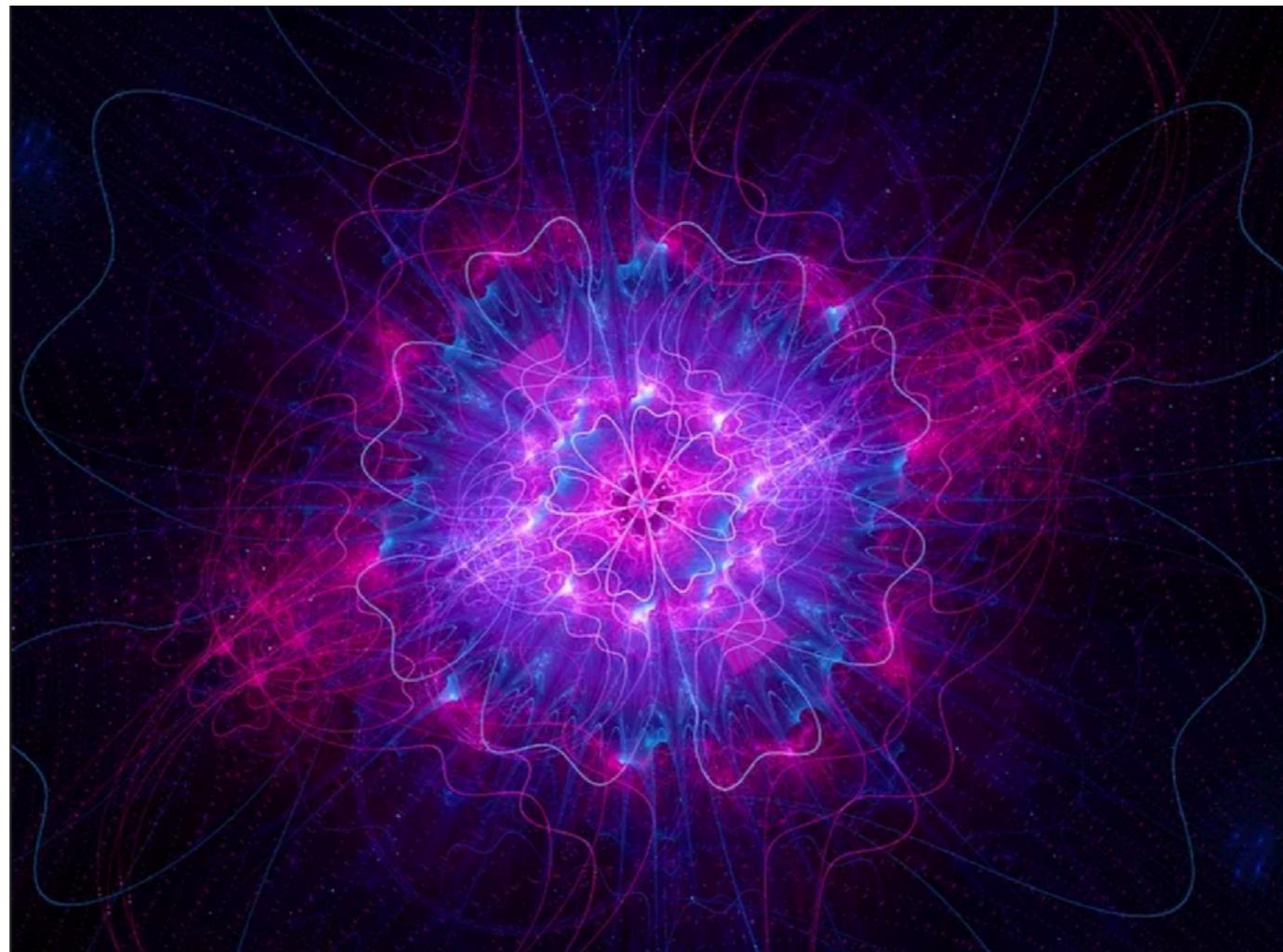


# Higgs physics: recent developments

***Gudrun Heinrich***

*Karlsruhe Institute of Technology*



an artist's view of  
the Higgs boson  
Sakkmesterke  
Shutterstock.com

CRC Annual Meeting, 6.10.2020

# Higgs-related questions

- Higgs properties (mass, CP, width)
- couplings to vector bosons and fermions → flavour physics  
neutrino masses
- Higgs potential (self-couplings)
- Higgs and the Universe  
(meta-stability, baryogenesis, portal to dark matter, ...)
- the only elementary scalar? compositeness?

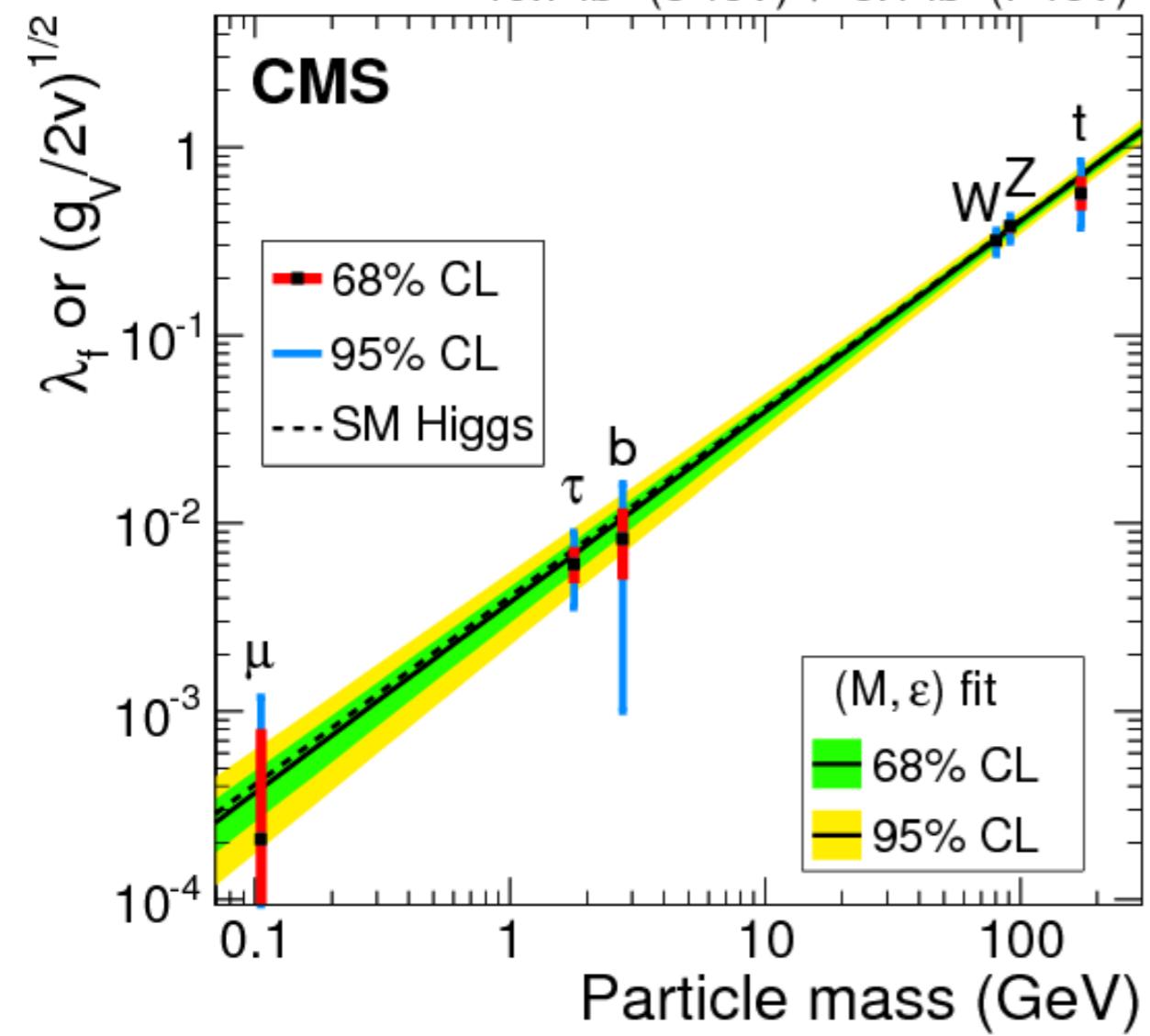
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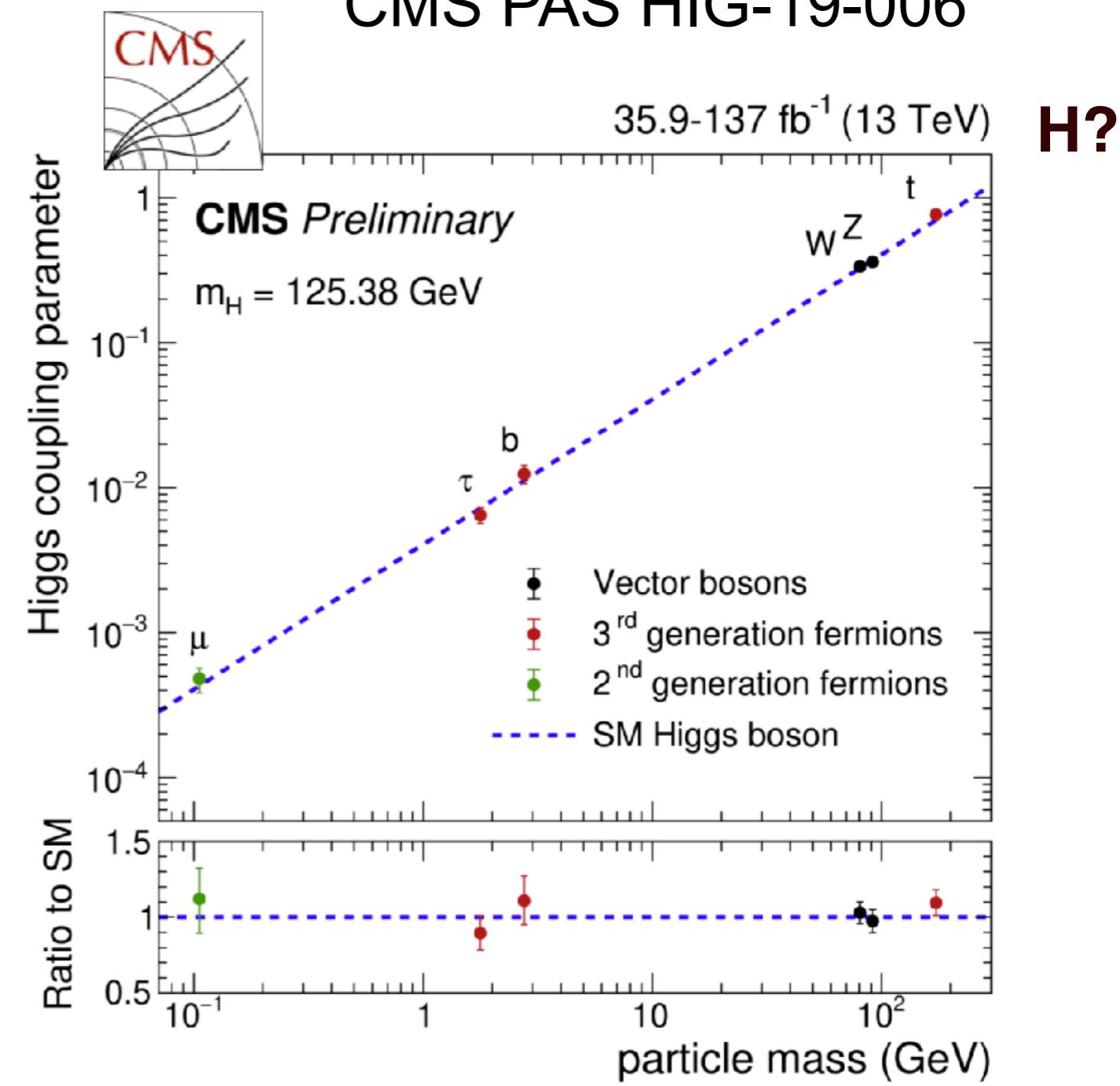
The Higgs sector might be a window to physics at higher scales

# Higgs couplings

Run I



CMS PAS HIG-19-006



H?

# How do we address these questions?

- precision measurements
- test specific BSM models
- EFT parametrisations of new physics effects

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d=6}^{\infty} \frac{c_i}{\Lambda^{d-4}} \mathcal{O}_i$$

$$\Rightarrow (\sigma \times BR) = (\sigma \times BR)_{\text{SM}} (1 + \Delta)$$

for typical energy scale  $E$  of measurement:  $\Delta \sim \left(\frac{E}{\Lambda}\right)^2$

# The SM as an effective field theory

$$\Delta \sim \left( \frac{E}{\Lambda} \right)^2$$

example Higgs production: typical energy scale  $E \sim v = 0.25 \text{ TeV}$

$$\Rightarrow \Delta \sim (0.25)^2 \left( \frac{\text{TeV}}{\Lambda} \right)^2 \sim 0.06 \left( \frac{\text{TeV}}{\Lambda} \right)^2$$

$\Rightarrow$  to generate  $\gtrsim 1\%$  deviations need  $\Lambda \lesssim 2.5 \text{ TeV}$

boosted Higgs, tails of distributions:  $E \sim 1 \text{ TeV}$

$\Rightarrow$  with  $\Lambda = 2.5 \text{ TeV}$  we achieve  $\Delta = 1/(2.5)^2 \simeq 16\%$

# The SM as an effective field theory

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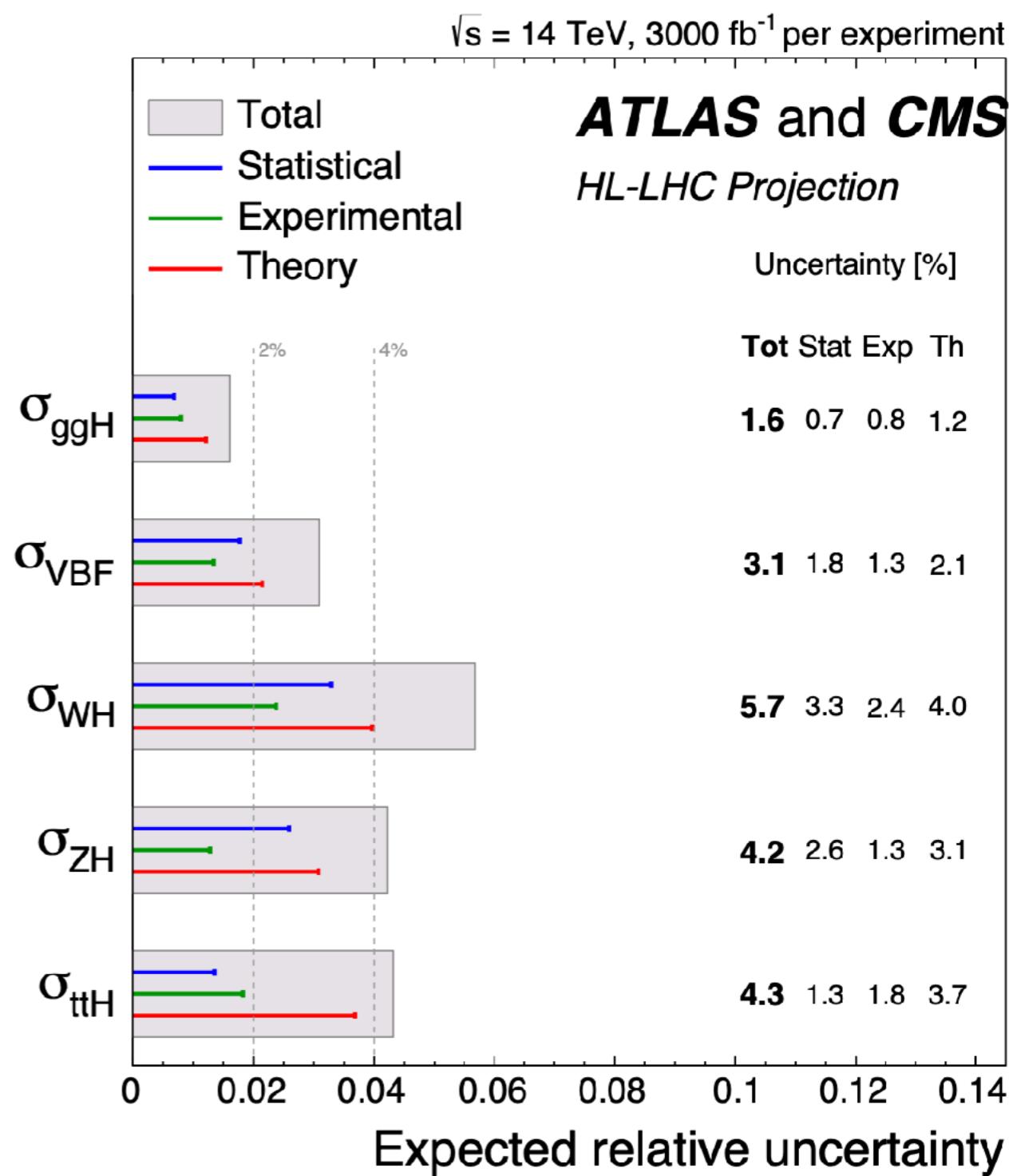
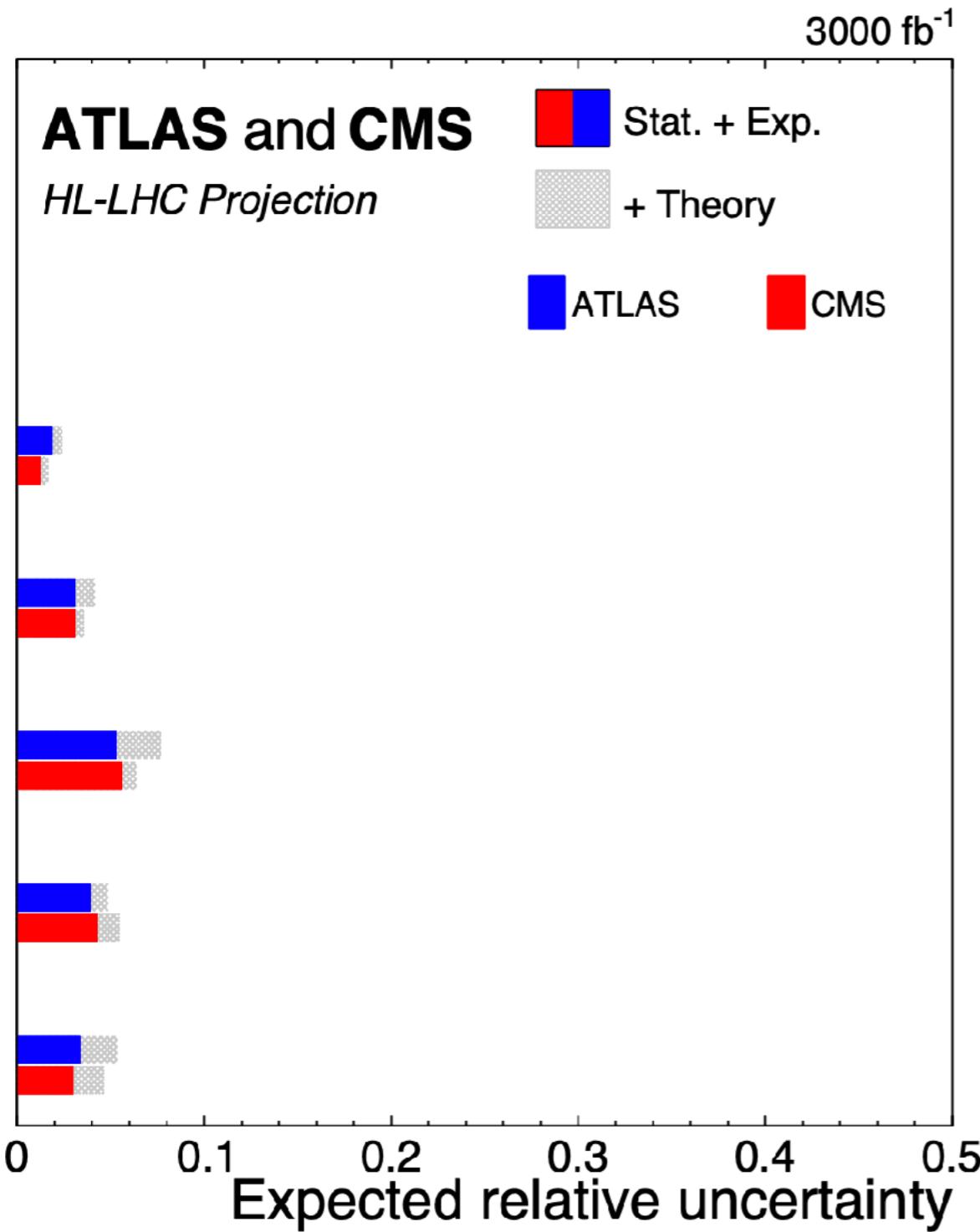
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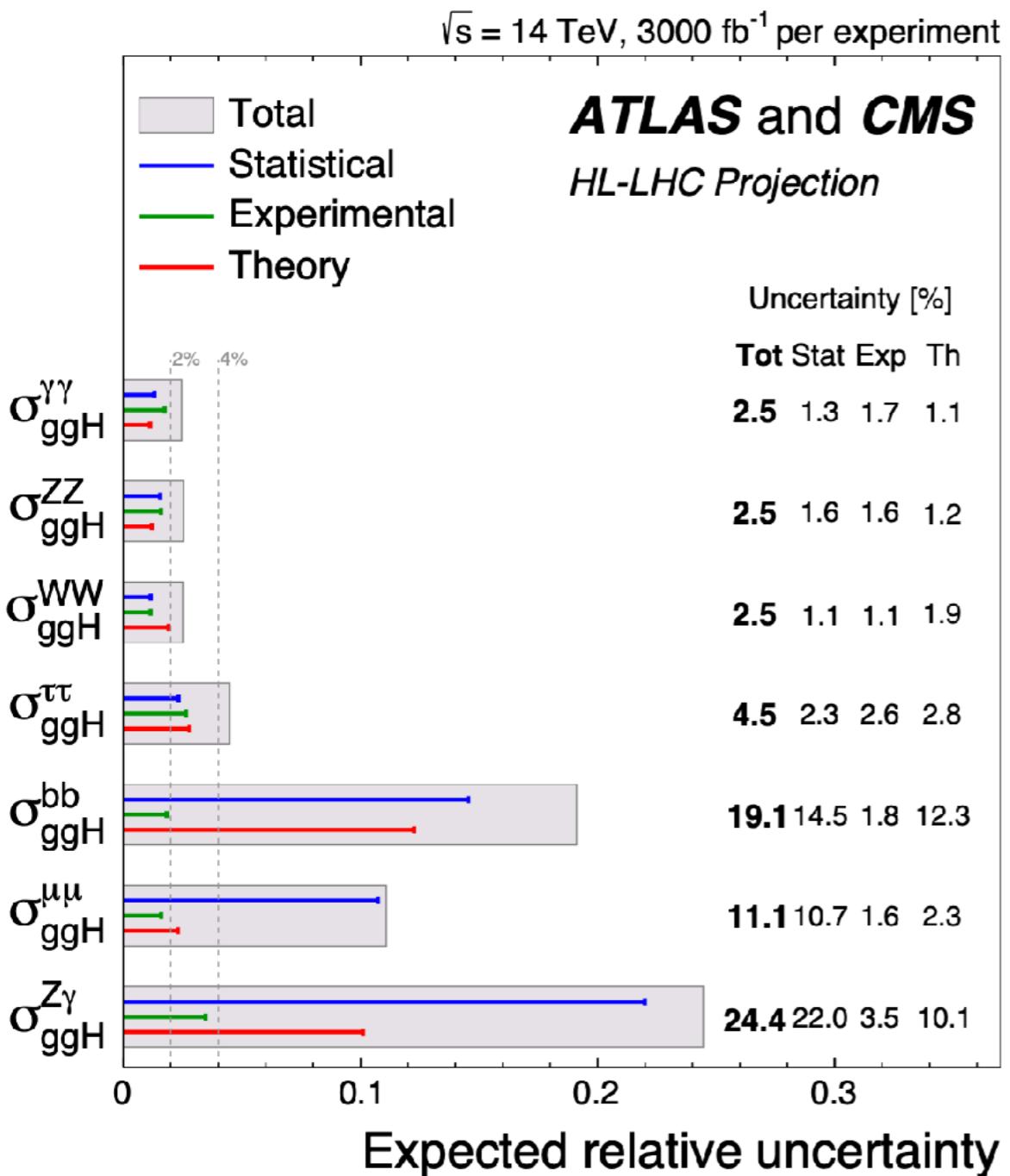
$\Rightarrow$  off-shell measurements, tails of distributions very important!

# precision

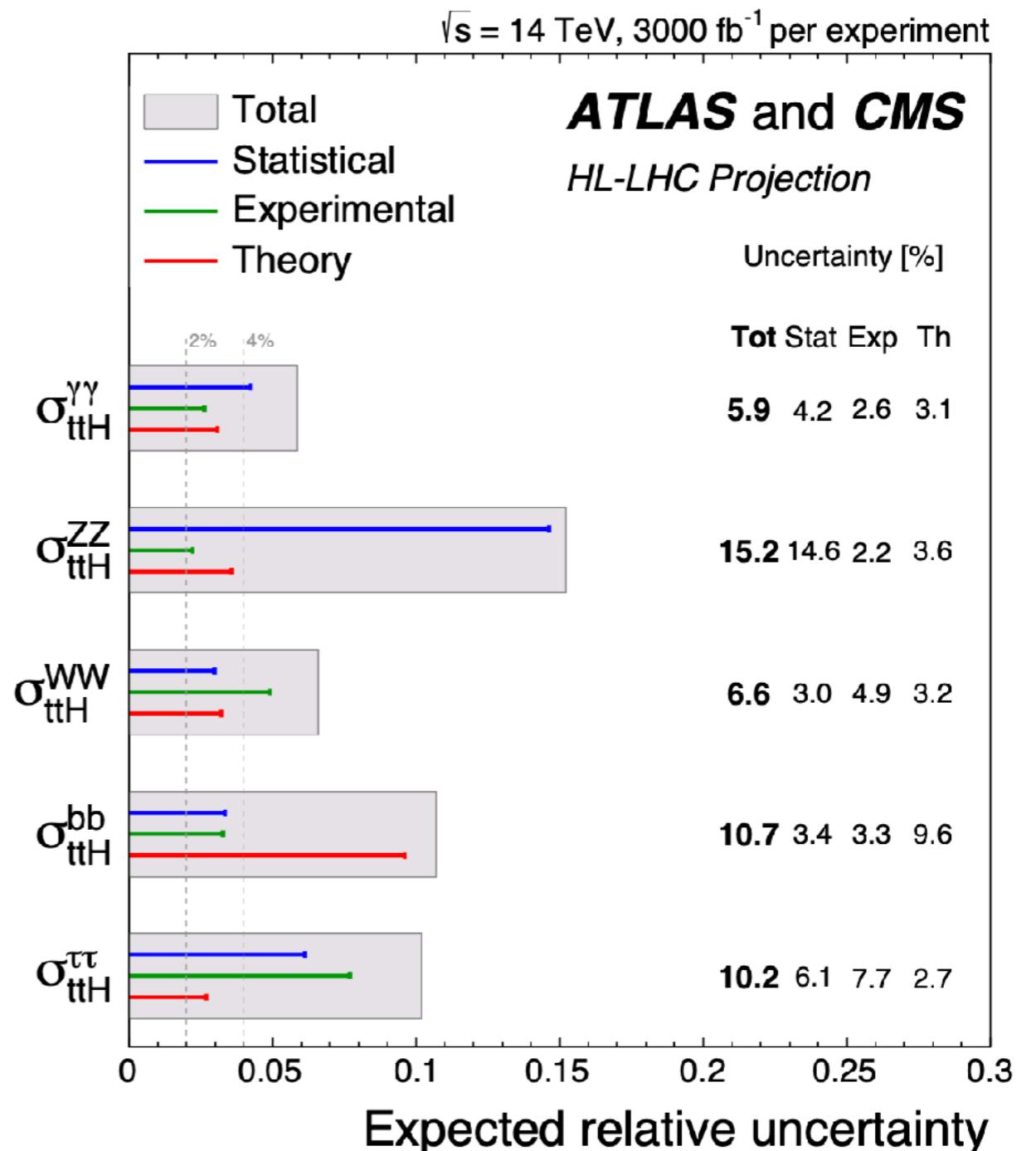


# projected uncertainties

## gluon fusion



## tH



# fixed order precision frontier

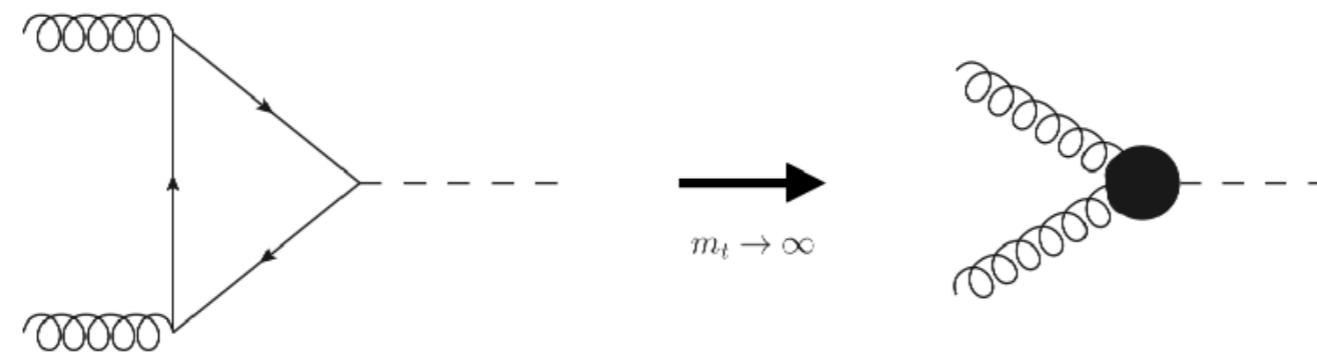
**N3LO** available for:

gluon fusion Higgs, bbH, Drell-Yan, VBF H, VBF HH, gluon fusion HH

	Drell-Yan	gluon fusion Higgs
LO	1970	1978
NLO	1978-80	1991 (HTL) 1995 (full mt)
NNLO	1991	2002 (HTL) 2009-2020 (mass effects)
N3LO	2020 Duhr, Dulat, Mistlberger	2015 (HTL, threshold exp.) Anastasiou, Duhr, Dulat, Herzog, Mistlberger 2018 (HTL) Mistlberger 2020 Das, Moch, Vogt partial N4LO

# aside: heavy top limit

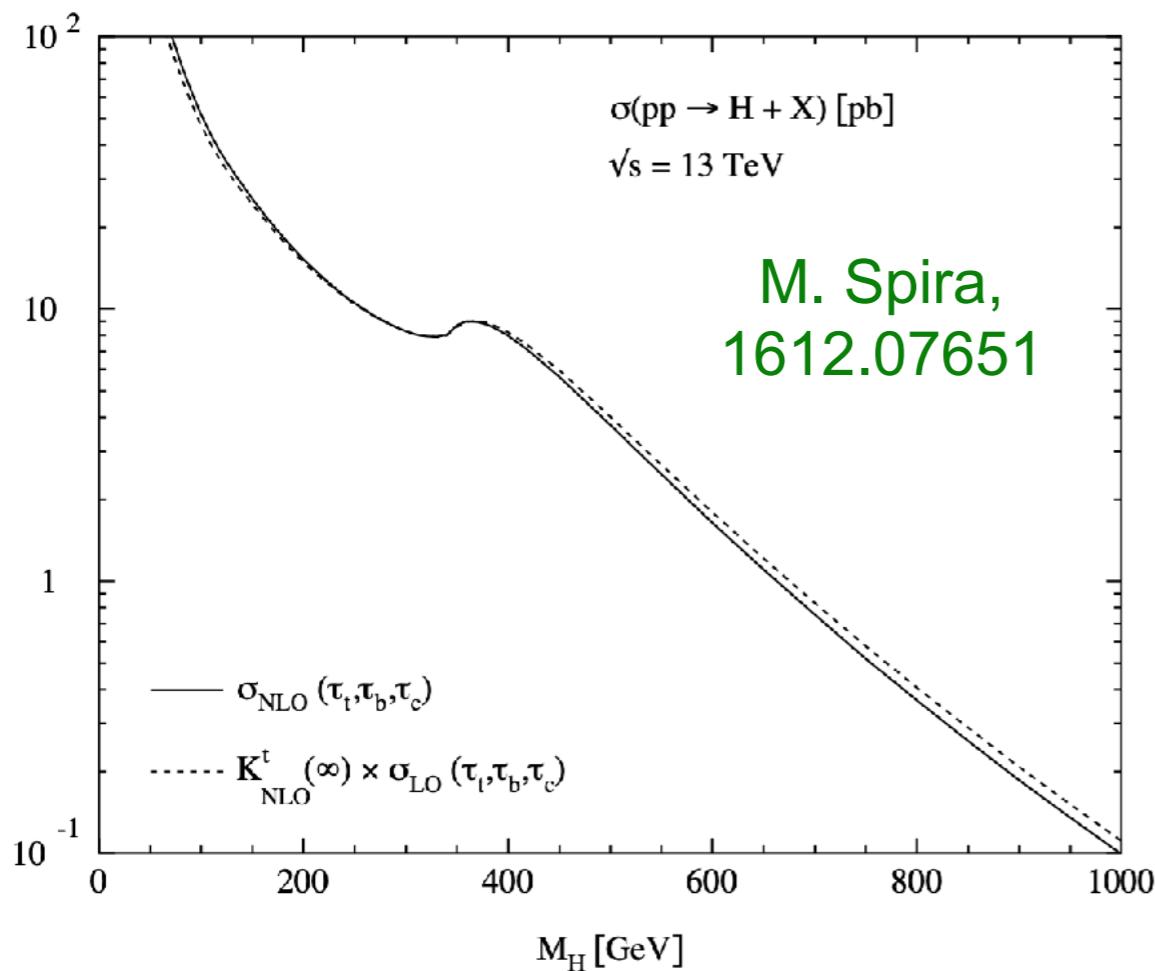
- Higgs production in gluon fusion:  
leading order already contains one loop  
(same for HH, HJ, HZ, ... in gluon fusion)
- many calculations of high perturbative order use “heavy top limit” (HTL)



- good approximation for inclusive Higgs production if rescaled with full Born
- not justified if top loops can be resolved (e.g. high energy tails of distributions)  
(in fact only justified below threshold,  $E \lesssim 2m_t$ )  
example HH production: only valid for  $250 \text{ GeV} \leq m_{HH} \lesssim 350 \text{ GeV}$

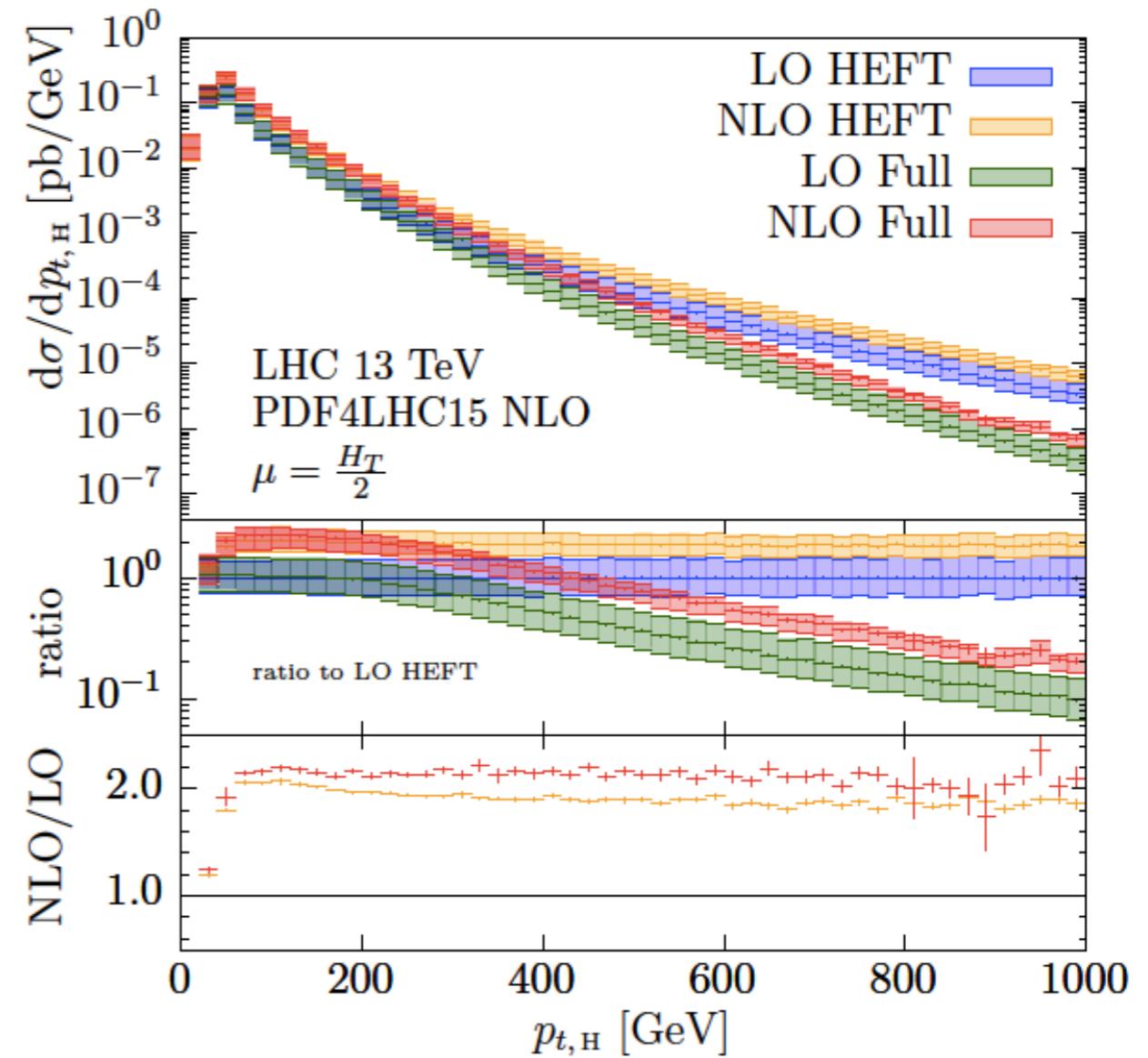
# heavy top limit

inclusive Higgs production



"Born-improved" NLO HTL

Higgs+jet production



Jones, Kerner, Luisoni '18

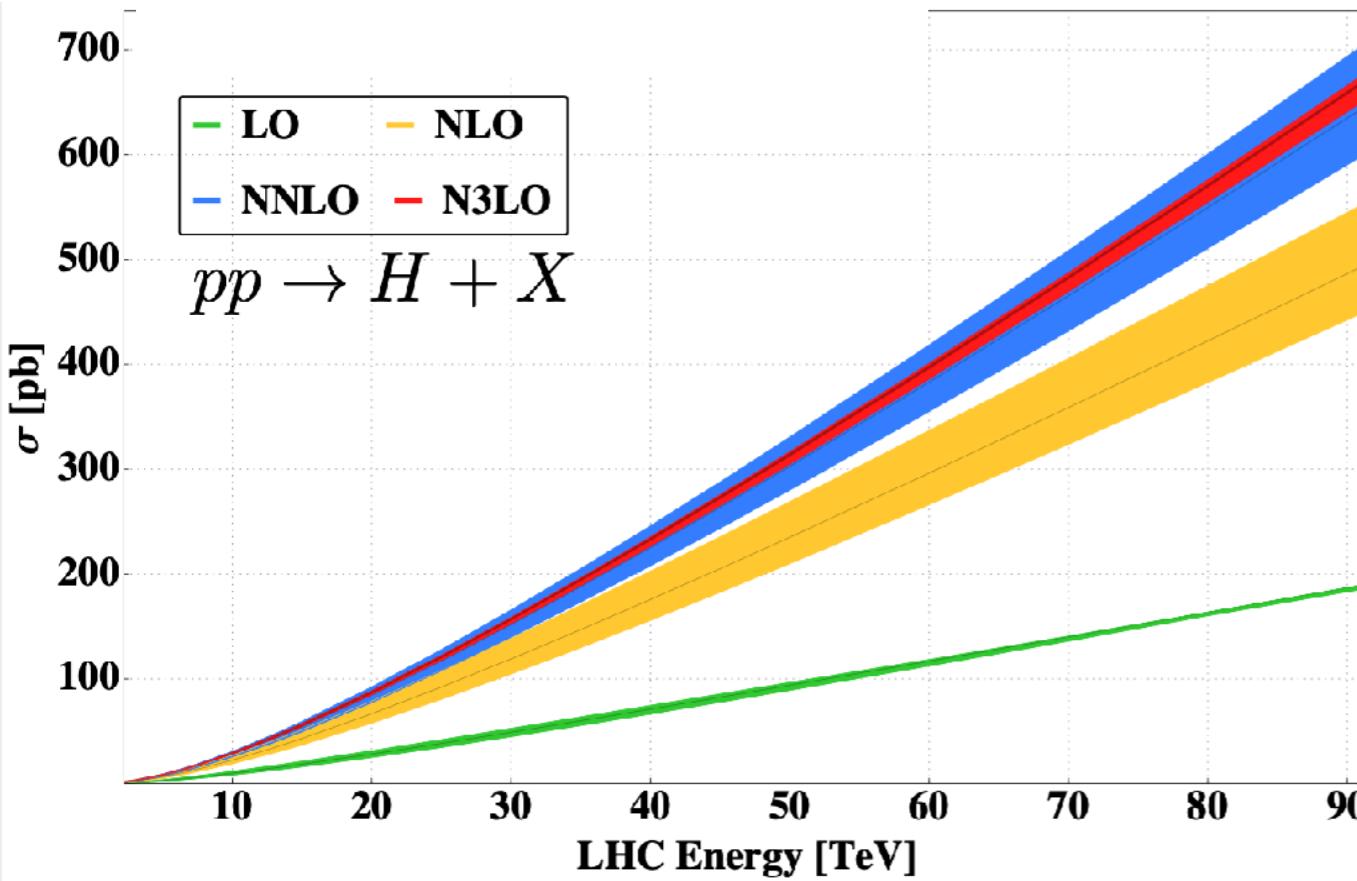
("HEFT"=HTL)

# fixed order precision frontier

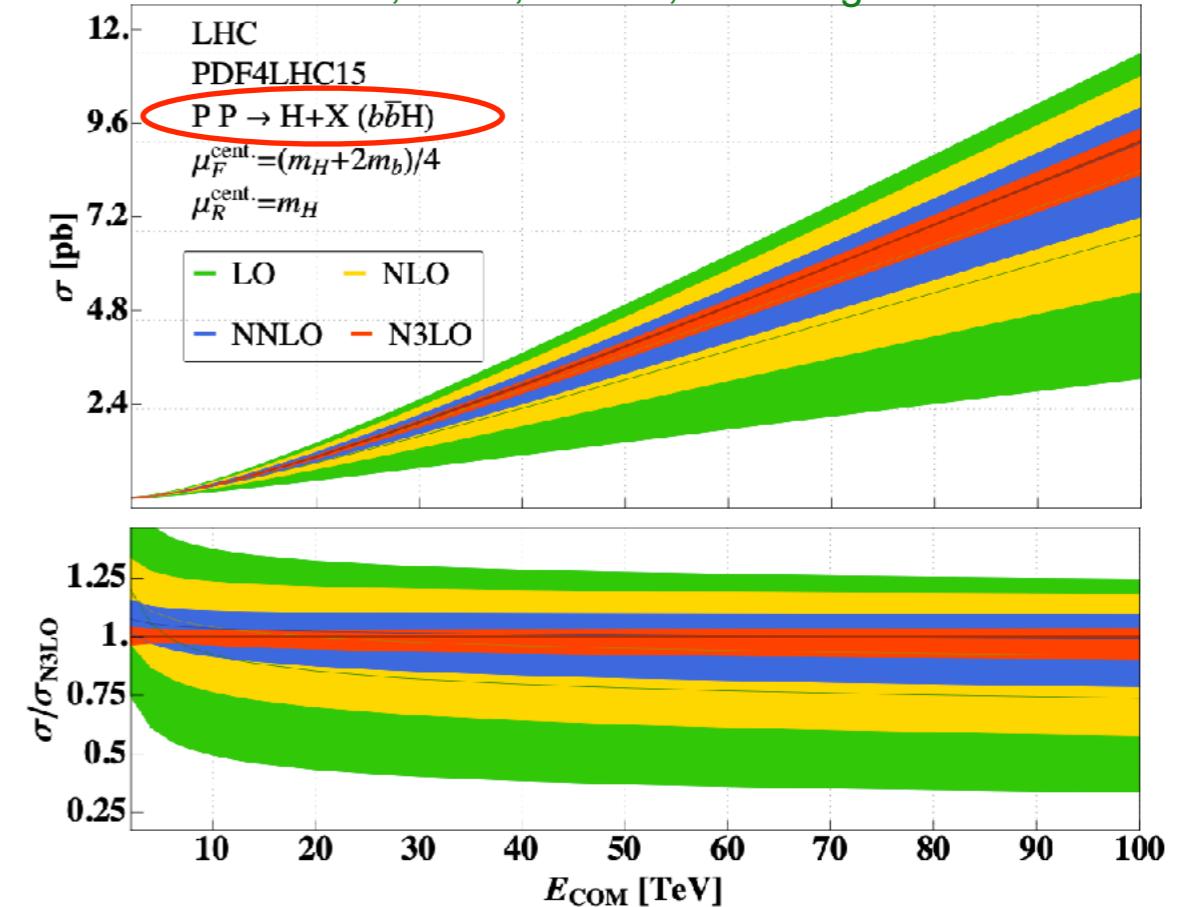
	VBF Higgs	Higgs pairs gluon fusion
LO	1979	1988
NLO	1992 (structure func.approx.) 2003 (full)	1998 (HTL) 2016 (full mt)
NNLO	2015	2013 (HTL) 2013-2020 (mass effects)
N3LO	2016 Dreyer, Karlberg (VBF HH 2018)	2019 (HTL+mass effects) Chen, Li, Shao, Wang

# precision frontier

Anastasiou, Duhr, Dulat, Herzog, Mistlberger '15



Duhr, Dulat, Hirschi, Mistlberger '20



shift of focus:

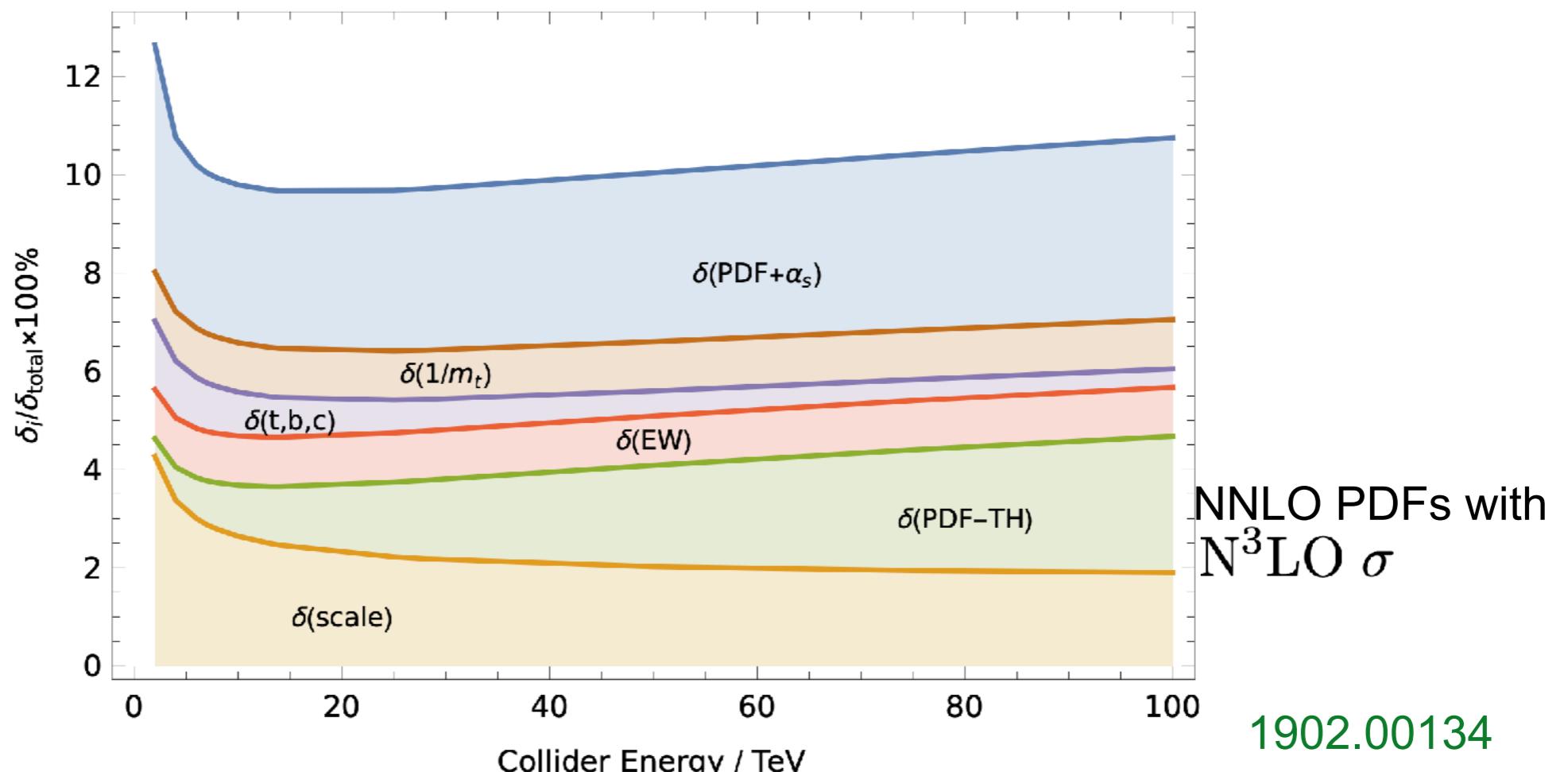
- at N3LO scale uncertainties under control, but need to address
- QCDxEW corrections
  - massive quarks at higher orders
  - PDF,  $\alpha_s$  uncertainties, non-perturbative effects
  - parton shower uncertainties

# H in gluon fusion: uncertainties

$\delta(\text{scale})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$	$\delta(\text{PDF})$	$\delta(\alpha_s)$
+0.10 pb -1.15 pb	$\pm 0.56$ pb	$\pm 0.49$ pb	$\pm 0.40$ pb	$\pm 0.49$ pb	$\pm 0.89$ pb	+1.25 pb -1.26 pb
+0.21% -2.37%	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$	$\pm 1.85\%$	+2.59% -2.62%

2009.00516

scale uncertainties no longer the dominant uncertainties



# Hbb

N3LO in 5-flavour scheme Duhr, Dulat, Hirschi, Mistlberger 2004.04752  
 matched to NLO in 4-flavour scheme ( $m_b \neq 0$ )

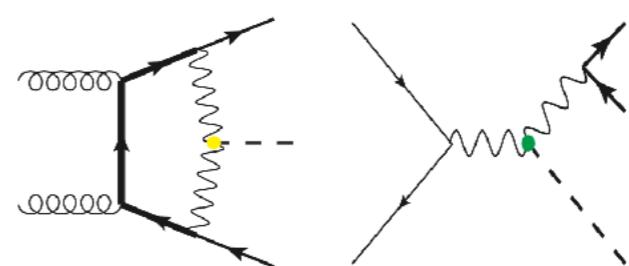
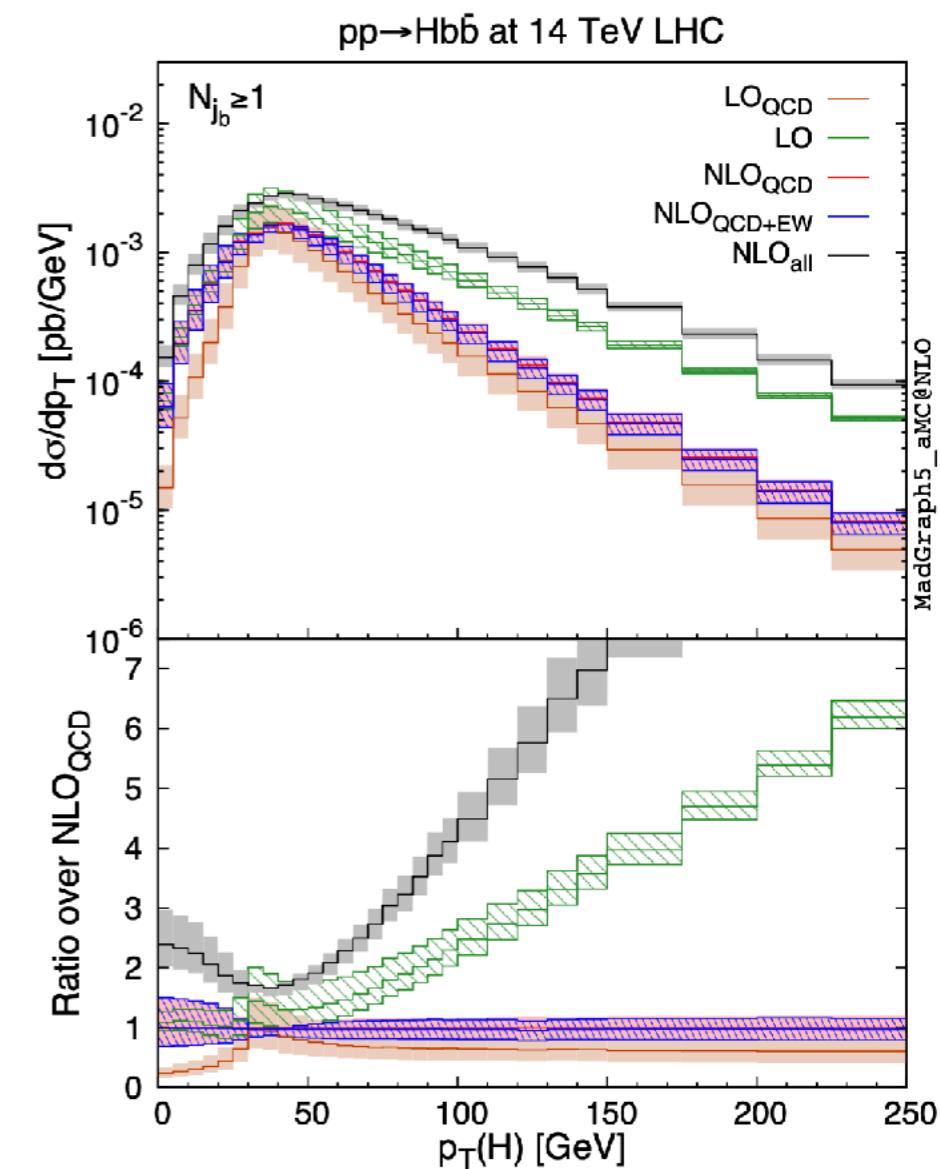
4FS	-	-	LO	NLO
5FS	LO	NLO	NNLO	$N^3LO$

$pp \rightarrow Hb\bar{b}$  as a way to directly measure  $y_b$ :

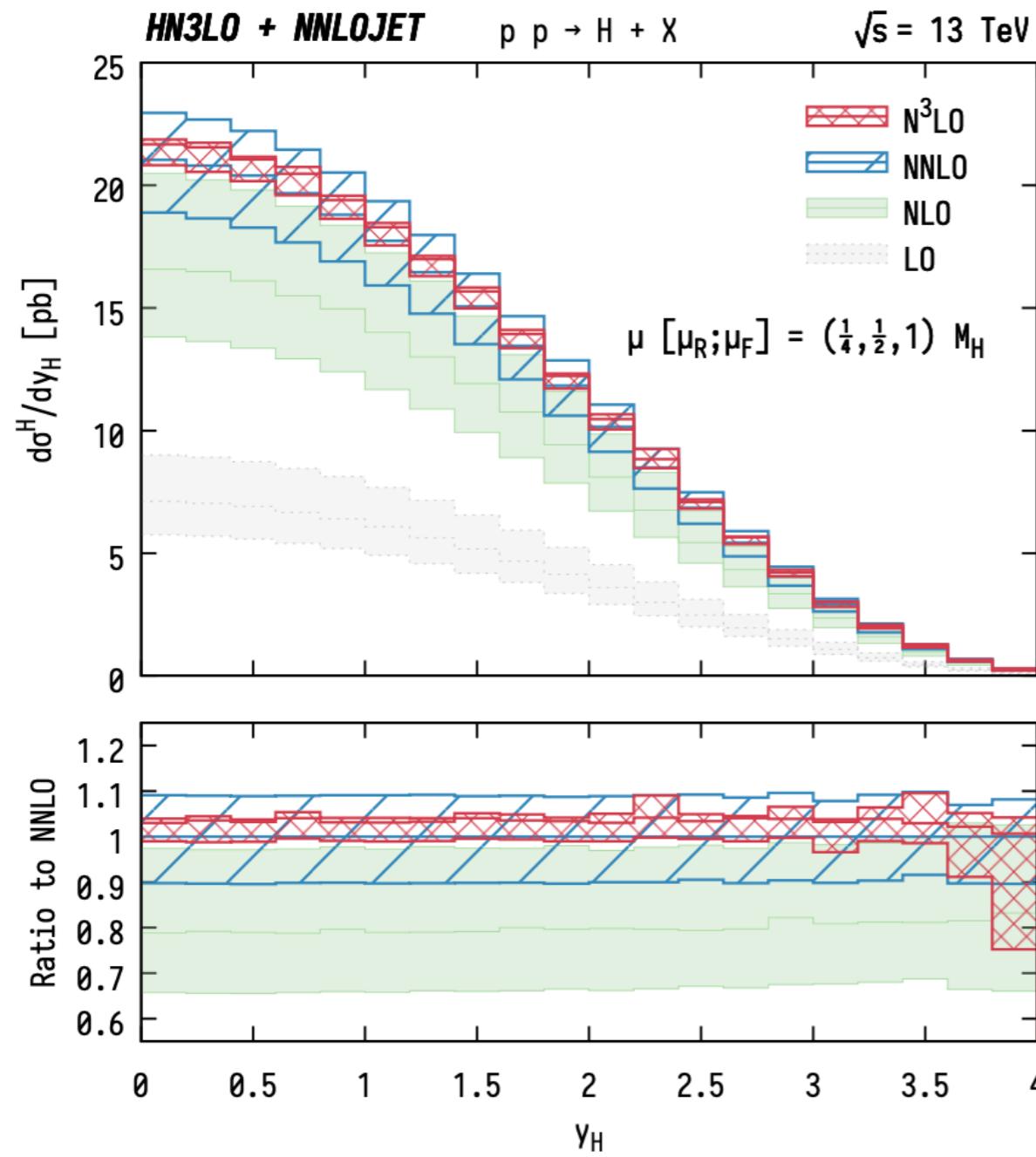
Pagani, Shao, Zaro 2005.10277

calculation of full QCD-EW NLO corrections,  
 including ZH and VBF production channels

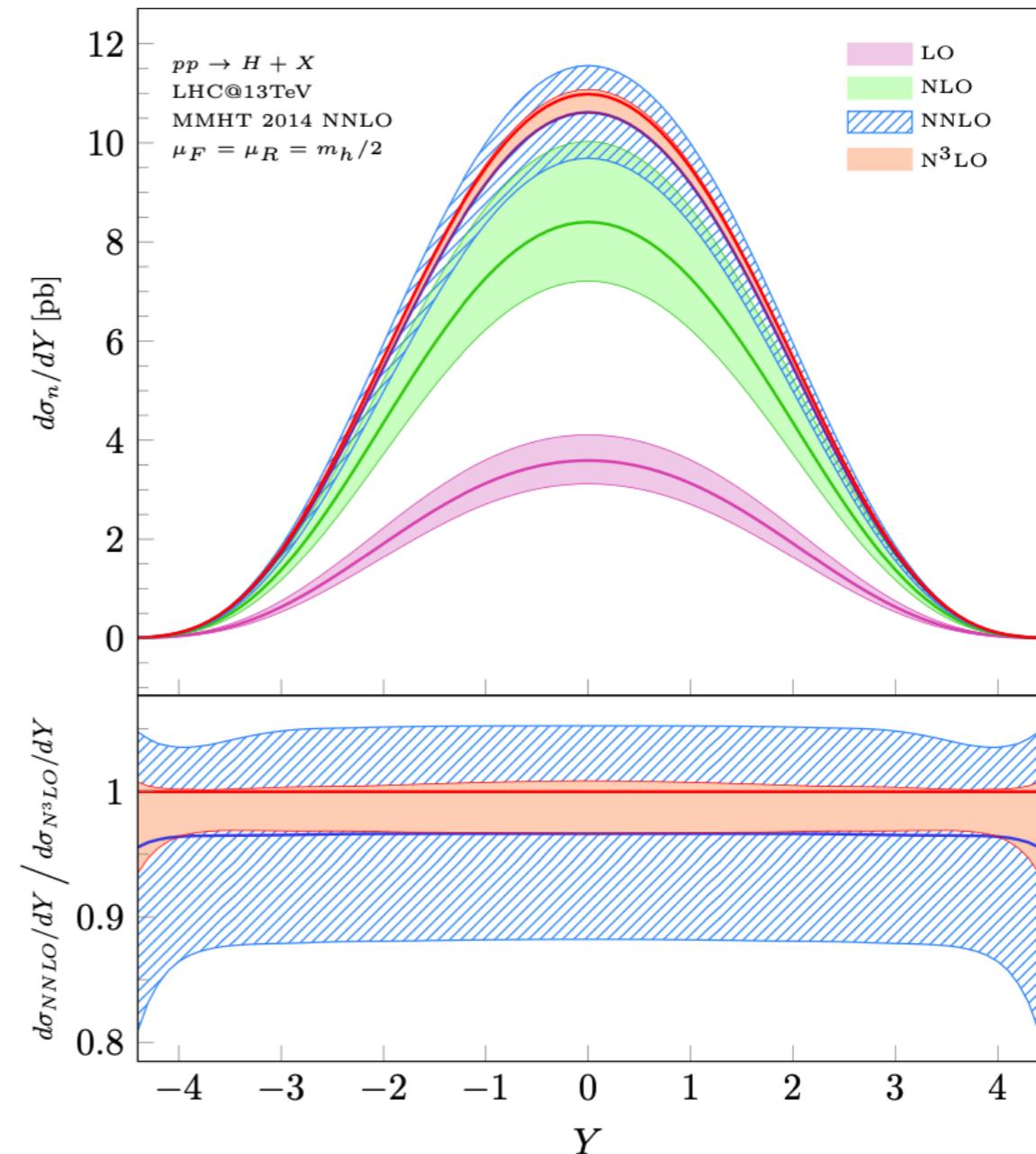
**conclusion:** overwhelming backgrounds,  
 in particular due to VBF and  
 $ZH(Z \rightarrow b\bar{b})$



# differential N3LO results



Cieri, Chen, Gehrmann, Glover, Huss  
1807.11501



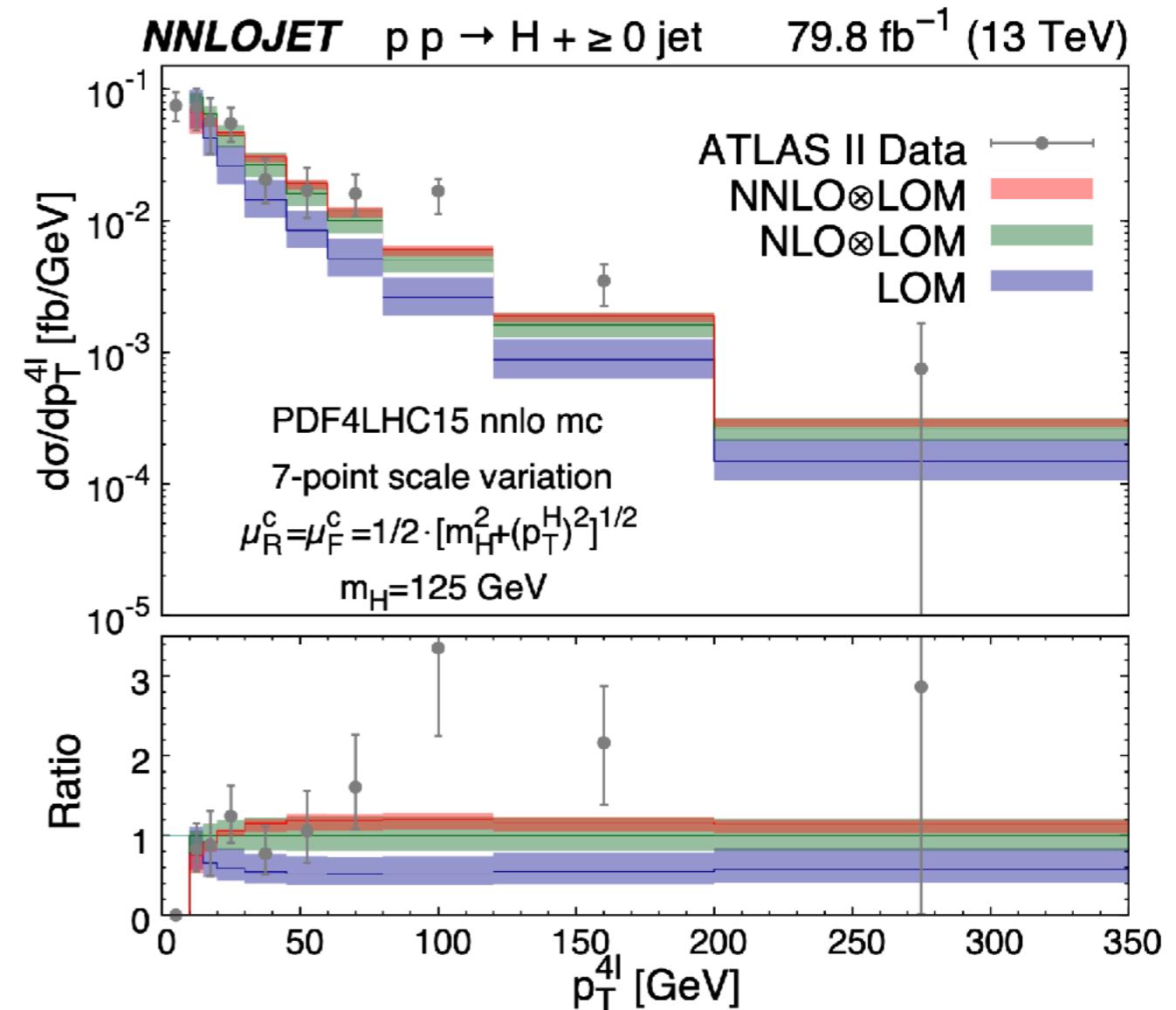
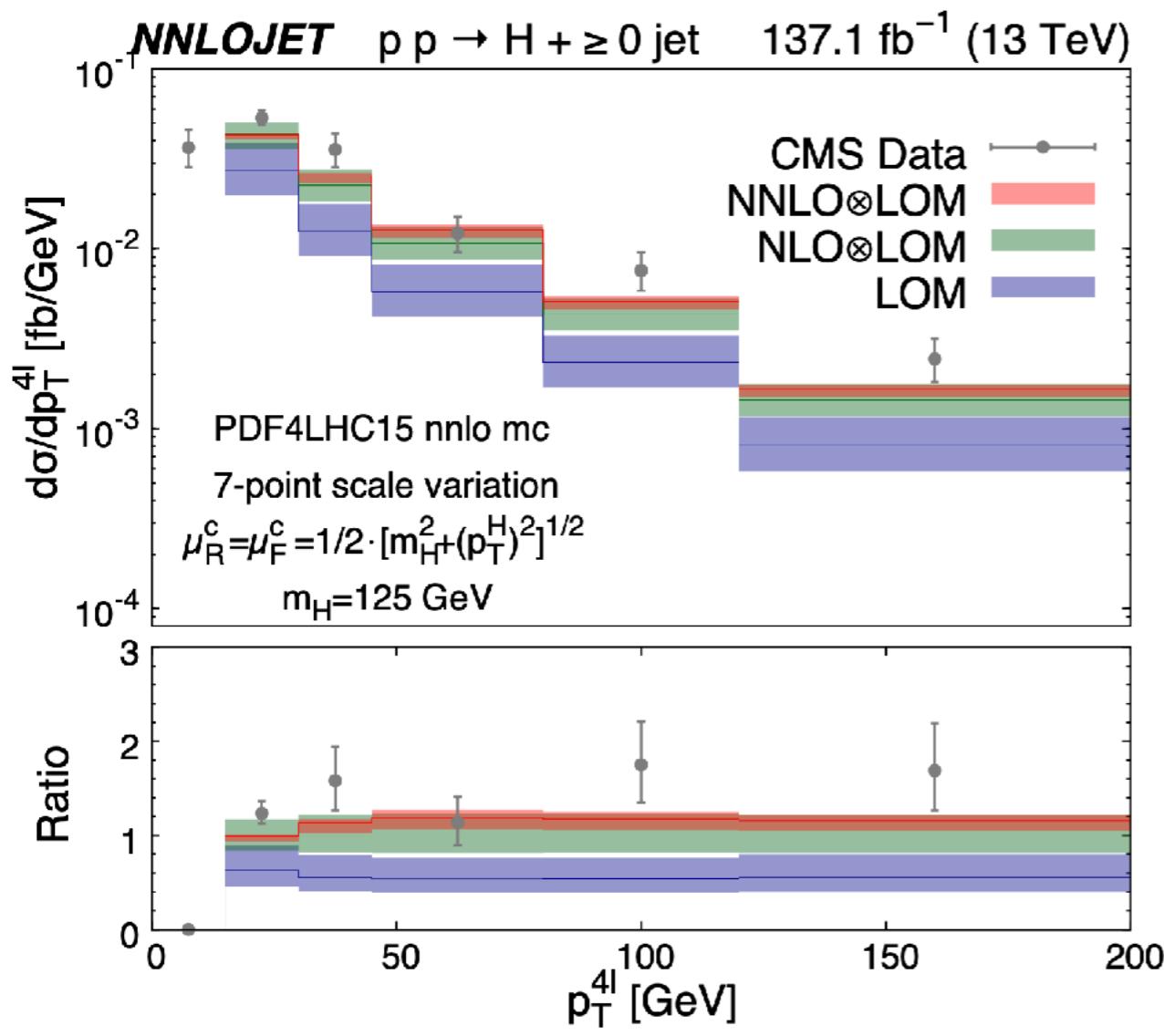
Dulat, Mistlberger, Pelloni  
1810.09462

scale uncertainties reduced by more than 50% w.r.t. NNLO

# gluon fusion H NNLO differential results

$pp \rightarrow H + \leq 1 j \rightarrow 4l + \leq 1 j$

Chen, Gehrmann, Glover, Huss  
1905.13738

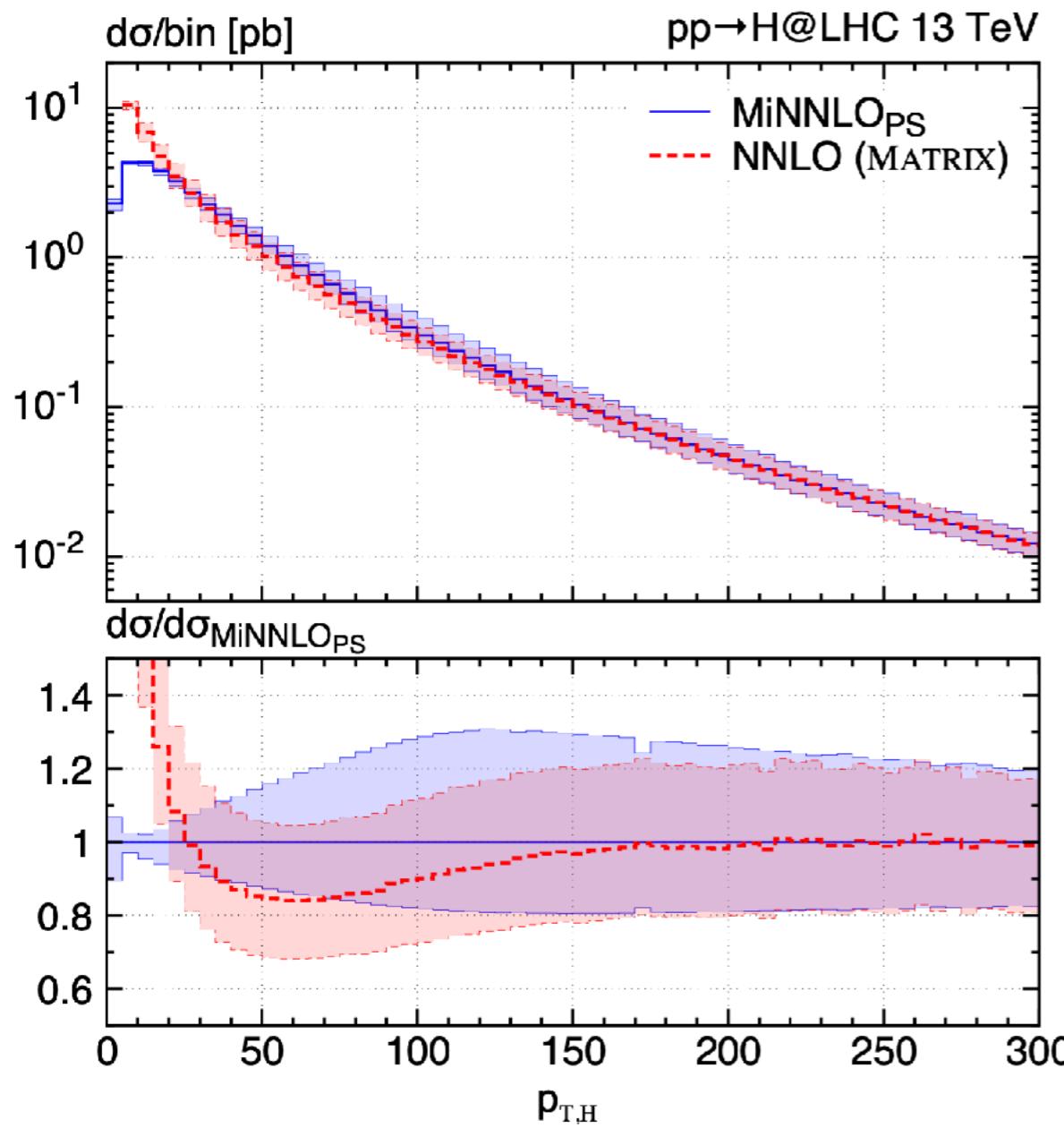


study of perturbative stability of lepton acceptance cuts

# beyond fixed order

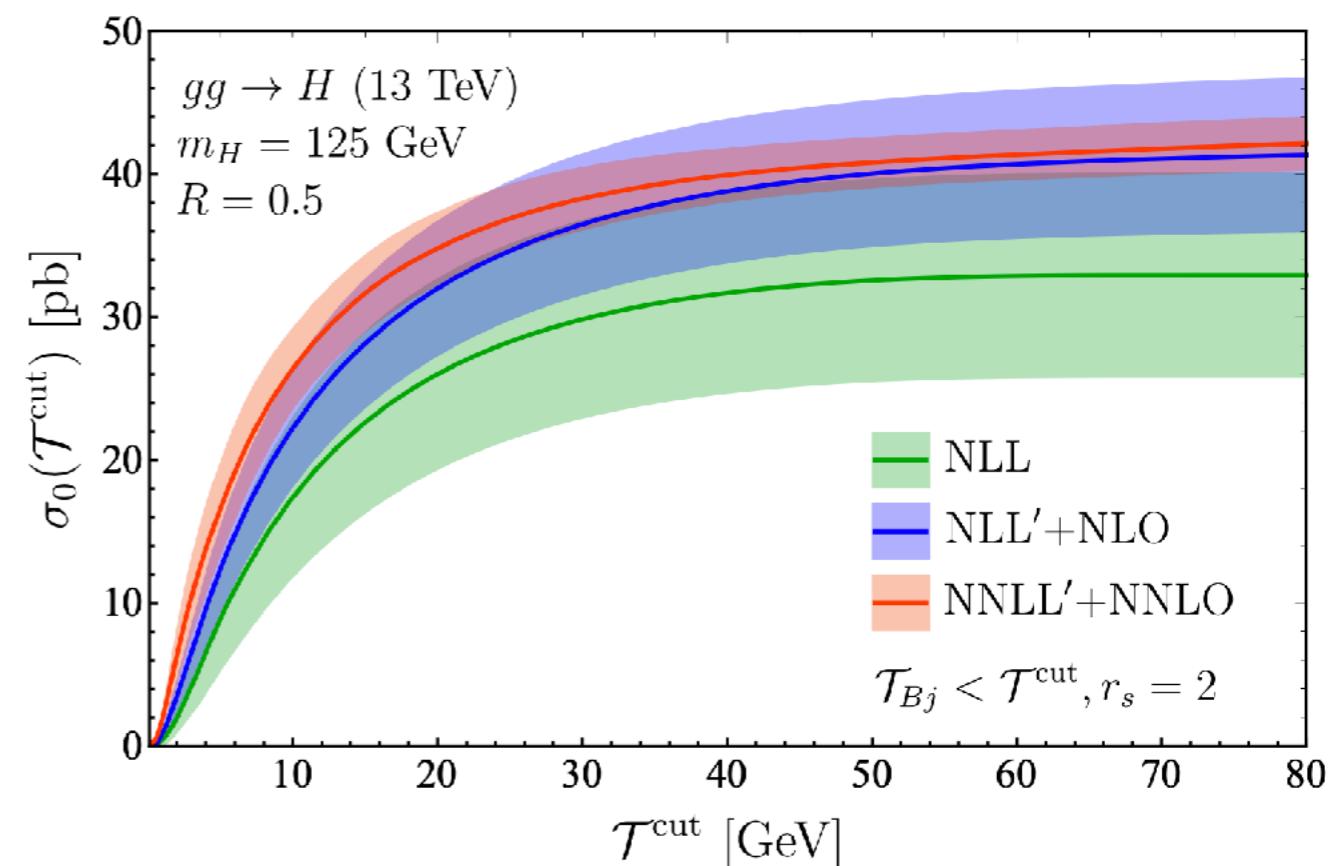
NNLO+PS

Monni, Re, Wiesemann  
2006.04133



Higgs production with a jet veto

Gangal, Gaunt, Tackmann, Vryonidou  
2003.04323

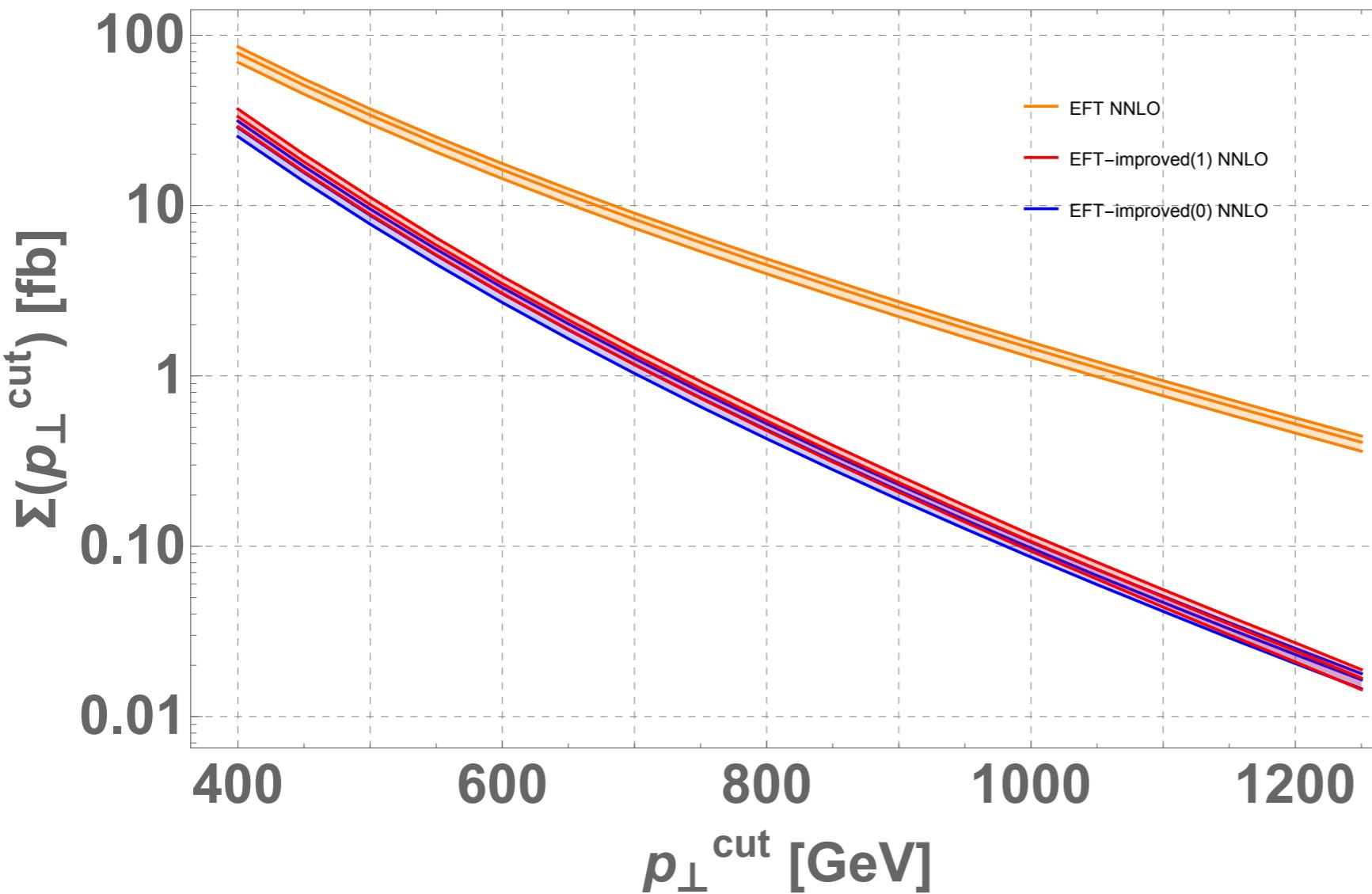


resummation up to NNLL'+NNLO with  
rapidity dependent jet veto  
reduced sensitivity to hadronisation effects

# large-p<sub>T</sub> Higgs + jet production

combine NNLO (HTL) with NLO (full  $m_t$ ) (not unique)

$$\Sigma^{\text{EFT-improved (1), NNLO}}(p_{\perp}^{\text{cut}}) \equiv \frac{\Sigma^{\text{SM, NLO}}(p_{\perp}^{\text{cut}})}{\Sigma^{\text{EFT, NLO}}(p_{\perp}^{\text{cut}})} \Sigma^{\text{EFT, NNLO}}(p_{\perp}^{\text{cut}})$$



7-point scale variations  
red curve also contains  
estimated  $\delta_{m_t}$   
(on-shell top mass scheme)

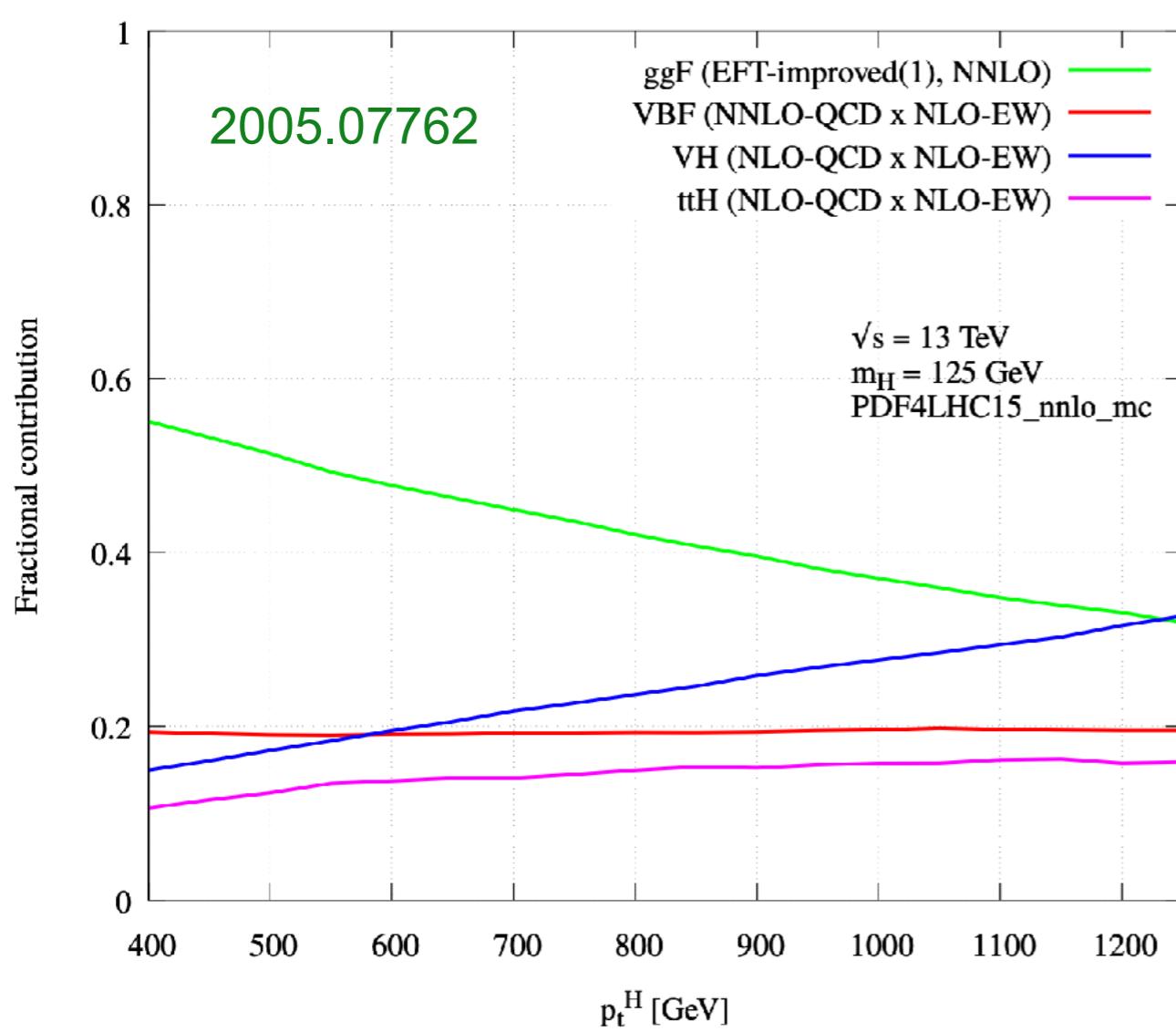
# large-pT Higgs + jet production

Becker et al. 2005.07762

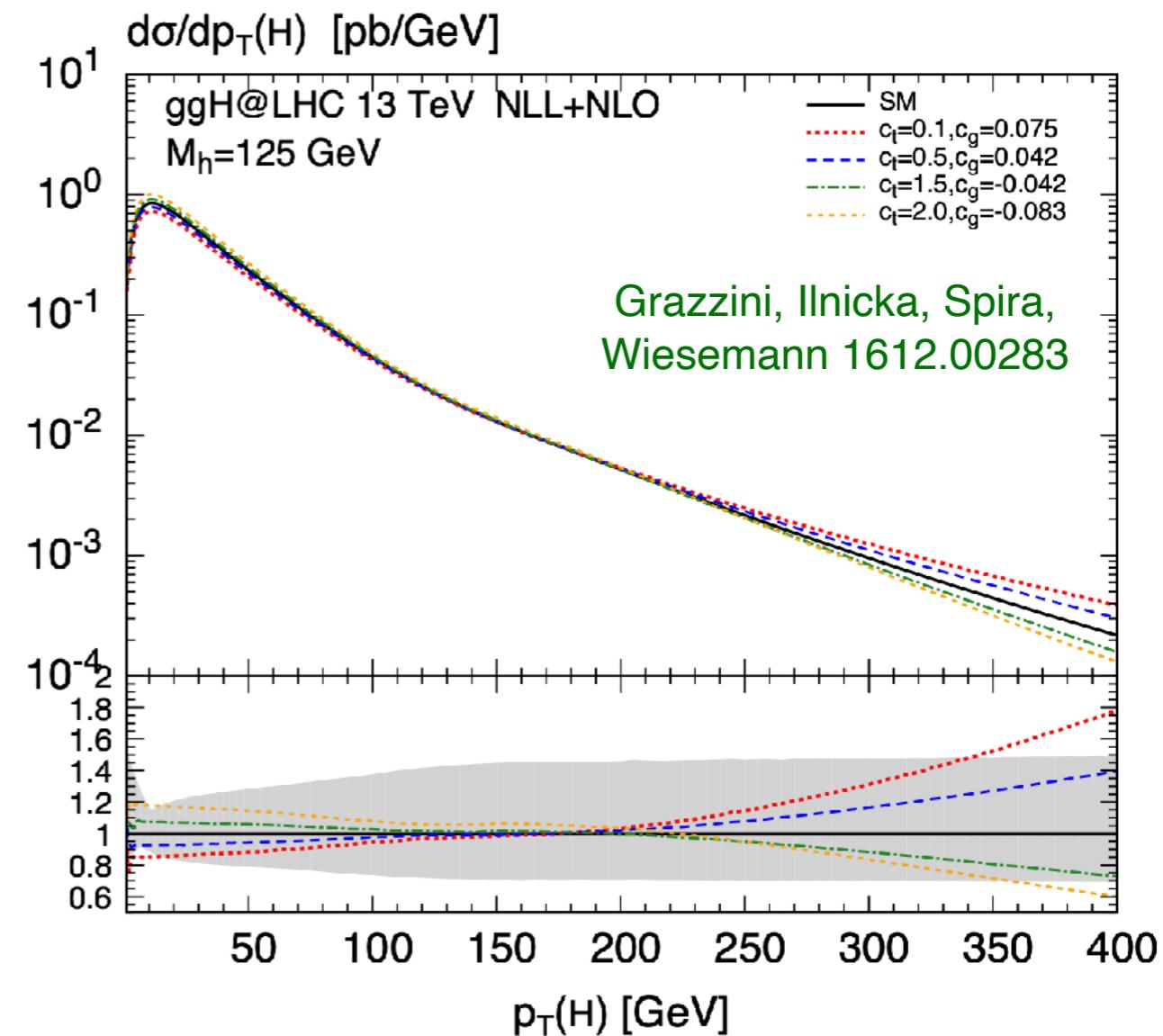
$p_T^{\text{cut}}$	NNLO <sub>quad.unc.</sub> <sup>approximate</sup> [fb]	HJ-MINLO [fb]	MG5_MC@NLO [fb]
400 GeV	$33.3^{+10.9\%}_{-12.9\%}$	$29^{+24\%}_{-21\%}$	$31.5^{+31\%}_{-25\%}$
430 GeV	$23.0^{+10.8\%}_{-12.8\%}$	-	$21.8^{+31\%}_{-25\%}$
450 GeV	$18.1^{+10.8\%}_{-12.8\%}$	$16.1^{+22\%}_{-21\%}$	$17.1^{+31\%}_{-25\%}$

reasonable agreement with state-of-the art generators  
within (large) uncertainties

# large-pT Higgs + jet production



other channels gain importance  
at large  $p_T$ , in particular VH

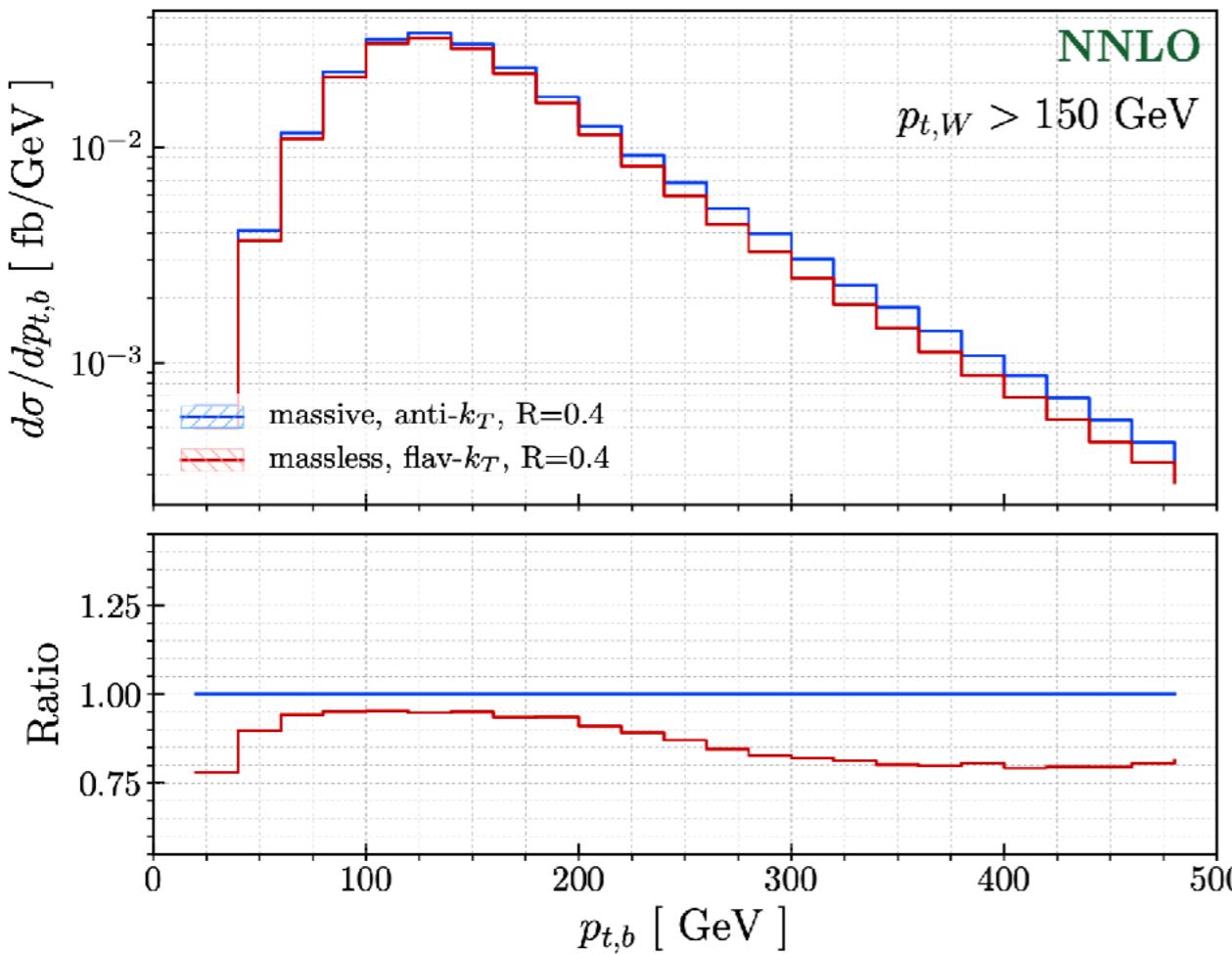


effects of anomalous couplings  
mostly at high  $p_T$

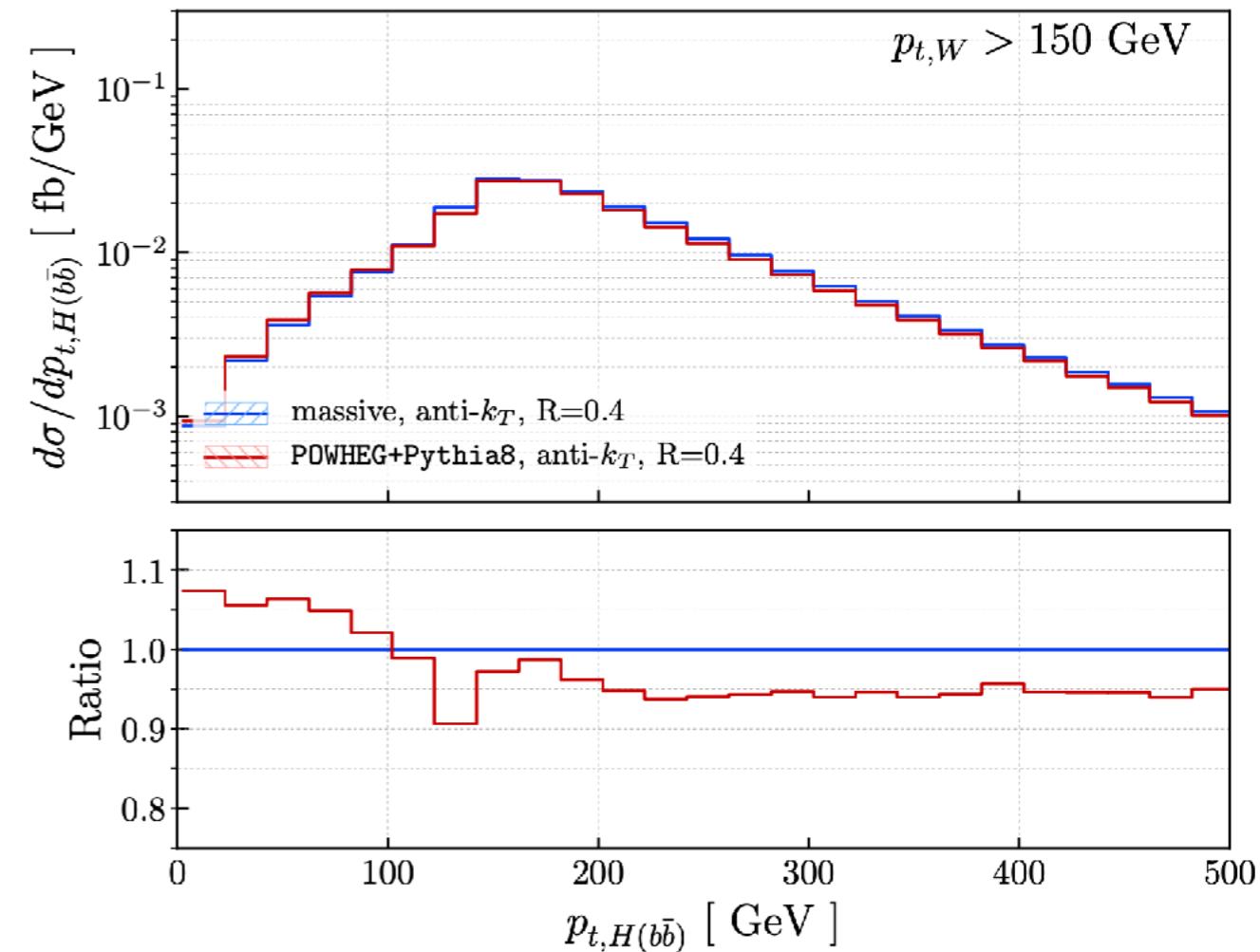
# vector bosons associated production

WH production at NNLO with  $H \rightarrow b\bar{b}$  with massive b-quarks

Behring, Bizon, Caola, Melnikov, Röntsch 2003.08321



significant differences between  
massive and massless case



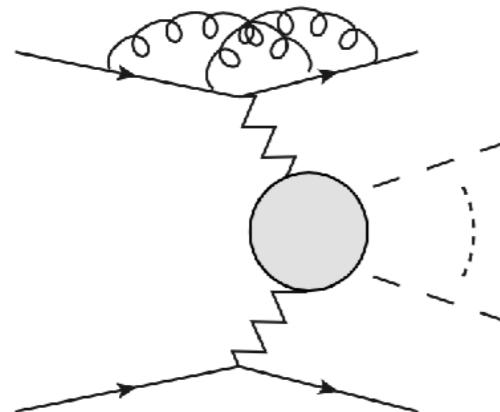
and NNLO vs NLO+PS

# H and HH in vector boson fusion

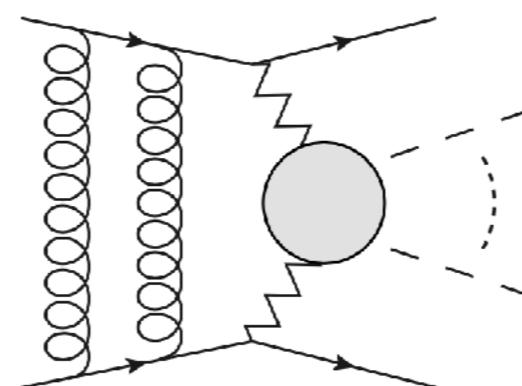
calculated up to N3LO in structure function approach Dreyer, Karlberg '16 (H), '18 (HH)

non-factorisable contributions to VBF H Lui, Melnikov, Penin 1906.10899

non-factorisable contributions to VBF H and HH Dreyer, Karlberg, Tancredi 2005.11334



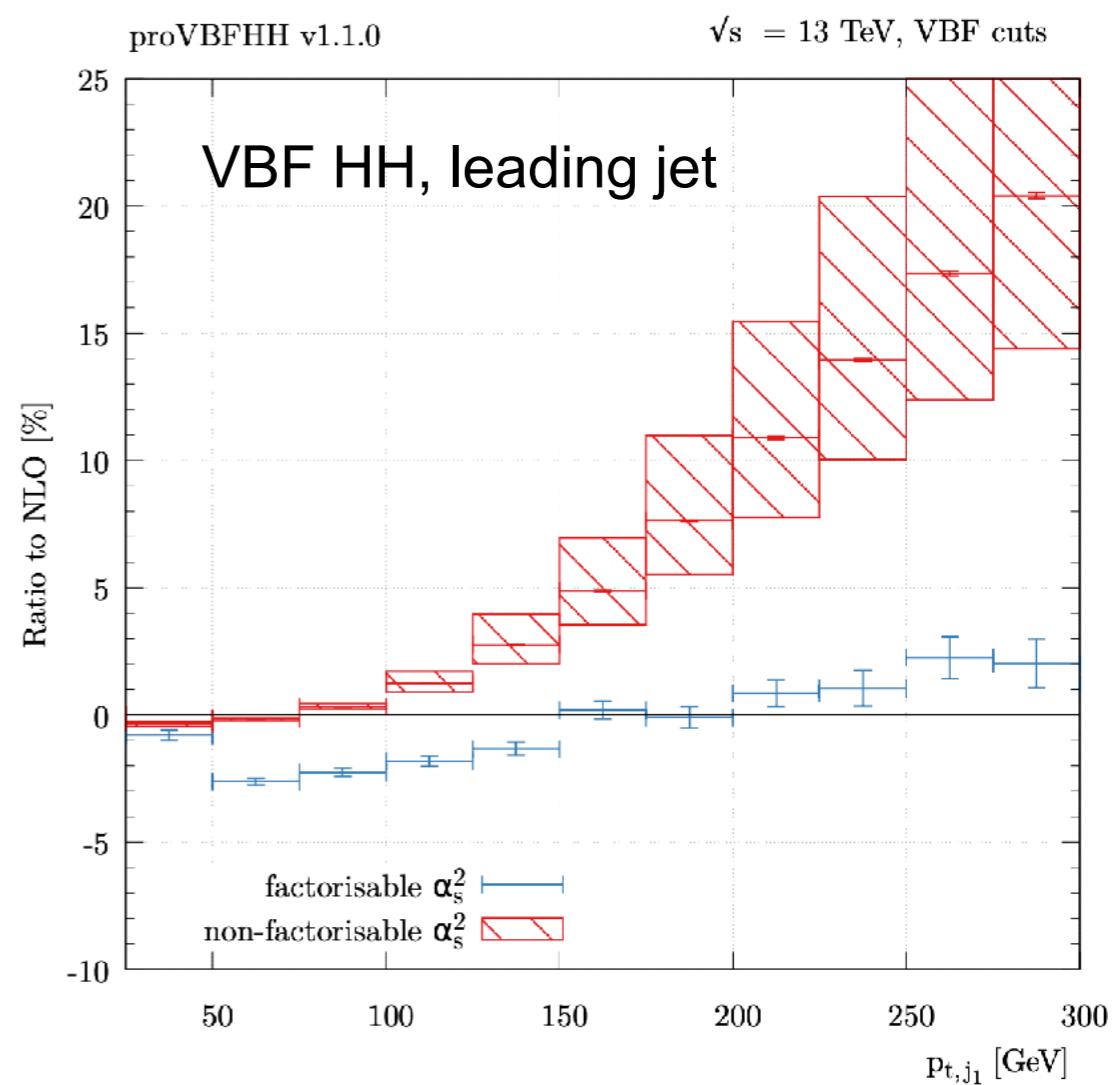
factorisable



non-factorisable

VBF H: non-factorisable corrections (mostly) within scale uncertainty band

VBF HH: cancellation among diagrams spoiled by non-factorisable corrections  
⇒ relative size large



# The Higgs Potential

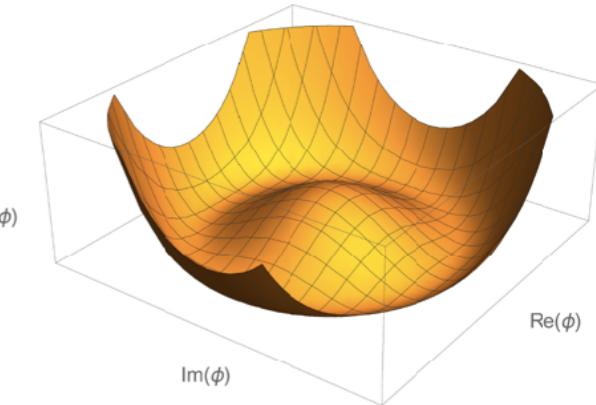
**SM:**  $V(\Phi) = -\frac{1}{2}\mu^2\Phi^2 + \frac{1}{4}\lambda\Phi^4$



EW symmetry breaking

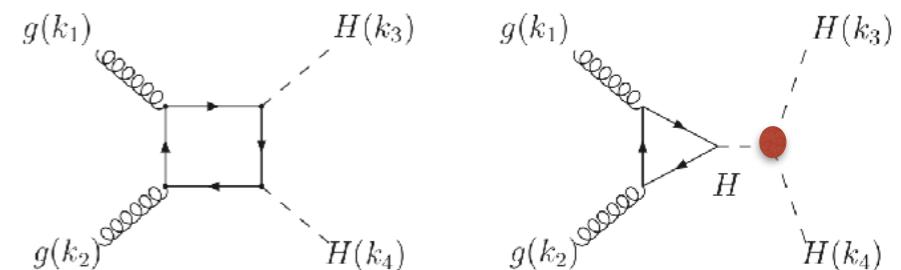
$$\frac{m_h^2}{2} h^2 + \frac{m_h^2}{2v} h^3 + \frac{m_h^2}{8v^2} h^4$$

$\lambda_{3h}$   
completely  
determined  
in the SM

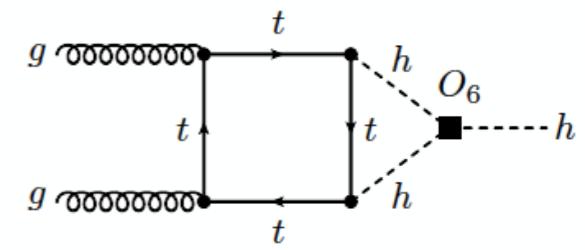


- is it really of this form?
- how large (or small) can the triple Higgs coupling be?

try to get information from

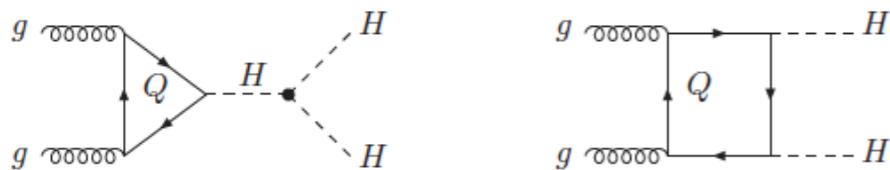


- non-resonant HH production (direct measurement)
- indirect constraints (e.g. from single H)

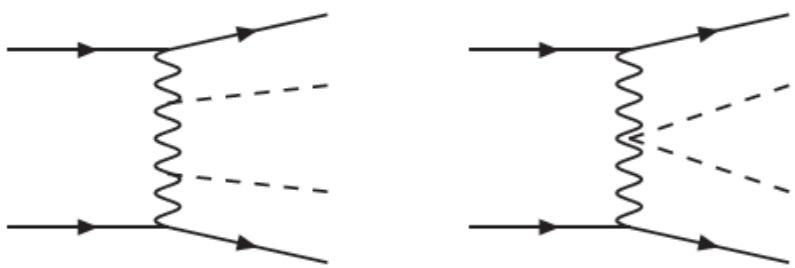


# HH production channels

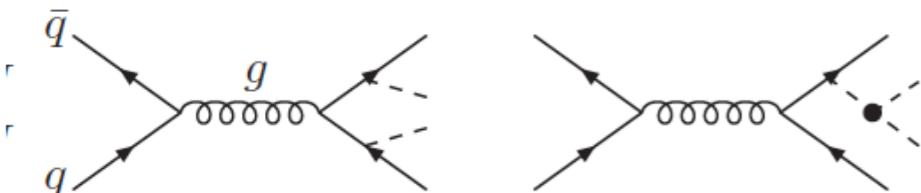
- gluon fusion



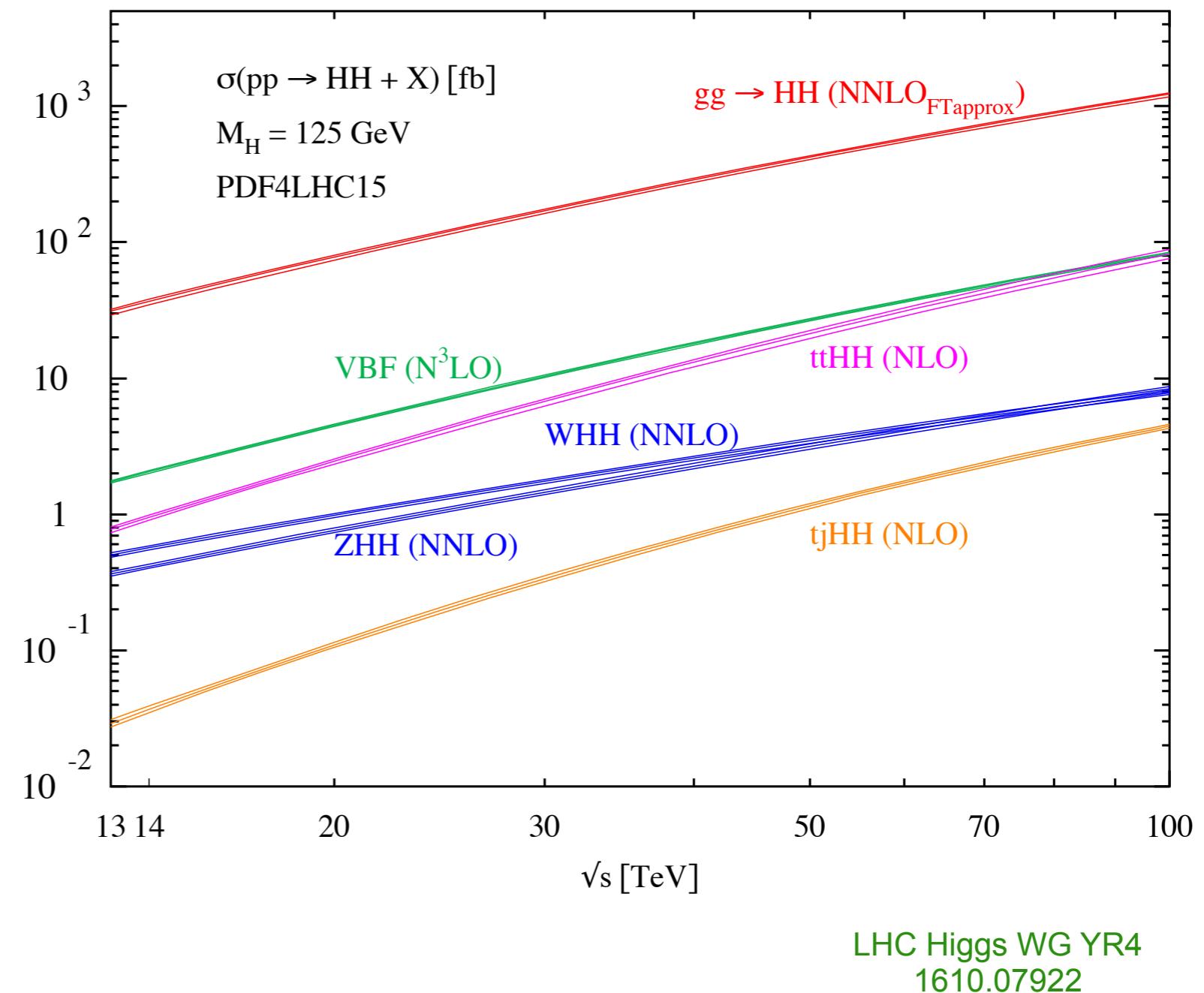
- vector boson fusion



- top-quark associated



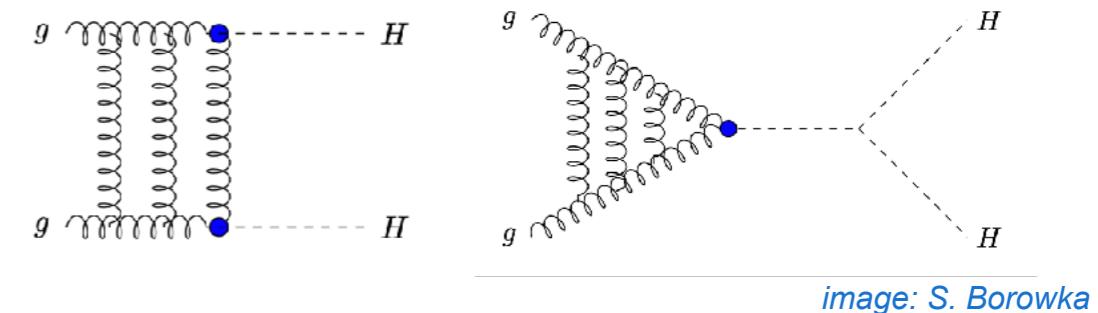
- Higgs-strahlung



# Higgs boson pair production in gluon fusion

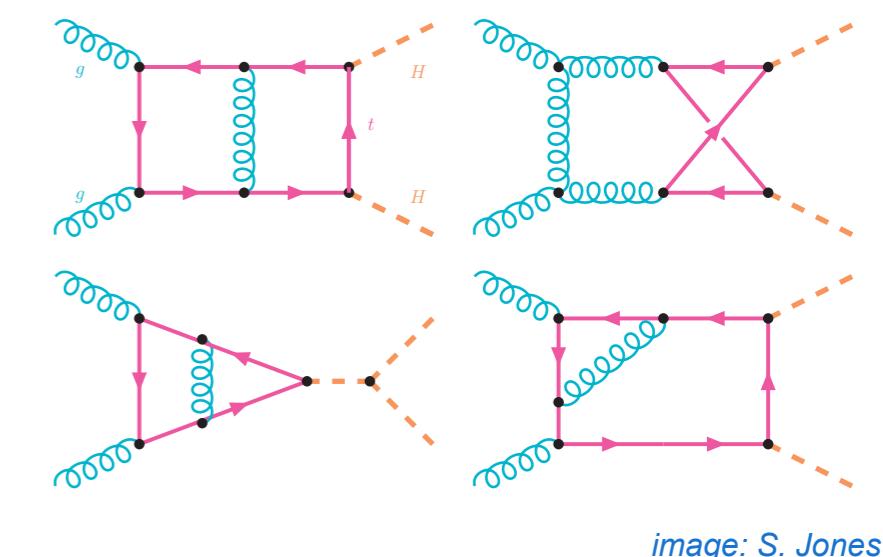
current status:

**N3LO:** Chen, Li, Shao, Wang '19  
(HTL with mt effects)



**NNLO:** De Florian, Mazzitelli '13  
Grigo, Melnikov, Steinhauser '14

**NNLO<sub>FTapprox</sub>** Grazzini, Kallweit, GH, Jones,  
current recommendation of Kerner, Lindert, Mazzitelli '18  
LHC Higgs Working Group



**NLO full  $m_t$**

Borowka, Greiner, GH, Jones, Kerner, Schlenk et al. '16

Baglio, Campanario, Glaus Mühlleitner, Spira, Streicher '18

Davies, GH, Jones, Kerner, Mishima, Steinhauser, Wellmann '19

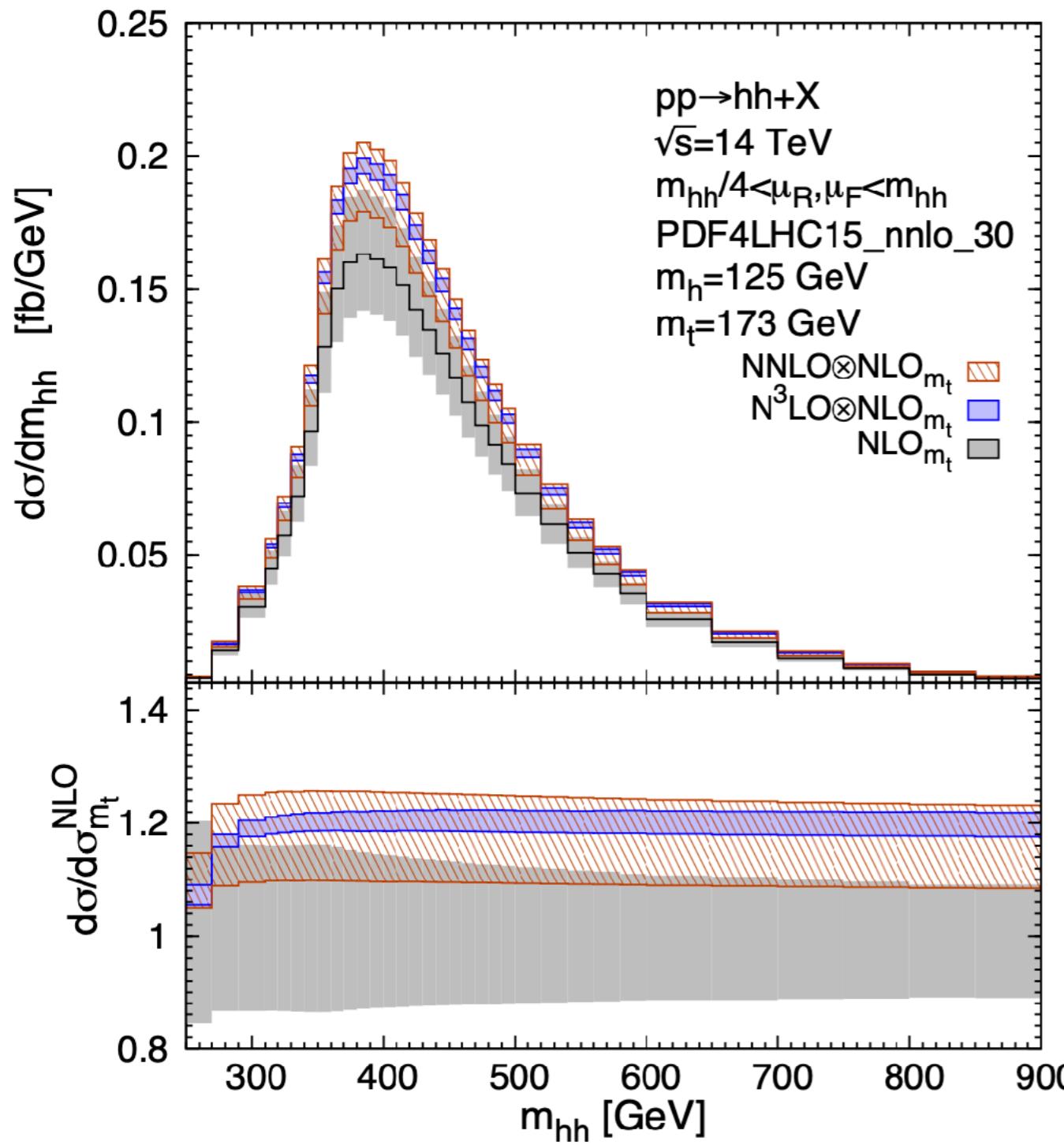
top quark mass scheme uncertainties: pole mass versus  $\overline{\text{MS}}$  mass

Baglio, Campanario, Glaus Mühlleitner, Ronca, Spira 2008.11626

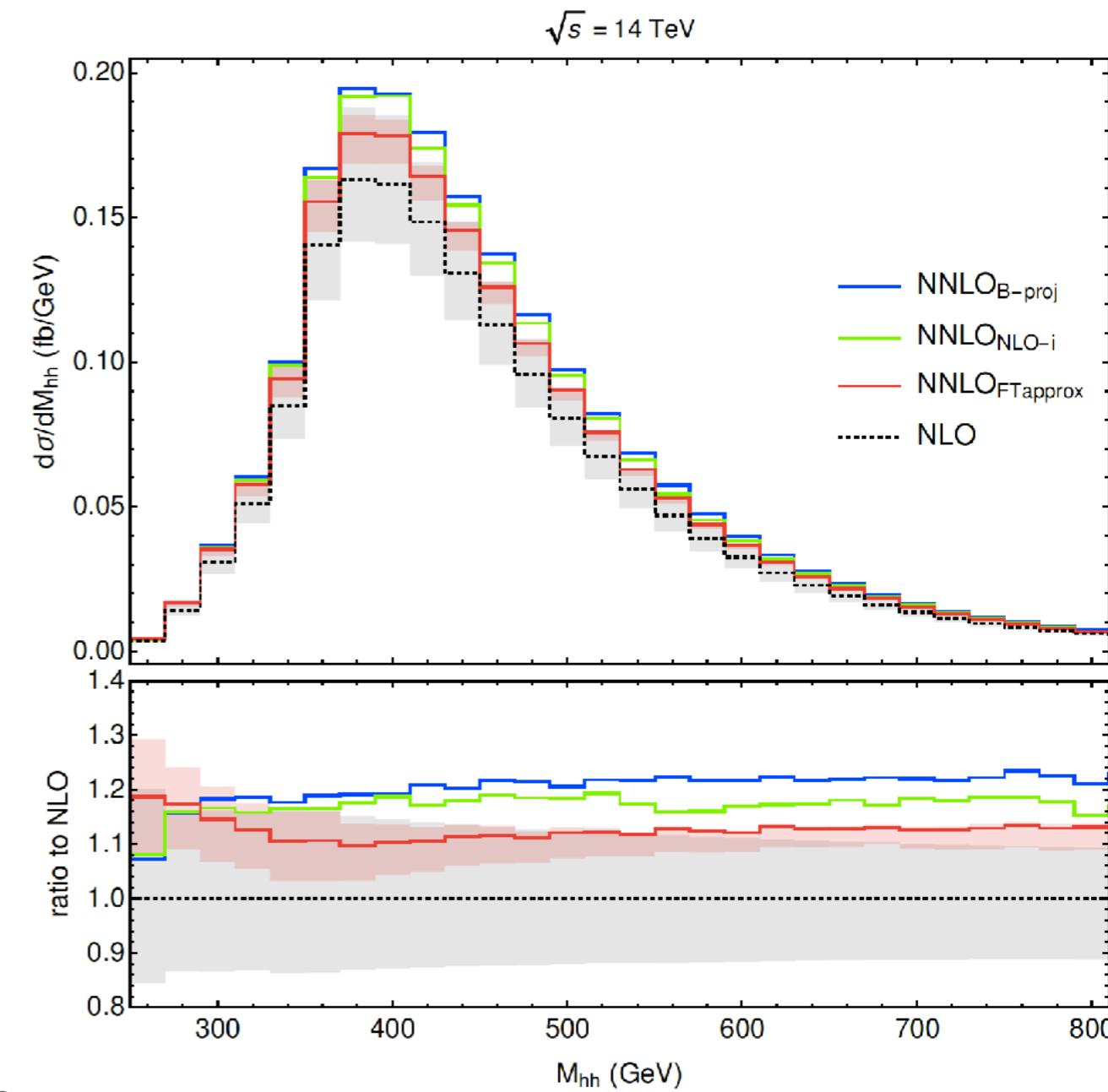
# Higgs boson pair production in gluon fusion

Chen, Li, Shao, Wang 1912.13001

Grazzini, Kallweit, GH, Jones, Kerner,  
Lindert, Mazzitelli 1803.02463



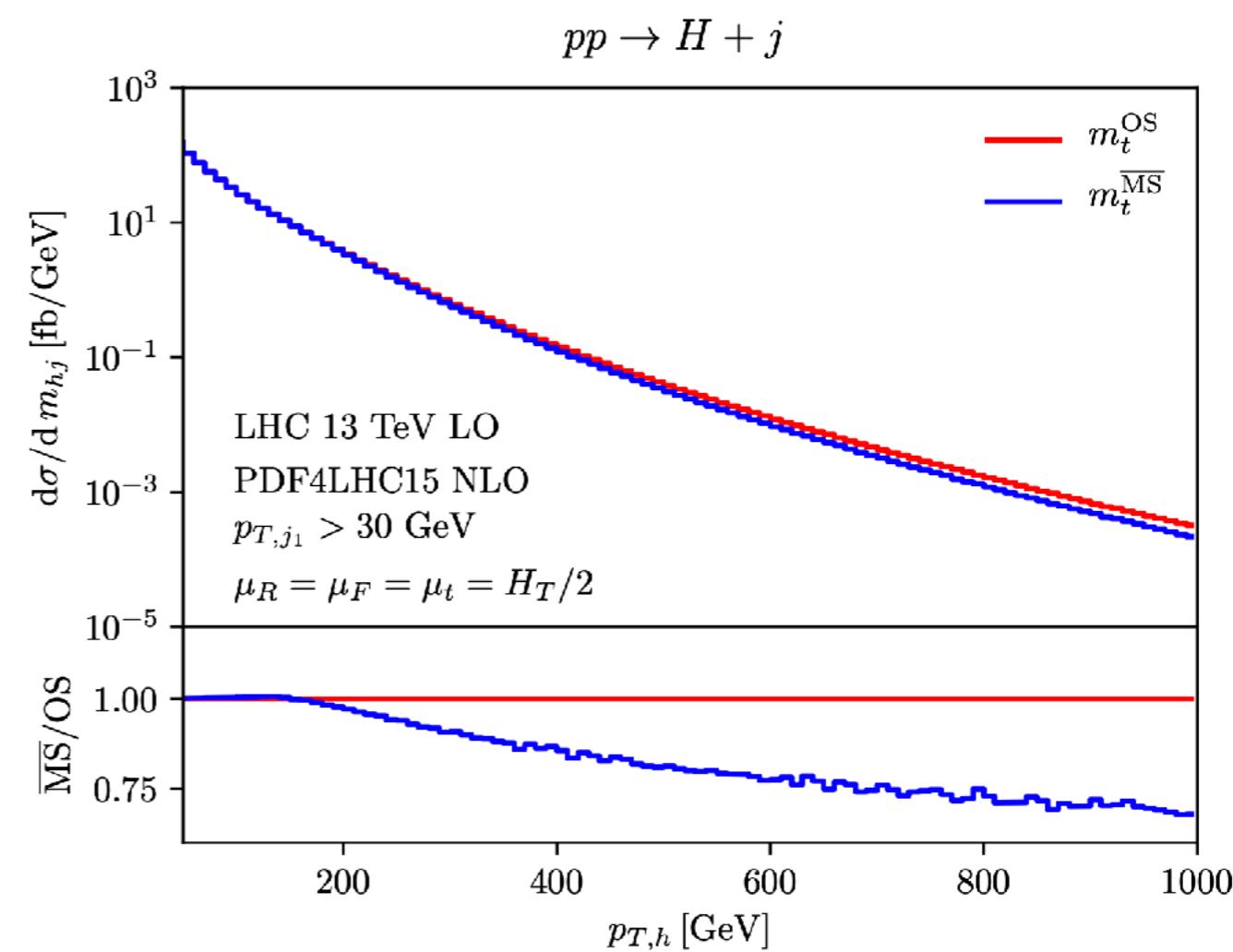
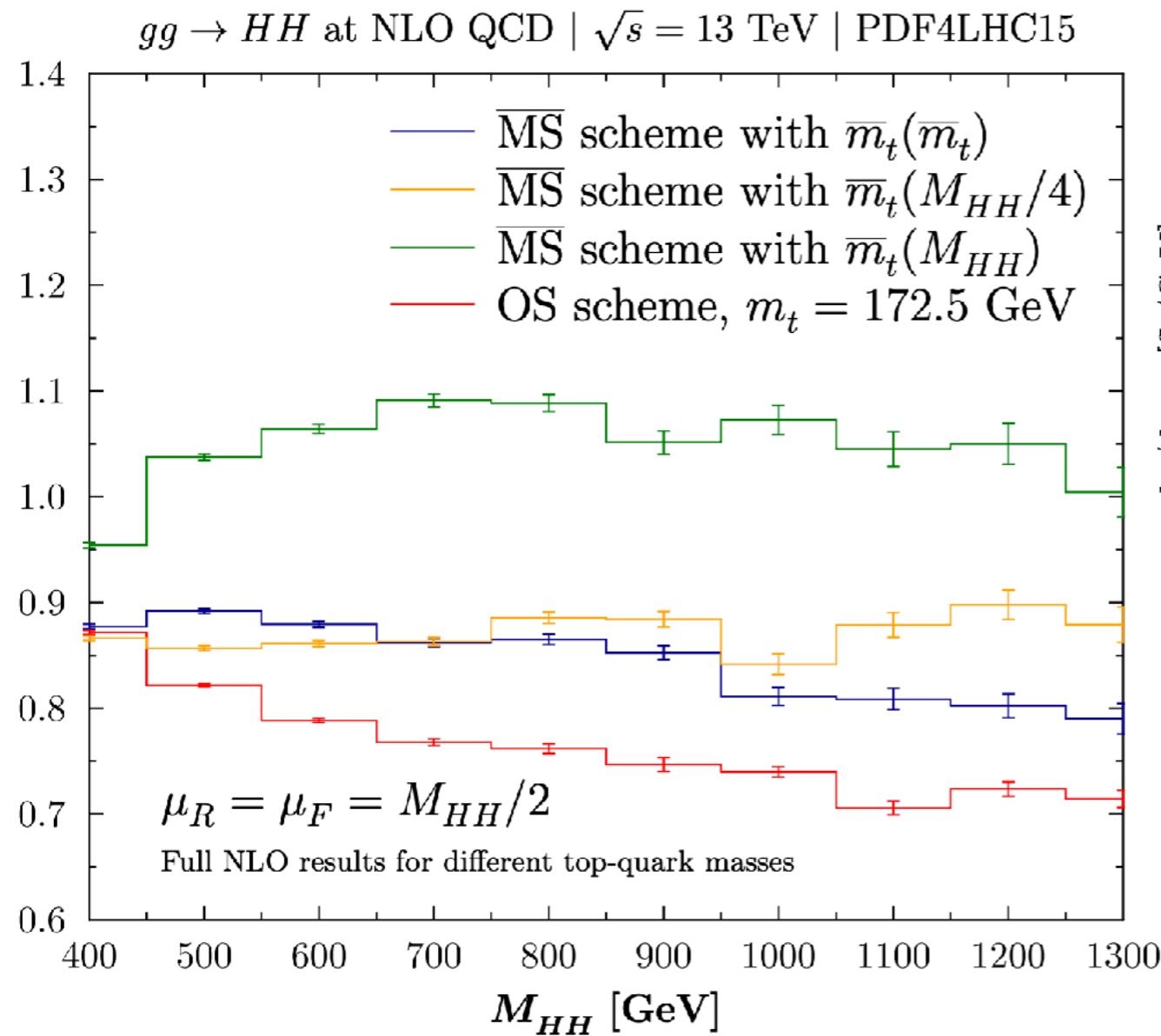
$\sqrt{s} = 14$  TeV



# scheme dependence

$$\overline{m}_t(m_t) = \frac{m_t}{1 + \frac{4}{3} \frac{\alpha_s(m_t)}{\pi} + K_2 \left( \frac{\alpha_s(m_t)}{\pi} \right)^2 + K_3 \left( \frac{\alpha_s(m_t)}{\pi} \right)^3}$$

relation between pole mass and  $\overline{\text{MS}}$  mass



also present in other loop induced processes

Baglio, Campanario, Glaus Mühlleitner,  
Ronca, Spira 2008.11626

Jones, Spira Les Houches 2019

# HH at NLO within EFT

SMEFT:

$$\begin{aligned}\Delta\mathcal{L}_{\text{dim}6} = & \frac{\bar{c}_H}{2v^2}\partial_\mu(\phi^\dagger\phi)\partial^\mu(\phi^\dagger\phi) + \frac{\bar{c}_u}{v^2}y_t(\phi^\dagger\phi\bar{q}_L\tilde{\phi}t_R + \text{h.c.}) - \frac{\bar{c}_6}{2v^2}\frac{m_h^2}{v^2}(\phi^\dagger\phi)^3 \\ & + \frac{\bar{c}_{ug}}{v^2}g_s(\bar{q}_L\sigma^{\mu\nu}G_{\mu\nu}\tilde{\phi}t_R + \text{h.c.}) + \frac{4\bar{c}_g}{v^2}g_s^2\phi^\dagger\phi G_{\mu\nu}^a G^{a\mu\nu}\end{aligned}$$

HEFT (non-linear EFT):

$$\begin{aligned}\Delta\mathcal{L}_{d\chi\leq 4} = & -m_t\left(\cancel{c}_t\frac{h}{v} + \cancel{c}_{tt}\frac{h^2}{v^2}\right)\bar{t}t - \cancel{c}_{hhh}\frac{m_h^2}{2v}h^3 \\ & + \frac{\alpha_s}{8\pi}\left(\cancel{c}_{ggh}\frac{h}{v} + \cancel{c}_{gghh}\frac{h^2}{v^2}\right)G_{\mu\nu}^a G^{a,\mu\nu}\end{aligned}$$

SMEFT relations:  $c_t = 1 - \frac{\bar{c}_H}{2} - \bar{c}_u$  ,  $c_{tt} = -\frac{\bar{c}_H + 3\bar{c}_u}{2}$  ,  $c_{hhh} = 1 - \frac{3}{2}\bar{c}_H + \bar{c}_6$  ,

$$c_{ggh} = 2c_{gghh} = 128\pi^2\bar{c}_g .$$

# HH K-factors

K-factors as functions of the BSM couplings

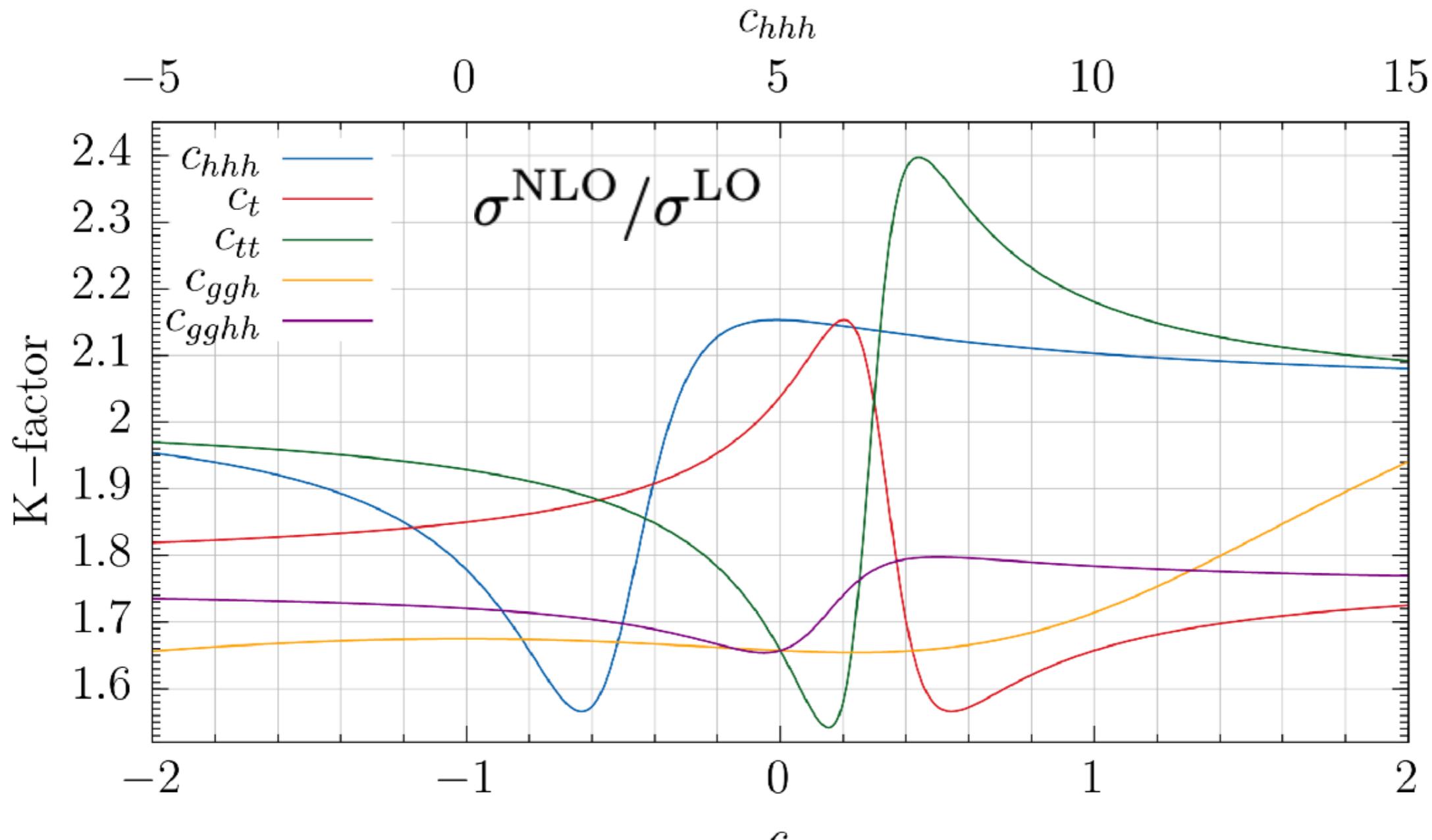


figure: L.Scyboz

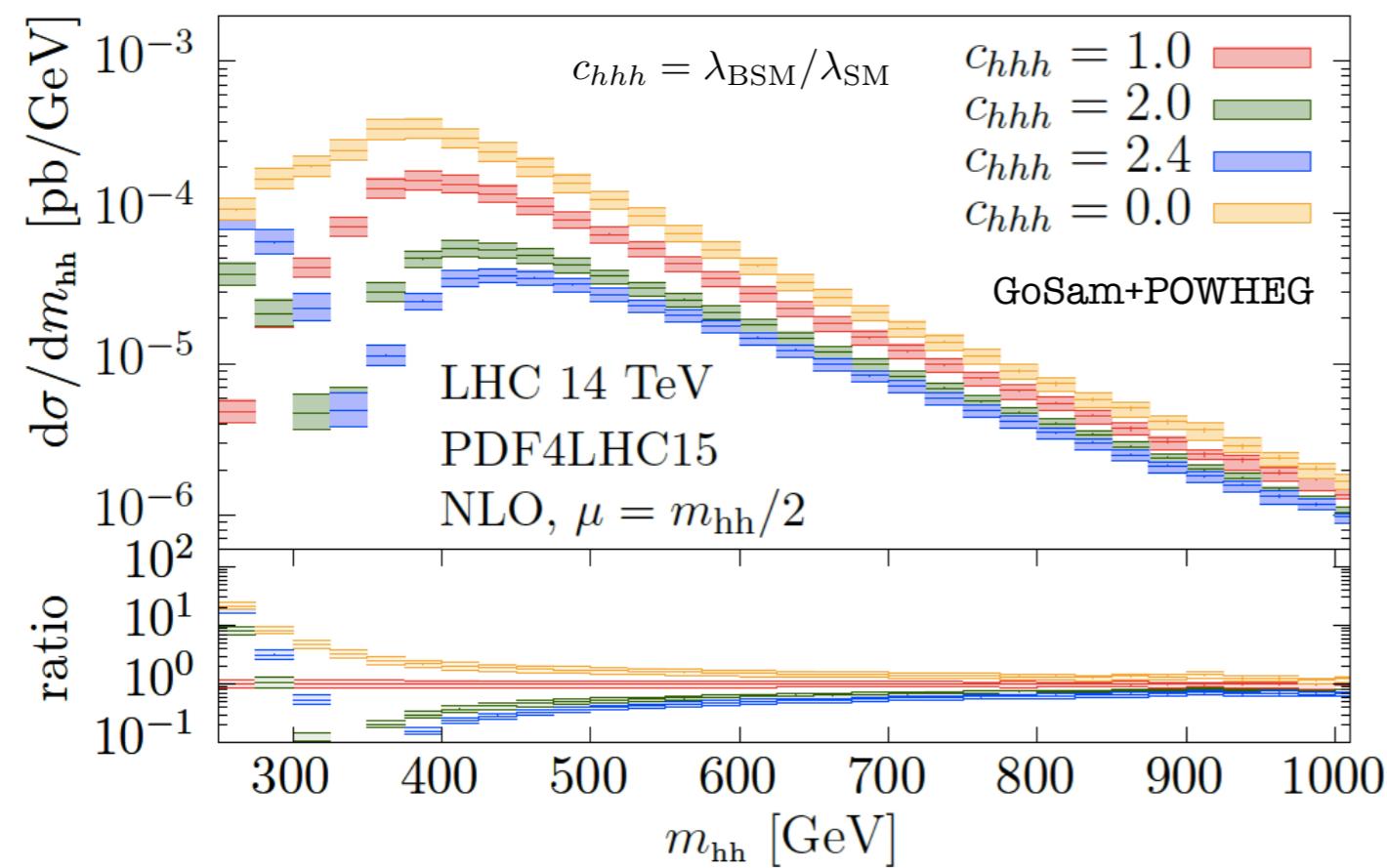
vary substantially (much less variation in heavy top limit)

# HH full NLO MC tool

- Monte Carlo program (within Powheg-Box) to produce full NLO results for Higgs pair production in gluon fusion  
GH, Jones, Kerner, Luisoni, Scyboz 2006.16887,1903.08137
- interface to Pythia and two different Herwig parton showers
- 5 anomalous couplings  $c_{hhh}, c_t, c_{tt}, c_{ggh}, c_{gggh}$  can be varied by the user
- publicly available at

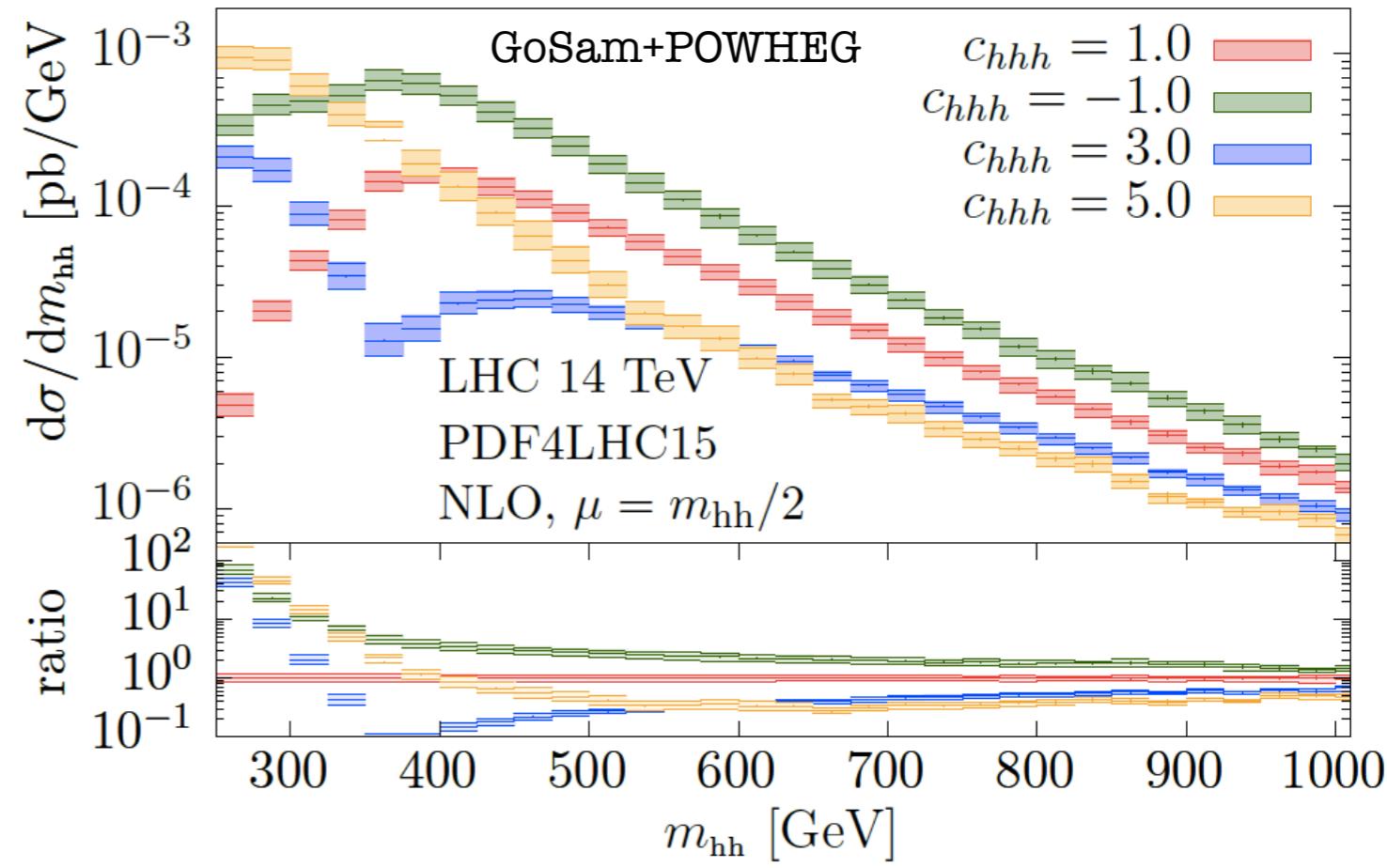
<http://powhegbox.mib.infn.it/User-Process-V2/ggHH>

# HH invariant mass with variation of the self-coupling

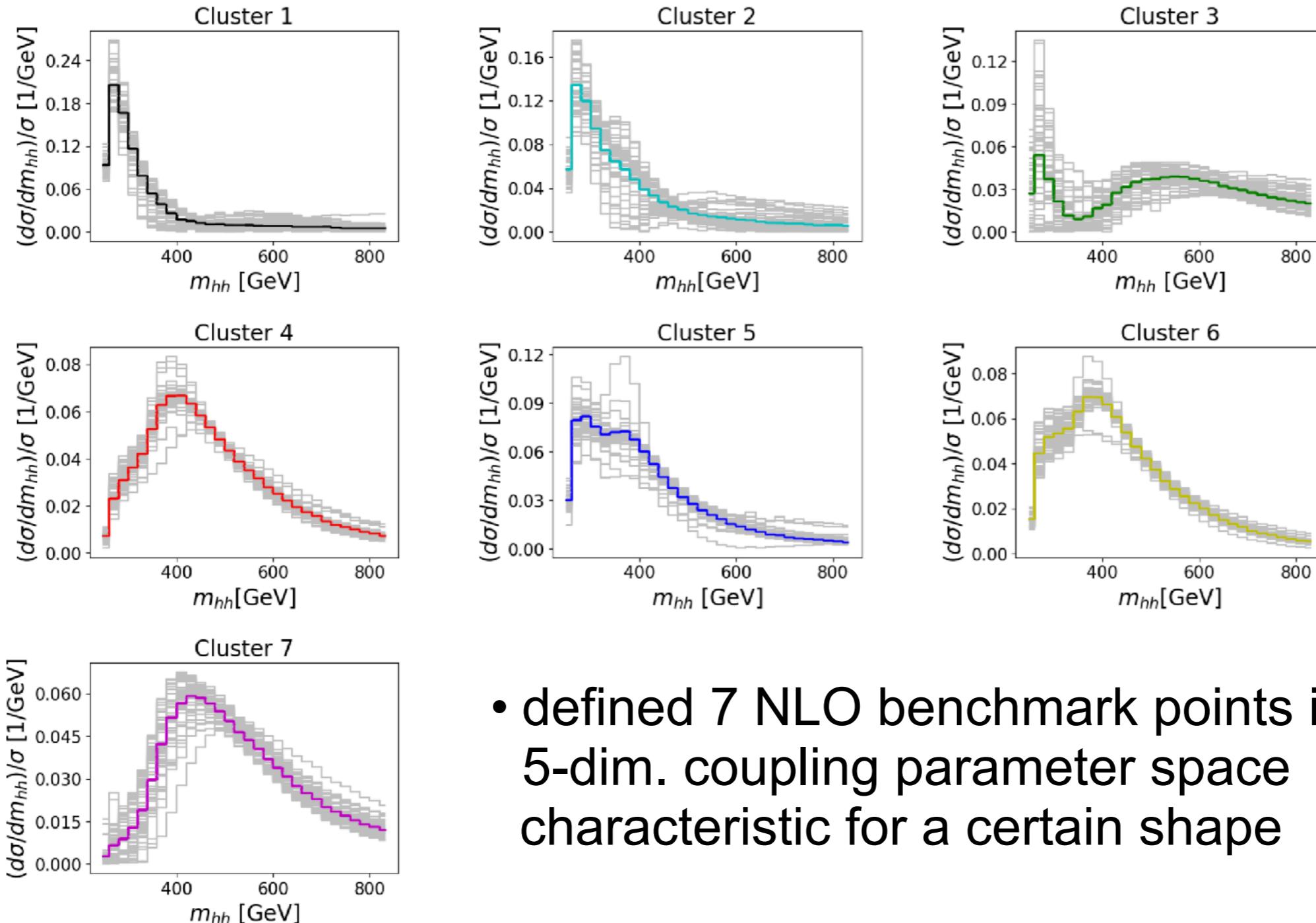


bands: 3-point scale variations

dip in  $m_{hh}$  distribution  
at 350 GeV for  $c_{hhh} \sim 2.4$   
due to maximal destructive  
interference

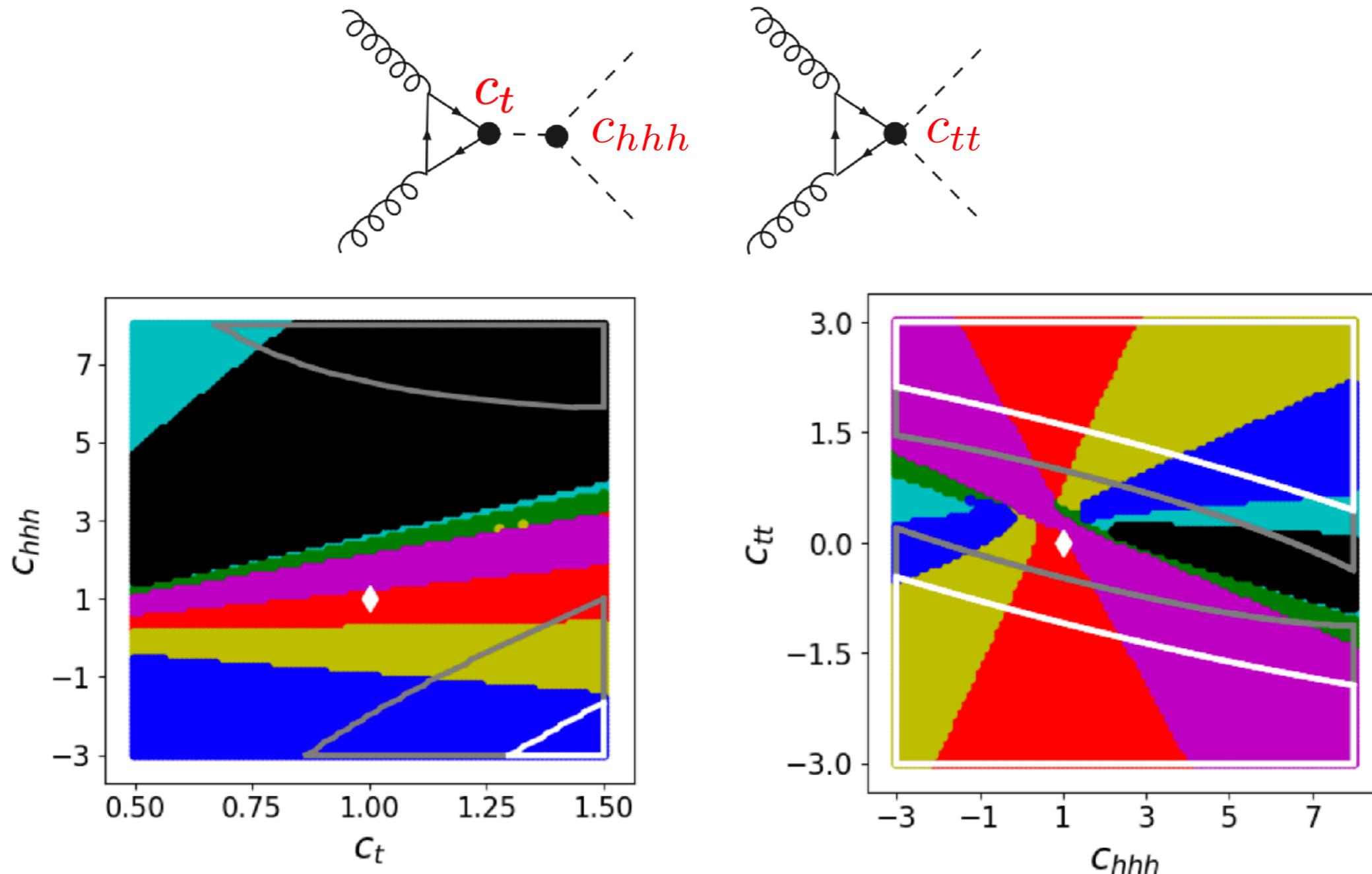


# $m_{hh}$ shape analysis



- defined 7 NLO benchmark points in 5-dim. coupling parameter space characteristic for a certain shape
- based on autoencoder and K-means clustering Capozi, GH 1908.08932

# $m_{hh}$ shape analysis



$c_{hhh}$  and  $c_{ttt}$  have strong influence on shape  
shape combined with bounds on total  $\sigma$  gives better constraints

# Summary

- the Higgs sector might offer windows to new physics
- precision is the key at current energies
- great progress in precision calculations
  - for some processes scale uncertainties no longer the dominant uncertainties
- **current main challenges:**
  - mass effects
  - mixed EW-QCD corrections
  - $2 \rightarrow 3$  processes at NNLO
  - reduce PDF,  $\alpha_s$ -uncertainties
  - NNLO+PS/analytic resummation
  - BSM, EFT + higher orders

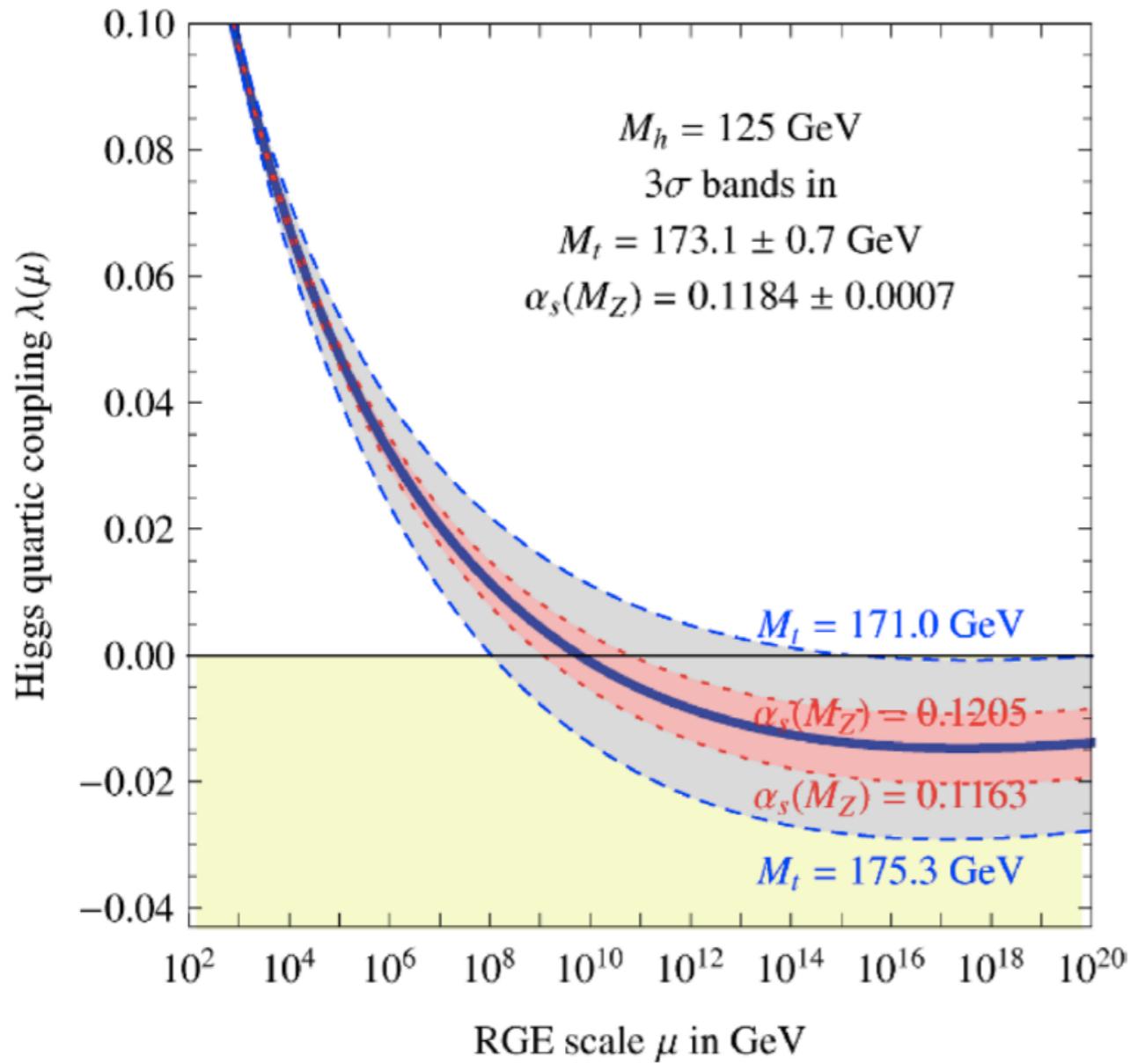
# The Standard Model is unlikely to be the full picture



with precision we may see imprints of physics at higher scales!  
(e.g. watch the shadows)

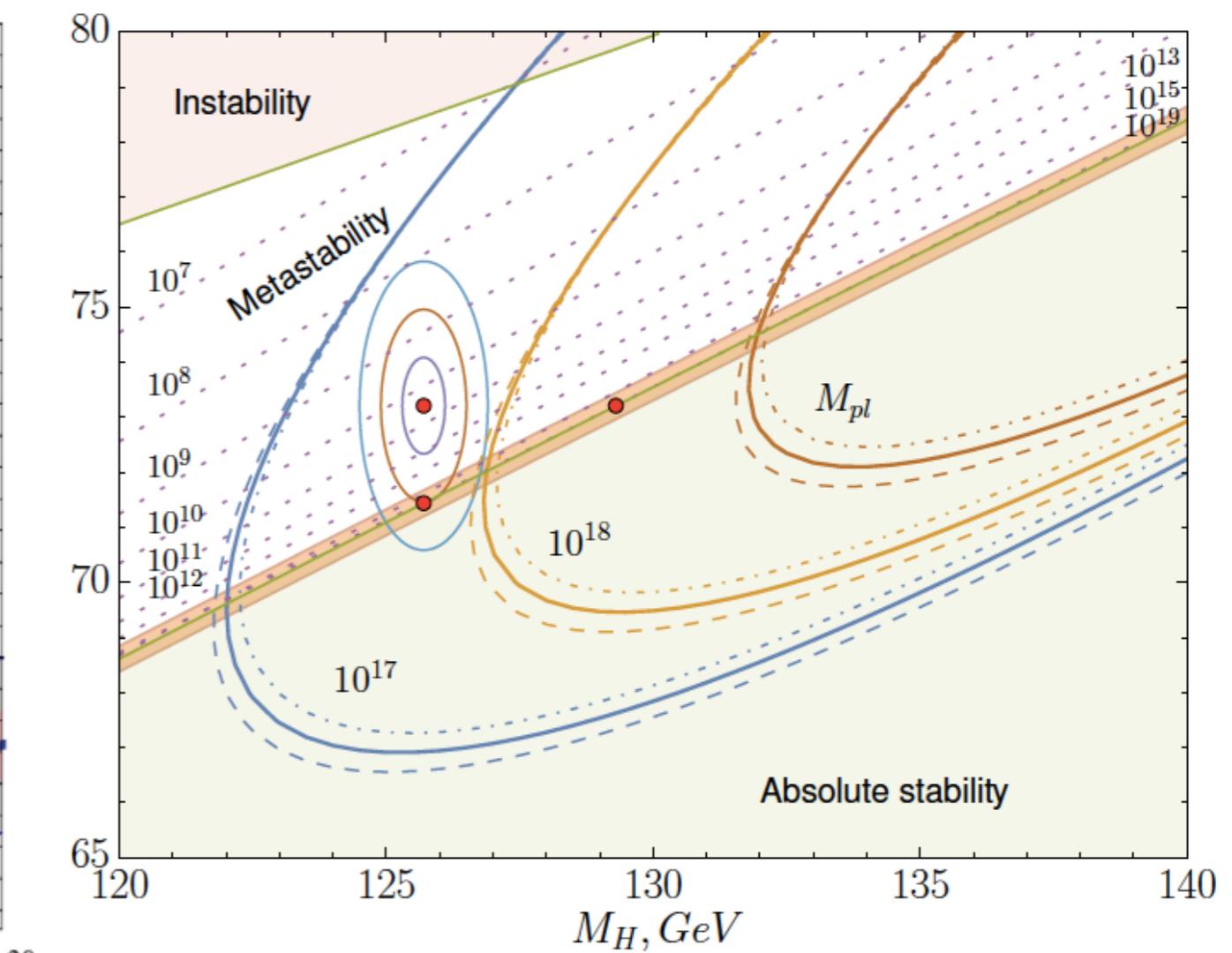


# Higgs and the universe



Degrassi, Di Vita, Elias-Miro, Espinosa,  
Giudice, Isidori, Strumia '12

$\lambda = \lambda(\mu)$  is a running coupling



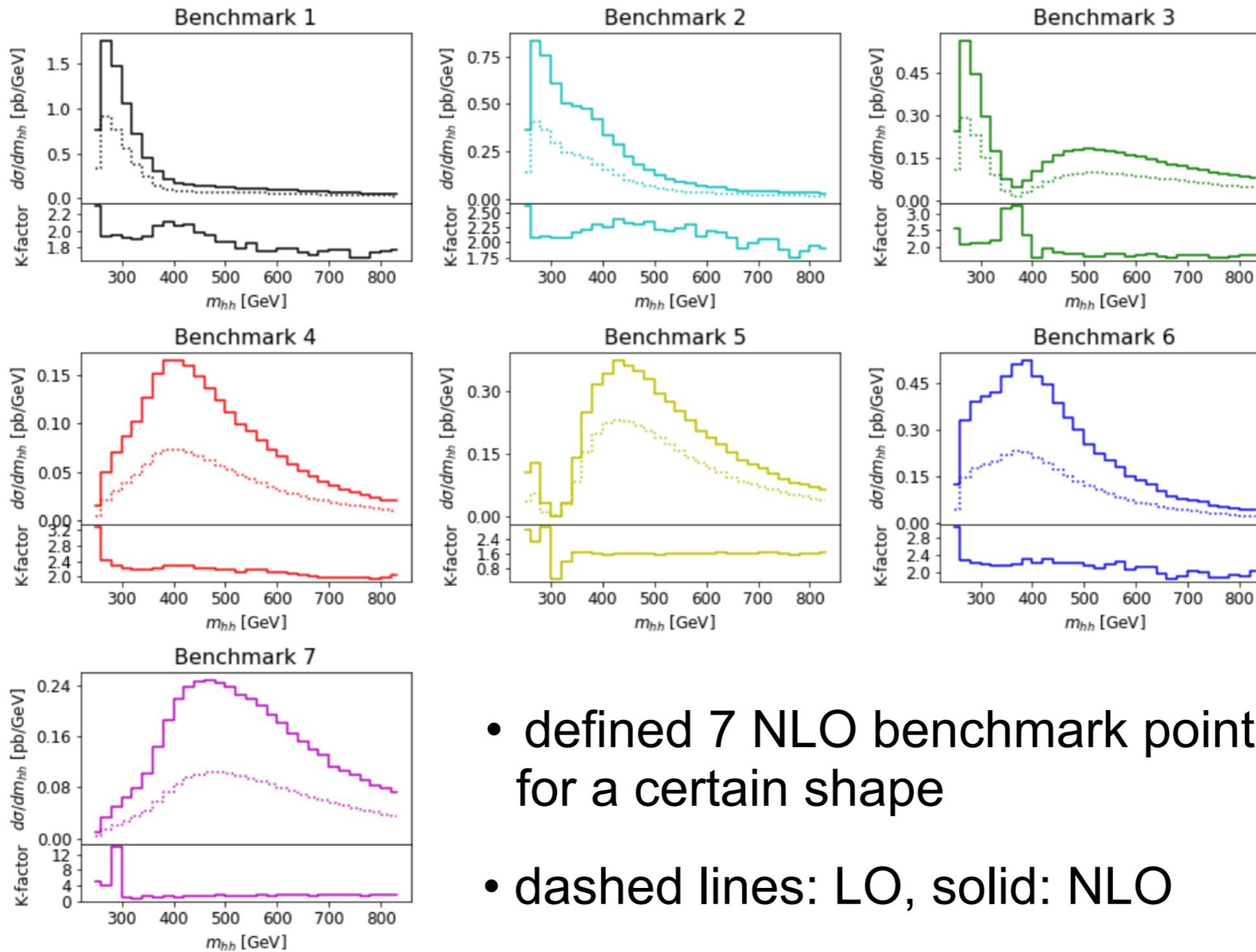
Bednyakov, Kniehl, Pikelner, Veretin '15

Buttazzo, Degrassi, Giardino, Giudice,  
Sala, Salvio, Strumia '13

(through quantum corrections, in the SM  
dominated by top and Higgs loops)

# HH shape analysis

Capozi, GH 1908.08932

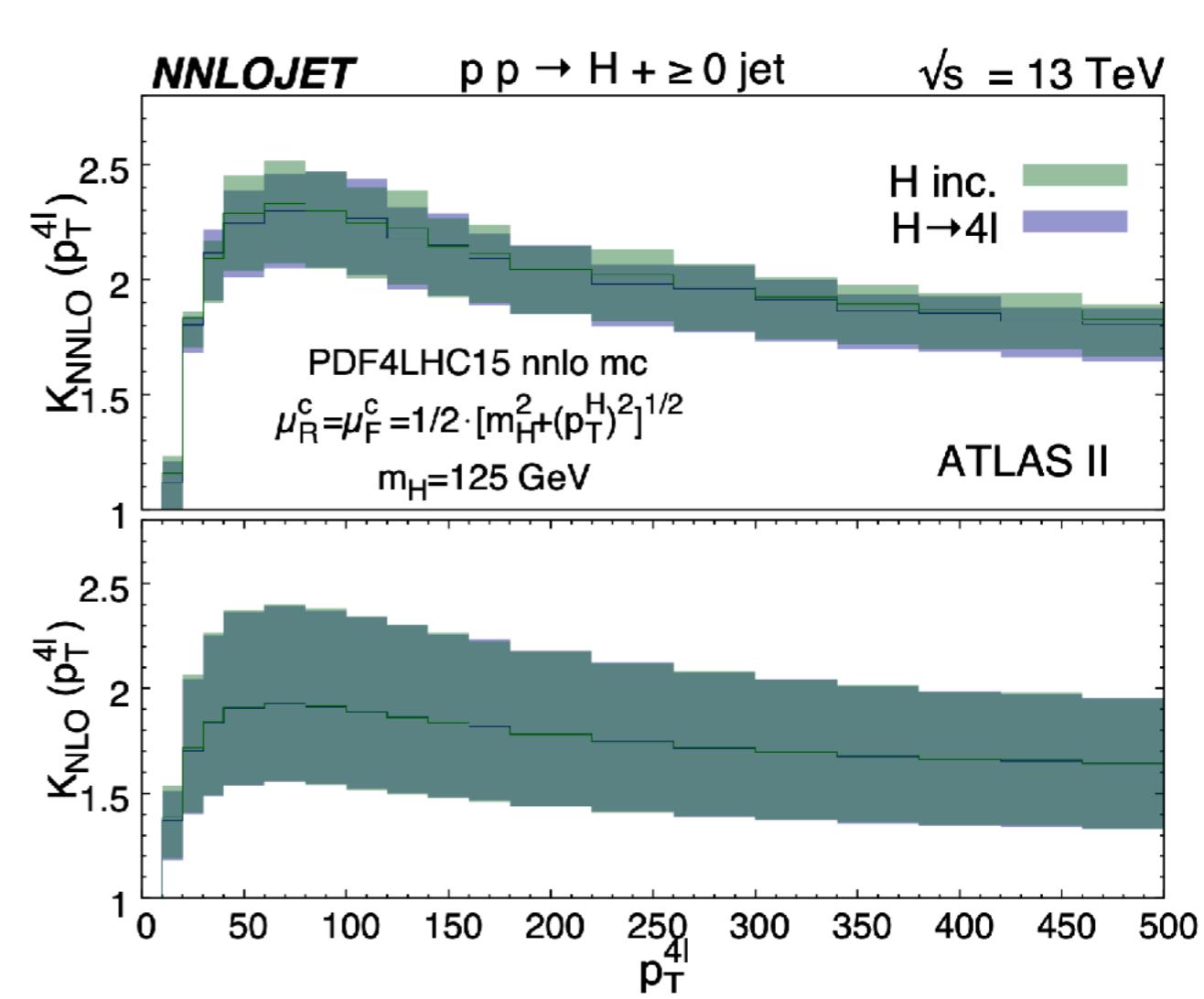
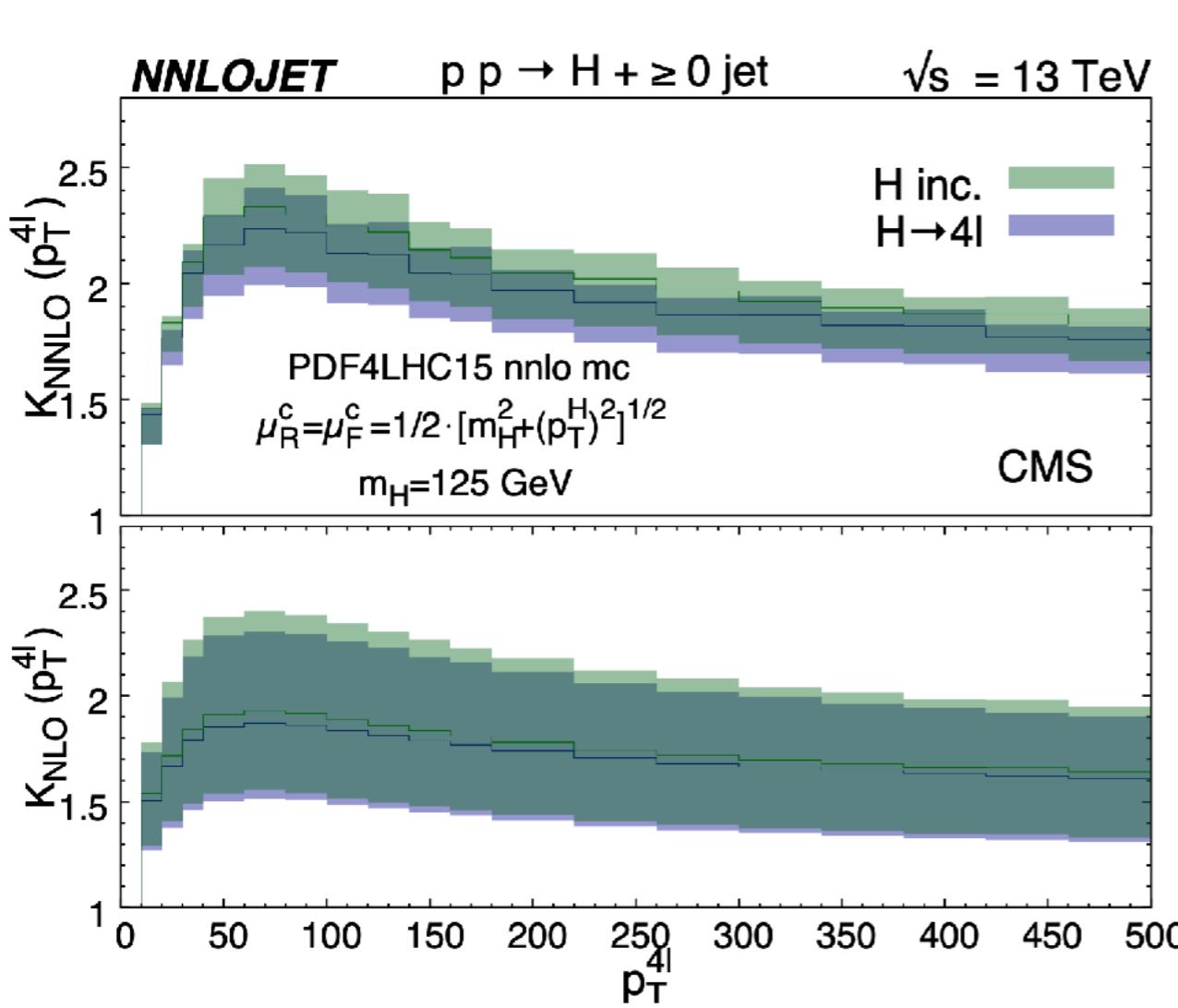


- defined 7 NLO benchmark points characteristic for a certain shape
- dashed lines: LO, solid: NLO

# ggF H NNLO differential results

$pp \rightarrow H + \leq 1 j \rightarrow 4l + \leq 1 j$

Chen, Gehrmann, Glover, Huss  
1905.13738



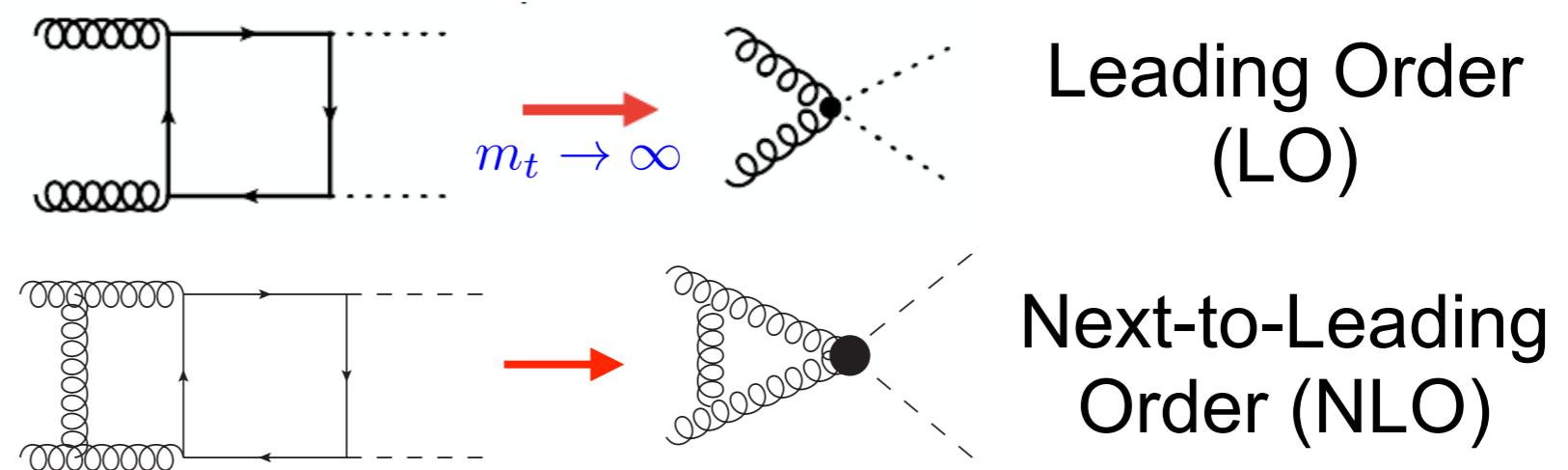
study of perturbative stability of lepton acceptance cuts

# Invariant mass of the Higgs boson pair

Observable:  $m_{hh}^2 = (p_{h_1} + p_{h_2})^2$

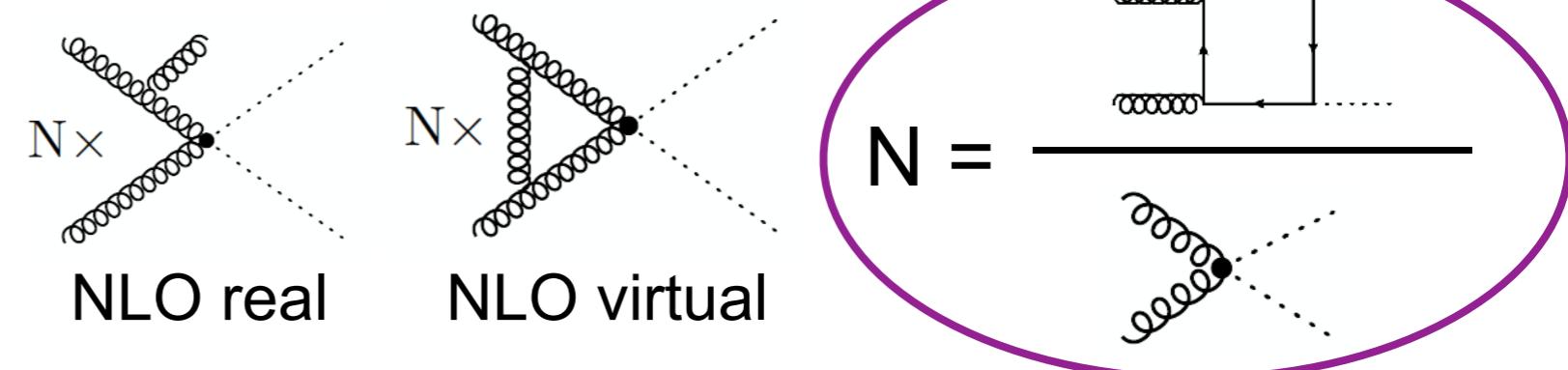
approximations:

- $m_t \rightarrow \infty$  limit (HEFT):  
("Higgs Effective Field Theory")

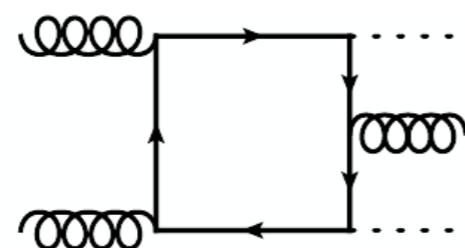


- Born-improved HEFT:

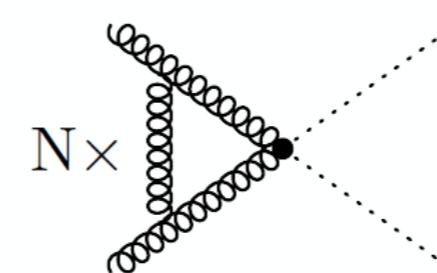
$$d\sigma_{m_t \rightarrow \infty}^{\text{NLO}} \times \frac{d\sigma^{\text{LO}}(m_t)}{d\sigma^{\text{LO}}_{m_t \rightarrow \infty}}$$



- FTapprox:



NLO real:  
full  $m_t$ -dependence



NLO virtual:  
Born-improved HEFT

# full NLO combined with NNLO

Grazzini, Kallweit, GH, Jones, Kerner, Lindert, Mazzitelli; 1803.02463

## Technical ingredients

Tree-level and one-loop amplitudes (HEFT and full- $M_t$ ) → OpenLoops  
[Cascioli, Lindert, Maierhofer, Pozzorini]

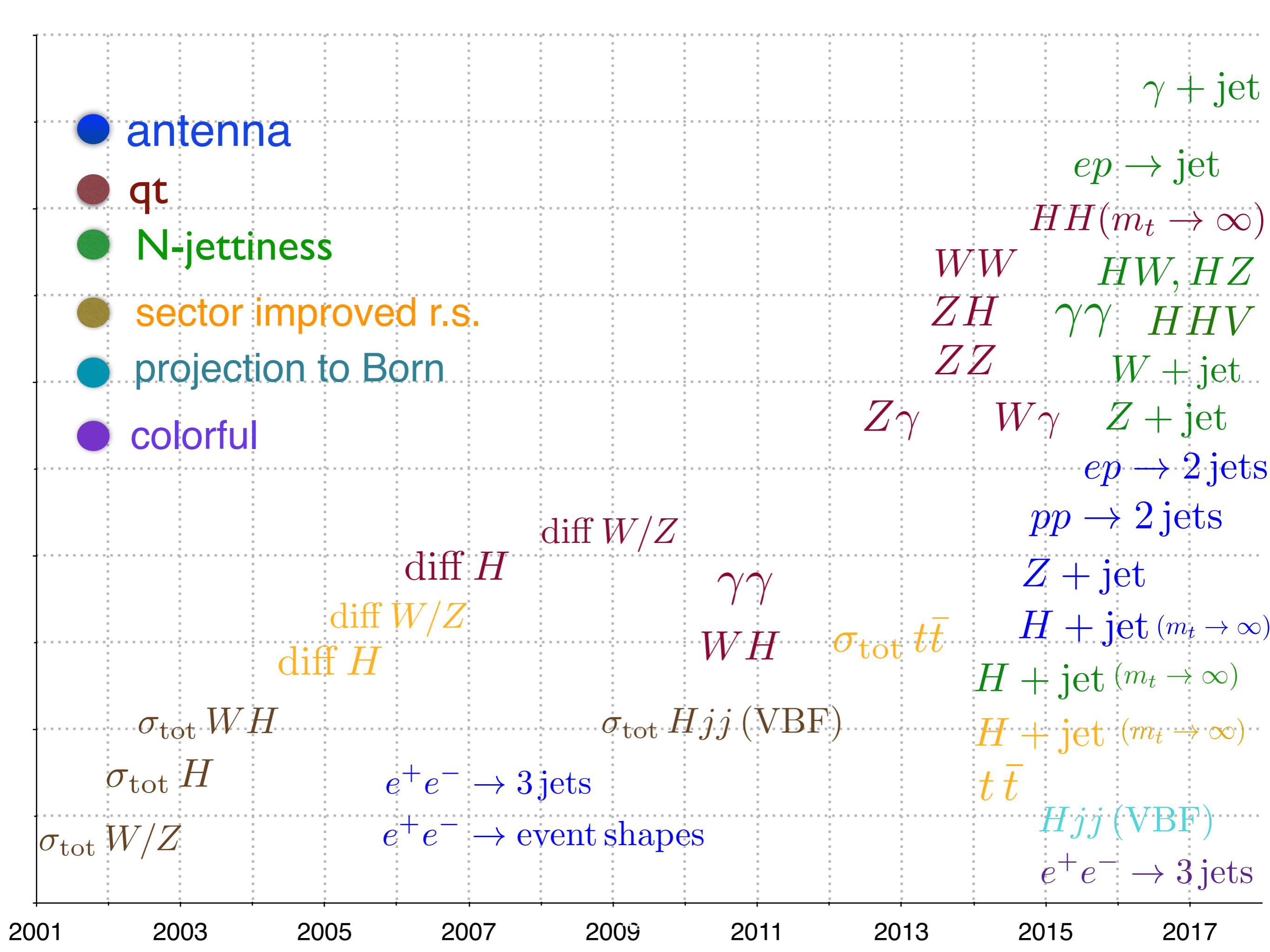
Full NLO (two-loop) virtual corrections → two dimensional grid + interpolation  
[Borowka, Greiner, Heinrich, Jones, Kerner, Schlenk, Zirke, '16]

Analytical results for NNLO two-loop corrections in the HEFT  
[de Florian, JM, '13]

NNLO subtraction formalism:  $q_T$ -subtraction  
[Catani, Grazzini, '07]

Implementation based on public code MATRIX  
[Kallweit, Grazzini, Wiesemann, '17]

slide by Javier Mazzitelli



# NNLO revolution?

antenna

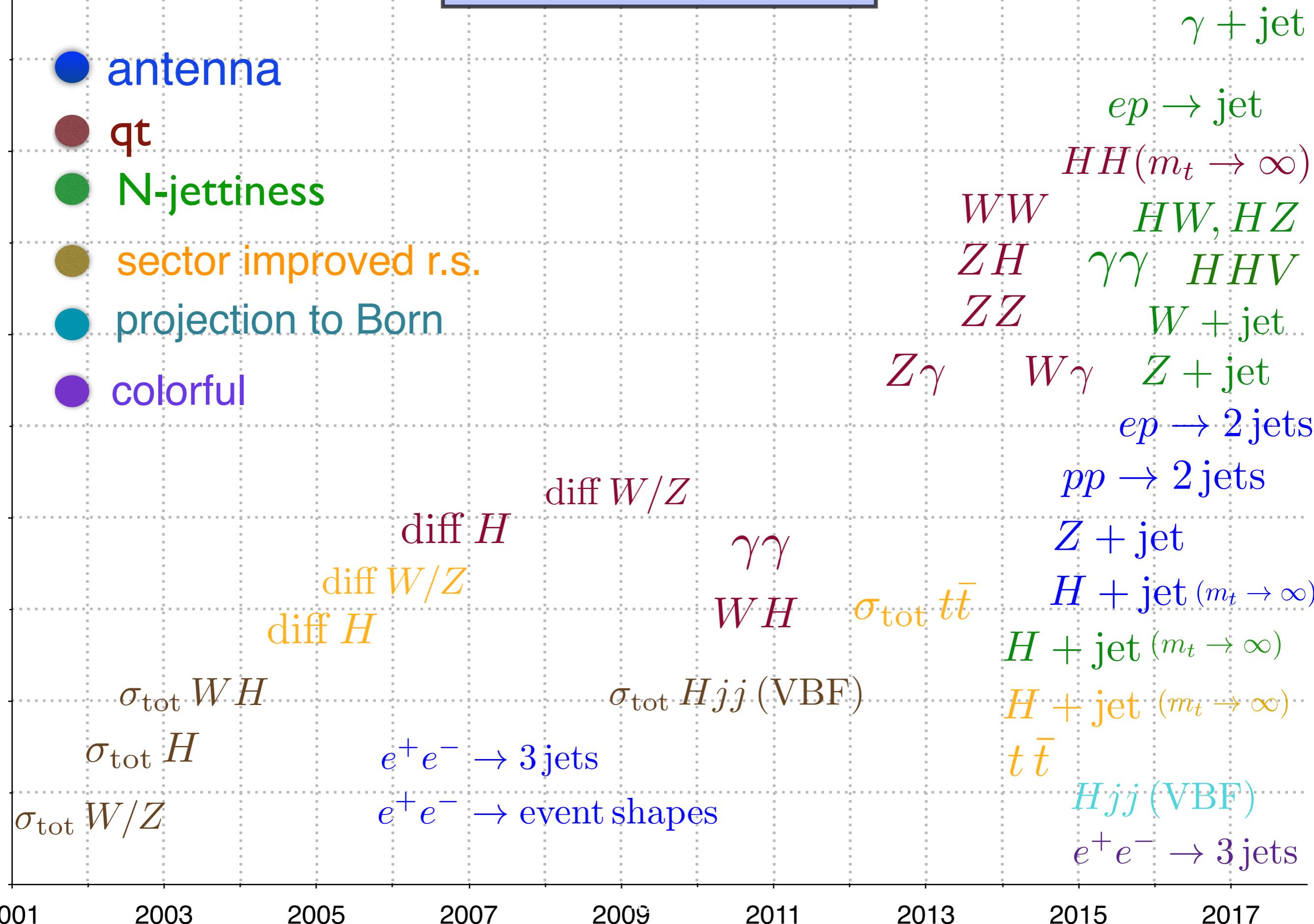
qt

N-jettiness

sector improved r.s.

projection to Born

colorful



2001 2003 2005 2007 2009 2011 2013 2015 2017