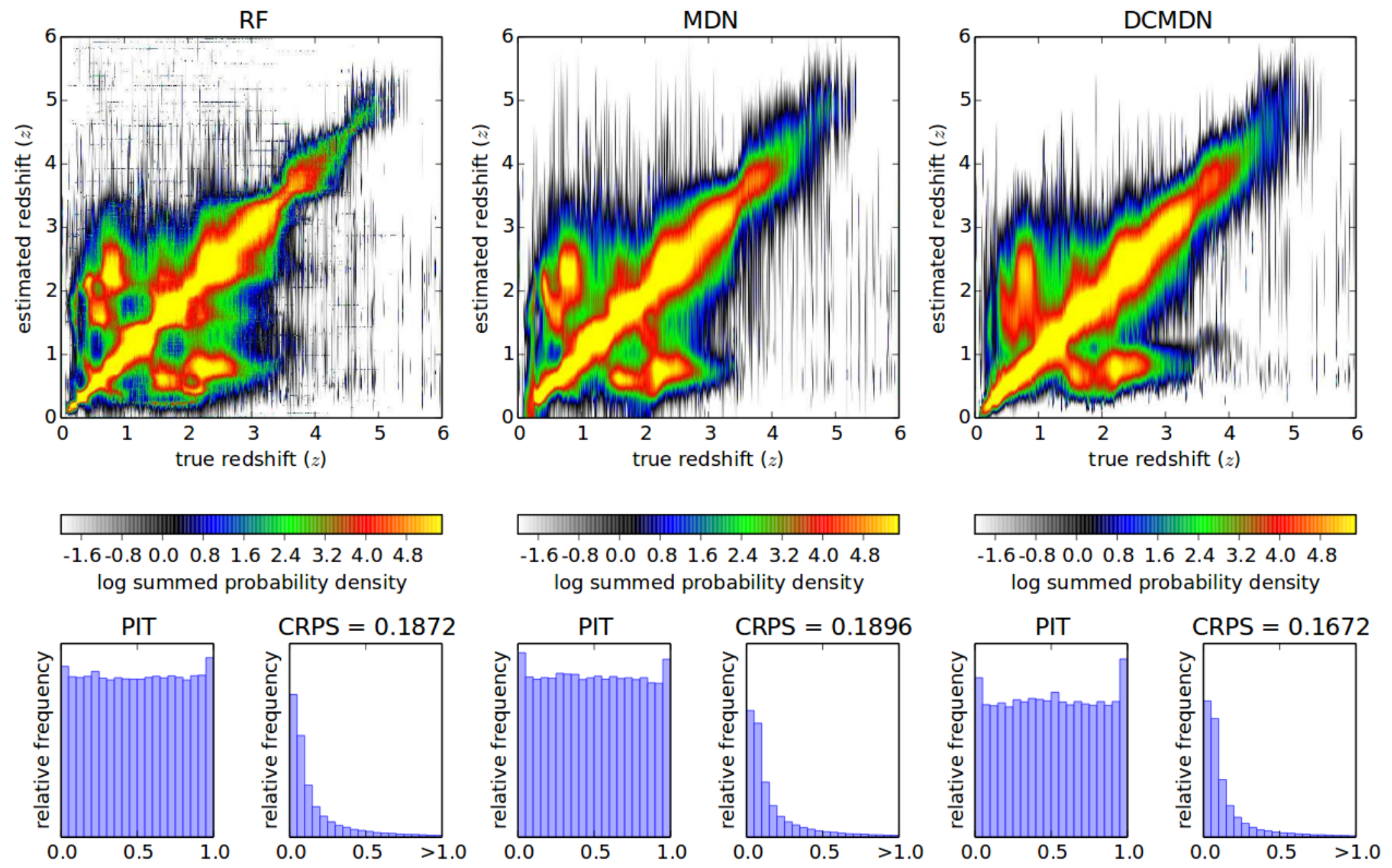


Healpix / HiPS / IVOA



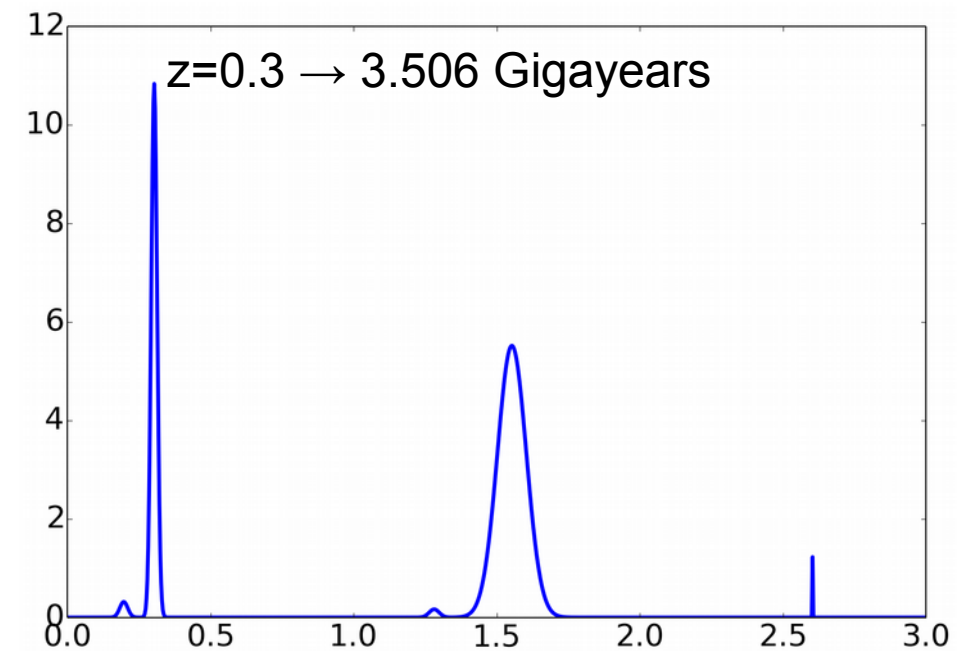
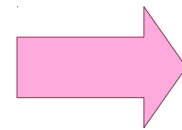
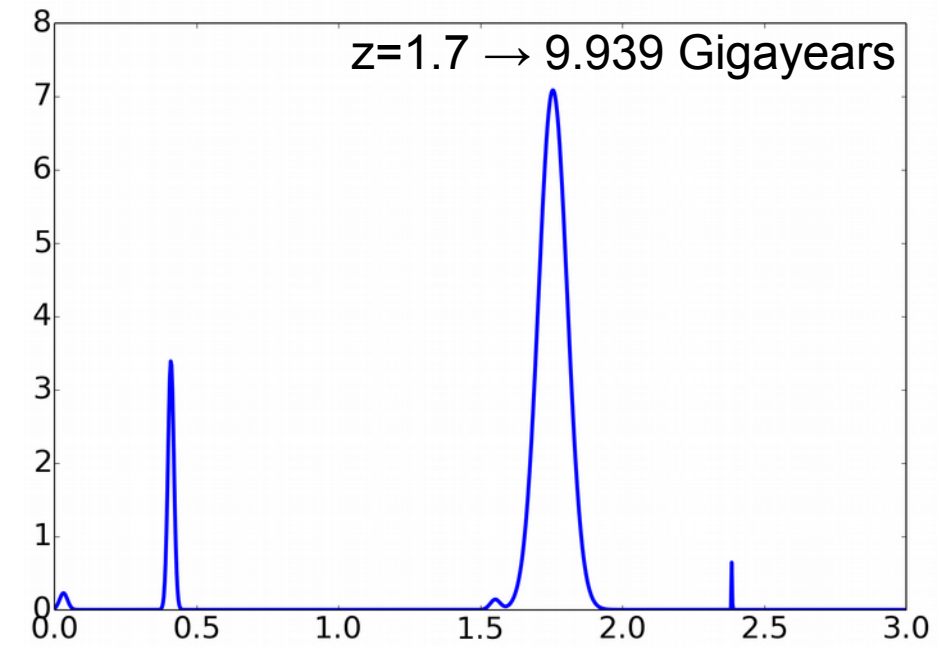
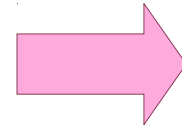
```
230 if name:
231     surveyAddress = "atlas-spt-hips-2.s3-website-ap-southeast-2.amazonaws.com/ATLAS-SPT-64x64"
232     surveyAddress = "alaska.u-strasbg.fr/DSS/DSS2Merged" # DSS red
233
234     coordinate = [350.86, -55.225]
235     size = [200, 200]
236     resolution = 0.002
237
238     myHiPSfs = HiPSfs(surveyAddress) # create access
239
240     image = myHiPSfs.extractCoordinate(coordinate, size, resolution, nested=True) # extract data array
241
242     pyplot.figure()
243     pyplot.imshow(image, aspect='auto', interpolation="nearest")
244     pyplot.gca().invert_yaxis()
245     pyplot.show()
```


Results



D'Isanto 2018

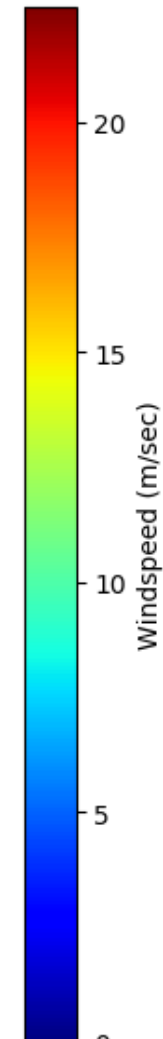
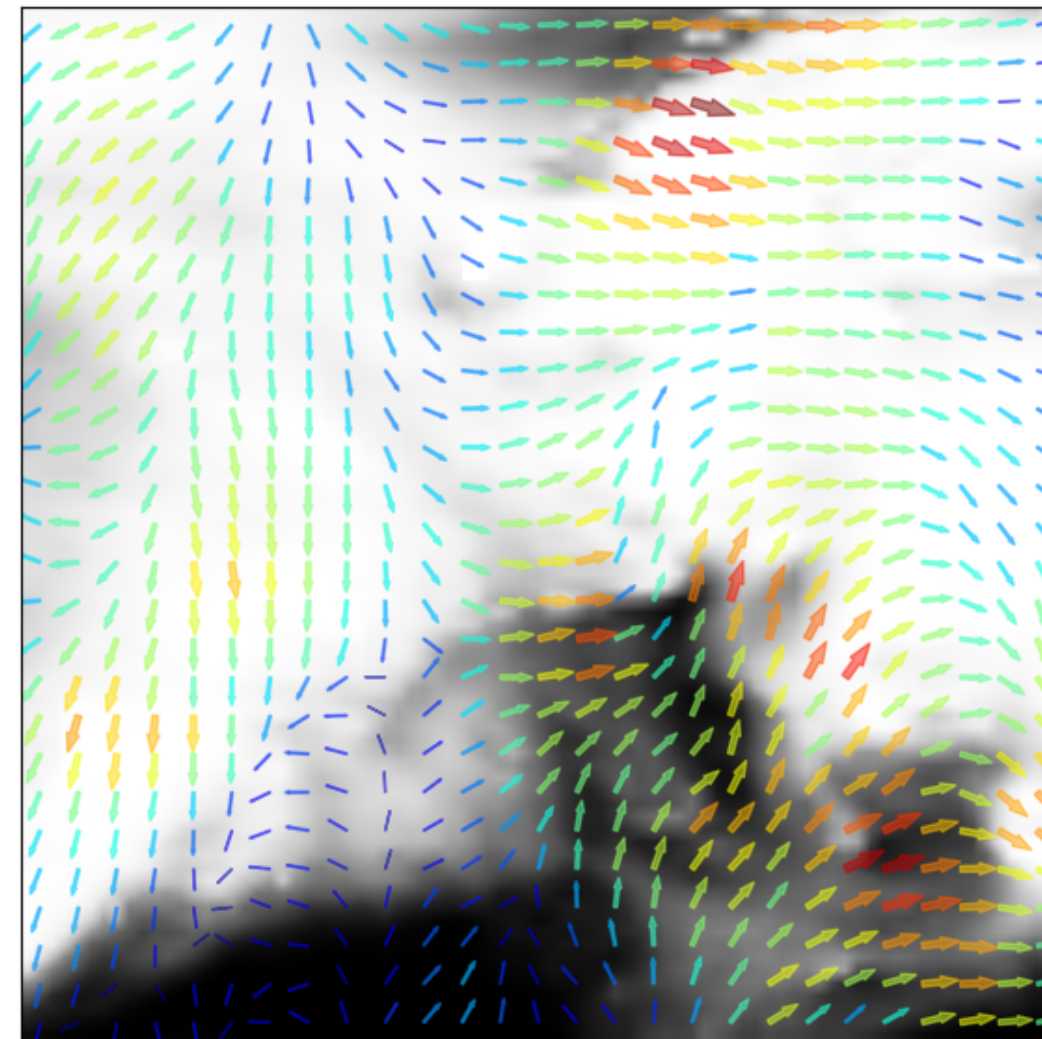
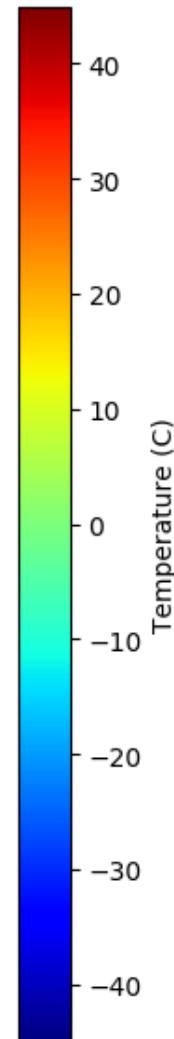
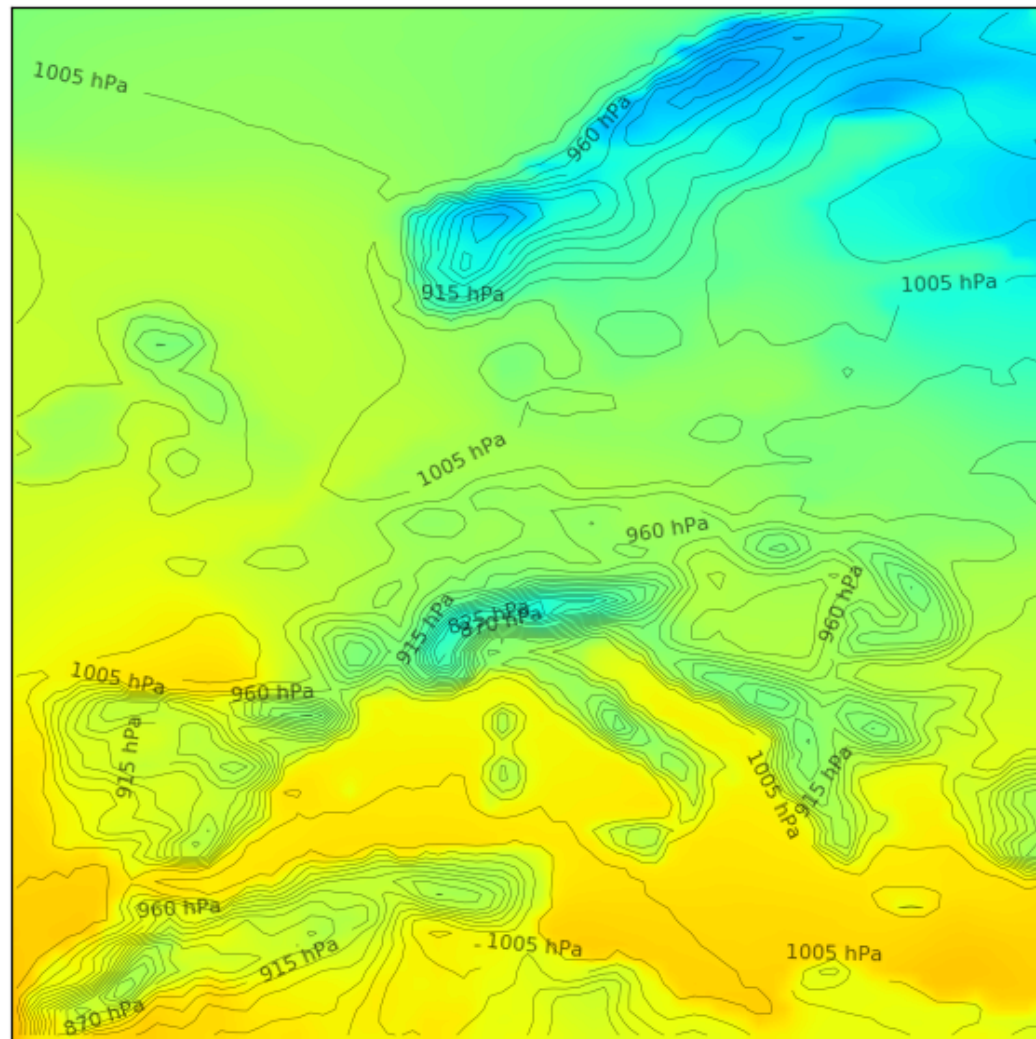
Challenges / Limitations



Weather Forecast Simulations



European Centre for Medium-Range Weather Forecasts (ECMWF)

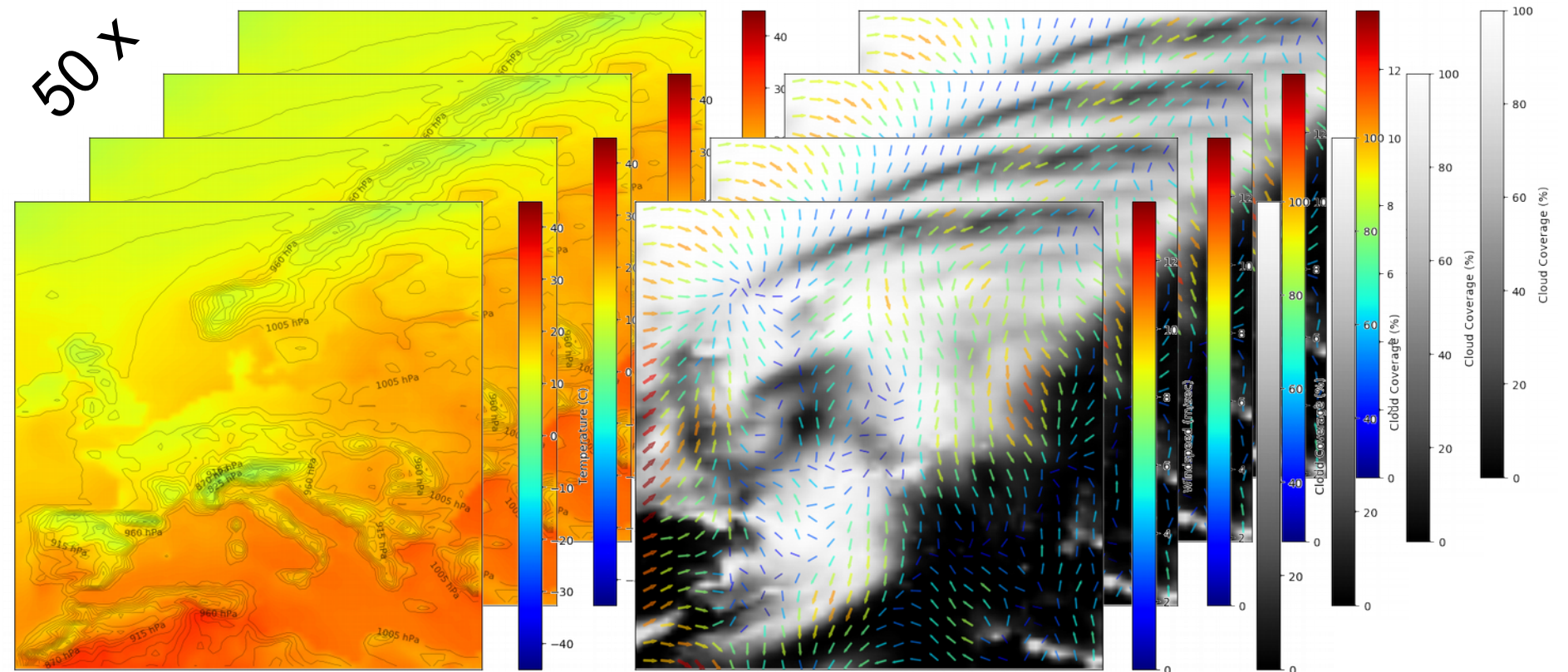


Weather Forecast Simulations



In this example 18 parameters on 81x81 grid for Europe (0.5°, 0.5°)

- t2m: air temperature 2m above ground
- cape: convective available potential energy
- sp: surface pressure
- tcc: total cloud cover
- sshf: sensible heat flux
- slhf: latent heat flux
- u10: 10-meter U-wind
- v10: 10-meter V-wind
- d2m: 2-meter dew point temperature
- ssr: short wave radiation flux
- str: long wave radiation flux
- sm: soil moisture
- u pl500: u-wind at 500 hPa
- v pl500: v-wind at 500 hPa
- u pl850: u-wind at 850 hPa
- v pl850: v-wind at 850 hPa
- gh pl500: Geopotential at 500 hPa
- q pl850: specific humidity at 850 hPa



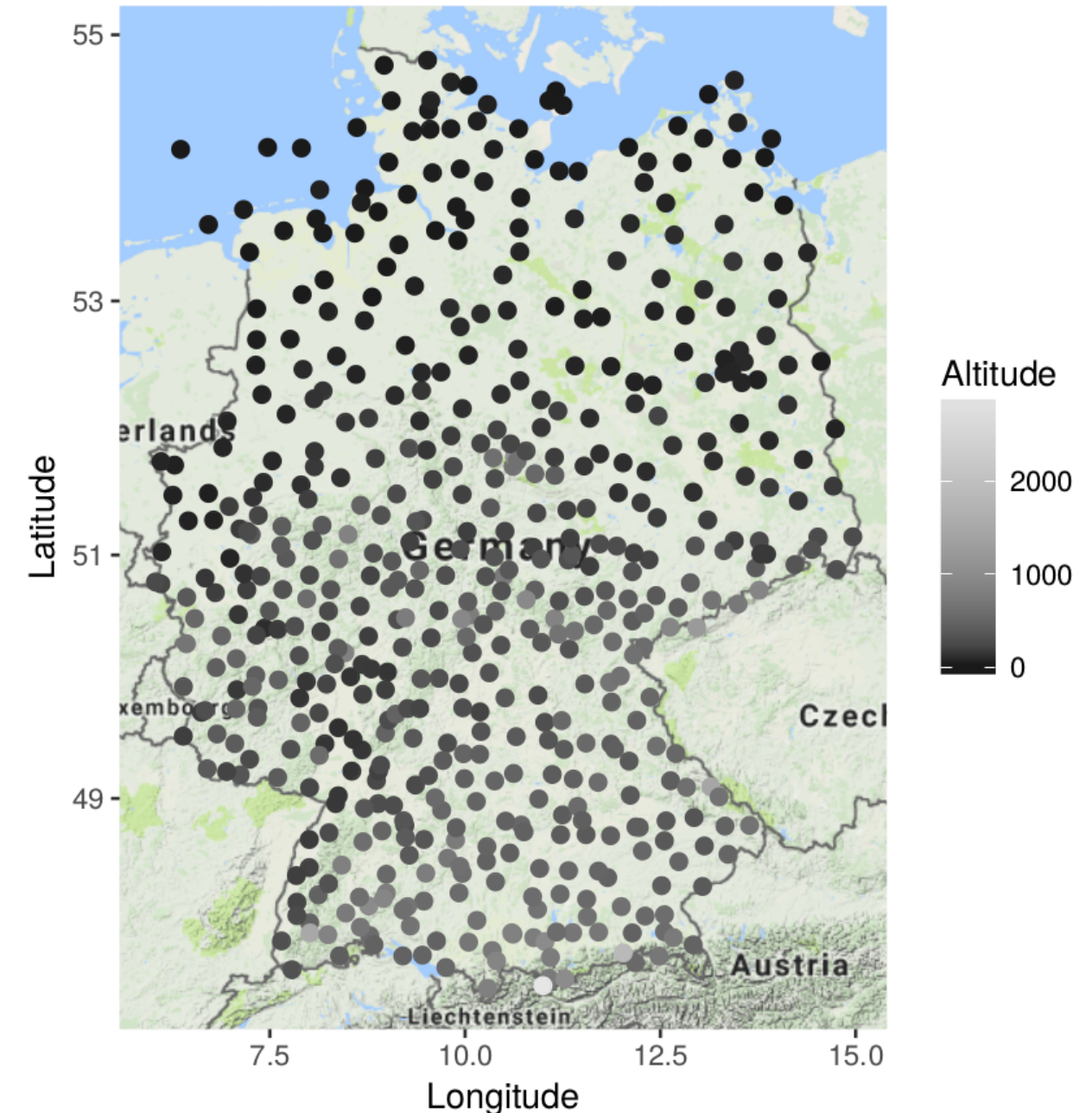
Statistical Post-Processing



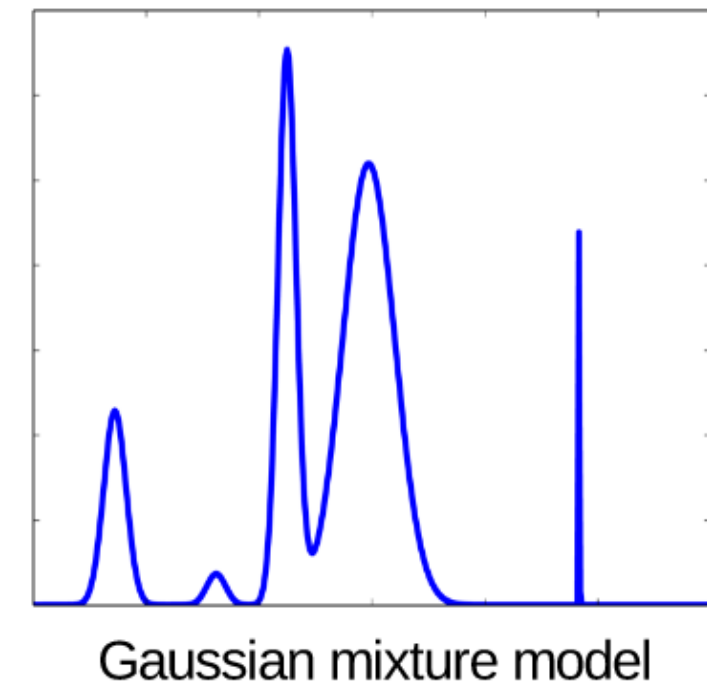
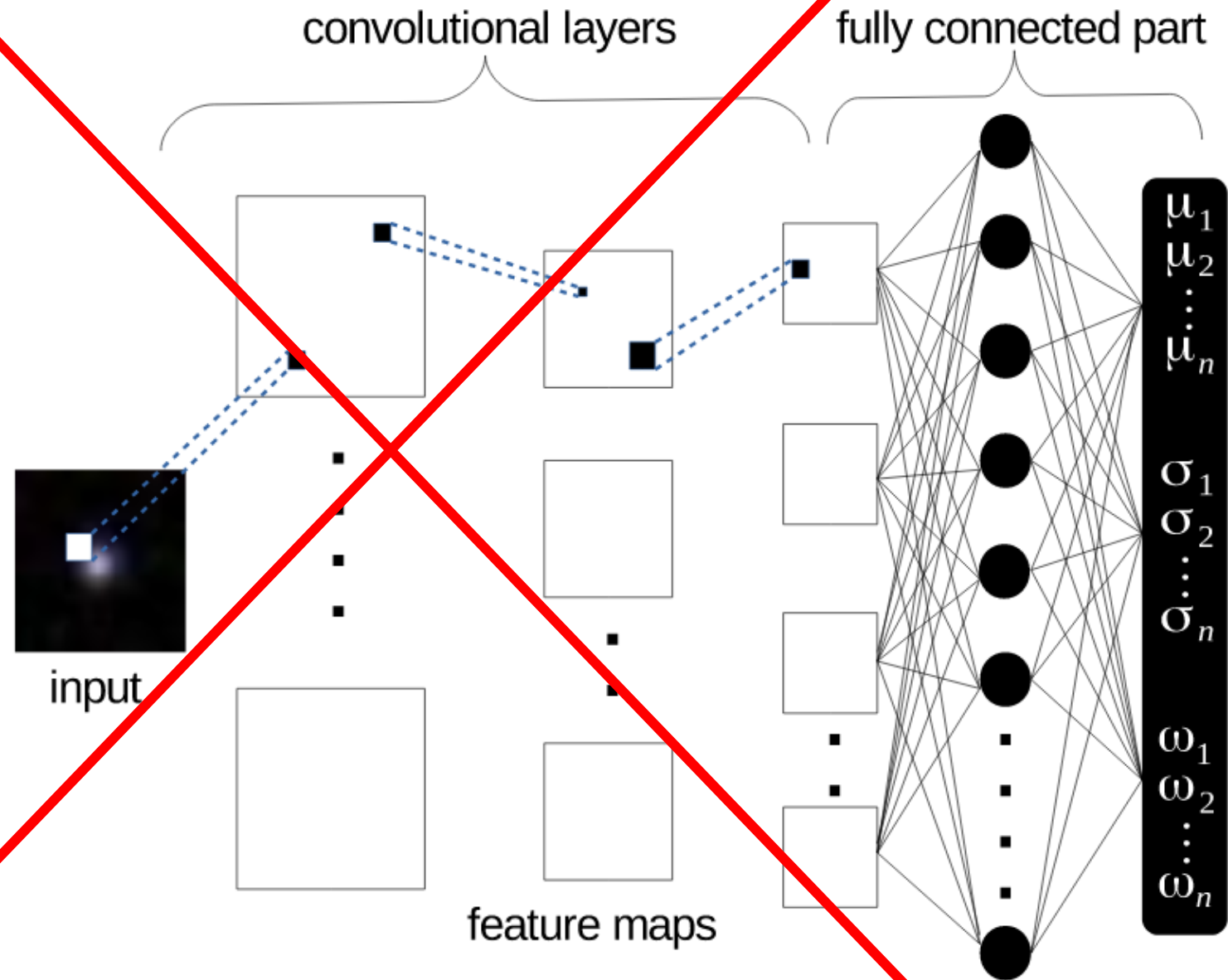
to predict for single stations

- 537 stations with measurements
 - (lat, long, alt, orog., land/sea)
- 48h forecast lead time
- 18 x 2 parameters (mean, stddev)
- 2007-2015 for training
- 2016 for testing

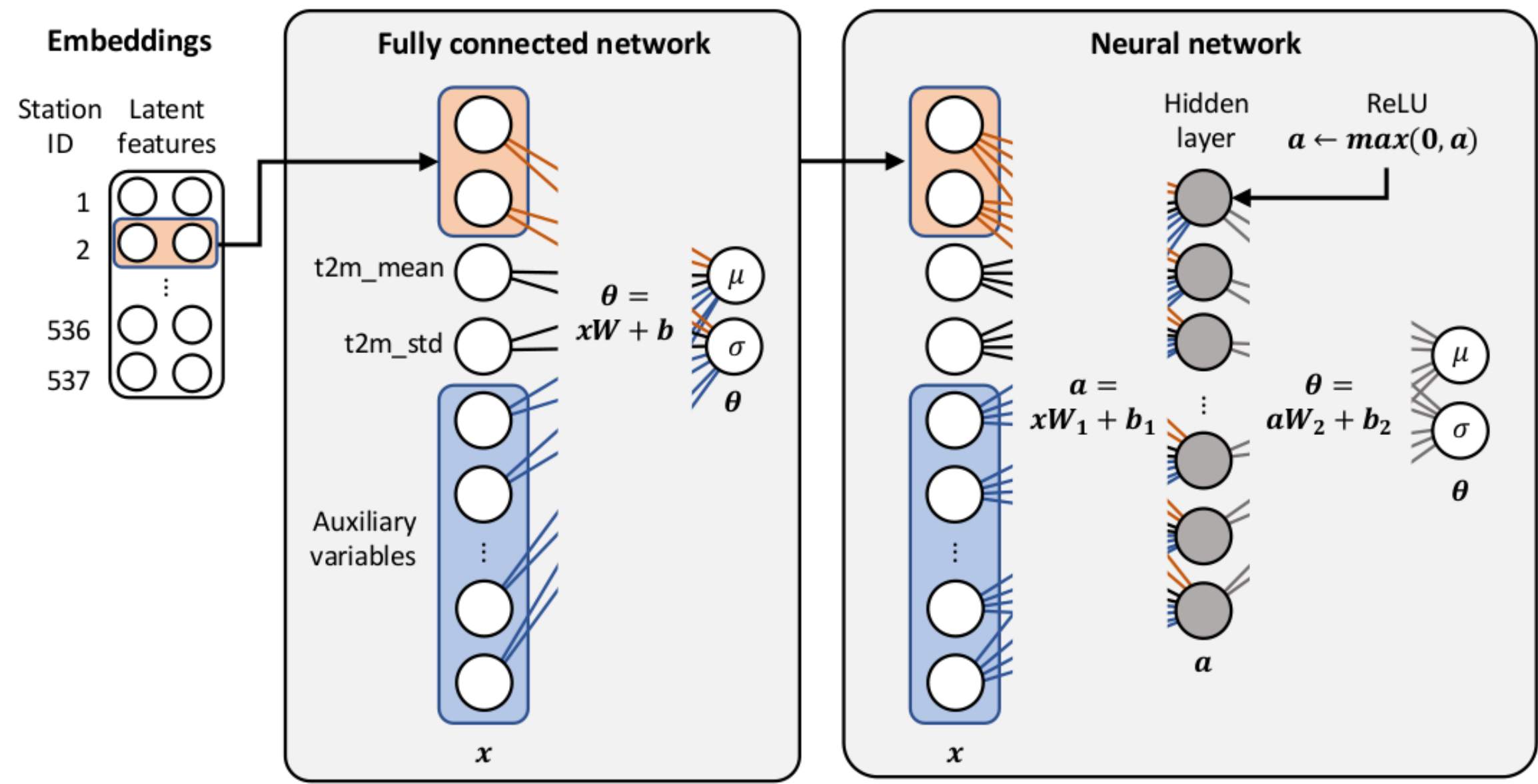
with best method CRPS=0.81



DCN meet MDN



Using DCMDN

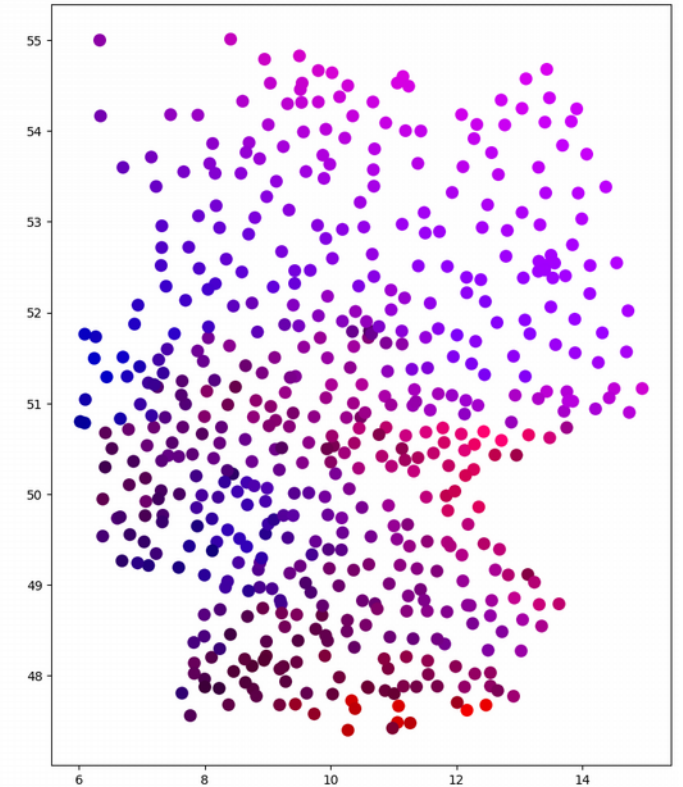
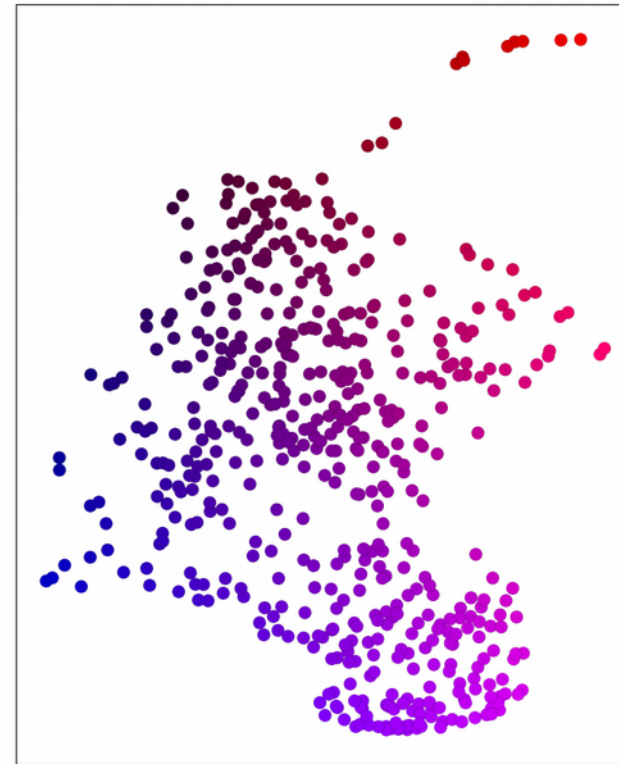
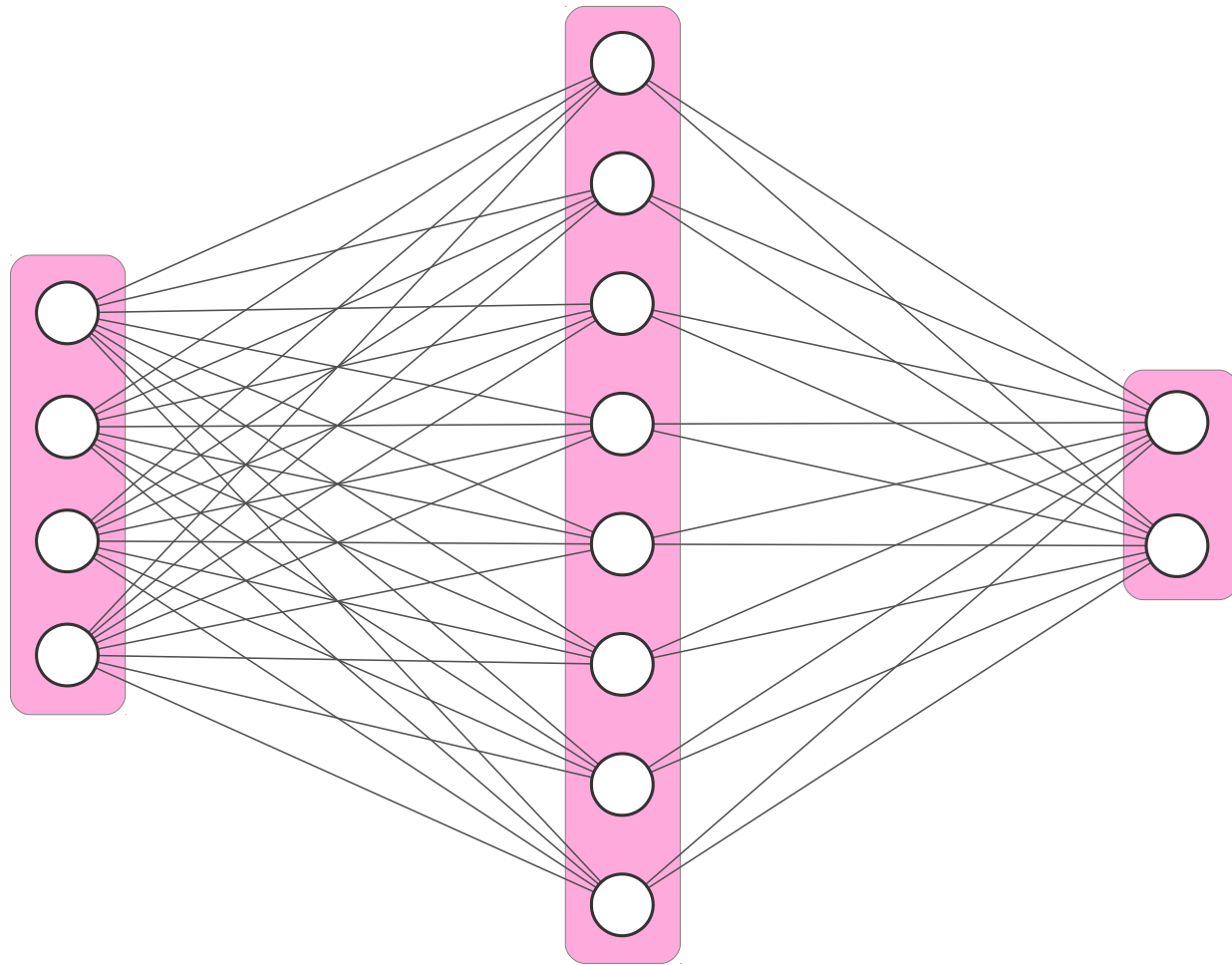


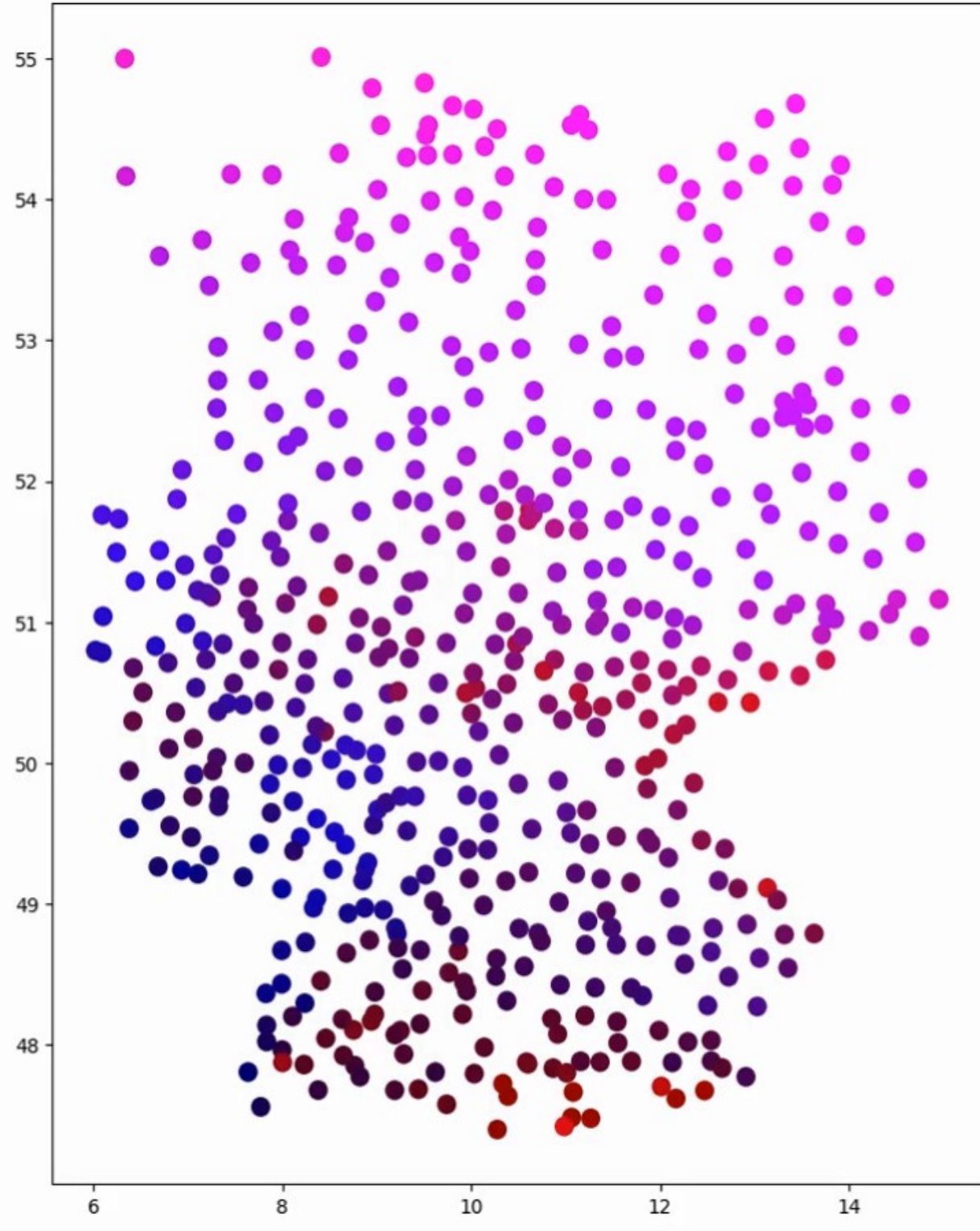
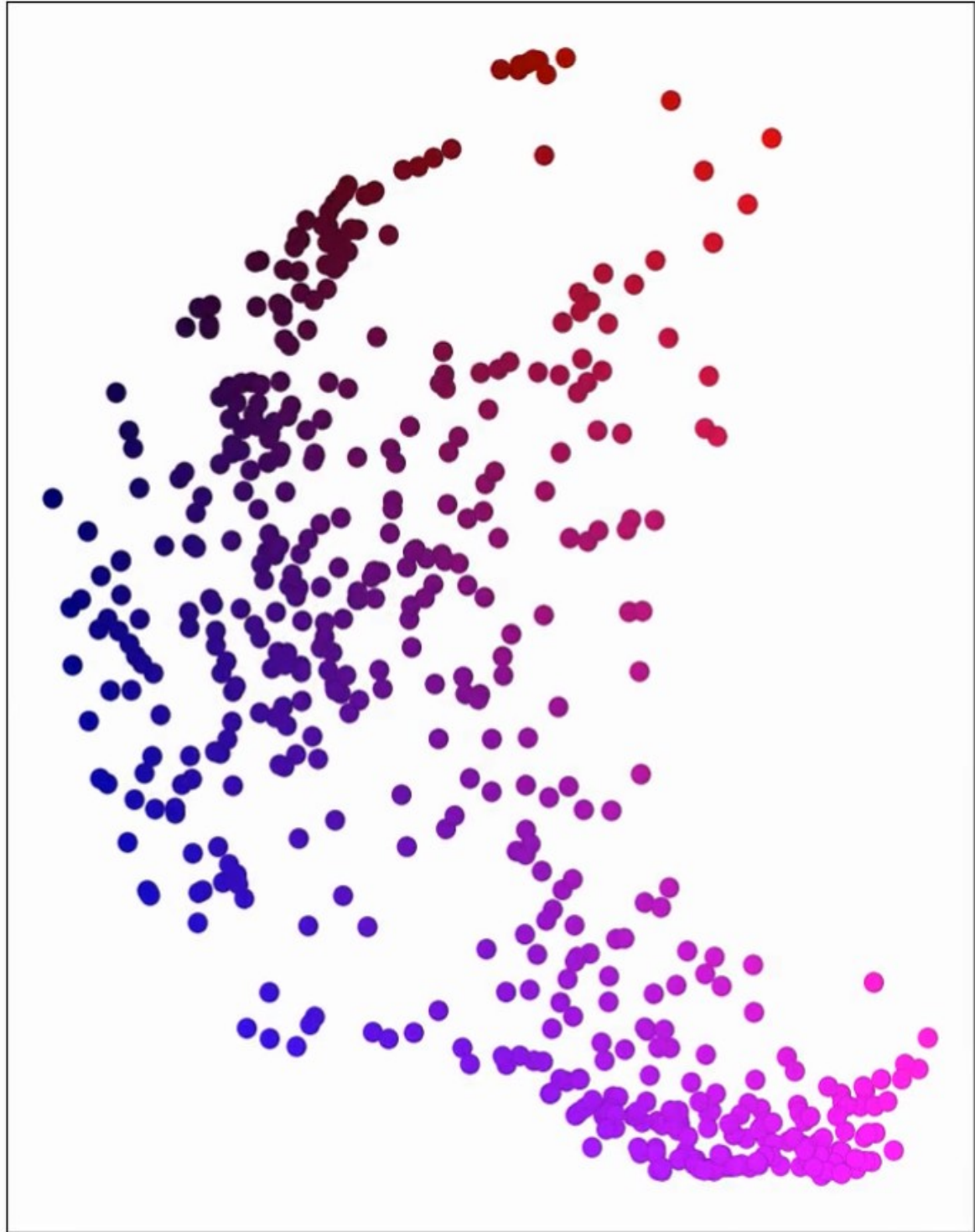
CRPS=0.78

Rasp and Lerch 2018

Projecting Station Parameters

latitude, longitude, altitude, orography



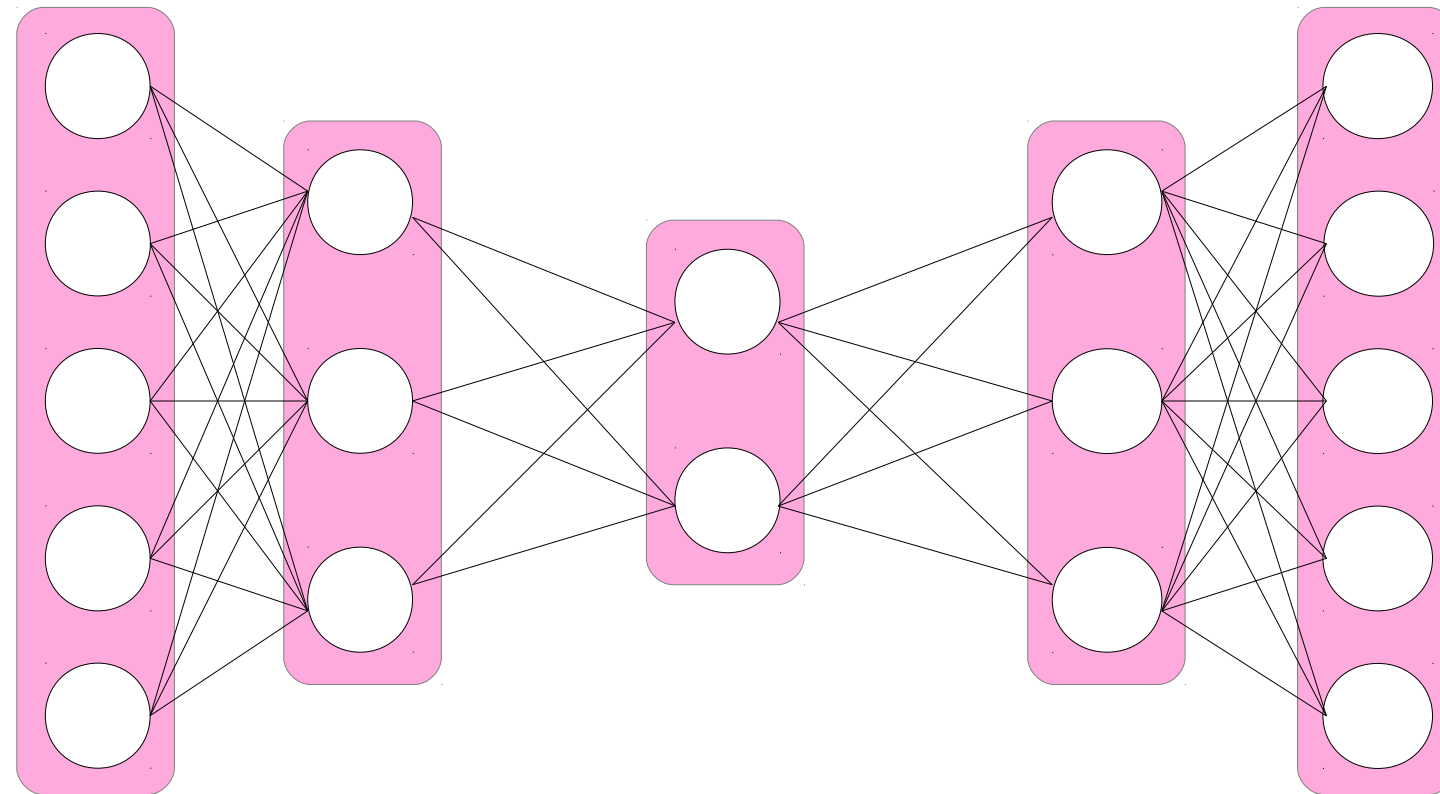


More Complex Network

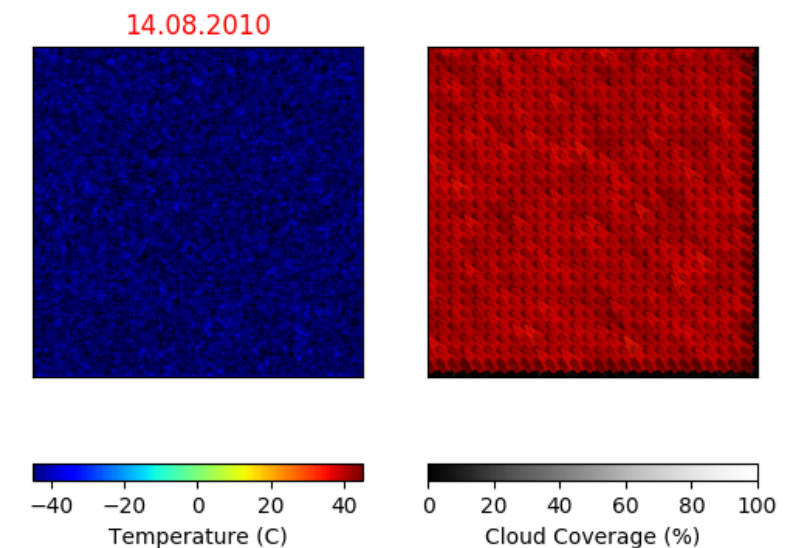
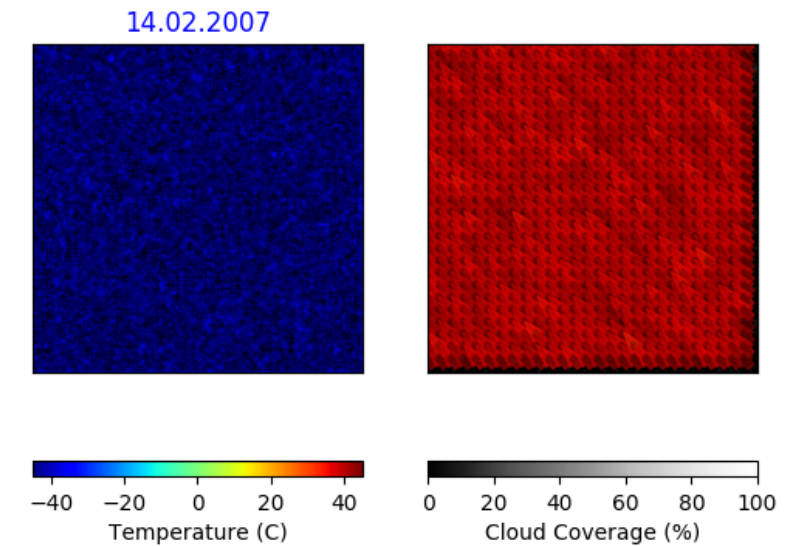
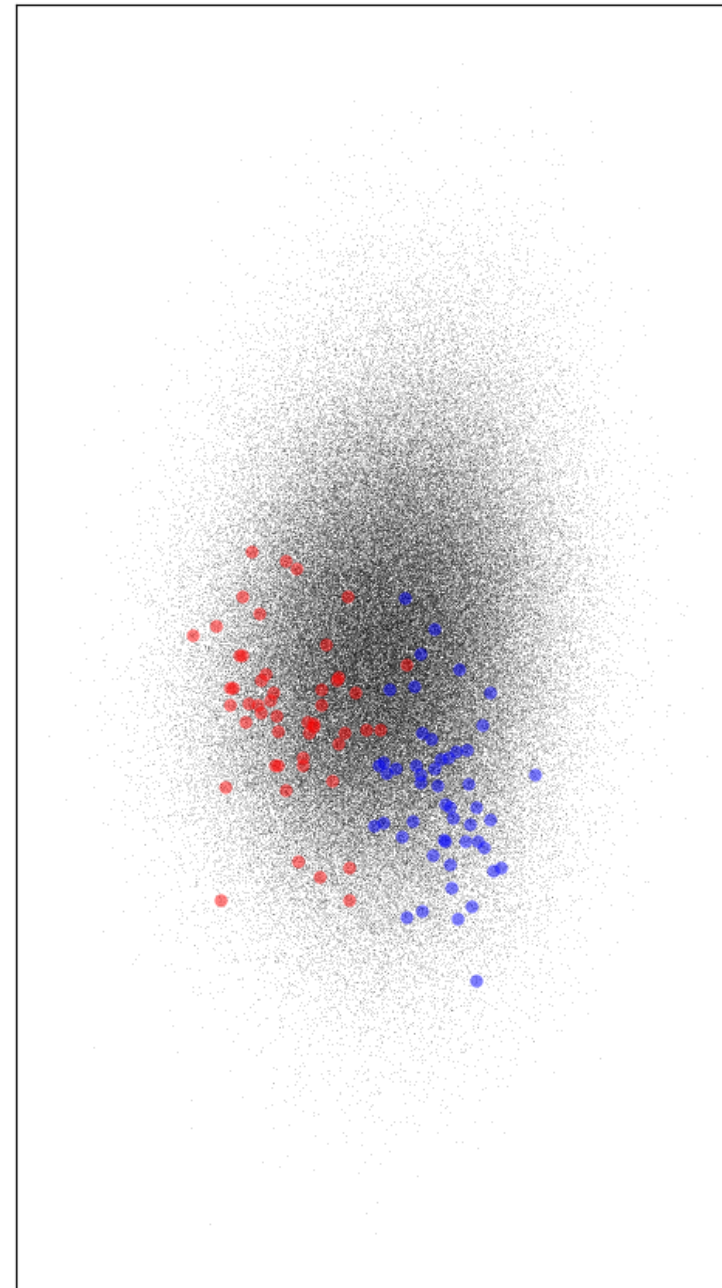
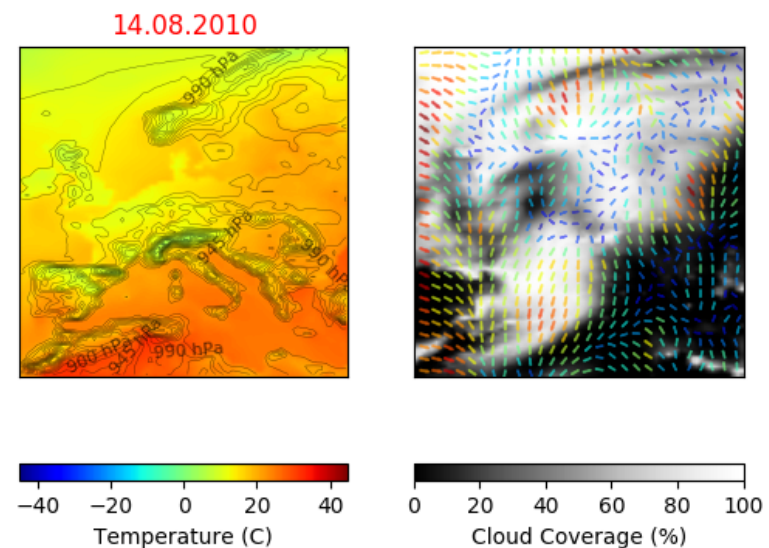
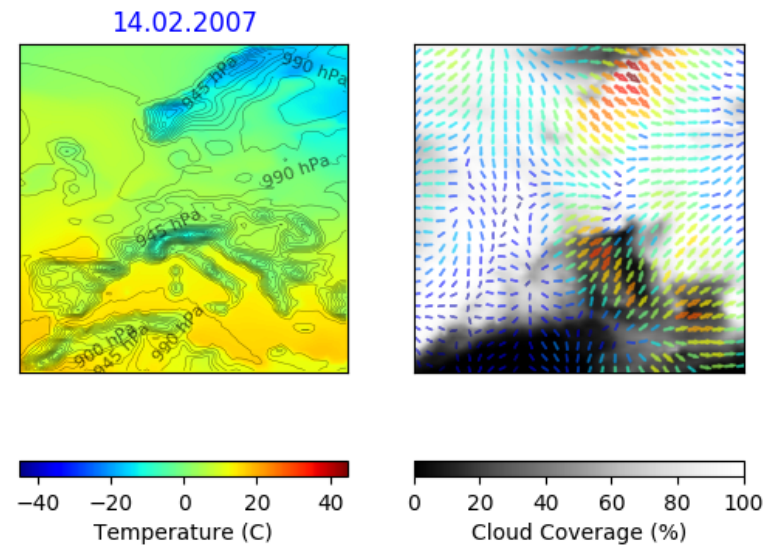
DCMDN → whole ensemble $50 \times 81 \times 81 \times 17 \times 535 \times 3667$

- not enough data for training

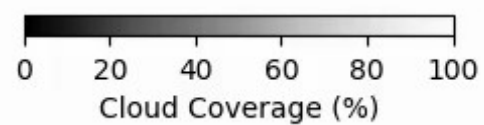
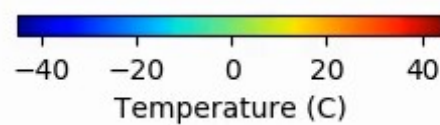
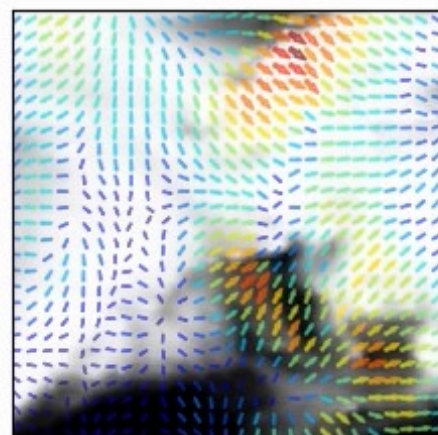
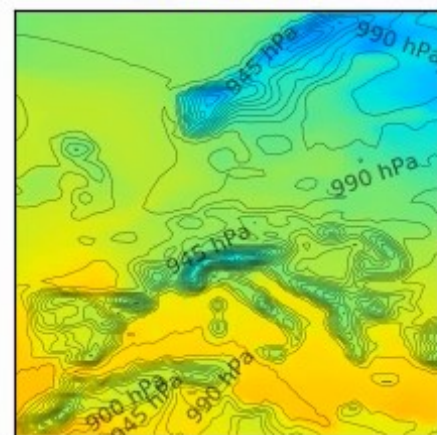
Use different strategy with autoencoders



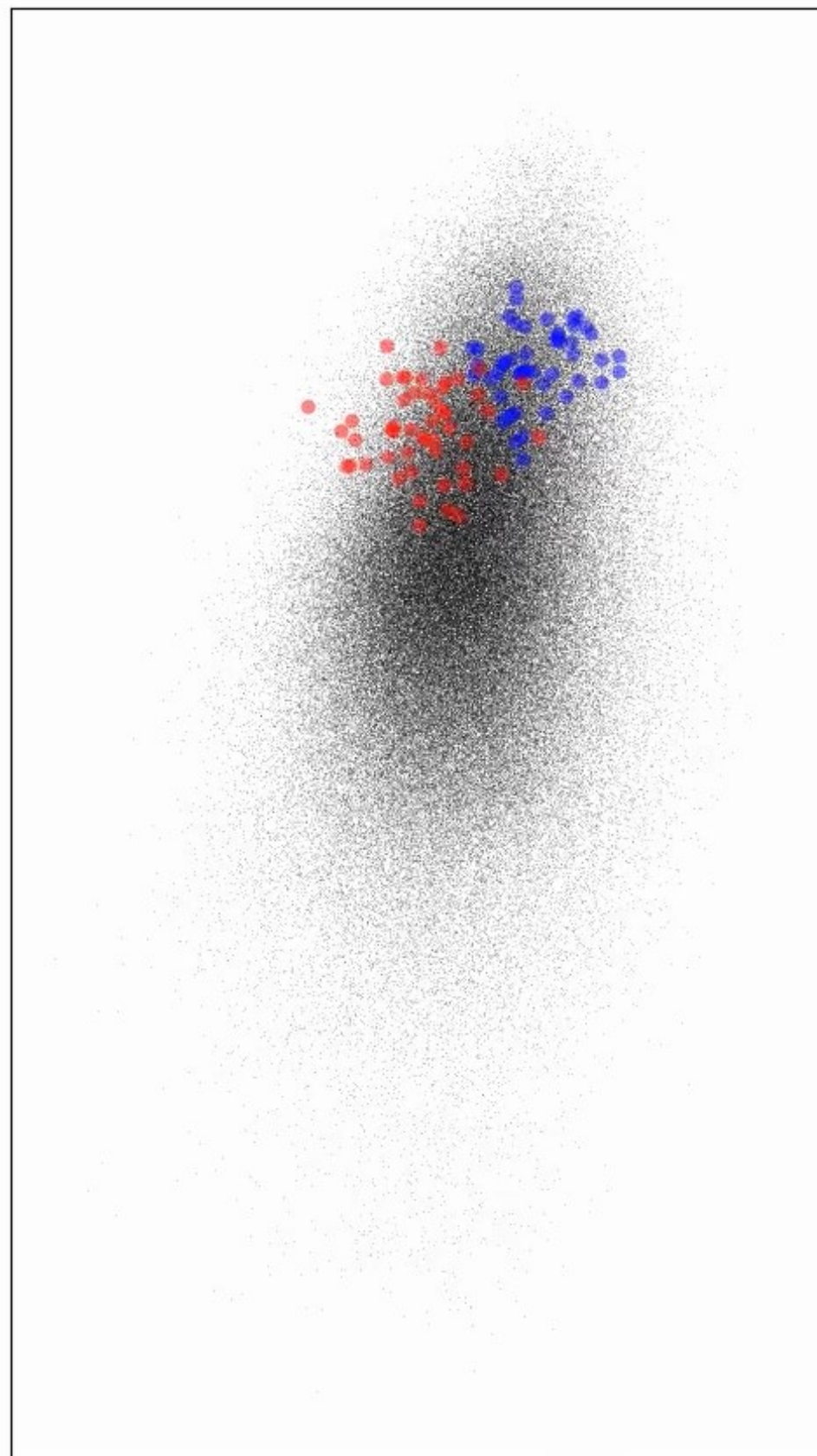
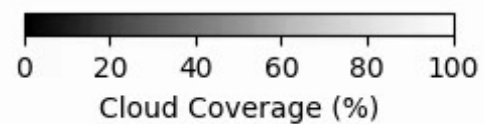
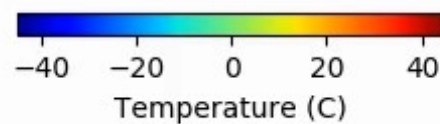
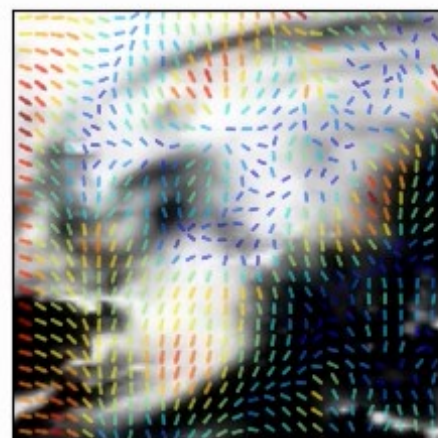
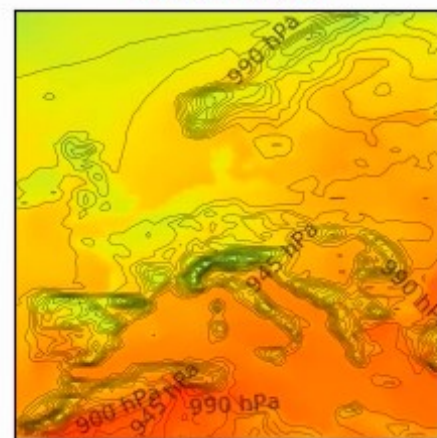
Projecting Forecast Ensembles



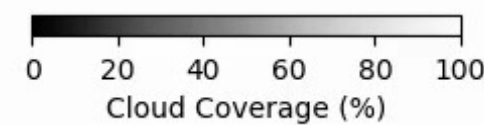
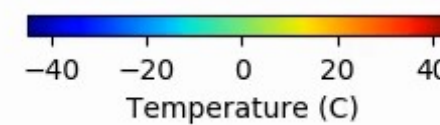
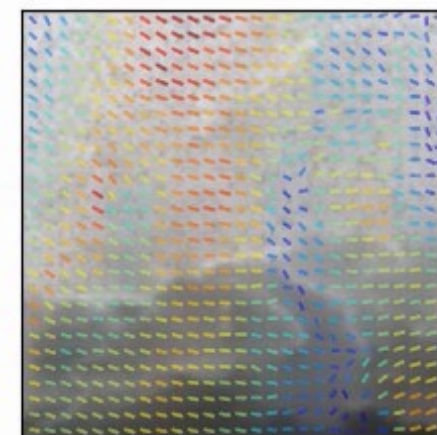
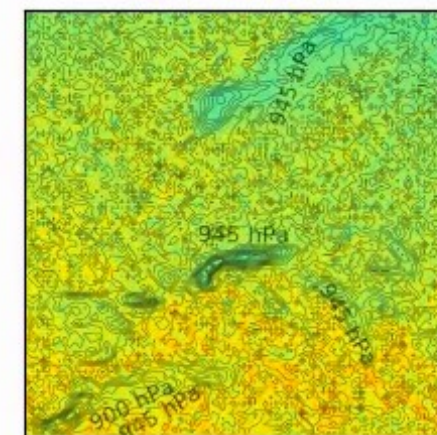
14.02.2007



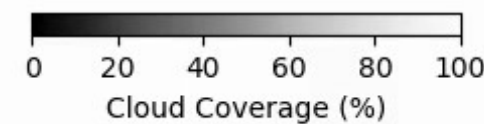
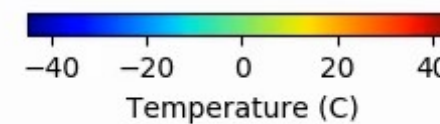
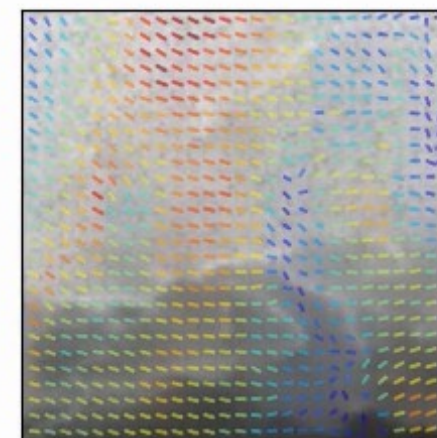
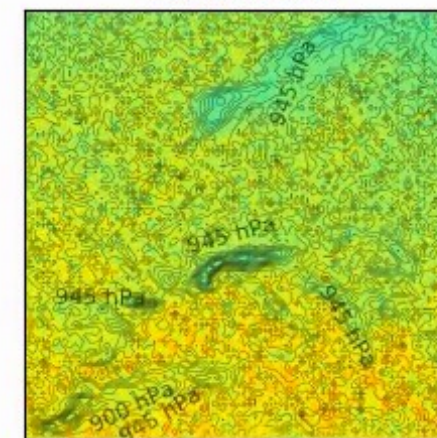
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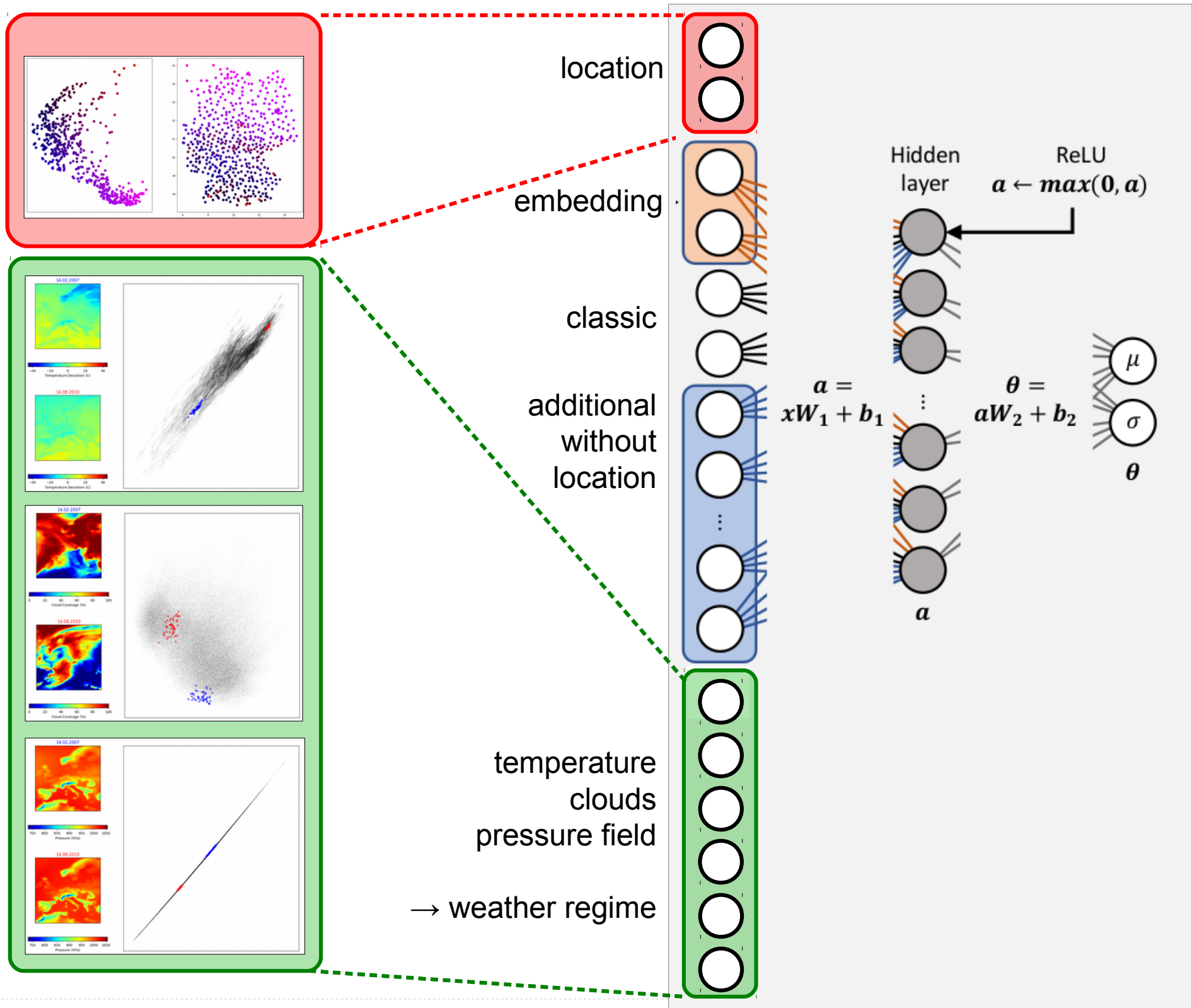


14.02.2007



14.08.2010





Conclusion

Compressing complex data might add interpretability

Use of proper scores for training helps a lot → CRPS