

# Simulation of Extensive Air Showers with Deep Neural Networks

Marcel Köpke, Markus Roth

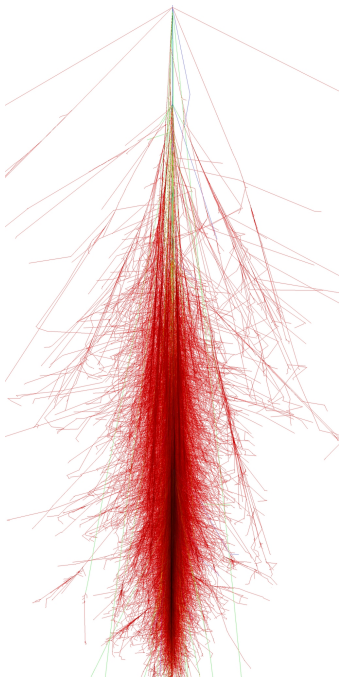
Big Data Science in Astroparticle Research – Workshop

INSTITUTE FOR NUCLEAR PHYSICS (IKP), FACULTY OF PHYSICS  
KARLSRUHE INSTITUTE OF TECHNOLOGY (KIT)

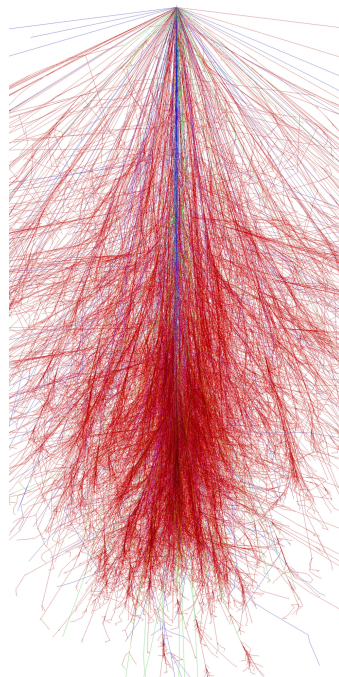


# CORSIKA 7 [1]

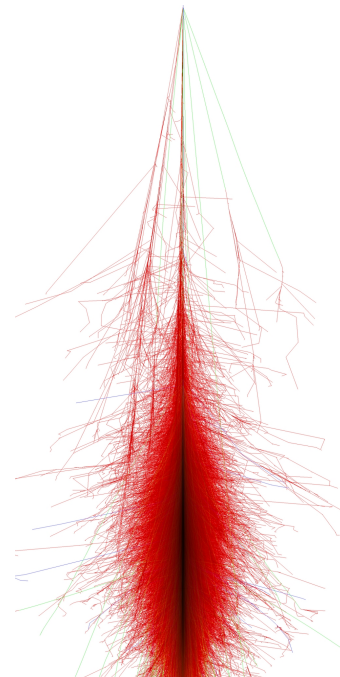
- Extensive air shower Monte Carlo simulation framework
- Different types of interaction models (EPOS-LHC, QGSJET, SIBYLL, ...)



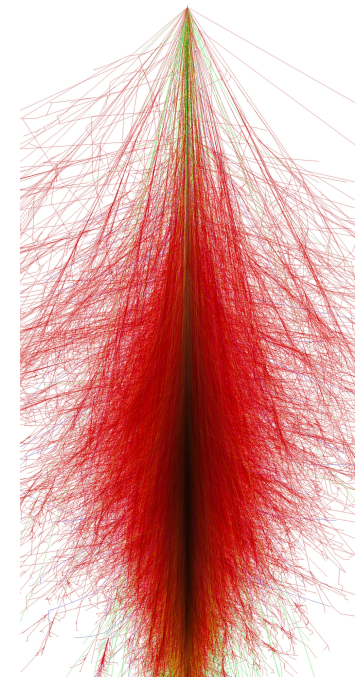
1 TeV Proton



1 TeV Iron

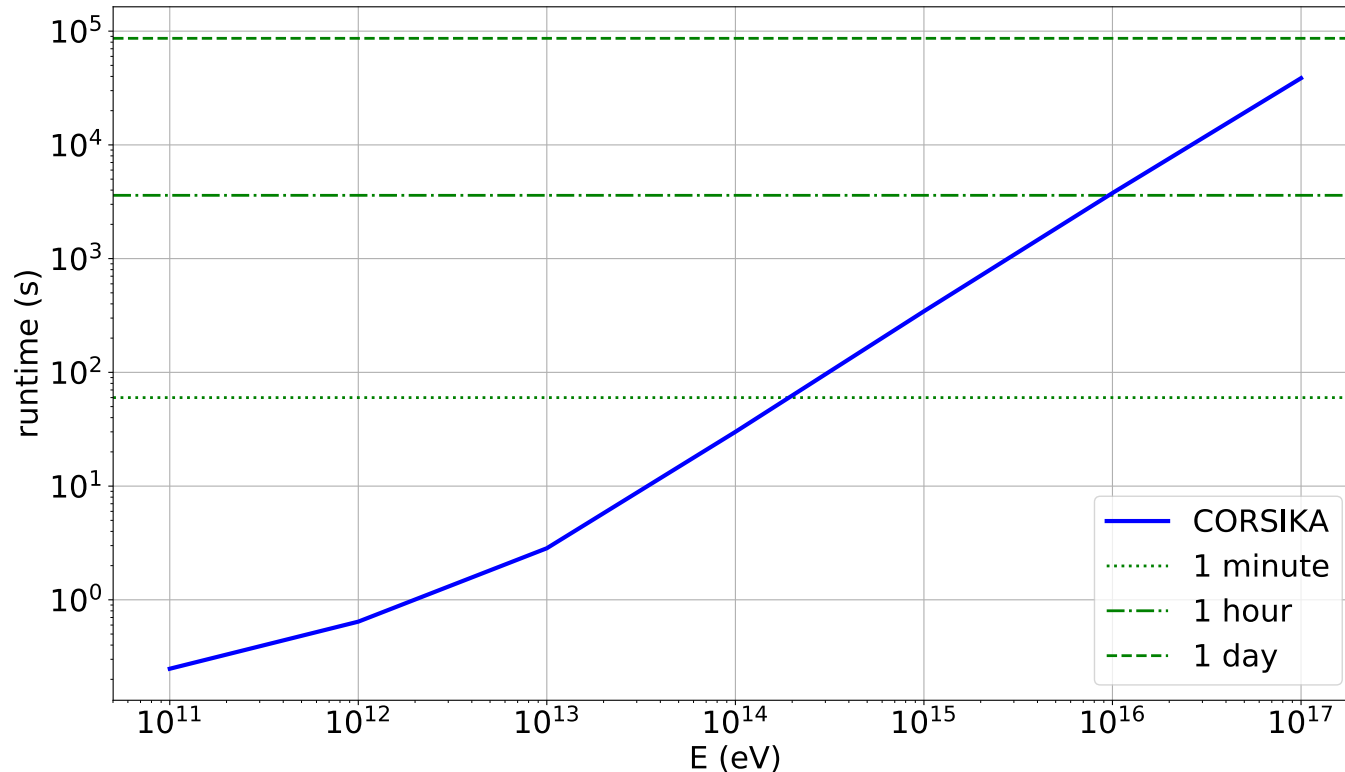


10 TeV Proton



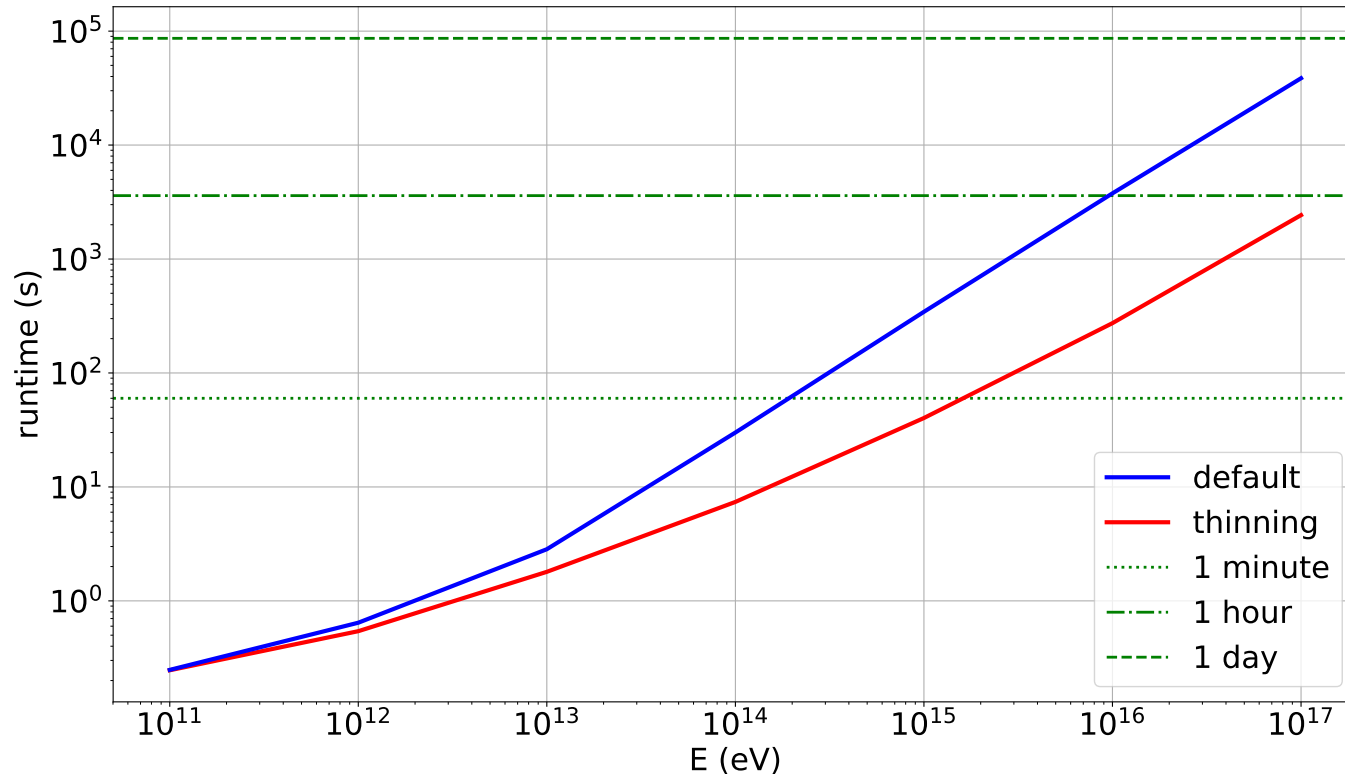
10 TeV Iron

# Motivation

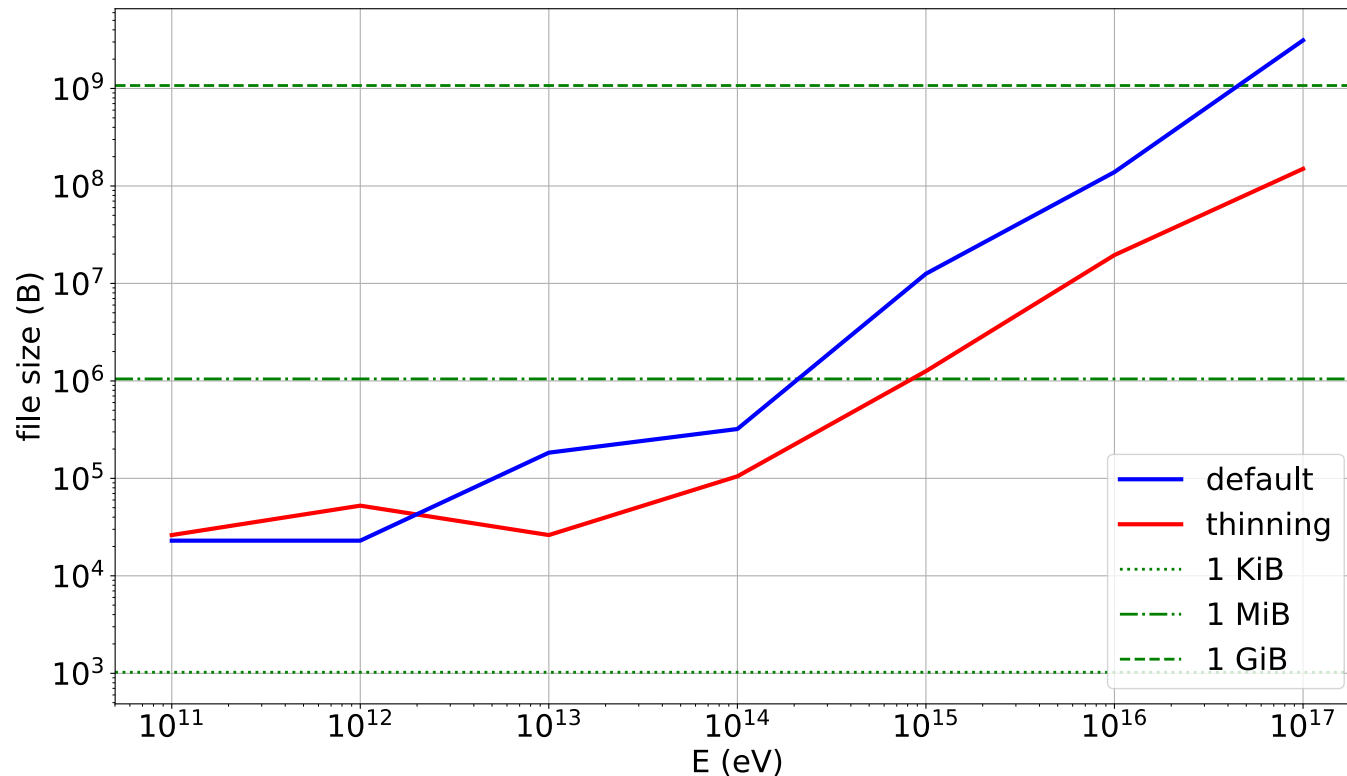


- The time complexity of CORSIKA 7 simulations rises approximately linearly with the primary particle energy

# Thinning

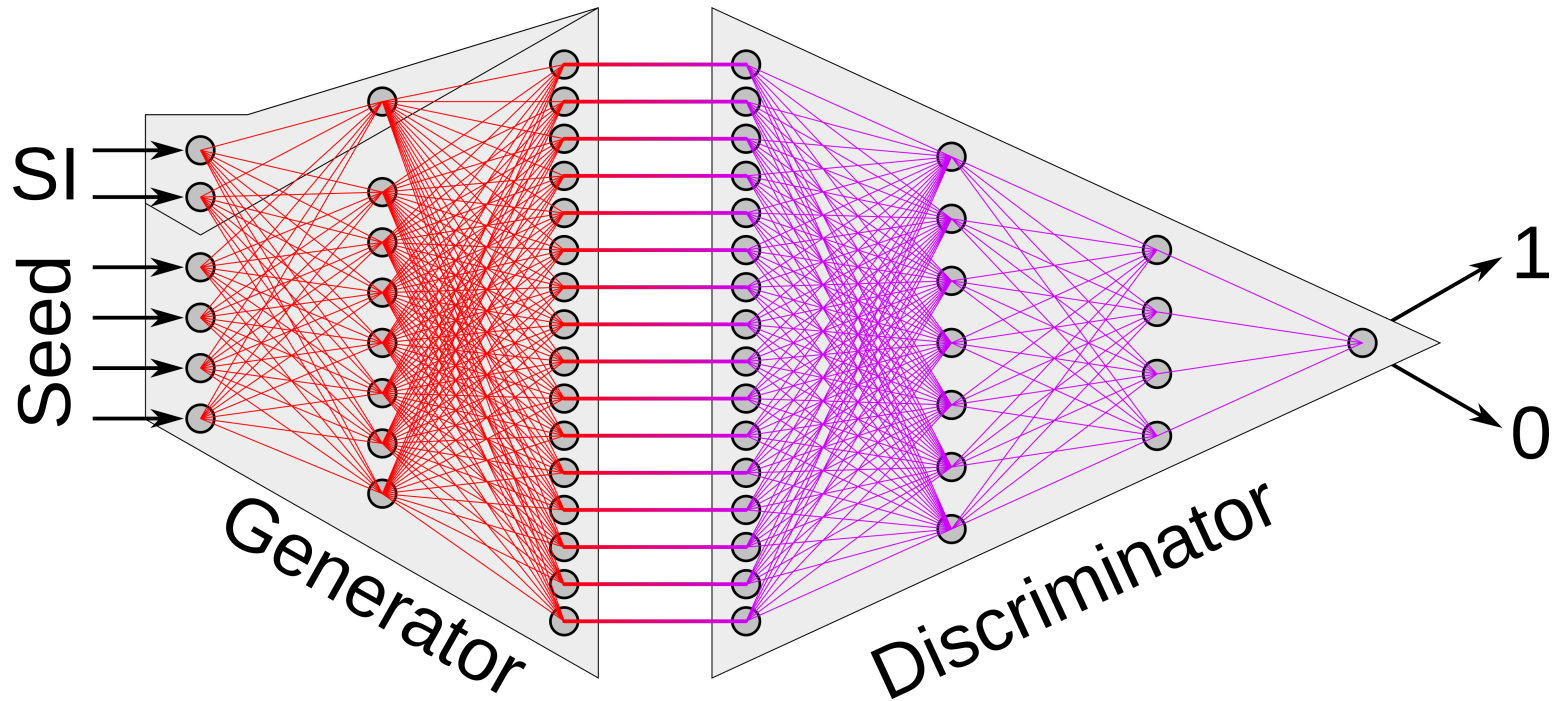


- Reduces (effective) particle content by particle-aggregation
- Preserves shower properties to leading order
- Reduces shower-to-shower fluctuations



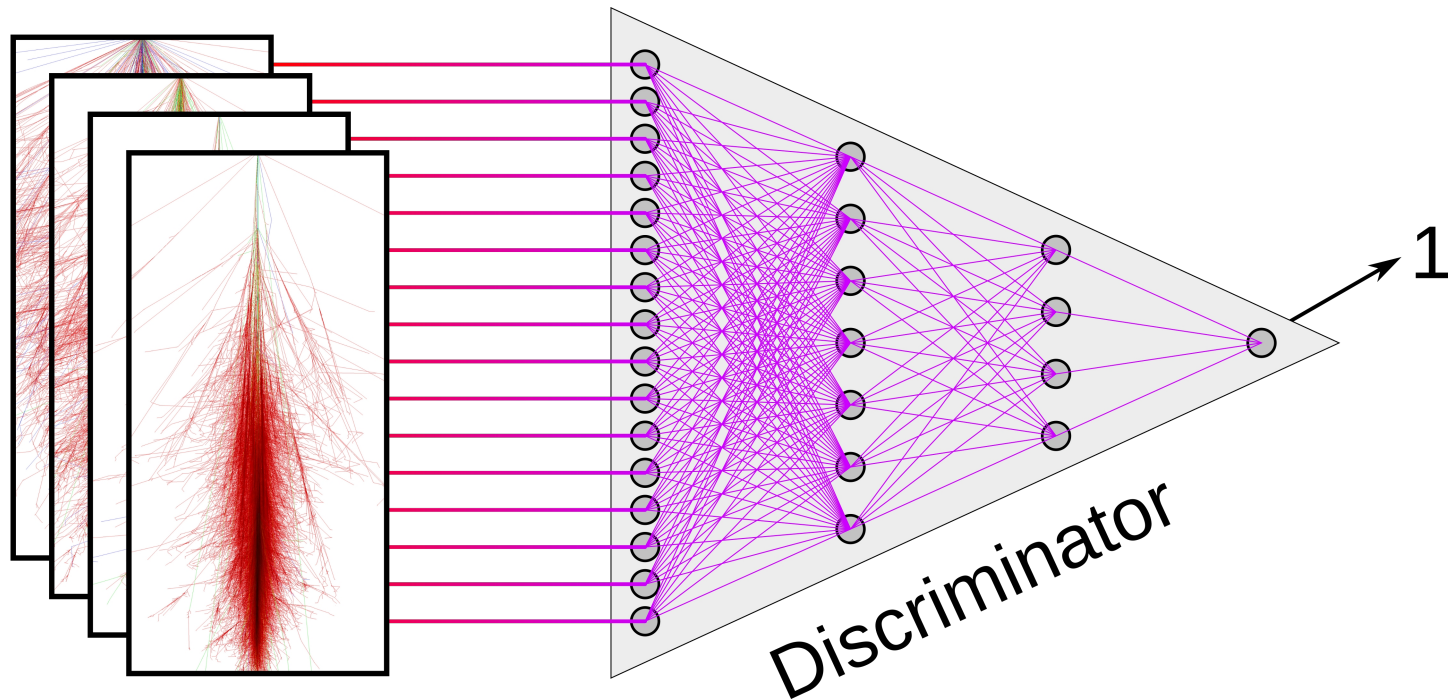
- Shower library required for analyses and model training
- Trained model = effective compression of shower library

# Generative Adversarial Neural Network (GAN)



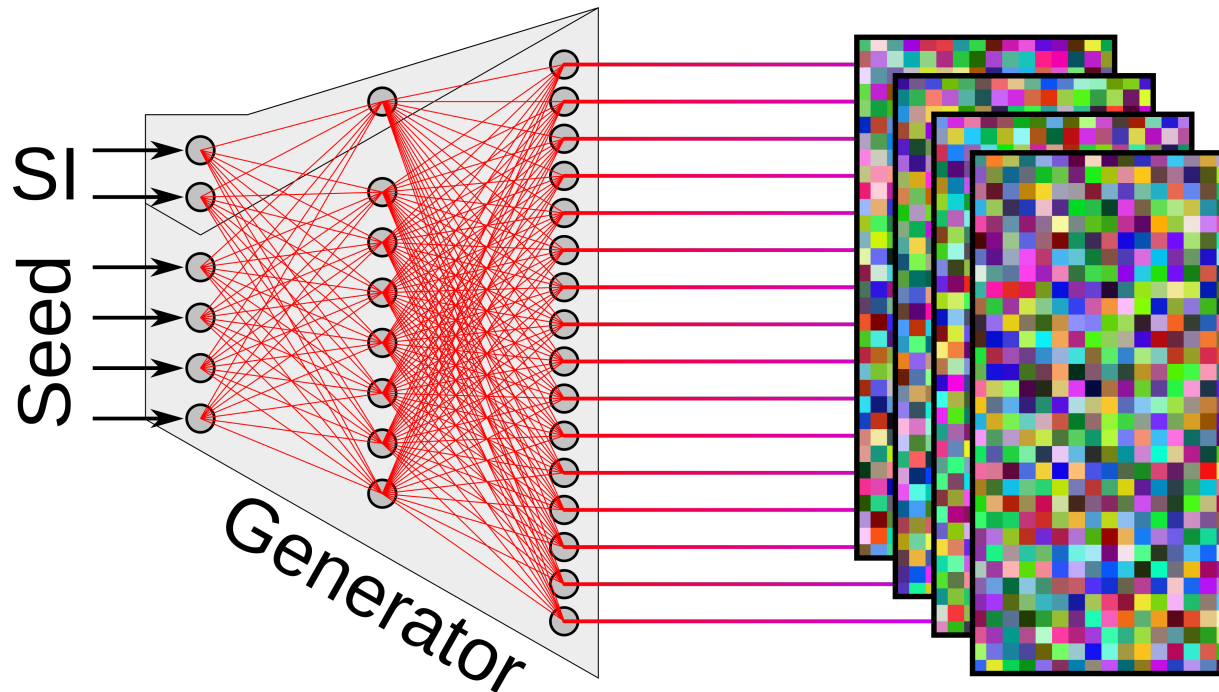
- Train discriminator on real (1) and generated (0) data
- Train generator to outsmart the discriminator

# Training: Discriminator (Part 1)



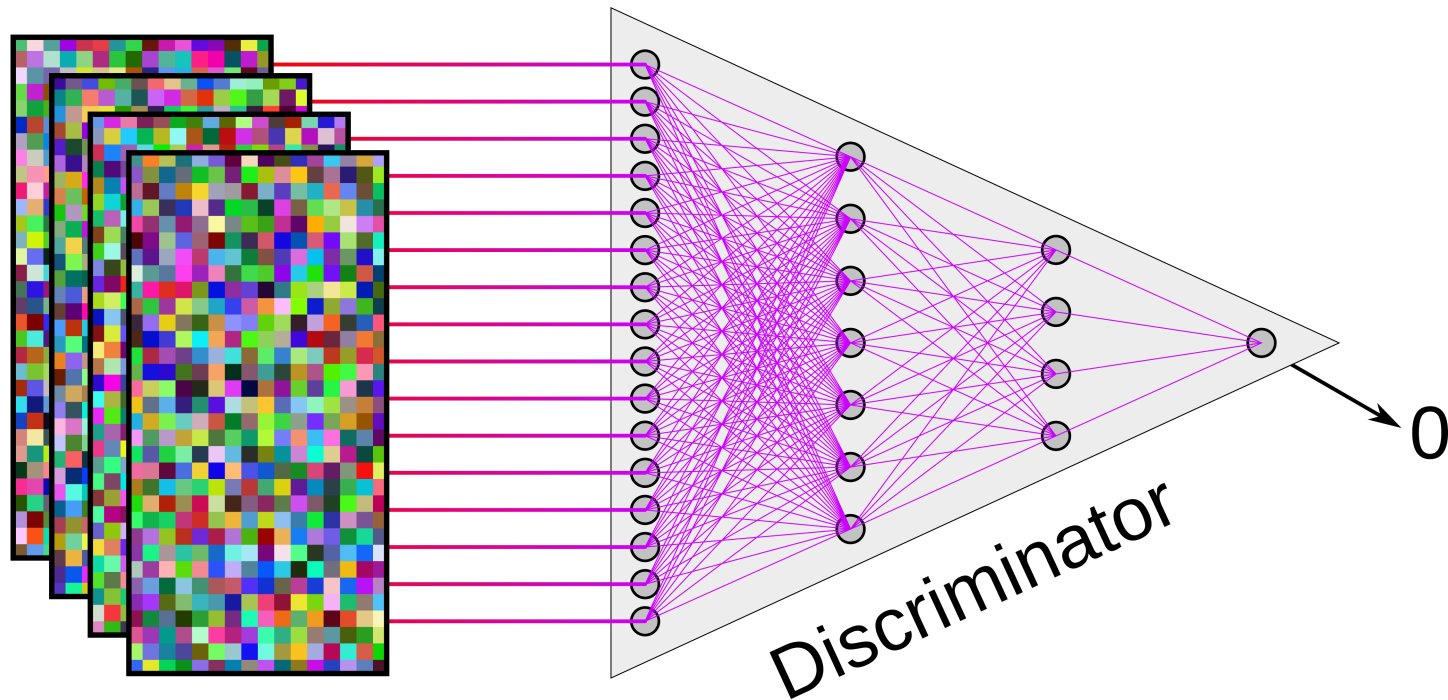
- Train discriminator on real (1) and generated (0) data
- Train generator to outsmart the discriminator

# Training: Sampling



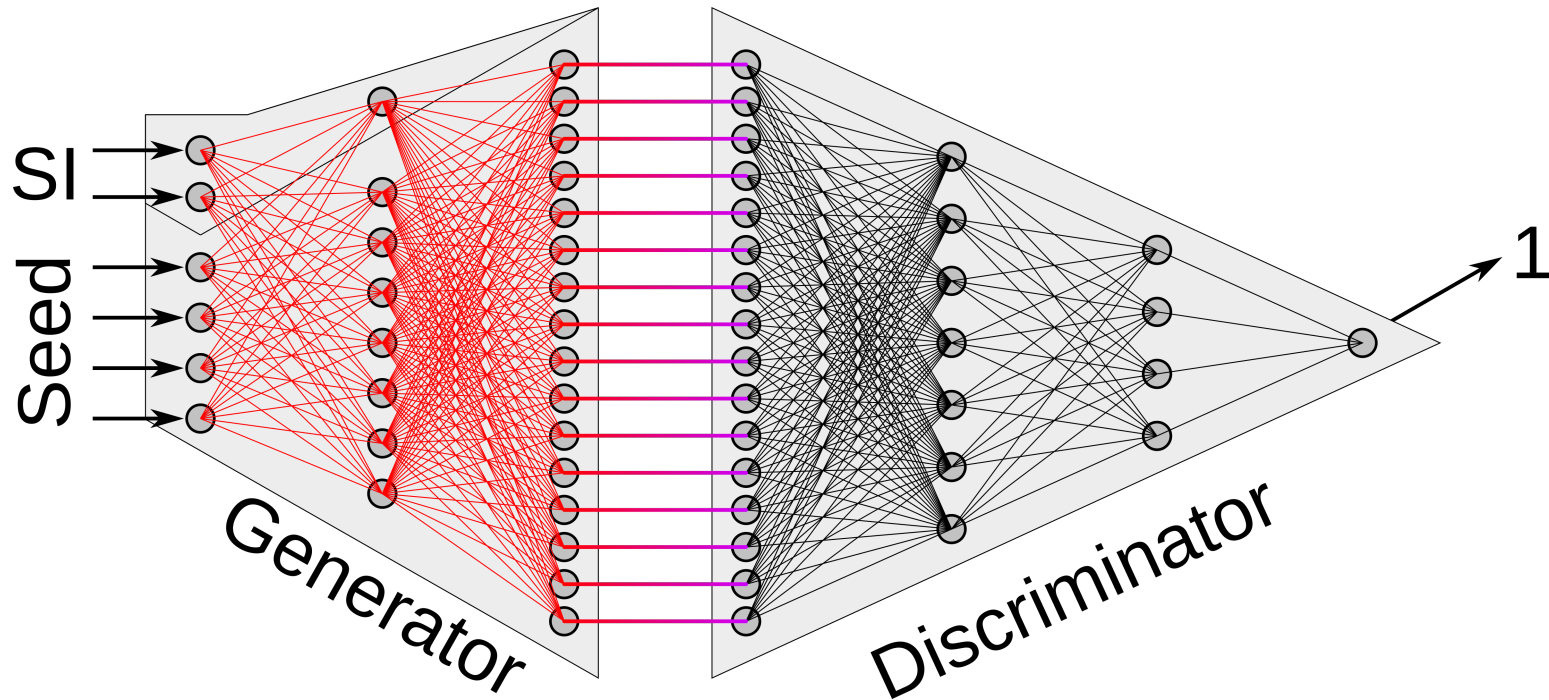
- Train discriminator on real (1) and generated (0) data
- Train generator to outsmart the discriminator

# Training: Discriminator (Part 2)



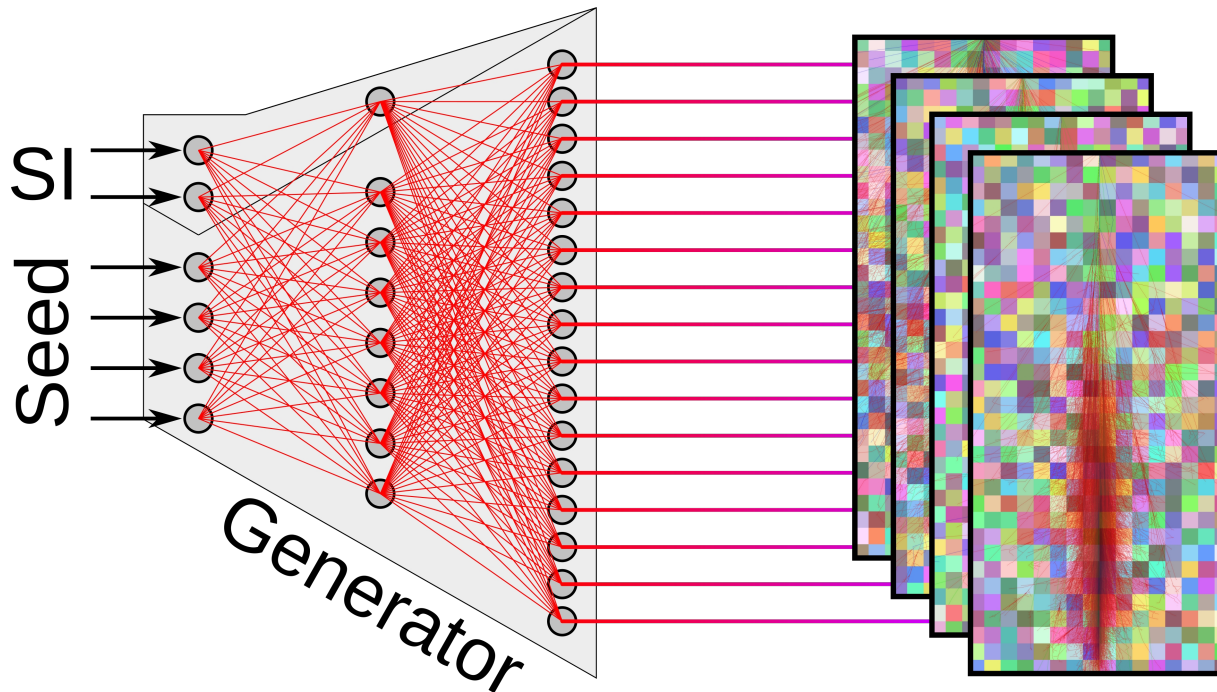
- Train discriminator on real (1) and generated (0) data
- Train generator to outsmart the discriminator

# Training: Generator



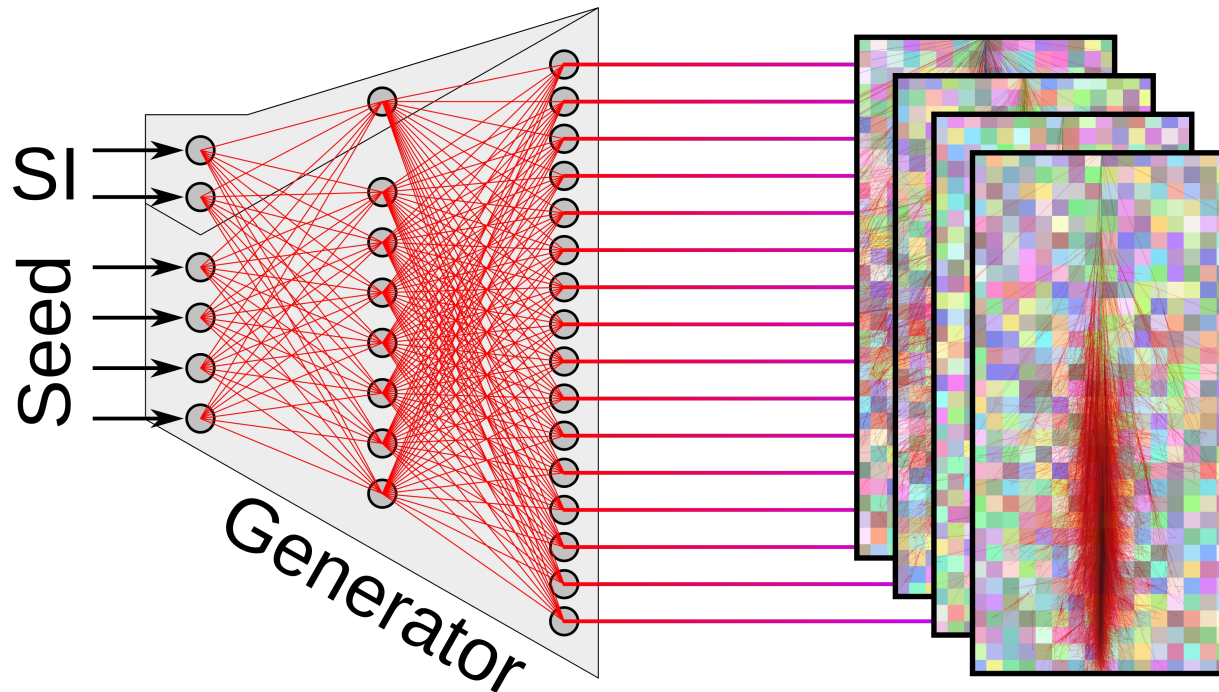
- Train discriminator on real (1) and generated (0) data
- Train generator to outsmart the discriminator

# Training: Result



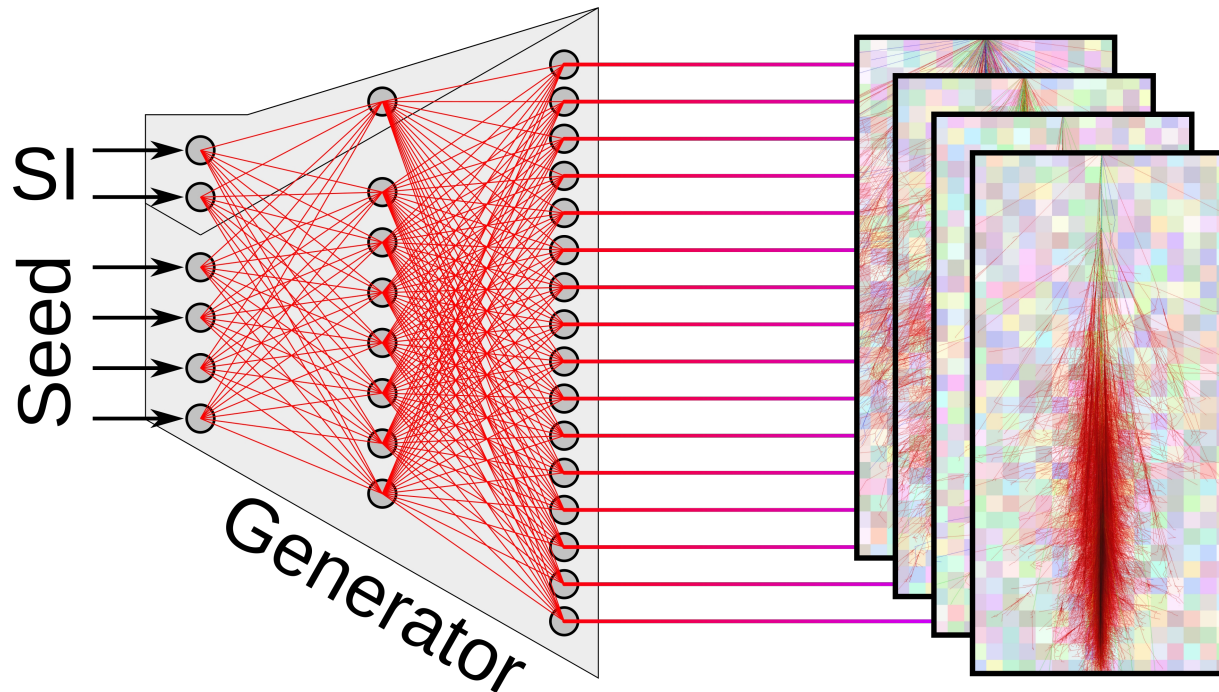
- Train discriminator on real (1) and generated (0) data
- Train generator to outsmart the discriminator

# Training: Result



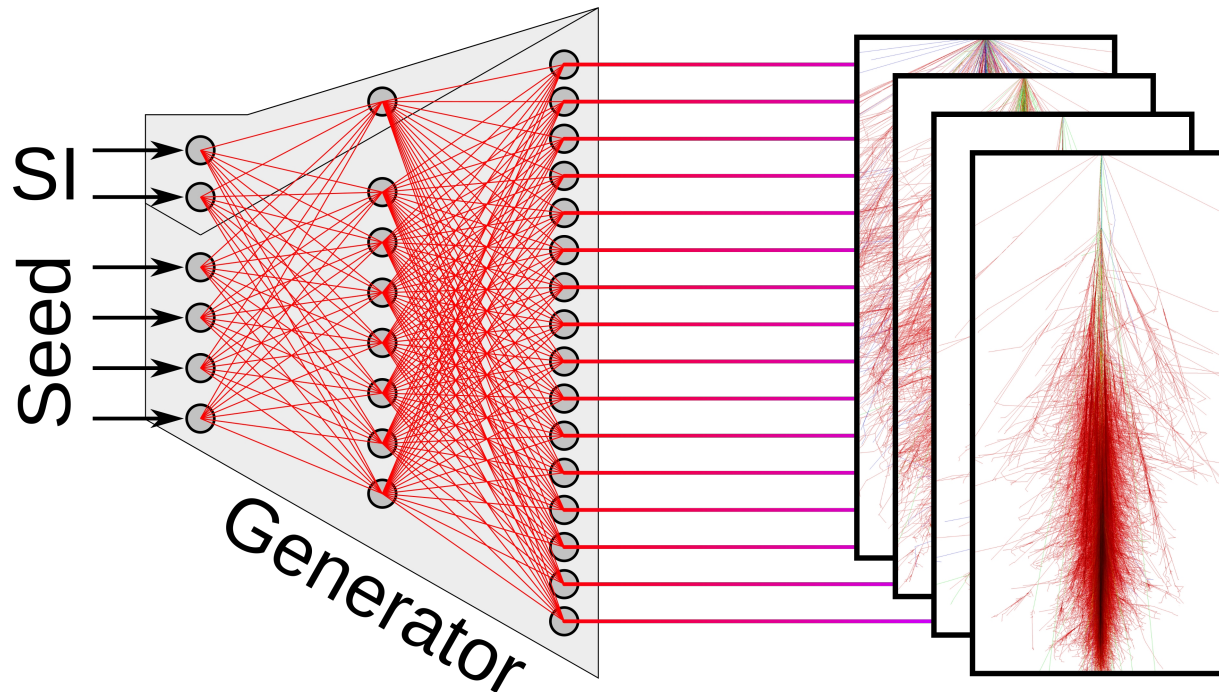
- Train discriminator on real (1) and generated (0) data
- Train generator to outsmart the discriminator

# Training: Result



- Train discriminator on real (1) and generated (0) data
- Train generator to outsmart the discriminator

# Training: Result



- Train discriminator on real (1) and generated (0) data
- Train generator to outsmart the discriminator

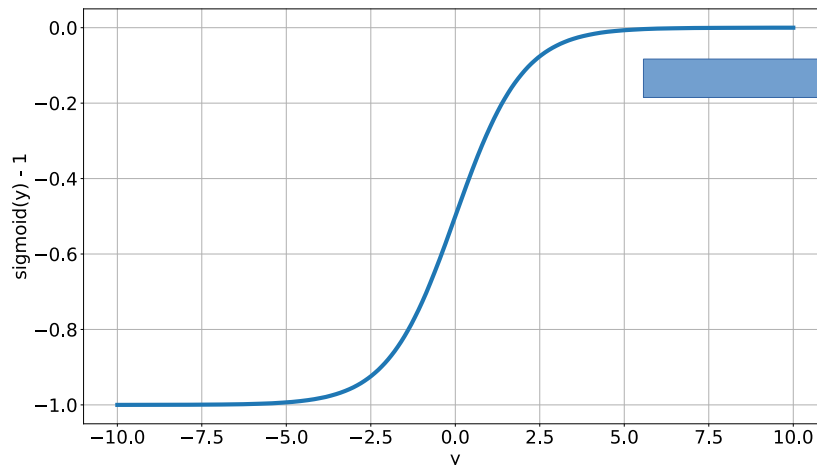
# Cross Entropy

- $$\text{CE} = \sum_i -z_i \cdot \log(p_i) + (z_i - 1) \cdot \log(1 - p_i)$$

with  $z$  (true) label and  $p$  probability (NN output)

- $z = 1: -\log(\text{sigmoid}(y))$

$$\Rightarrow \frac{d}{dy} (-\log(\text{sigmoid}(y))) = \text{sigmoid}(y) - 1$$



vanishing  
gradients

# Cross Entropy

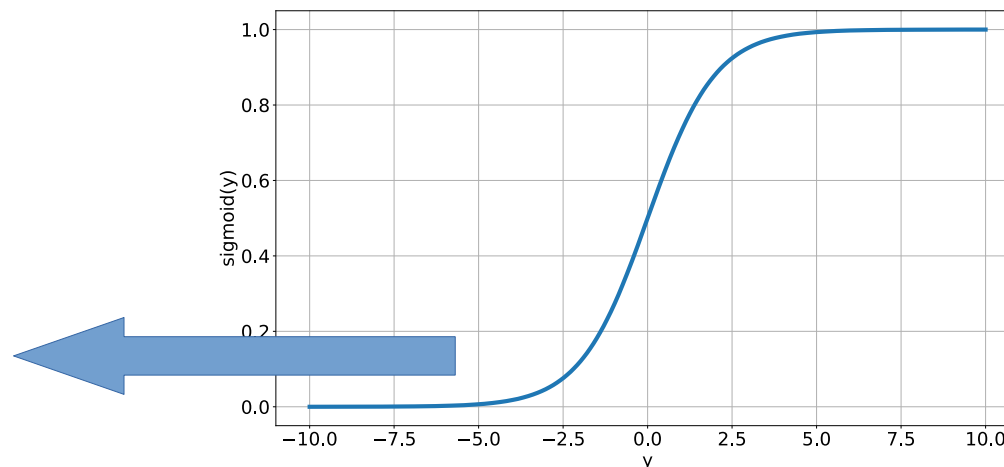
- $$\text{CE} = \sum_i -z_i \cdot \log(p_i) + (z_i - 1) \cdot \log(1 - p_i)$$

with  $z$  (true) label and  $p$  probability (NN output)

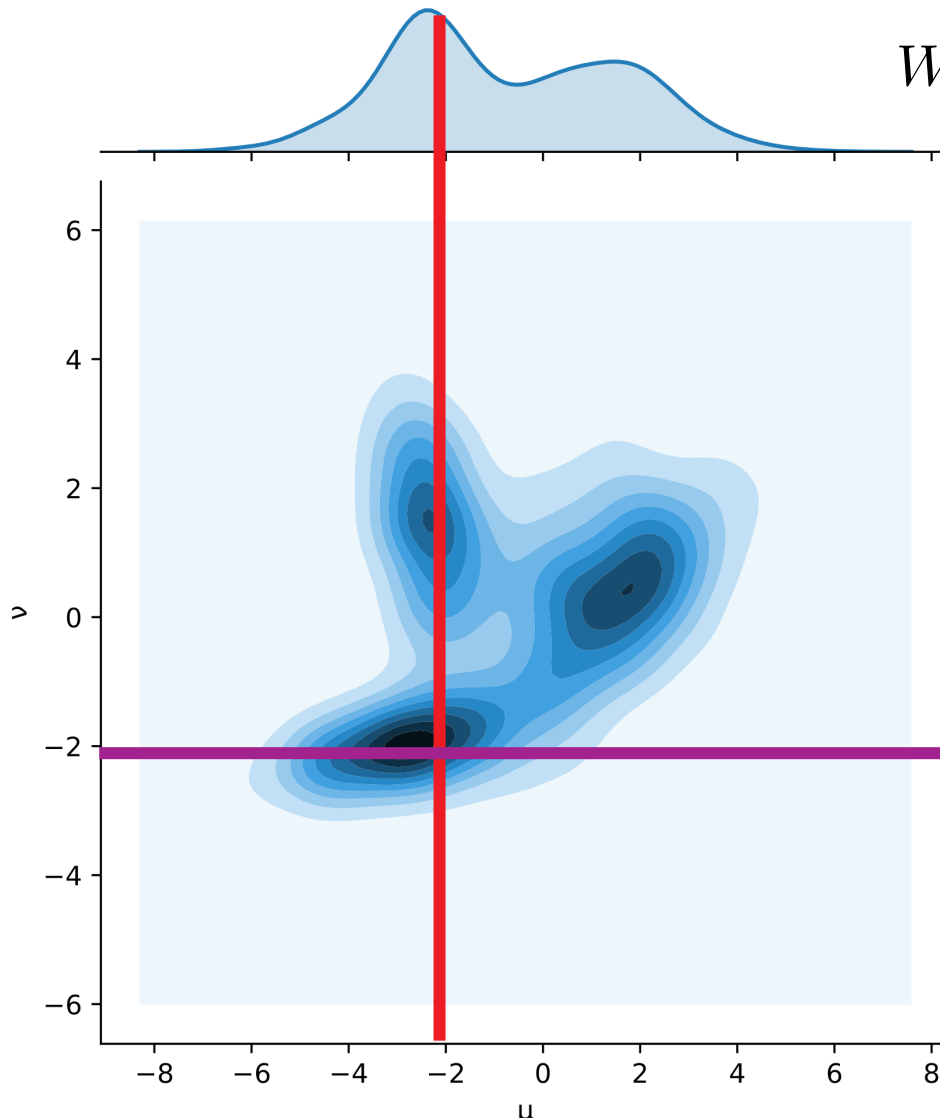
- $z = 0: -\log(1 - \text{sigmoid}(y))$

$$\Rightarrow \frac{d}{dy} (-\log(1 - \text{sigmoid}(y))) = \text{sigmoid}(y)$$

vanishing  
gradients



# Wasserstein Distance [2]



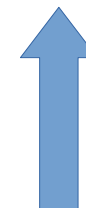
$$W(\mu, \nu) = \inf_{\gamma} \int d(x, y) \cdot \gamma(x, y) \, dx dy$$

total (minimal) cost to move all mass



$$\int d(x, y) \cdot \gamma(x, y) dy = c(x)$$

cost to move mass above/below x



$$\int \gamma(x, y) dy = \mu(x)$$

**red:** total mass piled up at x

# Kantorovich-Rubinstein Duality

- $W(\mu, \nu) = \sup_{f \in Lip_{\leq 1}} \mathbb{E}_{x \sim \mu}[f(x)] - \mathbb{E}_{y \sim \nu}[f(y)]$
- $f$  = Neural Network
- Lipschitz continuous:  $|f(x_1) - f(x_2)| \leq L \cdot \|x_1 - x_2\|$
- Gradient is bounded  $\rightarrow$  Gradient penalty  $|||\nabla f||| - 1| \rightarrow 0$

# Gradient Penalty

- $$W(\mu, \nu) = \sup_{f \in Lip \leq 1} \mathbb{E}_{x \sim \mu}[f(x)] - \mathbb{E}_{y \sim \nu}[f(y)]$$

- $$\mathbb{E}_{x \sim \mu}[f(x)] \rightarrow \infty \quad \mathbb{E}_{y \sim \nu}[f(y)] \rightarrow -\infty$$

- $$f \rightarrow a \cdot f \quad \text{and} \quad a \rightarrow \infty$$

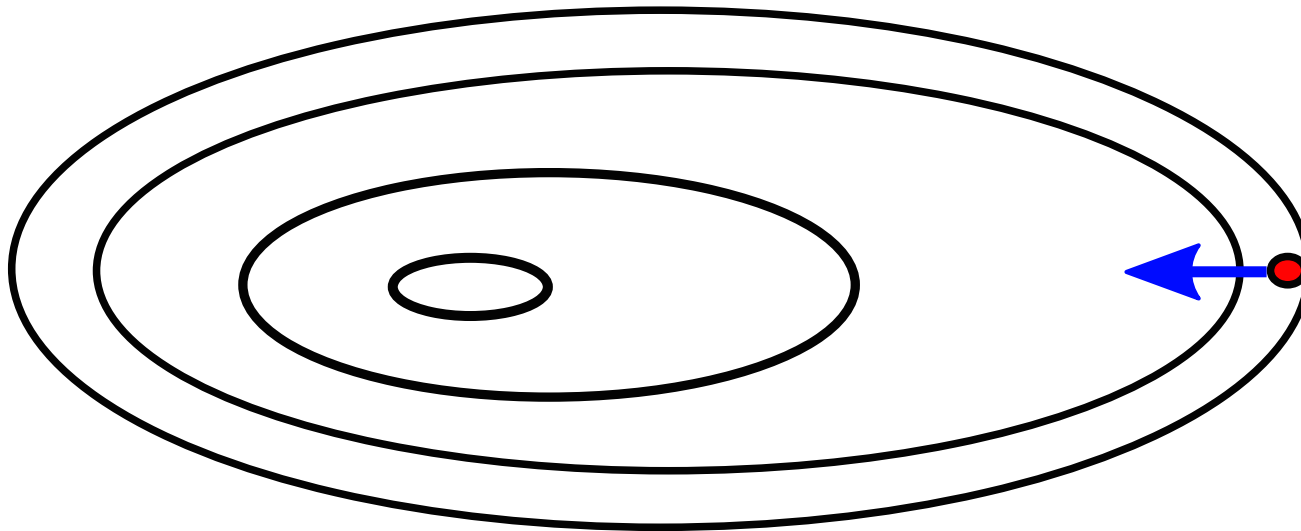
- But 
$$|a \cdot f(x) - a \cdot f(y)| \leq L \|x - y\|$$

$$\Rightarrow a \cdot \|\nabla f\| \leq L$$

# Learning Rate and Momentum

## ■ Ordinary classification:

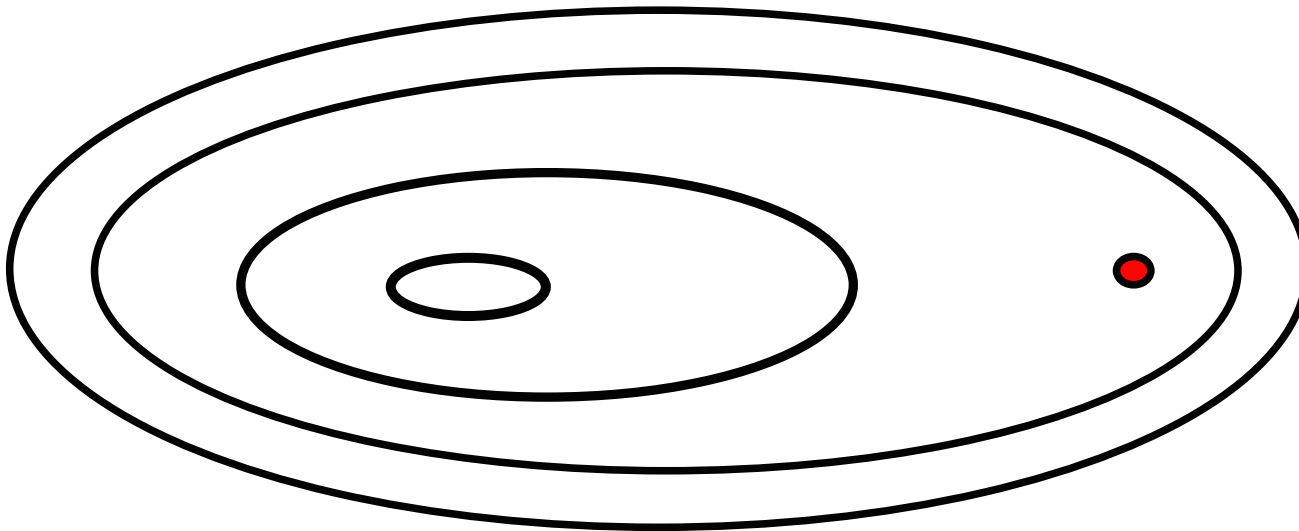
- Gradient



# Learning Rate and Momentum

## ■ Ordinary classification:

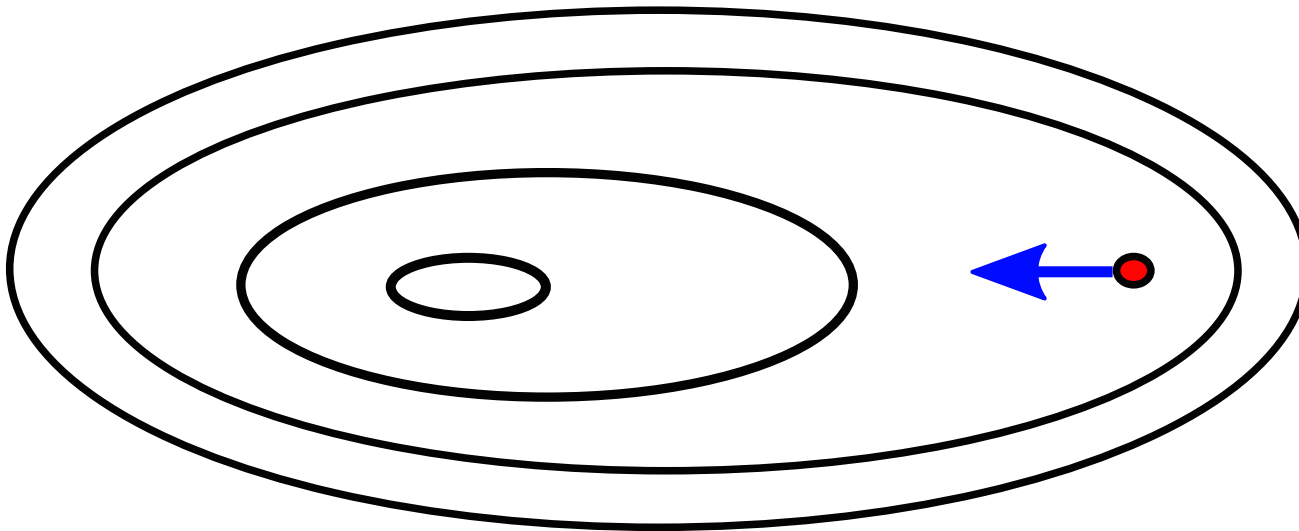
- Step



# Learning Rate and Momentum

## ■ Ordinary classification:

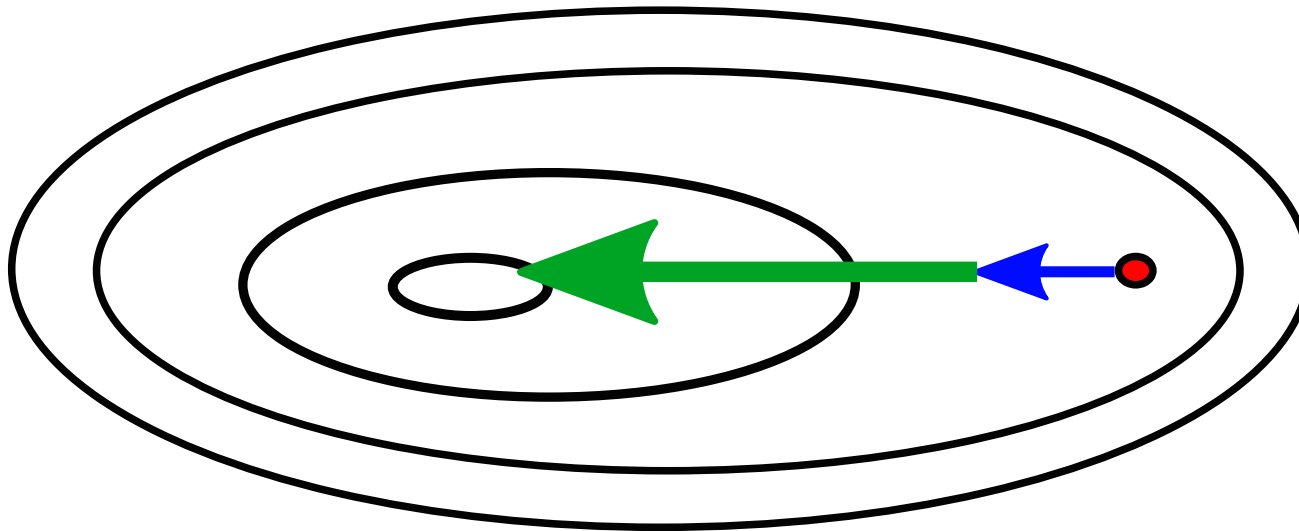
- Gradient



# Learning Rate and Momentum

## ■ Ordinary classification:

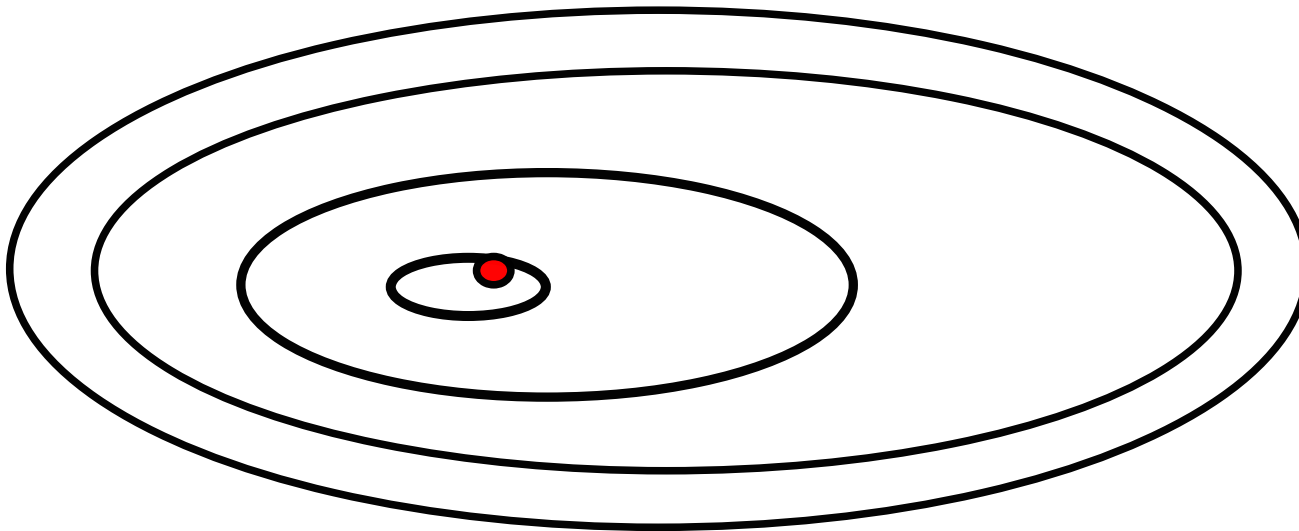
- Momentum



# Learning Rate and Momentum

## ■ Ordinary classification:

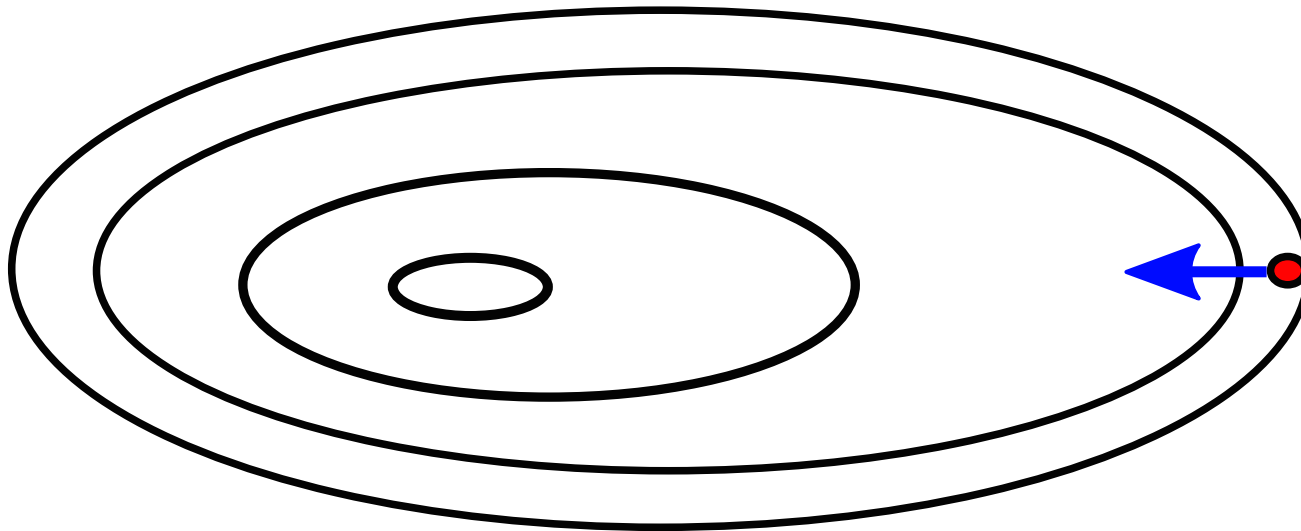
- Step



# GAN: Learning Rate and Momentum

## ■ Discriminator classification:

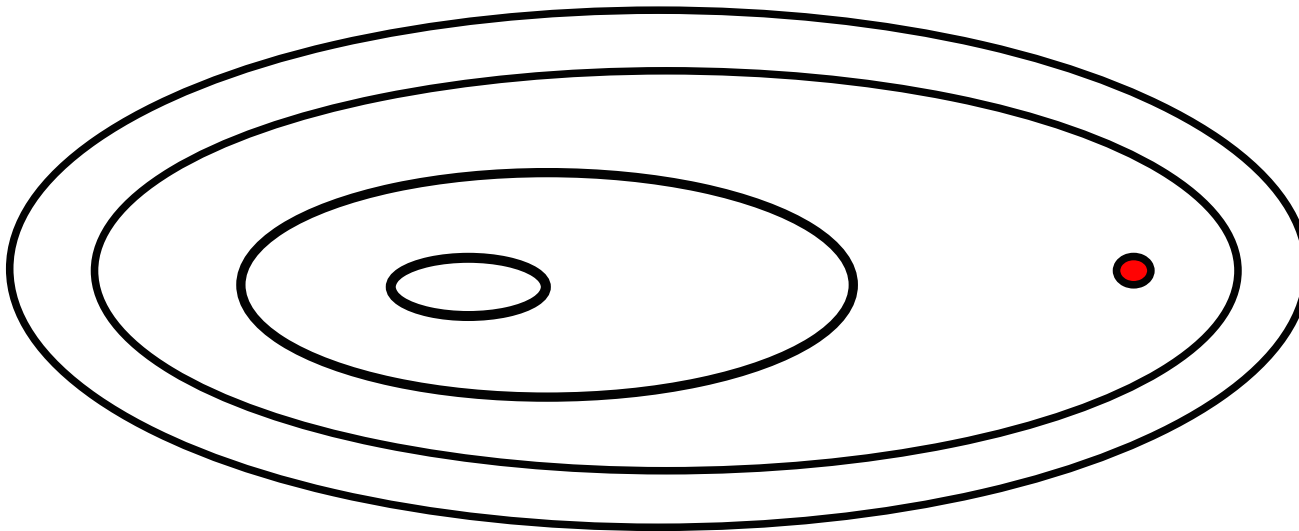
- Gradient



# GAN: Learning Rate and Momentum

## ■ Discriminator classification:

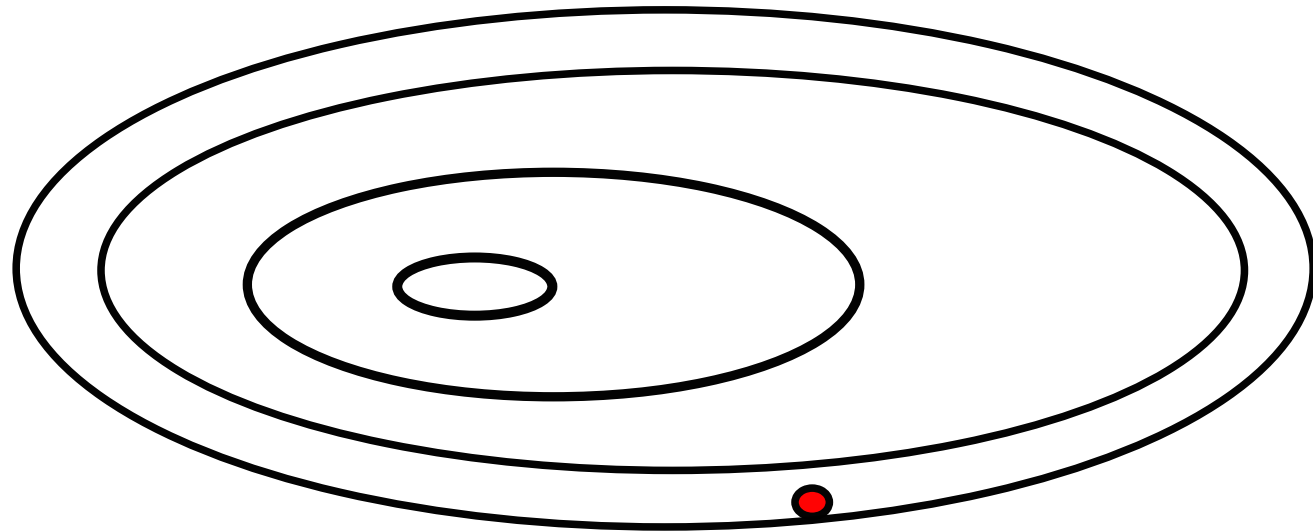
- Step



# GAN: Learning Rate and Momentum

## ■ Discriminator classification:

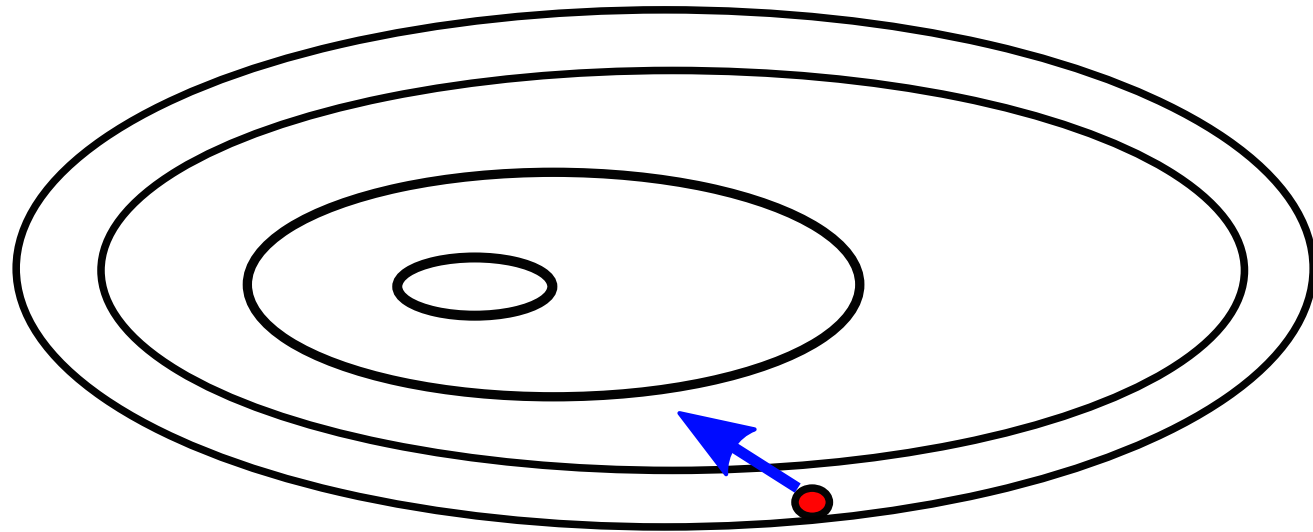
- Generator training



# GAN: Learning Rate and Momentum

## ■ Discriminator classification:

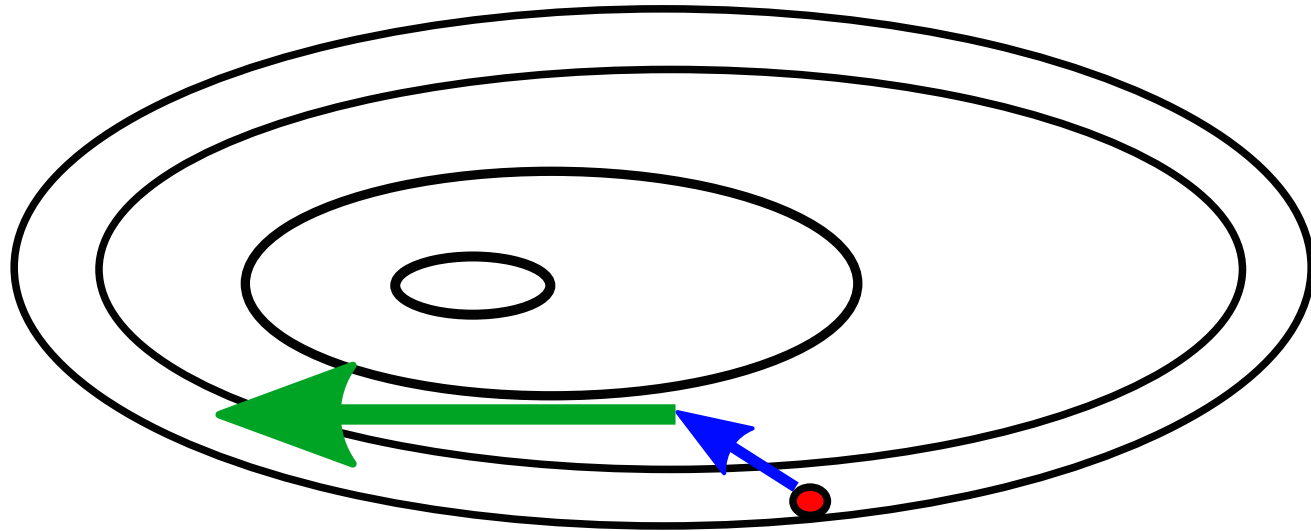
- Gradient



# GAN: Learning Rate and Momentum

## ■ Discriminator classification:

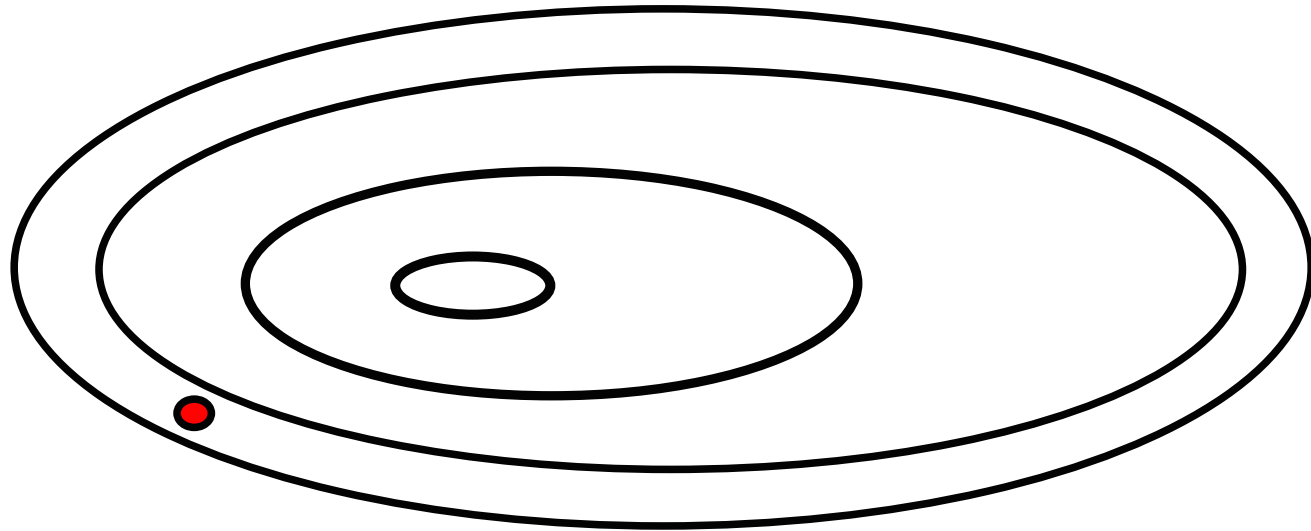
- Momentum



# GAN: Learning Rate and Momentum

## ■ Discriminator classification:

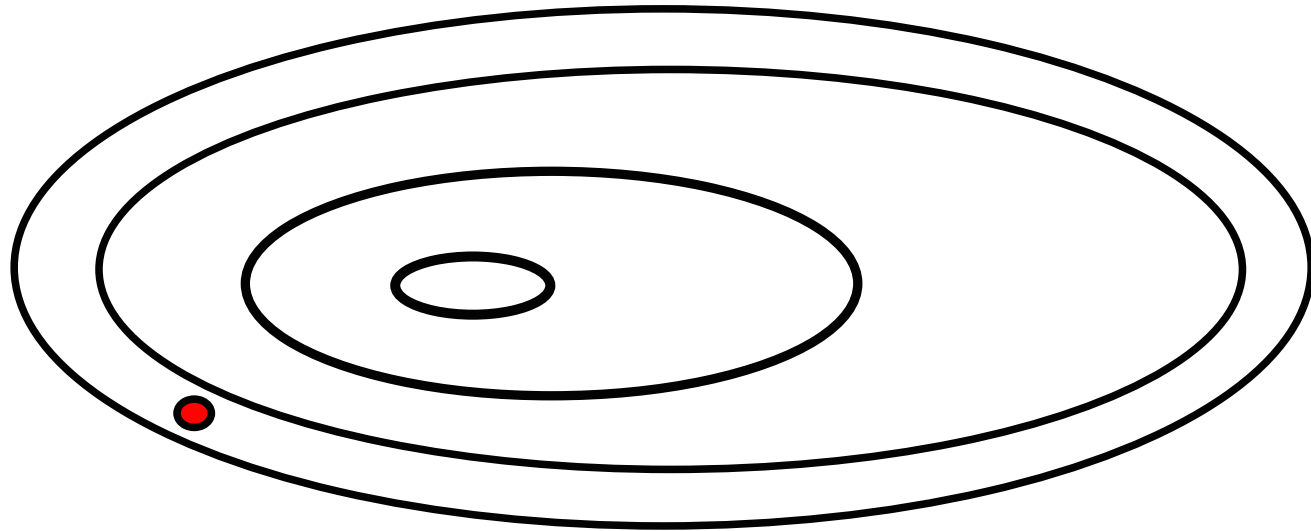
- Step



# GAN: Learning Rate and Momentum

## ■ Discriminator classification:

– Step



■ Adam:  $\alpha \leq 10^{-4}$      $\beta_1 = 0.5$      $\beta_2 = 0.9$

# Summary

- The Wasserstein distance is a measure of the distance of (data) distributions.
- The implicit usage of Lipschitz continuous functions acts as a regulator for the discriminator.
- The regulator removes a malicious scaling degree of freedom.
- The Wasserstein loss is less prone to vanishing gradients.
- Use smaller (than usual) learning rates and less momentum.



# First Test (CONEX)

## ■ CONEX: Hybrid Extensive Air Shower Simulation

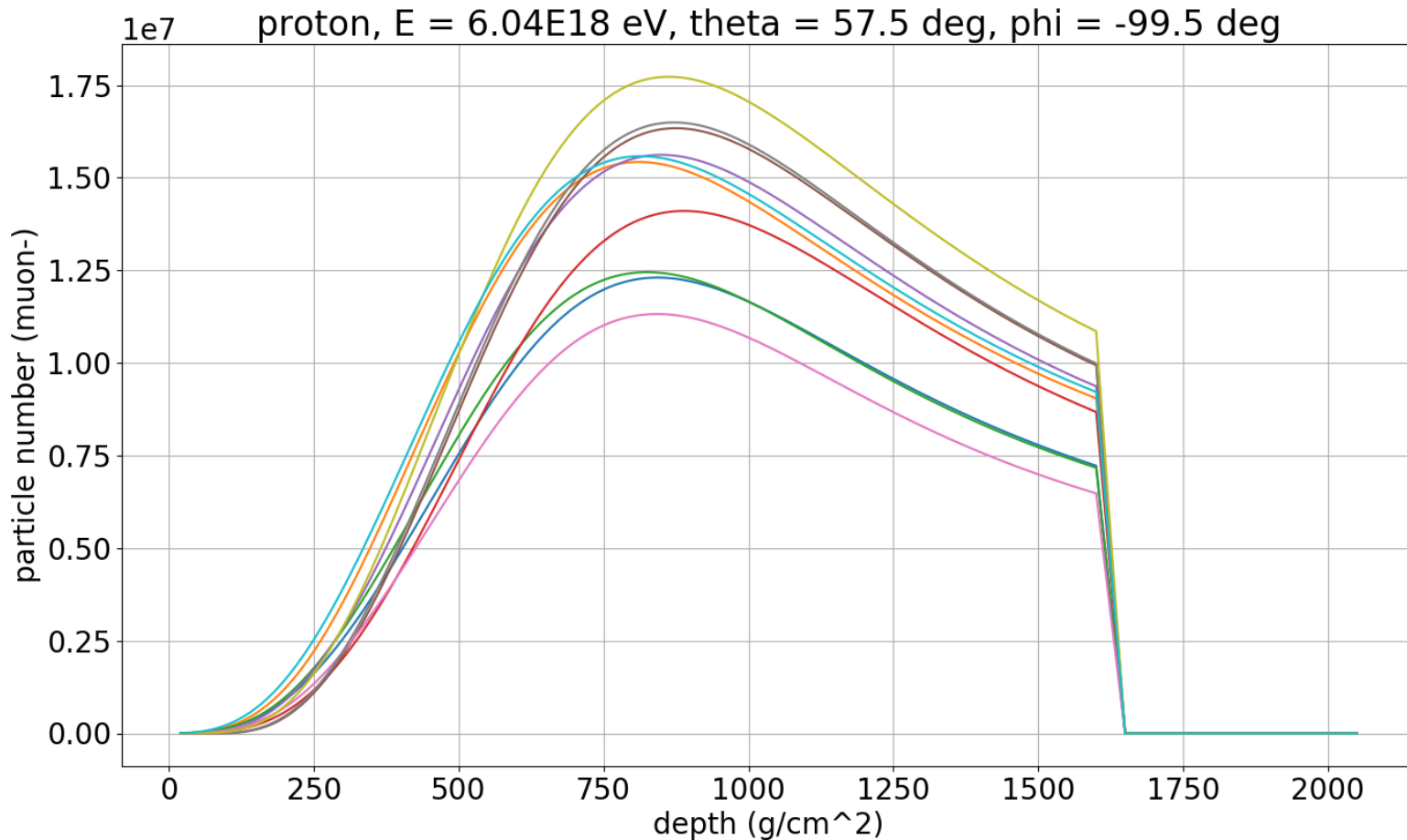
- first: Monte Carlo until energy threshold (3D)
- then: cascade equation solver (1D)
- provides longitudinal profile only
- runtime: seconds – minutes

## ■ Configuration:

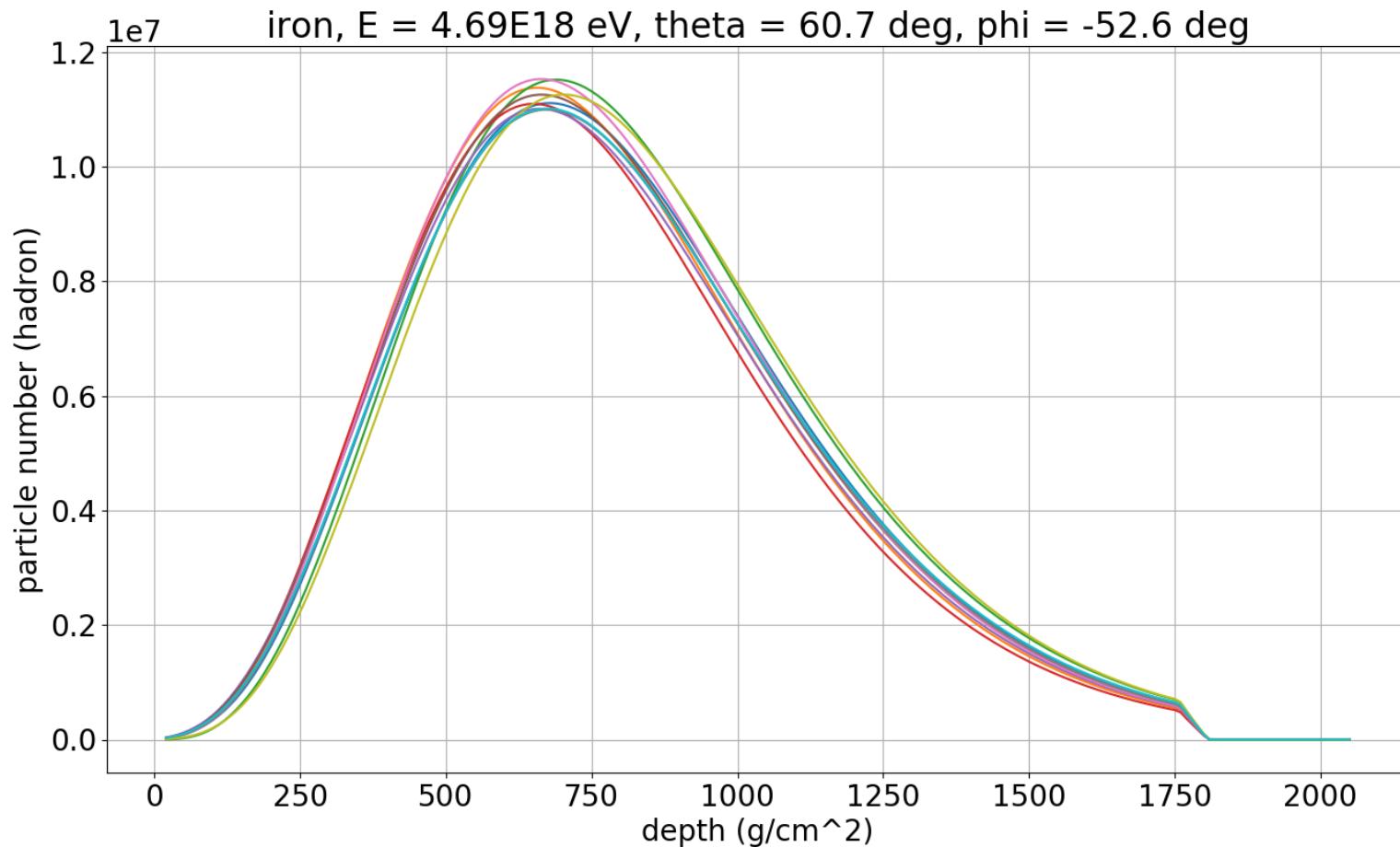
- $E = 1\text{E}17 \dots 1\text{E}19 \text{ eV}$
- Zenith = 0 ... 65 deg
- Azimuth = -180 ... 180 deg

## ■ Generated 200k + 300k datapoints

# Shower-to-Shower Fluctuations



# Shower-to-Shower Fluctuations



# (conditional) WGAN

## ■ Generator:

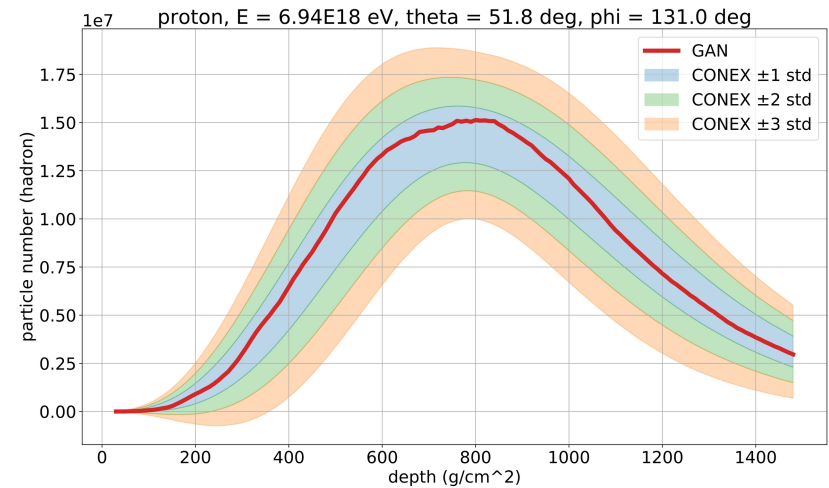
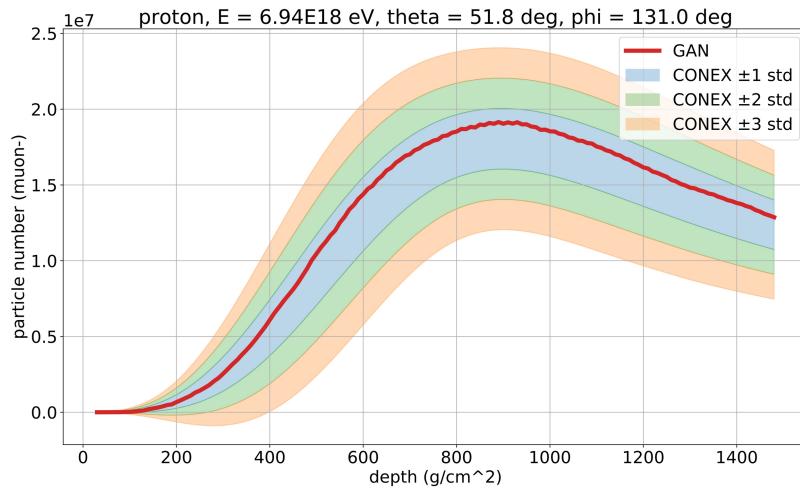
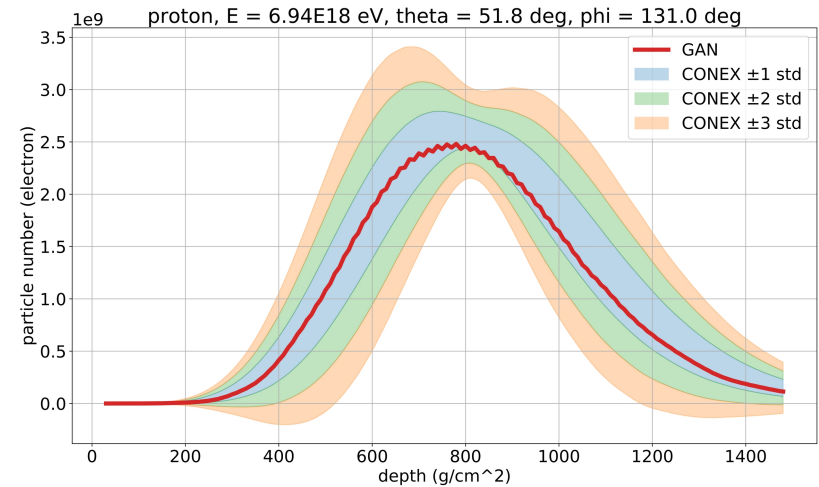
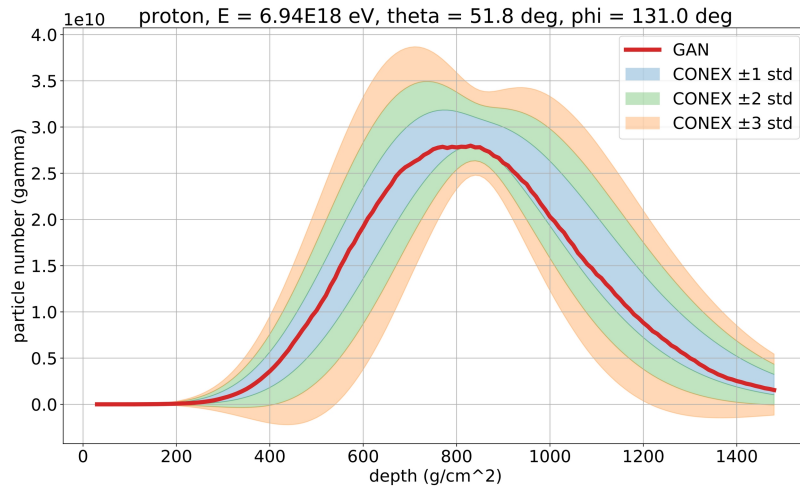
- 5x Dense
- 5x TransposeConvolution + Convolution
- Activation: tanh

## ■ Discriminator:

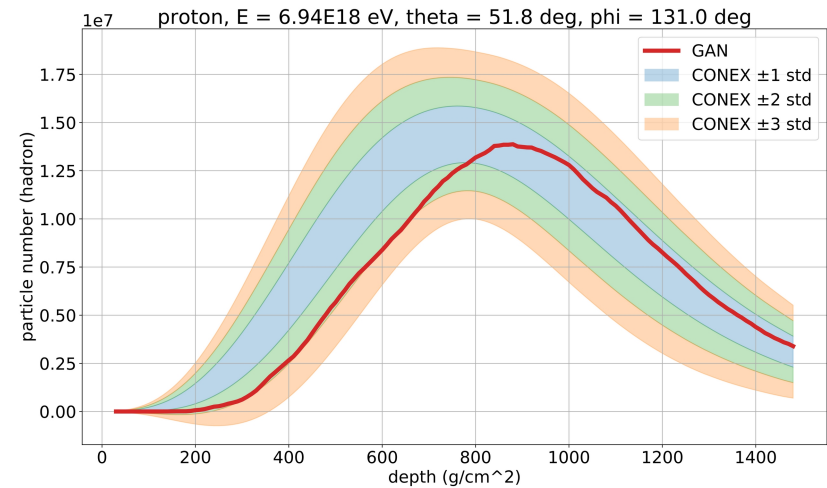
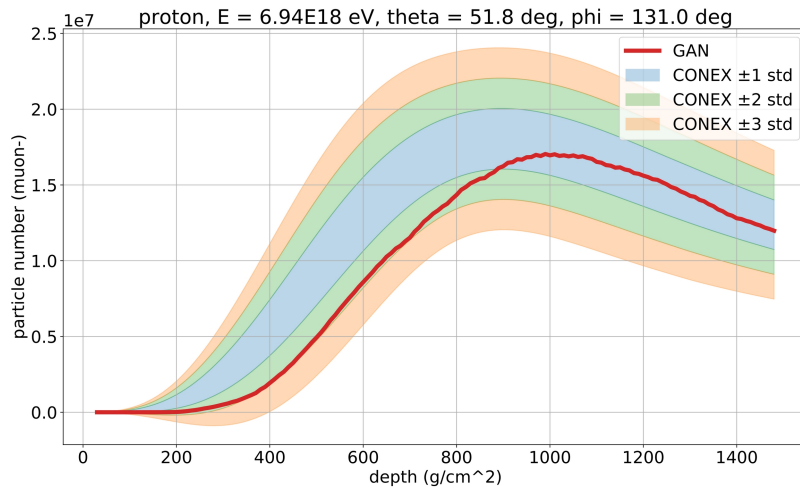
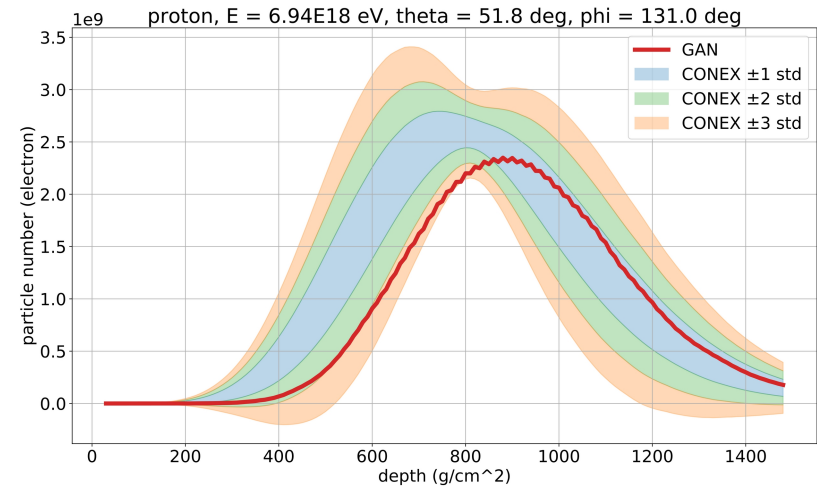
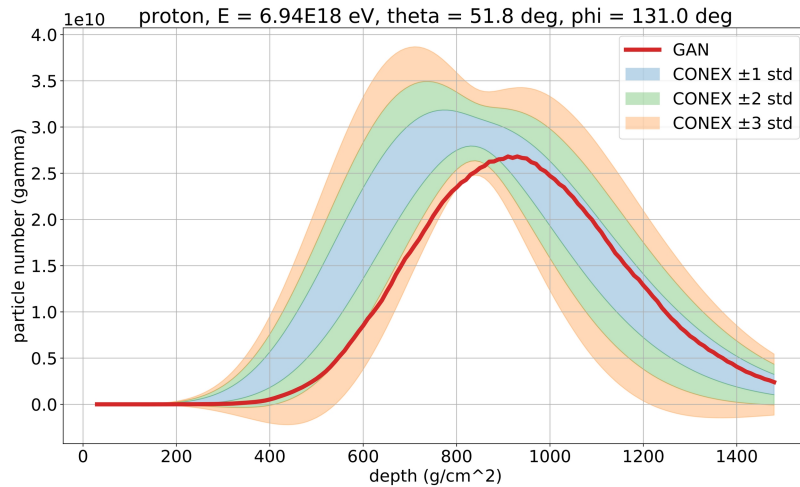
- 3x Dense
- 7x Convolution
- 2x Dense
- Activation: tanh

## ■ Trainable parameters: 79.072.457

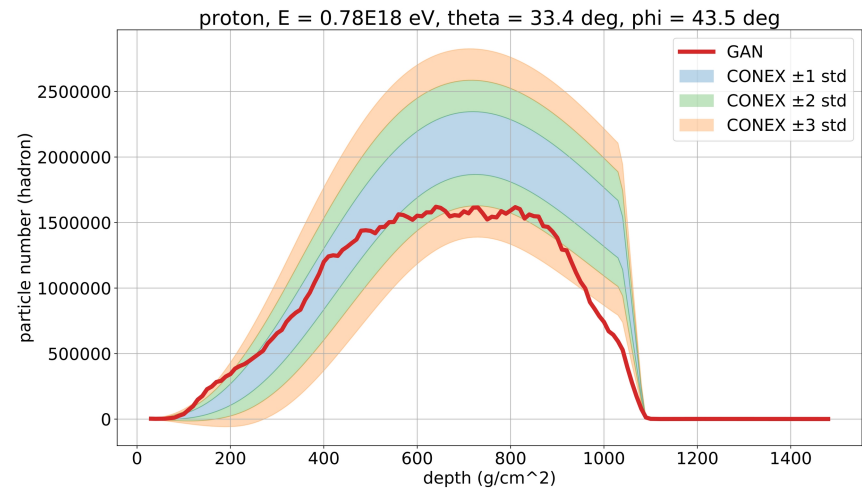
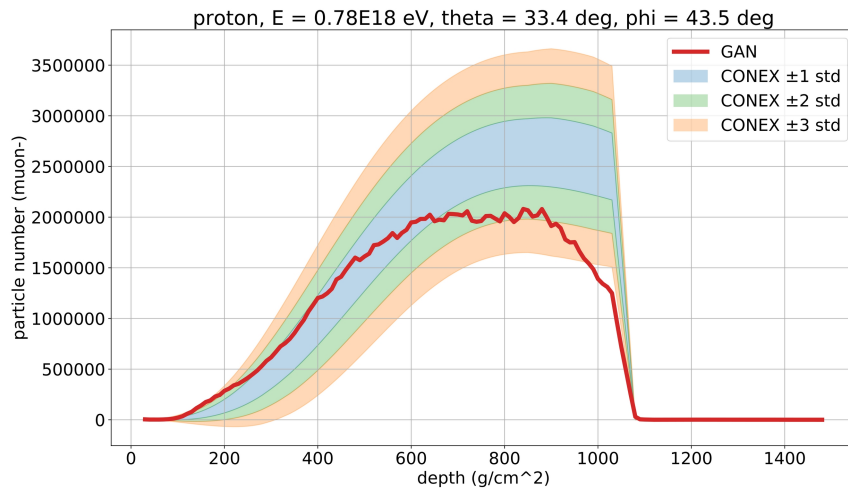
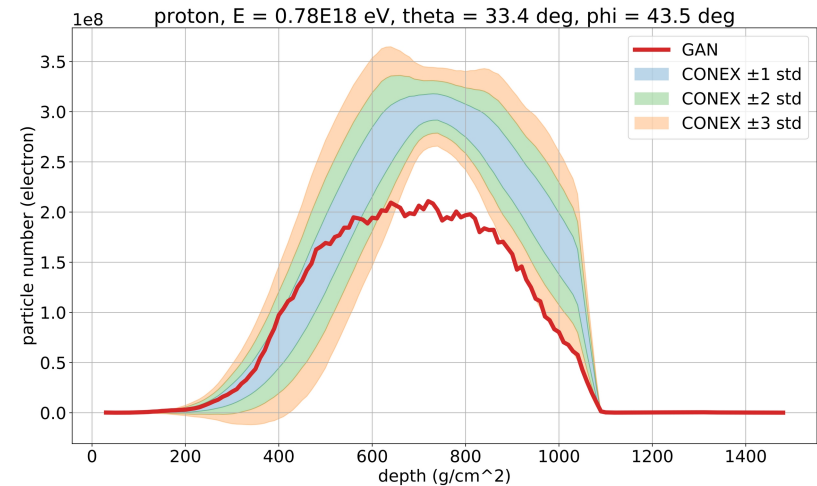
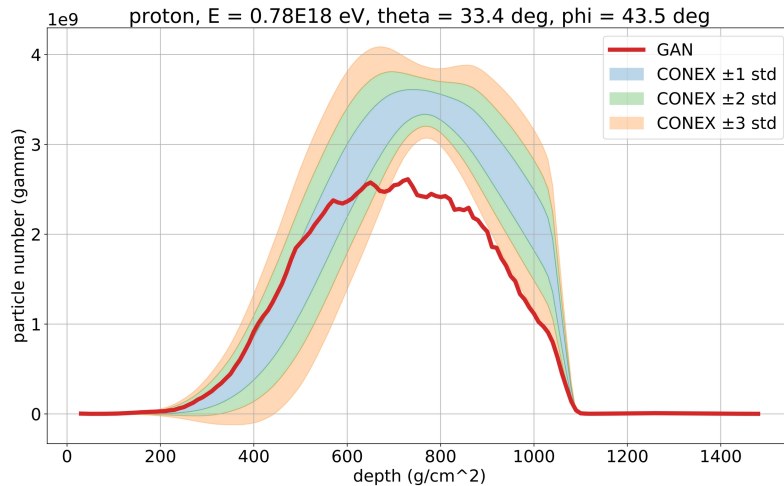
# CONEX vs. GAN



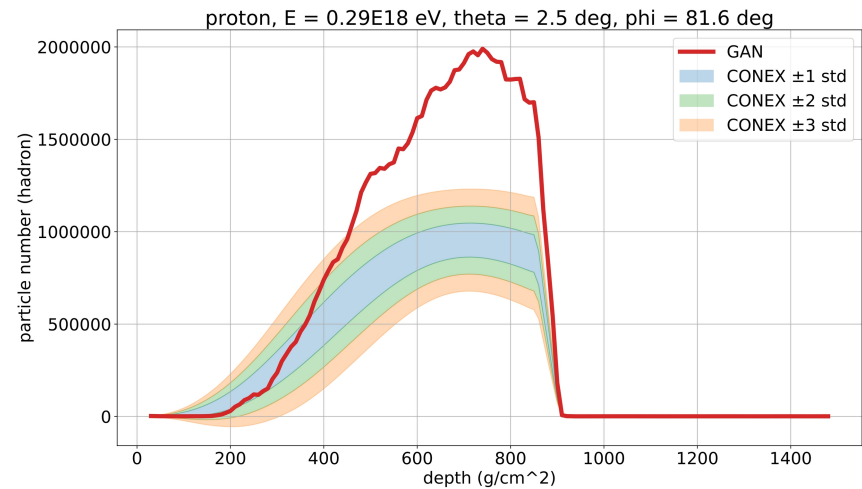
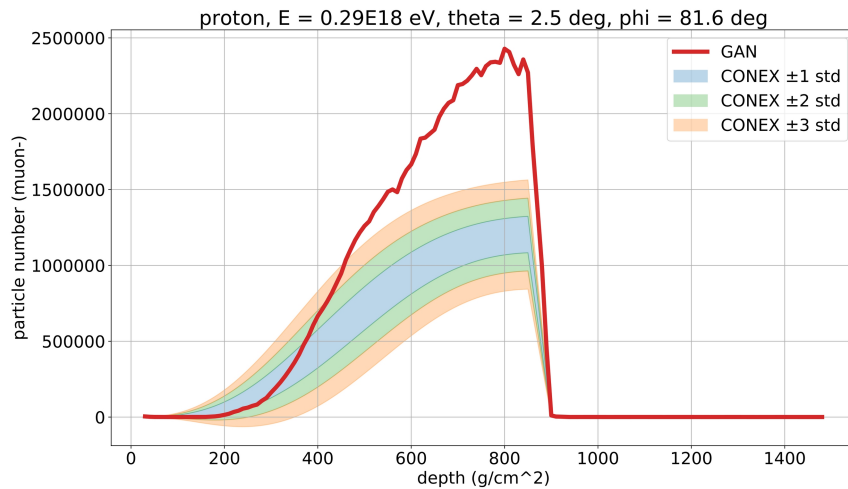
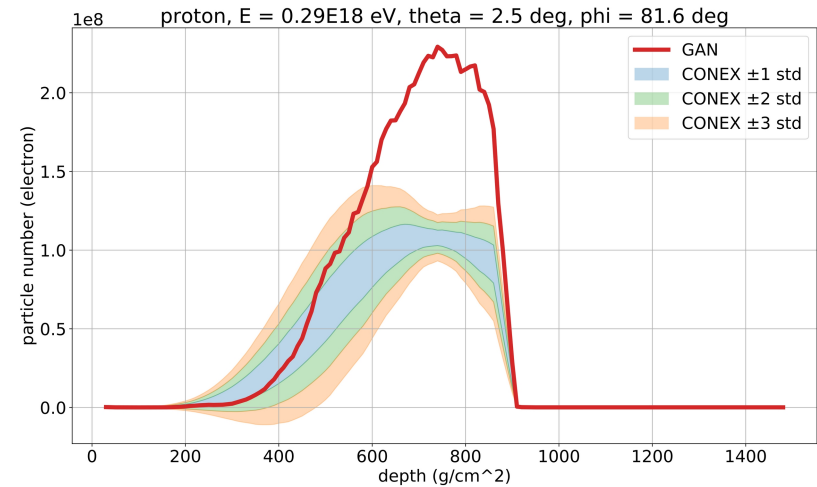
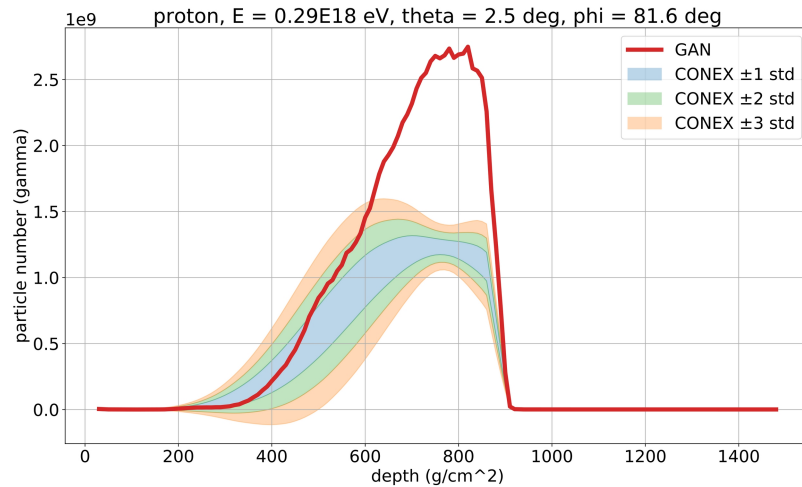
# CONEX vs. GAN



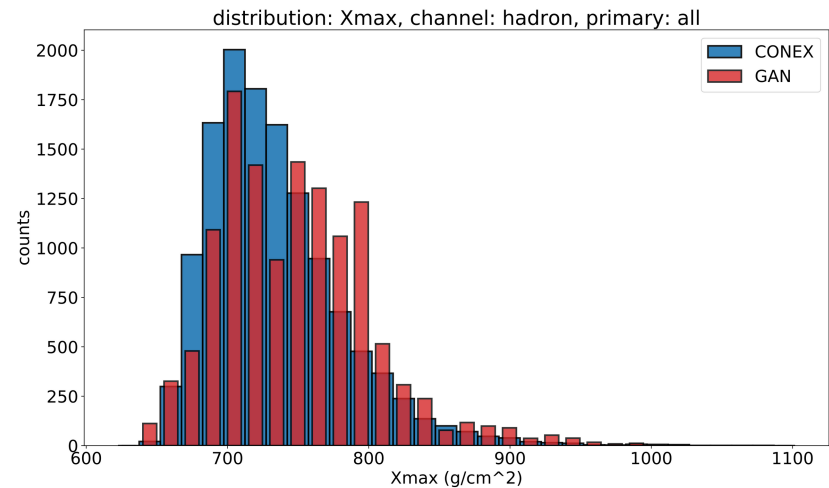
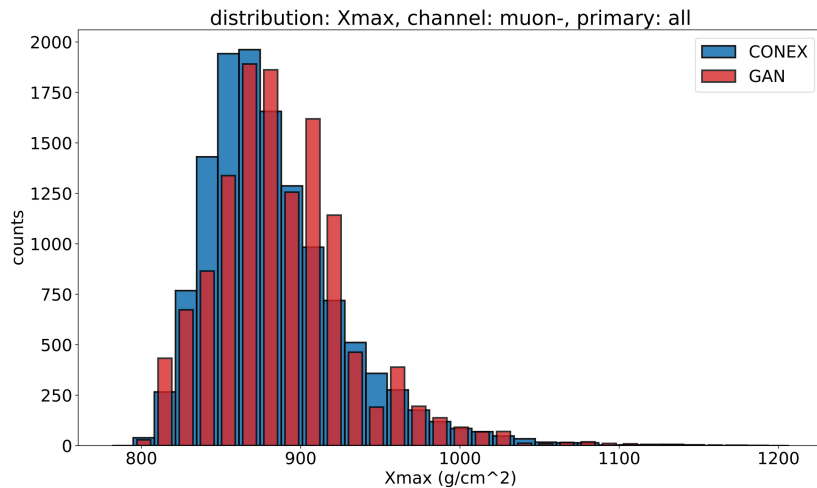
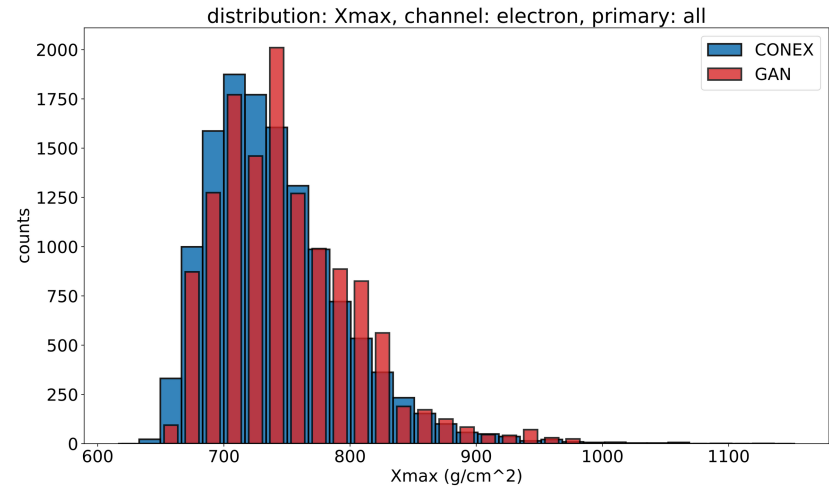
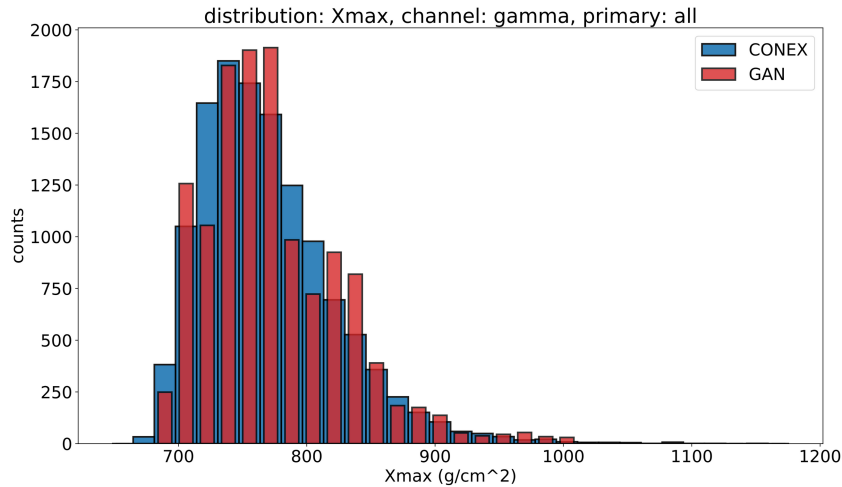
# CONEX vs. GAN



# CONEX vs. GAN



# Xmax Distribution ( $E > 5E18$ eV, $\theta > 35$ deg)

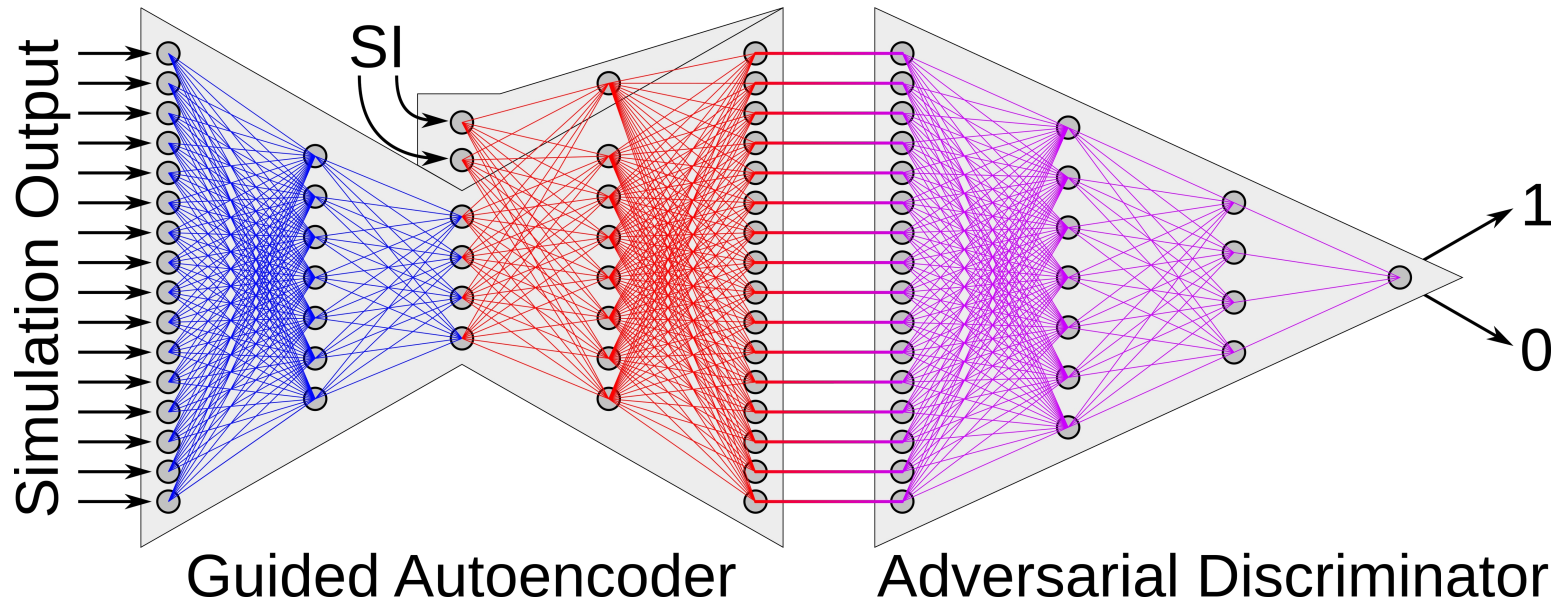


# What's next?

- Fix low energy behavior (oversampling, architecture, constrainers, ...)
- Verify and improve interpolation behavior
- Test adversarial vulnerability
- Template matching/reconstruction
- Refining with data

# Fast Implicit Simulation Heuristic (FISH)

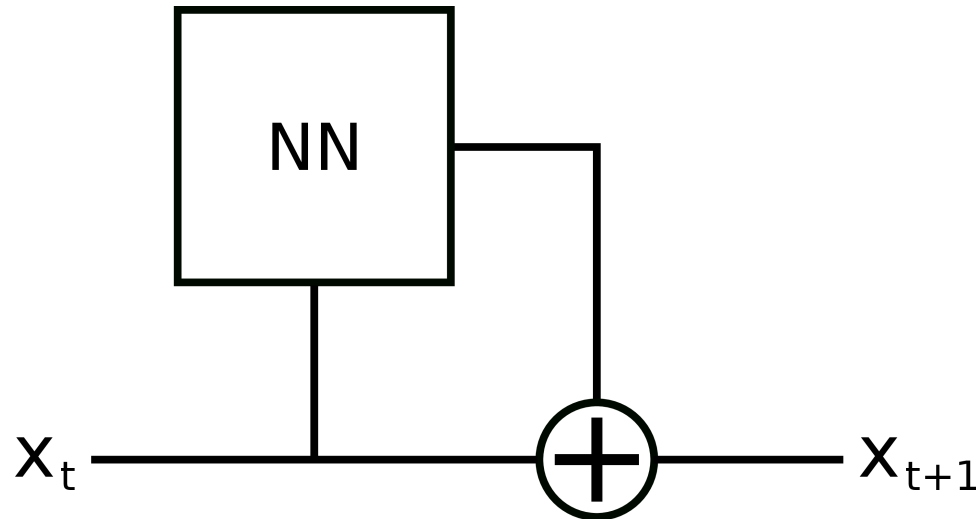
## ■ Autoencoder with Adversarial Metric



- Simulation Input (SI) can be extended with meta-parameters
- Discriminator can be refined with real measurements

# Adjustable Accuracy [3]

## ■ ResNet



## ■ Translate to ordinary differential equation (ODE)

$$x_{t+1} = x_t + f(x_t, \theta_t) \Rightarrow \frac{dx(t)}{dt} = f(x(t), t, \theta)$$

## ■ Solve with standard ODE solver

## ■ Adapt solver accuracy on the fly (training: high, inference: low)

# References

- Title picture:  
Photo by Pixabay from Pexels
- Backup picture:  
Photo by Anthony from Pexels
- [1] CORSIKA 7: <https://www.ikp.kit.edu/corsika/>
- [2] Wasserstein Distance:  
Lambdabadger / CC BY-SA (<https://creativecommons.org/licenses/by-sa/4.0>)
- [3] „Neural Ordinary Differential Equations“ - Ricky T. Q. Chen, Yulia Rubanova, Jesse Bettencourt, David Duvenaud – arXiv: [1806.07366](https://arxiv.org/abs/1806.07366)