

# NLO mixed QCD-electroweak corrections to Higgs boson gluon fusion

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In collaboration with  
K. Melnikov, E. Panzer, L. Tancredi, V. A. Smirnov

# Topics

- 1 Motivations
- 2 Amplitude
- 3 LO & Virtual NLO
- 4 Real NLO
- 5 Conclusions & Outlook

# Particle physics after the Higgs boson

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## Evidences of New Physics

- **Direct observation**: main paradigm  
On-shell production and subsequent decay
- **Indirect search**: complementary approach  
Investigation of known processes at higher precision to unveil deviations
  - Accurate experimental results
  - Small theoretical uncertainties

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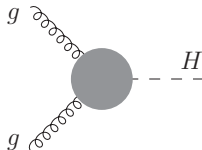
## Higgs boson: good candidate

- Yukawa coupling
- Only spin-0 elementary particle in the SM
- Still under investigation

# Higgs boson precision physics [\[1602.00695\]](#) [\[1610.07922\]](#) [\[1802.00833\]](#)

## Higgs gluon fusion

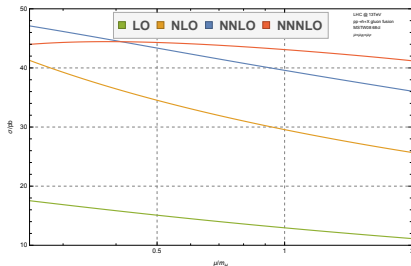
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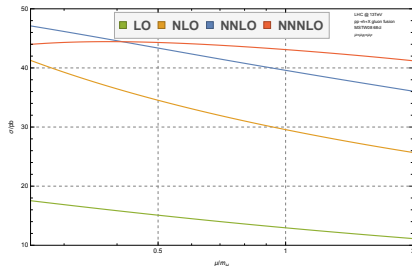




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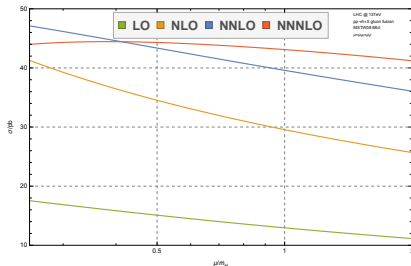
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Quark mass dependence    Electroweak contributions    PDF refinement

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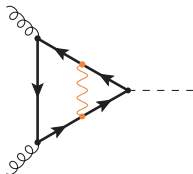
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# QCD-Electroweak contributions [\[ph0404071\]](#) [\[ph0407249\]](#) [\[ph0610033\]](#)

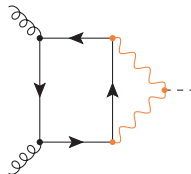
## Leading Order

Yukawa coupling  $\alpha_S \alpha Y_t$



- top dominant

Electroweak coupling  $\alpha_S \alpha^2 v$

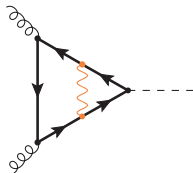


- light quarks dominant

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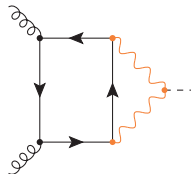
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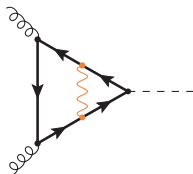


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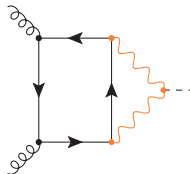
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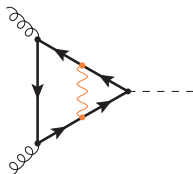
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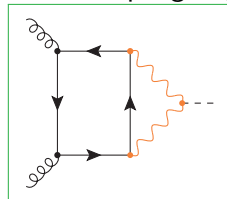
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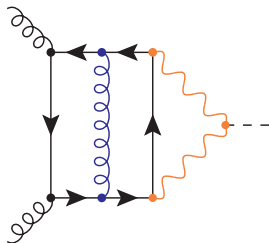
Exact NLO computation required

## Construction of the amplitude

## 1 Feynman diagrams

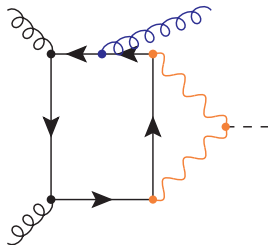
[Nog93]

Virtual NLO  $\alpha_S^2 \alpha^2 v$



47 diagrams

Real NLO  $\alpha_S^{3/2} \alpha^2 v$



21 diagrams

# Construction of the amplitude

① Feynman diagrams

[Nog93]

② Tensor structures

[1707.06453]

No axial terms:  $\gamma_5$ -dependence drops summing over isospin doublets

$$gg \rightarrow H$$

$$\mathcal{M}_{\lambda_1 \lambda_2}^{c_1 c_2} = \delta^{c_1 c_2} \epsilon_{\lambda_1}(\mathbf{p}_1) \cdot \epsilon_{\lambda_2}(\mathbf{p}_2) [\mathcal{F}_2 + \mathcal{F}_3]$$



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$$gg \rightarrow Hg$$

$$\mathcal{M}_{\lambda_1 \lambda_2 \lambda_3}^{c_1 c_2 c_3} = f^{c_1 c_2 c_3} \epsilon_{\lambda_1, \mu}(\mathbf{p}_1) \epsilon_{\lambda_2, \nu}(\mathbf{p}_2) \epsilon_{\lambda_3, \rho}^*(\mathbf{p}_3)$$

$$[g^{\mu\nu} p_2^\rho \mathcal{F}_{002} + g^{\mu\rho} p_1^\nu \mathcal{F}_{010} +$$

$$+ g^{\nu\rho} p_3^\mu \mathcal{F}_{300} + p_3^\mu p_1^\nu p_2^\rho \mathcal{F}_{312}]$$

# Construction of the amplitude

① Feynman diagrams

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② Tensor structures

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③ Form factors

Diagrams contain either only  $W^\pm$  or only  $Z$

$$\mathcal{F} \propto 4 A(\mathbf{x}, m_W) + \frac{2}{\cos^4 \theta_W} \left[ \frac{5}{4} - \frac{7}{3} \sin^2 \theta_W + \frac{22}{9} \sin^4 \theta_W \right] A(\mathbf{x}, m_Z)$$

- $W^\pm$  couples to  $\{u, d, c, s\}$
- $Z$  couples to  $\{u, d, s, c, b\}$

# Construction of the amplitude

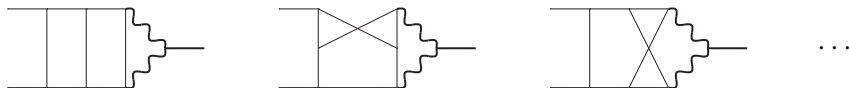
- 1 Feynman diagrams
- 2 Tensor structures
- 3 Form factors
- 4 Master Integrals

[Nog93]

[1707.06453]

[1201.4330] [1705.05610]

Virtual NLO: 95 3-loop MIs



Real NLO: 61 2-loop MIs



# Evaluation of 3-point Master Integrals

## ① Differential equations

[Kot91] [ph9306240] [th9711188] [th9912329]

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- Differentiate the MIs w.r.t. masses or kinematics

$$\left\{ \begin{array}{l} \frac{\partial}{\partial M^2} \text{ (orange bubble) } = \text{ (black bubble) } \\ \frac{\partial}{\partial M^2} \text{ (red bubble) } = \text{ (black bubble with left dot) } + \text{ (black bubble with right dot) } \end{array} \right.$$

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- Apply IBPs to the r.h.s.

$$\begin{aligned} \text{ (black bubble with left dot) } - \text{ (black bubble with bottom dot) } &= \frac{-1 + \varepsilon}{M^2 (4M^2 - p^2)} \text{ (orange bubble) } + \frac{1 - 2\varepsilon}{4M^2 - p^2} \text{ (red bubble) } \\ \text{ (black bubble with top dot) } &= \frac{1 - \varepsilon}{M^2} \text{ (orange bubble) } \end{aligned}$$

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### Homogeneous system of differential equations

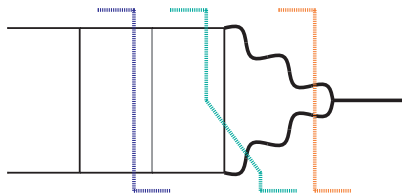
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- ① Differential equations [Kot91] [ph9306240] [th9711188] [th9912329]
- ② Canonical fuchsian form [1012.6032] [1304.1806] [1412.2296]

Highly non-trivial but very useful

$$\frac{d}{dy} \mathbf{F}(y, \varepsilon) = \varepsilon \sum_c \mathcal{B}_c \frac{1}{y - a_c} \mathbf{F}(y, \varepsilon)$$



$s$	$0$	$m^2$	$4m^2$	$[\infty]$
$y := \frac{\sqrt{1-4M^2/s-1}}{\sqrt{1-4M^2/s+1}}$	$+1$	$e^{\pm i\pi/3}$	$-1$	$[0]$

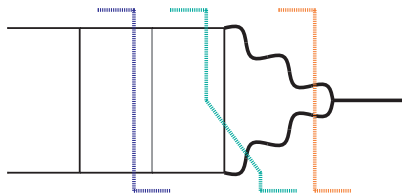


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$$\begin{aligned}
 F(y, \varepsilon) = & \quad F_0^{(0)} \\
 & + \varepsilon \left[ \int_y B(\xi_1) d\xi_1 F_0^{(0)} + F_0^{(1)} \right] \\
 & + \varepsilon^2 \left[ \int_y B(\xi_1) \int_{\xi_1} B(\xi_2) d\xi_2 d\xi_1 F_0^{(0)} + \int_y B(\xi_2) d\xi_2 F_0^{(1)} + F_0^{(2)} \right] \\
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Goncharov Polylogarithms (GPLs)

$$G(a_{c_n}, a_{c_{n-1}}, \dots, a_{c_1}; y) = \int_0^y \frac{1}{\xi - a_{c_n}} G(a_{c_{n-1}}, \dots, a_{c_1}; \xi) d\xi$$

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Large-mass expansion

$$\mathbf{L} \left[ \text{Diagram} \right] = \left\{ \begin{array}{l} \text{Diagram 1} \times \text{Diagram 2} + \\ + \text{Diagram 3} + s \frac{2(1+\varepsilon)}{2-\varepsilon} \text{Diagram 4} + \mathcal{O} \left( \frac{(-s)^2}{(m^2)^4} \right) \end{array} \right.$$

$\mathbf{F}_0^{(n)}$	0	1	2	3	4	5	6
Values	1	—	$\pi^2$	$\zeta(3)$	$\pi^4$	$\frac{\pi^2 \zeta(3)}{\zeta(5)}$	$\frac{\pi^6}{\zeta^2(3)}$

# Real emissions

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- Soft gluon approximation [ph0102227] [1209.0673]
- In  $gg \rightarrow H$  PDFs suppress extra gluons with large momentum
- Eikonal approximation ( $E_g \rightarrow 0$ )

$$\left| \text{Diagram 1} \right|^2 \Rightarrow \left| \text{Diagram 2} \right|^2 \Rightarrow 4\pi\alpha_S N_C \frac{2 p_1 \cdot p_2}{p_1 \cdot p_4 p_2 \cdot p_4} \left| \text{Diagram 3} \right|^2$$

Diagram 1: A gluon-gluon fusion loop (EW) with two external gluons and a dashed line.

Diagram 2: A gluon-gluon fusion loop (EW) with two external gluons and a dashed line, with a soft gluon emission from the top-left vertex.

Diagram 3: A gluon-gluon fusion loop (EW) with two external gluons and a dashed line.

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$\sigma_{\text{LO}}^{\text{QCD}} = 20.6 \text{ pb}$        $\sigma_{\text{LO}}^{\text{QCD-EW}} = 21.7 \text{ pb} \Rightarrow +5.3 \% \text{ at LO}$

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- **Square roots**: non-rationalizable at once, change of variables on-the-fly

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- **3-scale problem**: boundary conditions not straightforward
- **Square roots**: non-rationalizable at once, change of variables on-the-fly
- **Cumbersome results**: last two orders of the non-planar top sector missing

## Direct integration

[1403.3385]

## Feynman parameters

$$\mathcal{I}(a_1, \dots, a_7) \propto \left[ \prod_{k=1}^7 \int_0^{+\infty} x_k^{a_k-1} dx_k \right] \frac{\delta(1 - \bar{x})}{\mathcal{U}^{\sum a_i + 3D/2} \mathcal{F}^{\sum a_i - D}}$$

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Direct integration requires

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[0804.1660] [0910.0114]

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- The Master Integrals are finite in  $\epsilon$  [th960618] [0911.0252]
  - UV finiteness: negative SDD
  - IR finiteness: translate integrals in  $D = 6$

$$\mathcal{I}^{D+2}(a_1, \dots, a_7) = \frac{16}{s t u (D-4)(D-3)} \int \tilde{d}^D k_1 \tilde{d}^D k_2 \frac{G(k_1, k_2, p_1, p_2, p_3)}{\mathcal{D}_1^{a_1} \dots \mathcal{D}_7^{a_7}}$$

Gram determinant  $G$ : cures soft and collinear divergences

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[1403.3385]

## Feynman parameters

$$\mathcal{I}(a_1, \dots, a_7) \propto \left[ \prod_{k=1}^7 \int_0^{+\infty} x_k^{a_k-1} dx_k \right] \frac{\delta(1-\bar{x})}{\mathcal{U}^{\sum a_i + 3D/2} \mathcal{F}^{\sum a_i - D}}$$

Direct integration requires

- $\mathcal{U}$  &  $\mathcal{F}$  linearly reducible [0804.1660] [0910.0114]

There exists an order of integration over  $x_k$  for which the result is a l.c. of GPLs

- The Master Integrals are finite in  $\epsilon$  [th960618] [0911.0252]
  - UV finiteness: negative SDD
  - IR finiteness: translate integrals in  $D = 6$

$$\mathcal{I}^{D+2}(a_1, \dots, a_7) = \frac{16}{s t u (D-4)(D-3)} \int \tilde{d}^D k_1 \tilde{d}^D k_2 \frac{G(k_1, k_2, p_1, p_2, p_3)}{\mathcal{D}_1^{a_1} \dots \mathcal{D}_7^{a_7}}$$

Gram determinant  $G$ : cures soft and collinear divergences

Master Integrals in quasi-finite basis computed using [HyperInt](#).

# $gg \rightarrow Hg$ amplitude

- Rich alphabet: 49 letters, 4 square roots

$$R_0 = \sqrt{m_h^2(m_h^2 - 4m_V^2)} / (-m_h^2)$$

$$R_1 = \sqrt{1 - 4m_V^2/(t + u)}$$

$$R_2 = \sqrt{R_0^2 - 4m_V^2 su/t} / (-m_h^2)$$

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- Final form of the amplitude
- $\Omega_{+++} \ni \log, \text{Li}_2, \text{Li}_3$ : fast, stable expressions both in Euclidean and physical regions
- $\Omega_{++-} \ni \log, \text{Li}_2, \text{Li}_3, G_4$  (to be done:  $G_4 \rightarrow \text{Li}_4, \text{Li}_{2,2}$ )

# Conclusions & Outlook

QCD-EW corrections to Higgs production: important for precision physics

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Analytic results for NLO QCD light-quark corrections to  $gg \rightarrow H(g)$

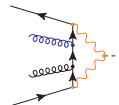
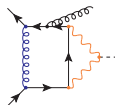
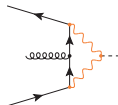
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## The road ahead

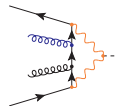
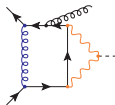
- $qg \rightarrow Hq$  QCD-EW with light quarks



Analytic results for NLO QCD light-quark corrections to  $gg \rightarrow H(g)$

## The road ahead

- 
- A Feynman diagram showing a photon (represented by a wavy line) decaying into an electron-positron pair. The photon line enters from the left and splits into two lines: an electron line (solid line with an arrow pointing right) and a positron line (solid line with an arrow pointing left). The electron and positron lines then interact via a virtual photon (represented by a wavy line) which splits into another electron-positron pair. The final electron and positron lines exit to the right.



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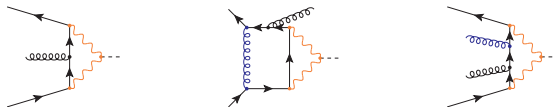
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QCD-EW corrections to Higgs production: important for precision physics

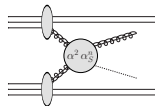
Analytic results for NLO QCD light-quark corrections to  $gg \rightarrow H(g)$

## The road ahead

- $qg \rightarrow Hq$  QCD-EW with light quarks



- Computation of  $\sigma_{PP \rightarrow H+j}$  QCD-EW with light quarks



- **Very long run:**  $\sigma_{PP \rightarrow H+j}$  QCD-EW top + light quarks

Thank you for your attention

