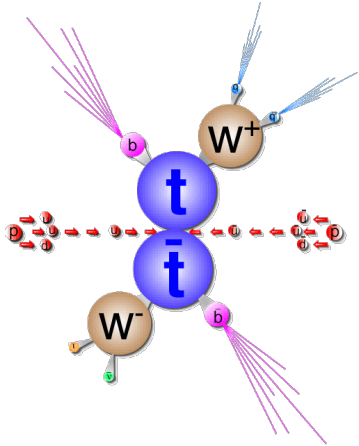


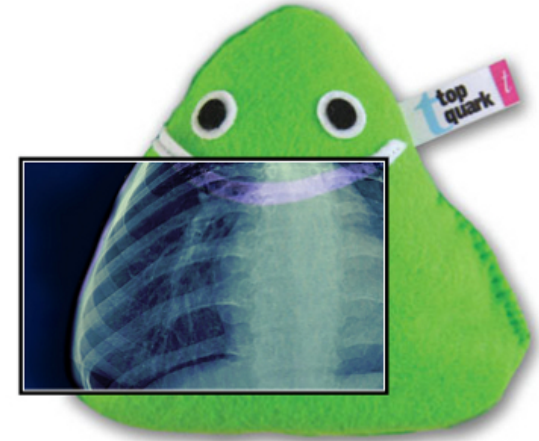
Project B1b: Precision top-quark physics at the LHC



PIs: M. Worek & M. Czakon



Outline



- Introduction
- Status of theoretical predictions $\Rightarrow$ QCD
- State-of-the-art (fixed order) theoretical predictions for:

$$pp \rightarrow t\bar{t}, t\bar{t}\gamma, t\bar{t}W^{\pm}, t\bar{t}Z$$

- Modeling of top quark production & decays $\Rightarrow$ *top quark in di-lepton channel*
 - NWA
 - Off-shell top quark effects

Papers in Project B1b (so far...)

NNLO

1. NNLO QCD corrections to leptonic observables in top-quark pair production and decay
 - [Czakon](#), Mitov, Poncelet
 - arXiv: 2008.11133
2. Higher order corrections to spin correlations in top quark pair production at the LHC
 - Behring, [Czakon](#), Mitov, Papanastasiou, Poncelet
 - *Phys. Rev. Lett.* **123** (2019) 082001

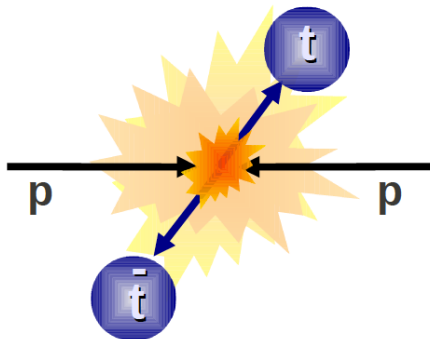
NLO

1. The simplest of them all: $t\bar{t}W^\pm$ at NLO accuracy in QCD
 - Bevilacqua, [Bi](#), Hartanto, Kraus, [Worek](#)
 - *JHEP* **08** (2020) 043
2. Off-shell vs on-shell modelling of top quarks in photon associated production
 - Bevilacqua, Hartanto, Kraus, [Weber](#), [Worek](#)
 - *JHEP* **2003** (2020) 154
3. Towards Constraining Dark Matter at the LHC: Higher order QCD predictions for $pp \rightarrow t\bar{t} + p_T^{miss}$
 - Bevilacqua, Hartanto, Kraus, Weber, [Worek](#)
 - *JHEP* **1911** (2019) 001

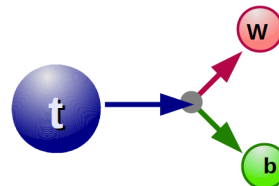
Why top quark is special

- Infrared structure of **QCD** $\Rightarrow$ Precision physics
 - Extract SM parameters as precisely as possible $\Rightarrow \alpha_s$ & m_t
 - Constraining gluon PDFs
 - Verify couplings to other particles $\Rightarrow \gamma, H, Z, W^\pm$
- Background process to various SM studies $\Rightarrow$ *Higgs boson*
- Window to New Physics
 - Direct searches $\Rightarrow$ Main background to many BSM scenarios
 - Indirect searches $\Rightarrow$ Precision tests of properties, rare decays, various top quark production modes

Production



Decays



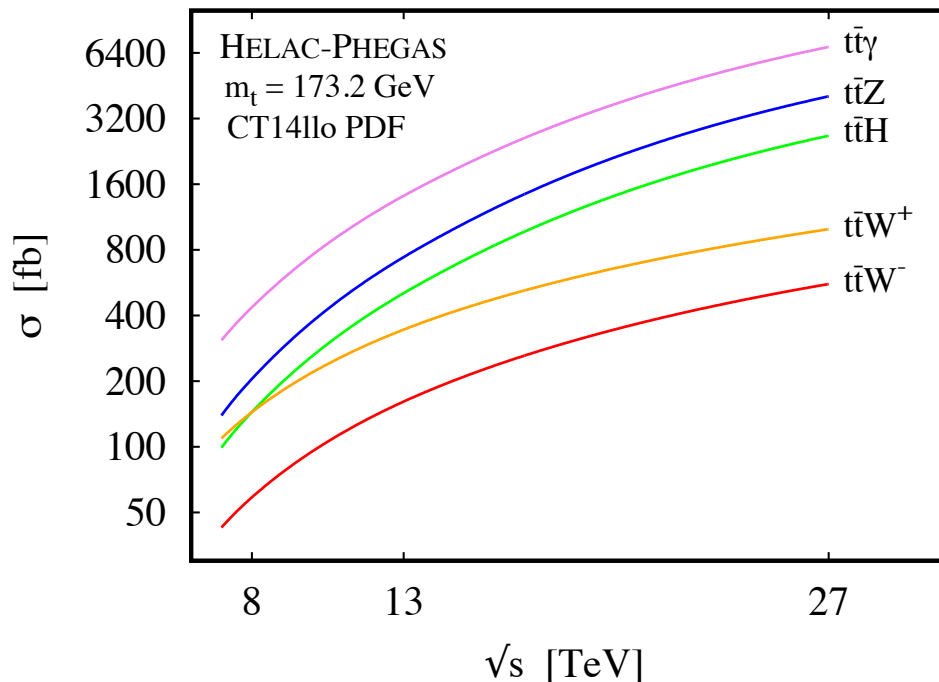
Intrinsic properties



$tt(j)$ & ttV

- NNLO in NWA $\Rightarrow tt$ di-lepton channel
- NLO with off-shell top quarks $\Rightarrow tt, ttj$ di-lepton channel
- Besides $tt(j)$ more exclusive final states can be accessed @ LHC

$t\bar{t}\gamma, t\bar{t}Z, t\bar{t}H, t\bar{t}W^+, t\bar{t}W^-$ @ LHC



*Stable top
quarks*

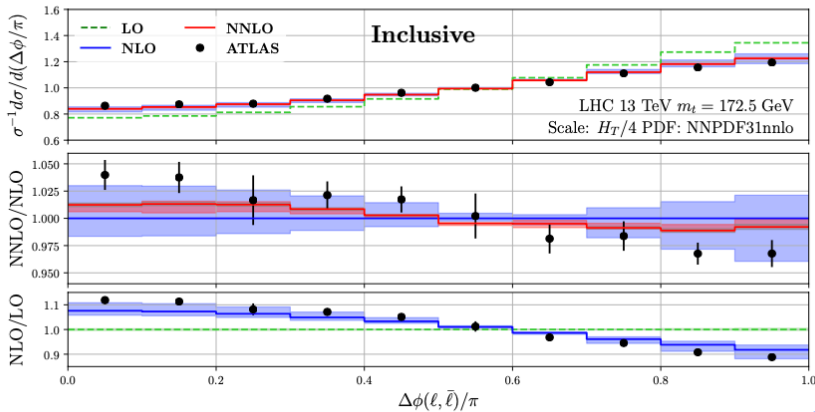
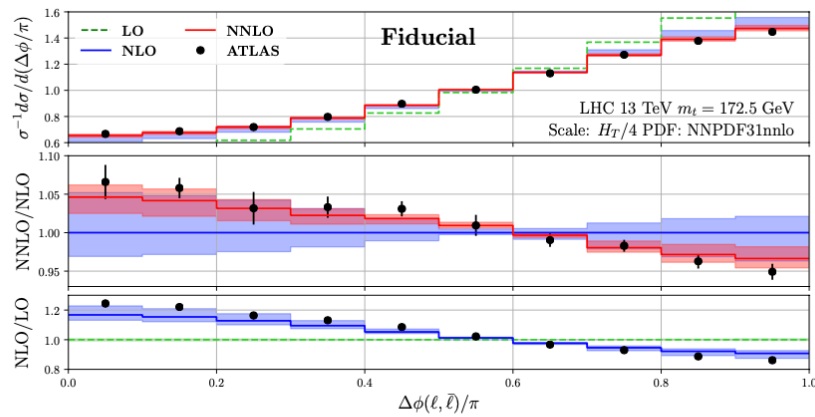
HELAC-PHEGAS

Cafarella, Papadopoulos, Worek '09

Top-Quark Pair Production & Decays

Normalized differential $t\bar{t}$ cross-section $\Rightarrow$ Azimuthal opening angle between two leptons

agreement



tension

*Top quarks in NWA
di-lepton channel*

Behring, Czakon, Mitov, Papanastasiou, Poncelet '19

Inclusive $\Rightarrow$ does not assume any selection cuts

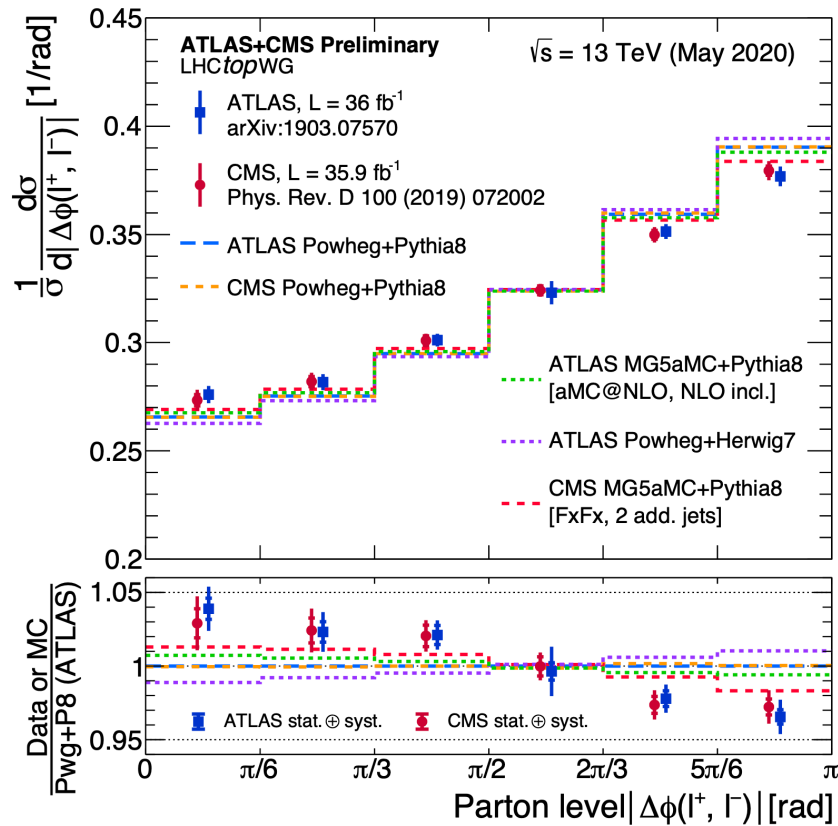
Fiducial $\Rightarrow$ based on the ATLAS selection cuts

Proper modeling of top-quark production & decay essential

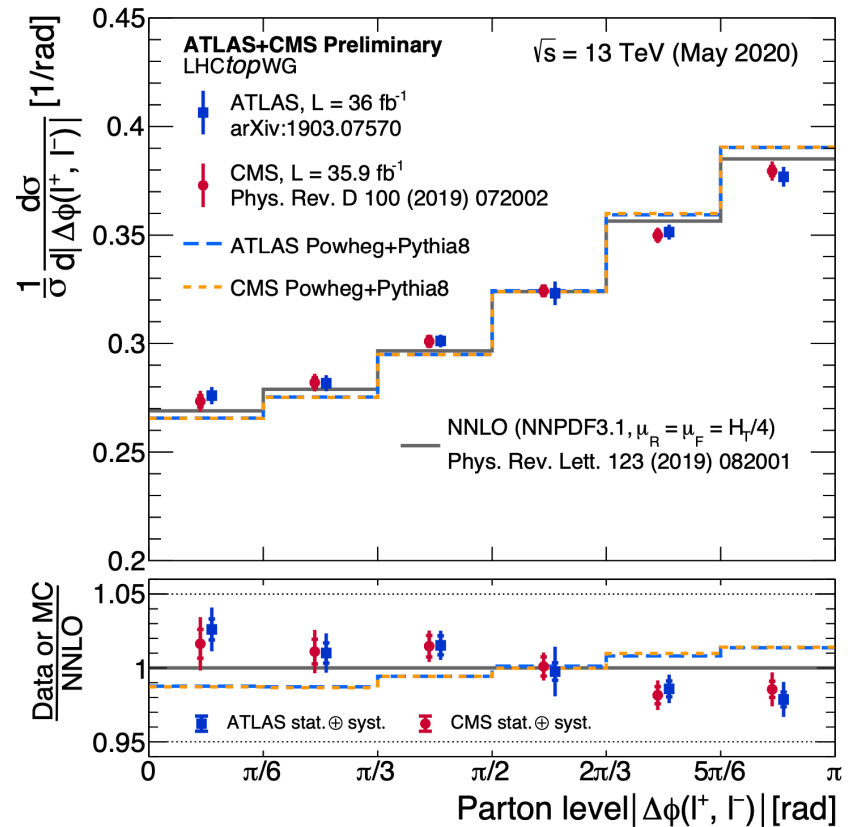
Top-Quark Pair Production & Decays

Normalized differential $t\bar{t}$ cross-section
 $\Rightarrow$ Azimuthal opening angle between two leptons

LHCtopWG



Comparison to Powheg &
 Mad-Graph5_aMC@NLO

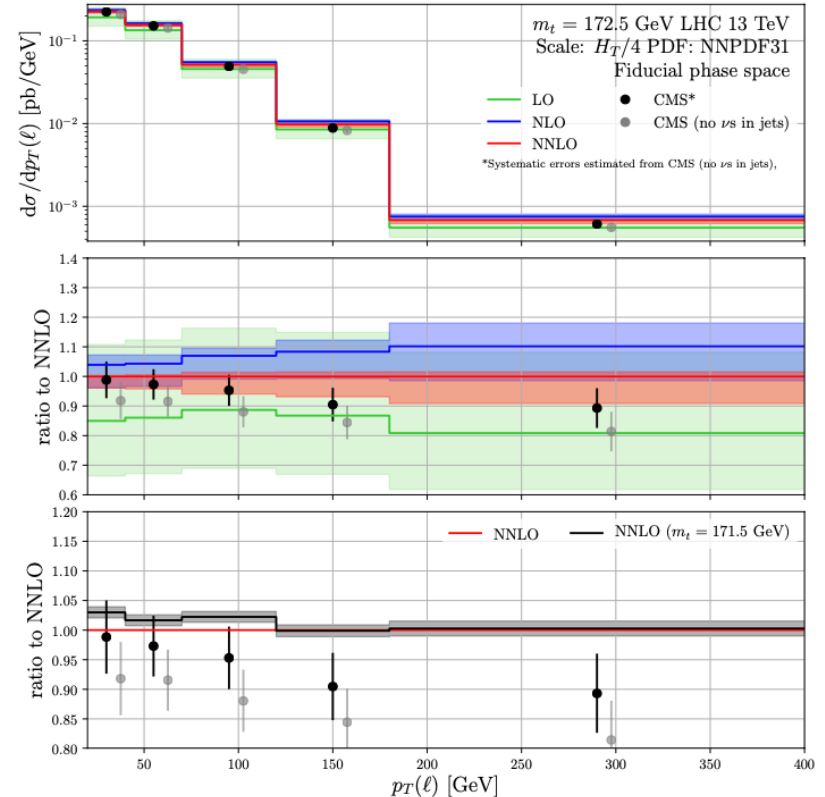
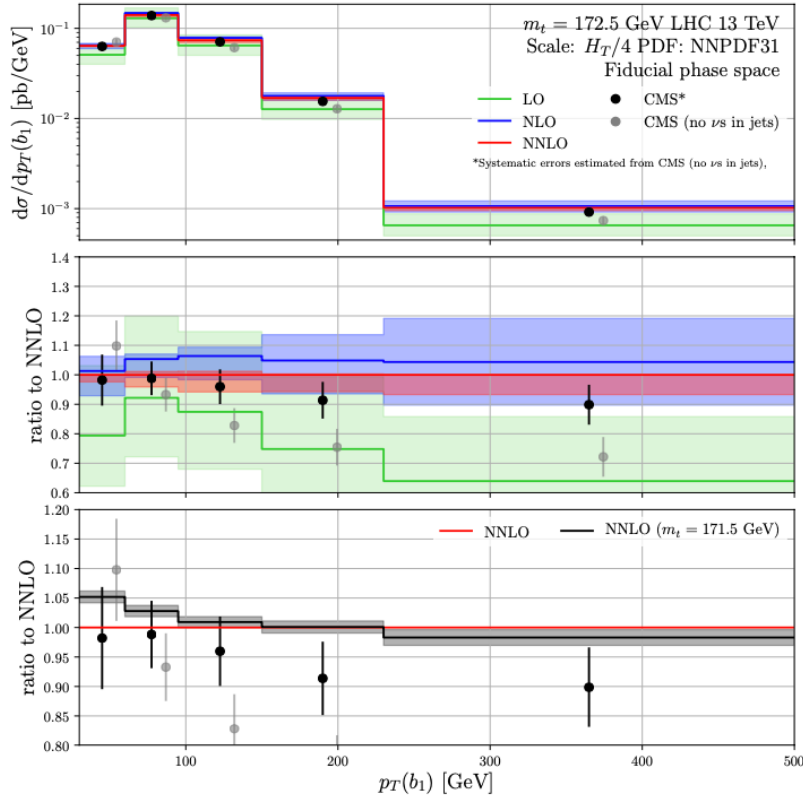


Comparison to NNLO QCD
 predictions in the NWA

Top-Quark Pair Production & Decays

Fiducial PS
CMS cuts

Czakon, Mitov, Poncelet '20



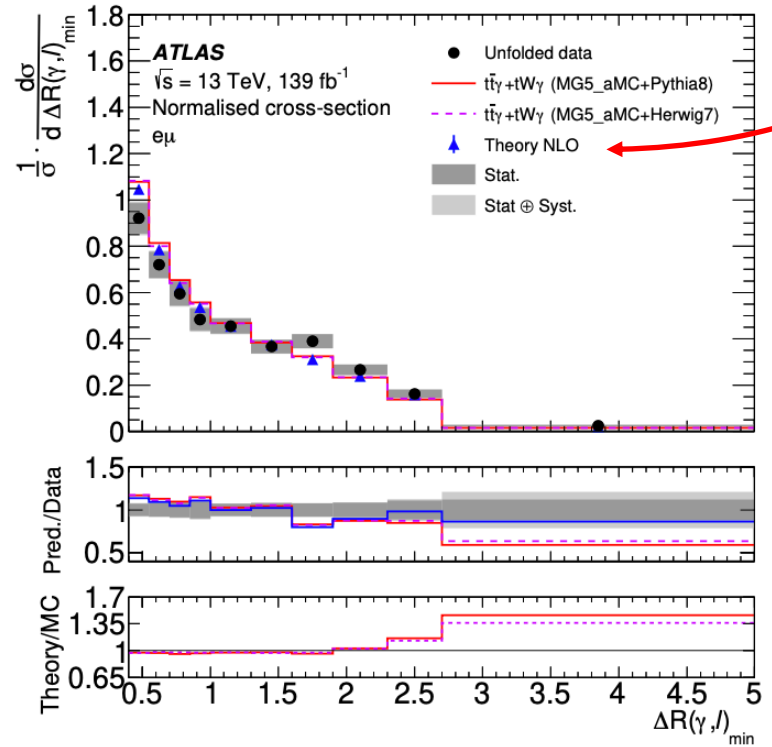
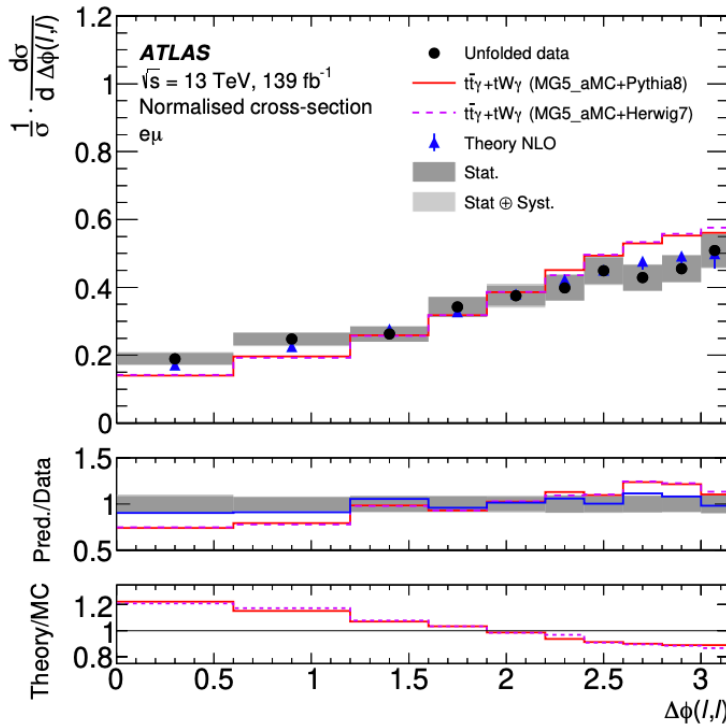
- p_T of *b-jet* & *lepton* $\Rightarrow$ Difference between two data sets $\Rightarrow$ With and without neutrinos from semileptonic B-decays
- All observables strongly affected $\Rightarrow$ Overall normalization & shape

Combined $t\bar{t}\gamma + tW\gamma$ Production & Decays

$e\mu$ channel

ATLAS Collaboration '20
JHEP 09 (2020) 049

HELAC-NLO



Predictions	$p_T(\gamma)$		$ \eta(\gamma) $		$\Delta R(\gamma, \ell)_{\min}$		$\Delta\phi(\ell, \ell)$		$ \Delta\eta(\ell, \ell) $	
	χ^2/ndf	p -value	χ^2/ndf	p -value	χ^2/ndf	p -value	χ^2/ndf	p -value	χ^2/ndf	p -value
$t\bar{t}\gamma + tW\gamma$ (MG5_aMC+Pythia8)	6.3/10	0.79	7.3/7	0.40	20.1/9	0.02	30.8/9	<0.01	6.5/7	0.48
$t\bar{t}\gamma + tW\gamma$ (MG5_aMC+Herwig7)	5.3/10	0.87	7.7/7	0.36	18.9/9	0.03	31.6/9	<0.01	6.8/7	0.45
Theory NLO	6.0/10	0.82	4.5/7	0.72	13.5/9	0.14	5.8/9	0.76	5.6/7	0.59

NWA & Off-Shell Effects

Complete off-shell effects

- Off-shell top quarks are described by Breit-Wigner propagators
- Double-, single- as well as non-resonant top-quark contributions are included
- All interference effects consistently incorporated at matrix element level

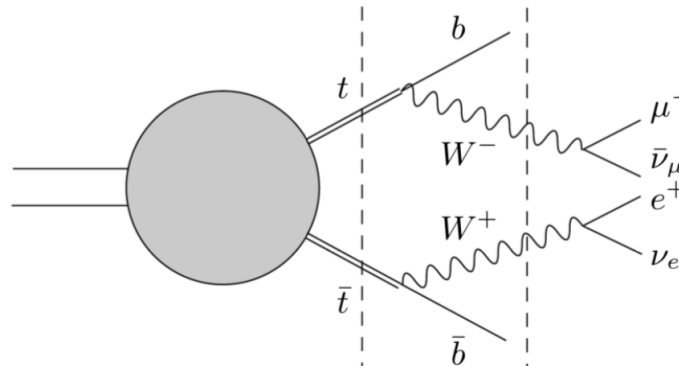
NWA

- Works in the limit $\Rightarrow \Gamma_t/m_t \rightarrow 0$

$$\Gamma_t = 1.35159 \text{ GeV}, m_t = 173.2 \text{ GeV}, \Gamma_t/m_t \approx 0.008$$

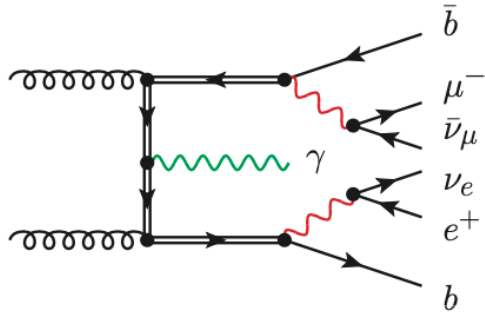
- Incorporates only double resonant contributions
- Restricts the unstable top quarks (W gauge bosons) to on-shell states

$$pp \rightarrow t\bar{t} \rightarrow W^+W^-b\bar{b} \rightarrow e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}$$

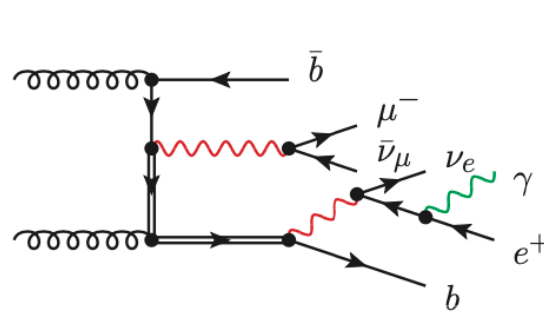


NWA & Off-Shell Effects

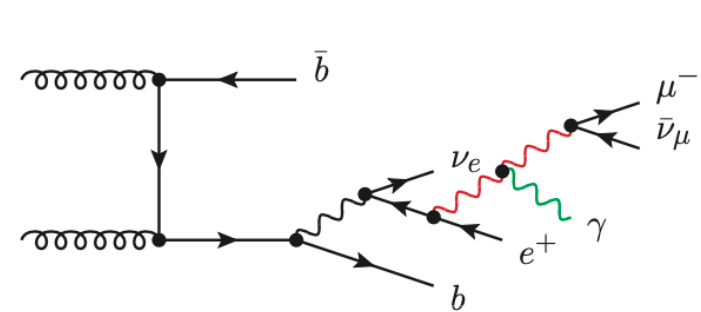
- Feynman Diagrams $\Rightarrow$ 628 @ LO for gg channel versus 38 in NWA
- 8 diagrams with photon in production and 30 in decay stage



two top-quark resonances

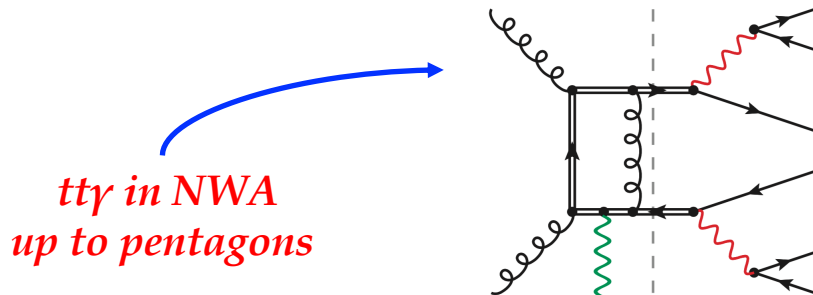


one top-quark resonance

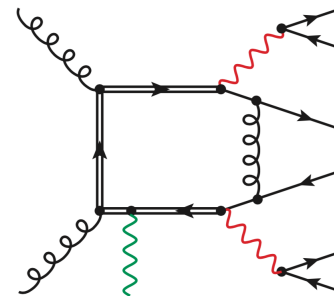


no top-quark resonances

- NLO $\Rightarrow$ 4348 real emission & 36032 @ 1-loop for gg channel
- Most complicated $\Rightarrow$ 90 heptagons & 958 hexagons



*ttγ in NWA
up to pentagons*



*ttγ full
up to heptagons*

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$$

How Good Is the NWA ?

- Should be accurate for sufficiently inclusive observables
- Off-shell effects for integrated fiducial $\sigma_{tt} \Rightarrow$ *at few % level* @ NLO in QCD

• tt (di-lepton)	Denner, Dittmaier, Kallweit, Pozzorini '11 '12 Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek '11 Frederix '14 Heinrich, Maier, Nisius, Schlenk, Winter '14 Denner, Pellen '16 (EW+QCD) Jezo, Lindert, Nason, Oleari, Pozzorini '16 (PS)
• tt (lepton+jets)	Denner, Pellen '18
• ttH (di-lepton)	Denner, Feger '15 Denner, Lang, Pellen, Uccirati '17 (EW+QCD)
• ttj (di-lepton)	Bevilacqua, Hartanto, Kraus, Worek '16 '18
• $tt\gamma$ (di-lepton)	Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19 '20
• $ttZ, Z \rightarrow \nu_l \bar{\nu}_l$ (di-lepton)	Bevilacqua, Hartanto, Kraus, Weber, Worek '19
• ttW (di-lepton)	Bevilacqua, Bi, Hartanto, Kraus, Worek '20 Denner, Pelliccioli '20
• $ttbb$ (di-lepton)	Denner, Lang, Pellen '20

Fiducial Cross Section for $t\bar{t}\gamma$

HELAC-NLO

$e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}\gamma$ @ LHC_{13TeV}

MODELLING APPROACH	σ^{LO} [fb]	σ^{NLO} [fb]
full off-shell ($\mu_0 = H_T/4$)	$7.32^{+2.45 (33\%)}_{-1.71 (23\%)}$	$7.50^{+0.11 (1\%)}_{-0.45 (6\%)}$
NWA ($\mu_0 = m_t/2$)	$8.08^{+2.84 (35\%)}_{-1.96 (24\%)}$	$7.28^{+0.99 (13\%)}_{-0.03 (0.4\%)}$
NWA ($\mu_0 = H_T/4$)	$7.18^{+2.39 (33\%)}_{-1.68 (23\%)}$	$7.33^{+0.43 (5.9\%)}_{-0.24 (3.3\%)}$
NWA $_{\gamma\text{-prod}}$ ($\mu_0 = m_t/2$)	$4.52^{+1.63 (36\%)}_{-1.11 (24\%)}$	$4.13^{+0.53 (13\%)}_{-0.05 (1.2\%)}$
NWA $_{\gamma\text{-prod}}$ ($\mu_0 = H_T/4$)	$3.85^{+1.29 (33\%)}_{-0.90 (23\%)}$	$4.15^{+0.12 (2.3\%)}_{-0.21 (5.1\%)}$
NWA $_{\gamma\text{-decay}}$ ($\mu_0 = m_t/2$)	$3.56^{+1.20 (34\%)}_{-0.85 (24\%)}$	$3.15^{+0.46 (15\%)}_{+0.03 (0.9\%)}$
NWA $_{\gamma\text{-decay}}$ ($\mu_0 = H_T/4$)	$3.33^{+1.10 (33\%)}_{-0.77 (23\%)}$	$3.18^{+0.31 (9.7\%)}_{-0.03 (0.9\%)}$
NWA _{LOdecay} ($\mu_0 = m_t/2$)		$4.85^{+0.26 (5.4\%)}_{-0.48 (9.9\%)}$
NWA _{LOdecay} ($\mu_0 = H_T/4$)		$4.63^{+0.44 (9.5\%)}_{-0.52 (11\%)}$

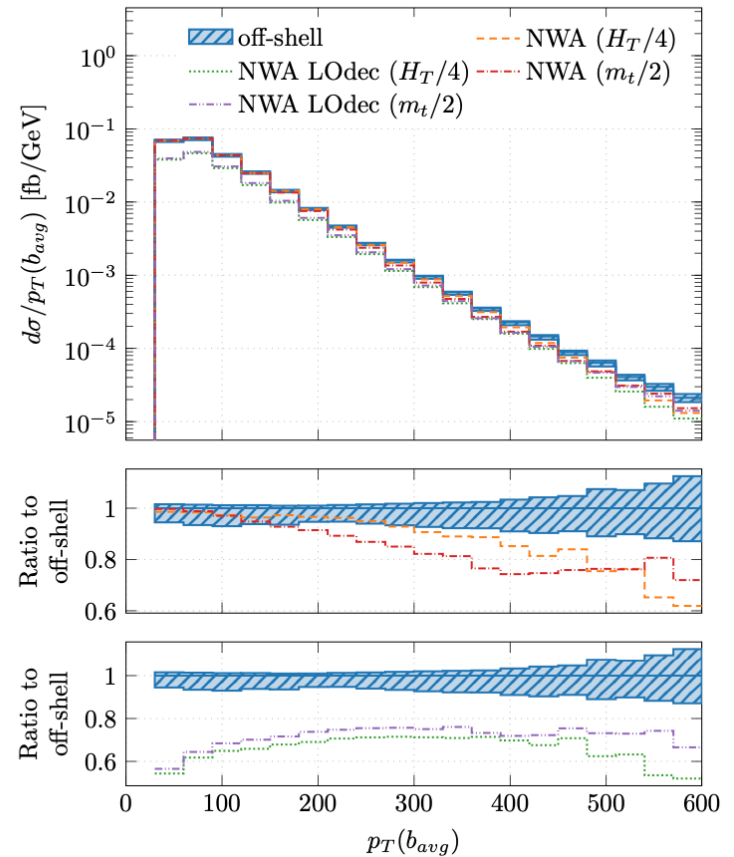
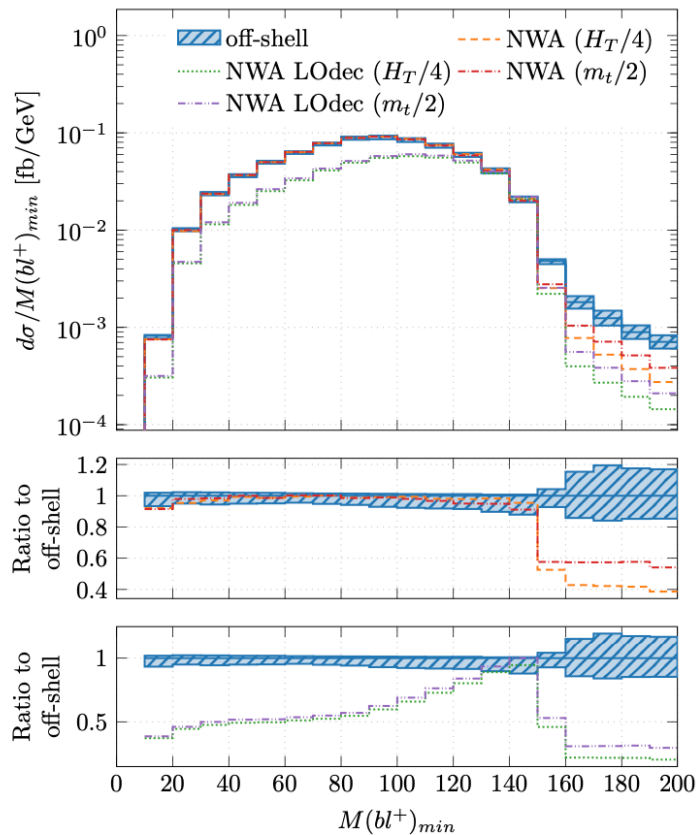
Various approaches for the modelling of top quark production & decays

- Off-shell effects **3%**
- Consistent with $\Gamma_t/m_t \approx 0.8\%$
- 57%** $\Rightarrow$ γ emitted in production
- 43%** $\Rightarrow$ γ emitted in decay stage
- For $p_{T,b} > 25 \text{ GeV}$ it is **50%-50%**
- NLO QCD corrections to top quark decays are negative and not small
- 17%** $\Rightarrow \mu_0 = 1/2 m_t$
- 12%** $\Rightarrow \mu_0 = 1/4 H_T$
- Theoretical uncertainties not underestimated for the full NWA

How Good Is the NWA ?

- *Dimensionful* observables are sensitive to non-factorizable top quark corrections $\Rightarrow$ *Tens of per cent* in specific phase-space regions
- *Kinematical edges & high p_T regions*

$e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ @ LHC₁₃TeV



Various Phase-space Regions

$e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ @ LHC_{13TeV}

Bevilacqua, Hartanto, Kraus, Weber, Worek '20

- 3 different resonance histories $\Rightarrow$ Resolved jet at NLO gives 9 in total

(i)	$t = W^+(\rightarrow e^+ \nu_e) b$	and	$\bar{t} = W^-(\rightarrow \mu^- \bar{\nu}_\mu) \bar{b},$
(ii)	$t = W^+(\rightarrow e^+ \nu_e) b \gamma$	and	$\bar{t} = W^-(\rightarrow \mu^- \bar{\nu}_\mu) \bar{b},$
(iii)	$t = W^+(\rightarrow e^+ \nu_e) b$	and	$\bar{t} = W^-(\rightarrow \mu^- \bar{\nu}_\mu) \bar{b} \gamma$

- Compute for each history Q and pick the one that minimises the Q value

$$Q = |M(t) - m_t| + |M(\bar{t}) - m_t|$$

- Double-resonant (DR):** $|M(t) - m_t| < n \Gamma_t,$ and $|M(\bar{t}) - m_t| < n \Gamma_t$

- Two single-resonant regions (SR):**

$$|M(t) - m_t| < n \Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| > n \Gamma_t.$$

$$|M(t) - m_t| > n \Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| < n \Gamma_t$$

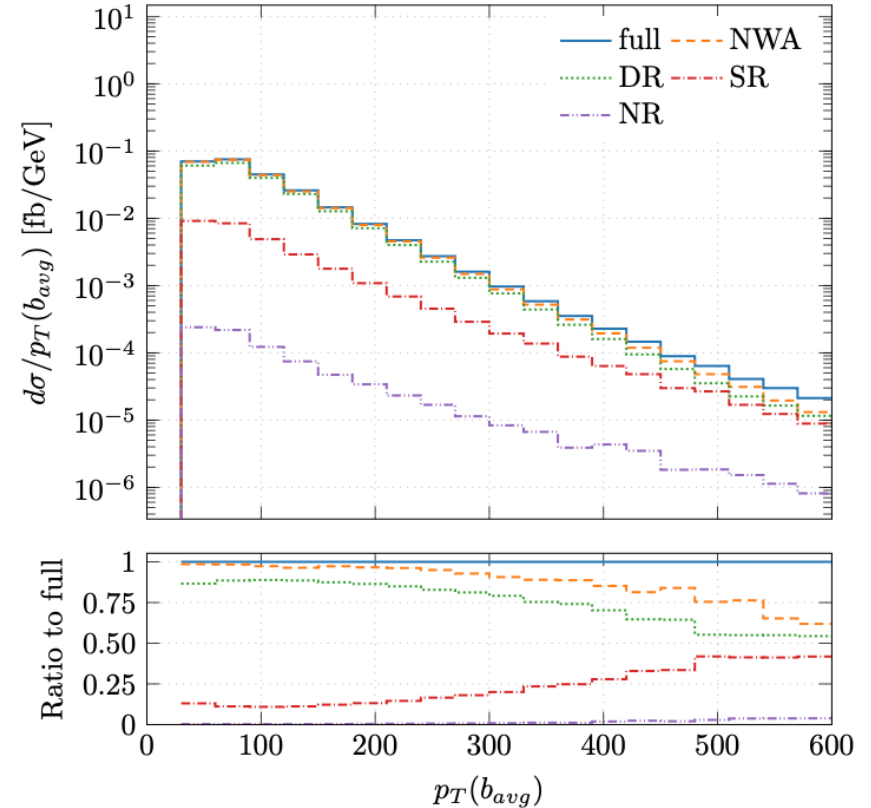
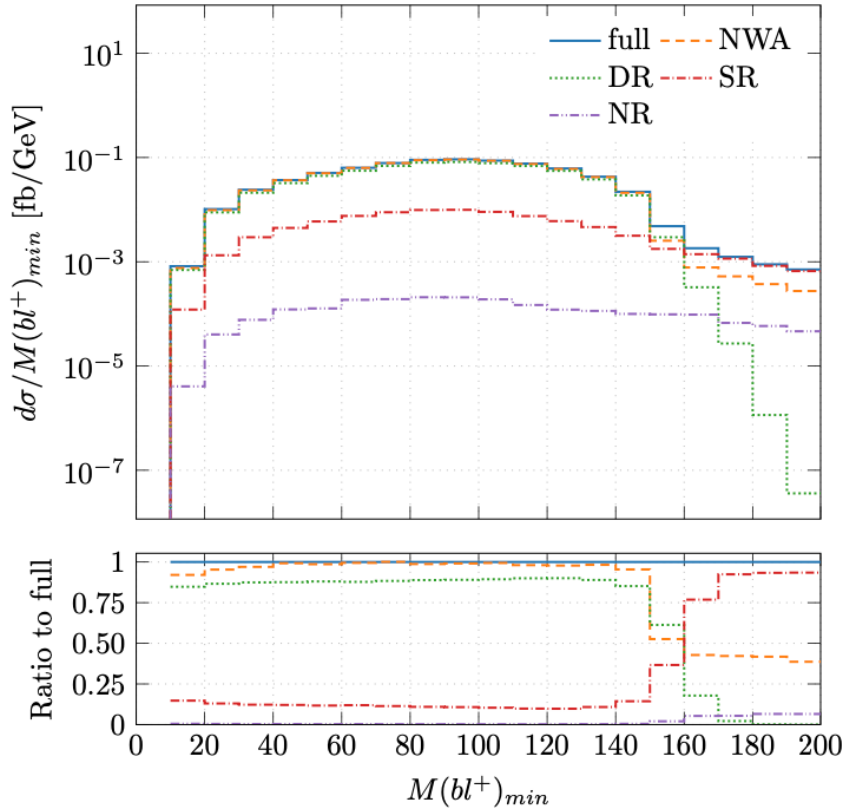
- Non-resonant region (NR):**

$$|M(t) - m_t| > n \Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| > n \Gamma_t$$

Various Phase-space Regions

HELAC-NLO

$e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ @ LHC₁₃TeV



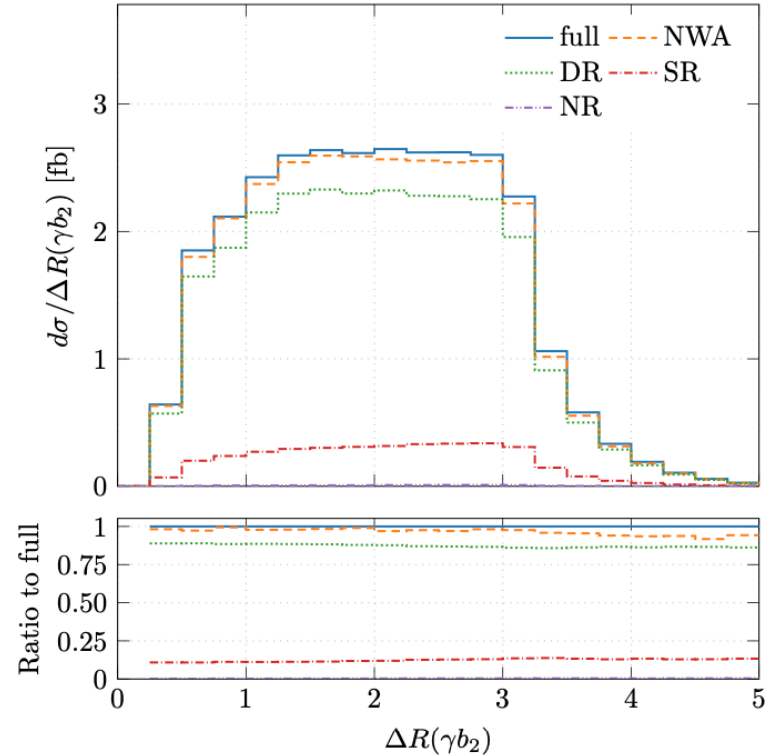
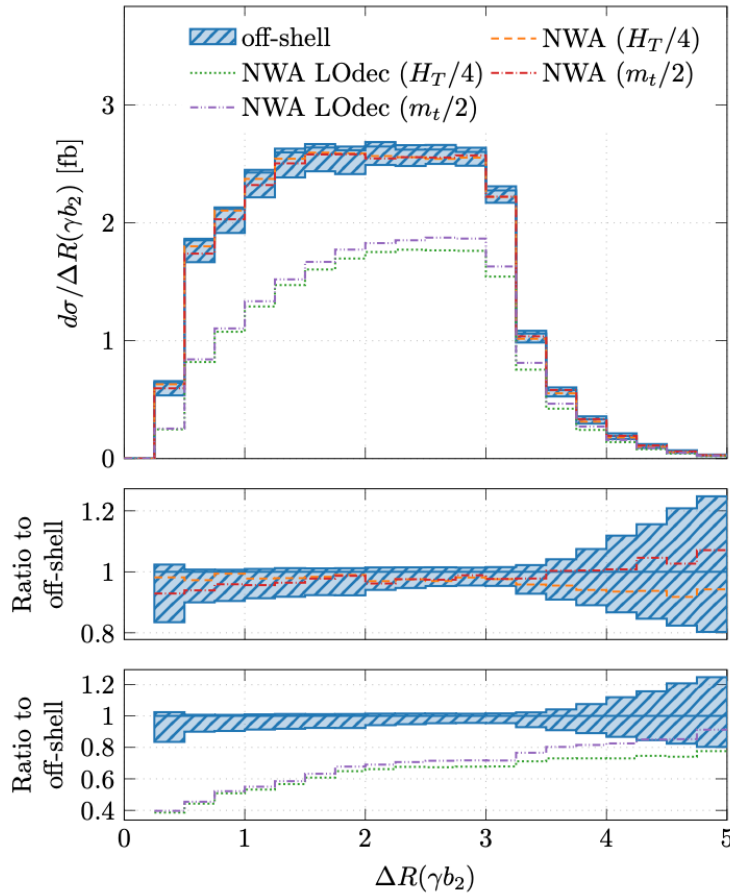
Bevilacqua, Hartanto, Kraus, Weber, Worek '20

Off-shell effects:

- High p_T region of various dimensionful observables
- Vicinity of kinematical edges
- Contribute up to **50% – 60%**

Various Phase-space Regions

$e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ @ LHC₁₃TeV

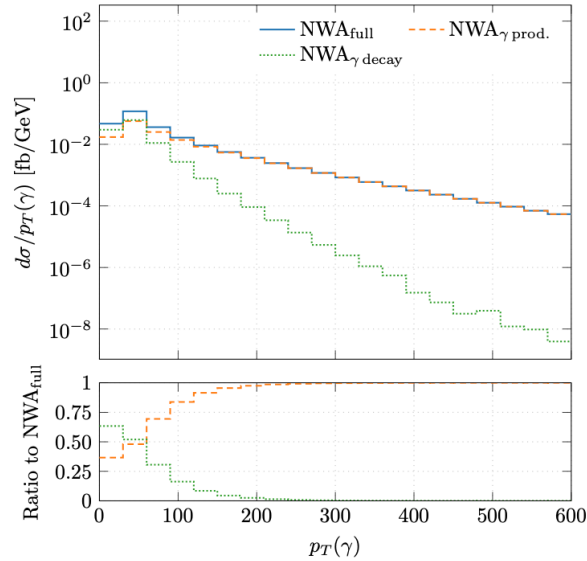
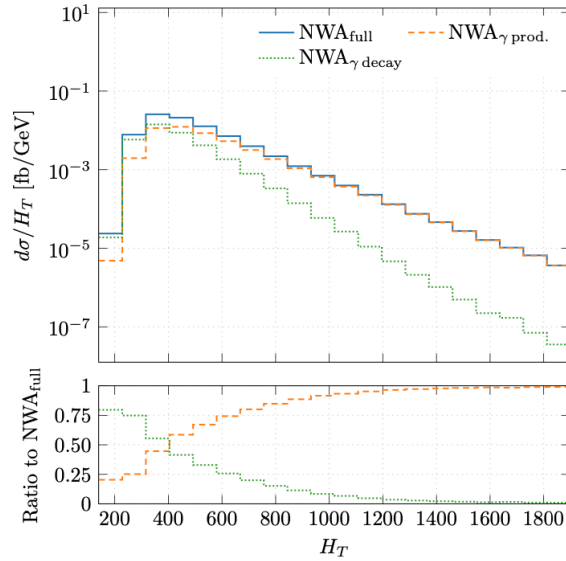


Bevilacqua, Hartanto, Kraus, Weber, Worek '20

- Observables sensitive to top quark off-shell effects $\Rightarrow$ Substantial contributions from single top quark process
- *Dimensionless observables rather insensitive to top quark off-shell effects*

γ in Production & Decays $\Rightarrow$ Differential Level

Bevilacqua, Hartanto, Kraus, Weber, Worek '20



HELAC-NLO

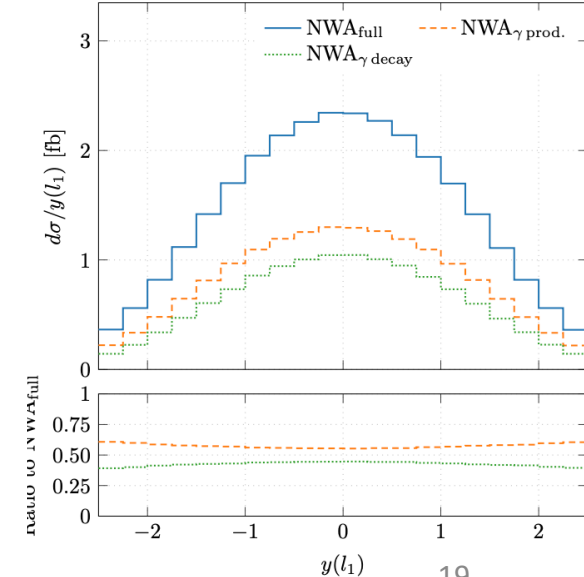
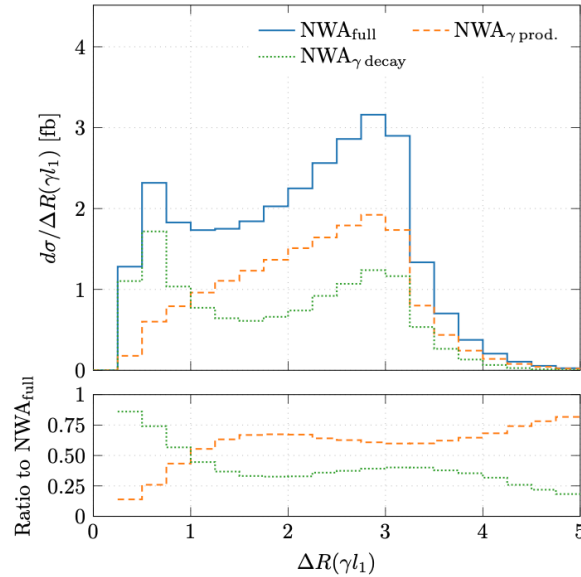
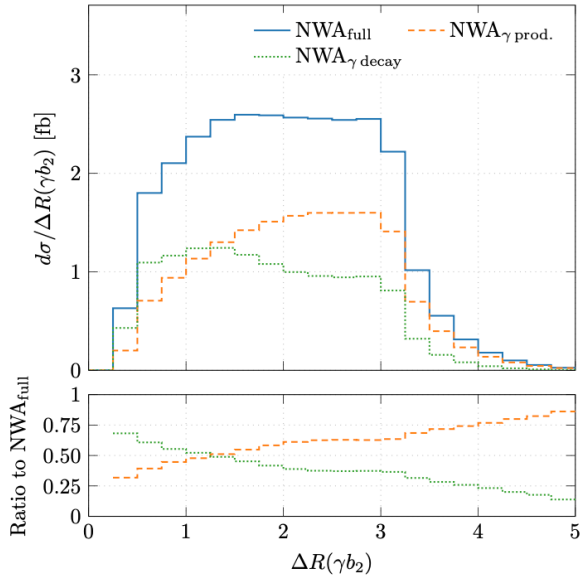
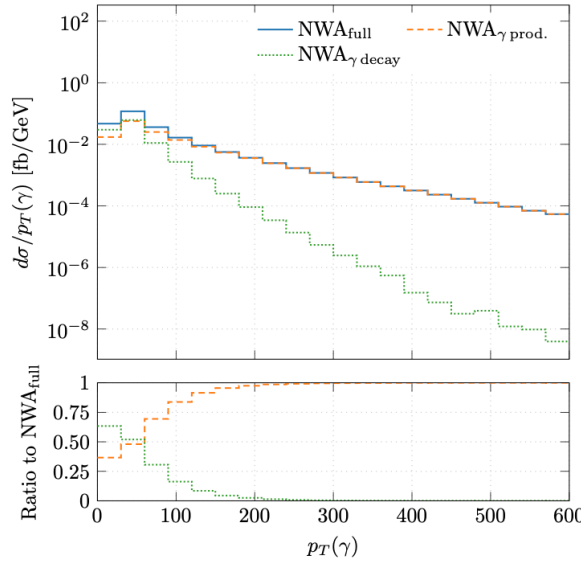
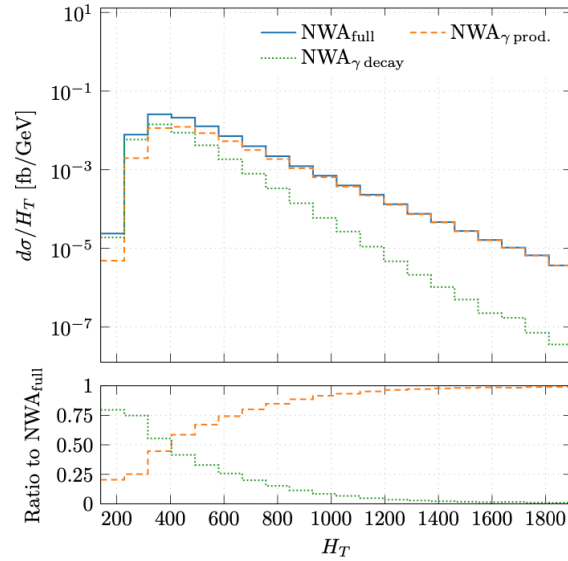
- Diverse picture
- Photon emission in decays can be reduced
 - $H_T > 400 \text{ GeV}$
 - $p_T(\gamma) > 50 \text{ GeV}$

γ in Production & Decays $\Rightarrow$ Differential Level

Bevilacqua, Hartanto, Kraus, Weber, Worek '20

HELAC-NLO

- Diverse picture
- Photon emission in decays can be reduced
 - $H_T > 400 \text{ GeV}$
 - $p_T(\gamma) > 50 \text{ GeV}$



ttW with dynamical & fixed scale

HELAC-NLO

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} e^+ \nu_e @ \text{LHC}_{13\text{TeV}}$$

Bevilacqua,
Bi,
Hartanto,
Kraus,
Worek '20

$\mu_R = \mu_F = \mu_0 = m_t + m_W/2$							
PDF	$p_T(j_b)$	σ^{LO} [ab]	δ_{scale}	σ^{NLO} [ab]	δ_{scale}	δ_{PDF}	$\sigma^{\text{NLO}}/\sigma^{\text{LO}}$
NNPDF3.0	25	106.9	+27.7 (26%) -20.5 (19%)	123.2	+6.3 (5%) -8.7 (7%)	+2.1 (2%) -2.1 (2%)	1.15
	30	99.2	+25.8 (26%) -19.1 (19%)	113.1	+5.4 (5%) -7.8 (7%)	+1.9 (2%) -1.9 (2%)	1.14
	35	90.8	+23.7 (26%) -17.5 (19%)	102.6	+4.7 (5%) -6.8 (7%)	+1.7 (2%) -1.7 (2%)	1.13
	40	82.1	+21.5 (26%) -15.9 (19%)	92.0	+4.0 (4%) -6.1 (7%)	+1.6 (2%) -1.6 (2%)	1.12

$\mu_R = \mu_F = \mu_0 = H_T/3$							
PDF	$p_T(j_b)$	σ^{LO} [ab]	δ_{scale}	σ^{NLO} [ab]	δ_{scale}	δ_{PDF}	$\sigma^{\text{NLO}}/\sigma^{\text{LO}}$
NNPDF3.0	25	115.1	+30.5 (26%) -22.5 (20%)	124.4	+4.3 (3%) -7.7 (6%)	+2.1 (2%) -2.1 (2%)	1.08
	30	106.5	+28.2 (26%) -20.8 (20%)	113.9	+3.5 (3%) -6.8 (6%)	+1.9 (2%) -1.9 (2%)	1.07
	35	97.0	+25.7 (27%) -18.9 (20%)	103.1	+3.1 (3%) -6.0 (6%)	+1.7 (2%) -1.7 (2%)	1.06
	40	87.2	+23.2 (27%) -17.0 (20%)	92.3	+2.8 (3%) -5.3 (6%)	+1.5 (2%) -1.5 (2%)	1.06

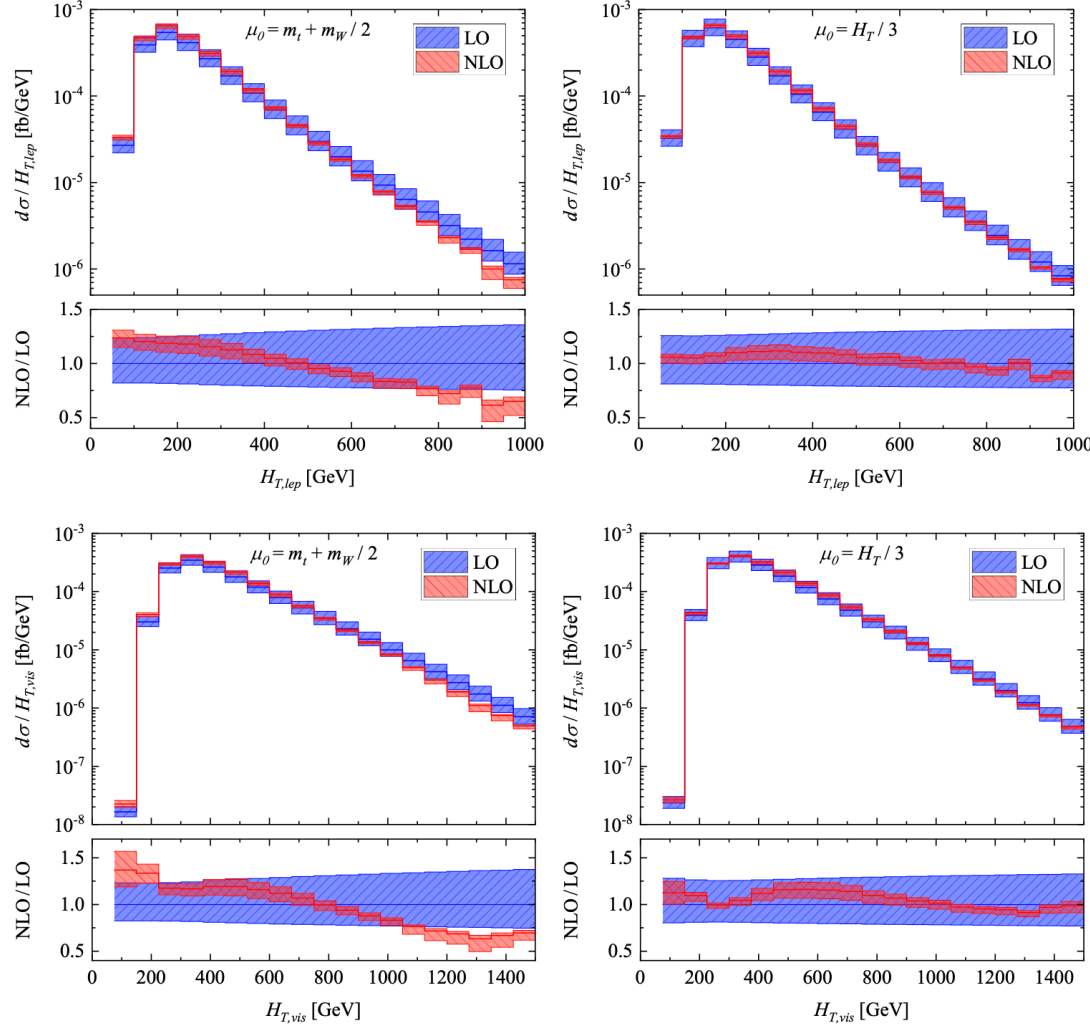
ttW stable with respect to central scale choice in fiducial regions

ttW with dynamical scale

HELAC-NLO

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} e^+ \nu_e @ \text{LHC}_{13\text{TeV}}$$

Bevilacqua, Bi, Hartanto, Kraus,
Worek '20



Fixed scale

- NLO QCD $\Rightarrow$ +25% up -35%
- Uncertainties $\Rightarrow$ 15% – 20%
- Perturbative instabilities in TeV regions

Dynamical scale

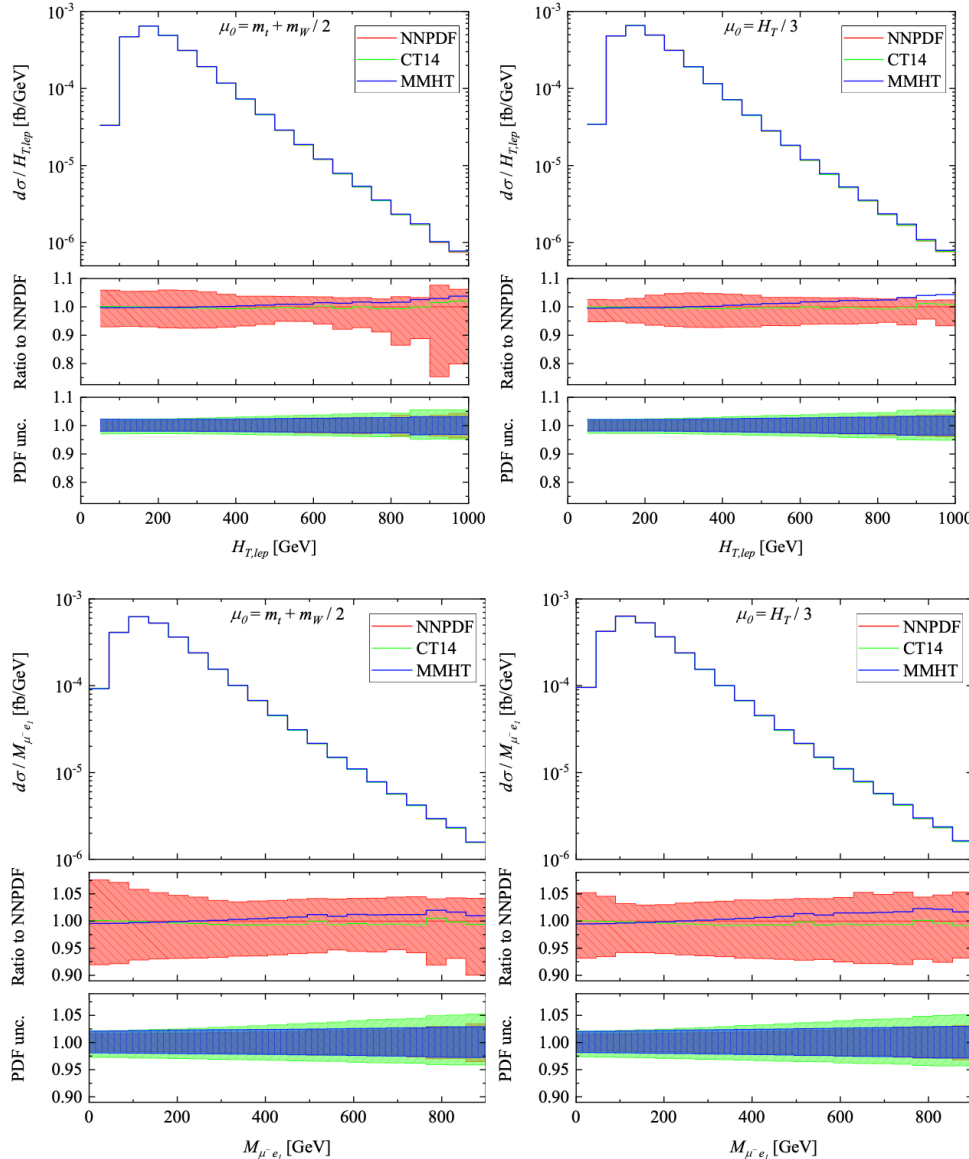
- NLO QCD $\Rightarrow$ $\pm 10\%$
- Uncertainties $\Rightarrow$ 5% – 10%
- Stabilises tails and keeps NLO uncertainty bands within LO ones

ttW with dynamical scale

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} e^+ \nu_e @ \text{LHC}_{13\text{TeV}}$$

HELAC-NLO

Bevilacqua, Bi, Hartanto, Kraus,
Worek '20



- PDF uncertainties $\Rightarrow$ 5%
- Negligible when contrasted with scale dependence
- Differences between results for various PDF sets are similar in size to internal PDF uncertainties
- For dynamical scale choice PDF uncertainties and scale dependence can be similar in high p_T regions

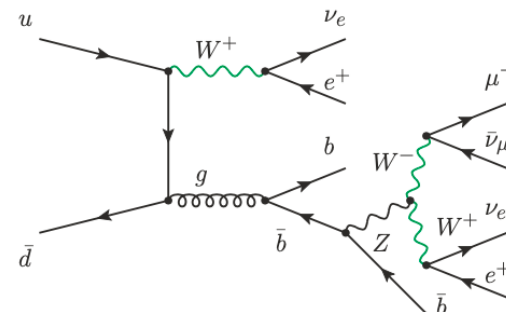
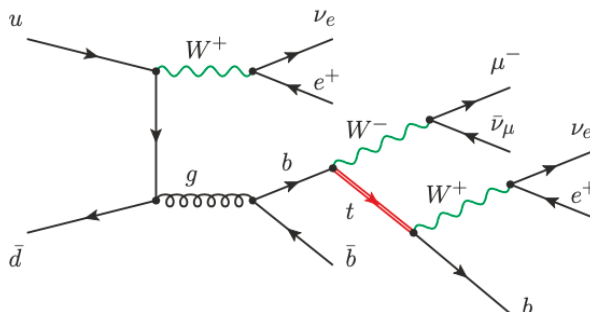
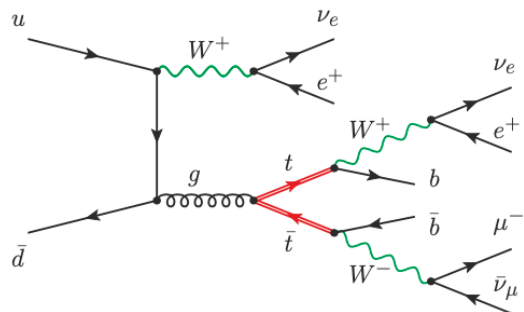
ttW with dynamical & fixed scale

HELAC-NLO

Bevilacqua, Bi, Hartanto, Kraus, Worek '20

MODELLING APPROACH	σ^{LO} [ab]	σ^{NLO} [ab]
full off-shell ($\mu_0 = m_t + m_W/2$)	$106.9^{+27.7 (26\%)}_{-20.5 (19\%)}$	$123.2^{+6.3 (5\%)}_{-8.7 (7\%)}$
full off-shell ($\mu_0 = H_T/3$)	$115.1^{+30.5 (26\%)}_{-22.5 (20\%)}$	$124.4^{+4.3 (3\%)}_{-7.7 (6\%)}$
NWA ($\mu_0 = m_t + m_W/2$)	$106.4^{+27.5 (26\%)}_{-20.3 (19\%)}$	$123.0^{+6.3 (5\%)}_{-8.7 (7\%)}$
NWA ($\mu_0 = H_T/3$)	$115.1^{+30.4 (26\%)}_{-22.4 (19\%)}$	$124.2^{+4.1 (3\%)}_{-7.7 (6\%)}$
NWA _{LOdecay} ($\mu_0 = m_t + m_W/2$)		$127.0^{+14.2 (11\%)}_{-13.3 (10\%)}$
NWA _{LOdecay} ($\mu_0 = H_T/3$)		$130.7^{+13.6 (10\%)}_{-13.2 (10\%)}$

Results for various approaches for modelling of top quark production and decays



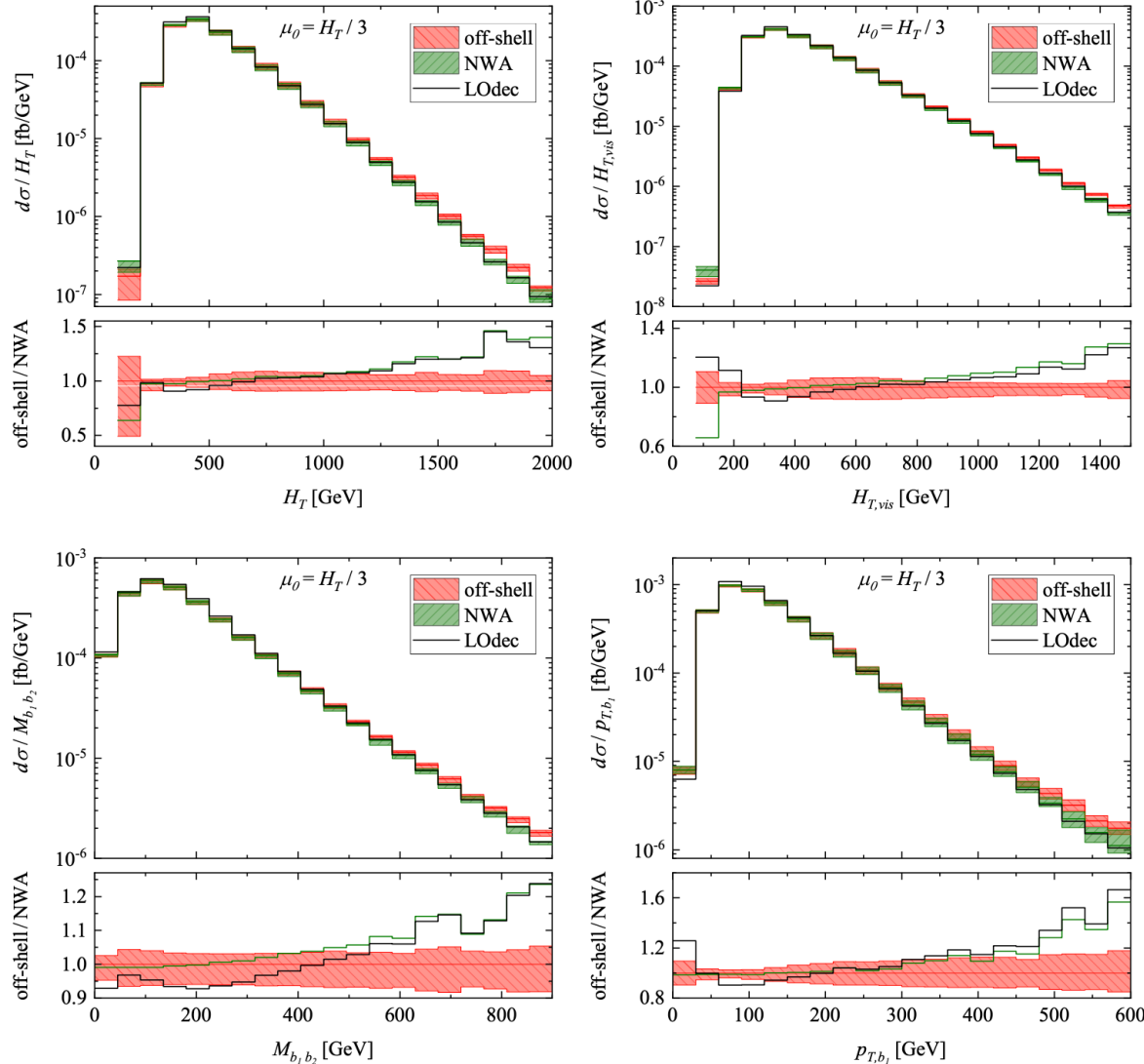
- Complete top-quark off-shell effects $\Rightarrow$ **0.2%**
- NLO QCD corrections to top-quark decays $\Rightarrow$ **3%** for fixed scale $\Rightarrow$ **5%** for dynamical scale
- Theoretical uncertainties are similar for off-shell case and NWA $\Rightarrow$ **6% – 7%**
- For NWA_{LOdecay} $\Rightarrow$ Rise up to **10% – 11%**

ttW with dynamical scale

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} e^+ \nu_e @ \text{LHC}_{13\text{TeV}}$$

HELAC-NLO

Bevilacqua, Bi, Hartanto, Kraus,
Worek '20



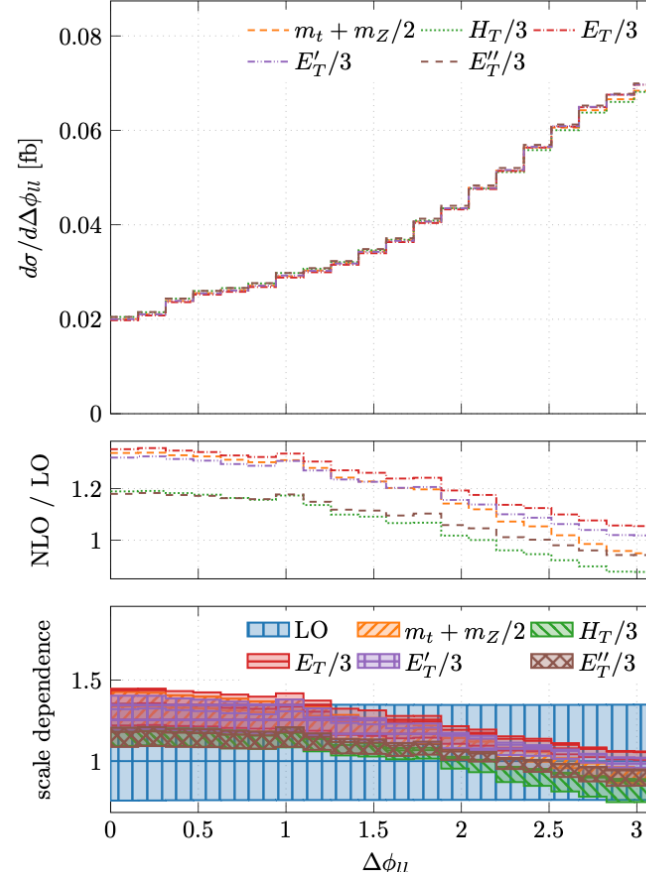
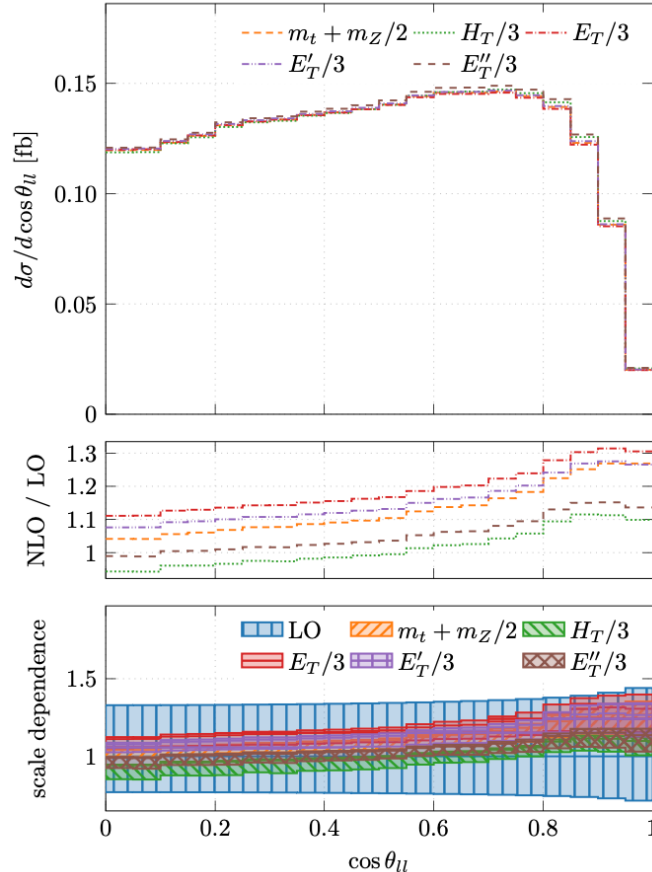
- Top-quark off-shell effects **30% – 70%**
- Large discrepancies between full NWA description & $\text{NWA}_{\text{LOdecay}}$
- Differences also in regions currently scrutinised by ATLAS & CMS experiments

ttZ ($Z \rightarrow \nu\nu$) with dynamical scale

HELAC-NLO

- Searches of new physics $\Rightarrow tt + p_T^{miss}$
- New physics observables $\Rightarrow p_T^{miss}, \cos\ell\ell, \Delta\phi\ell\ell, \Delta y\ell\ell, H_T, E_T$

$e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} \bar{\nu}_\tau \nu_\tau @ \text{LHC}_{13\text{TeV}}$



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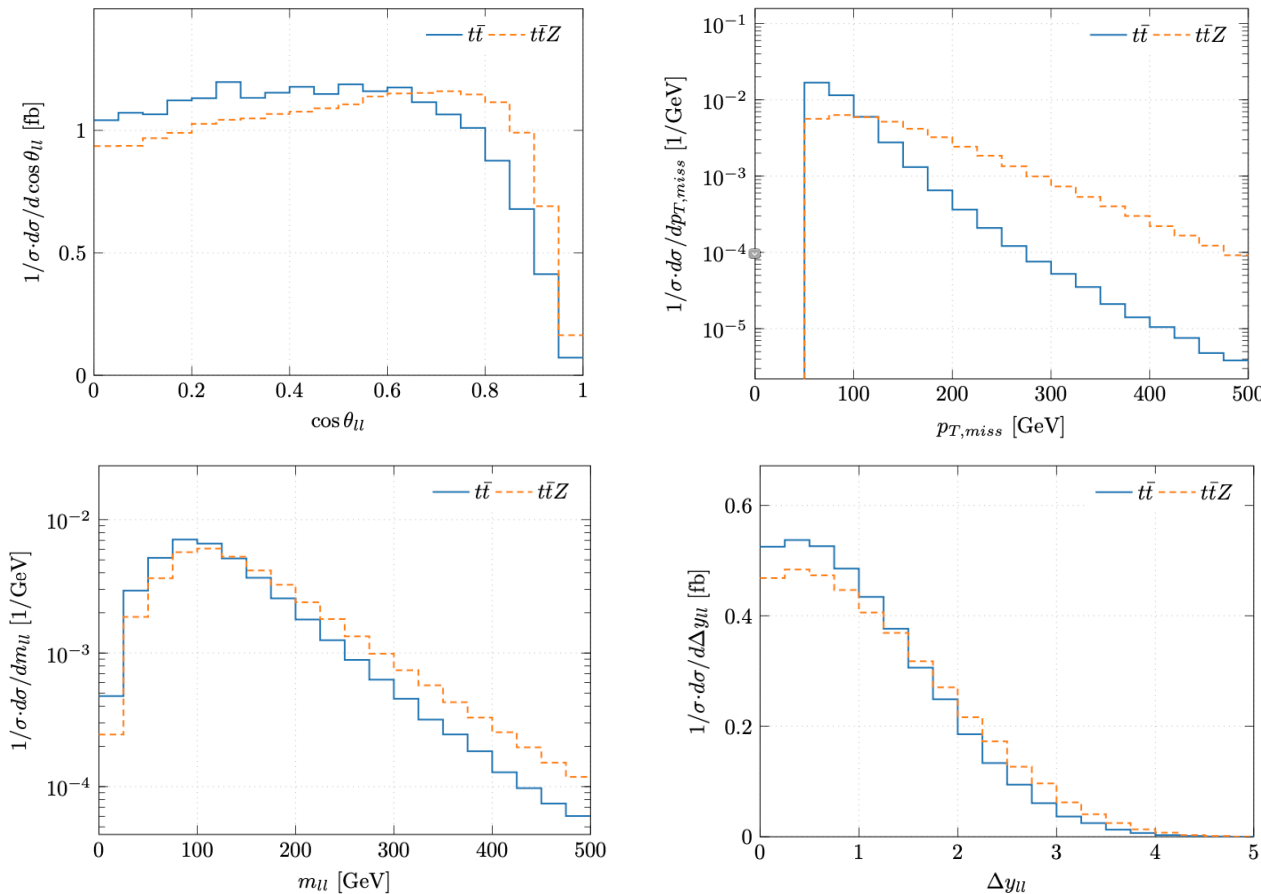
- Uncertainties reduced when going from LO to NLO
- Substantial non-flat K-factors

ttZ ($Z \rightarrow \nu\nu$) with dynamical scale

HELAC-NLO

- Searches of new physics $\Rightarrow t\bar{t} + p_T^{miss}$
- New physics observables $\Rightarrow p_T^{miss}, \cos\ell\ell, \Delta\phi\ell\ell, \Delta y\ell\ell, H_T, E_T$

$e^+\nu_e \mu^-\bar{\nu}_\mu b\bar{b}\bar{\nu}_\tau\nu_\tau @ \text{LHC}_{13\text{TeV}}$



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- Reducible and irreducible backgrounds
- $t\bar{t}$ production process does not exhibit long enough tails in p_T^{miss}
- Might impact exclusion limits

Summary

- *Proper modeling of top quark production & decay essential already now in presence of inclusive cuts:*
- NNLO QCD corrections to $t\bar{t}$ in NWA (di-lepton decay channel)
- NLO QCD corrections to $t\bar{t}V$ (top quarks in di-lepton channel)
 - Corrections to production & decays $\Rightarrow$ NLO $t\bar{t}$ spin correlations
 - Possibility of using kinematic-dependent μ_R & μ_F scales
 - Complete off-shell effects for top quarks
- *Even more important for:*
 - Exclusive cuts & High luminosity measurements
 - New Physics searches & Might impact exclusion limits
 - SM parameter extraction
- Top quarks play important role in virtually every LHC analysis $\Rightarrow$ *SM & BSM*
- *Lots of data, sophisticated analyses, precision measurements $\Rightarrow$ Should be compared to state-of-the-art theoretical predictions*
- Our full off-shell results for $t\bar{t}$, $t\bar{t}l$, $t\bar{t}Z$, $t\bar{t}W$
 - Stored $\Rightarrow$ *Ntuples Files* $\Rightarrow$ *Les Houches & ROOT Files*



Backup Slides

Various Phase-space Regions

$e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ @ LHC₁₃TeV

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- $n = 15 \rightarrow$ boundaries outside which effects of Γ_t in BW propagator $< 1\%$
- DR region is set to for $m_t = 173.2 \text{ GeV}$

$M(t) \in (152.9, 193.5) \text{ GeV}$	$M(\bar{t}) \in (152.9, 193.5) \text{ GeV}$
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- Contributions at the integrated cross section level for these 3 regions

$\sigma_{\text{DR}}^{\text{NLO}} = 6.57 \text{ fb},$	$\sigma_{\text{SR}}^{\text{NLO}} = 0.91 \text{ fb},$	$\sigma_{\text{NR}}^{\text{NLO}} = 0.02 \text{ fb}$
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- DR contribution to full $\sigma_{t\bar{t}\gamma} \rightarrow 88\% \rightarrow$ SR comprises $12\% \rightarrow$ NR only 0.5%
- Should we instead use $n = 5$

$$\sigma_{\text{DR}}^{\text{NLO}} = 4.82 \text{ fb}, \sigma_{\text{SR}}^{\text{NLO}} = 2.50 \text{ fb} \text{ and } \sigma_{\text{NR}}^{\text{NLO}} = 0.18 \text{ fb.}$$

- DR = 64%, SR = 33%, NR = 3%